

1 BHT2  $J/\psi$   $R_{pA}$  Run15 AnaNote

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# 1 Data QA - Bad Run Rejection

The data taking encounters random and unexpected events from time to time. Some effects on performance may also accumulate over time. These could result in abnormal detector readout and therefore unreliable reconstruction. The data QA - bad run rejection defines a list of runs to be rejected due to significant difference of reconstruction variable distributions compared to the other runs. Only the variables that are related to this analysis are looked at.

## 1.1 Procedure

The rejection happens in an iterative manner. Each iteration is called a “round”. The remaining runs in the previous round will be the complete set that the next round will work on. In each round, profile histograms of 39 variable distributions vs run index are checked independently. For each variable, the runs that satisfy “the criteria” will be marked as “to be rejected”, and will be rejected at the end of each round collectively, after all 39 variables are checked. I.e., a run could be marked as “to be rejected” multiple times in a round. The iteration ends when not a single run is marked as “to be rejected” in the latest round. All the runs that have been rejected, as well as runs without any entries, are listed as “bad runs”.

The following is a complete list of 39 checked variables:

hRefMult, hnPrimary, hnBEMCMatch, hTPCVz, hTPCVx, hTPCVy, hnHitsFit, hnHitsDedx, hDca, hPt, hEta, hPhi, hDedx, hNSigmaE, hNSigmaPi, hNSigmaK, hNSigmaP, hZDCX, hBemcZDist, hBemcPhiDist, hBemcbTowE, hBemcE0, hBemcAdc0, hBemcEvP, hBBCX, hBemcE, hTrgdBemcAdc0, hTrgdBemcE0, hTrgdBemcE, hTrgdBemcbTowE, hTrgdBemcEvP, hTrgdBemcZDist, hTrgdBemcPhiDist, hTrgdNSigmaE, hTrgdPt, hTrgdEta, hTrgdPhi, hnBemcE, hnTrgdE

## 1.2 Criteria

The criteria is used when checking each profiles histograms (PH) of variable distribution in order to mark the “to be rejected” runs.

**Define: Center** Fit the PH of *val* vs *RunIdx* to a straight line with least square method, but with the error bar ignored. This straight line is considered as the **Center**. In each collision system for certain variables, the profile histogram shows obvious discontinuity and a linear fit will yield a slope that does not correspond to development of any trend. In such cases, the slope parameter is fixed at 0. The following is a list of variables with the slope fit parameter fixed to 0.

**p+p** hTPCVx, hTPCVy, hEta, hPhi

**p+Au** hnBEMCMatch, hTPCVz, hTPCVx, hTPCVy, hBemcEvP, hTrgdBemcEvP, hTrgdEta, hTrgdPhi

**Define:  $\mu, \sigma$**  Move the axis in the Y axis direction by  $b$ , which is the y intersection of **Center**, and then rotate the axis by  $\theta$  where  $\theta$  is the slope angle of **Center**. The new Y coordinates are  $y' = (y - b)\cos\theta - x\sin\theta$ .  $\mu$  is the mean of  $y'$  and  $\sigma$  is the standard deviation of  $y'$ .  $\mu$  is close to 0 but slightly deviate from 0 due to float accuracy and fit details. Such a deviation is negligible.

**Define:  $5\sigma$  Band** Area between the straight lines  $y' = \mu \pm 5 \times \sigma$  is defined to be the  **$5\sigma$  Band**. The band is carried over back to the original coordinate system before rotation and transition.

**Rejection** Let the **segment**:  $x = \text{Center}$ ,  $\text{Center} - \text{Error} \leq y \leq \text{Center} + \text{Error}$  represent the corresponding run, where “Center” and “Error” are the bin center and bin error respectively. If the **segment** has no overlap with the  **$5\sigma$  Band**, then it is marked as “to be rejected”.

91 **1.3 Result**

92 The runs rejected in different rounds are collectively presented in Fig.1 for p+p collisions and in Fig.2  
 93 for p+Au collisions.

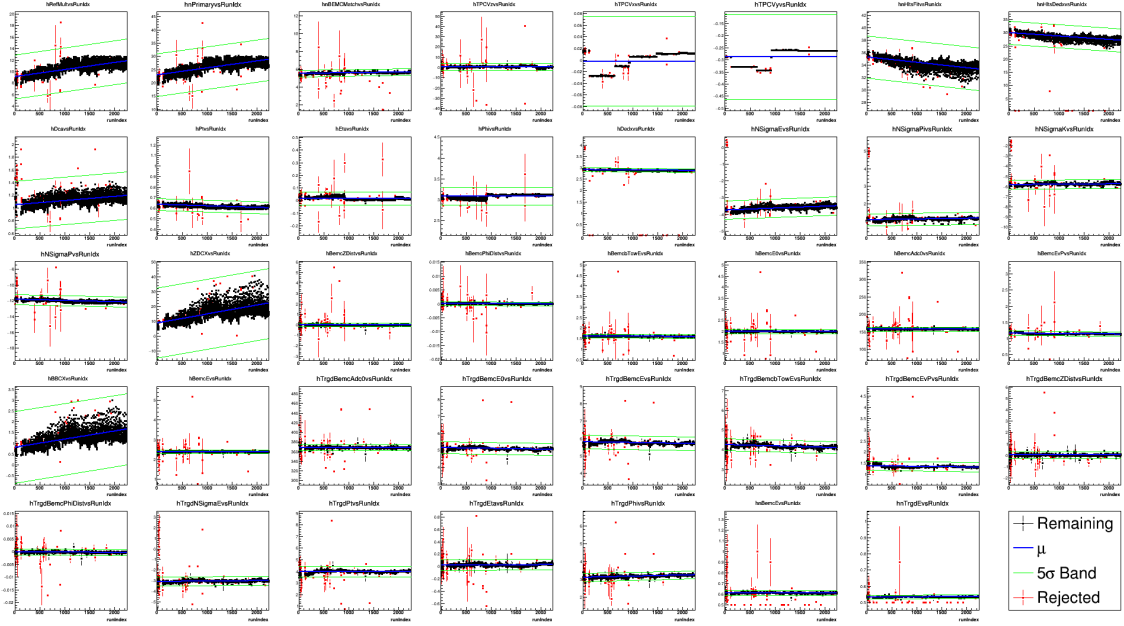


Figure 1: Bad Run Rejection for p+p

- 94 The following is a list of rejected runs in p+p collisions (including “empty” runs without any entry):  
 95 16044110, 16044111, 16044112, 16044123, 16044124, 16044125, 16044126, 16044127, 16044128, 16044129,  
 96 16044132, 16044133, 16044138, 16045001, 16045047, 16045048, 16045049, 16045070, 16045082, 16045083,  
 97 16045084, 16045085, 16045086, 16045087, 16045088, 16045089, 16045090, 16045093, 16045095, 16045096,  
 98 16045097, 16045098, 16045099, 16045100, 16045102, 16045103, 16045104, 16045105, 16045106, 16045108,  
 99 16045109, 16045110, 16045111, 16045112, 16045113, 16045114, 16045115, 16045116, 16045117, 16045118,  
 100 16045119, 16045120, 16046003, 16046005, 16046006, 16046007, 16046008, 16046009, 16046010, 16046011,  
 101 16046012, 16046013, 16046014, 16046015, 16046016, 16046017, 16046018, 16046019, 16046020, 16046021,  
 102 16046032, 16046033, 16046034, 16046035, 16046036, 16046037, 16046038, 16046039, 16046040, 16046041,  
 103 16046042, 16046043, 16046044, 16046045, 16046046, 16046048, 16046049, 16046050, 16046057, 16046058,  
 104 16046059, 16046061, 16046062, 16046064, 16046065, 16046066, 16046067, 16046073, 16046076, 16046077,  
 105 16046078, 16047004, 16047005, 16047008, 16047101, 16047102, 16047103, 16047104, 16047106, 16050048,  
 106 16050049, 16052046, 16052048, 16052051, 16052087, 16052088, 16055124, 16055127, 16058070, 16058073,  
 107 16060018, 16060036, 16060043, 16060064, 16061035, 16061076, 16062008, 16062009, 16062011, 16062014,  
 108 16062048, 16063096, 16063097, 16063099, 16065011, 16066028, 16067045, 16067046, 16067047, 16069045,  
 109 16069050, 16069052, 16069060, 16071001, 16071002, 16071003, 16071006, 16071007, 16071076, 16072046,  
 110 16072047, 16073004, 16073007, 16073015, 16079045, 16080012, 16080043, 16082014, 16083003, 16084003,  
 111 16085005, 16087018, 16088014, 16089021, 16091039, 16091040, 16091042, 16091050, 16095027, 16096030,  
 112 16097028, 16100023, 16100024, 16100025, 16101006, 16101032, 16104002, 16104022, 16107004, 16107042,  
 113 16108032, 16110006, 16115029, 16115056

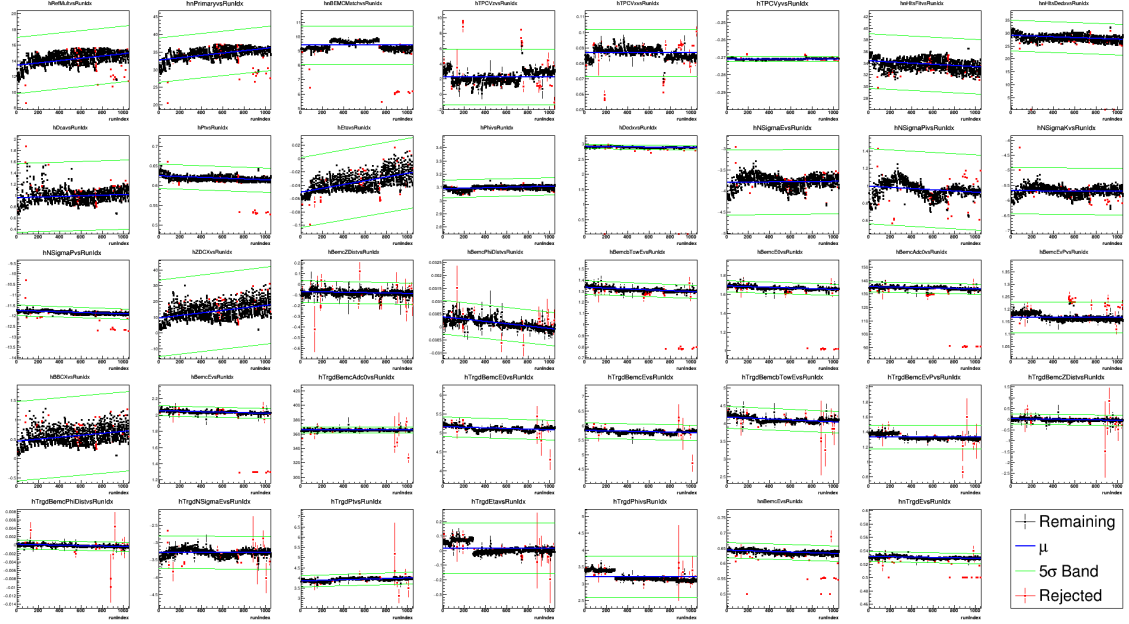


Figure 2: Bad Run Rejection for p+Au

114 The following is a list of rejected runs in p+Au collisions (including “empty” runs without any entry):  
 115 16125038, 16125046, 16125052, 16127005, 16127048, 16127049, 16128006, 16128056, 16129019, 16130012,  
 116 16130015, 16130016, 16130032, 16131030, 16131032, 16132021, 16132022, 16134012, 16134042, 16139021,  
 117 16142046, 16142061, 16142065, 16142069, 16142073, 16142077, 16143005, 16143009, 16143011, 16143013,  
 118 16143015, 16143031, 16143036, 16143039, 16143052, 16144002, 16144013, 16144037, 16144069, 16148016,  
 119 16149001, 16149002, 16149003, 16149004, 16149005, 16149008, 16149009, 16149010, 16149011, 16149013,  
 120 16149014, 16150001, 16150003, 16150042, 16154010, 16154021, 16155017, 16155031, 16155039, 16156010,  
 121 16156028, 16157034, 16157047, 16157048, 16157071, 16158021, 16158039, 16159009, 16159019

## 122 2 Embedding QA

123 Efficiency is studied with  $J/\psi$  embedding in real data and an event generator **EvtGen**. Embedding  
 124 are mainly used in order to study the behavior of single electron’s in terms of efficiency. Together with  
 125 **EvtGen**, we calculate the  $J/\psi$  reconstruction efficiency. Such combination of these tools is due to the  
 126 limitation of decay models of  $J/\psi$  in embedding and lacking of description of detector response in **Evt-**  
 127 **Gen**.

128 The purpose of embedding QA is to confirm that the embedding has good enough representation  
 129 of the data in most aspects. Additional treatment and argument is needed where embedding can’t  
 130 describe the real data well. All related single track variable distribution is compared between the data  
 131 and embedding. The distributions of kinematics of  $J/\psi$  candidates are also compared. The difference  
 132 between data and embedding is also covered by systematic uncertainty estimation. The exhausted list  
 133 of plots can be found in the appendix 7.1.

134 The conclusion is that the embedding describes the data well enough in most aspects. The momen-  
 135 tum resolution is underestimated, therefore needs additional smearing. The consistency between data  
 136 and embedding of  $E/p$  and  $dca$  distribution is not as satisfactory as others, therefore cuts on those are  
 137 loosened in order to reduce the systematic uncertainties.

## 139 3 Event and Track Selection

140 The event and track selection cuts used in p+p and p+Au are identical in order to reduce the  
 141 systematic uncertainty. The event trigger is the  $BHT2 \times BBC$  trigger.

142 Only events not rejected by the event level selection will be studied. In the di-electron pairs, both  $e^\pm$   
 143 are required to pass all tracking quality cuts and electron identification cuts. At least 1 of the  $e^\pm$  needs

144 to pass the electron trigger cuts. After  $J/\psi$  reconstruction, the only the RC  $J/\psi$  within the interested  
 145 kinematics range are studied. The  $J/\psi$  mass window is not listed here and will be discussed in later  
 146 sections. The selection cuts are listed below in the tables:

147

Event Selection	
$ Vz  \leq 80$ [cm]	Ranking < 0

Tracking Quality					
nHitsFit $\geq$ 20	nHitsDedx $\geq$ 10	0.52 $\leq$ nHitsRatio $\leq$ 1.02	DCA<1.5 [cm]	$p_T \geq 1$	$ \eta  < 1$

Electron Identification		
$0.5 < \frac{E}{p} < 2.5$ [c]	$-1.5 < n\sigma_e < 2.5$	$e > 0.1$ GeV/c <sup>2</sup>

Electron Trigger Cut		
Dsmadc>18	Adc0 $\geq$ 300	$p_T > 4.3$ (3.5) [GeV/c]

148 Note: The electron trigger  $p_T$  cut used to extract the invariant cross section (invariant yield) in p+p  
 149 (p+Au) collisions (4.3 GeV/c) is different from the cut used when calculating nuclear modification factor  
 150  $R_{e,xtpA}$  (3.5 GeV/c).

151 Near the start of the electron trigger threshold, the trigger efficiency from embedding is at higher  
 152 risk of being unreliable. This difference is taken into account in the systematic uncertainty by varying  
 153 the trigger cut regardless of the trigger  $p_T$ . The systematic uncertainty can be reduced by moving the  
 154 trigger  $p_T$  cut towards the trigger efficiency plateau (see plots for the EID efficiencies, TRG type)

155 In terms of invariant cross section (invariant yield) measurement, a higher trigger  $p_T$  cut is used in  
 156 order to reduce the systematic uncertainty.

157 When it comes to  $R_{e,xtpA}$ , since the data of the 2 collision systems were taken from the same year  
 158 and the related detector setup were identical, such a difference between embedding and data should be  
 159 mostly cancelled out by taking the ratio. One can worry less about the systematic uncertainty when  
 160 reaching away from the plateau. Therefore, trigger electron  $p_T$  cut is lowered to 3.5 GeV/c in order to  
 161 gain more  $J/\psi$  counts raw yield in the first  $p_T$  bin.

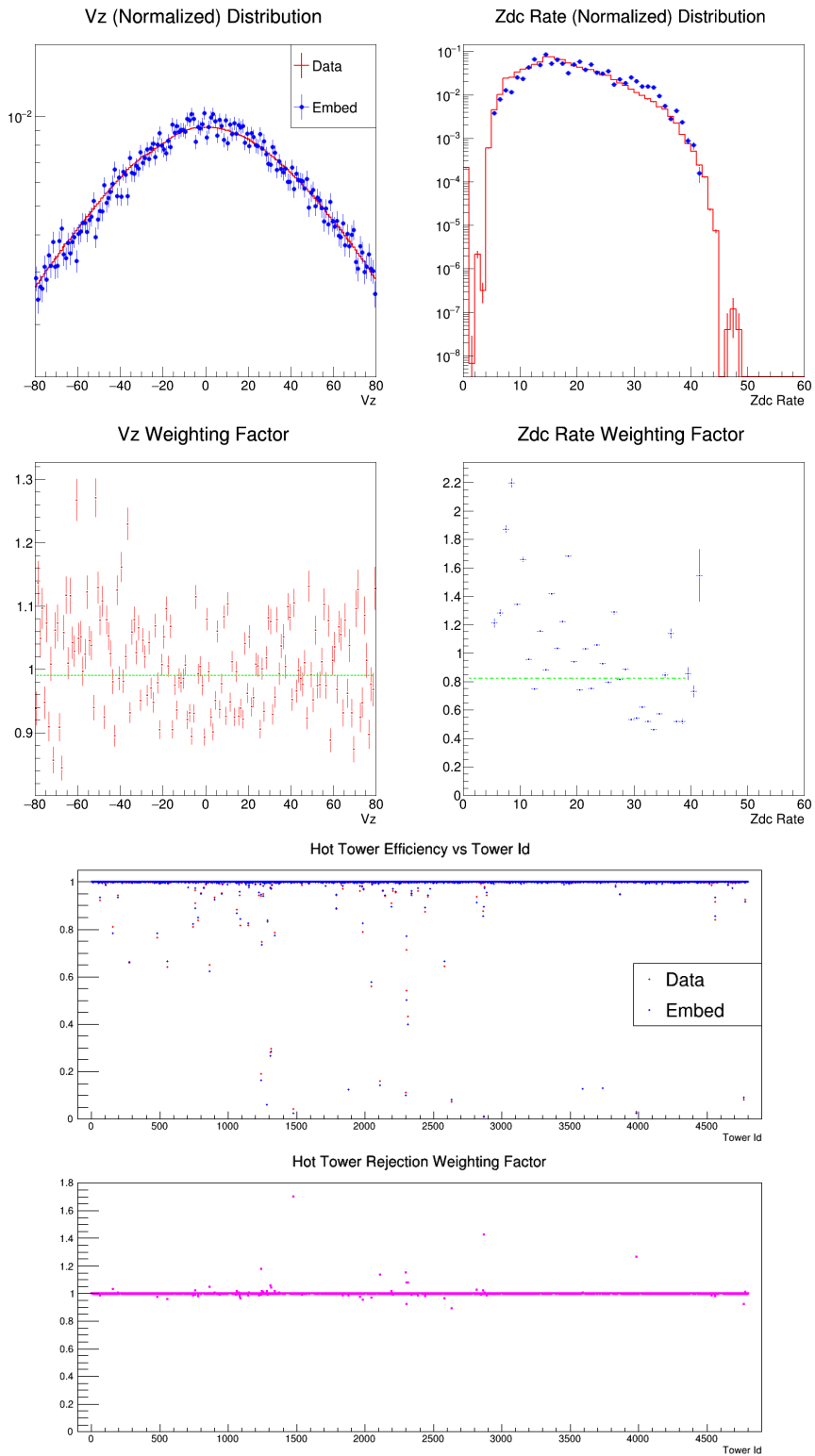
$J/\psi$ Kinematics Range	
$4 < p_T^{J/\psi} < 12$ [GeV/c]	$ y^{J/\psi}  < 1$

## 162 4 TPC Vz, Zdc Rate and Hot Tower Rejection Weighters

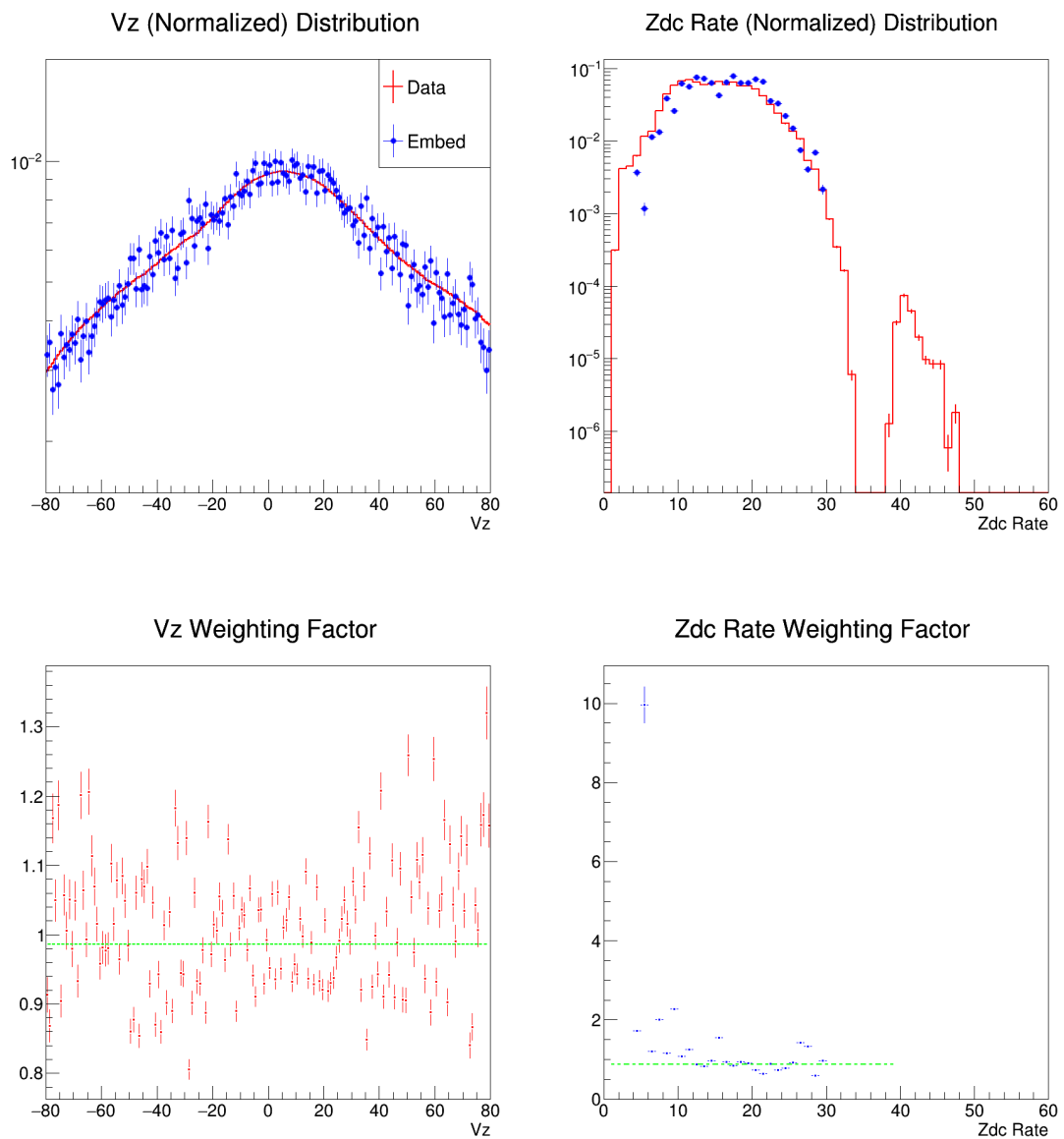
163 On the event level, the TPC Vz and luminosity (Zdc Rate) distribution have small but noticeable  
 164 difference between data and embedding. A weighting factor as a function of TPC Vz (Zdc rate) is needed  
 165 in order to reduce the effect from possible efficiency dependence on TPC Vz (Zdc rate). The weighting  
 166 factor is calculated by taking the ratio of the normalized TPC Vz (Zdc rate) distribution, of the data  
 167 against embedding. Due to the limit of statistics, TPC Vz and Zdc rate dependencies are assumed to  
 168 be uncorrelated.

169 The real data used to do embedding is only a subset of the entire dataset. As a result, the Zdc Rate  
 170 in some bins have 0 entries in embedding while the data have entries. This makes it impossible to do  
 171 weighting for these bins. Therefore those Zdc rate bins in data are discarded and defined as ‘‘Bad Bins’’.  
 172 Hot Tower Rejection is applied in order to avoid fired BEMC towers which leads to fake candidates. The  
 173 Hot Tower is defined run by run, i.e., there exists a hot tower list for each run. The probability fraction  
 174 that a tower is working properly can be calculated by taking the ratio of number of events that a tower is  
 175 normal against the total number of events. There is noticeable difference in the such a fraction between  
 176 real data and embedding. To compensate for such difference, a similar weighting factor is calculated for  
 177 Hot Tower Rejection by taking the ratio of normal fraction in data against that in embedding for each  
 178 individual tower.

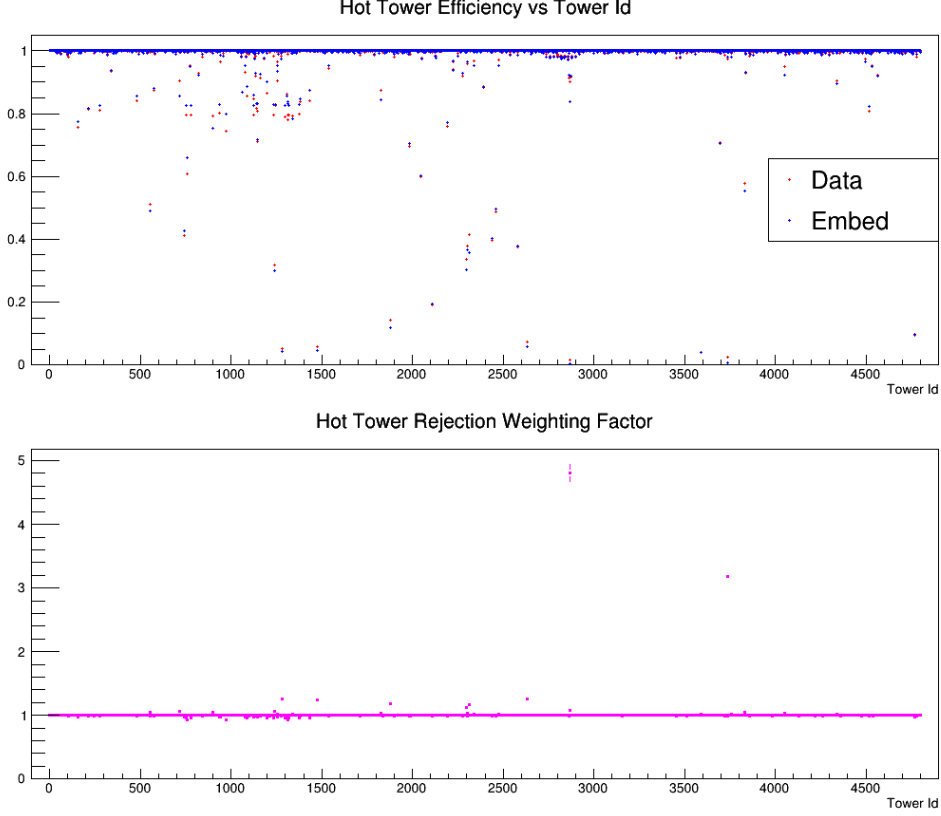
179 **p+p** Around 0.09% of events is discarded due to absence of Zdc rate in embedding:



180 **p+Au** Around 1.1% of events is discarded due to absence of Zdc rate in embedding:







181 These weighting factors are applied in embedding on event level.

## 182 5 The Analysis

### 183 5.1 Overview

184 There are 3 physics results in this analysis: the differential cross section in p+p collisions, the invari-  
 185 ant yield in p+Au collisions, and the nuclear modification factor  $R_{e\text{t}pA}$ .

186 The cross section in p+p is proportional to the invariant yield with a difference of a scale factor of  
 187 the non-single diffractive (NSD) cross section in p+p.

188 The  $R_{e\text{t}pA}$  is the yield ratio of p+Au against p+p, scaled by the average number of binary nucleon-  
 189 nucleon collisions  $\langle N_{coll} \rangle$ .

190  
 191 The  $p_T$  differentiated yield per unit rapidity is calculated by the following formula:

$$192 \frac{d^2 N}{dp_T dy} = \frac{1}{\Delta p_T \Delta y} \cdot \frac{1}{N_{MB}^{eqv} \epsilon_{MB}^{gvtx}} \cdot \frac{\epsilon_{MB}^{BBC} \epsilon_{MB}^{gvtx}}{\epsilon_{J/\psi}^{BBC} \epsilon_{J/\psi}^{gvtx}} \cdot \frac{N_{J/\psi}^{raw}}{\epsilon_{J/\psi}^{RC}}$$

193 where:

194  $\Delta y = 2$  corresponds to the rapidity acceptance  $|y| < 1$

195  $N_{MB}^{eqv}$  is the equivalent number of MB events, which is calculated based on BBCMB trigger with  
 196 in-bunch pileup correction.

197  $\epsilon_X^{gvtx}$  is the good vertex efficiency of X (X = MB, J/ψ). This is studied with PYTHIA(p+p)/HIJING(p+Au)  
 198 + GEANT embedded in zero-bias data.

199  $\frac{\epsilon_{MB}^{BBC} \epsilon_{MB}^{gvtx}}{\epsilon_{J/\psi}^{BBC} \epsilon_{J/\psi}^{gvtx}}$  is the trigger bias factor, in which  $\epsilon_X^{BBC}$  is the beam-beam counter efficiency of X (X =  
 200 MB, J/ψ). This is studied with PYTHIA(p+p)/HIJING(p+Au) + GEANT embedded in zero-bias data.

201  $N_{J/\psi}^{raw}$  is the raw yield of J/ψ

202  $\epsilon_{J/\psi}^{RC}$  is the J/ψ reconstruction efficiency

204

205 The  $\epsilon_{J/\psi}^{RC}$  consists of many aspects and they are studied in different ways.  
 206 The  $n\sigma_e$  is entirely data driven due to the its discrepancy between data and embedding.  
 207 The single electron (track level) efficiencies as well as the momentum resolution (in principle also the  
 208 resolution of pseudo-rapidity  $\eta$  and azimuthal angle  $\phi$ , but they appears to be negligible) extracted from  
 209 embedding are translated to EvtGen in order to simulate the  $J/\psi$  reconstruction with a more realistic  
 210 decay model. The resulting reconstructed  $J/\psi$  mass distribution from EvtGen serves as the fit template  
 211 of the signal part for raw yield extraction in real data. At the same time, by comparing the reconstructed  
 212 (**RC**)  $J/\psi$  mass distribution to the Monte Carlo (**MC**) one, one can get the RC efficiency.  
 213 In terms of the raw yield extraction, the unlike-sign minus like-sign (**US-LS**) mass distributions is  
 214 fit to a fit function which consists of the  $J/\psi$  signal and residual background:  
 215 
$$f(M_{e^+e^-}) = N_{J/\psi} \times \text{TEMPLATE}(M_{e^+e^-}) + N_{ResBG} \times e^{-bM_{e^+e^-}}$$
  
 216 where  $N_{J/\psi}$ ,  $N_{ResBG}$  are the normalization factors of the signal and residual background respectively,  
 217 and the formula for residual background is empirical and arbitrary. The raw yield is then extracted by  
 218 integrating the  $N_{J/\psi} \times \text{TEMPLATE}(M_{e^+e^-})$ . The raw yield is then corrected by the  $J/\psi$  RC efficiency.  
 219 The embedding samples for STAR experiments usually overestimate the performance in terms of  
 220 measuring momentum (underestimate the resolution). In order to overcome this issue, a technique of  
 221 “additional smearing” is performed. The general idea is to assign a new RC  $p_T$  to each RC track in  
 222 embedding and in EvtGen, while  $\eta$  and  $\phi$  stay untouched, where the new RC  $p_T$  is determined by the old  
 223 RC  $p_T$  and MC  $p_T$  in a pattern. The “pattern” can be varied, and among the variations it is determined  
 224 by minimizing the difference between the RC mass distribution from EvtGen and from the fit result of  
 225 real data.  
 226

## 227 5.2 Number of equivalent MB events based on BBCMB

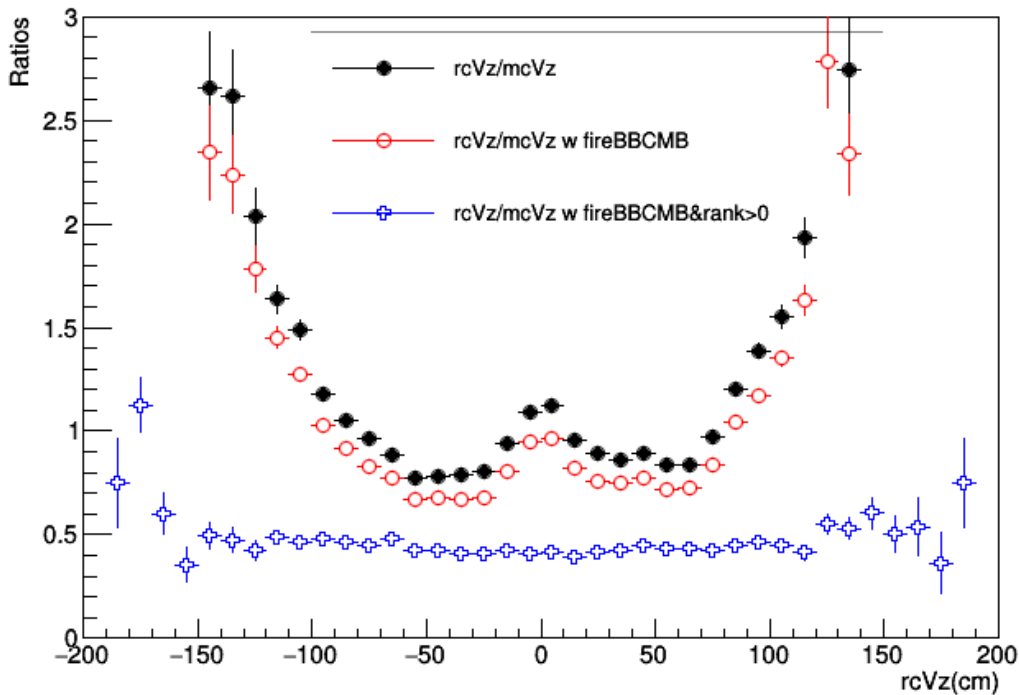


Figure 3: Ratio  $\frac{rcV_z}{mcV_z}$  in the simulation

228 The figure 3 shows the Ratios of reconstructed  $V_z$  over the MC  $V_z$  in the simulation, as the blue  
 229 points shown, after requiring  $Ranking > 0$  for the BBC triggered events, the ratio  $\frac{rcV_z}{mcV_z}$  is flat, which  
 230 suggests that the reconstructed  $V_z$  distribution should have the same shape as the true  $V_z$  ( $mcV_z$  is the  
 231 input true  $V_z$  in the simulation). Based on this we could get the fraction of events falling in our analysis

232 cut window  $|Vz| < 80$  cm.

233

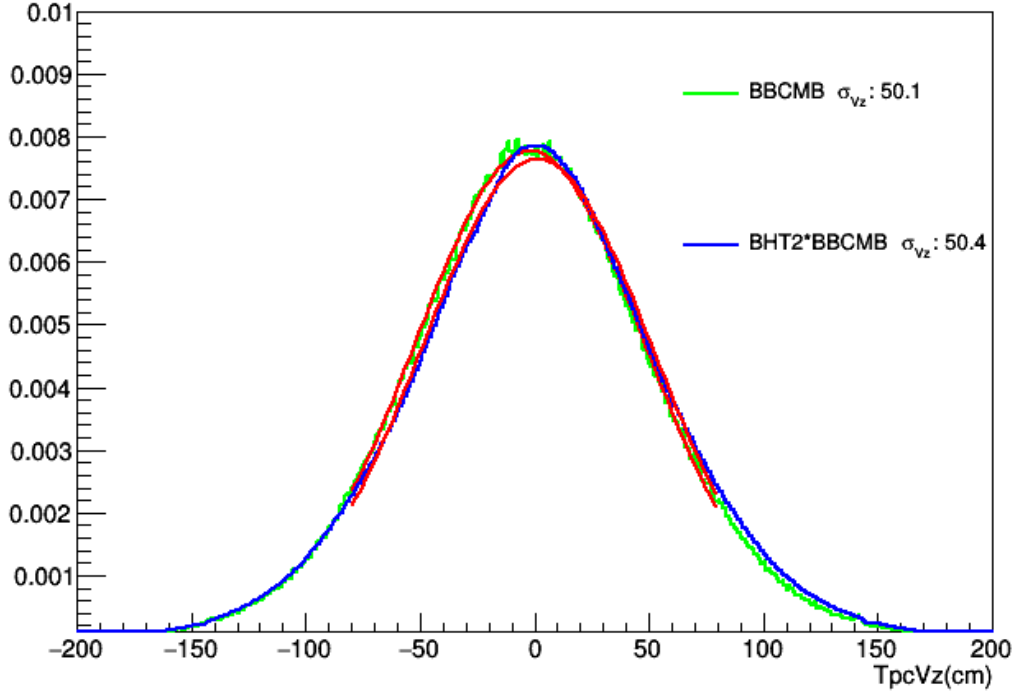


Figure 4: The Tpc Vz with  $Ranking > 0$  in the Run15pp real data

234 figure 4 show the reconstructed Vz by TPC of BBCMB and BHT2\*BBCMB triggered events. Based  
 235 on the real shape of these histograms, we can get the fraction of  $\frac{|Vz| < 80}{|Vz| < 200}$  is 0.8698 for all recorded  
 236 BBCMB events and 0.8584 for all recorded BHT2\*BBCMB events.

237

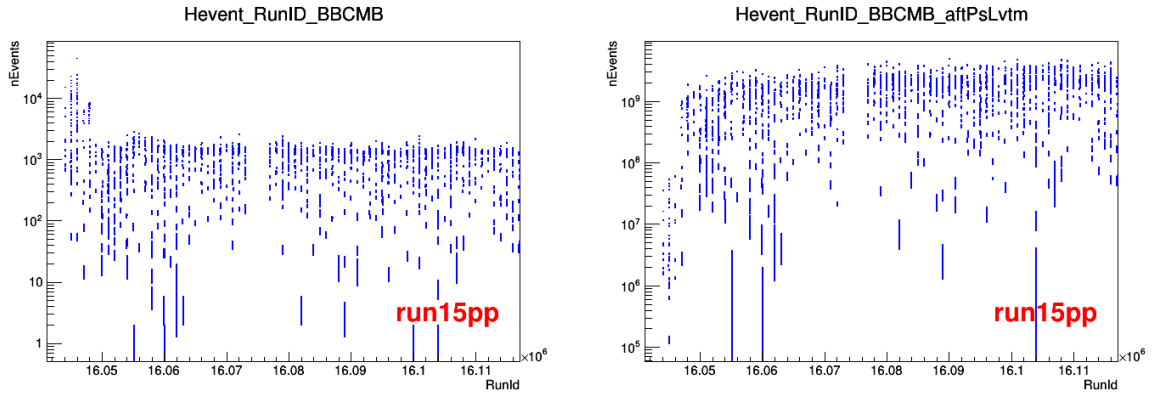


Figure 5: The left panel shows the number of recorded BBCMB events with both BBCMB trigger and BHT2\*BBCMB trigger on-line vs Run number, the right panel shows the number of equivalent BBCMB events vs Run number

238 And after sum of the number of equivalent MB BBC MB events over all runs and multiply the fraction  
 239 of  $\frac{|Vz| < 80}{|Vz| < 200}$  and multiply the fraction of analyzed BHT2\*BBCMB events, the total number of equivalent  
 240 MB events corresponding to our analyzed BHT2\*BBCMB data can be obtained as:

241

242

$$N_{MB}^{eqv.}(\text{for all analyzed BHT2 events}) = N_{MB}^{eqv.}(\text{BBCMB and BHT2 on-line}) * \frac{N_{BHT2}(\text{analyzed})}{N_{BHT2}(\text{BBCMB and BHT2 on-line})} =$$

243  $2.7621 \times 10^{12}$

244 Same thing can be done to p+Au collisions and the plots are shown as following:

245

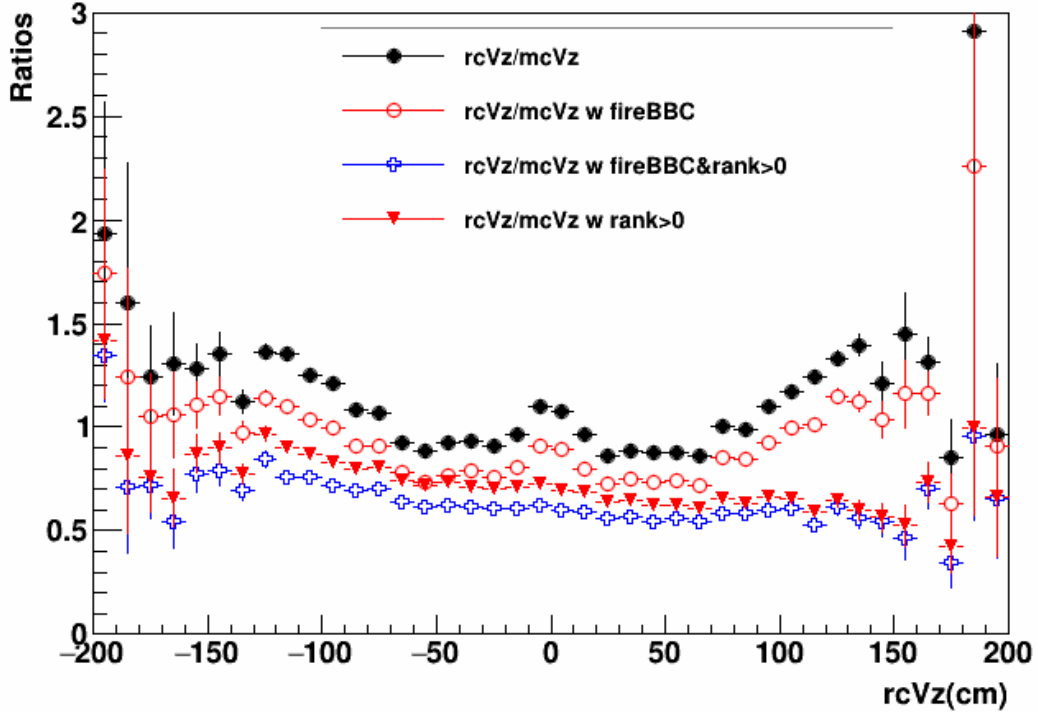


Figure 6: Ratio  $\frac{rcV_z}{mcV_z}$  in the simulation

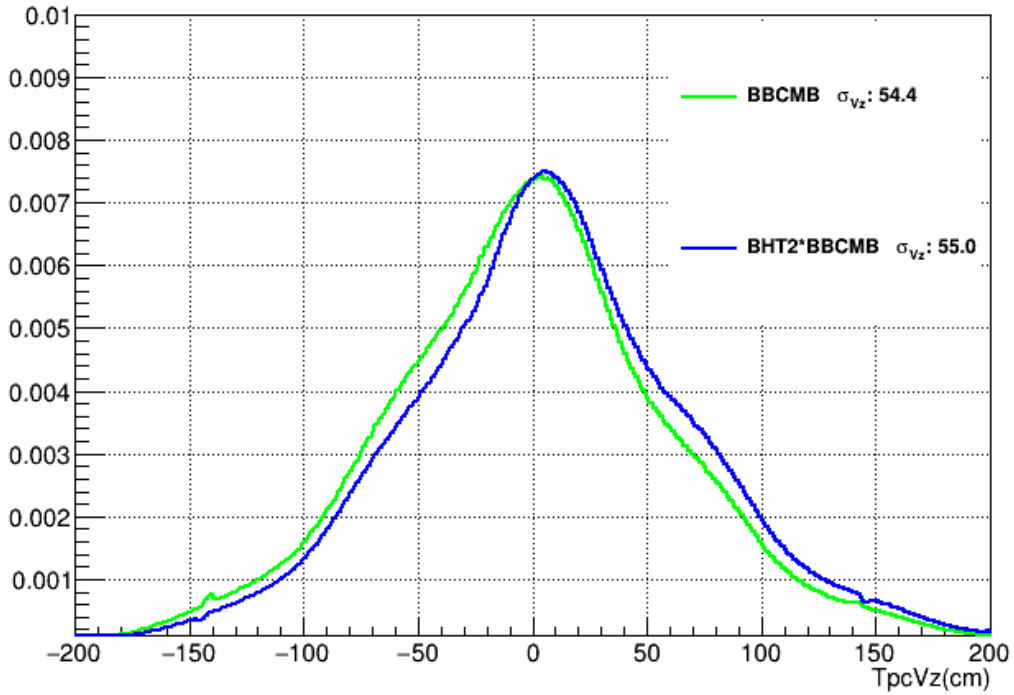


Figure 7:  $V_z$  distribution of BBCMB and BHT2 triggered events of Run15 pAu

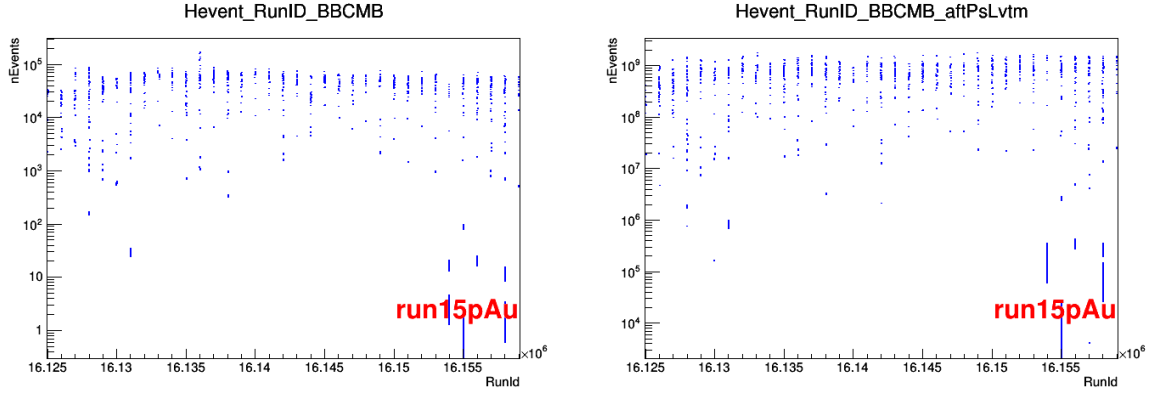


Figure 8: The left panel shows the number of recorded BBCMB events with both BBCMB trigger and BHT2\*BBCMB trigger on-line vs Run number, the right panel shows the number of equivalent BBCMB events corresponding to the left panel vs Run number

246 The  $N_{MB}^{eqv.} = 5.5211 \times 10^{11}$

### 247 5.3 In-bunch pileup correction

248 Due to the very high luminosity with 2015 p+p 200 GeV collisions, there might be more than one  
 249 collisions happened during a bunch crossing, so we need to consider the contribution from the in-bunch  
 250 pileup. Assuming that  $\lambda$  is the probability that one collision happens during a given bunch-crossing.  
 251 Then the probability of that there are k collisions happen in a bunch-crossing would be:

$$P_k[\text{k collisions in a bunch-crossing}] = \frac{\lambda^k e^{-\lambda}}{k!}$$

253 and we would have:  $P_0 = e^{-\lambda}$ ,  $P_1 = \lambda e^{-\lambda}$ ,  $P_2 = \frac{\lambda^2}{2} e^{-\lambda}$  and  $P_3 = \frac{\lambda^3}{6} e^{-\lambda}$

254 The contribution of  $k \geq 3$  is much smaller compared to  $k=1$  and  $k=2$ , when the BBC is fired from  
 255 collisions, we can only consider  $k=1$  and  $k=2$  cases. Let  $\epsilon$  as the BBC single side fire efficiency ( $\epsilon = 0.9$ ).

