



Measurements of $d-\Lambda$ correlations from STAR

Yu Hu (胡昱)

for the STAR collaboration

Lawrence Berkeley National Laboratory

15th Workshop on Critical Point and Onset of Deconfinement

Scientific Program

- *Critical Point
- *Phase Transitions
- *Deconfined Matter
- *Hadronization
- *Compact Stars
- *Experimental Facilities, Detector and Methods
- *Next Generation Methods in Data Analysis

CPOD 2024

LOC: X. Dong, V. Koch*, G. Odianes, N. Xu*
Conference Coordinator: L. Bonifacio

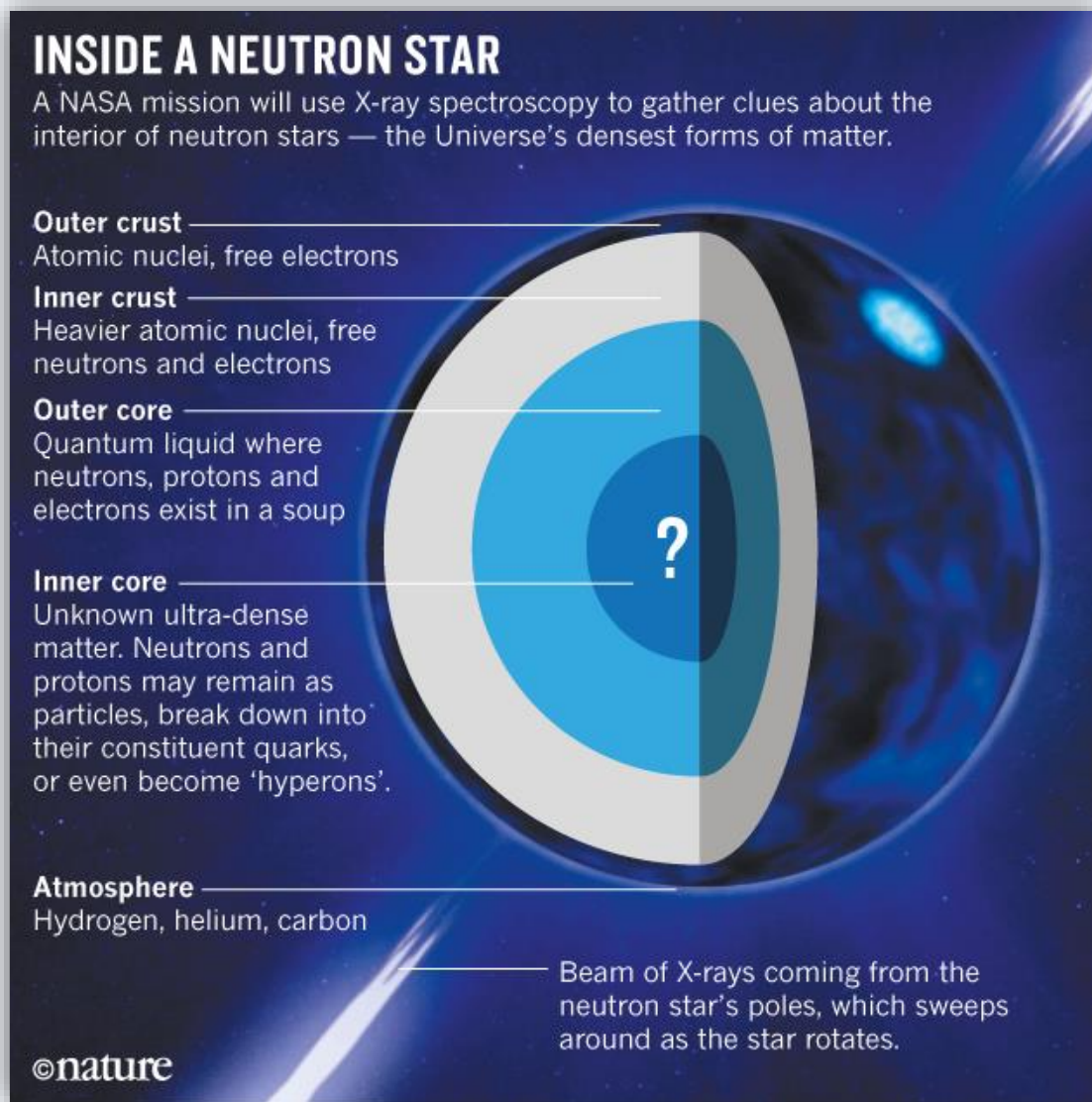
Berkeley, CA, May 20-24



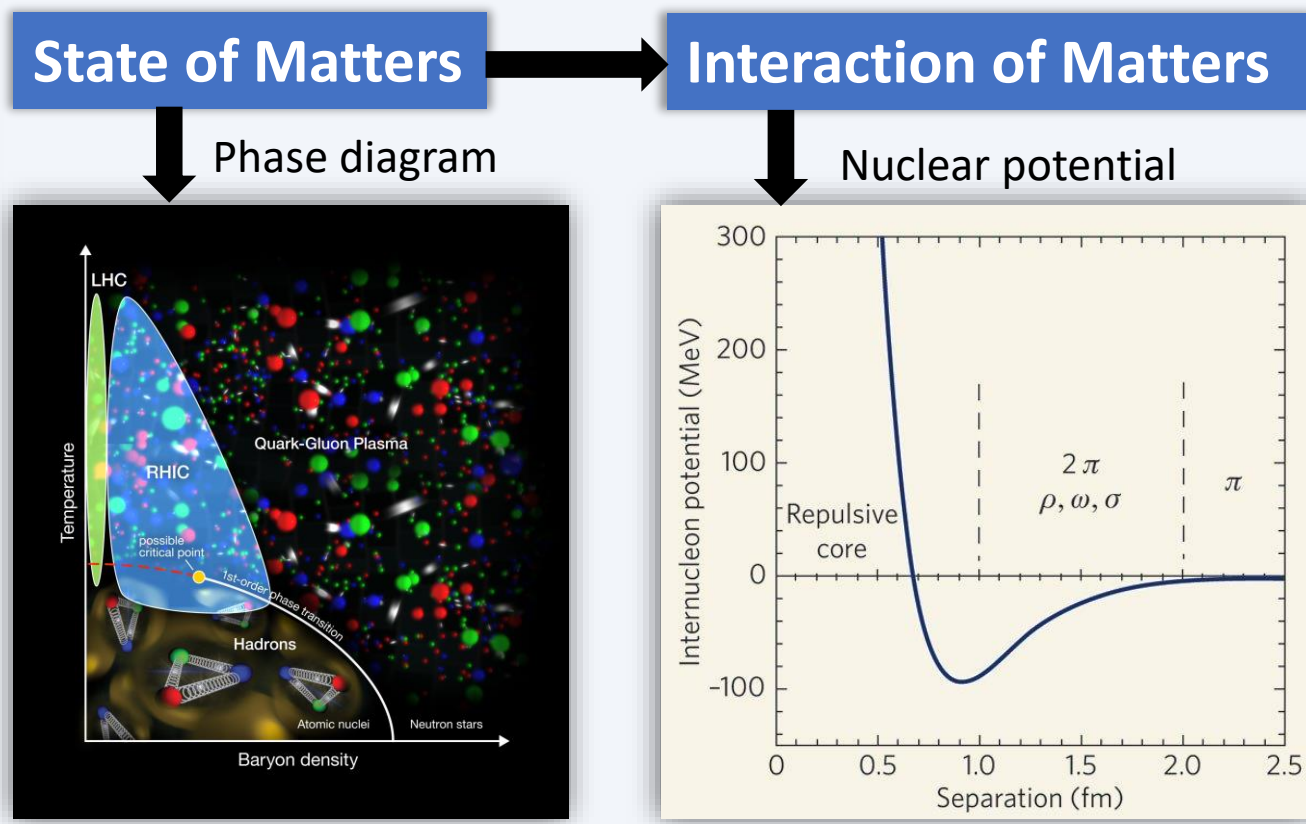
Outlines

- ❖ Introductions & Lednicky-Lyuboshitz (L-L) approach
- ❖ Particle identification
- ❖ p- Λ & d- Λ correlation function
 - ❖ Source size with L-L approach
 - ❖ Correlation function & spin states
 - ❖ Scatterings length (f_0) and effective range (d_0)