- 256 • Then, for  $k=1$ , the probability of that two sides of BBC are fired:

$$P_{BBC}[k = 1] = P_1 * \epsilon^2$$

- 257 • Then, for  $k=2$ , two sides of BBC are fired can be the following cases:

- 258 1. two collisions both fire two sides of BBC
- 259 2. one collision fire two sides of BBC and another one fire only one side of BBC
- 260 3. one collision fire two sides of BBC and another one fired nothing
- 261 4. one collision fire only one side of BBC and the other collision fire the other side of BBC

262 Then, the probability of that two sides of BBC are fired:

$$263 P_{BBC}[k = 2] = P_2 * [\epsilon^4 + 4 * \epsilon^3(1 - \epsilon) + 2 * \epsilon^2(1 - \epsilon)^2 + 2 * \epsilon^2(1 - \epsilon)^2] = P_2 * [\epsilon^2(2 - \epsilon)^2]$$

264 So, among the BBC triggered events, fraction of  $k=2$  events can be obtained by:

$$265 \text{Fraction}(k = 2) = \frac{P_{BBC}[k = 2]}{P_{BBC}[k = 1] + P_{BBC}[k = 2]} = \frac{P_2 * [\epsilon^2(2 - \epsilon)^2]}{P_2 * [\epsilon^2(2 - \epsilon)^2] + P_1 * \epsilon^2} = \frac{\lambda(2 - \epsilon)^2}{2 + \lambda(2 - \epsilon)^2}$$

266 If we assume the BBC rates are all due to the real collisions, then we would have:

$$\lambda \cong \frac{BBCRate/\epsilon^2}{9.383MHz * (102/120)}$$

267 A roughly estimation of the fraction of  $k=2$ : for the BBC rate at 0.5 MHz, 1.3 MHz, 2.5 MHz,  $\lambda =$   
 268 0.0774, 0.201, 0.387, the  $\text{Fraction}(k = 2) = 5.2\%$ ,  $12.4\%$ ,  $21.5\%$ .

269 Note that: The above estimation assumed the BBC rate from the real data are all coming from the  
 270 real collisions.

### 271 5.3.1 How to quantify the contribution of in-bunch pile-up

272 The BBC rate in per bunch-crossing due to the real collisions should be the expectation of  $k=1$  and  
 273  $k=2$  collisions, then we have the following relation:

$$\frac{BBCRate}{9.838MHz * \frac{102}{120}} = 1 * P_1 * \epsilon^2 + 2 * P_2 * \epsilon^2(2 - \epsilon)^2 + \dots \cong \lambda e^{-\lambda} \epsilon^2 + \lambda^2 e^{-\lambda} \epsilon^2(2 - \epsilon)^2$$

274 then, when  $\lambda$  is small and  $\epsilon$  close to 1 we would have:

275

$$\frac{BBCRate/\epsilon^2}{9.838MHz * \frac{102}{120}} = \lambda e^{-\lambda} + \lambda^2 e^{-\lambda}(2 - \epsilon)^2 \cong \lambda$$

276 Considering the strong correlation between BBC trigger and the VPD trigger, we can make use of  
 277 the VPD trigger rate to calculate the corresponding BBC rate due to the real collision.

$$BBCRate = VPDRate * Slope = \frac{nVPDEvts * Prescale_{VPD}}{RunTime * LiveTime_{VPD}} * Slope, \text{ for a given run}$$

278 then, we would have:

$$\lambda \cong \frac{BBCRate/\epsilon^2}{9.838MHz * \frac{102}{120}} = \frac{nVPDEvts * Prescale_{VPD}}{RunTime * LiveTime_{VPD}} * Slope * \frac{1}{\epsilon^2} * \frac{1}{9.838MHz * \frac{102}{120}}$$

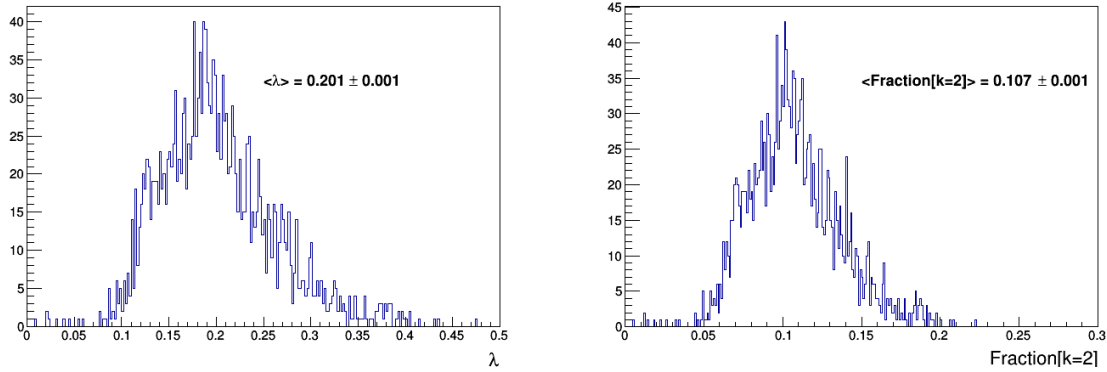


Figure 9: The left panel shows the  $\lambda$  distribution and the right panel shows the  $fraction[k = 2]$  distribution

279 and for each run, we could get a  $\lambda$  and a  $Fraction[k = 2]$ , so to calculate the average of  $Fraction[k =$   
 280  $2]$  for all runs, we could do:

$$\langle Fraction[k = 2] \rangle = \frac{\sum_{firstRun}^{lastRun} eqv.MB[iRun] * Fraction(iRun)}{\sum_{firstRun}^{lastRun} eqv.MB[iRun]}$$

281 and the average  $\lambda$  and the average  $Frac[k = 2]$  are obtained as  $0.201 \pm 0.001$  and  $0.107 \pm 0.001$ . Thus,  
 282 the number of equivalent MB events should be corrected by:

$$N_{MB}^{eqv.,In-bunch-corr} = N_{MB}^{eqv.} * (1 + \langle Frac[k = 2] \rangle) = 2.7621 * 10^{12} * (1 + 0.107) = 3.06 * 10^{12}$$

283 Given that there's a small difference in the total number of analyzed BHT2\*BBC events between  
 284 the study on raw yield (206.584M) and the study on the  $N_{MB}^{eqv.}$  (211.8M), an additional scale factor of  
 285  $206.584/211.8$  is applied, yielding the final  $N_{MB}^{eqv.,finale} = 2.98 * 10^{12}$  for p+p.

286 Similar thing can be done for p+Au collisions. The following is the relevant figure:

287

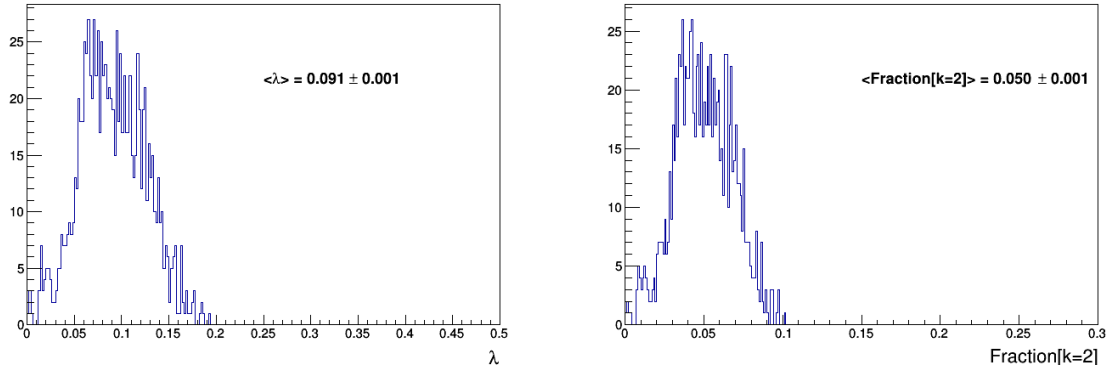


Figure 10: The left panel shows the  $\lambda$  distribution and the right panel shows the  $\text{fraction}[k = 2]$  distribution

288 The in-bunch pileup correction factor for p+Au collision is  $\langle \text{Frac}[k = 2] \rangle = 0.05 \pm 0.01$ . The total  
 289 number of BHT2\*BBCMB events in the raw yield study and the  $N_{MB}^{eqv.}$  study are 168.165M and 165.8M  
 290 respectively. Therefore the final  $N_{MB}^{eqv., finale} = 5.88 \times 10^{11}$  for p+Au.

291

## 292 5.4 Trigger bias study

293 In our simulation, Pythia and HIJING is used as the event generator for p+p and p+Au collisions  
 294 respectively. Then let the MC event go to STAR GEANT, and then mix the MC hits with those from the  
 295 Zero-bias data. In this way, the trigger bias study is done under the environment same as the real data  
 296 taking. And the Trigger bias definition is different for different method to calculate the equivalent MB  
 297 events. In the Trigger Bias study, we present two results corresponding to the two different methods to  
 298 calculate the equivalent MB events.

### 299 5.4.1 p+p

300 **Simulation setup** The event generator is Pythia8.162 + LHAPDF-6.1.4 (LHAPDF is a general pur-  
 301 pose C++ interpolator, used for evaluating PDFs from discretised data files, [detail document](#)). And  
 302 for the simulation, we have two kinds of events: MB only event and with  $J/\psi$  or  $\Upsilon$  event. For the MB  
 303 only event, the Pythia setting is "pythia8→Set("SoftQCD:minBias = on")". For the  $J/\psi$  or  $\Upsilon$  event,  
 304 a tuned settings named "STAR Heavy flavor tune" are used. And the details about the heavy flavor  
 305 tune can be found at: [STAR HF Tune](#)

- 306 • Pythia8 + GEANT + Zero-Bias embedding

307 Embed the simulated event into the Zero-bias triggered real data (daq files)

308 The daq files are picked up from every 2 runs, cover full run ranges

- 309 • Library: SL16d

- 310 • Chain options for simulation production:

311 "ry2015c geant gstar agml usexgeom Form(sdt%s,timestamp.Data())"

- 312 • Vertex setting:

313 1. Vx and Vy: Get the time stamp based the run-number, and cast the time stamp to bfc, let  
 314 it get the beam line shape from the database by itself. It will set the vx and vy to be same as in  
 315 real data

316 2. Vz: Set the Vz distribution with the Gaussian shape fitted from data

- 317 • Chain options used in the reconstruction step of simulation:

318 **fzin, gen<sub>T</sub>, geomT, sim<sub>T</sub>, TpcRS, sdtYYMMDD.HHMMSS, ry2015c, DbV20160418,**  
 319 **pp2015c, btof, mtd, mtdCalib, pp2pp, fmsDat, fmsPoint, fpsDat, BEMcChkStat, CorrX,**  
 320 **OspaceZ2, OGridLeak3D, -hitfilt, TpxClu, bbcSim, pxlFastSim, istFastSim, btofSim,**

emcY2, emcSim, EEfs, mtdsim, TpcMixer, GeantOut, MiniMcMk, McAna, IdTruth,  
-in, useInTracker, -emcDY2

- with  $J/\psi$  or  $\Upsilon$  filter:

$J/\psi$  event:  $|y_{J/\psi}| < 1, |\eta_{e^+/e^-}| < 1, p_T(e^+/e^-) > 0.2 \text{ GeV}/c$

$\Upsilon$  event:  $|y_\Upsilon| < 1, |\eta_{e^+/e^-}| < 1, p_T(e^+/e^-) > 0.2 \text{ GeV}/c$

$D_0$  event:  $|y_{D_0}| < 1, |\eta_{(K/\pi)}| < 1, p_T(K/\pi) > 0.2 \text{ GeV}/c$

## Result

- Luminosity in the simulation(Zero-bias) is weighted to what in the real data.
- Definition of BBC trigger: both BBC East and BBC West fired, denoted as "BBCAnd"
- Vertex cut:  $|Vz| < 80 \text{ cm}$  (default vertex)
- dVzCut:  $|rcVz - mcVz| < 1.5 \text{ cm}$
- Good Vertex: dVzCut and *Ranking*  $> 0$

For the  $J/\psi$  or  $\Upsilon$  cross-section calculation in this case:

$$\sigma_{J/\psi} = \frac{\sigma_{MB}}{N_{MB}^{equiv.} \epsilon_{MB}^{goodvtx}} * \frac{N_{J/\psi}^{raw}}{\epsilon_{J/\psi}^{Trig} \epsilon_{J/\psi}^{trk} \epsilon_{J/\psi}^{eID}} * \frac{\epsilon_{MB}^{BBC} \epsilon_{MB}^{goodvtx}}{\epsilon_{J/\psi}^{BBC} \epsilon_{J/\psi}^{goodvtx}}$$

As the  $N_{MB}^{equiv.}$  is corrected by the in-bunch pile up effects( $Frack[k=2]$ ), thus the corresponding  $\epsilon_{MB}^{BBC}$ ,  $\epsilon_{J/\psi}^{BBC}$ ,  $\epsilon_{MB}^{goodvtx}$ ,  $\epsilon_{J/\psi}^{goodvtx}$  should also be corrected accordingly.

The BBC trigger efficiency can be corrected by:

$$\langle \epsilon \rangle = \epsilon[k=1] * Frack[k=1] + \epsilon[k=2] * Frack[k=2] \quad \langle \epsilon_{MB}^{BBC} \rangle = \epsilon_{MB}^{BBC} [k=1] * Frack[k=1] + \epsilon_{MB}^{BBC} [k=2] * Frack[k=2]$$

and we have:

- $\epsilon_{MB}^{BBC} [k=1] = \epsilon_1^2$ , and  $\epsilon_{MB}^{BBC} [k=2] = \epsilon_1^2 (2 - \epsilon_1)^2$
- $\epsilon_{J/\psi}^{BBC} [k=1] = \epsilon_2^2$ , and  $\epsilon_{J/\psi+MB}^{BBC} [k=2] = \epsilon_1^2 \epsilon_2^2 + [2\epsilon_1^2 \epsilon_2 (1 - \epsilon_2) + 2\epsilon_2^2 \epsilon_1 (1 - \epsilon_1)] + [\epsilon_1^2 (1 - \epsilon_2^2) + \epsilon_2^2 (1 - \epsilon_1^2)] + 2\epsilon_1 (1 - \epsilon_1) \epsilon_2 (1 - \epsilon_2) = (\epsilon_1 + \epsilon_2 - \epsilon_1 \epsilon_2)^2$

Where  $\epsilon_1$  is BBC single side efficiency from the MB only event simulations and  $\epsilon_2$  is the BBC single side efficiency from Jpsi or Upsilon event simulations.

Note that for the BBC efficiency of  $J/\psi$  event, we can ignore the probability of 2  $J/\psi$  produced in a bunch crossing, instead, we consider 1  $J/\psi$  event + 1 MB event here.

FireType/EvtType	MBonly	$J/\psi$	$\Upsilon$	$D_0$
BBCsingleFire	0.9278	0.9119	0.9038	0.9179
BBCdoubleFire	0.8603	0.8316	0.8166	0.8425

Table 1: Run15 pp BBC single fire and double fire efficiencies

And for the good vertex reconstruction efficiency.  $\epsilon_{MB}^{goodvtx}$  will be canceled, so it doesn't need any further corrections.

And for the ZB data, the probabilities of k=0, k=1 and k=2 can be given by Poisson distributions:  $P_0 = e^{-\lambda}$ ,  $P_1 = \lambda e^{-\lambda}$ ,  $P_2 = \frac{\lambda^2}{2} e^{-\lambda}$ . Let the probability to produce a  $J/\psi$  in a event be  $p_{J/\psi}$ ,  $p_{J/\psi}$  should be  $\ll P_0, P_1, P_2$ .

K/ $\epsilon_{BBC}$	$\epsilon_{MB}^{BBC}$	$\epsilon_{MB+J/\psi}^{BBC}$	$\epsilon_{MB+\Upsilon}^{BBC}$	$\epsilon_{MB+D_0}^{BBC}$
K=1	0.8608	0.8316	0.8169	0.8425
K=2	0.9896	0.9873	0.9862	0.9882

Table 2: Run15 pp BBC efficiencies for K=1 and K=2



351 Since a MC  $J/\psi$  event is embedded into a Zero-Bias event, in principle, each event in these simulation  
 352 should be:

$$1 J/\psi \text{ event} + 1 \text{ ZB event}$$

353 And for the  $\epsilon_{J/\psi}^{goodvtx}$  in the PYTHIA+GEANT+ZeroBias simulation is from the total contribution of  
 354  $1 J/\psi \text{ event} + 1 \text{ ZB event}(k=0, k=1, k=2)$ . Thus the relative contributions of  $k=0, k=1, k=2$  will be  
 355 proportional to  $p_{J/\psi} * p_0 : p_{J/\psi} * p_1 : p_{J/\psi} * p_2$ , which is actually same as in the real data of our analysis.  
 356 Thus  $\epsilon_{J/\psi}^{goodvtx}$  can be obtained directly from the PYTHIA+GEANT+ZeroBias simulations.

$\langle \epsilon_{MB}^{BBC} \rangle$	$\langle \epsilon_{J/\psi}^{BBC} \rangle$	$\langle \epsilon_{\Upsilon}^{BBC} \rangle$	$\langle \epsilon_{D_0}^{BBC} \rangle$
0.8746	0.8483	0.8350	0.8582

Table 3: Run15 pp BBC efficiencies

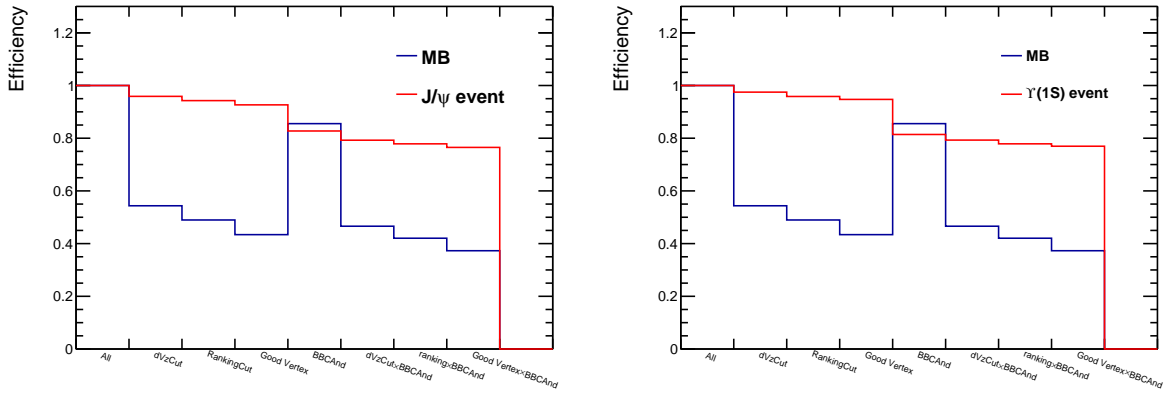


Figure 11:  $dVzCut: |mcVz - rcVz| < 1.5 \text{ cm cm}$ ;  $RankingCut: ranking > 0$ ; good Vertex:  $dVzCut \& RankingCut$ ;  $BBCAnd$ : BBC both sides fired; we are using the default vertex (highest ranking)

$\langle \epsilon_{MB}^{goodVtx} \rangle$	$\langle \epsilon_{J/\psi}^{goodVtx} \rangle$	$\langle \epsilon_{\Upsilon}^{goodVtx} \rangle$	$\langle \epsilon_{D_0}^{goodVtx} \rangle$
0.4340	0.9266	0.9472	0.8487

Table 4: Run15 pp good Vertex efficiency

357 And the final trigger bias factors (while BBC as the Base trigger) are calculated and listed in Table. 5

	$J/\psi$	$\Upsilon$	$D_0$
TrigBias	0.4829	0.4800	0.5211

Table 5: Run15 pp Trigger Bias  $\frac{\langle \epsilon_{MB}^{BBC} \rangle \langle \epsilon_{MB}^{goodvtx} \rangle}{\langle \epsilon_{e xtpArticle}^{BBC} \rangle \langle \epsilon_{e xtpArticle}^{goodvtx} \rangle}$ , Particle =  $J/\psi$  or  $\Upsilon$ .

358 **Contribution to global systematic uncertainty** The TrigBias is calculated using another Pythia8  
 359 tuning "Tune:4Cx". More information about the Tune:4Cx can be found at: [http://home.thep.lu.se/tor-](http://home.thep.lu.se/torbjorn/pythia81html/Tunes.html)  
 360 [bjorn/pythia81html/Tunes.html](http://home.thep.lu.se/torbjorn/pythia81html/Tunes.html).

361

	$J/\psi$	$\Upsilon$
TrigBias	0.4816	0.4837

Table 6: Run15 pp Trigger Bias  $\frac{\langle \epsilon_{MB}^{BBC} \rangle \langle \epsilon_{MB}^{goodvtx} \rangle}{\langle \epsilon_{e xtpArticle}^{BBC} \rangle \langle \epsilon_{e xtpArticle}^{goodvtx} \rangle}$ , Particle =  $J/\psi$  or  $\Upsilon$ .

362 Take the difference between the Trig-Bias results with HF-Tune and Tune:4Dx as the systematic  
 363 uncertainty of Trig-Bias.

364

	$J/\psi$	$\Upsilon$
TrigBias Sys.Error	2.7%	0.7%

Table 7: Systematic uncertainties of 2015 pp Trigger Bias of  $J/\psi$  or  $\Upsilon$ .

## 365 5.4.2 p+Au

366 **Simulation setup** The event generator is HIJING + LHAPDF-6.1.4 (LHAPDF is a general purpose  
 367 C++ interpolator, used for evaluating PDFs from discretised data files, [detail document](#)). And for the  
 368 simulation, we have two kinds of events: MB only event and with  $D^0$  event. (Quarkonium production  
 369 is not available in HIJING simulator,  $D^0$  is used to mimic the  $J/\psi$  events for the Trigger Bias study of  
 370 Run15 pAu.

371

- Settings for the MB-only events in HIJING:

```
372 hijing→SetImpact(0.0, 15.0); //Impact parameter (min, max) (fm)
373 hijing→hiparnt().ihpr2(4)=0; //Jet quenching (1=yes/0=no)
374 hijing→hiparnt().ihpr2(3)=0; //Hard scattering (heavy quark)
375 hijing→hiparnt().ihpr2(18) = 1; // Turn on/off B production
376 hijing→hiparnt().hipr1(10) = 2.0; // pT jet
377 hijing→hiparnt().ihpr2(8) = 10; // Max number of jets /nucleon
378 hijing→hiparnt().ihpr2(11) = 1; // Set baryon production
379 hijing→hiparnt().ihpr2(12) = 1; // Turn on/off decay of particles
380 hijing→hiparnt().hipr1(7) = 5.35; // Set B production
381 hijing→hiparnt().ihpr2(21) = 1; //Enable to track all particles
```

- Settings for the  $D^0$  events in HIJING:

```
382 hijing→SetImpact(0.0, 15.0); //Impact parameter (min, max) (fm)
383 hijing→hiparnt().ihpr2(4)=0; //Jet quenching (1=yes/0=no)
384 hijing→hiparnt().ihpr2(3)=0; //Hard scattering (heavy quark)
385 hijing→hiparnt().ihpr2(18) = 1; // Turn on/off B production
386 hijing→hiparnt().hipr1(10) = 2.0; // p T jet
387 hijing→hiparnt().ihpr2(8) = 10; // Max number of jets /nucleon
388 hijing→hiparnt().ihpr2(11) = 1; // Set baryon production
389 hijing→hiparnt().ihpr2(12) = 1; // Turn on/off decay of particles
390 hijing→hiparnt().hipr1(7) = 5.35; // Set B production
391 hijing→hiparnt().ihpr2(21) = 1; //Enable to track all particles
```

- HIJING + GEANT + Zero-Bias embedding

```
392 Embed the simulated event into the Zero-bias triggered real data (daq files)
393 The daq files are picked up from every 2 runs, cover full run ranges
```

- Library: SL16d

- Chain options for simulation production:

```
394 "ry2015c geant gstar agml usexgeom Form(sdt%s,timestamp.Data())"
```

395

- 400 • Vertex setting:
  - 401 1. Vx and Vy: Get the time stamp based the run-number, and cast the time stamp to bfc, let  
402 it get the beam line shape from the database by itself. It will set the vx and vy to be same as in  
403 real data
  - 404 2. Vz: Set the Vz distribution with the Gaussian shape fitted from data
- 405 • Chain options used in the reconstruction step of simulation:
 

406 **fzin, gen<sub>T</sub>, geomT, sim<sub>T</sub>, TpcRS, sdtYYMMDD.HHMMSS, ry2015c, DbV20160418,**  
 407 **pp2015c, btof, mtd ,mtdCalib,pp2pp, fmsDat, fmsPoint, fpsDat, BEmcChkStat, CorrX,**  
 408 **OSpaceZ2, OGridLeak3D, -hitfilt, TpxClu, bbcSim, pxlFastSim,istFastSim, btofSim,**  
 409 **emcY2, emcSim, EEFs, mtdsim, TpcMixer, GeantOut, MiniMcMk, McAna, IdTruth,**  
 410 **-in, useInTracker, -emcDY2**
- 411
- 412 • with  $J/\psi$  or  $\Upsilon$  filter:
 

413  $J/\psi$  event:  $|y_{J/\psi}| < 1, |\eta_{e^+/e^-}| < 1, p_T(e^+/e^-) > 0.2 \text{ GeV}/c$   
 414  $\Upsilon$  event:  $|y_\Upsilon| < 1, |\eta_{e^+/e^-}| < 1, p_T(e^+/e^-) > 0.2\text{GeV}/c$   
 415  $D_0$  event:  $|y_{D_0}| < 1, |\eta_{(K/\pi)}| < 1, p_T(K/\pi) > 0.2 \text{ GeV}/c$

416 **Result** After considering the in-bunch pileup contribution, the BBC trigger efficiency can be corrected  
 417 by:

$$\langle \epsilon \rangle = \epsilon[k=1]*\text{Frac}[k=1] + \epsilon[k=2]*\text{Frac}[k=2] < \epsilon_{MB}^{BBC} \rangle = \epsilon_{MB}^{BBC}[k=1]*\text{Frack}[k=1] + \epsilon_{MB}^{BBC}[k=2]*\text{Frack}[k=2]$$

K/ $\epsilon_{BBC}$	$\epsilon_{MB}^{BBC}$	$\epsilon_{MB+D_0}^{BBC}$
K=1	0.8355	0.8823
K=2	0.9829	0.9865

Table 8: Run15 pAu BBC efficiencies for K=1 and K=2

418 and we have:

- 419 •  $\epsilon_{MB}^{BBC}[k=1] = \epsilon_E(MB) * \epsilon_W(MB)$
- 420 •  $\epsilon_{MB}^{BBC}[k=2] = \epsilon_E(MB) * \epsilon_W(MB) * (2 - \epsilon_E(MB))(2 - \epsilon_W(MB))$
- 421 •  $\epsilon_{D_0}^{BBC}[k=1] = \epsilon_E(D_0) * \epsilon_W(D_0)$
- 422 •  $\epsilon_{D_0+MB}^{BBC}[k=2]$ 

$$423 = \epsilon_E(MB) * \epsilon_W(MB) * \epsilon_E(D_0) * \epsilon_W(D_0) + \epsilon_E(MB) * \epsilon_W(MB) * \epsilon_E(D_0) * (1 - \epsilon_W(D_0)) + \epsilon_E(MB) * \epsilon_W(MB) * (1 - \epsilon_E(D_0)) * \epsilon_W(D_0) + \epsilon_E(MB) * (1 - \epsilon_W(MB)) * \epsilon_E(D_0) * \epsilon_W(D_0) + (1 - \epsilon_E(MB)) * \epsilon_W(MB) * \epsilon_E(D_0) * \epsilon_W(D_0) + \epsilon_E(MB) * \epsilon_W(MB) * (1 - \epsilon_E(D_0)) * (1 - \epsilon_W(D_0)) + (1 - \epsilon_E(MB)) * (1 - \epsilon_W(MB)) * \epsilon_E(D_0) * \epsilon_W(D_0) + \epsilon_E(MB) * (1 - \epsilon_W(MB)) * (1 - \epsilon_E(D_0)) * \epsilon_W(D_0) + (1 - \epsilon_E(MB)) * \epsilon_W(MB) * \epsilon_E(D_0) * (1 - \epsilon_W(D_0))$$

$$428 = \epsilon_E(MB) * \epsilon_W(MB) * \epsilon_E(D_0) * \epsilon_W(D_0) - \epsilon_E(MB) * \epsilon_W(MB) * (\epsilon_E(D_0) + \epsilon_W(D_0)) - (\epsilon_E(MB) + \epsilon_W(MB)) * \epsilon_E(D_0) * \epsilon_W(D_0) + \epsilon_E(MB) * \epsilon_W(MB) + \epsilon_E(D_0) * \epsilon_W(D_0) + \epsilon_E(MB) * \epsilon_W(D_0) + \epsilon_W(MB) * \epsilon_E(D_0)$$

431 Where  $\epsilon_E(MB), \epsilon_W(MB), \epsilon_E(D_0), \epsilon_W(D_0)$  is BBC single side efficiencies from the MB only or the  $D_0$   
 432 event simulations. Note that for the BBC efficiency of  $D_0$  event, we can ignore the probability of 2  $D_0$   
 433 produced in a bunch crossing, instead, we consider 1  $D_0$  event + 1 MB event here.

$\langle \epsilon_{MB}^{BBC} \rangle$	$\langle \epsilon_{D_0}^{BBC} \rangle$
0.8428	0.8874

Table 9: Run15 pAu BBC efficiencies

$\langle \epsilon_{MB}^{goodVtx} \rangle$	$\langle \epsilon_{D_0}^{goodVtx} \rangle$
0.5464	0.9268

Table 10: Run15 pAu good Vertex efficiency

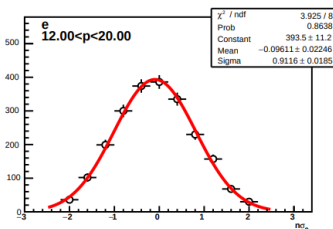
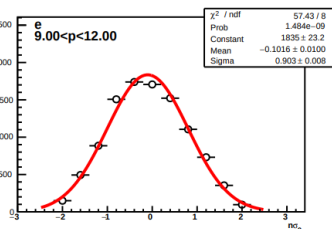
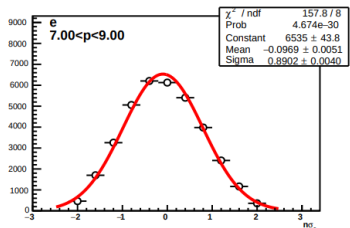
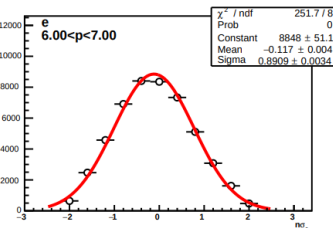
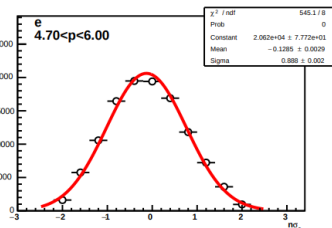
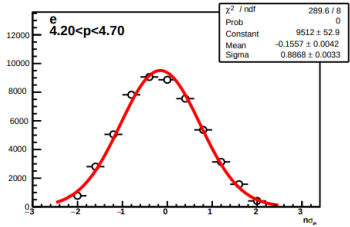
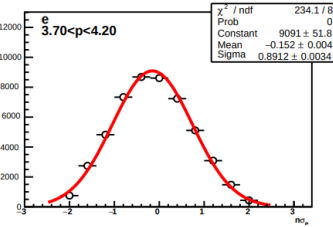
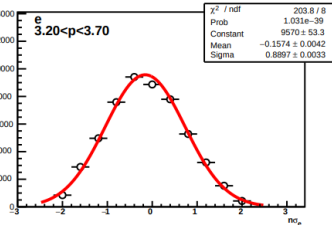
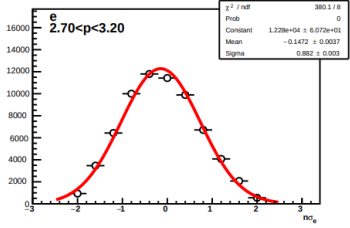
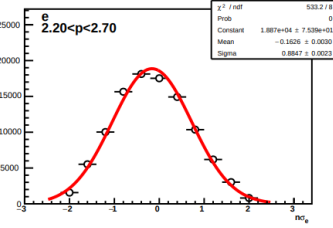
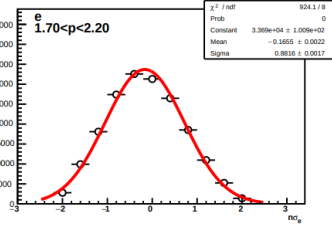
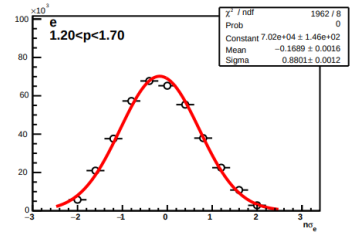
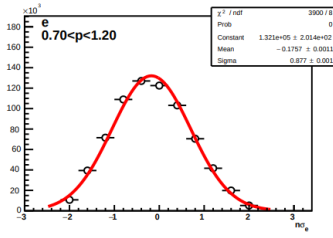
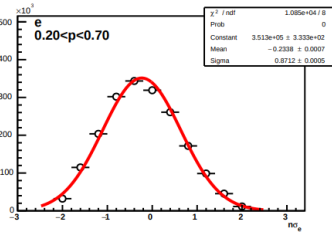
	$D_0$
TrigBias	0.5599

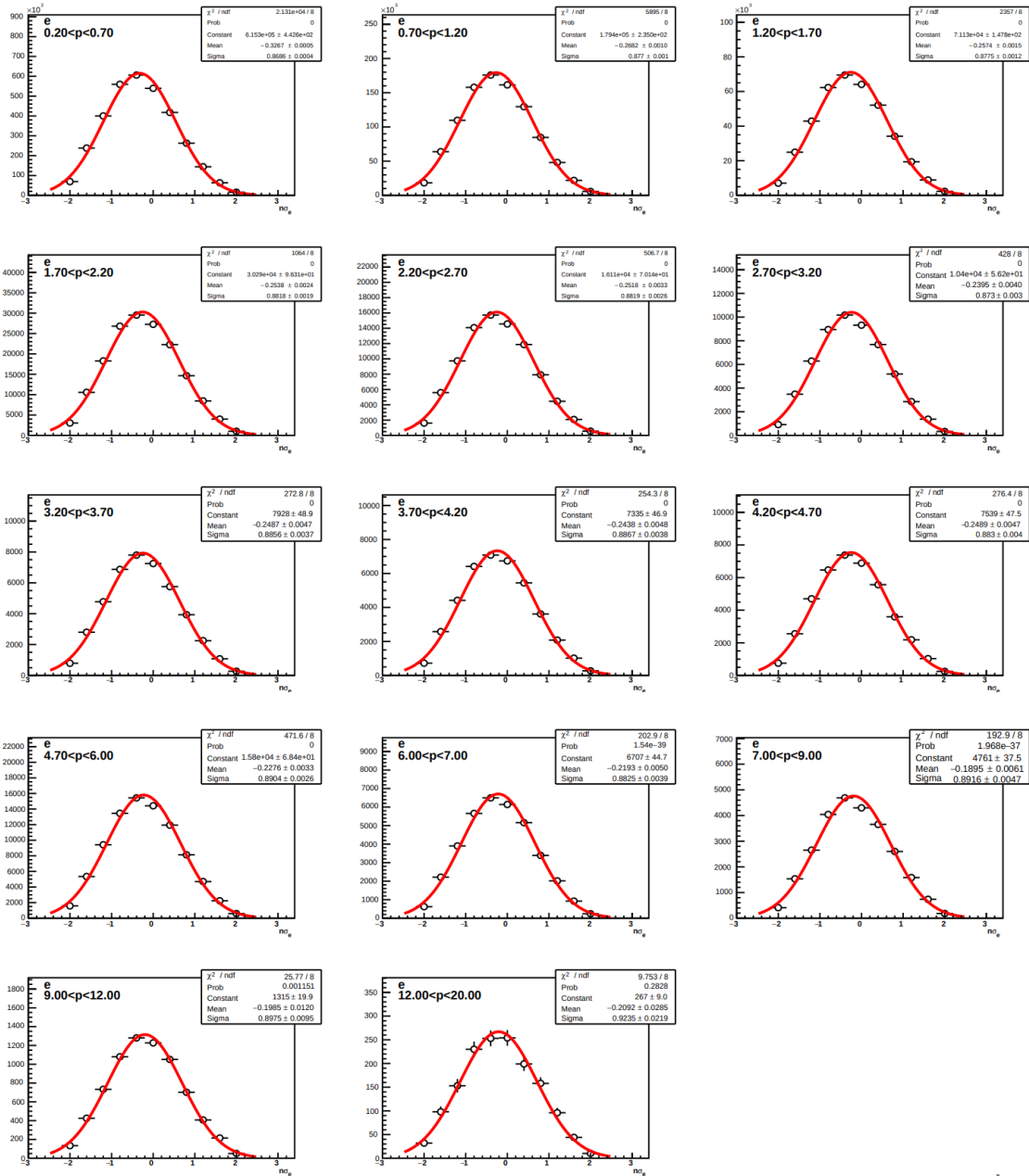
Table 11: Run15 pAu Trigger Bias  $\frac{\langle \epsilon_{MB}^{BBC} \rangle \langle \epsilon_{MB}^{goodvtx} \rangle}{\langle \epsilon_{e_xtpArticle}^{BBC} \rangle \langle \epsilon_{e_xtpArticle}^{goodvtx} \rangle}$ , Particle =  $D_0$ .

## 434 5.5 Data Driven $n\sigma_e$ Efficiency

435 The STAR embedding does not provide acceptable simulation on the  $n\sigma_e$  (see Embedding QA ap-  
436 pendix), therefore the  $n\sigma_e$  efficiency is extracted from data with photonic electron pairs. In this analysis,  
437 the photonic electron pairs are selected by requiring  $M_{ee} < 0.24\text{GeV}/c^2$  and  $\text{DCA}_{ee} < 1$  cm on top of  
438 basic tracking quality and kinematics cuts. The mean and width of  $n\sigma_e$  distribution are extracted from  
439 this sample as functions of momentum ( $p$ ). Both mean and width show asymptotic behavior towards con-  
440 stant. Therefore, functions are extrapolated over  $p > 20$  GeV/c with constant fits in  $3 < p < 20\text{GeV}/c$ .  
441 With these functions, and given  $n\sigma_e$  cuts and reconstructed  $p$  of each track, we can calculate the proba-  
442 bility of the track being selected, which is by definition the  $n\sigma_e$  efficiency. The following shows how the  
443 momentum range is binned and Gaussian fit results in each bin for both p+p and p+Au:  
444

445 **p+p**





## 5.6 Single $e^\pm$ Efficiencies and $p_T$ Smearing Templates in Embedding

The single  $e^\pm$  efficiencies are extracted from embedding to be utilized in EvtGen, in order to implement a more realistic decay model. All cuts mentioned in the “Event and Track Selection” section is applied based on embedding result, with one exception of the data driven  $n\sigma_e$  efficiency implementation. The other cuts will accept or reject the events/tracks, while the  $n\sigma_e$  distribution extracted from the previous section provides the  $n\sigma_e$  efficiency as a function of  $e^\pm$  reconstructed momentum and serve as weighting factors. Only the prompt daughter  $e^\pm$ s (before interacting with detector materials) are included, i.e. scattering electrons are not included.

The following is a list of cuts used in this analysis of different category:

**Tracking:** nHitsFit, nHitsDedx, nHitsRatio, DCA,  $n\sigma_e$ ,  $\eta$ ,  $p_T$

457 **Electron Identification:** e/p, deposited energy

458 **Trigger electron:** Adc0, Dsmadc, trigger  $p_T$

459 Cuts are combined into groups for convenience. The groups are named by “TPC” cuts, “EID” cuts  
460 and “Trigger” cuts (short as “TRG”).

461 1. “TPC” includes all cuts that have non-negligible  $\varphi$  dependence and must exclude cuts that  
462 directly depend on reconstructed momentum ( $p_T^{RC}$ ): nHitsFit, nHitsDedx, nHitsRatio, DCA,  $\eta$

463 2. “TRG” includes the only 3 trigger related cuts: Adc0, Dsmadc

464 3. “EID” includes the rest of the cuts (deposited energy in EMC tower e, e/p,  $n\sigma_e$ ), must have  
465 positive  $p_T$ )

466 Such grouping is mainly for the following consideration:

467 1) All cuts that could influence “ $p_T$  smearing” and “additional smearing” are contained in a single  
468 group (TPC)

469 2) All cuts whose variable directly depend on on  $p_T^{RC}$  are contained in a single group (EID)

470 3) All cuts that has  $\varphi$  dependence are contained in a single group (TPC)

471 4) All cuts that reject positrons and electrons differently are contained in a single group (TPC)

472 The following are the definition of efficiencies. The kinematics variable  $p_T$ ,  $\eta$  and  $\varphi$  are all in MC  
473 level.