 - ❖ Λ separation energy of ${}^3_{\Lambda}\text{H}$
- ❖ Summary & Outlooks

QCD Dense Matter & Nucleon-Nucleon/Hyperon Interactions



Credit: Source: Adapted from NASA Goddard SVS
Nature volume 546, page18 (2017)



- ❖ Structure of nuclear and hyper-nuclei matter
- ❖ Role of Nucleon-Nucleon (N-N) and Hyperon-Nucleon (Y-N) interactions in the Equation-of-State

<https://www.bnl.gov/newsroom/news.php?a=219079>
<https://www.quora.com/What-does-the-potential-function-for-the-strong-nuclear-force-look-like>

Low-E scattering experiment & Effective Range Expansion

Low energy elastic scatterings:

$$k \cot(\delta(k)) = -\frac{1}{a} + \frac{1}{2}r_0k^2 + O(k^4)$$

$\delta(k)$: phase shift

a : Fermi scattering length at zero energy

r_0 : effective range

O : higher order contribution

Cross section:

$$\lim_{k \rightarrow 0} \sigma_e = 4\pi a^2$$

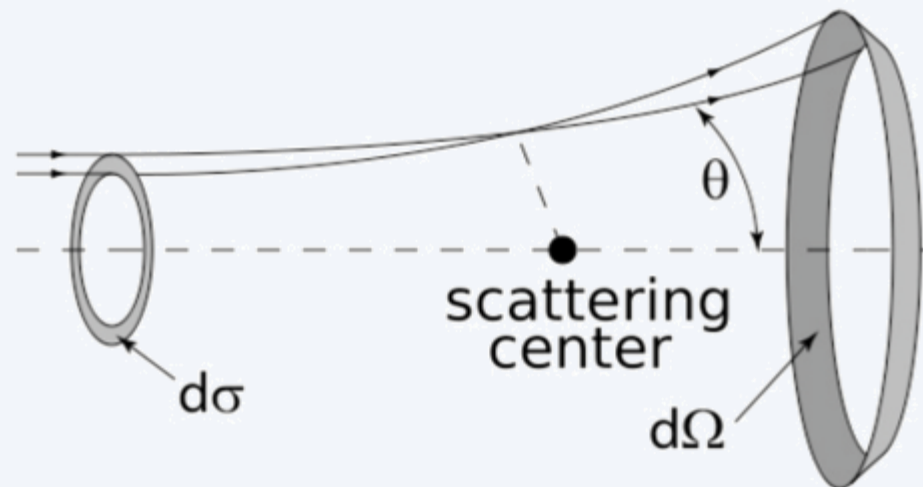
Binding energy:

$$\frac{1}{a} = \gamma - \frac{1}{2}r_0\gamma^2$$

❖ $B = \frac{\gamma^2}{2\mu}$

❖ μ : reduced mass

❖ γ : binding momentum



H. A. Bethe, *Phy. Rev.* 76 (1949) 38

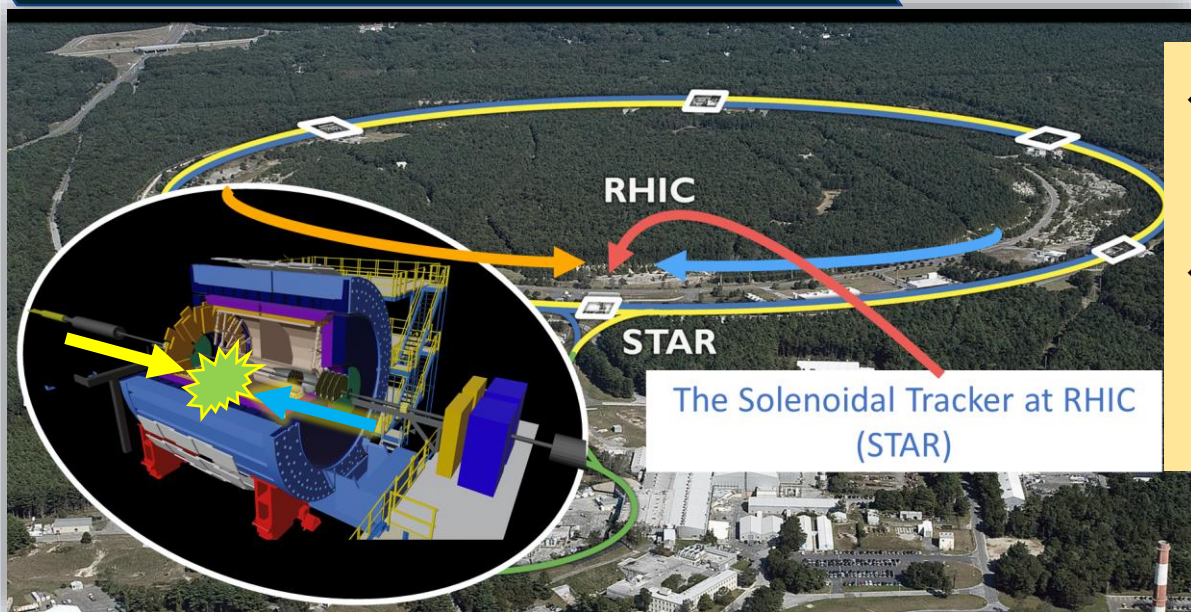
For the n-p scattering:

$$S_0: \quad a = -23.714 \text{ fm} \quad r_0 = 2.73 \text{ fm}$$

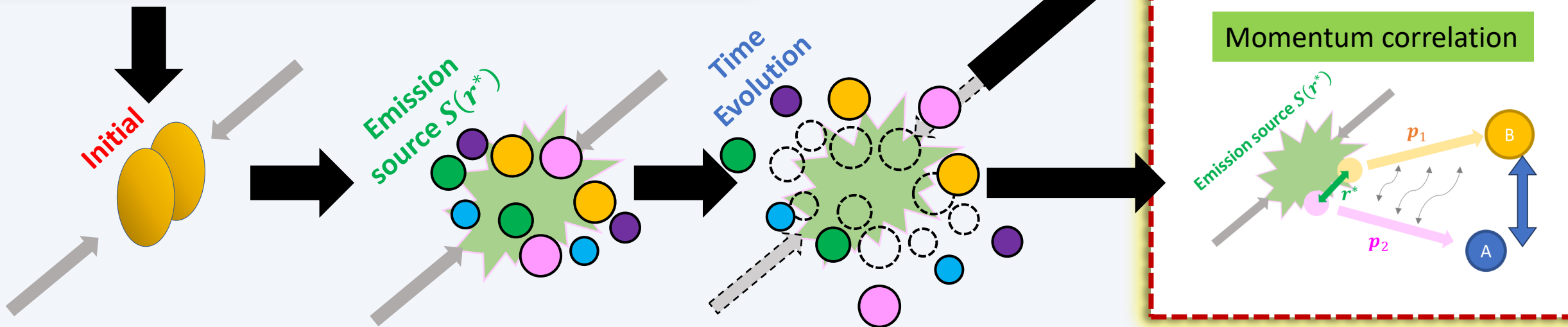
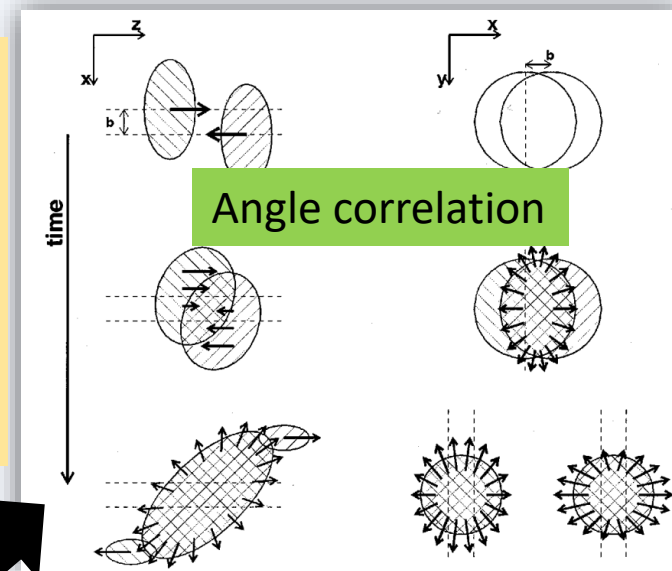
$$S_1: \quad a = 5.425 \text{ fm} \quad r_0 = 1.749 \text{ fm}$$