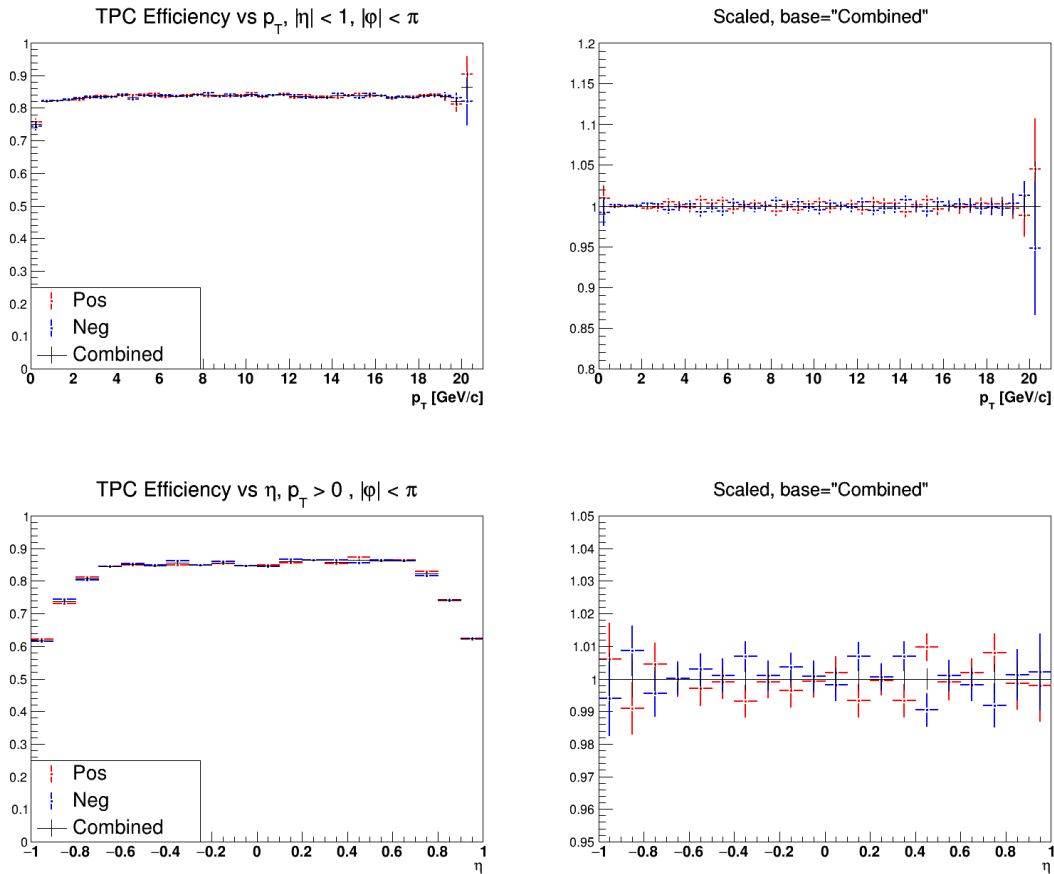
474 1. The TPC have  $p_T$ ,  $\eta$  and  $\varphi$  dependence, and electrons and positrons are treated separately. The  
475 definition is as follows:

$$476 \epsilon_{\pm}^{TPC}(p_T, \eta, \varphi) = \frac{N_{\pm}^{TPC}(p_T, \eta, \varphi)}{N_{\pm}^{MC}(p_T, \eta, \varphi)}$$

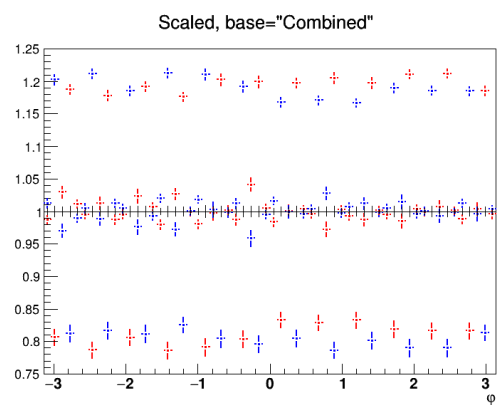
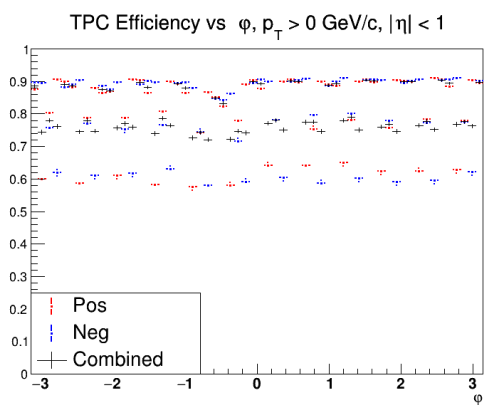
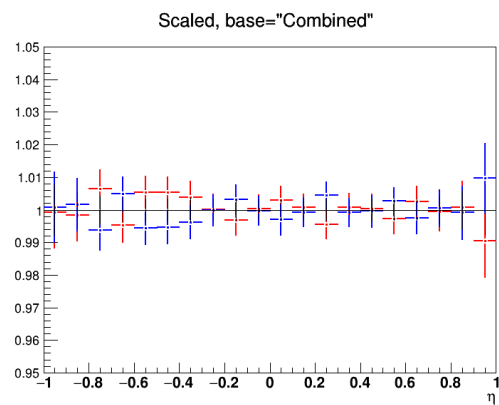
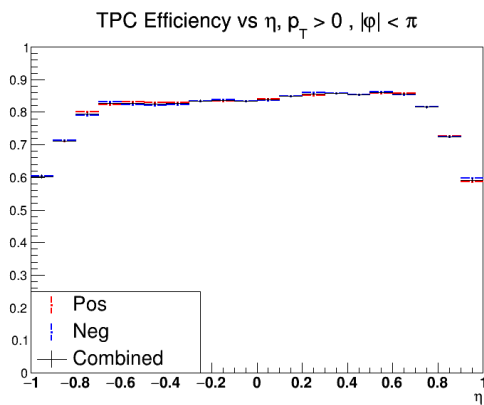
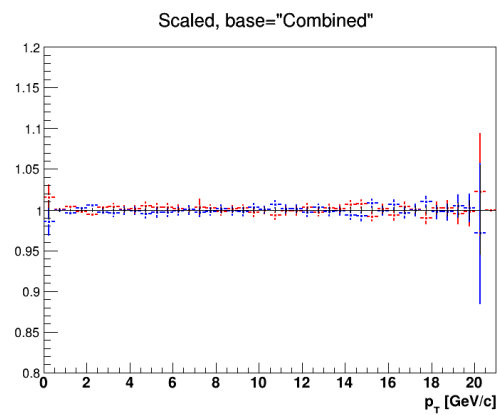
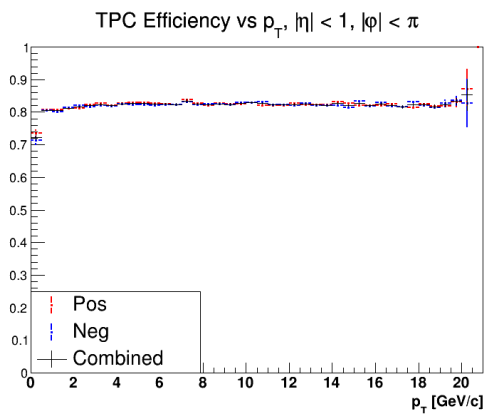
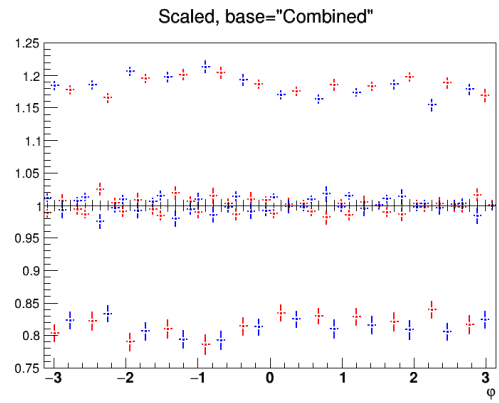
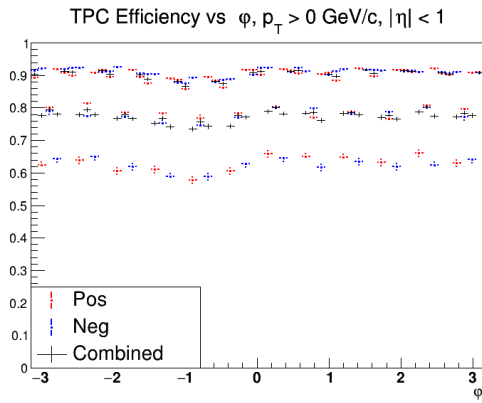
477 where the  $N_{\pm}^{MC}$  is the number of MC electron/positron, and  $N_{\pm}^{TPC}$  is the number of electron/positron  
478 that passed TPC cuts. The following plots show the dependency of TPC efficiency on  $p_T$ ,  $\eta$  and  $\varphi$ .

479 Significant difference is observed in  $\varphi$  dependence. These are purely for demonstration purposes since  
480 they are integrated over 2 out of 3 designed variable ( $p_T$ ,  $\eta$  and  $\varphi$ ).

481 **p+p**



## p+Au





483 2. The EID efficiency is calculated separately for 3 “types” of  $e^\pm$ : 1) Triggered, short as TRG (pass  
 484 TPC, EID and TRG); 2) Non-triggered, short as !TRG or NTR (pass TPC, EID while rejected by TRG);  
 485 3) the union of the previous 2, short as ALL (pass TPC and EID). The efficiencies are defined as follows:

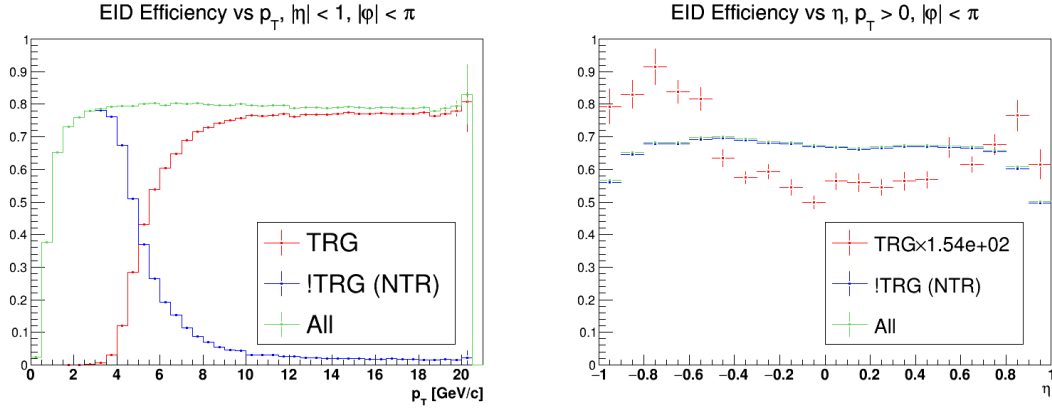
486 2.1 TRG:  $\epsilon^{EID,TRG}(p_T, \eta) = \frac{N_e^{TPC,EID,TRG}(p_T,\eta)}{N_e^{TPC}(p_T,\eta)}$

487 2.2 !TRG:  $\epsilon^{EID,!TRG}(p_T, \eta) = \frac{N_e^{TPC,EID,!TRG}(p_T,\eta)}{N_e^{TPC}(p_T,\eta)}$

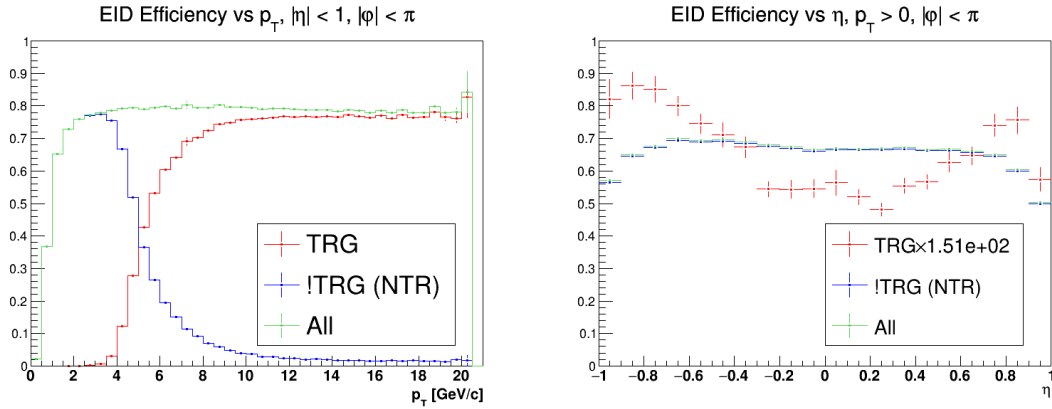
488 2.3 ALL:  $\epsilon^{EID}(p_T, \eta) = \frac{N_e^{TPC,EID}(p_T,\eta)}{N_e^{TPC}(p_T,\eta)}$

489 The following plots show the dependency of EID efficiencies on  $p_T$  and  $\eta$ . These are purely for  
 490 demonstration purposes since they are integrated over 1 out of 2 designed variable ( $p_T$  and  $\eta$ ).

491 **p+p**



492 **p+Au**



493 The distributions of  $\frac{p_T^{RC}}{p_T^{MC}} - 1$  are extracted separately for the aforementioned 3 types of electrons in  
 494 different  $e^\pm$  MC  $p_T$  bins. They will be used as  $e^\pm$   $p_T$  smearing templates in the next step where EvtGen  
 495 is utilized. The following plots show the templates for  $e^\pm$  with MC  $p_T$  between 0.5 to 12.5 GeV/c for  
 496 p+p and p+Au collisions.

## 497 5.7 J/ $\psi$ Reconstruction in EvtGen and J/ $\psi$ Efficiency

498 The single  $e^\pm$  efficiencies and  $p_T$  smearing templates are fed into EvtGen. A straight forward J/ $\psi$   
 499 reconstruction process is listed below:

- 500 1. EvtGen decays a J/ $\psi$  into di-electron pairs. We have access to their MC level momentum  
 501 information.
- 502 2. The di-electron pair ( $e_1, e_2$ ) can be detected in the following combination of  $e^\pm$ :  
 503 1)  $e_1$  - TRG,  $e_2$  - !TRG  
 504 2)  $e_1$  - !TRG,  $e_2$  - TRG  
 505 3)  $e_1$  - TRG,  $e_2$  - TRG

506 3. All 3 cases are taken into account for each  $J/\psi$  decay. In each case, both  $e_1$  and  $e_2$  obtain a  
507 smeared  $p_T$  according to template corresponds to its type (TRG, !TRG), and then be used to reconstruct  
508  $J/\psi$ . The RC  $J/\psi$  is weighted by the multiplication of RC efficiency of both daughter. Afterwards, like  
509 in real data, basic kinematics cut are applied (on  $p_T$  and  $\eta$ ) to accept or reject the RC  $J/\psi$ . It's worth  
510 noting that, although all 3 cases contribute to the RC  $J/\psi$  counts, they contributes to different kinematics  
511 range due to the difference in the  $e^\pm$  smearing templates used in each case.

512 Alternatively,  $(e_1, e_2)$  can be detected in another combination:

- 513 1)  $e_1$  - TRG,  $e_2$  - ALL
- 514 2)  $e_1$  - ALL,  $e_2$  - TRG
- 515 3)  $e_1$  - TRG,  $e_2$  - TRG

516 Here, instead of summing up all 3 cases, one needs to subtract 3) from then sum of 1) and 2). In  
517 the ‘‘Choice of Decay Model’’ section, we will see that both combinations can reproduce the embedding  
518  $J/\psi$  efficiency in the  $p_T$  range of interest (below 12 GeV/c), while in the high  $p_T$  range the **TRG+All**  
519 combination has less bias in high  $p_T$  range compared to the **TRG+!TRG**. Therefore the **TRG+All**  
520 combination is chosen in this analysis.

521 The  $J/\psi$  RC efficiency is then calculated by making a ratio of number of RC  $J/\psi$  falls in a mass  
522 window ( $2.6 < \text{mass} < 3.35 \text{ GeV}/c^2$ ) against MC  $J/\psi$  on the entire mass spectrum. It's worth noting that  
523 the embedding MC  $J/\psi$  does not have a single value mass, but a very narrow Breit-Wigner peak at the  
524  $J/\psi$  mean mass. The EvtGen is also set up to produce same MC  $J/\psi$  mass distribution for consistency.

## 525 5.8 Signal Extraction

526 All cut mentioned in the ‘‘Event and Track Selection’’ are applied in signal extraction for real data.  
527 The  $e^\pm$  in real data are paired into unlike-sign (**US**) and like-sign (**LS**) pairs. The LS is a good estimation  
528 of the uncorrelated combinatorial background contribution in US. It's worth noting that, in embedding,  
529 such a combinatorial background is zero by construction since pairs are included only and if only those  
530 pairs are the prompt daughters of the same  $J/\psi$ . The **US-LS** histograms are main subjects of study in the  
531 raw signal extraction section. It is integrated over  $\varphi$  and  $|y| < 1$ , and has  $p_T$  and pair mass dependence.  
532 Parctically speaking, the **US-LS** is considered as mass distributions in 6 wide  $p_T$  bins, with the bin edge  
533 of 4, 5, 6, 7, 8, 10 and 12 GeV/c.

### 534 5.8.1 Special Treatment of Low Effective Counts Bins

535 ROOT uses  $\sqrt{N}$  as the symmetric uncertainty of  $N$  counts bins by default, assuming they are in  
536 Poisson distribution with large statistics. Therefore, low effective counts bins need special treatment to  
537 compensate for underestimation of uncertainty. The unified confidence interval  $[\mu_1, \mu_2]$  of 90% and 95%  
538 for the mean of a Poisson variable given  $n$  observed events is listed below:

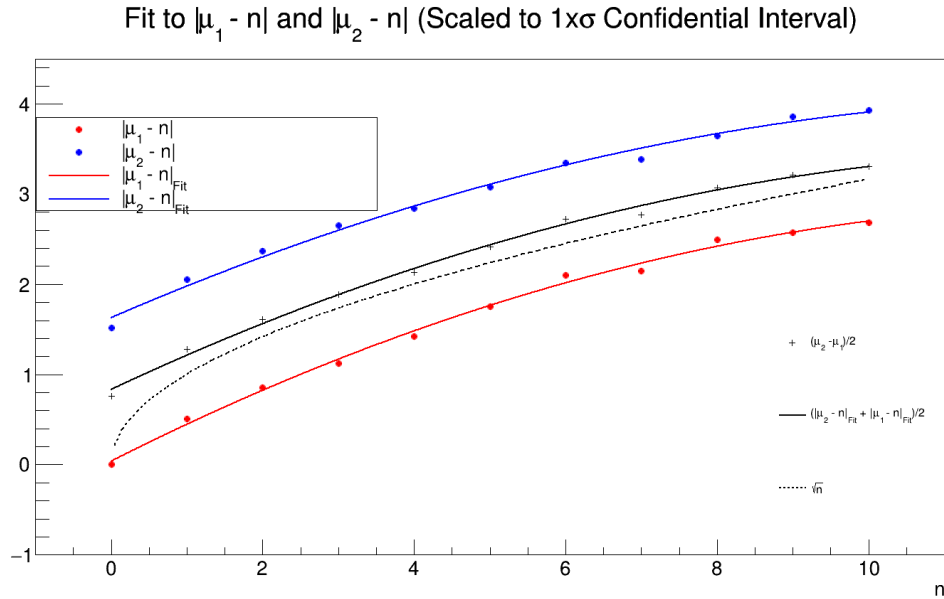
539 [Ref [https://pdg.lbl.gov/2023/reviews/contents\\_sports.html](https://pdg.lbl.gov/2023/reviews/contents_sports.html) Table 40.4]

	$1 - \alpha = 90\%$		$1 - \alpha = 95\%$	
n	$\mu_1$	$\mu_2$	$\mu_1$	$\mu_2$
0	0.00	2.44	0.00	3.09
1	0.11	4.36	0.05	5.14
2	0.53	5.91	0.36	6.72
3	1.10	7.42	0.82	8.25
4	1.47	8.60	1.37	9.76
5	1.84	9.99	1.84	11.26
6	2.21	11.47	2.21	12.75
7	3.56	12.53	2.58	13.81
8	3.96	13.99	2.94	15.29
9	4.36	15.30	4.36	16.77
10	5.50	16.50	4.75	17.82

540 The upper and lower limits are asymmetric. The 90% and 95% confidence interval is comparable to  
541  $2\sigma$  and  $1.64\sigma$  width in Gaussian respectively. In terms of the interval limits, slight inconsistency can  
542 be found between 90% and 95% after scaling the deviation  $|\mu_1 - n|, |\mu_2 - n|$  (from mean to the limits),  
543 to Gaussian  $1\sigma$  equivalent,  $\sqrt{n}$ . Therefore, the arithmetic average of the deviations are calculated.  
544 In the following figure, the points of  $|\mu_1 - n|, |\mu_2 - n|$  are the aforementioned average. These average values

545 are fit to the quadratic function separately. For simplicity, the average of the 2 fit functions  $f_{mid}(n)$  is  
 546 assigned to be the half width of a symmetric confidence interval centered at  $n$ .

547



548 This will enable treatment to non-integer effective counts bins due to weighting. The “ $\sqrt{n}$ ” curve  
 549 and the original half width  $\frac{\mu_2 - \mu_1}{2}$  points are also plotted for comparison. The correction will compensate  
 550 the underestimation of statistic uncertainties. The “effective counts” is defined by  $N = (\frac{C}{err})^2$ , where  $C$   
 551 is the bin content and  $err$  is the bin error. If  $N \leq 10$ ,  $f_{mid}(N)$  is assigned to be the corrected uncertainty  
 552 for this bin; when  $N > 10$  the difference is small so no treatment is applied.

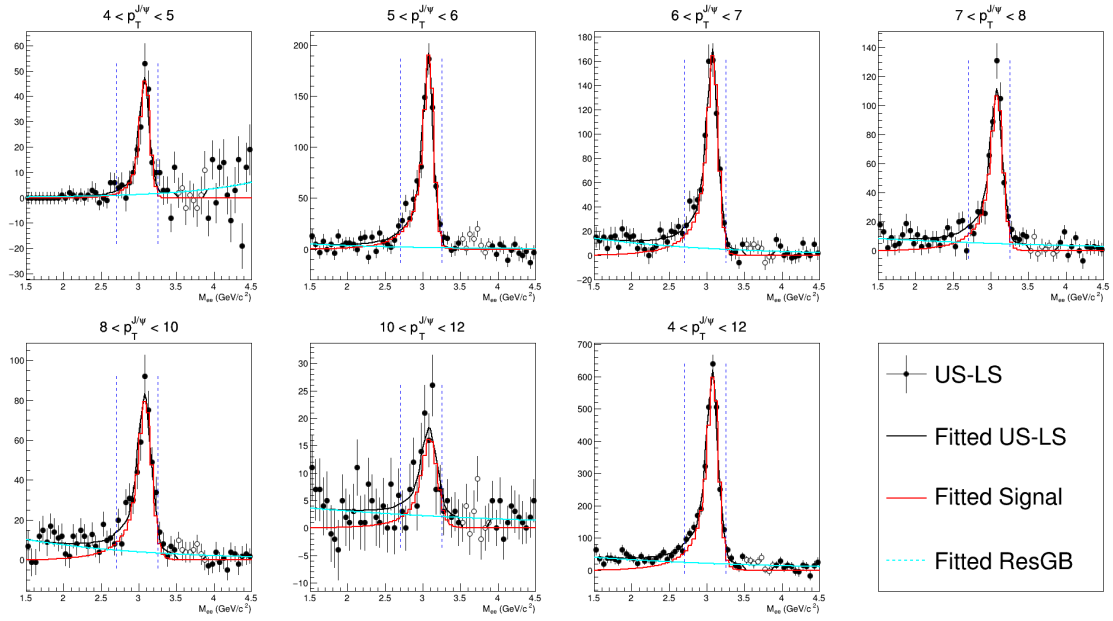
553 This special treatment is applied to **US** and **LS** after they are integrated over  $\varphi$  and  $|y| < 1$  and  
 554 rebinned in  $p_T$  and mass axis. Then **LSs** is subtracted from **USs**, yielding **US-LSs**, which are the  
 555 histograms studied in the following subsections.

### 556 5.8.2 Raw Yield Estimation

557 The aforementioned **US-LS** histograms are fit to functions with 2 contributions: signal (**SIG**) +  
 558 residual background (**ResBG**). The **SIG** is the normalized RC mass distribution from EvtGen, with a  
 559 scale factor  $N_{SIG}$  for normalization; the **ResBG** is arbitrary and chosen to be a exponential function  
 560  $N_{ResBG} \times e^{-bM_{e^+e^-}}$ , where  $N_{ResBG}$  is for normalization. The number of free parameters in those fits is  
 561 3:  $N_{SIG}$ ,  $N_{ResBG}$ , and  $b$ . The fit range is set to be  $1.5 < M_{e^+e^-} < 4.5 GeV/c^2$ . The fit options used are:  
 562 1) **I**, fit the integral of the function in the bin instead of the function value at bin center; 2) **M**, attempt  
 563 to find a better local minimum near the previous convergence. The following plots show the mass fit  
 564 in each  $p_T$  bin. (Note: the plots shown are after additional smearing, or more precisely “additionally  
 565 smeared fit”)

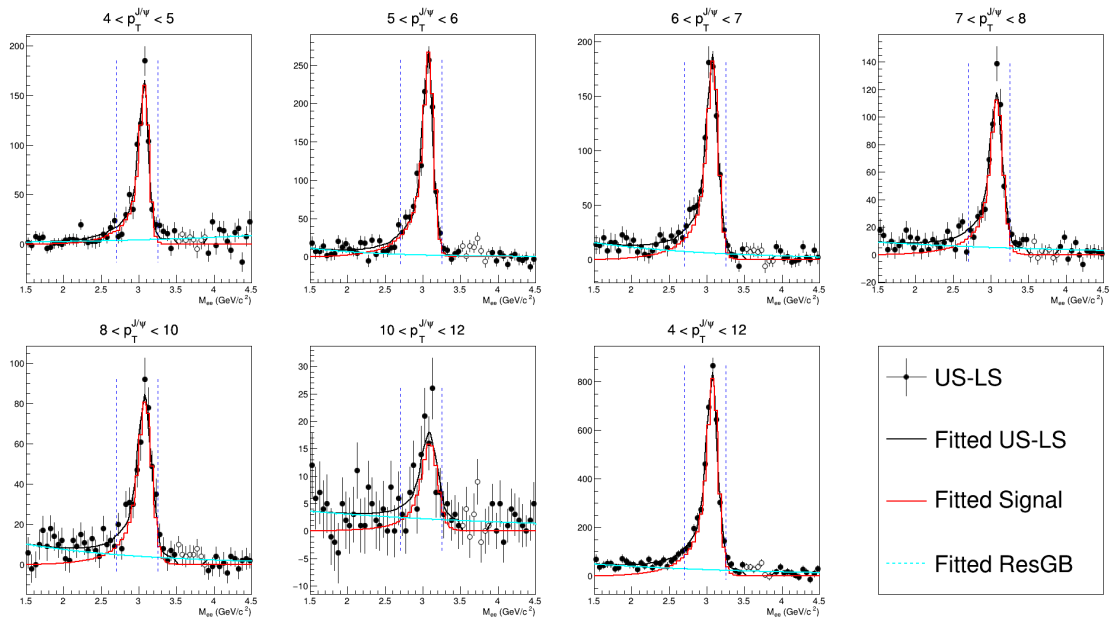
566 **p+p**

567 **Trigger  $p_T$  4.3 GeV/c**



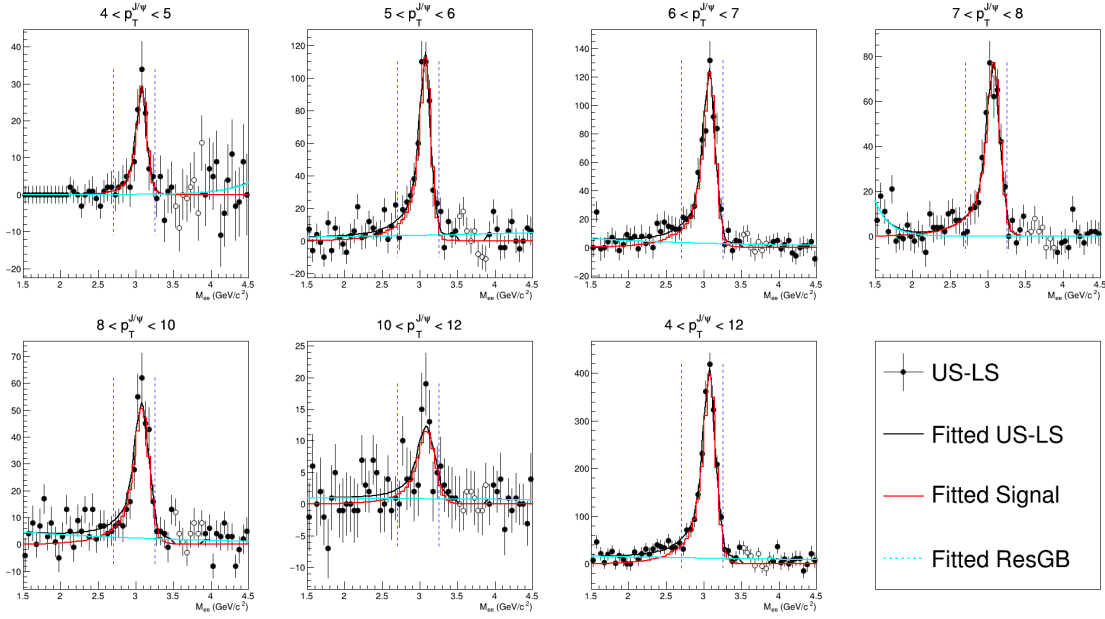
568

Trigger  $p_T$  3.5 GeV/c



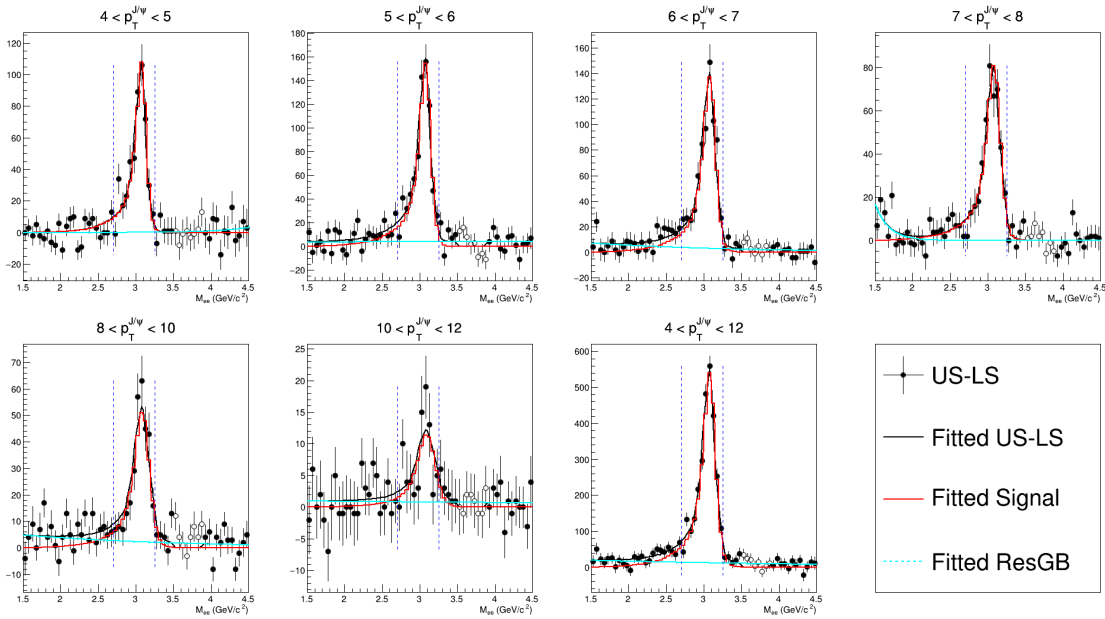
569 p+Au

570 Trigger  $p_T$  4.3 GeV/c



571

Trigger  $p_T$  3.5 GeV/c



572

The raw yield is estimated by subtracting the integral of resulting fit function's **ResBG** part from the integral of **US-LS**, within the mass window of 2.7 to 3.25 GeV/c<sup>2</sup>.

573

574

## 5.9 Additional Smearing and Parameter Optimization for the Momentum Resolution

575

576

As mentioned before, the embedding has overestimated the momentum resolution of  $e^\pm$  tracks. Additional smearing is aimed at providing a more realistic momentum resolution.

577

578

The resolution in  $\eta$  and  $\varphi$  are reasonably well-simulated therefore only the resolution in transverse momentum is additionally smeared.

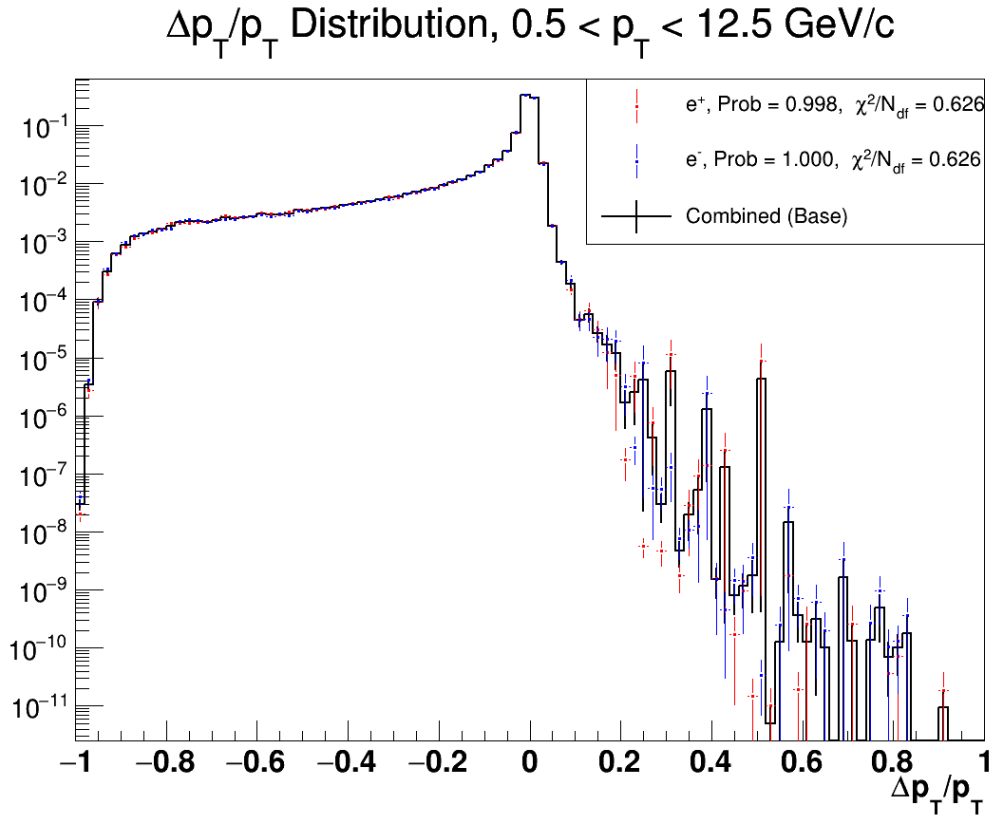
579

580

581 **5.9.1 Parameterization of RC Momentum Resolution in Embedding**

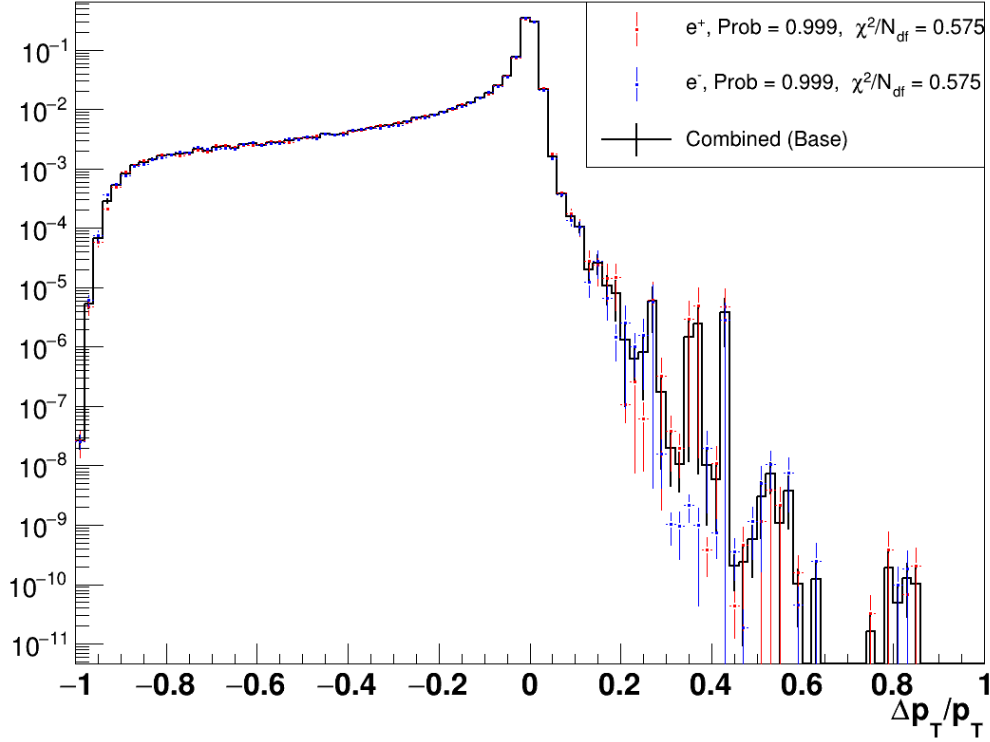
582 In this analysis, the  $e^\pm p_T$  resolution in embedding is characterized by the distribution of  $\frac{p_T^{RC}}{p_T^{MC}} - 1$ . A  
 583 comparison is made between positrons and electrons in this distribution, and they are consistent within  
 584 uncertainty. The positrons and electrons are combined for better precision. The following plots demon-  
 585 strates the embedding  $\frac{p_T^{RC}}{p_T^{MC}} - 1$  for electrons and positrons in p+p and p+Au collisions. Comparisons  
 586 are made in finer  $p_T$  bins but only the integrated ones are shown:  
 587

588 **p+p**



589 **p+Au**

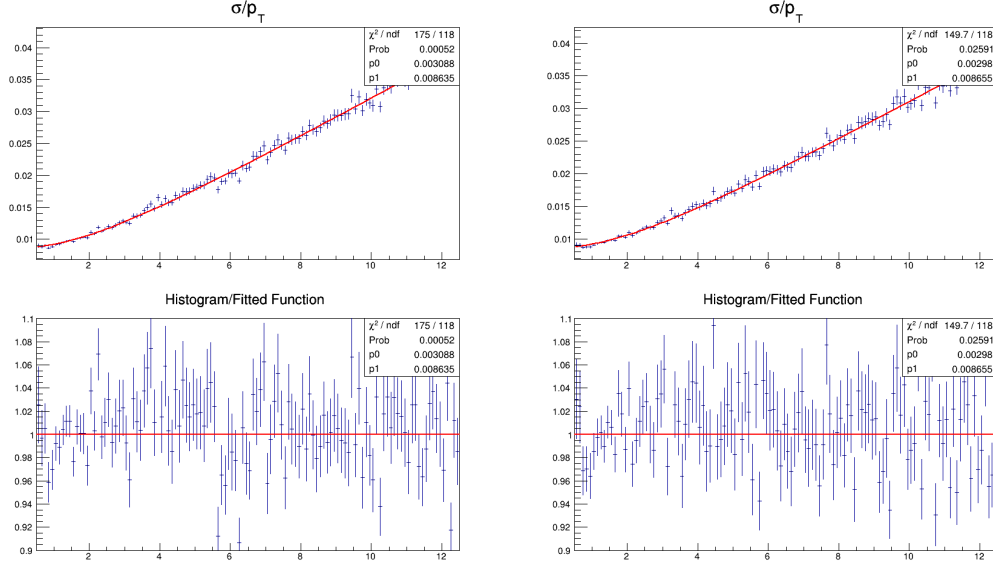
## $\Delta p_T/p_T$ Distribution, $0.5 < p_T < 12.5$ GeV/c



590 Near  $\frac{p_T^{RC}}{p_T^{MC}} - 1 = 0$  peak area, this distribution at different  $p_T^{MC}$  ( $p_T^{MC}$  bins) presents itself as a  
 591 Gaussian. Therefore, distributions at different  $p_T^{MC}$  are fit to Gaussian and the width of Gaussian as a  
 592 function of  $p_T^{MC}$  is extracted from this series of fit. This function can be well described by the following  
 593 empirical formula:  $f(p_T) = \sqrt{(ap_T)^2 + b^2}$ , where  $p_T$  is short for  $p_T^{MC}$  while  $a$  and  $b$  are parameters.

594 The fit range of aforementioned Gaussian fit for each  $p_T^{MC}$  bin is decided by a prior of  $f(p_T)$  and the  
 595 following empirical formula:  $x_{min} = -1.5 \times f(p_T)$ ,  $x_{max} = 2.0 \times f(p_T)$ . Essentially, this range includes  
 596 the  $-1.5\sigma$  to  $2.0\sigma$  region of the prior. The fit is conducted in an iterative manner, until the prior of  $f(p_T)$   
 597 is consistent with the resulting one. The selection of the scaling factors of  $-1.5$  and  $2.0$  is arbitrary but  
 598 carefully treated. It is intended to be as wide as possible, while within this fit range the distribution has  
 599 been guaranteed to be Gaussian. The ratio of histogram against the fit function is consistent to 1 within  
 600 fit range and starts to deviate from 1 when going outside. The following are the Gaussian fit for each  
 601  $p_T$  bin:

602 The following 2 plots demonstrate the fit for the width function in p+p and p+Au collisions:



## 5.9.2 Procedure of Additional Smearing

In embedding, the fit parameter  $a$  in the width function is varied to construct the additional smearing:  $a$  is varied to  $a' = a \times (1 + iStep \times 0.03)$  while  $b$  is kept the same in  $f(p_T) = \sqrt{(ap_T)^2 + b^2}$  ( $iStep = 0, 1, 2, \dots, 99$ ). The new  $f'(p_T)$  represents a new momentum resolution as a function of MC  $p_T$ . Therefore,

$$\frac{f'(p_T)}{f(p_T)} = \frac{\frac{p_T^{RC'} - p_T^{MC}}{p_T^{MC}}}{\frac{p_T^{RC} - p_T^{MC}}{p_T^{MC}}} = \frac{p_T^{RC'} - p_T^{MC}}{p_T^{RC} - p_T^{MC}}, \text{ yielding } p_T^{RC'} = \frac{f'(p_T)}{f(p_T)} \times p_T^{RC} + (1 - \frac{f'(p_T)}{f(p_T)}) \times p_T^{MC}, \text{ where } p_T^{RC'} \text{ is}$$

assigned to be the additional smeared RC  $p_T$ , whenever the original  $p_T^{RC}$  presents, both in embedding and EvtGen. I.e., the EID efficiencies and the smearing templates of 3 types (TRG, NTR, All) of electrons will obtain dependence on **iStep**. As a result, the RC  $J/\psi$  in embedding as well as in EvtGen also depend on **iStep**, and **iStep=0** corresponds to “no additional smearing”.

### 5.9.3 Optimization of Parameter $a$

The  $J/\psi$  mass resolution is influenced by the momentum resolution. Therefore, one can attempt to match the RC mass distribution to the real data while varying  $a'(iStep)$ . The optimized  $a'(iStep)$  is defined to be the one provides most consistency RC mass distribution. The exact approach is described below:

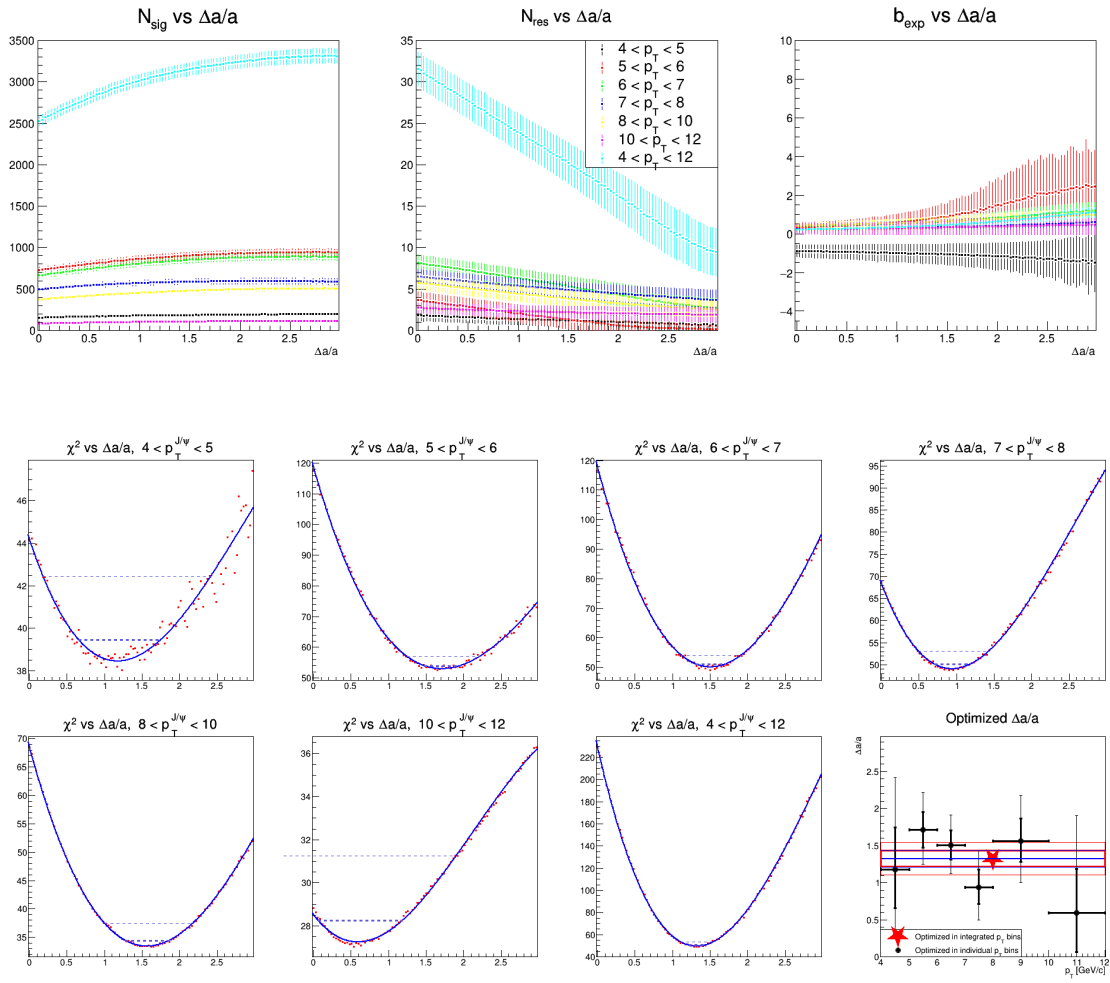
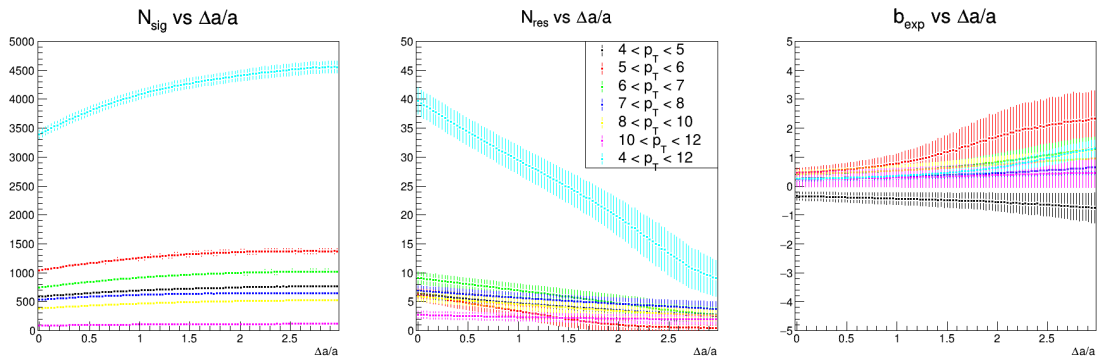
- 0) Generate the templates at different  $a'(iStep)$ ,  $iStep = 0, 1, 2, 3, \dots, 99$
  - 1) Conduct a series of “Signal Extraction” with each templates from step 0)
  - 2) Record the fit  $\chi^2$  as a function of  $\frac{\Delta a}{a} = iStep \times 0.03$ . The  $\chi^2$  describes how well the simulation is consistent with data
  - 3) Fit the  $\chi^2$  vs  $\frac{\Delta a}{a}$  to a 4<sup>th</sup> order polynomial function in order to avoid fluctuations
  - 4) Find the minimum of the fit function  $\chi_{min}^2$  and corresponding  $(\frac{\Delta a}{a})_{min}$  in range
  - 5) Use the closest integer to  $(\frac{\Delta a}{a})_{min}$  obtained in the 4) to be the optimized  $(\frac{\Delta a}{a})_{opt}$
  - 6) The lower/upper confidence interval of  $(\frac{\Delta a}{a})_{min}$  is determined by the  $x$  (or  $\frac{\Delta a}{a}$ ) coordinate of the closest intersection of  $y$  (or  $\chi^2$ ) =  $\chi_{min}^2 + z^2$  and the  $\chi^2$  fit function on the left/right side of  $(\frac{\Delta a}{a})_{min}$ , where  $z$  is the confidence level value. I.e.,  $z = 1$  in this formula has the equivalent statistical significance with  $1\sigma$  in Gaussian. The confidence interval is assigned to be an asymmetric uncertainty.
- $(\frac{\Delta a}{a})_{min}$  as well as the uncertainties are obtained in individual  $p_T$  bins and the  $p_T$  integrated bin.  $z = 1, 2$  are both calculated, represented by thin and thick error bars (boxes) for the individual  $p_T$  bins ( $p_T$  integrated bin)

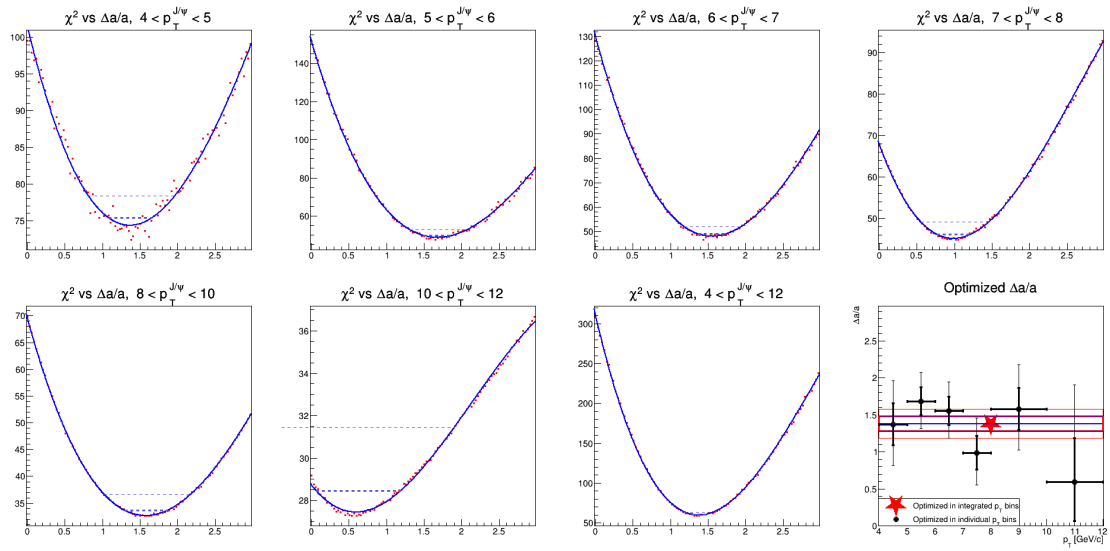
The fit result of the parameters are also monitored by looking at the fit parameters ( $N_{Sig}$ ,  $N_{Res}$ ,  $b_{exp}$ ) vs  $\frac{\Delta a}{a}$ . Intuitively, they should present themselves as continuous functions.

$N_{Sig}$ ,  $N_{Res}$ ,  $b_{exp}$  vs  $\frac{\Delta a}{a}$  and  $\chi^2$  vs  $\frac{\Delta a}{a}$  are shown as below:

**p+p**

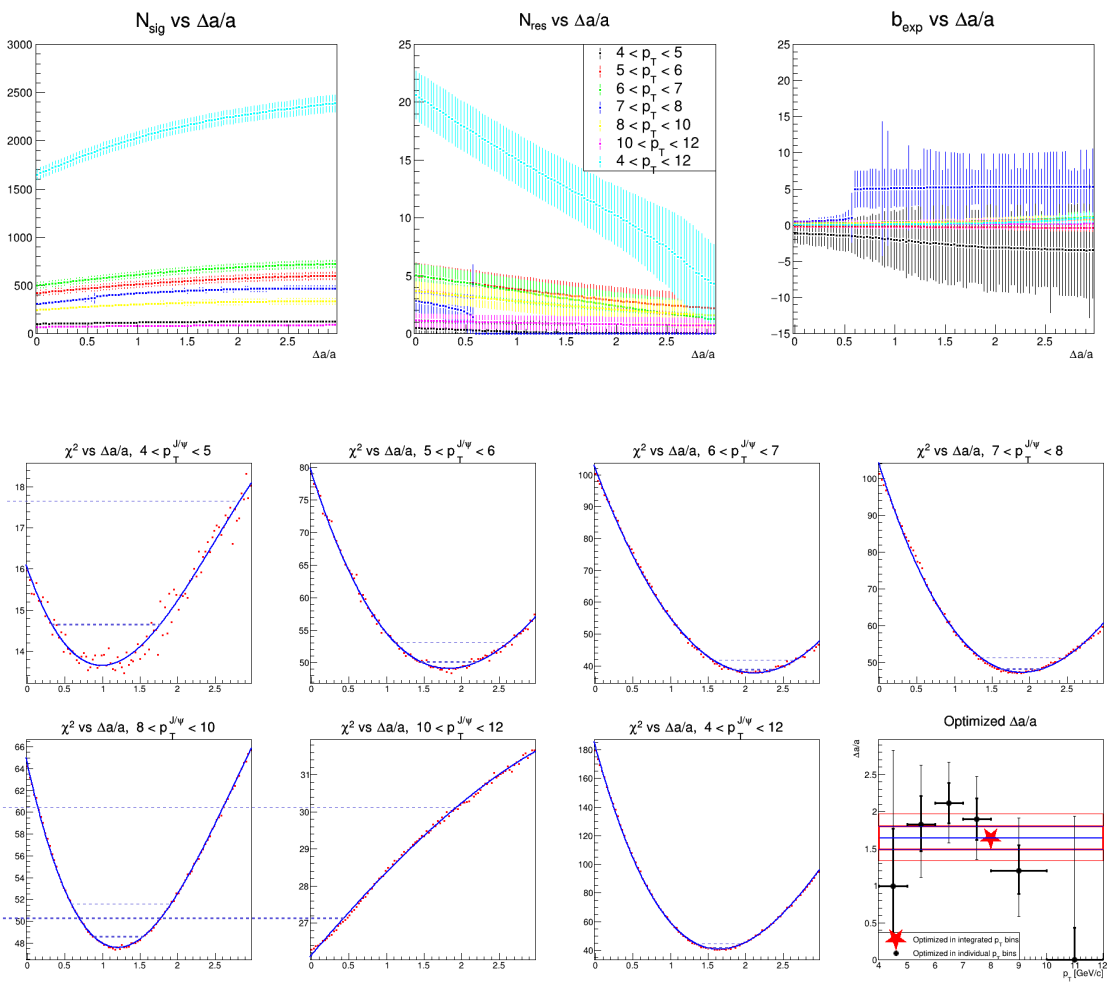


Trigger  $p_T = 4.3 \text{ GeV}/c$ Trigger  $p_T = 3.5 \text{ GeV}/c$ 

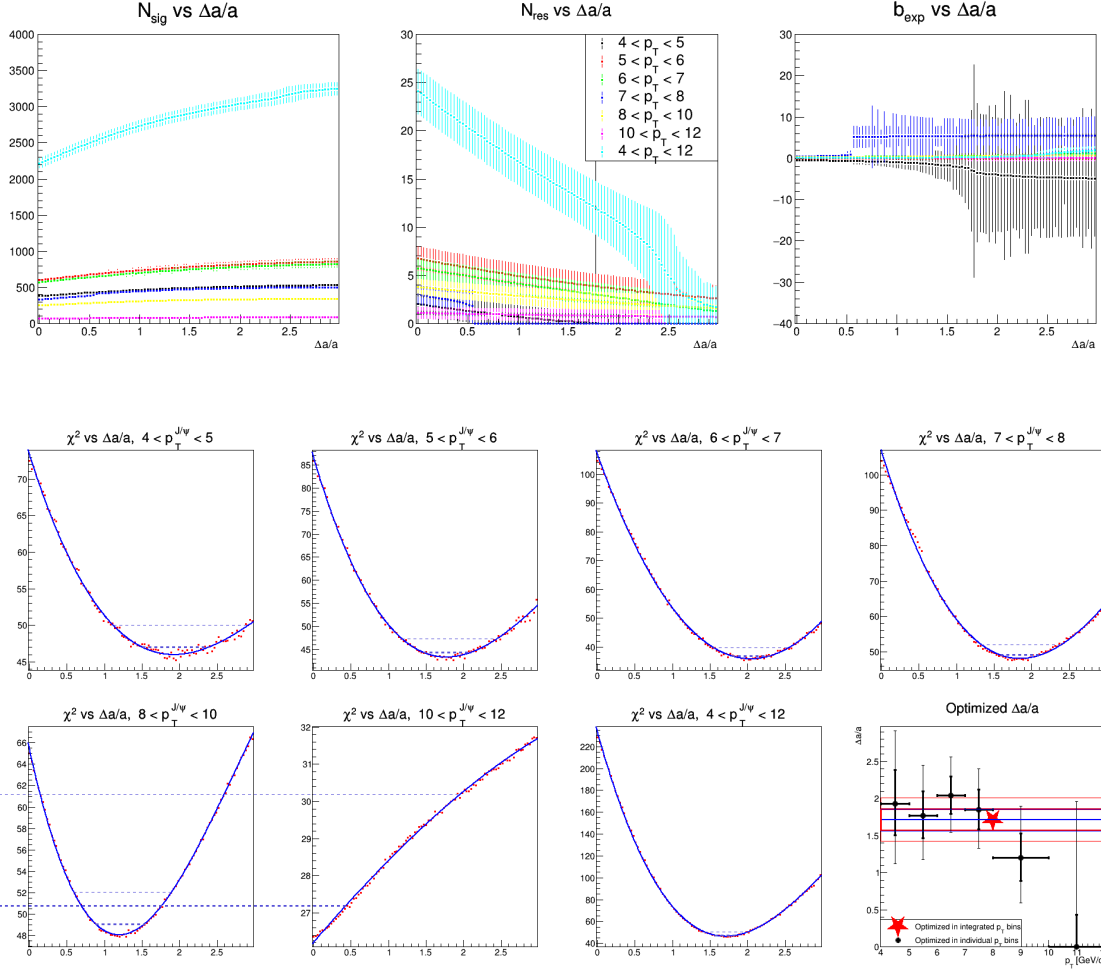


638 **p+Au**

639 **Trigger  $p_T = 4.3$  GeV/c**



640 **Trigger  $p_T = 3.5$  GeV/c**



641  $(\frac{\Delta a}{a})_{opt}$  vs  $p_T$  is statistically flat, and consistent with the one with the  $p_T$  integrated one. Therefore  
 642 the  $p_T$  integrated  $(\frac{\Delta a}{a})_{opt}$  is used as the optimized parameter without  $p_T$  dependence. Then in each  
 643 individual  $p_T$  bins, with the  $p_T$  integrated  $(\frac{\Delta a}{a})_{opt}$ , the  $J/\psi$  RC efficiency with additional smearing can  
 644 be calculated, and the raw yield extracted by templates with additional smearing is picked out from the  
 645 series of “Signal Extraction” result in 1).

## 646 5.10 Physics Results

647 With the raw yield extracted by templates with additional smearing,  $J/\psi$  RC efficiency with additional  
 648 smearing, one can calculate the physics results of this analysis. The physics results include the differential  
 649 cross section in p+p collisions, the invariant yield in p+Au collisions, and the nuclear modification factor  
 650  $R_{extpA}$ .

### 651 5.10.1 The Differential Cross Section in p+p Collisions and the Invariant Yield p+Au 652 Collisions

653 As a reminder, the electron trigger  $p_T$  cut used to reconstruct  $J/\psi$  for calculating the p+p cross  
 654 section and p+Au invariant yield is 4.3 GeV/c.

655 Recap: the  $p_T$  differentiated yield per unit rapidity is calculated by the following formula:

$$656 \frac{d^2 N}{dp_T dy} = \frac{1}{\Delta p_T \Delta y} \cdot \frac{1}{N_{MB}^{eqv} \epsilon_{MB}^{gvtx}} \cdot \frac{\epsilon_{MB}^{BBC} \epsilon_{MB}^{gvtx}}{\epsilon_{J/\psi}^{BBC} \epsilon_{J/\psi}^{gvtx}} \cdot \frac{N_{J/\psi}^{raw}}{\epsilon_{J/\psi}^{RC}}$$

657 where:  
 658

- 659  $\Delta y = 2$  corresponds to the rapidity acceptance  $|y| < 1$
- 660  $N_{MB}^{eqv}$  is the equivalent number of MB events
- 661  $\epsilon_X^{gvtx}$  is the good vertex efficiency of X (X = MB,  $J/\psi$ )

662  $\frac{\epsilon_{MB}^{BBC} \epsilon_{MP}^{gvtx}}{\epsilon_{J/\psi}^{BBC} \epsilon_{J/\psi}^{gvtx}}$  is the trigger bias factor, in which  $\epsilon_X^{BBC}$  is the beam-beam counter efficiency of X (X =  
663 MB, J/ $\psi$ )  
664  $N_{J/\psi}^{raw}$  is the raw yield of J/ $\psi$   
665  $\epsilon_{J/\psi}^{RC}$  is the J/ $\psi$  reconstruction efficiency  
666

667  **$p_T$  Position Determination** Due to the nature of binned data, the choice of  $x$  being equal to the  
668 bin center and substituting this value to calculate  $\frac{d^2N}{dp_T dy}$  is an approximation.  $\frac{d^2N}{dp_T dy}$  is chosen to be held  
669 untouched while a  $p_T$  shift technique is applied, in which a shifted  $p'_T$  is assigned to be  $x$  coordinate in  
670 order to make the integral of  $f(p_T)$  equals the product of bin width and  $f(p'_T)$  in each  $p_T$  bin, where  
671  $f(p_T)$  is an empirical fit function of  $\frac{d^2N}{dp_T dy}$  vs  $p_T$ . The  $p_T$  shift is conducted in an iterative manner as  
672 described below:

673 0) The starting point is the set of uncorrected  $p_T$ , denoted by  $S_0 = \{p_{T,0}^{(n_{bin})} | n_{bin} = 0, 1, 2, 3, 4, 5\}$   
674 where  $n_{bin}$  is the bin index. The uncorrected  $p_T$  is simply the bin center of each  $p_T$  bin.

675 1) In the  $i^{th}$  iteration ( $i = 1, 2, 3, 4, \dots$ ), use  $S_{i-1} = \{p_{T,i-1}^{(n_{bin})} | n_{bin} = 0, 1, 2, 3, 4, 5\}$  as the  $x$  coordinates  
676 in  $(p_T, \frac{d^2N}{dp_T dy})$ . Fit the set of points  $\{(p_T, \frac{d^2N}{dp_T dy})\}$  to  $f(p_T) = N \cdot p_T \cdot (1 + (\frac{p_T}{A})^2)^{-n}$ . This essentially  
677 maintains the integrated yield in this  $p_T$  bin invariant. The resulting function in this iteration is denoted  
678 by  $f_i(p_T)$ .

679 2) Solve for the root of  $p_{T,i}^{n_{bin}}$  in the equation below in each  $p_T$  bin:

$$680 \int_{l(n_{bin})}^{h(n_{bin})} f_i(p_T) dp_T = Width(n_{bin}) \cdot f_i(p_{T,i}^{(n_{bin})})$$

681 where  $l(n_{bin})$ ,  $h(n_{bin})$  and  $Width(n_{bin})$  is the lower bound, higher bound and bin width of the  $p_T$  bin  
682 with index  $n_{bin}$ . This constructs a map from  $p_{T,i-1}^{n_{bin}}$  towards  $p_{T,i}^{n_{bin}}$

683 3) Loop over step 1) and 2), until the resulting fit function is consistent with the previous iteration.  
684 The criteria is arbitrary, but set to “all parameters and their fit errors are identical up to 6 digits”.  
685 Denote this iteration has an index of  $i = N$

686 4) The procedure converges in the iteration of  $i = N - 1$ , therefore  $S_{N-1} = S_k, \forall k > N - 1, k \in \mathbb{Z}$  is  
687 the set of shifted  $p_T$  assigned.

688 The shifted  $p_T$  values in each  $p_T$  bin are listed in the following table.

689 The first 2 columns are obtained with the electron trigger  $p_T$  cut at 4.3 GeV/c. These 2 columns  
690 participate in the calculations of the final physics results of the differential cross section in p+p collisions  
691 and the invariant yield in p+Au collisions.

692 Such values were also extracted with the electron  $p_T$  cut at 3.5 GeV/c, but not shown in this table.  
693 Similar to the 4.3 GeV/c case, for the 3.5 GeV/c case the difference in the  $p_T$  position between p+p and  
694 p+Au is negligible. Therefore when calculating  $R_{eXtPA}$ , the  $1/p_T$  term, which converts the yield into  
695 invariant yield, is considered to cancel out after taking the p+Au/p+p ratio. The arithmetic average of  
696 the  $p_T$  positions in p+p and p+Au and are the assigned to be the visual  $p_T$  positions.  
697  
698

Assigned $p_T$ [GeV/c]			
$p_T$ Range [GeV/c]	p+p	p+Au	$R_{eXtPA}$
4 - 5	4.44182	4.44449	4.44745
5 - 6	5.44484	5.44643	5.44802
6 - 7	6.44896	6.44987	6.45060
7 - 8	7.45312	7.45361	7.45379
8 - 10	8.83719	8.83778	8.83684
10 - 12	10.86037	10.86004	10.85800

699 **Calculate the Invariant Yield** The invariant yield is calculated by the following formula:

$$700 \frac{d^2N}{2\pi p_T dp_T dy} = \frac{d^2N}{dp_T dy} \cdot \frac{1}{2\pi p_T}$$

701 where  $p_T$  on the right hand side is the shifted  $p_T$  assigned in the table above. For p+p collisions, the  
702

703 invariant yield is converted into differential cross section by multiplying the non-single diffractive (**NSD**)  
 704 cross section in p+p collisions  $\sigma_{pp}^{NSD} = 30.0 \pm 2.4 mb$  at 200 GeV:

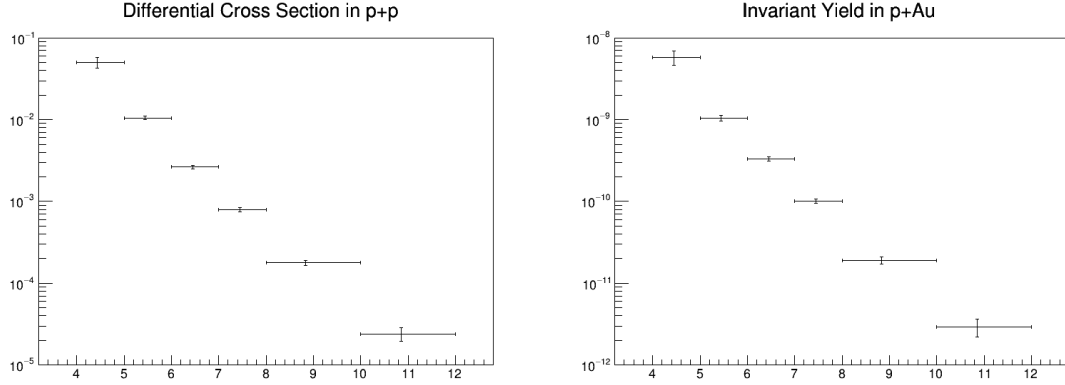
705

$$\frac{d^2\sigma}{2\pi p_T dp_T dy} = \frac{d^2N}{2\pi p_T dp_T dy} \cdot \sigma_{pp}^{NSD}$$

706

707 The following plots show the differential cross-section in p+p and the invariant yield in p+Au collisions.

708



### 709 5.10.2 Nuclear Modification Factor $R_{e\psi pA}$

710 The nuclear modification factor is calculated with the following formula:

711

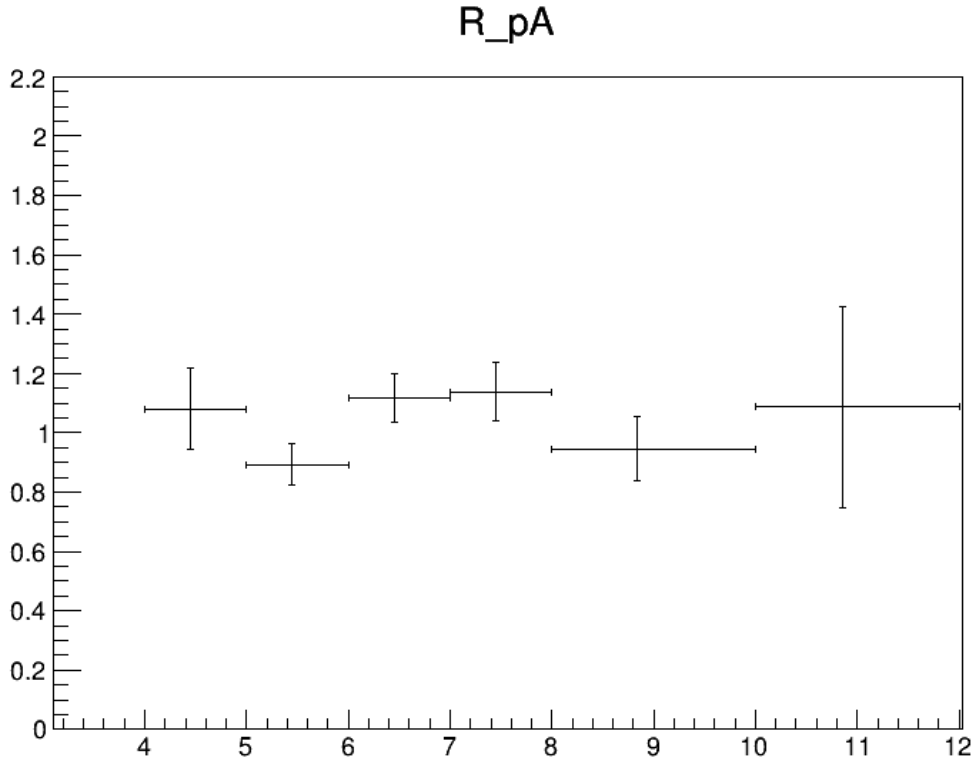
$$R_{e\psi pA} = \frac{1}{\langle N_{coll} \rangle / \sigma_{pp}^{inel.}} \cdot \frac{(\frac{d^2N}{2\pi p_T dp_T dy})_{e\psi pA}}{(\frac{d^2\sigma}{2\pi p_T dp_T dy})_{pp}}$$

712

713 where  $\sigma_{pp}^{inel.} = 42 mb$  is the inelastic cross-section of nucleon-nucleon collisions at 200 GeV in p+p collisions,  
 714 and  $\langle N_{coll} \rangle = 4.7 \pm 0.3$  is the average number of binary nucleon-nucleon collisions.

715 As a reminder, the electron trigger  $p_T$  cut used to reconstruct  $J/\psi$  for calculating the  $R_{e\psi pA}$  is 3.5  
 716 GeV/c. Therefore, the cross section in p+p collisions and invariant yield in p+Au collisions used to  
 717 calculate  $R_{e\psi pA}$  are different from their stand-alone physics result. The resulting  $R_{e\psi pA}$  is shown  
 718 as below:

719



## 6 Systematic Uncertainties

The systematic uncertainty is estimated separately for the three physics results: p+p cross section, p+Au invariant yield, and  $R_{extpA}$ , but they estimated in a same way.

Four aspects are included in the systematic uncertainties and each of them will be discussed:

1. Tracking
2. Electron identification
3. Electron triggering
4. Raw yield extraction

The contributions from them are assumed to be uncorrelated with each other.

### 6.1 Treatment of Undersampling

Each contribution of the systematic uncertainty is estimated by varying cut(s) or parameter. One can reconstruct  $J/\psi$  with the varied cut(s) or parameter and calculate the corresponding varied physics result. The systematic uncertainty contribution is related to the difference between the default physics result and each one of the varied results. In this analysis, some cut(s) only has one of variation. In this case, if the deviation is smaller than the quadrature difference between the statistical uncertainty of the default physics result and the varied one, this contribution is assigned to be 0 due to the fact that the deviation is suppressed by and most likely due to statistical fluctuation.

### 6.2 Independent Contribution from Each of the 4 Aspects

Details of each contribution is discussed.

**1. Tracking** The tracking quality cuts could be highly correlated. Therefore, three tracking quality cuts (nHitsFit, nHitsDedx, and DCA) are varied simultaneously in order to avoid any overestimation. There's only 1 set of variation and the undersampling is considered.

745 **2. Electron identification** The 2 electron identification cuts are selections by 2 independent de-  
 746 tector subsystems. Therefore the related 2 cuts ( $n\sigma_e$  and  $e/p$ ) are varied separately. One variation is  
 747 conducted to each cut and undersampling is considered for each of them. The total contribution from  
 748 electron identification is the quadrature sum of the 2.

749

750 **3. Electron triggering** It is independent from other factors. One ( $Adc0$ ) of the related cuts is  
 751 varied to a single variation and undersampling is considered.

752

753 **4. Raw yield extraction** The raw yield is extracted by a fit procedure. The fit range, the  
 754 integral mass window cut, the mass bin width, the fit function of contribution of residual background,  
 755 and how the signal integral is calculated (“semi bin-counting” or “fit integral”), are arbitrarily chosen.  
 756 The arbitrariness of these factors as well as the uncertainty of the additional smearing parameter cover the  
 757 “raw yield extraction” aspect of systematic uncertainty. They are assumed to be correlated.

758 The fit range has 4 variations.

759 The mass window cut has 4 variations.

760 The mass binning and the form of the form of the fit function of the residual background contribution  
 761 has 1 variation each, separately.

762 In terms of the signal integral, pure bin counting itself is an 0-biased and 0-variance estimator when  
 763 no background presents. In our case, one can either integrate over the signal contribution in the fit  
 764 function (fit integral), or integrate over the signal+background histogram and subtract the integral of  
 765 the fit function of the residual background contribution (semi bin-counting). The semi bin-counting is  
 766 chosen to be the default value under an uneducated and intuitive guess that it is less biased compared  
 767 to fit integral, nevertheless the difference between them is assigned as one of the contribution.

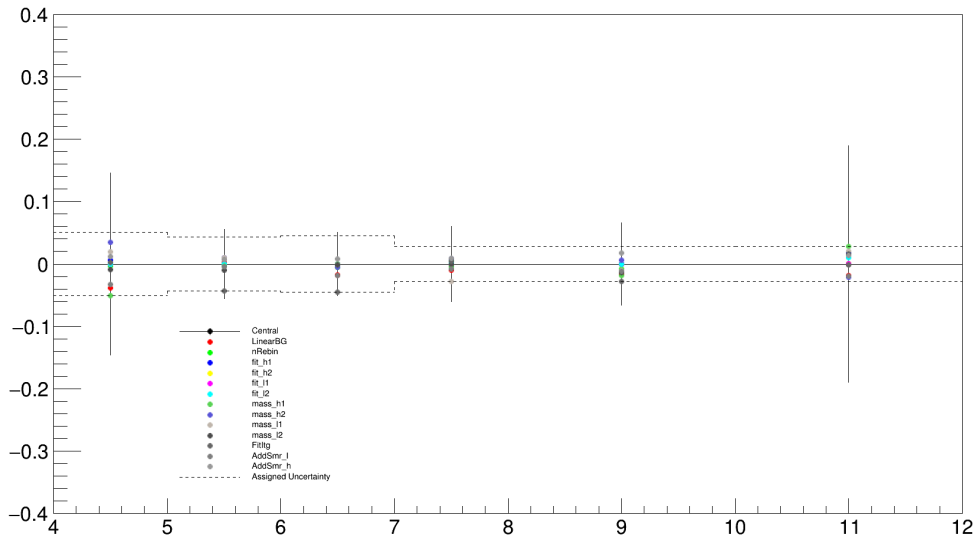
768 The optimized parameter ( $\frac{\Delta a}{a}$ ) is varied from  $(\frac{\Delta a}{a})_{opt}$  to the assigned lower and upper confidence  
 769 interval boundary at confidence level value  $z = 1$ .

770 Among the 13 correlated variations, the maximum deviation from the default value in each  $p_T$  bin is  
 771 assigned to be the total contribution from raw yield extraction as a conservative estimation.

772 The following plots show the relative deviations as a function of  $p_T$  for different variations:

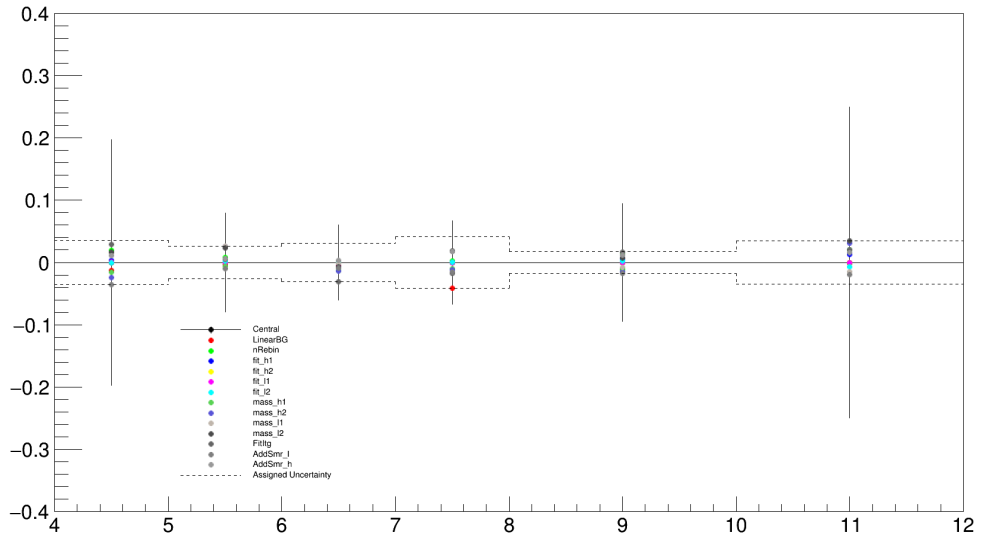
773 **p+p Cross Section**

Systematic Uncertainties from Raw Yield Extraction



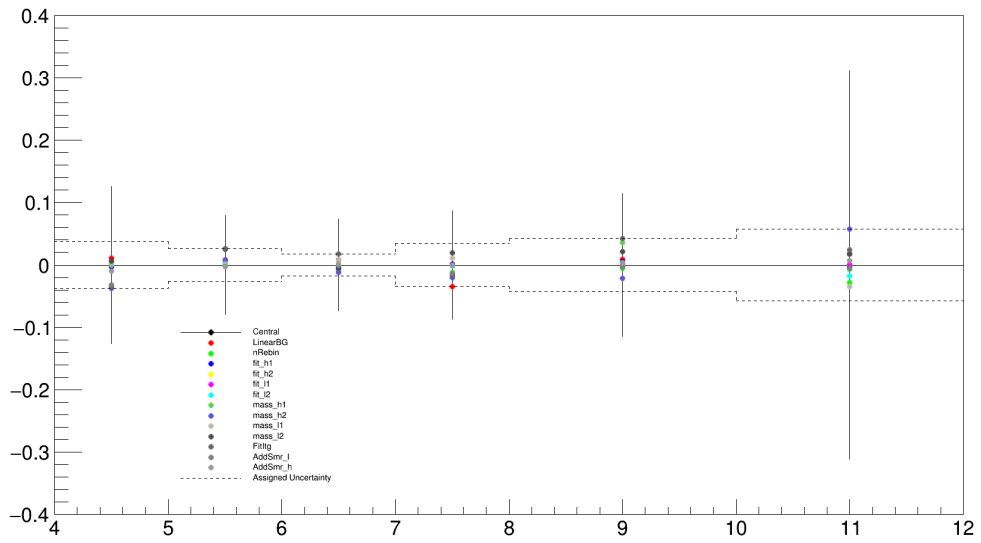
774 **p+Au Invariant Yield**

### Systematic Uncertainties from Raw Yield Extraction



775  $R_{extpA}$

### Systematic Uncertainties from Raw Yield Extraction



### 776 6.3 The Total Systematic Uncertainty

777 The total systematic uncertainty is the quadrature sum of the independent contributions from the  
 778 aforementioned 4 aspects.

779 The following is a summary table of all variations.

780

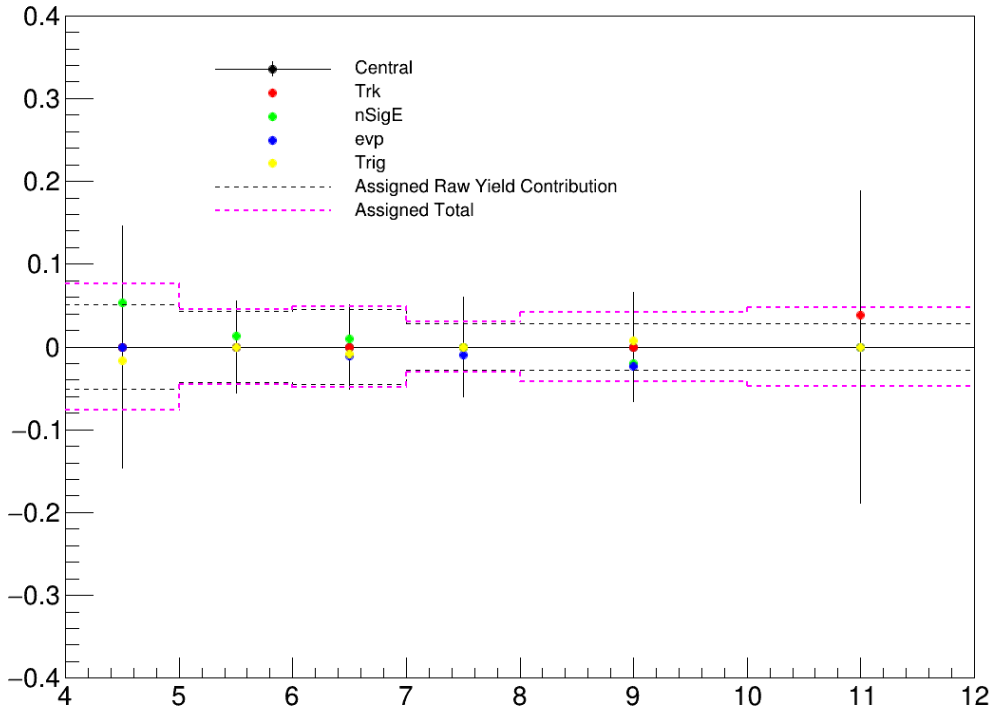


Variable Name	Default	Variation(s)
Tracking Quality (Simultaneously)		
nHitsFit	[20, $\infty$ )	[25, $\infty$ )
nHitsDedx	[10, $\infty$ )	[15, $\infty$ )
DCA	[0, 1.5)	[0, 1.4)
Electron Identification (Separately)		
$n\sigma_e$	(1.5, 2.5)	(-1.7, 2.5)
$\frac{E}{p}$	(0.5, 2.5)	(0.6, 2.4)
Electron Triggering		
Adc0	[300, $\infty$ )	[316, $\infty$ )
Raw Yield Extraction (Choose Maximum)		
Fit Range	[1.5, 4.5]	[1.5, 4.5 $\pm$ 0.05], [1.5 $\pm$ 0.05, 4.5]
Mass Window	[2.70, 3.25]	[2.70, 3.25 $\pm$ 0.05], [2.70 $\pm$ 0.05, 3.25]
Mass Bin Width	0.05 GeV/c <sup>2</sup>	0.025 GeV/c <sup>2</sup>
$f_{ResBG}(M_{e^+e^-})$	$A \cdot e^{-b \cdot M_{e^+e^-}}$	$a + b \cdot M_{e^+e^-}$
Signal Integral Method	semi bin-counting	fit integral
Parameter in Additional Smearing	$(\frac{\Delta a}{a})_{opt}$	lower and upper confidence interval limits

781 The following plots show the independent contributions and the quadrature sum as a function of  $p_T$   
782 for different variations. Note that in the EID contribution, each subject is independent from each other.  
783 Henceforth they are effectively 2 independent contributions to the total systematic uncertainty. For  
784 convenience, both of them are presented in this plot as independent contributions.