➡ $B_d = 2.2 \text{ MeV}$

Heavy Ion Collision Experiment



- ❖ Space and time evolution of particle-emitting source
- ❖ Final state interactions
 - ❖ N(-N)-Y interactions
 - ❖ hypernuclei structure



Baryon Correlation Function (CF)

Statistical

Momentum correlation function:

$$C(\mathbf{p}_1, \mathbf{p}_2) \equiv \frac{P(\mathbf{p}_1, \mathbf{p}_2)}{P(\mathbf{p}_1) \cdot P(\mathbf{p}_2)}$$

Single-particle
momentum

Experimental

$$C(k^*) = \mathcal{N} \frac{A(k^*)}{B(k^*)}$$

Same events

Mixed events

Normalization factor

k^* : particle momentum in the pair rest frame

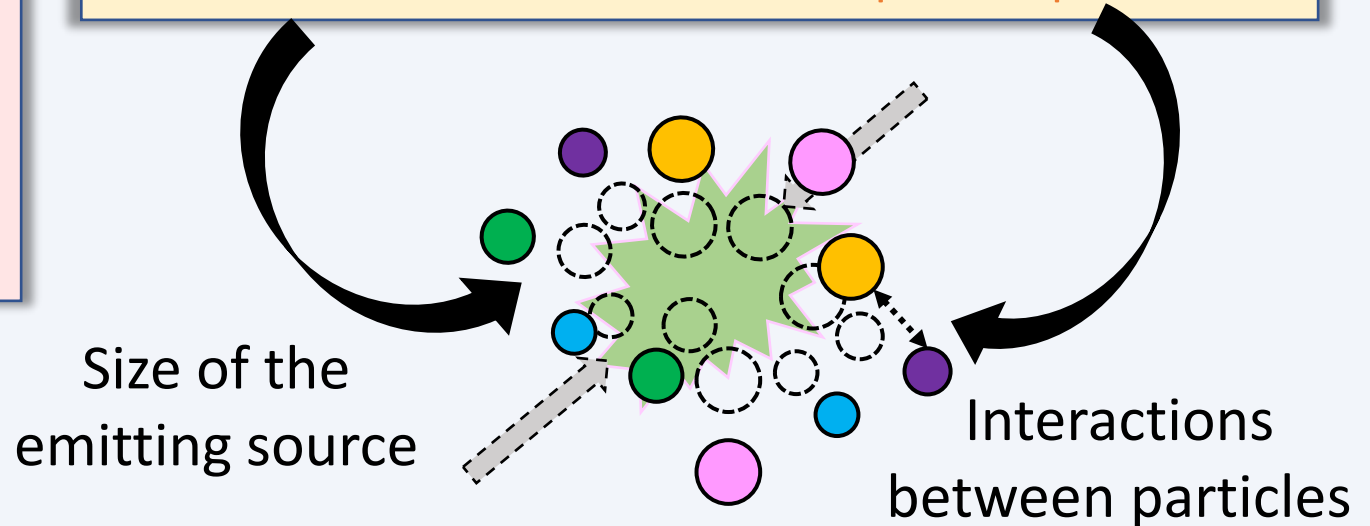
Modeling

Approximating the emission process
and the momenta of the particles:

$$C(k^*) = \int d^3r^* S(\mathbf{r}^*) |\Psi(\mathbf{r}^*, \mathbf{k}^*)|^2$$

Distribution of the
relative distance of
particle pair

Relative wave
function of the
particle pair



Lednicky-Lyuboshitz (L-L) Approach

Approximating the emission process and the momenta of the particles:

Modeling

$$C(\mathbf{k}^*) = \int d^3r^* S(\mathbf{r}^*) |\Psi(\mathbf{r}^*, \mathbf{k}^*)|^2$$

Distribution of the relative distance of particle pair

Relative wave function of the particle pair

Major Assumptions

Source

- ❖ Smoothness approximation for source function*
- ❖ Static and spherical Gaussian source
 - Single particle source: $S_i(x_i, p_i^*)$
 - Pair source (radius R_G): $S(x, p^*) \propto e^{-x^2/2R_G^2} \delta(t - t_0)$

Wave function

- ❖ S-wave scattering wave
- ❖ Effective range expansion for $\Psi(\mathbf{r}^*, \mathbf{k}^*)$
- ❖ Approximate the wave function by its asymptotic form

Gaussian source approximation:

$$S(\mathbf{r}^*) = (2\sqrt{\pi}R_G)^{-3} e^{-r^{*2}/4R_G^2}$$

Scattering amplitude:

Consider only S-wave $\Psi(r^*) = e^{-ir^* \cdot k^*} + \frac{f(k^*)}{r^*} e^{ir^* \cdot k^*}$

$$f(k^*) \approx \left(\frac{1}{f_0} + \frac{d_0 k^{*2}}{2} - ik^* \right)^{-1}$$

Scattering length:

$$a \rightarrow -f_0$$

Effective range:

$$r_0 \rightarrow d_0$$

Lednicky-Lyuboshitz (L-L) approach

R_G : spherical Gaussian source of pairs

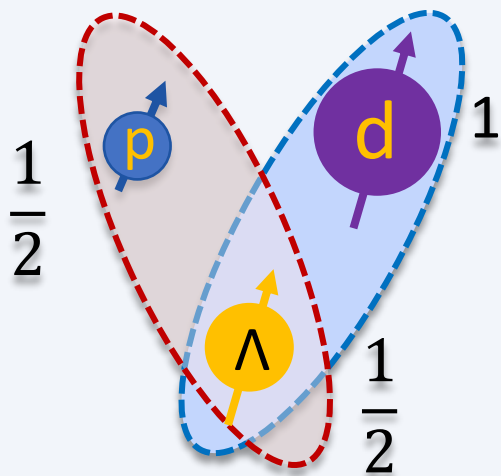
f_0 : scattering length

d_0 : effective range

*The smoothness approximation has been checked for expanding thermal sources, found to be very reasonable for large (RHIC-like) sources, but still questionable for smaller sources

Modeling with Separated Spin States

Singlet State	1S_0	(S)
Triplet State	3S_1	(T)



Doublet State	$^2S_{1/2}$	(D)
Quartet State	$^4S_{3/2}$	(Q)

Approximating the emission process and the momenta of the particles:

$$C(\mathbf{k}^*) = \int d^3r^* S(\mathbf{r}^*) |\Psi(\mathbf{r}^*, \mathbf{k}^*)|^2$$

Source Wave function

Modeling

Spin averaged

$|\Psi(\mathbf{r}^*, \mathbf{k}^*)|^2$ expanded with averaged parameters: \bar{f}_0 and \bar{d}_0

$$|\Psi(\mathbf{r}^*, \mathbf{k}^*)|^2 \rightarrow f_{S1} |\Psi_{S1}(\mathbf{r}^*, \mathbf{k}^*)|^2 + f_{S2} |\Psi_{S2}(\mathbf{r}^*, \mathbf{k}^*)|^2$$

Spin separated

$$C(\mathbf{k}^*) = \int d^3r^* S(\mathbf{r}^*) \left(\frac{1}{3} |\Psi_{1/2}(\mathbf{r}^*, \mathbf{k}^*)|^2 + \frac{2}{3} |\Psi_{3/2}(\mathbf{r}^*, \mathbf{k}^*)|^2 \right)$$