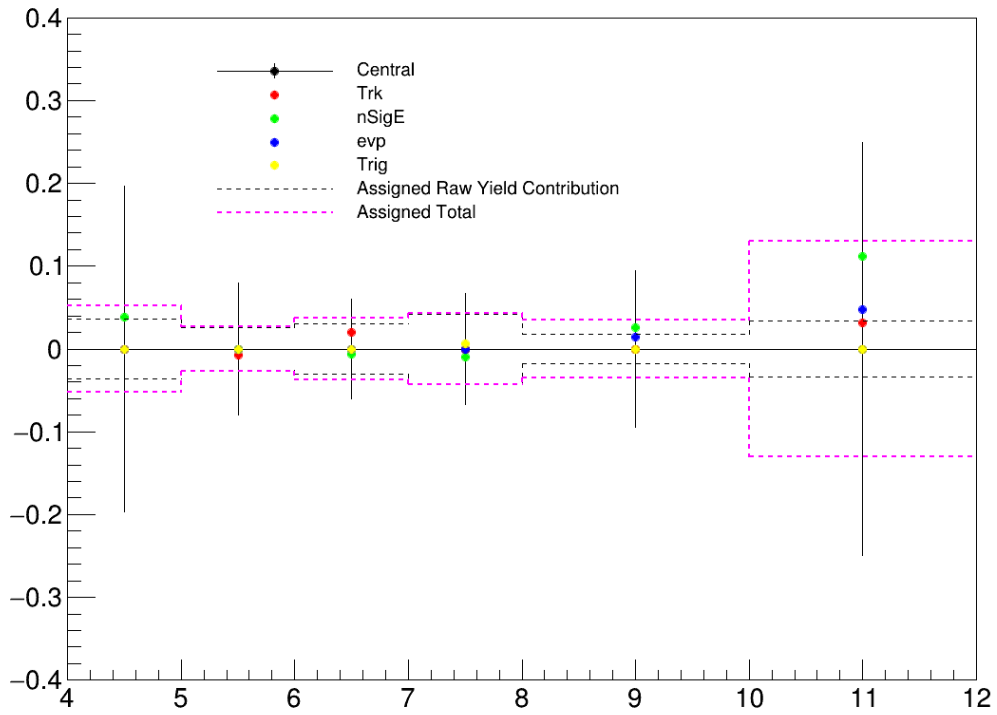
785 **p+p Cross Section**

Systematic Uncertainties from 5 Uncorrelated Aspects and the Total



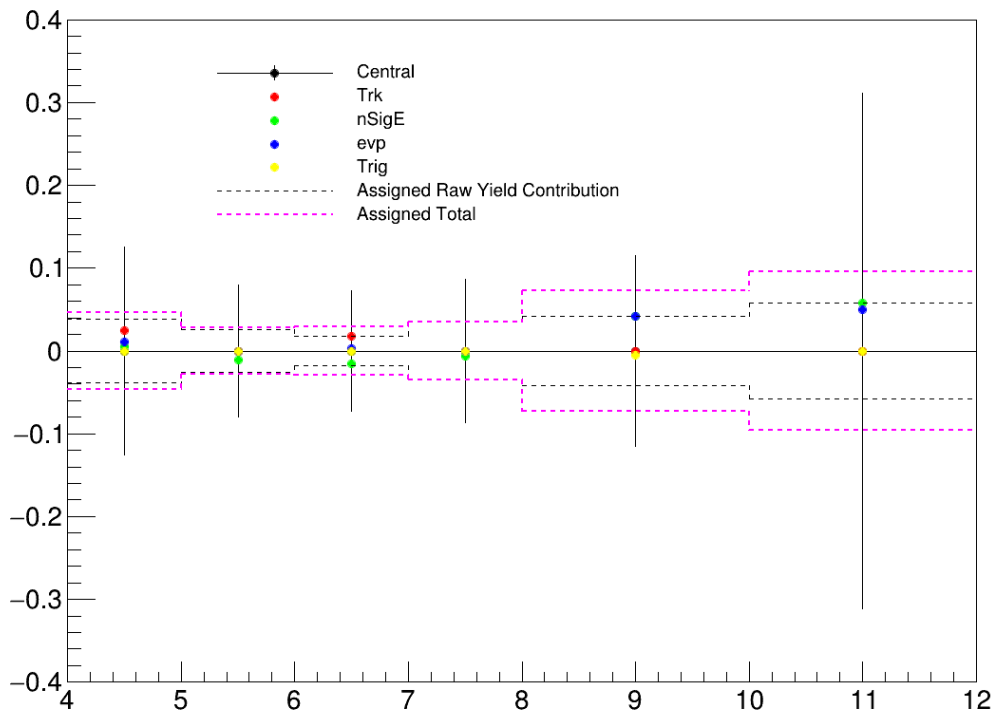
786 **p+Au Invariant Yield**

Systematic Uncertainties from 5 Uncorrelated Aspects and the Total



787  $R_{extpA}$

Systematic Uncertainties from 5 Uncorrelated Aspects and the Total



788 The three physics results (cross section in p+p collisions, invariant yield in p+Au collisions, and the  
 789  $R_{extpA}$  with error bars representing statistical uncertainty and boxes representing systematic uncer-

790 tainty are presented as follows:

791

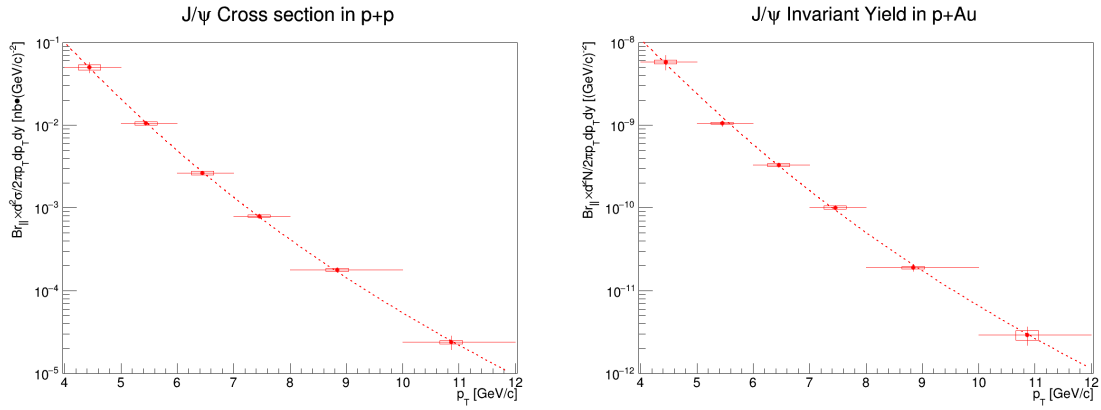


Figure 12: The dashed line is a function derived from the aforementioned fit function to the yield in p+p and p+Au,  $f(p_T) = N \cdot p_T \cdot (1 + (\frac{p_T}{A})^2)^{-n}$ , by factoring out the  $p_T$  term and multiplying the  $N$  parameter by  $\frac{\sigma_{pp}^{NSD}}{2\pi}$  and  $\frac{1}{2\pi}$ , respectively

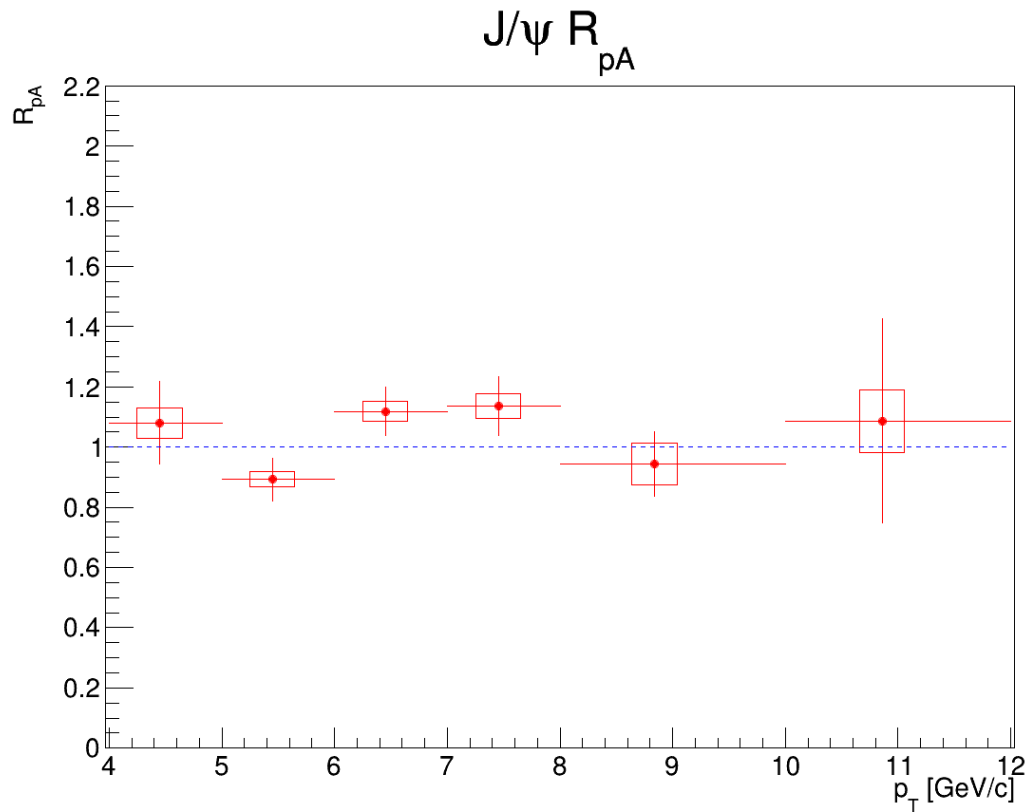


Figure 13: The blue dashed line represents unity

## 792 7 Appendices

793 Most of the appendix is temporarily removed to speed up compilation.

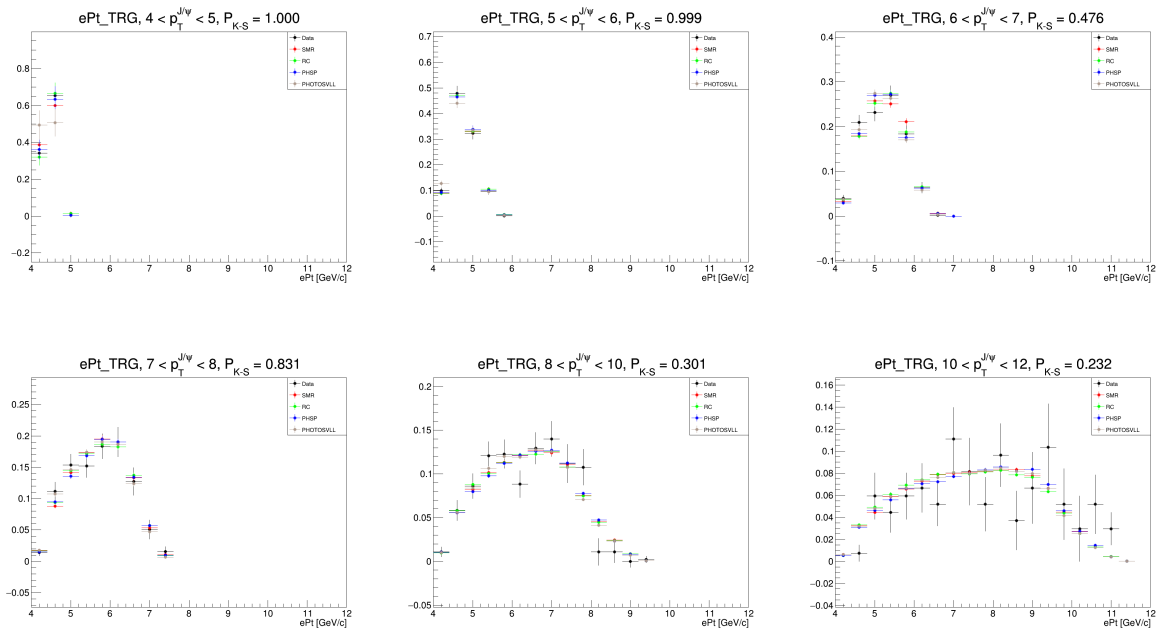
794 **7.1 Embedding QA Plots**

795 The distributions for single electrons in data are compared to those in embedding. These distributions  
 796 are corresponding to those electrons from  $J/\psi$  candidates without selection in  $J/\psi$  transverse momentum  
 797 ( $p_T$ ), rapidity ( $y$ ) or mass. The P values of Kolmogorov–Smirnov test between data and RC (original  
 798 embedding) are calculated and shown in the titles. Trigger electron and non-trigger electron are shown in  
 799 different plots. Comparisons in both p+p and p+Au collisions are made. In p+p, additional histograms  
 800 with additional smearing and folding with evtGen models are also present, as a side proof for the  
 801 rigorousness of the additional smearing procedure.

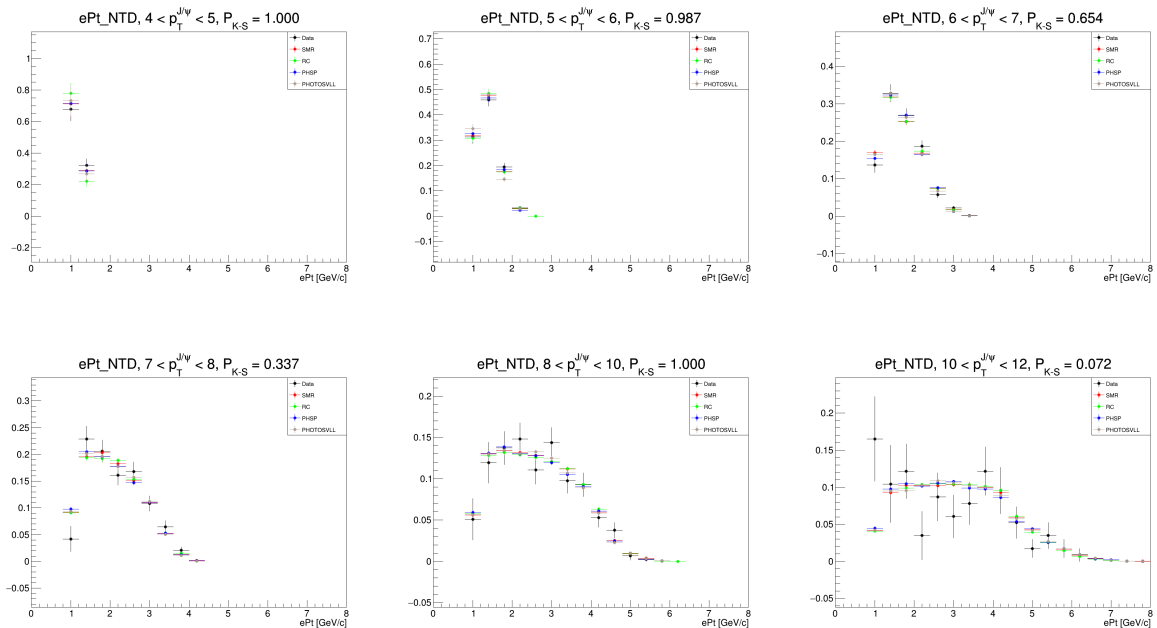
802 **Basic Kinematics**

803  $p_T$  [GeV/c<sup>2</sup>]

804 Triggered, p+p:

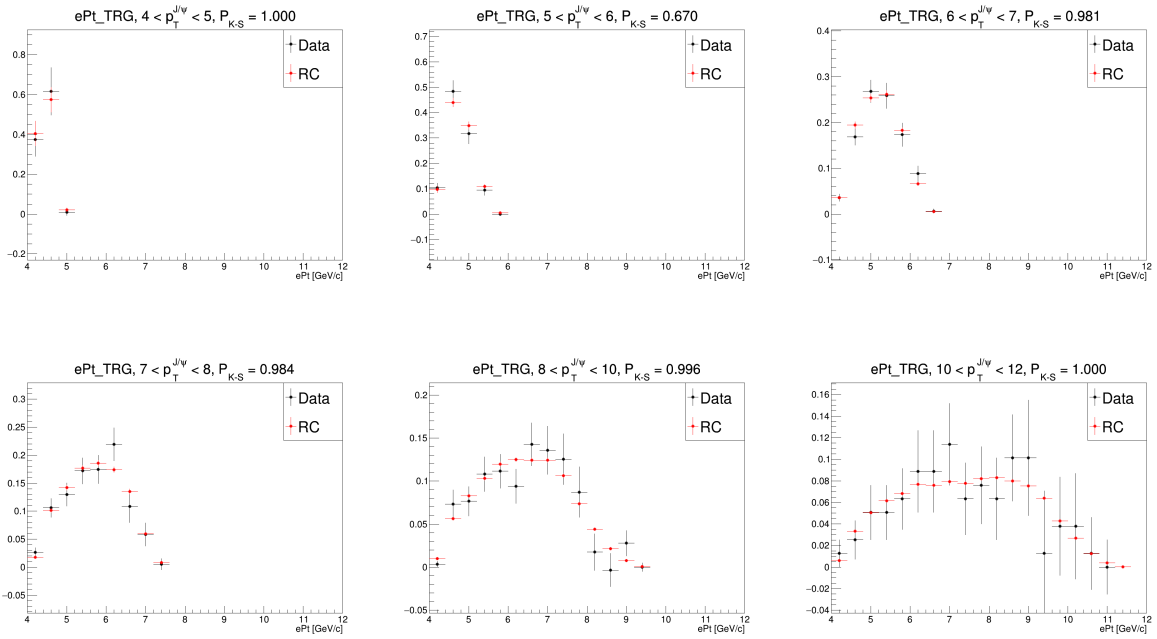


805 Non-triggered, p+p:



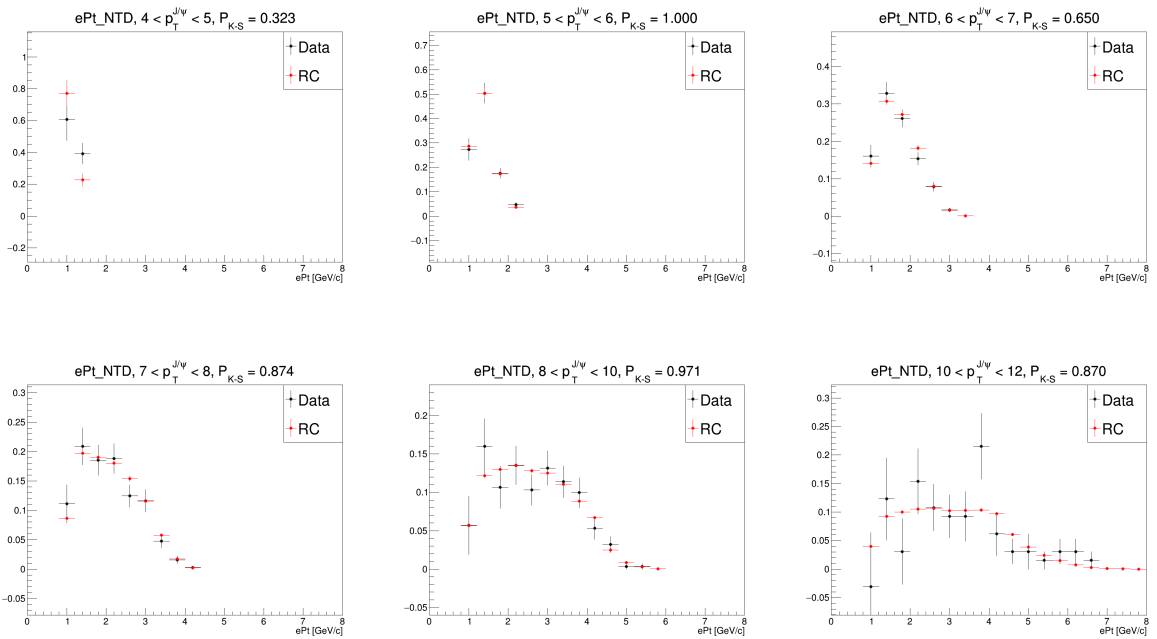
806

## Triggered, p+Au:



807

## Non-triggered, p+Au:

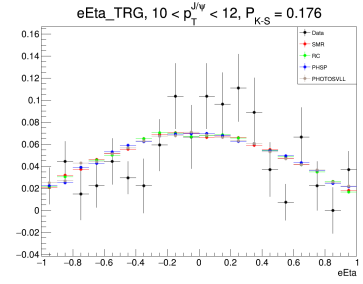
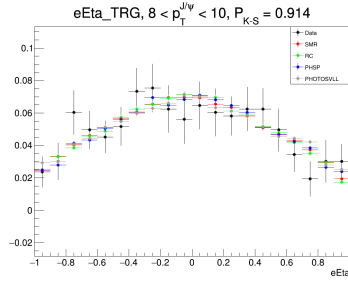
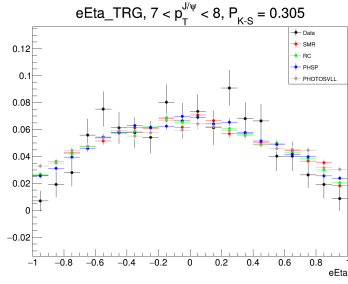
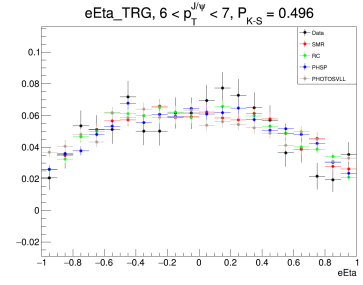
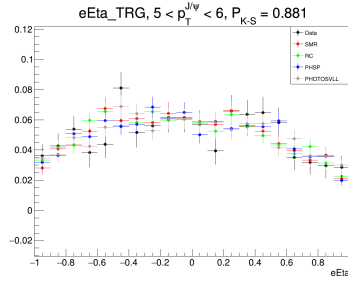
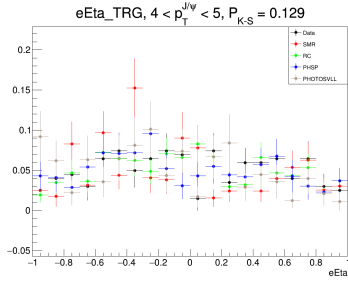


808

Pseudorapidity ( $\eta$ )

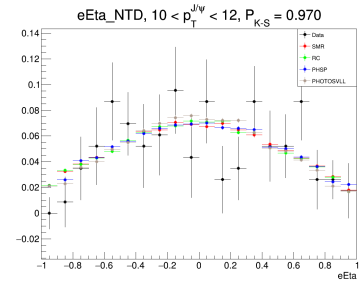
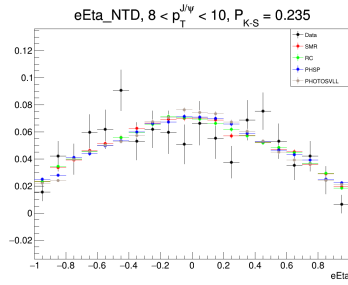
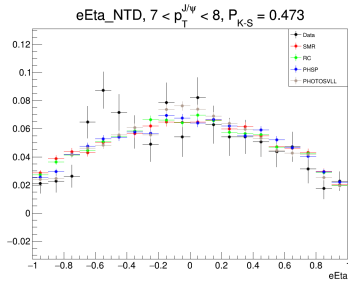
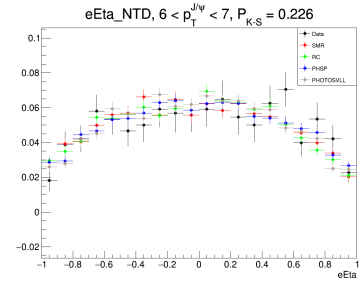
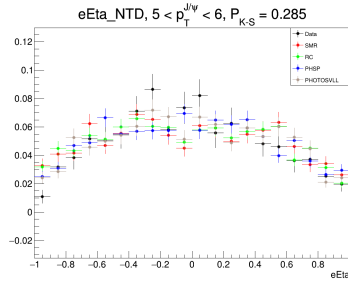
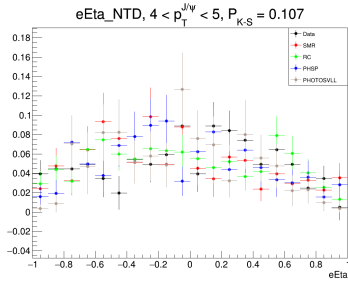
809

## Triggered, p+p:



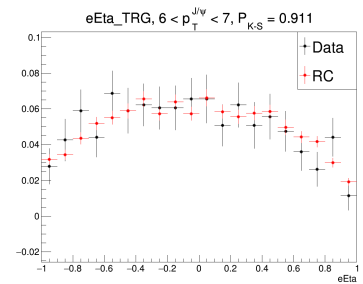
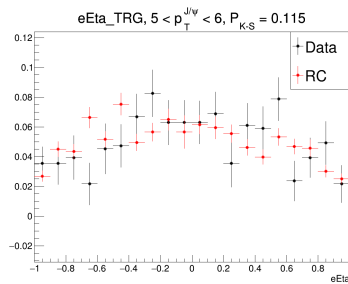
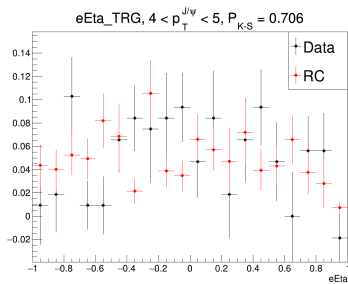
810

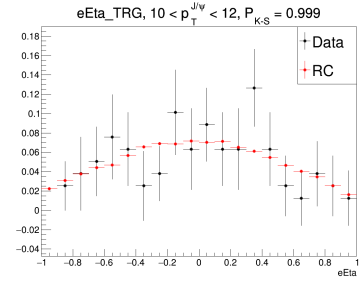
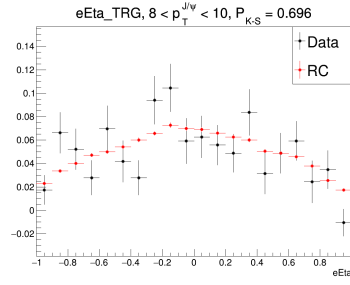
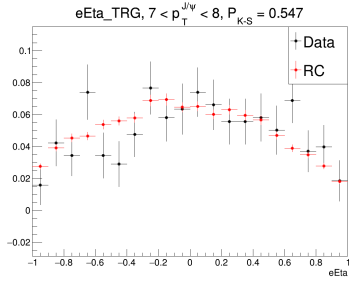
Non-triggered, p+p:



811

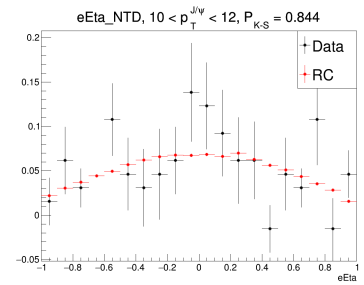
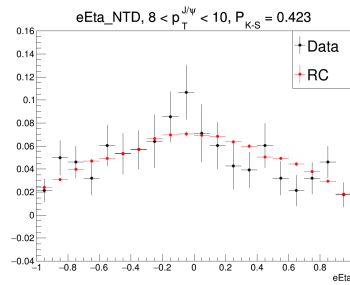
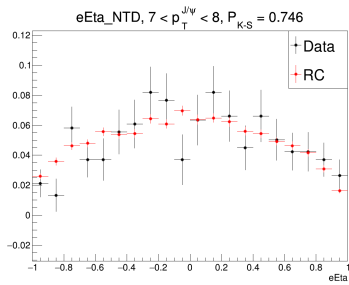
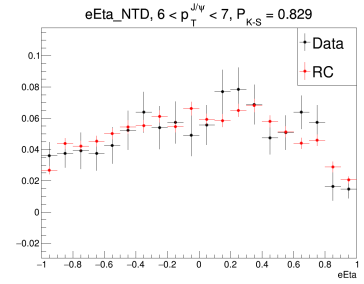
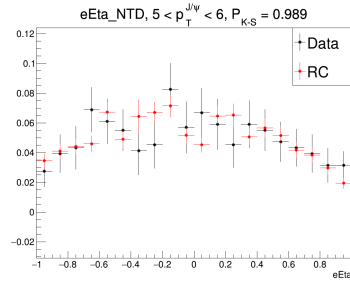
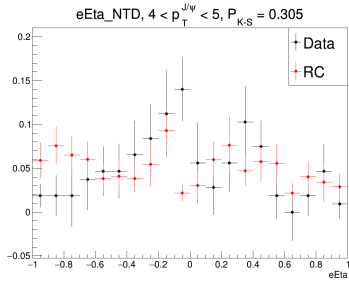
Triggered, p+Au:





812

Non-triggered, p+Au:

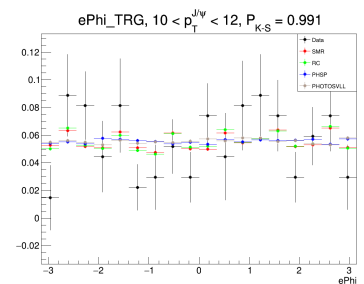
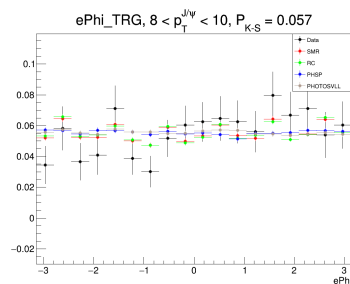
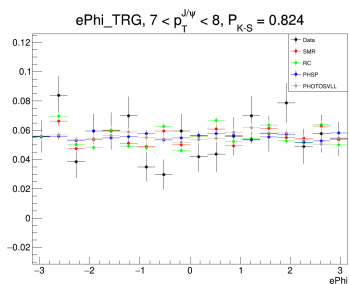
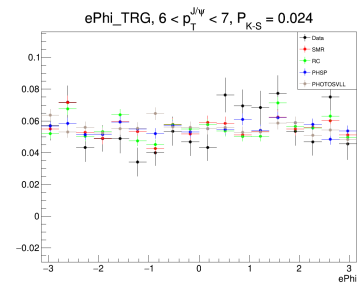
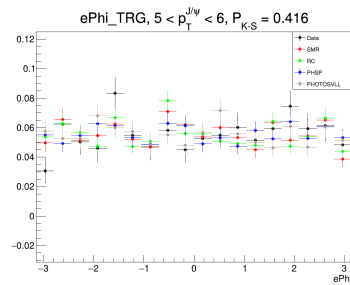
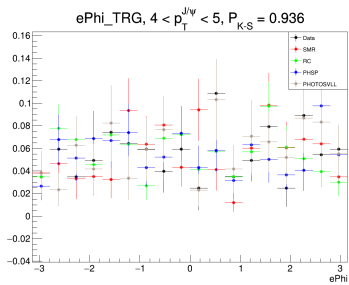


813

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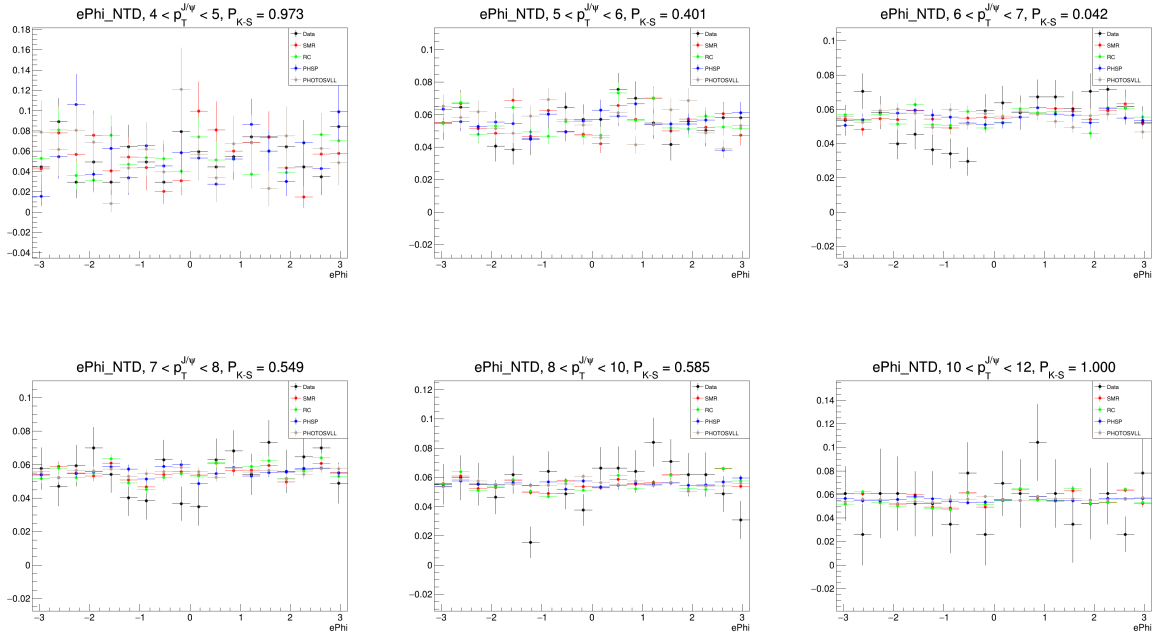
814

Triggered, p+p:



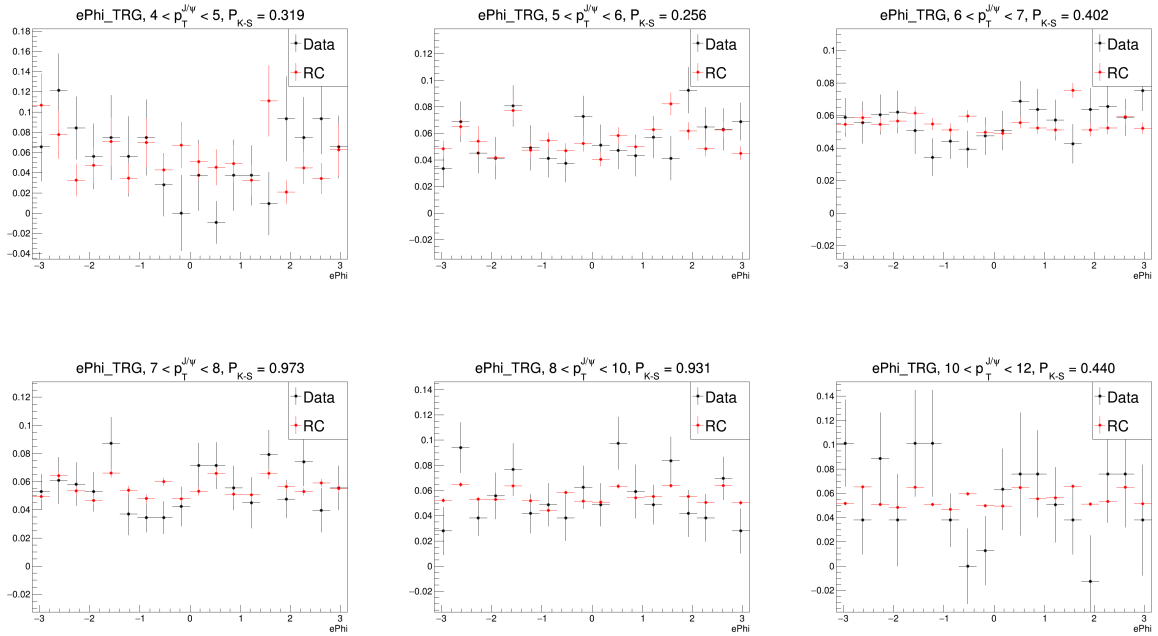
815

Non-triggered, p+p:



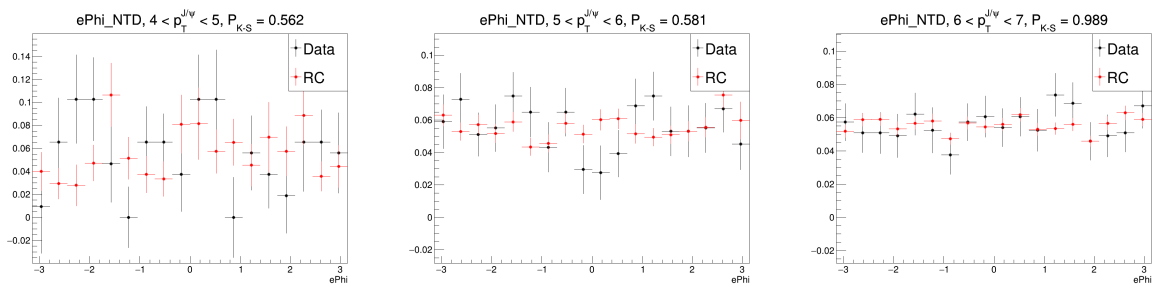
816

Triggered, p+Au:

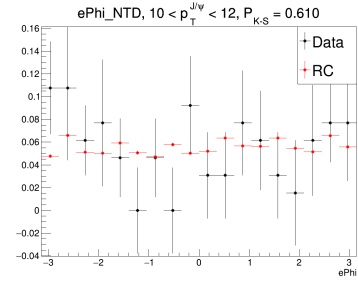
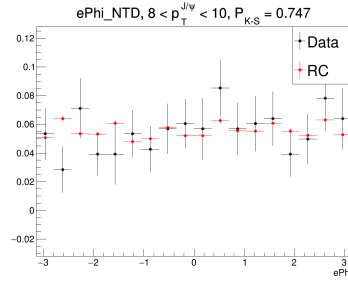
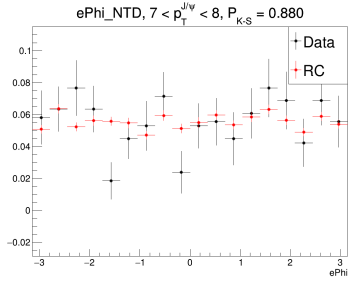


817

Non-triggered, p+Au:



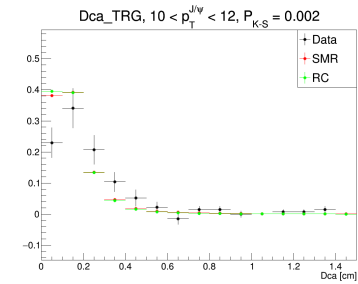
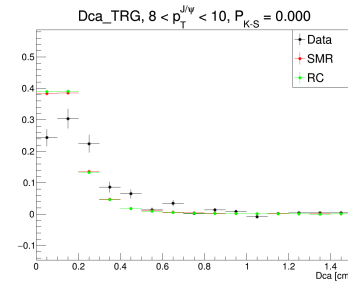
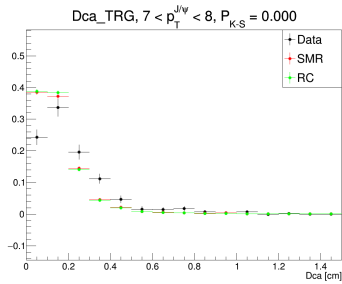
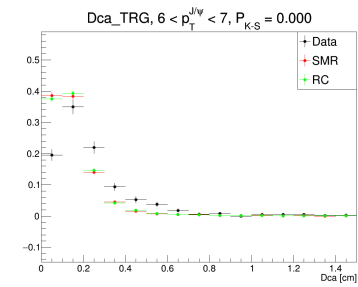
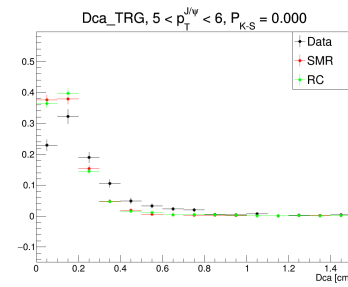
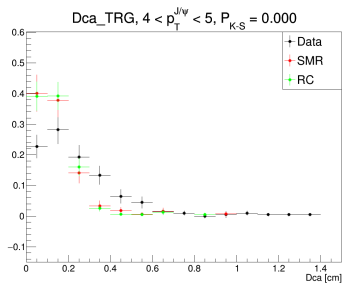




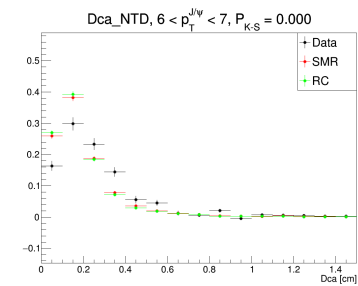
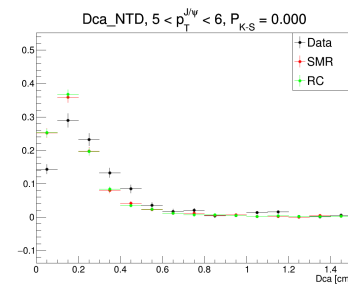
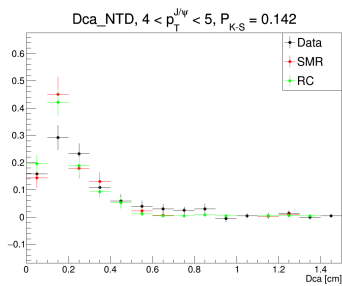
818 **Tracking Quality**

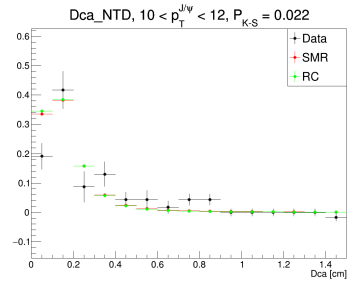
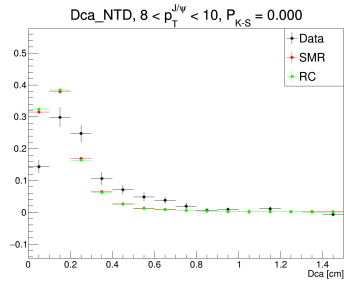
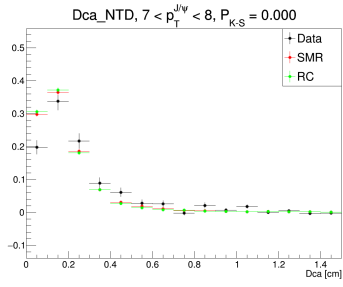
819 **Distance of Closest Approach (DCA) [cm]**

820 Triggered, p+p:



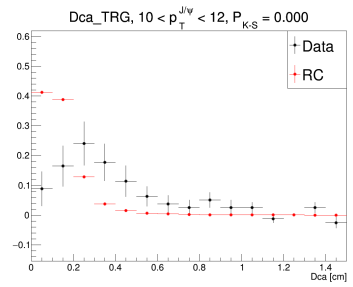
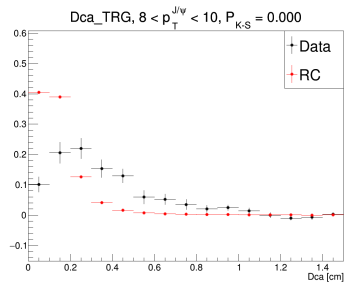
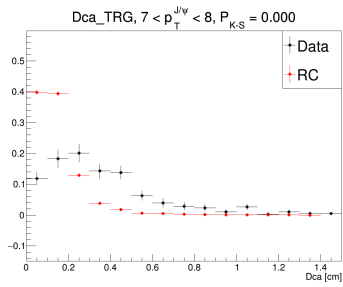
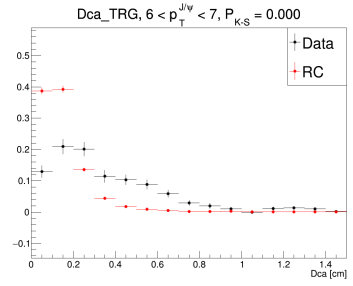
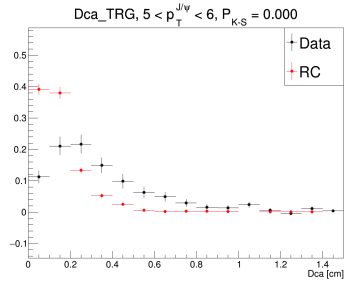
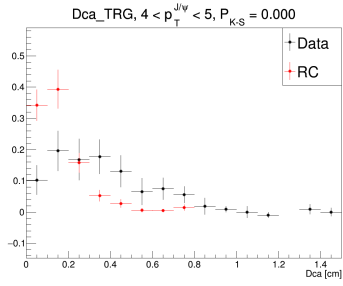
821 Non-triggered, p+p:





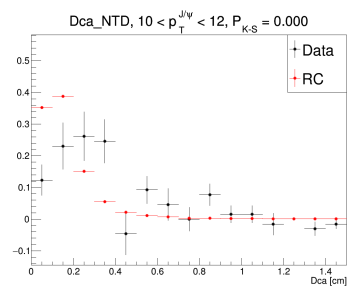
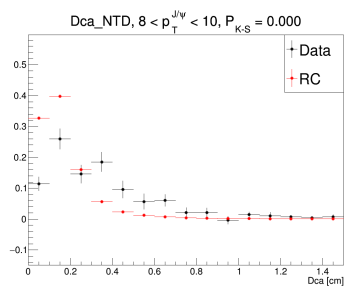
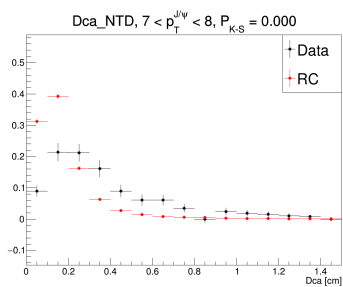
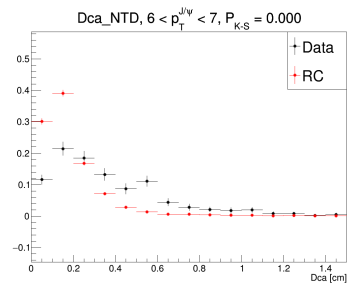
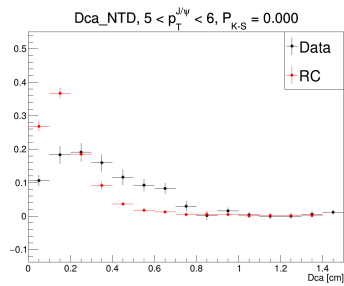
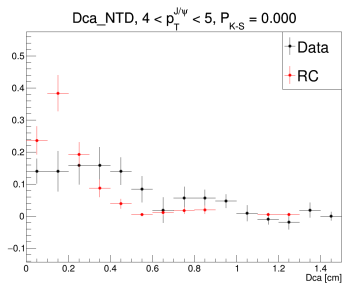
822

Triggered, p+Au:



823

Non-triggered, p+Au:

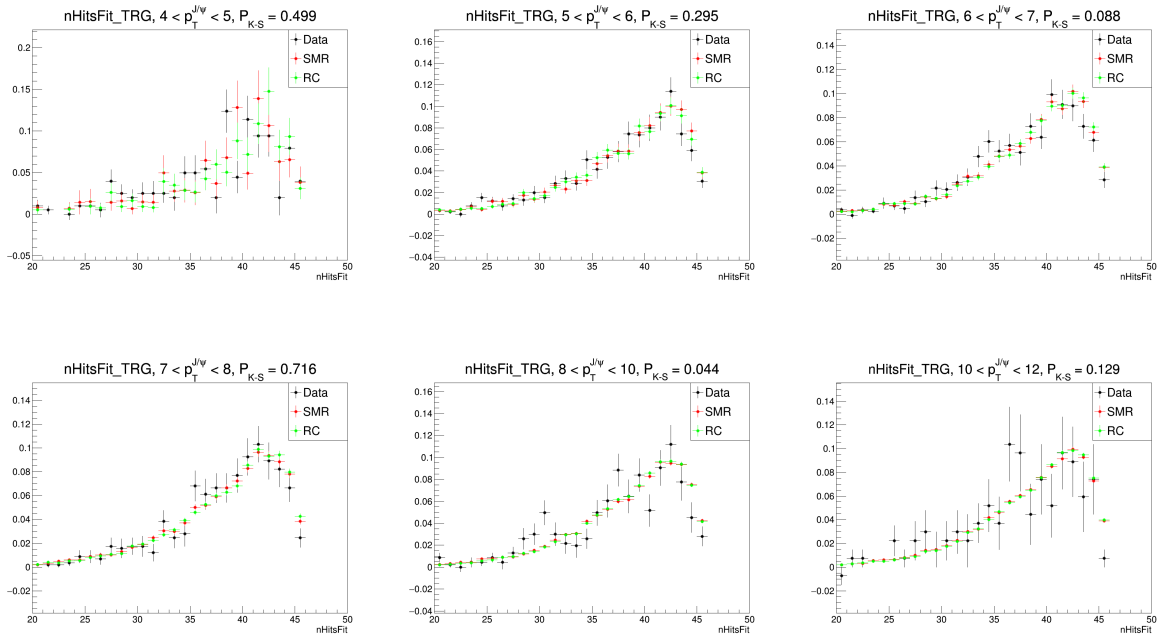


824

nHitsFit

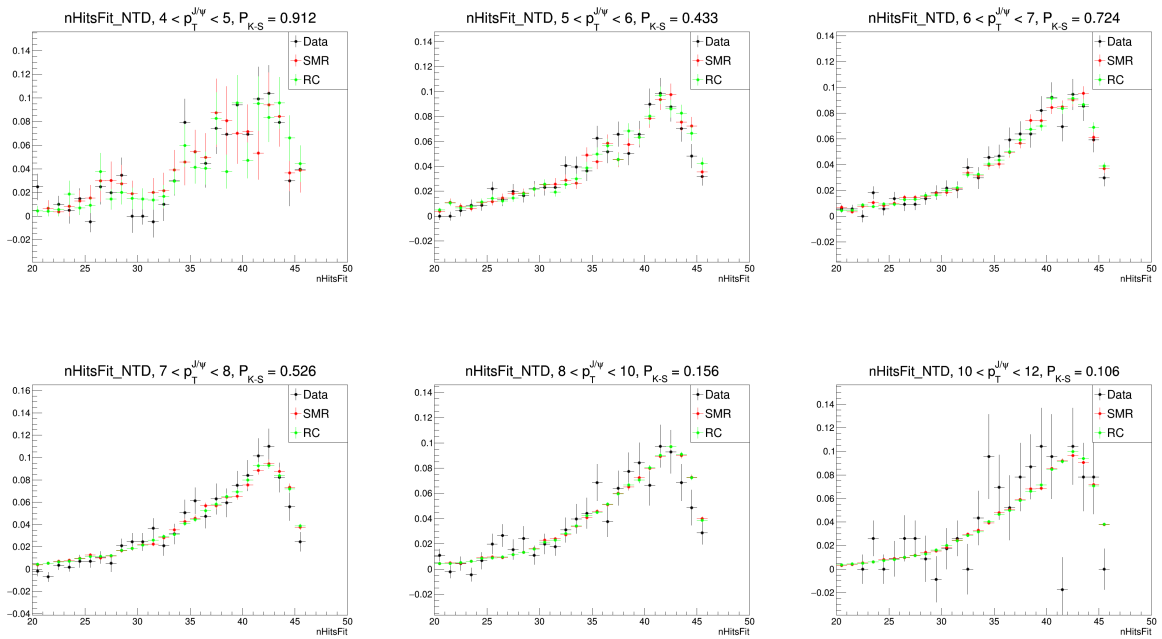
825

Triggered, p+p:



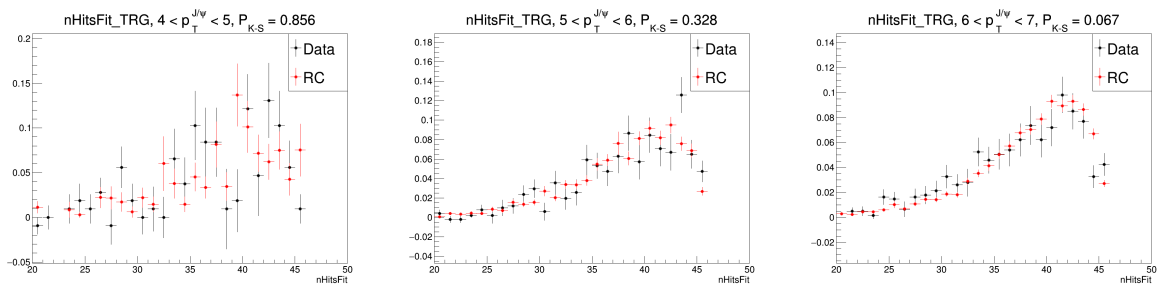
826

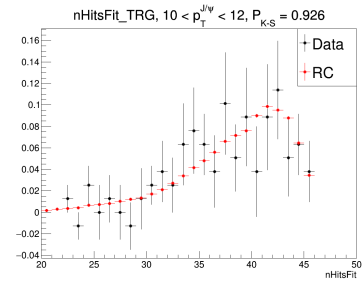
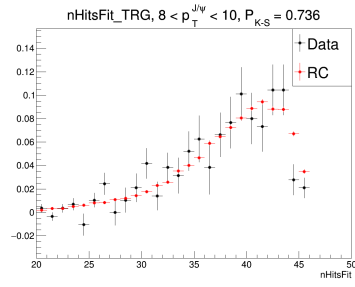
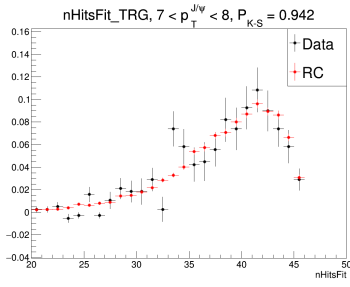
Non-triggered, p+p:



827

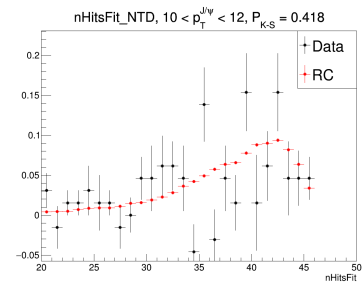
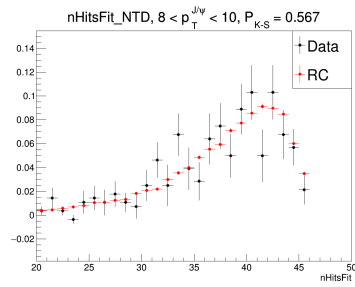
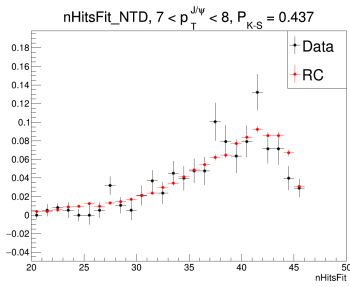
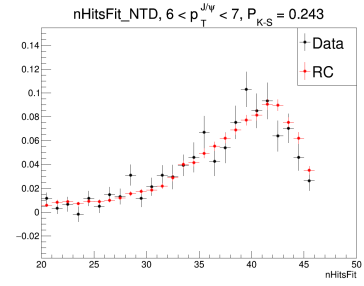
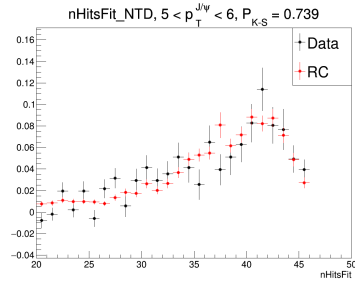
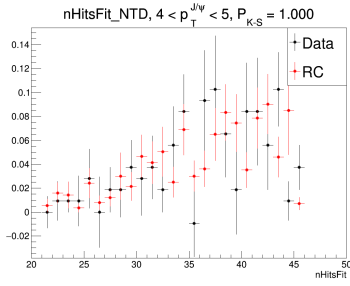
Triggered, p+Au:





828

Non-triggered, p+Au:

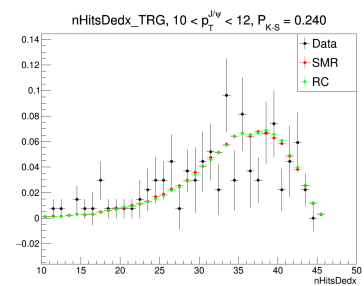
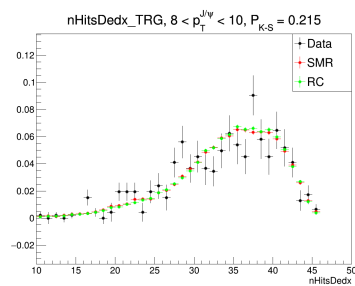
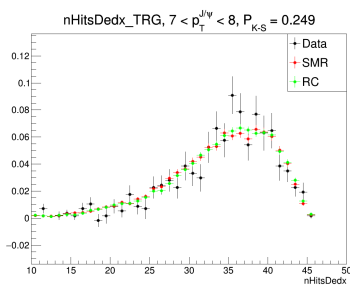
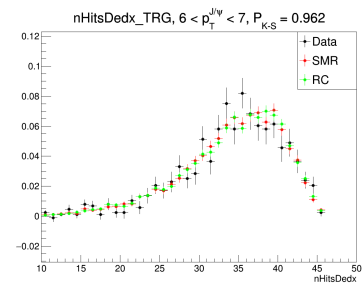
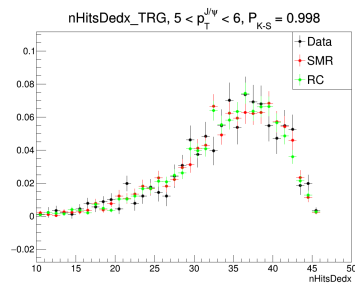
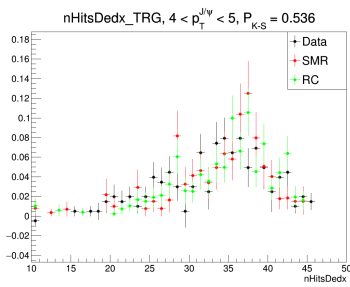


829

nHitsDedx

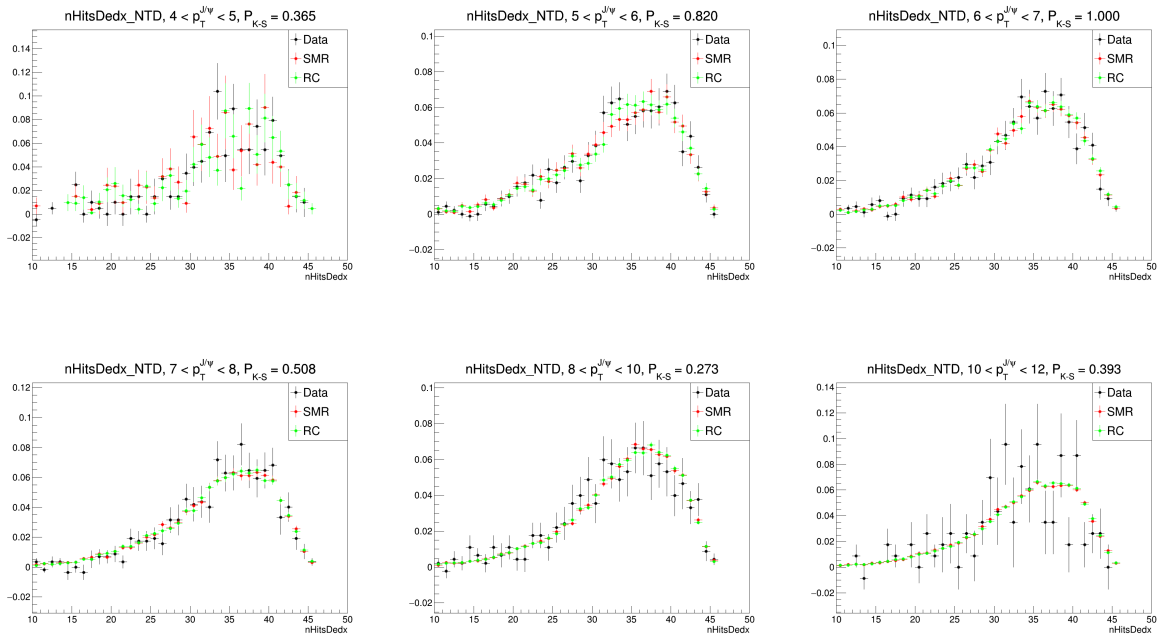
830

Triggered, p+p:



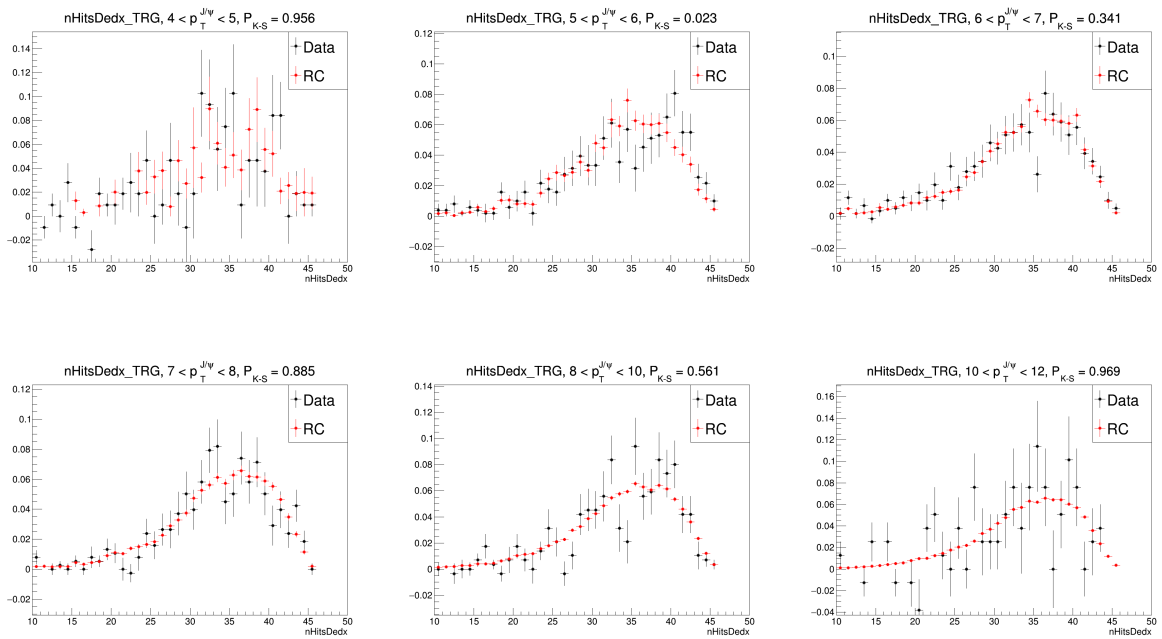
831

Non-triggered, p+p:



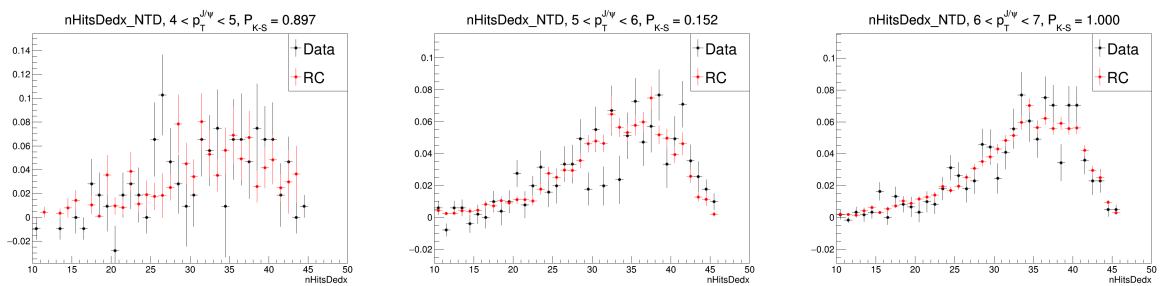
832

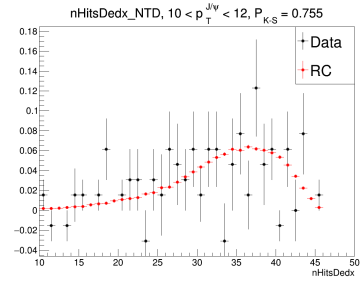
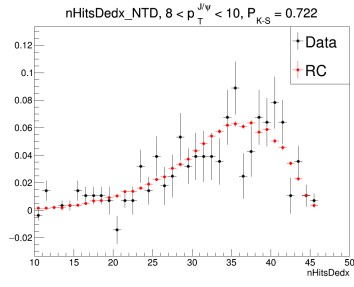
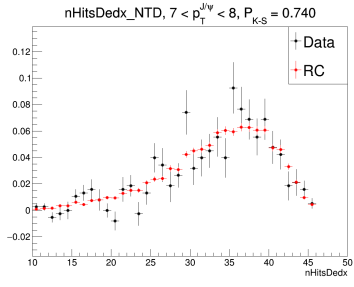
Triggered, p+Au:



833

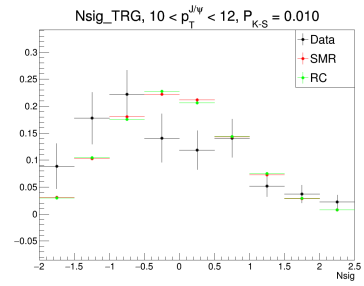
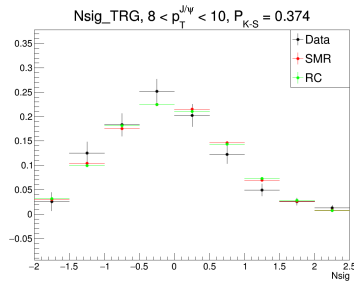
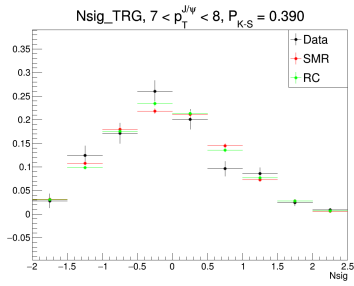
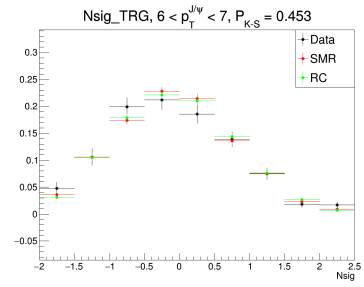
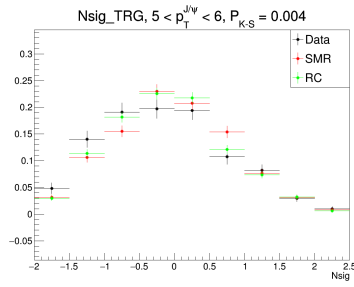
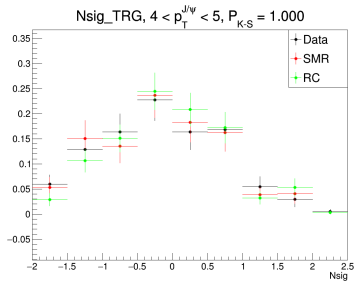
Non-triggered, p+Au:



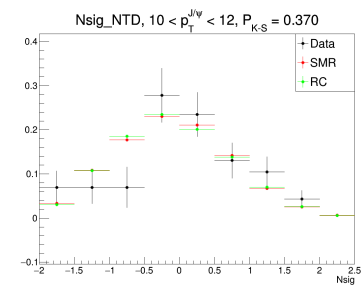
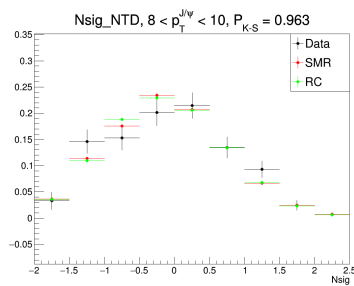
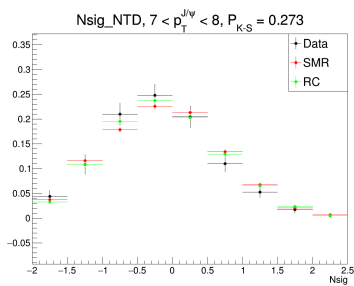
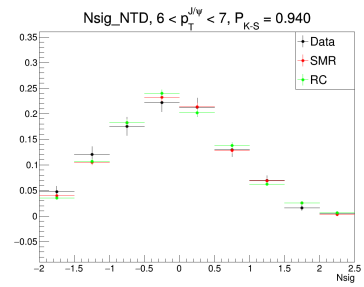
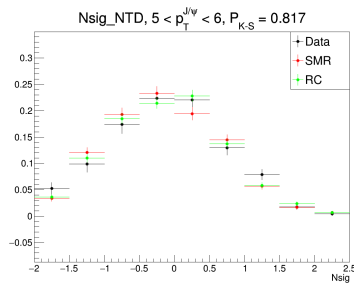
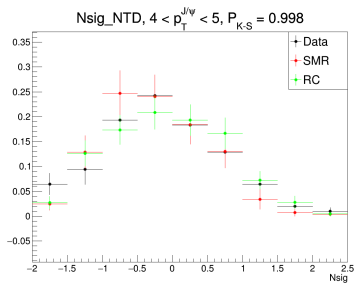


834  $n\sigma_e$

835 Triggered, p+p:

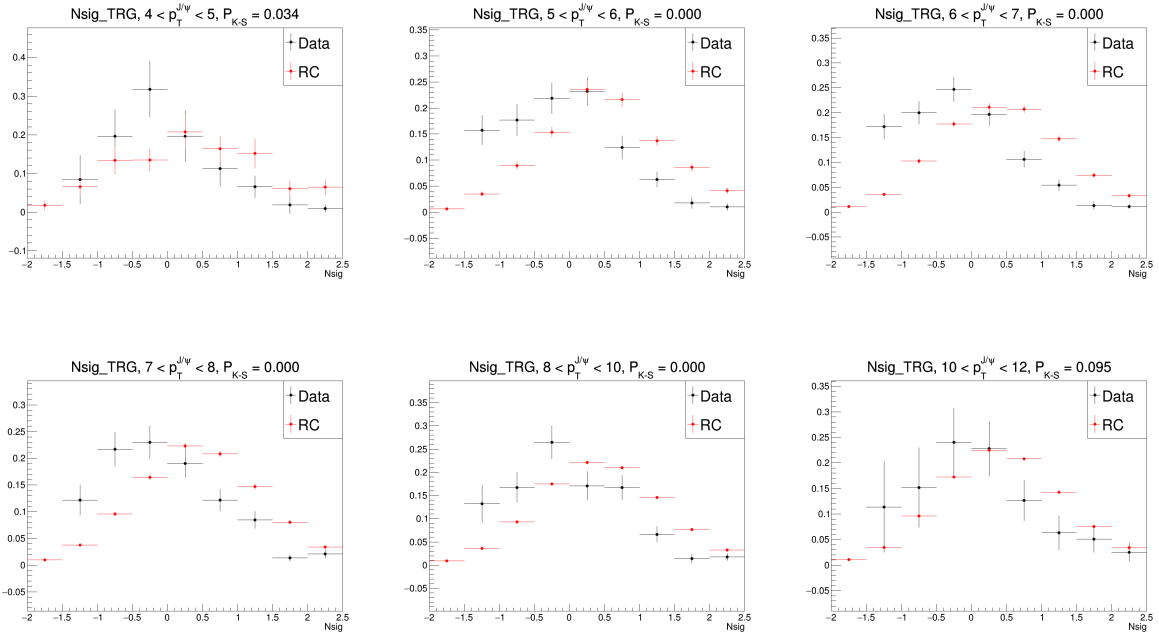


836 Non-triggered, p+p:



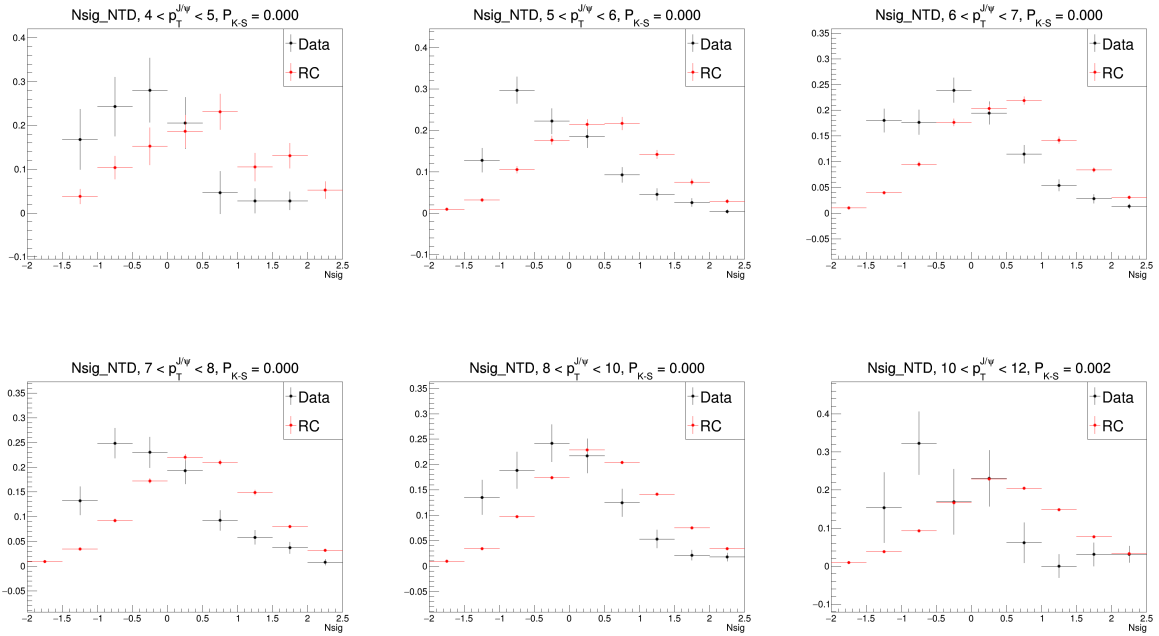
837

## Triggered, p+Au:



838

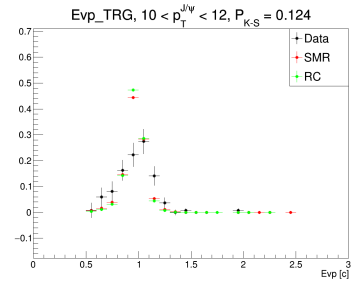
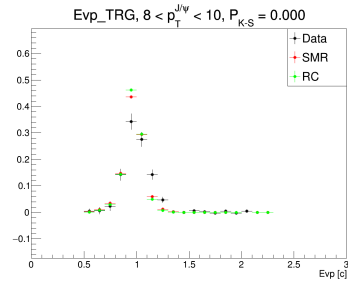
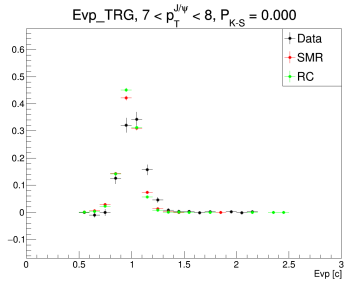
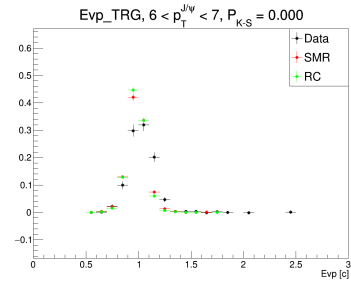
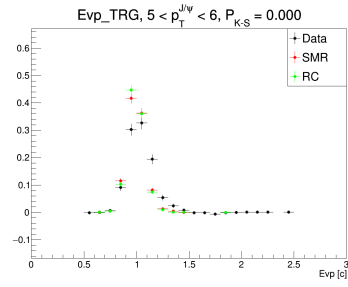
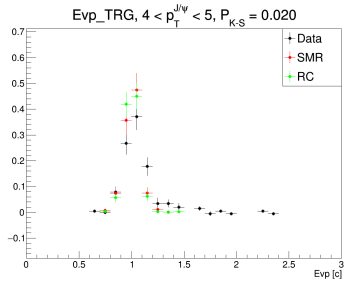
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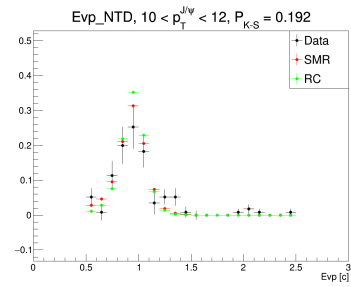
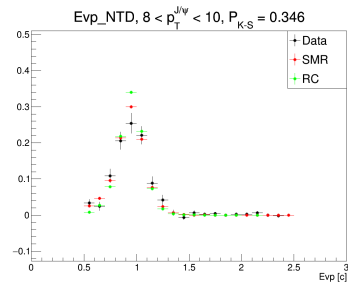
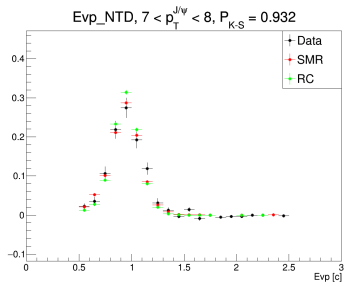
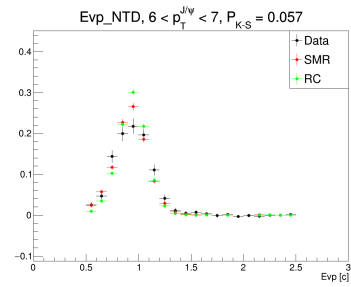
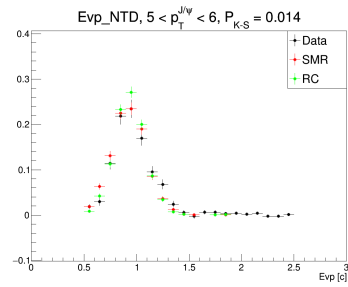
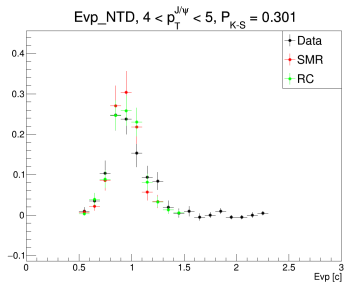
839 Others

840 e/p [c]

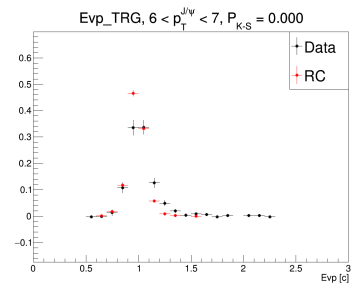
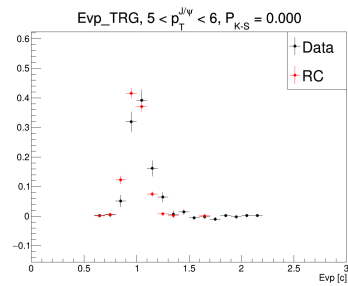
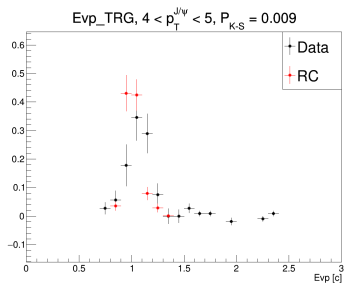
841 Triggered, p+p:



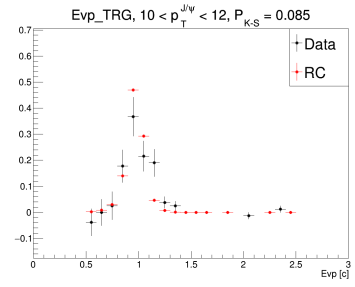
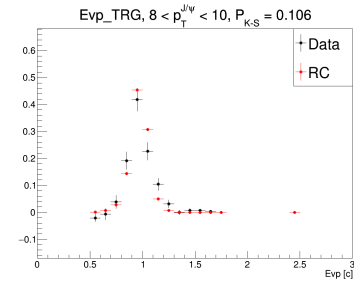
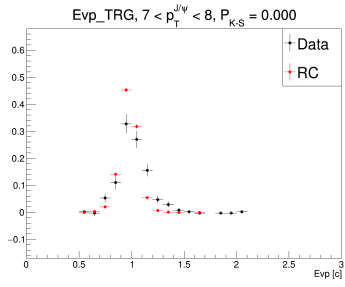
842 Non-triggered, p+p:



843 Triggered, p+Au:

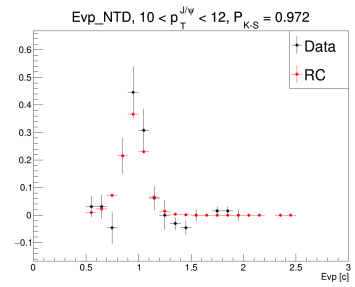
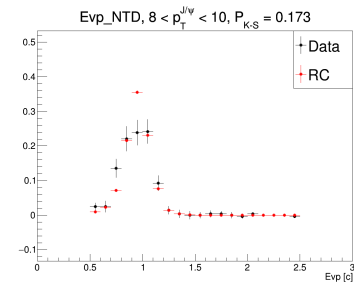
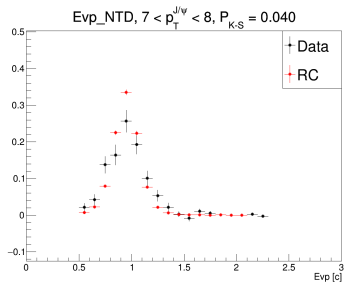
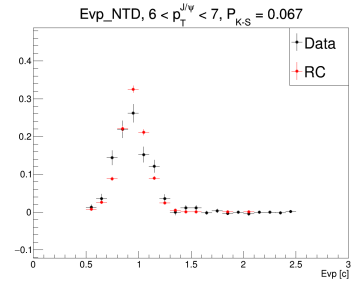
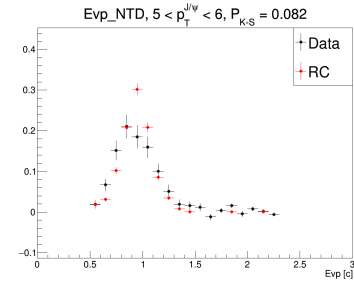
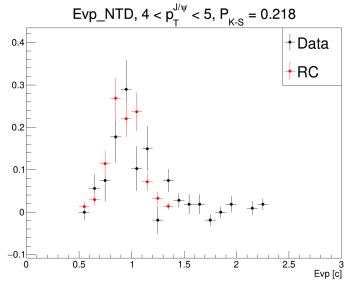






844

Non-triggered, p+Au:

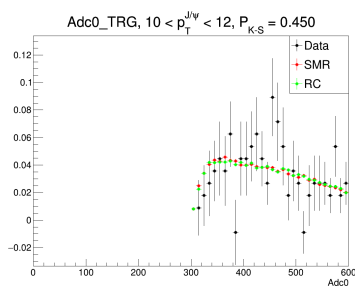
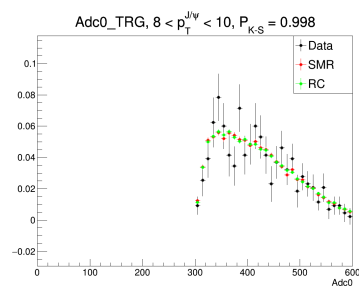
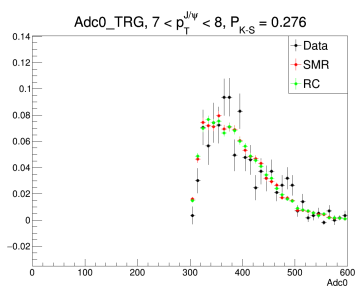
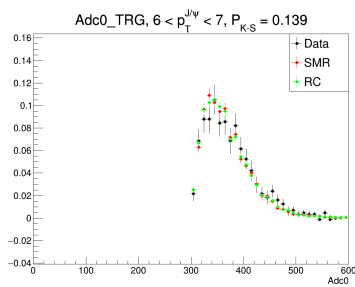
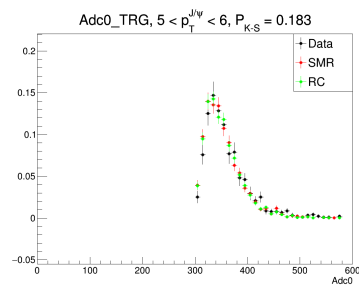
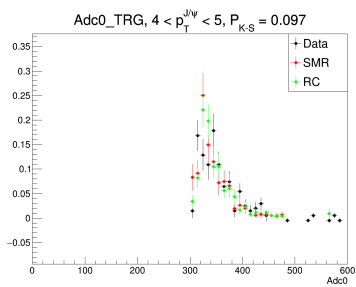


845

Adc0

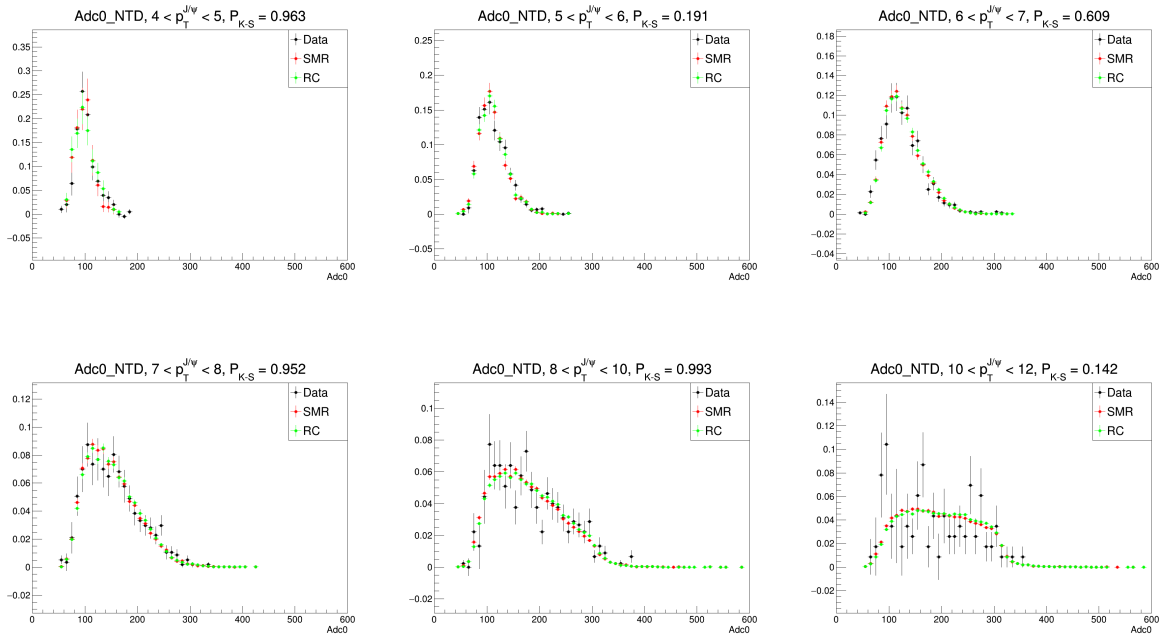
846

Triggered, p+p:



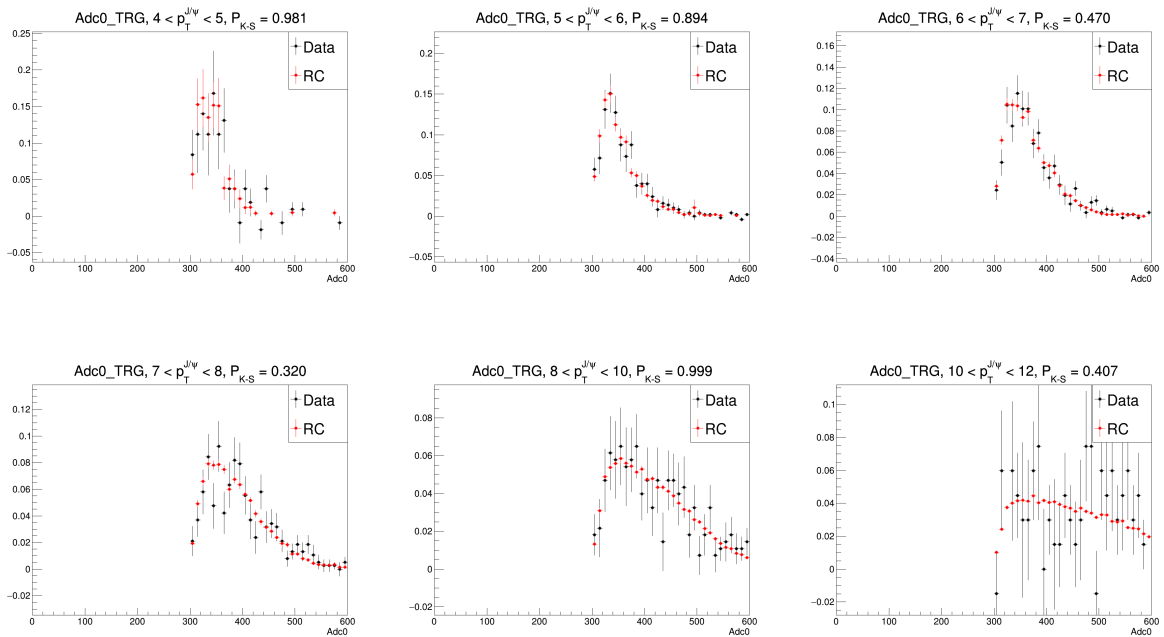
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Non-triggered, p+p:



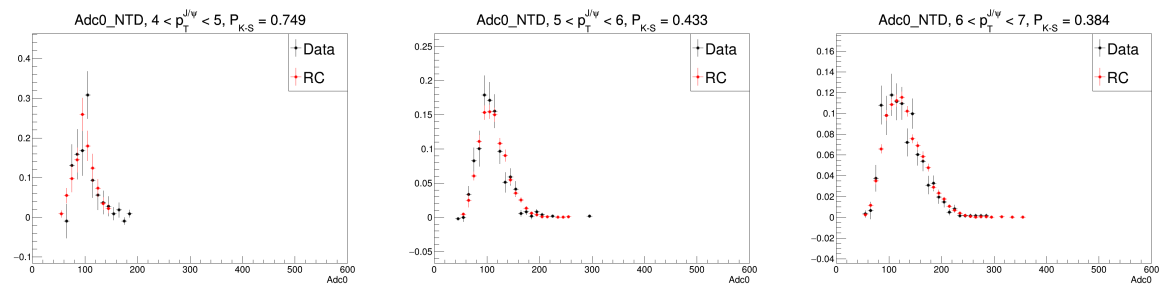
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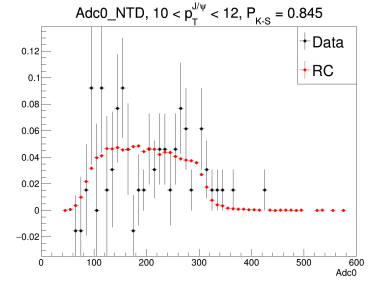
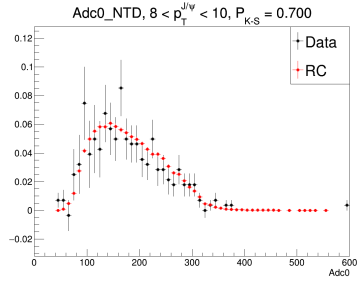
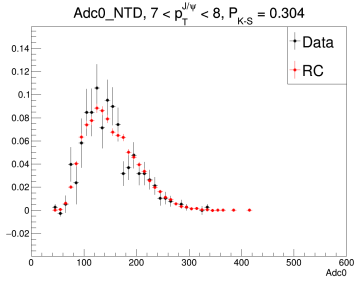
Triggered, p+Au:



849

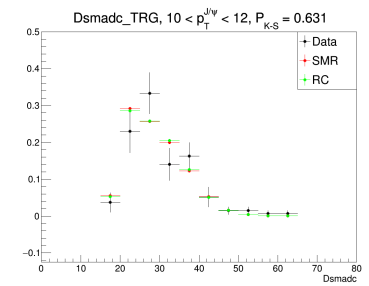
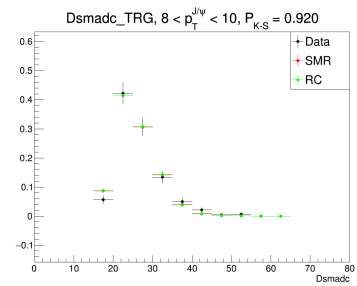
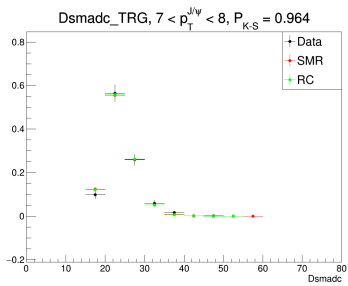
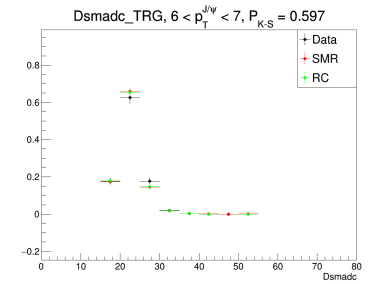
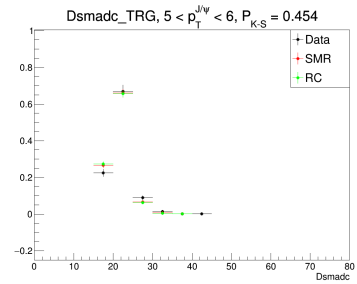
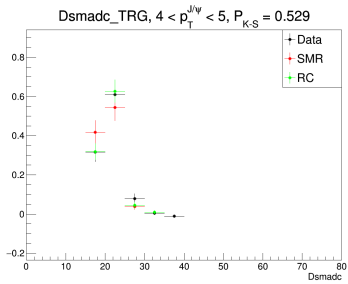
Non-triggered, p+Au:



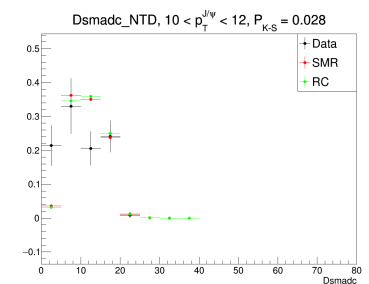
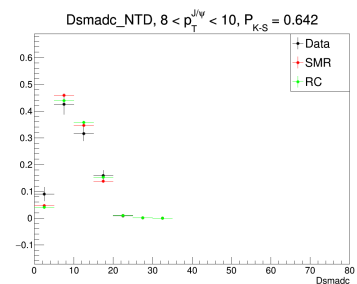
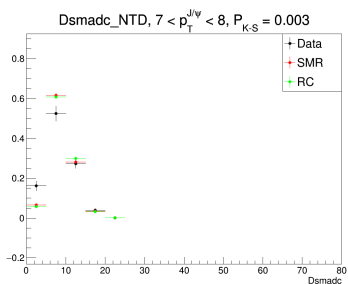
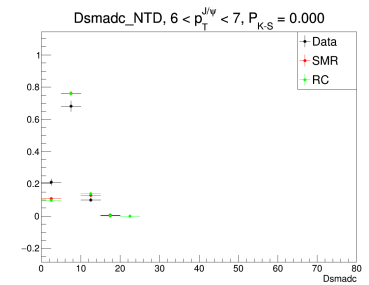
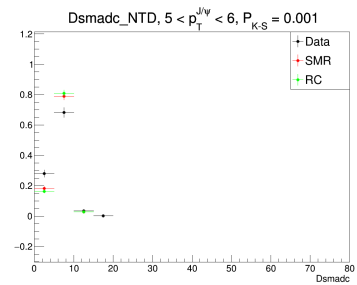
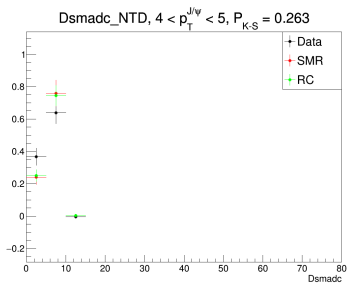


850 **Dsmadc**

851 Triggered, p+p:

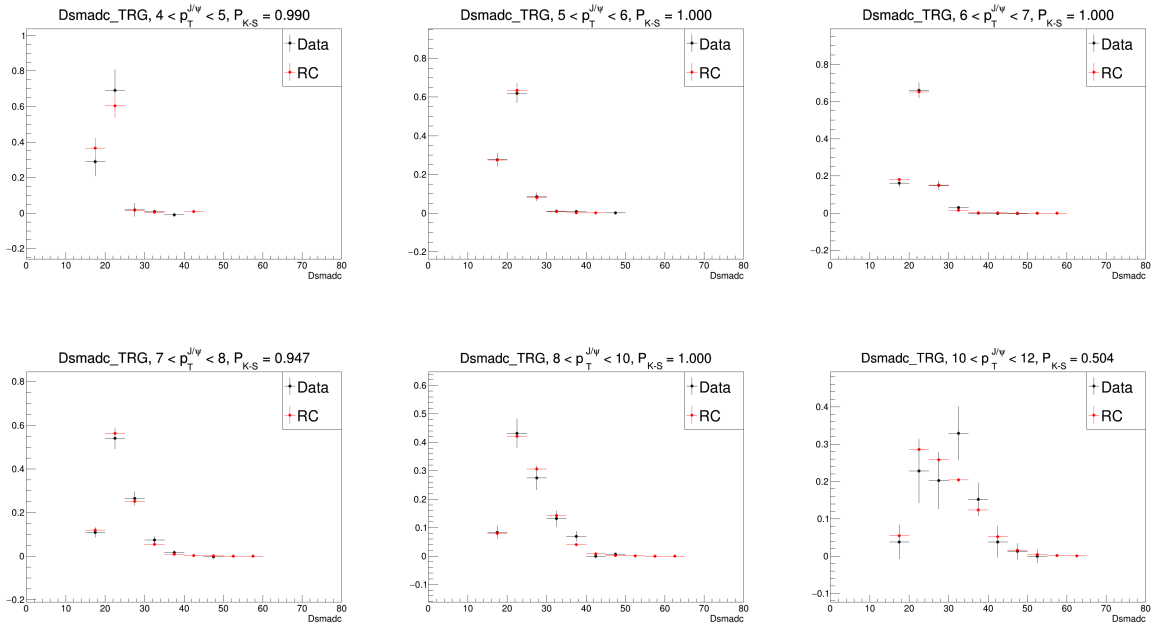


852 Non-triggered, p+p:



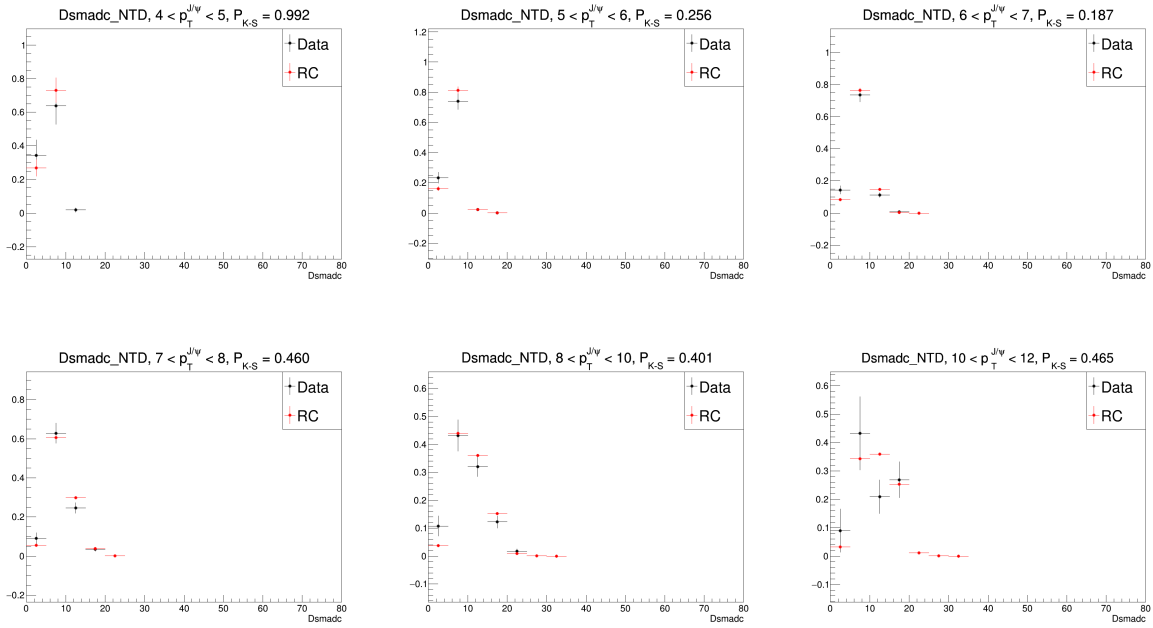
853

Triggered, p+Au:



854

Non-triggered, p+Au:

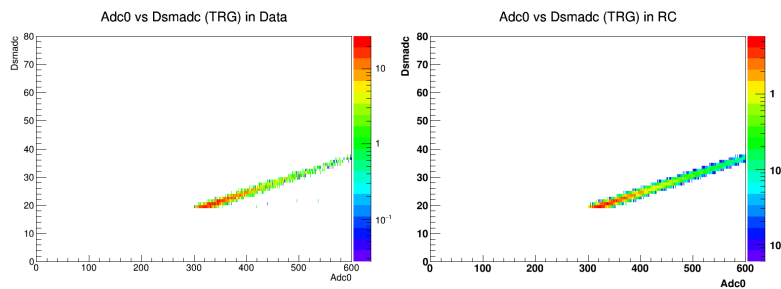


855

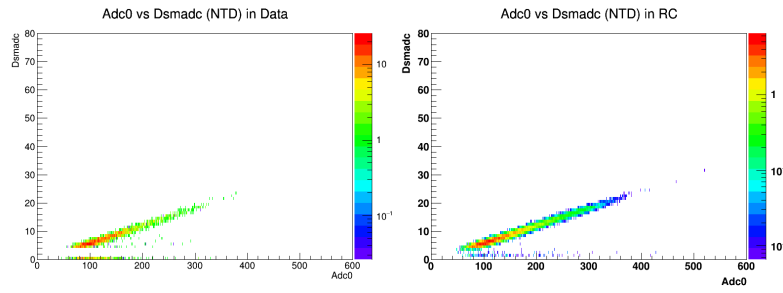
Dsmadc vs Adc0 (Integrated Over J/ψ p<sub>T</sub>)

856

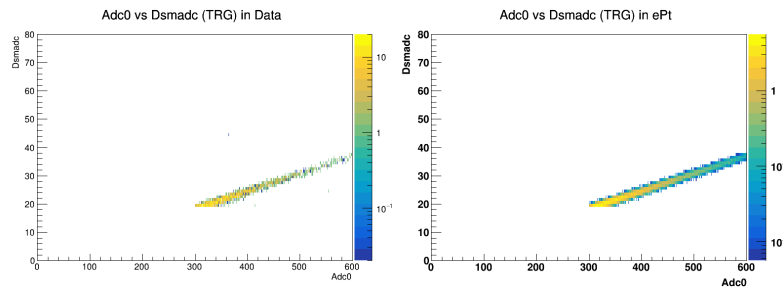
Triggered, p+p:



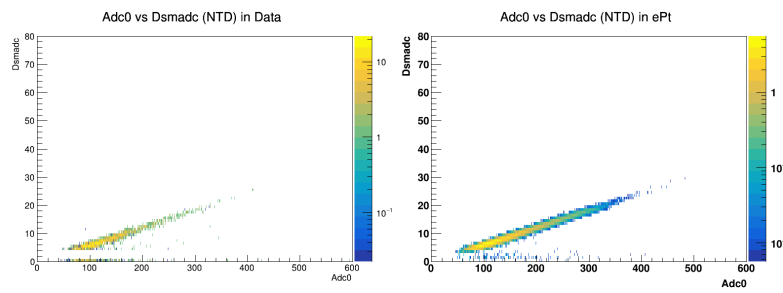
857 Non-triggered, p+p:



858 Triggered, p+Au:

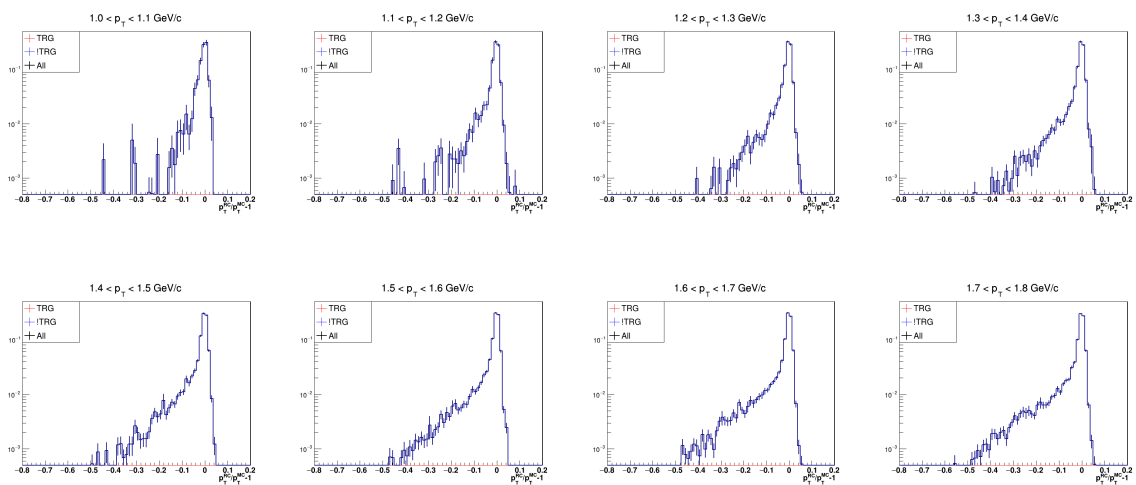


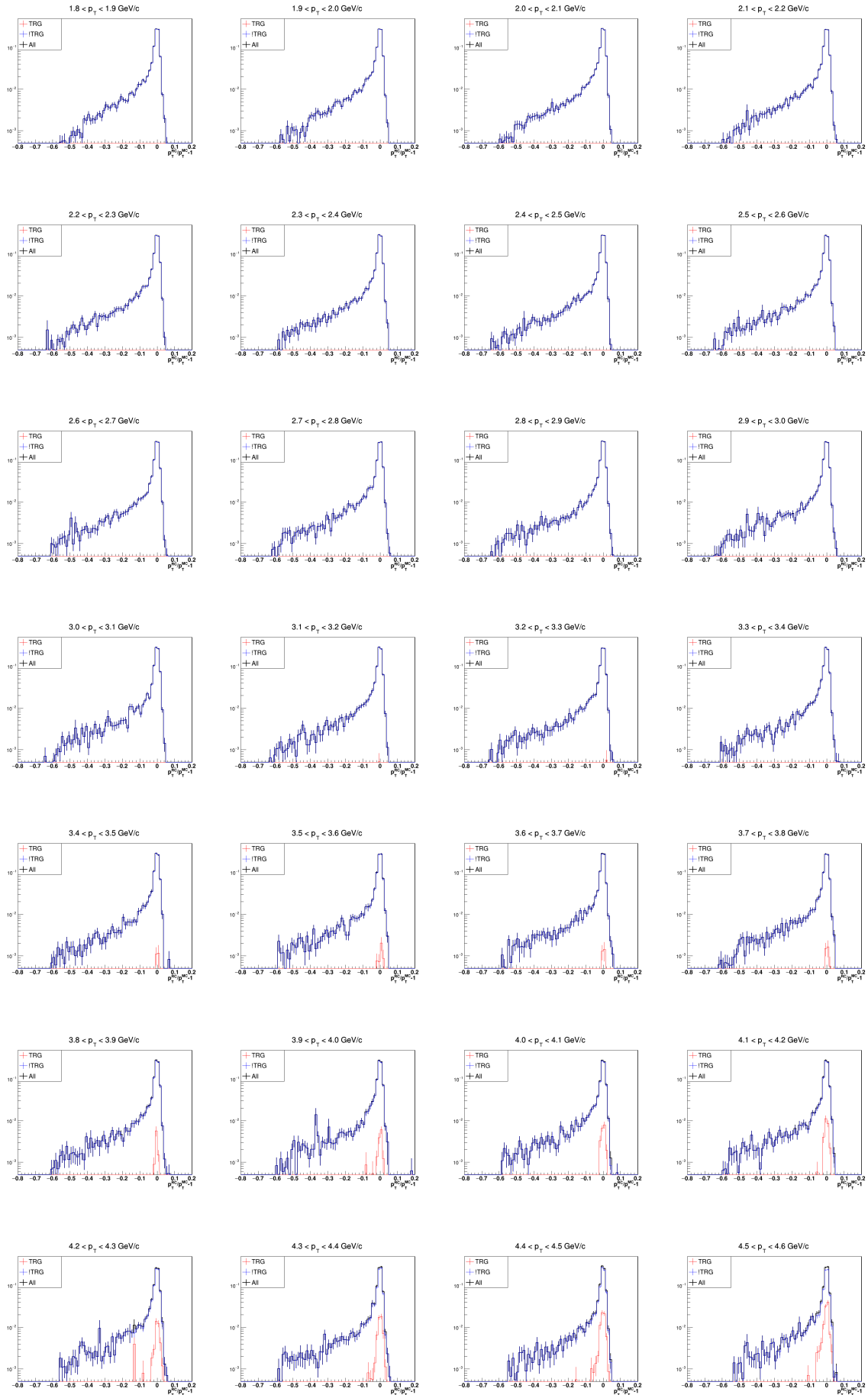
859 Non-triggered, p+Au:

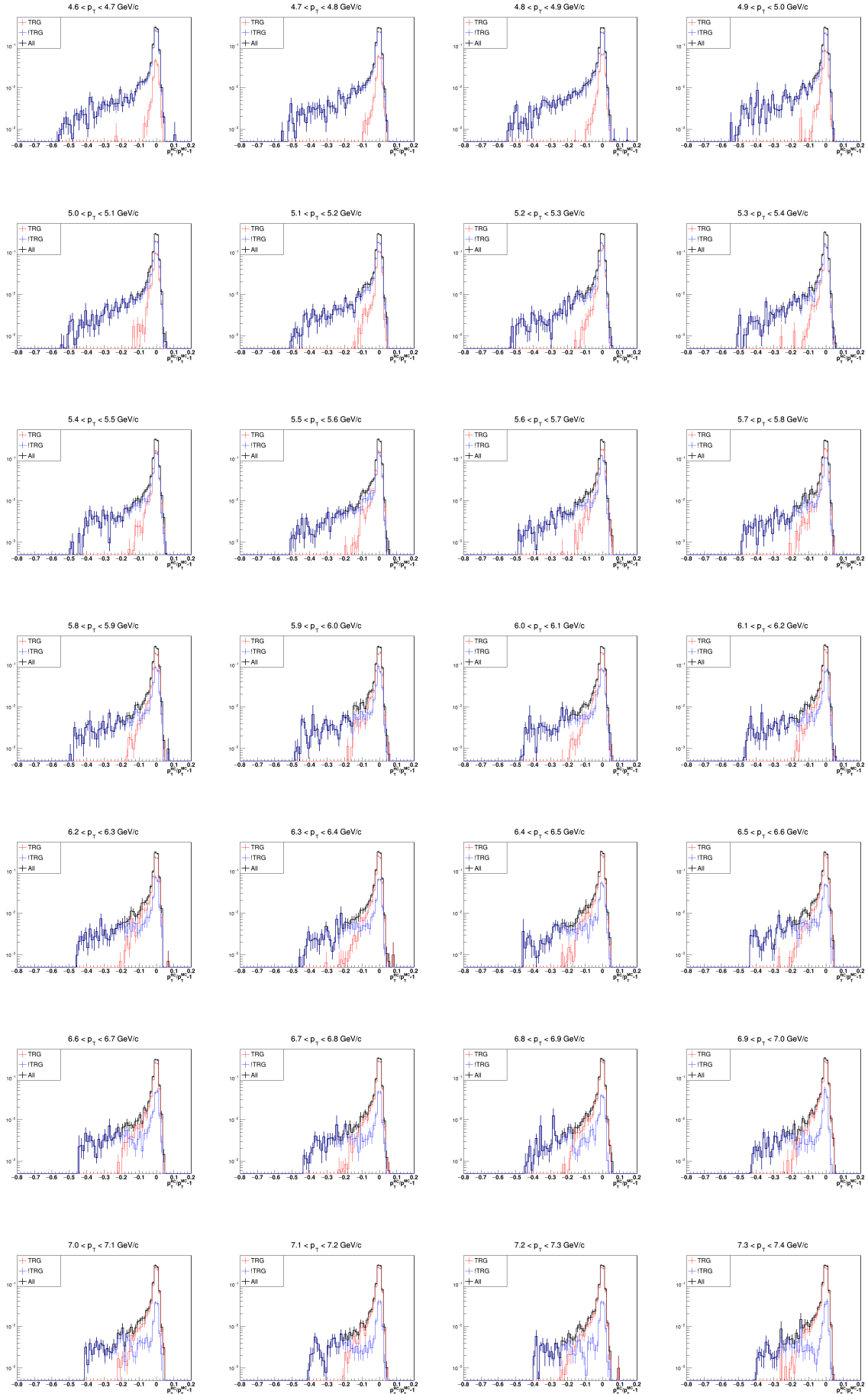


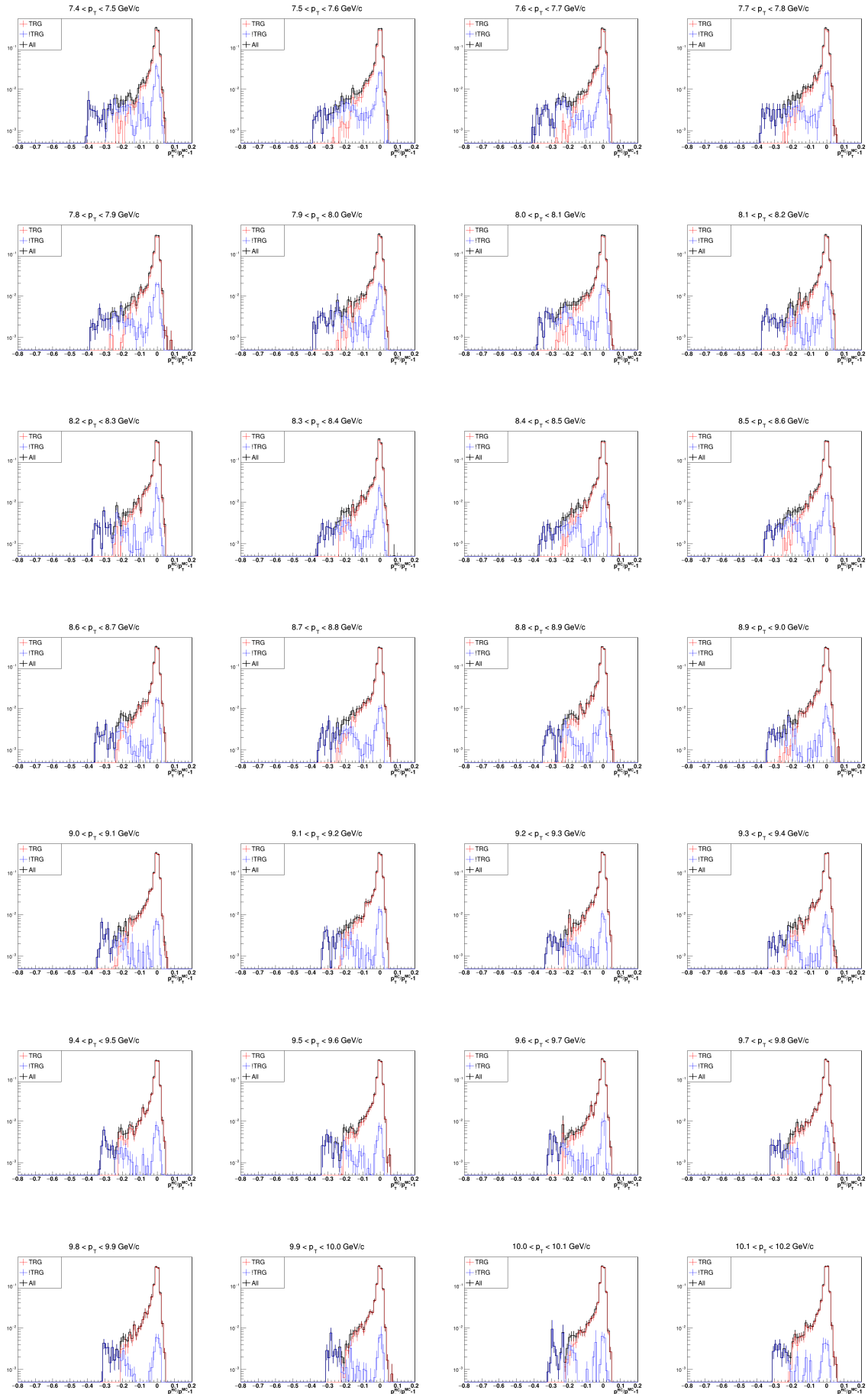
## 860 7.2 Smearing Templates

861 p+p

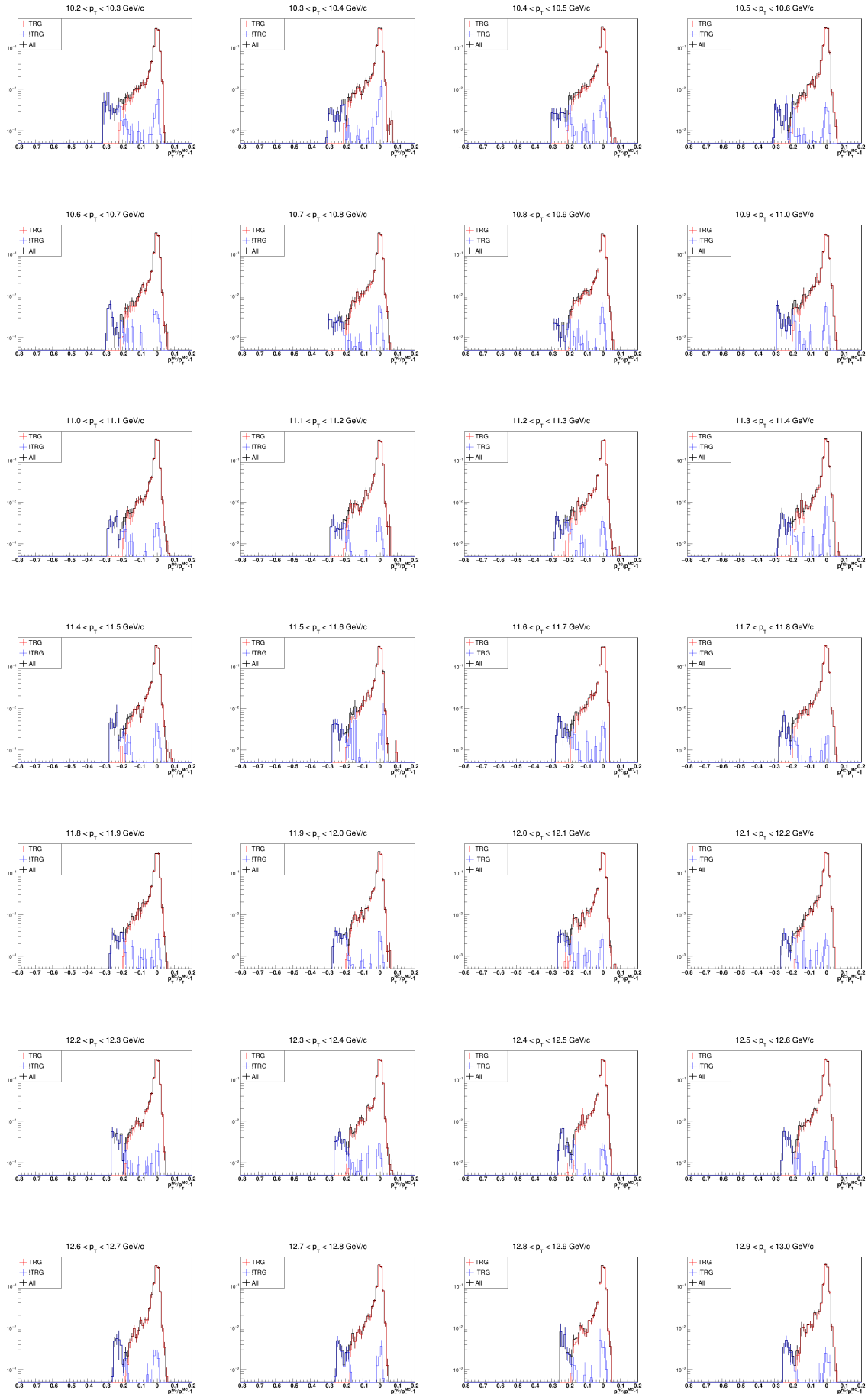


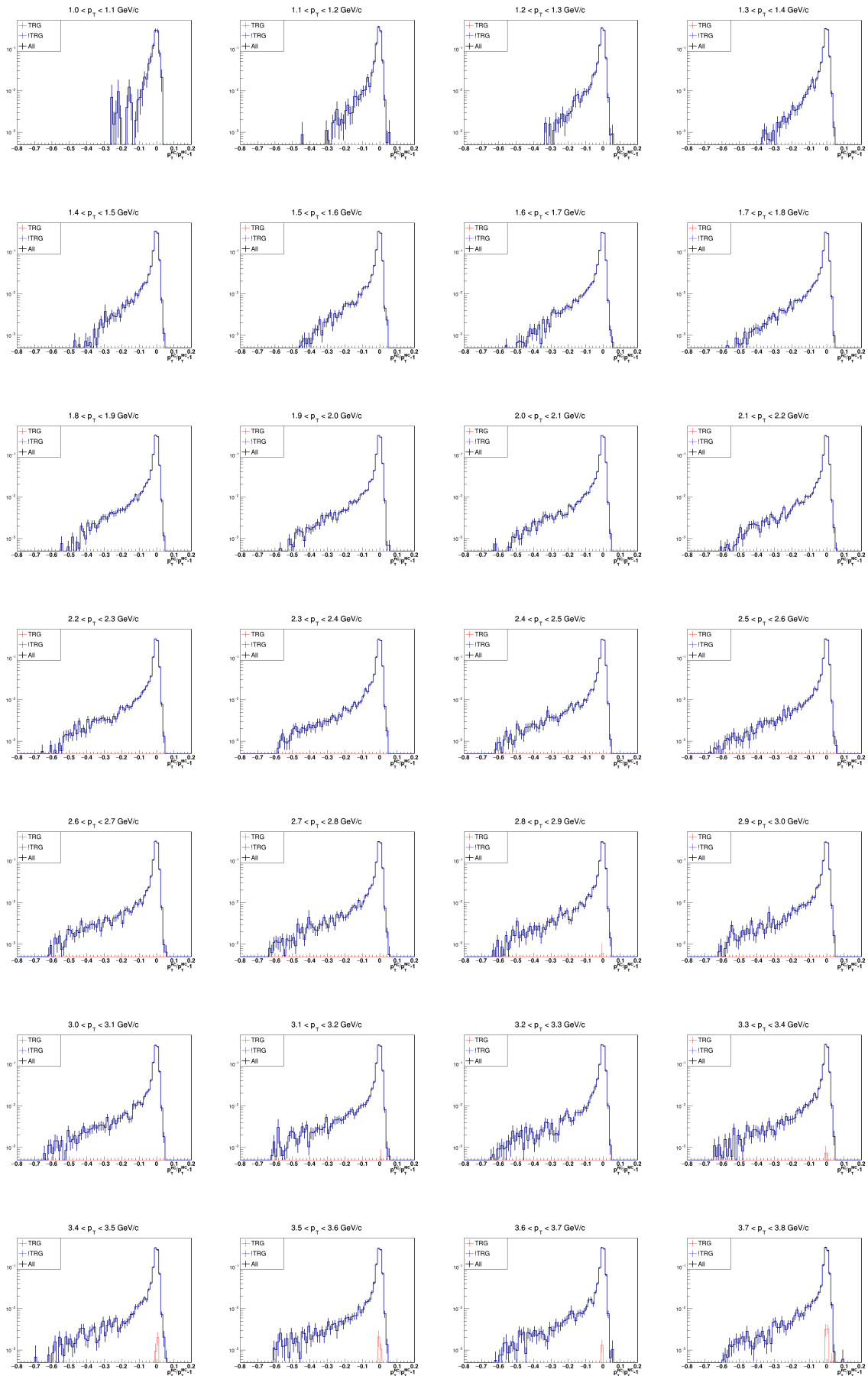


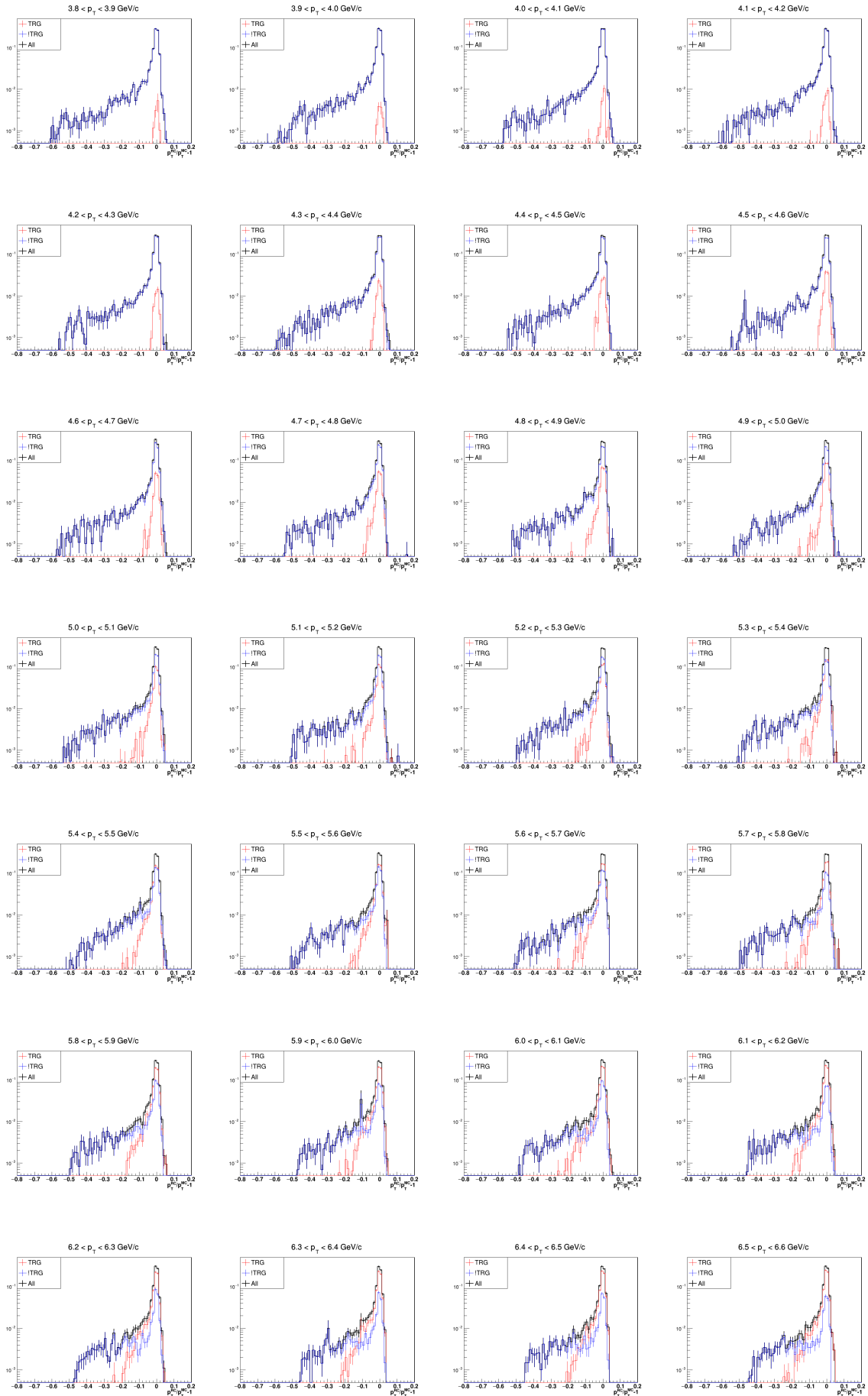


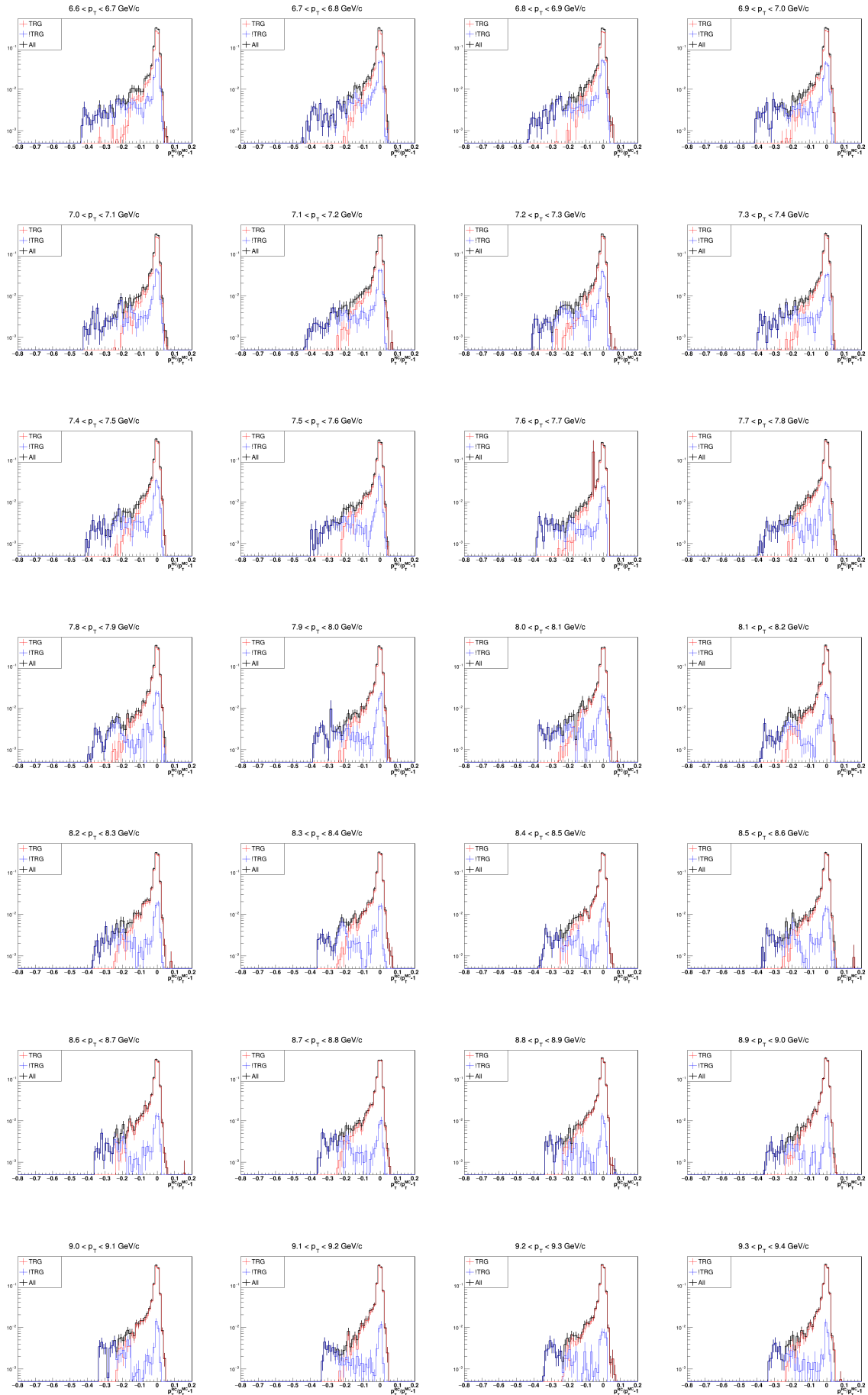


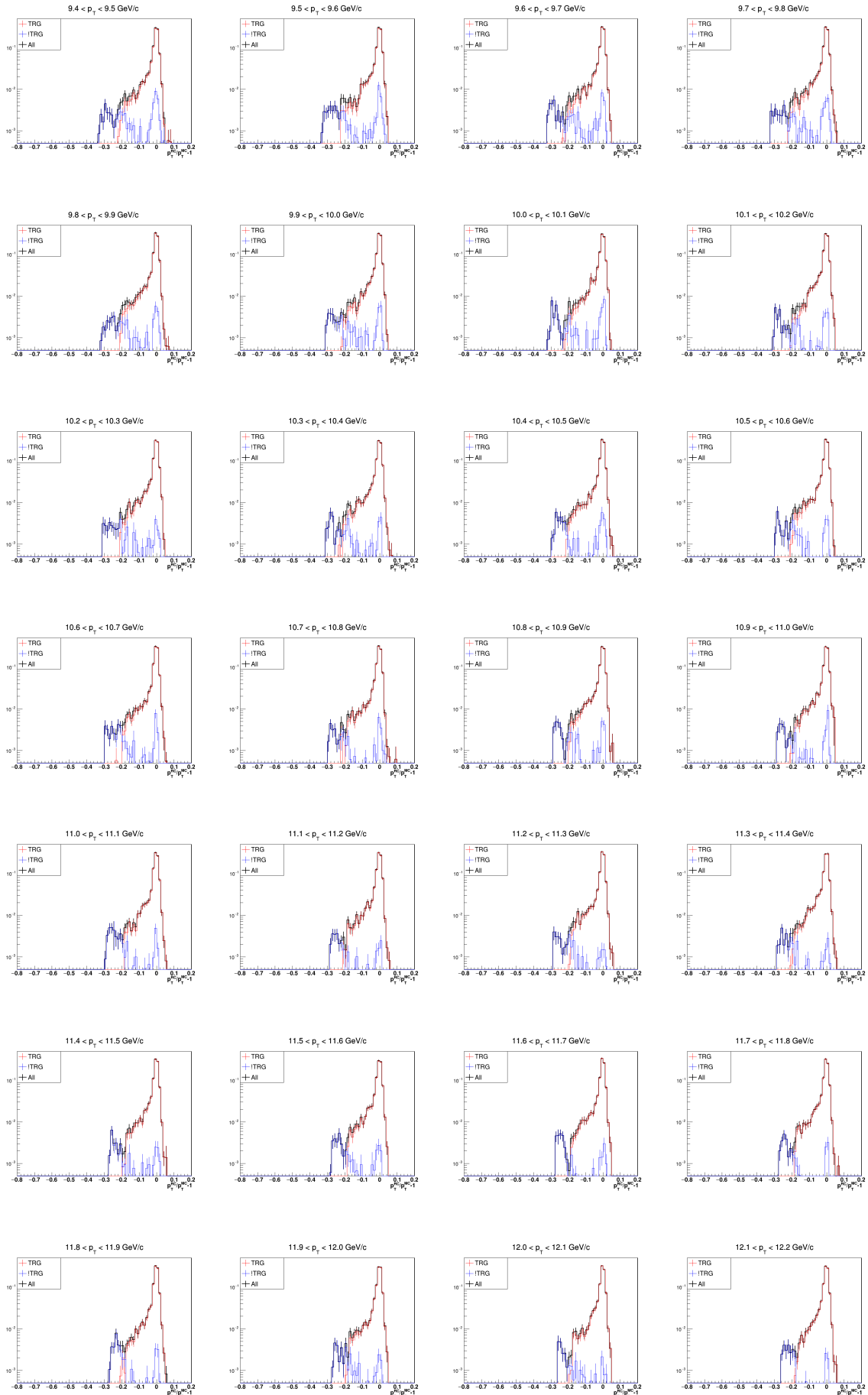


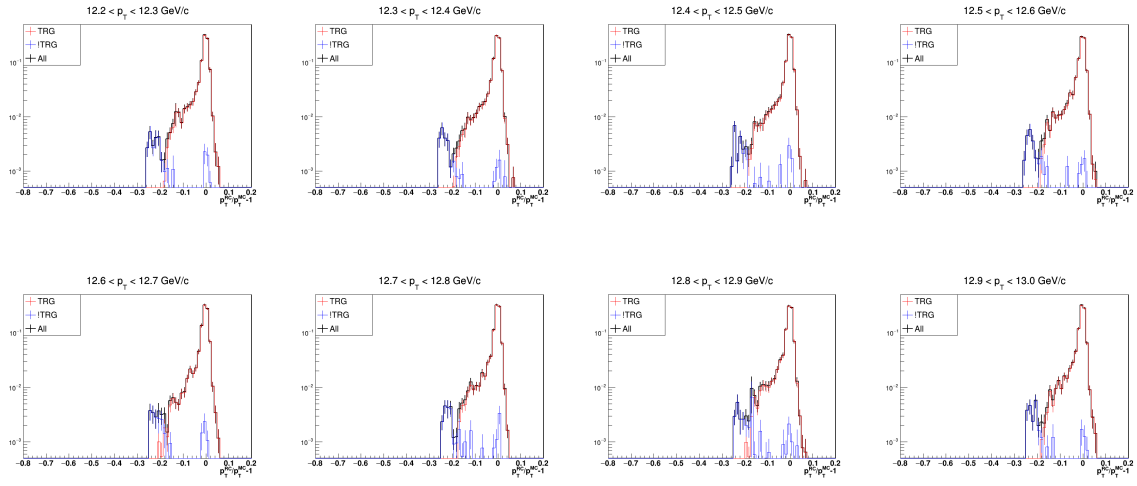




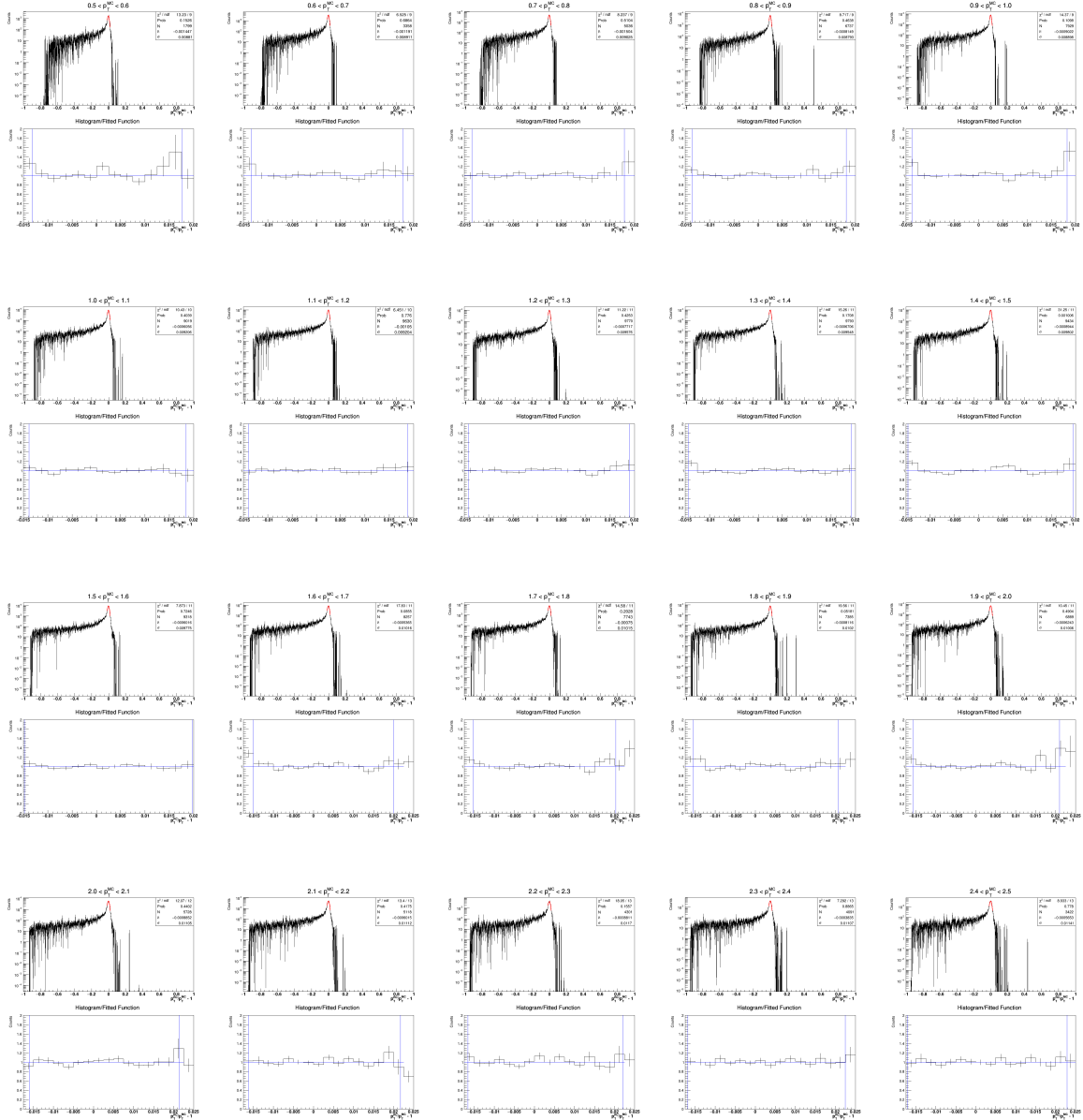


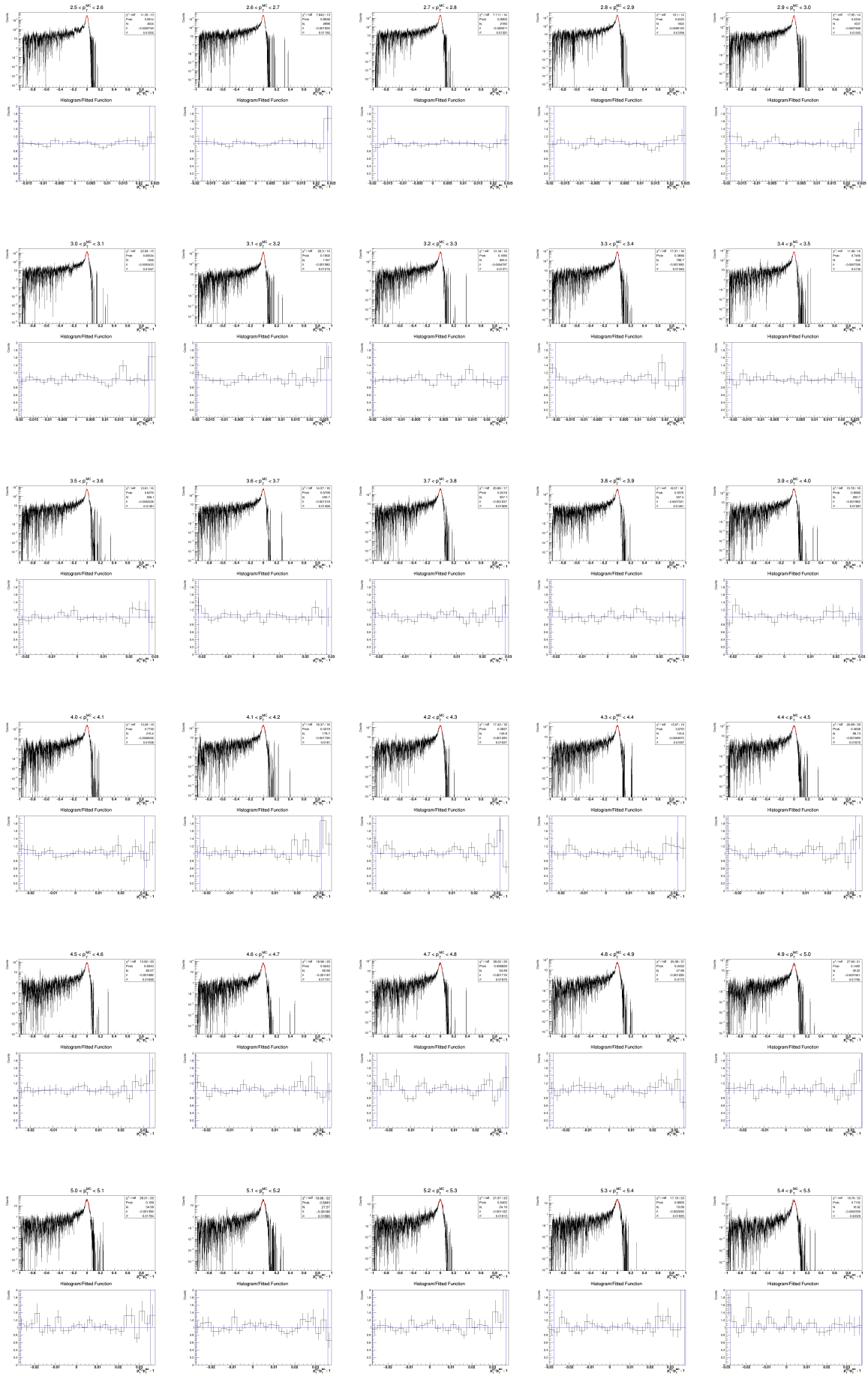


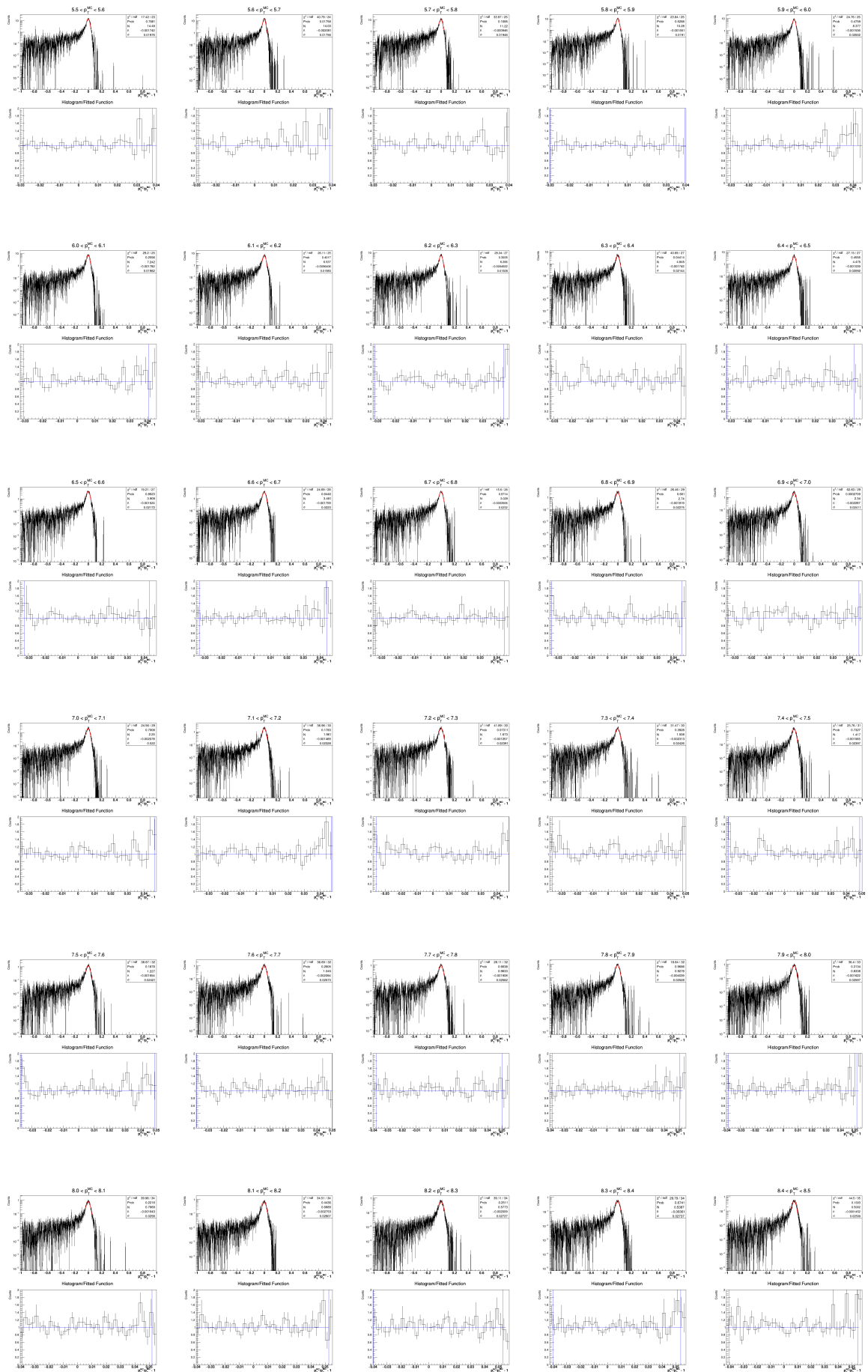




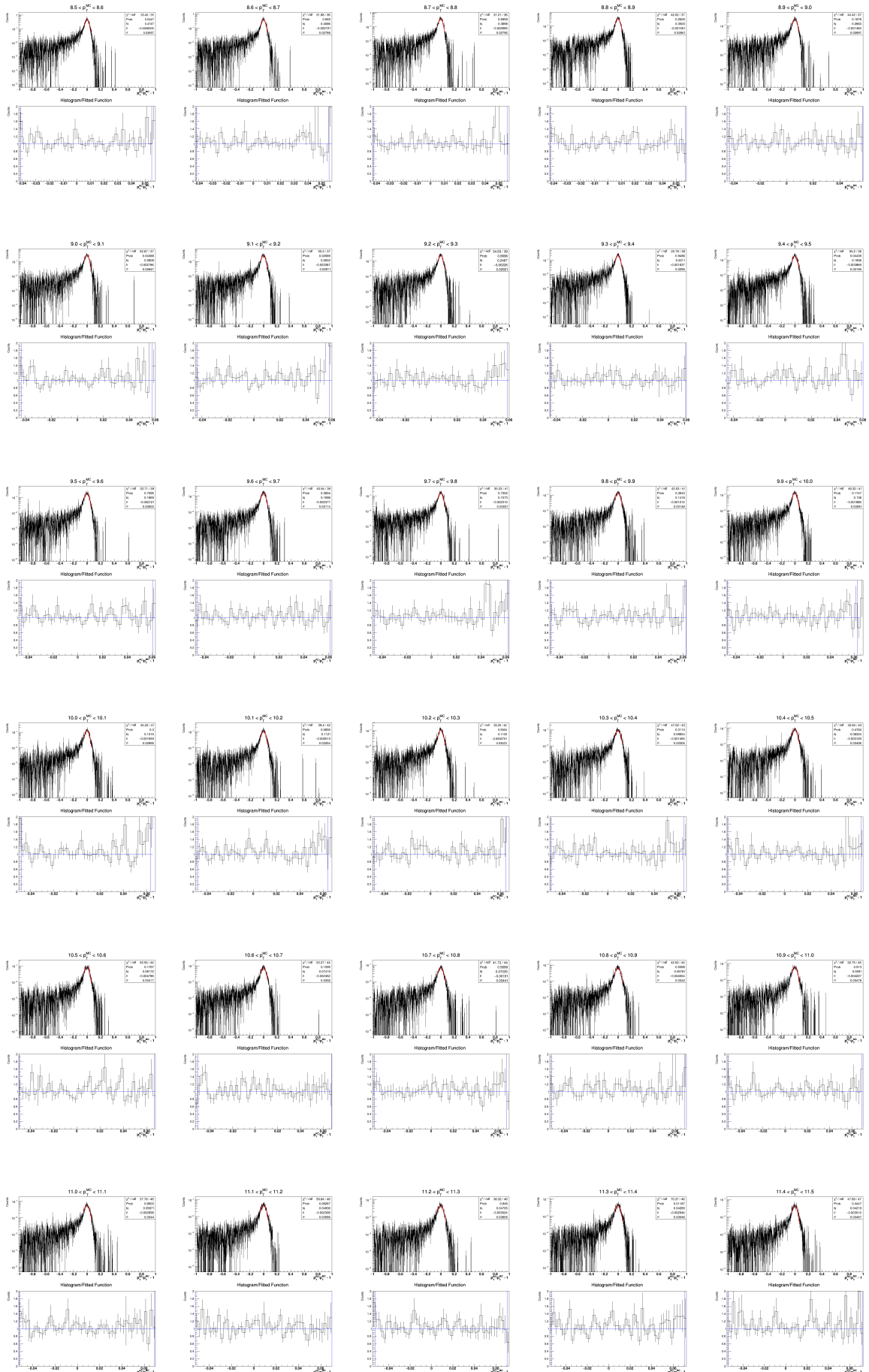
863 **7.3 Electron RC Momentum Distribution Fit**

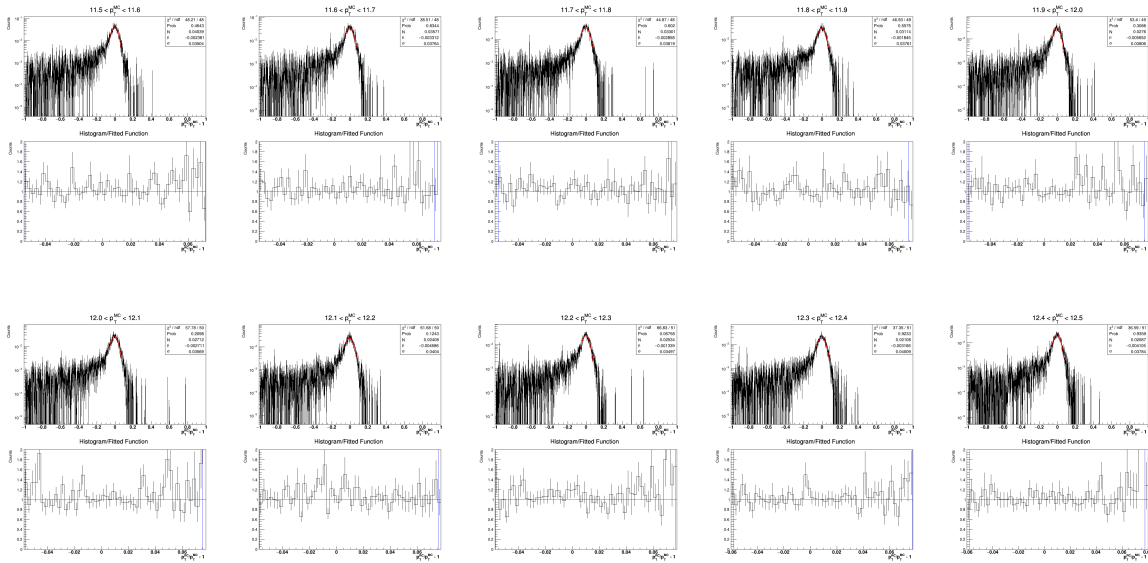






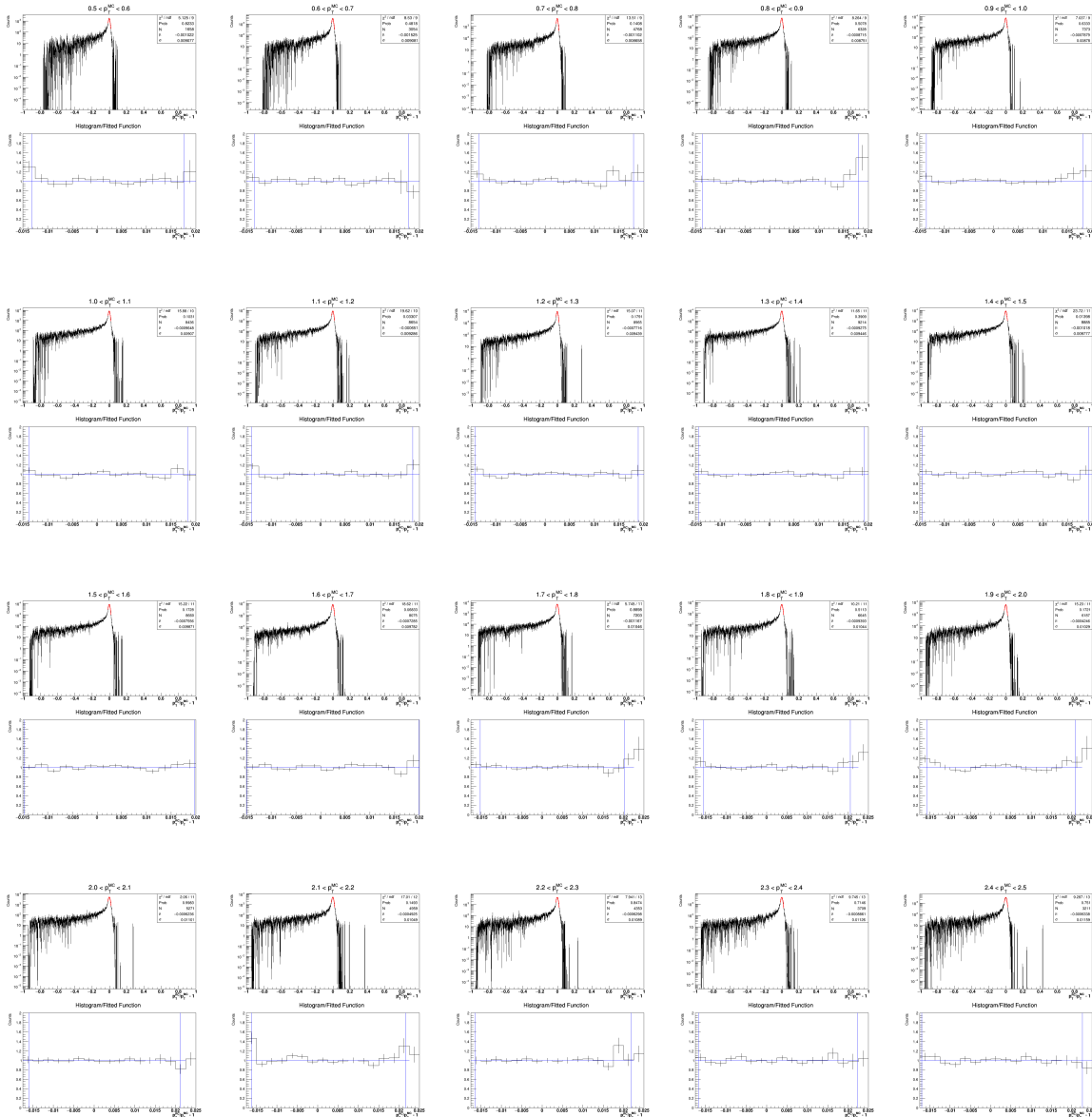


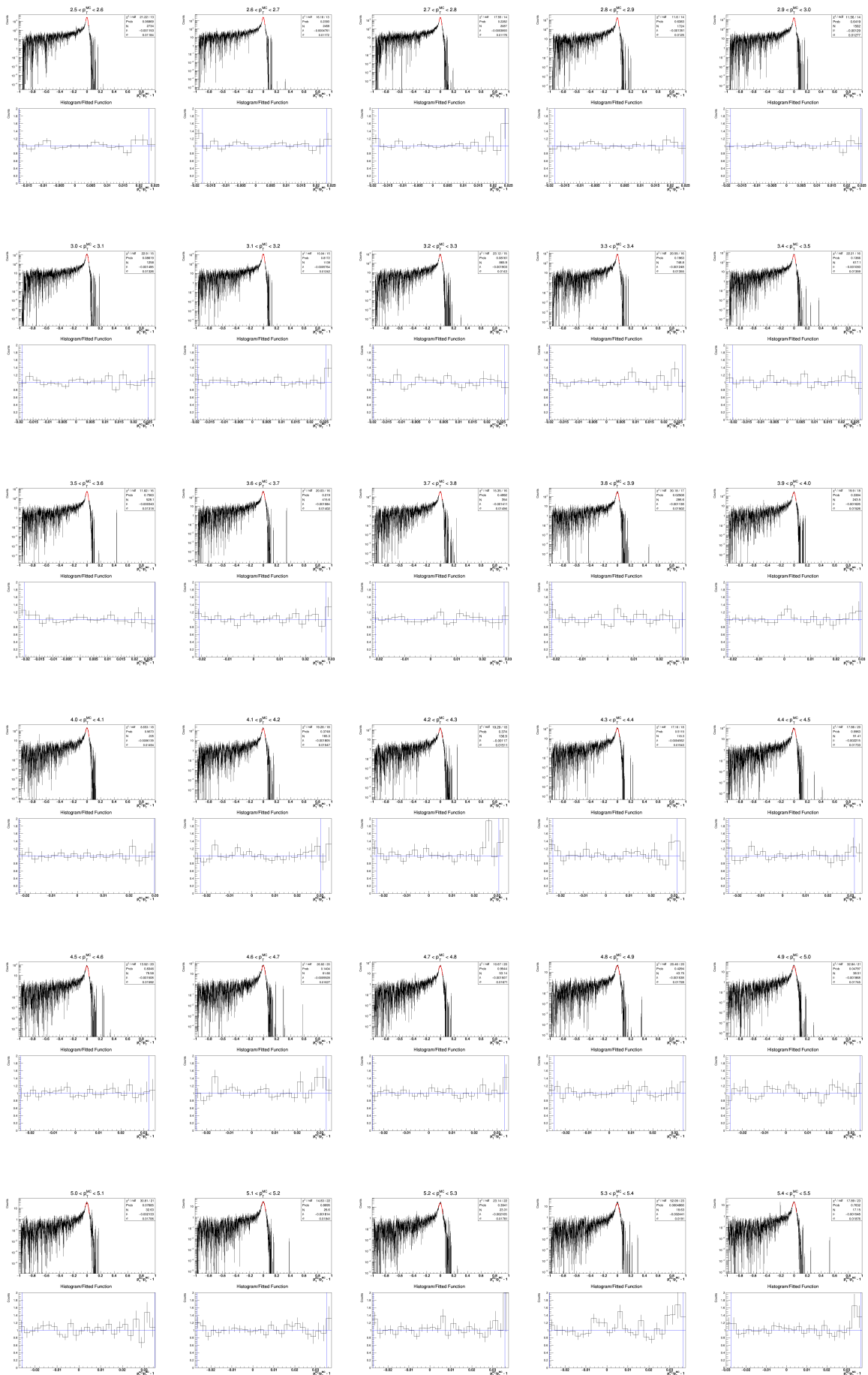


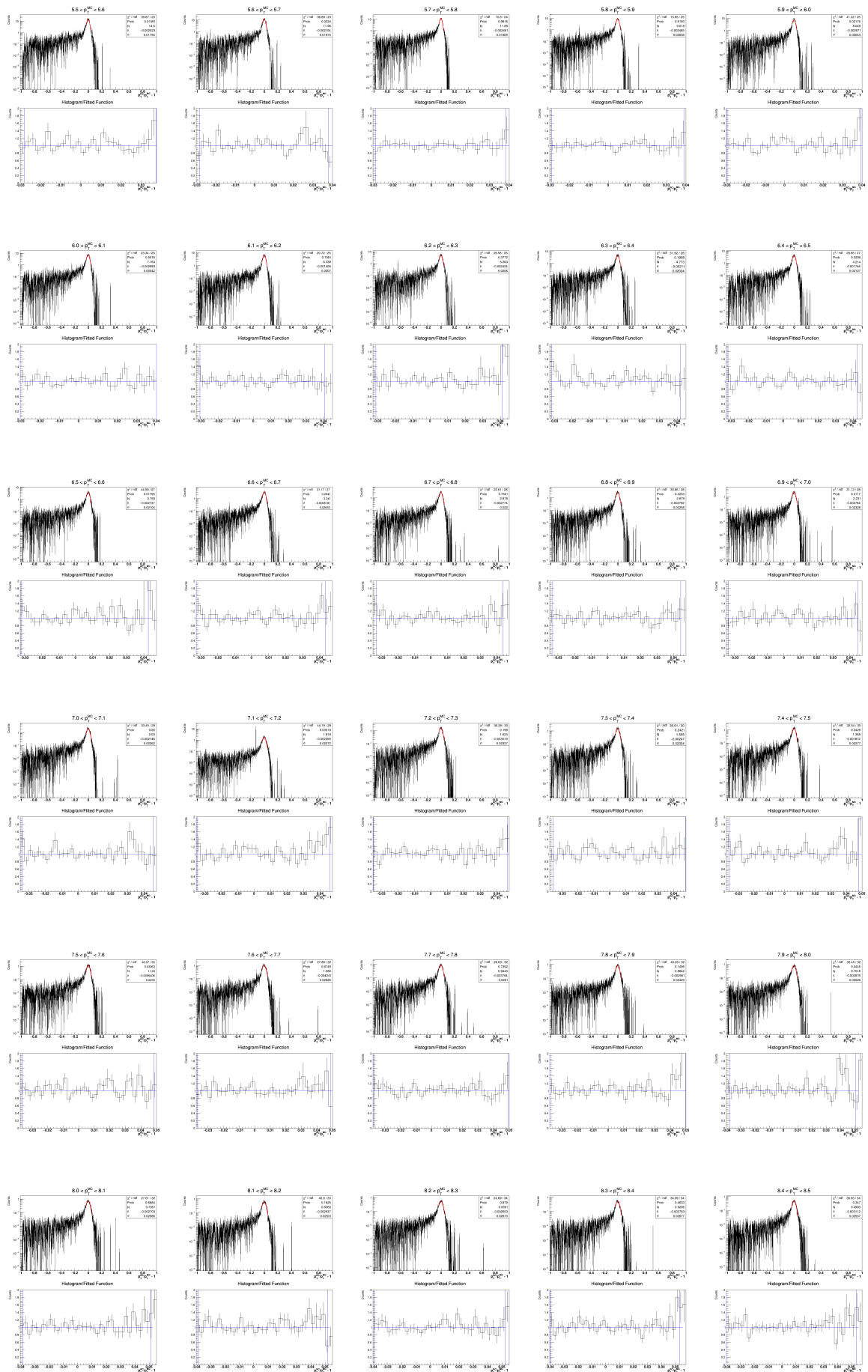


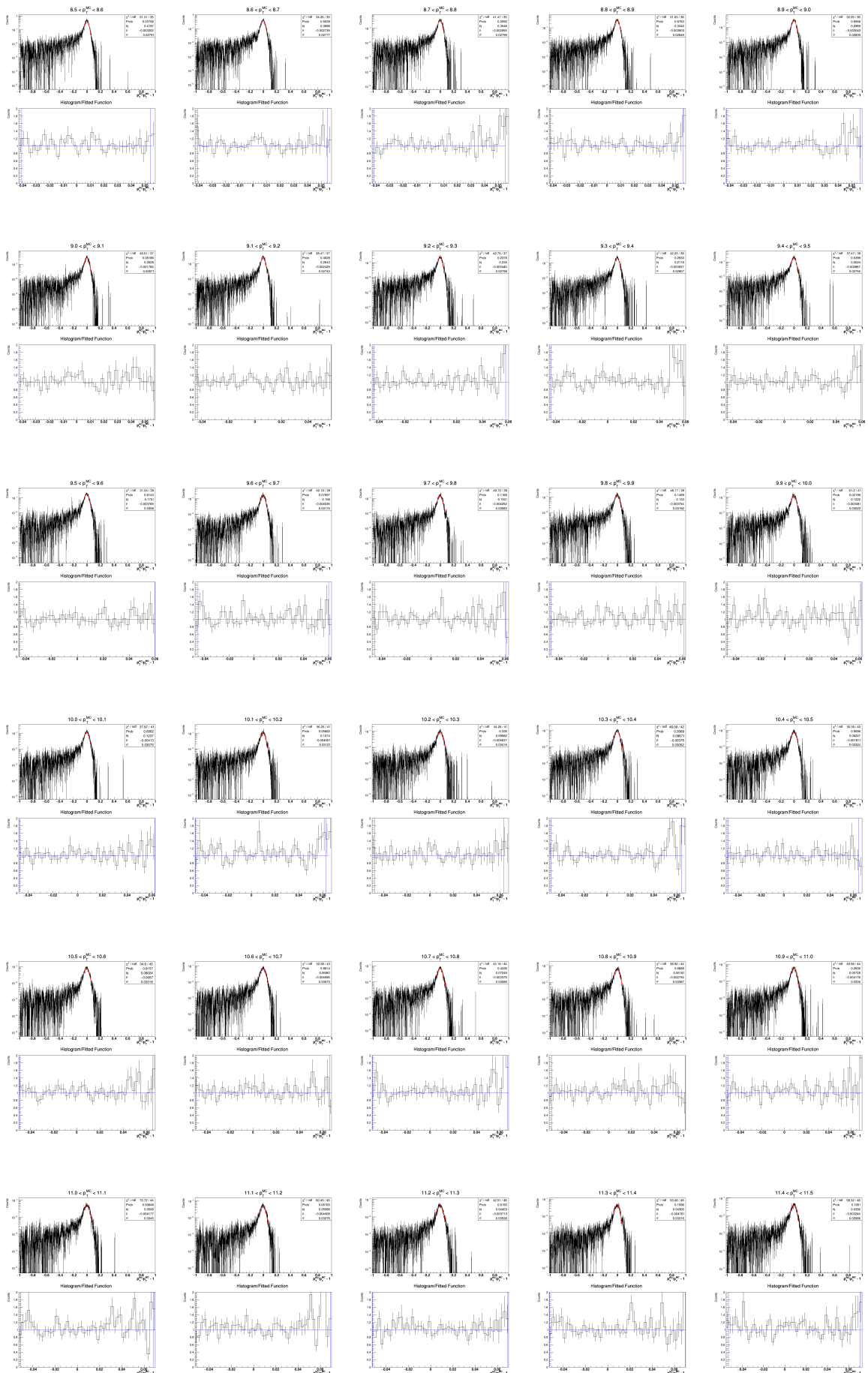
864

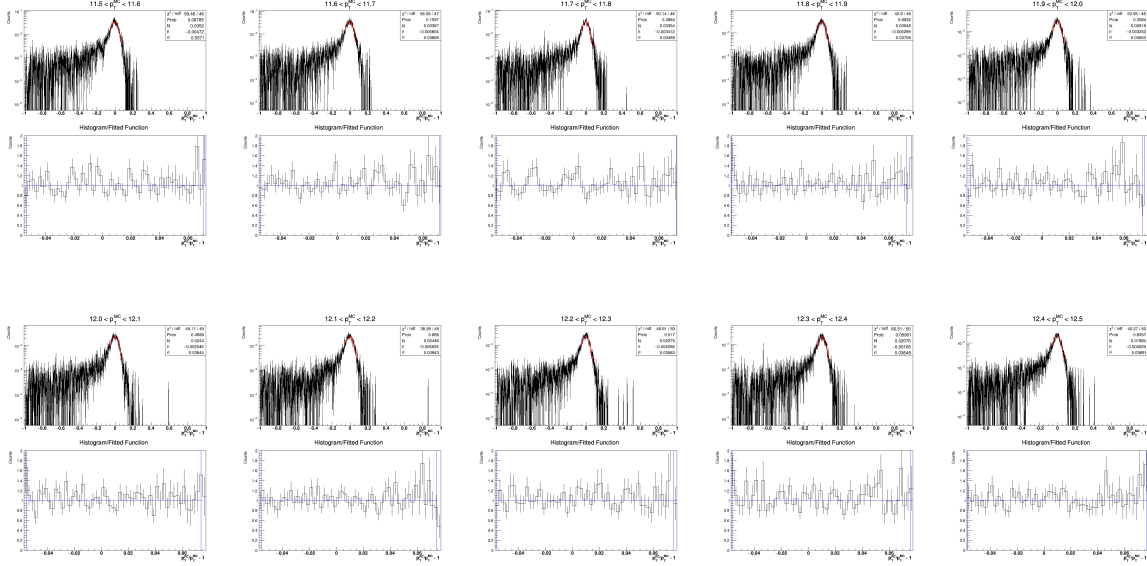
p+p











865 **p+Au**

## 866 7.4 p+p Cross Section - Results Combination

867 The inclusive  $J/\psi$  cross section in p+p collision result from this analysis is combined with measure-  
 868 ments using data taken in year 2009 (Run09) and 2012 (Run12). The combined result is reported in the  
 869 paper. The Run09 results utilize the BHT0 and BHT3 triggers, while the Run12 utilize MB, BHT0 and  
 870 BHT2 triggers.

871 The method used is called “Best Linear Unbiased Estimate” (BLUE). It minimize the total variance  
 872 (best), under the condition that the combined result is a weighted sum of each measurement (linear),  
 873 while also keeping the sum of the weights is 1 (unbiased). The physics quantity undergoes the BLUE  
 874 method is the yield. The yield in each  $p_T$  bin is combined independently. After getting the combined  
 875 yield as a function of  $p_T$ , the combined invariant yield (equivalently the cross section) is calculated and  
 876 the  $p_T$  position is decided in the same way as in this analysis.

877 The total variance is the sum of different variance entries. Each of the variance entries is calcu-  
 878 lated with an uncertainty entry, e.g. the statistical, various systematic or normalization uncertainties.  
 879 Different uncertainty entries are assumed to be mutually independent between each other by design.  
 880 Correlation between measurement from 3 dataset is considered when calculating each uncertainty entry.  
 881 In general, statistical, data driven systematic uncertainties are assumed to be uncorrelated, while the  
 882 rest is conservatively assumed to have correlation coefficient of 1.

883 In each  $p_T$  bin, the total variance  $\Delta^2$  is given by:

$$884 \Delta^2 = \Sigma_i (\sigma_i^T P_i \sigma_i) \quad (1)$$

885 where  $i$  identifies different uncertainty entries, column vector  $\sigma_i$  is defined to simplify the right hand side  
 886 of the above equation by:

$$887 \sigma_i = \begin{pmatrix} w_{09} \delta_{09,i} \\ w_{12} \delta_{12,i} \\ w_{15} \delta_{15,i} \end{pmatrix} \quad (2)$$

888 and  $P_i$  is the correlation matrix:

$$889 P_i = \begin{pmatrix} 1 & \rho_{09-12,i} & \rho_{09-15,i} \\ \rho_{12-09,i} & 1 & \rho_{12-15,i} \\ \rho_{15-09,i} & \rho_{15-12,i} & 1 \end{pmatrix} \quad (3)$$

890  $w_{year}$  is the weight assigned to the year,  $\delta_{year,i}$  is the uncertainty value corresponds to  $i$  and year, and  
 891  $\rho_{yearX-yearY,i} = \rho_{yearY-yearX,i}$  is the correlation coefficients between year X and year Y. As discussed,  
 892  $\rho_{X,Y,i} = 0$  when  $i$  corresponds to statistical and data driven systematic uncertainties, while  $\rho_{X,Y,i} = 1$   
 893 for the rest uncertainties. The weights satisfy:  $w_{09} + w_{12} + w_{15} = 1$ . By substitute  $w_{15} = 1 - w_{09} - w_{12}$ ,  
 894  $\Delta^2$  becomes a binary function of  $w_{09}$  and  $w_{12}$ . Since all the uncertainty entries are in the publication,

892 and all the correlation coefficients has got an educated guess, the problem is simply finding the local  
 893 minimum of  $\Delta^2(w_{09}, w_{12})$  within  $w_{09} \geq 0, w_{12} \geq 0, w_{09} + w_{12} \leq 1$ .

894 The difference in analysis procedure and aspects taken into account when calculating the systematic  
 895 uncertainties between the 3 measurement complex the combination. The following lists all the special  
 896 treatment in this combination practice.

897

898 **Absent of Estimation** Some of systematic uncertainties are not estimated in all three analyses. In  
 899 the case where the entry is not of concern, e.g. TOF related systematic uncertainties for Run09 and  
 900 Run15 where TOF is not used, those absent uncertainties are naturally assigned to be 0. For the  
 901 rest, an dedicated way to guess is established based on uncertainties from the “estimated year(s)” and  
 902 combination weights, so that it will not bias the relative combined uncertainty. Specifically, for single-  
 903 year absent case, the assigned value is essentially the relative uncertainty of the combined result of other  
 904 2 years with the given weights, while for dual-year absent case, i.e. the estimation is only given in one  
 905 analysis, this estimation on relative uncertainty is simply copied to the other runs.

906 **Assymmetric Uncertainty** The only case is the raw yield (RY) estimation uncertainty in Run09. One  
 907 needs to construct the contribution related to Run09 reasonably. The solution is to replace the Run09  
 908 data (with assymmetric uncertainty) with 2 “pseudo-data” (with symmetric uncertainty, corresponding to  
 909 the lower and higher limit respectively), each carrying a weight of  $\frac{w_{09}}{2}$ . The 2 “pseudo-data” is assumed to  
 910 have correlation coefficients of 1 between each other. This happens to convey the “unbiased” assumption  
 911 in the BLUE. The contribution in total variance that is solely related to Run09 is given by:

$$\begin{aligned} & \left(\frac{w_{09}}{2} \cdot \delta_{RY,low}\right)^2 + \left(\frac{w_{09}}{2} \cdot \delta_{RY,high}\right)^2 + 2 \cdot \left(\frac{w_{09}}{2} \cdot \delta_{RY,low}\right) \cdot \left(\frac{w_{09}}{2} \cdot \delta_{RY,high}\right) \\ & = w_{09}^2 \left(\frac{\delta_{RY,low} + \delta_{RY,high}}{2}\right)^2 \end{aligned} \tag{4}$$

912 which happens to equal to the result if one takes the average of the 2 uncertainties that correspond  
 913 to the lower and higher limit. Similarly, the contribution that reflects the correlation between Run09  
 914 and the other runs also takes the form of taking the average of the uncertainty correspond to the lower  
 915 and higher limits. This replacement allow us to obtain the weights with the BLUE method, then the  
 916 combined RY uncertainty entry for the lower and higher limit is calculated using  $w_{09}$  of  $\delta_{RY,low}$  and  $w_{09}$   
 917 of  $\delta_{RY,high}$  to calculate , respectively.

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919 These plots are simply overlaying the results from this analysis with published data.

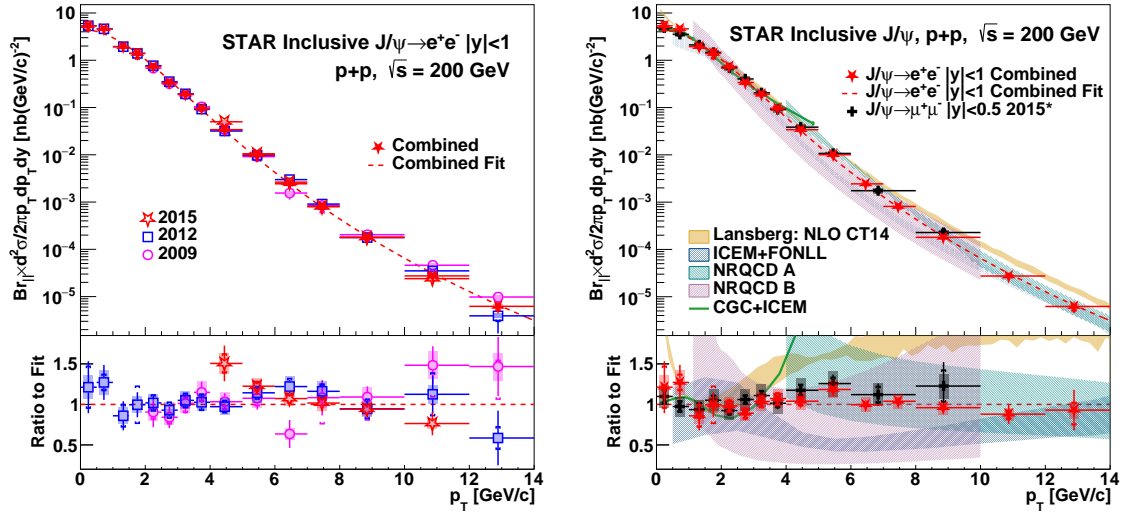


Figure 14: Inclusive  $J/\psi$  cross section as a function of  $p_T$  in p+p collisions at  $\sqrt{s} = 200$  GeV and comparison to STAR  $J/\psi \rightarrow \mu^+\mu^-$  measurement for  $|y| < 0.5$  at the same  $\sqrt{s}$  and to various model calculations for  $|y| < 0.5$ . Notice the “\*” marker indicates that the dimuon measurement is corrected for the rapidity coverage from  $|y| < 0.5$  to  $|y| < 1$ . This analysis (2015) is combined with 2 other published STAR  $J/\psi \rightarrow e^+e^-$  results with data taken in 2009 and 2012. The vertical bars represent the statistical uncertainties, while the brackets and transparent boxes represent the systematic uncertainty that is uncorrelated and correlated between  $p_T$  bins, respectively. The horizontal bars represent the bin width. The dashed line is a fit to the combined.

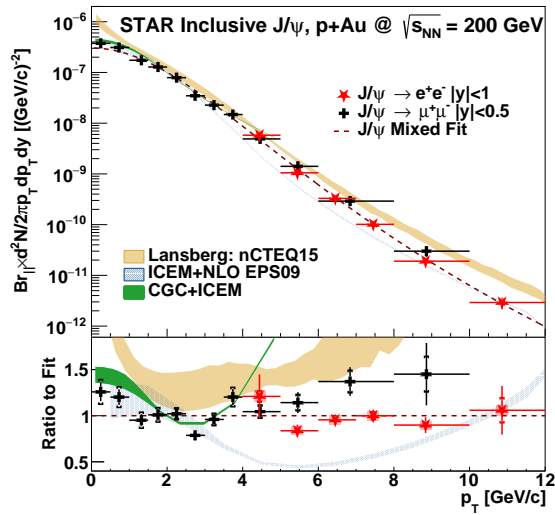


Figure 15: Inclusive  $J/\psi \rightarrow e^+e^-$  invariant yield as a function of  $p_T$  in p+Au collisions at  $\sqrt{s_{NN}} = 200$  GeV and comparison to STAR  $J/\psi \rightarrow \mu^+\mu^-$  measurement for  $|y| < 0.5$  at the same  $\sqrt{s_{NN}}$ , and to various model calculations. The dashed line is a mixed fit to dielectron and dimuon channel results, covering  $p_T$  range of 4–12 GeV/c and 0–4 GeV/c respectively. The representation of uncertainties and bin width is identical to Fig. 14.



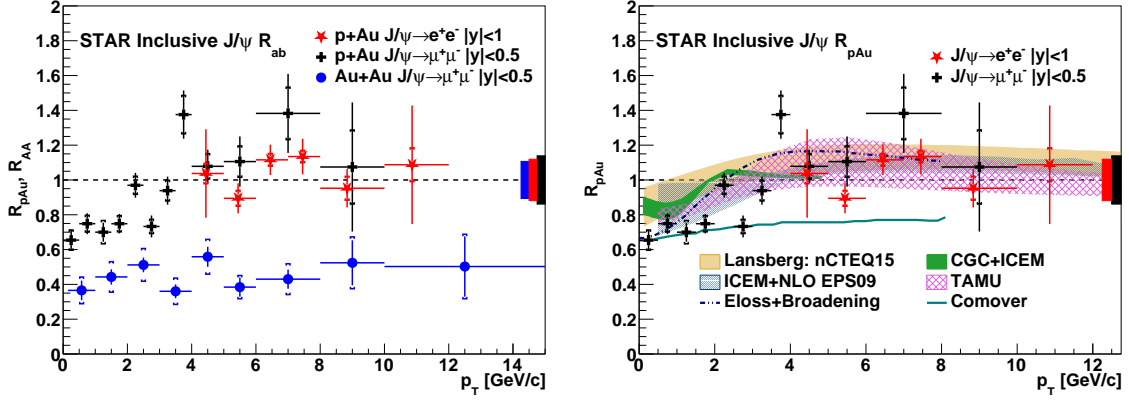


Figure 16: Inclusive  $J/\psi \rightarrow e^+e^-$   $R_{pAu}$  compared to the  $J/\psi \rightarrow \mu^+\mu^-$   $R_{pAu}$  as well as the  $R_{AA}$  in 0-20% central Au+Au collisions at the same  $\sqrt{s_{NN}}$ , and comparison on  $R_{pAu}$  between STAR  $J/\psi$   $R_{pAu}$  measurements dielectron and dimuon channel with various model calculations. The representation of uncertainties and bin width is identical to Fig. 14, with the exception of correlated uncertainties between  $p_T$  bins are represented by the boxes of the corresponding color around unity.