For separated spin states in d- Λ

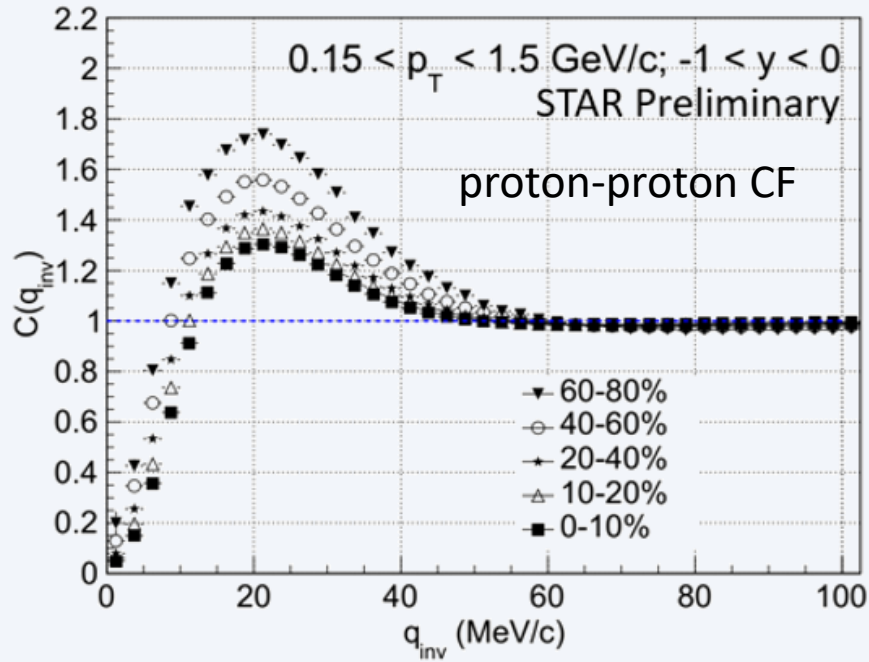
$f_0(D)$

$d_0(D)$

$f_0(Q)$

$d_0(Q)$

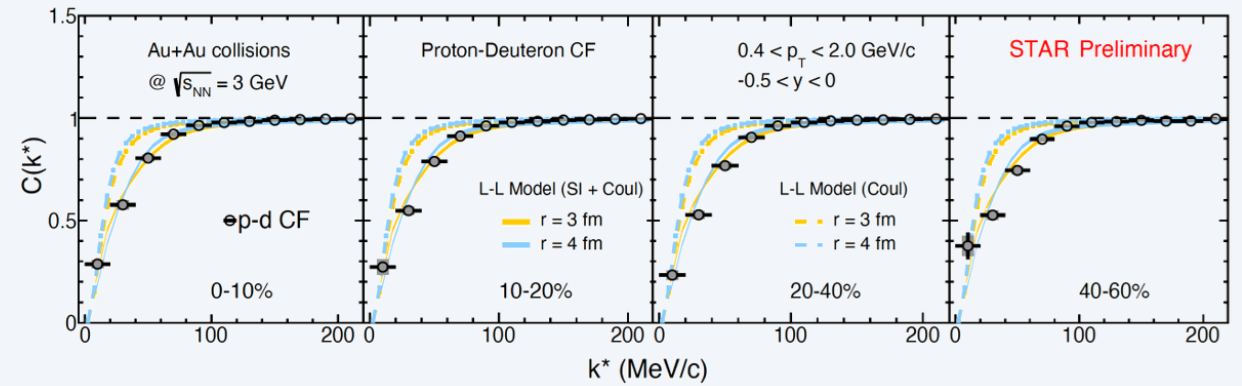
Correlation Function & Low-E Scattering Experiment



CF & low-E scattering results are consistent

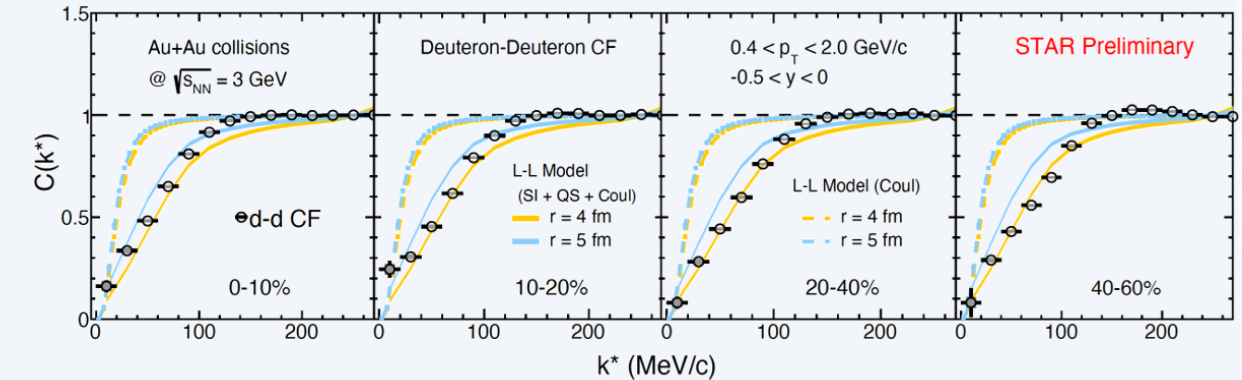
Correlation indicate strong interaction $f_0 \sim 7$ fm
 Low-E experiment found $a = -7.806 \pm 0.003$ fm

A valid method to study the interaction between baryons



Consistent with L-L model with Coulomb + repulsive interaction

Models	p-d	f_0 (fm)	d_0 (fm)	d-d	f_0 (fm)
	Doublet	-2.73	2.27	Singlet	-10.2
	Quartet	-11.88	2.63	Quintet	-7.5



Consistent with L-L model with Coulomb + QS + repulsive interaction

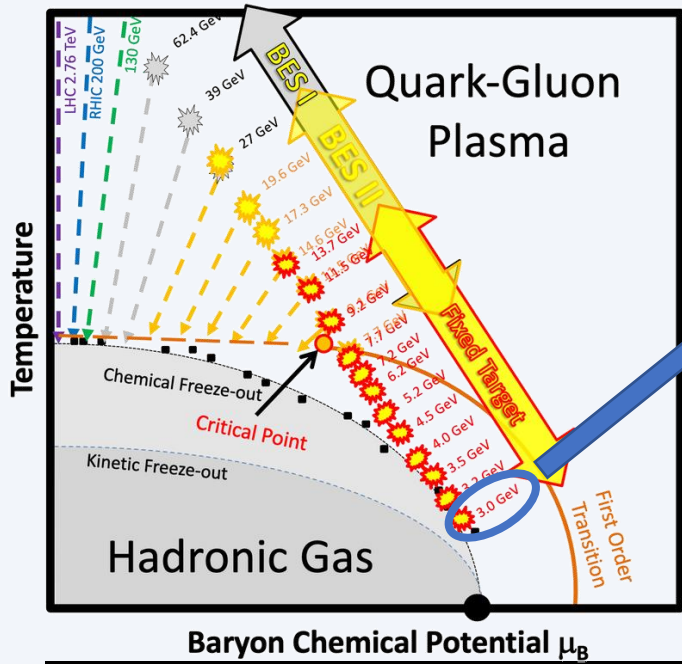
Ongoing studies @ STAR

J. Arvieux, NPA 221 (1974) 253

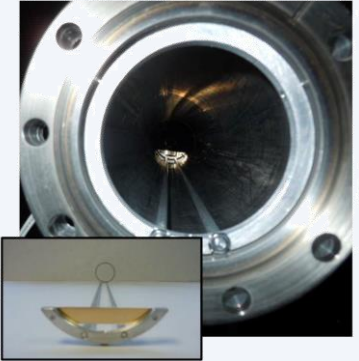
I.N. Filikhin and S.L. Yakovlev, Phys. Atom. Nucl. 63 (2000) 55 / 216

Robert B. Wiringa, et. al, Phys.Rev.C 51 (1995) 38-51

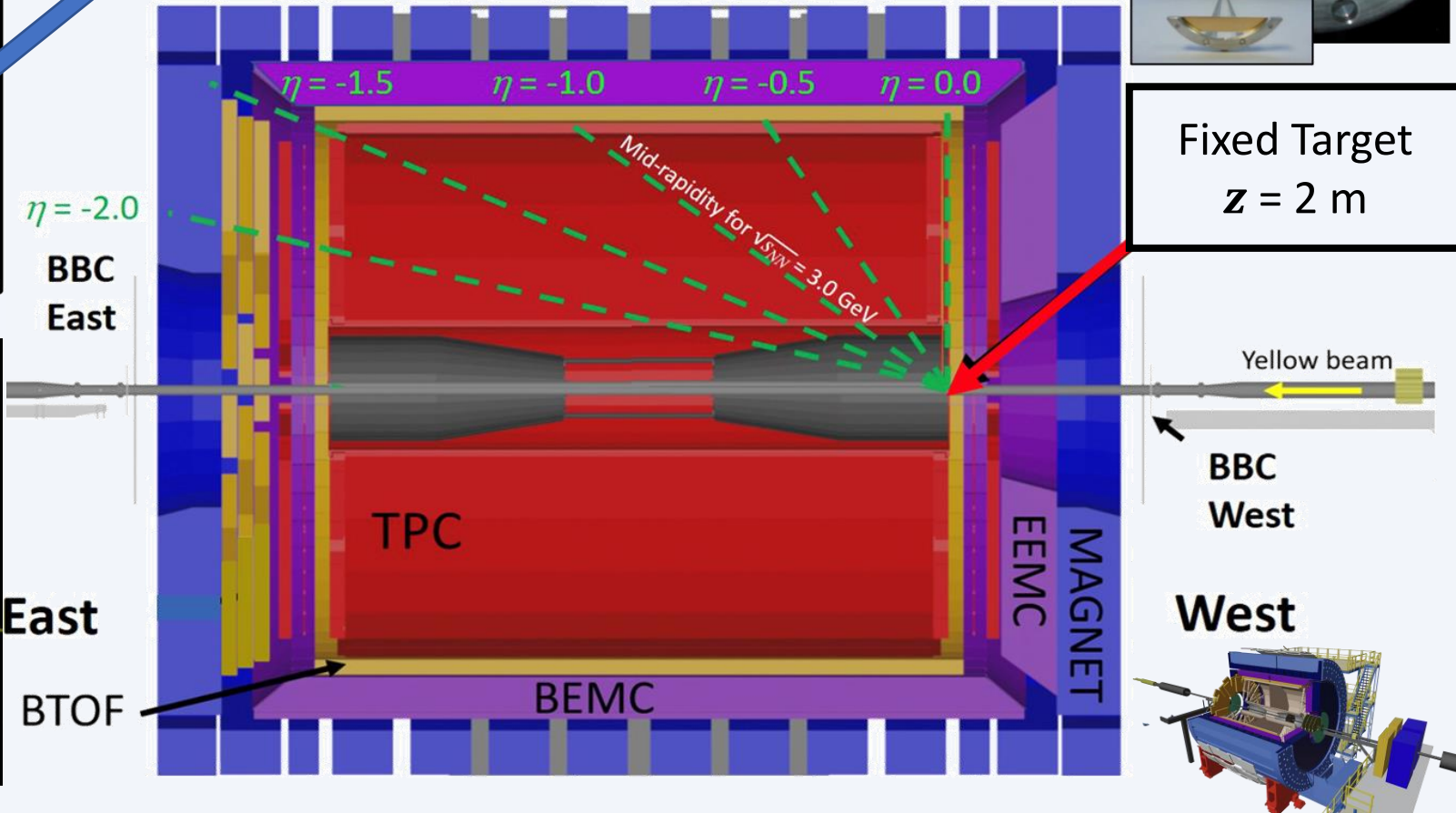
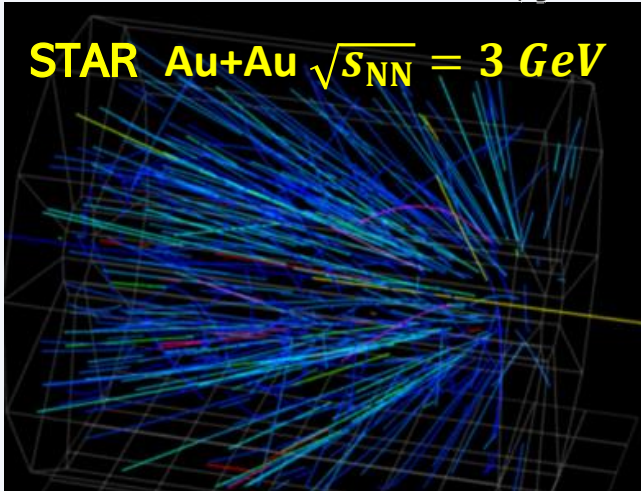
Beam Energy Scan – II & Fixed Target Setup



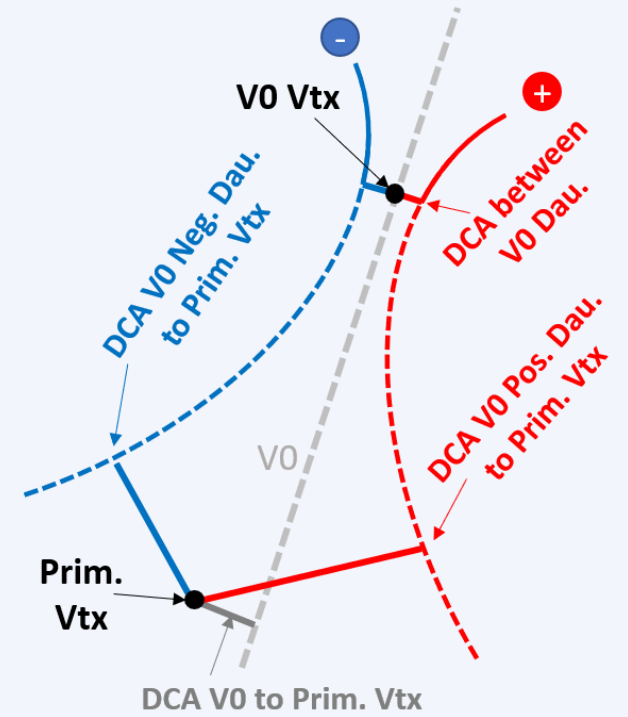
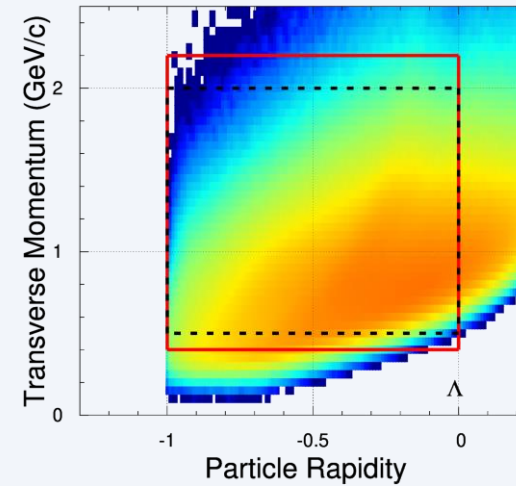
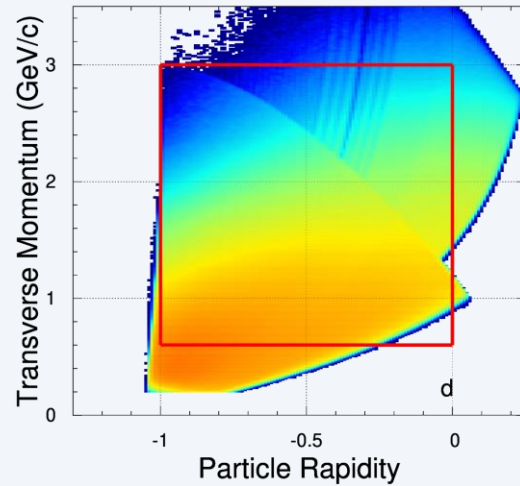
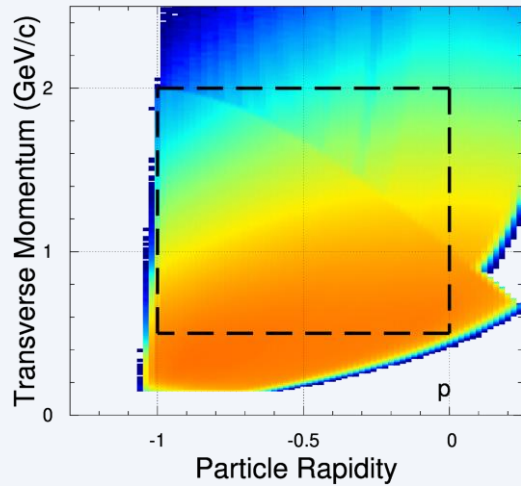
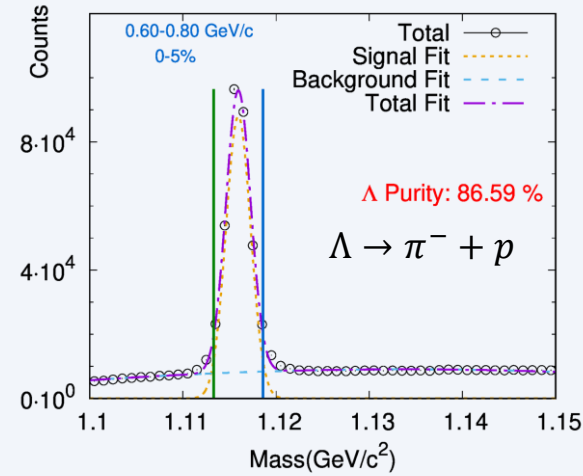
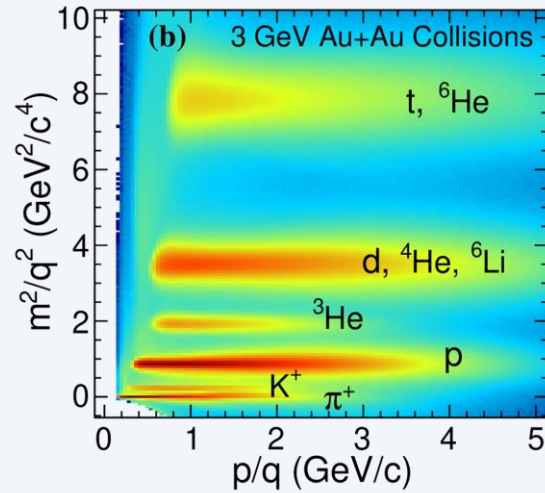
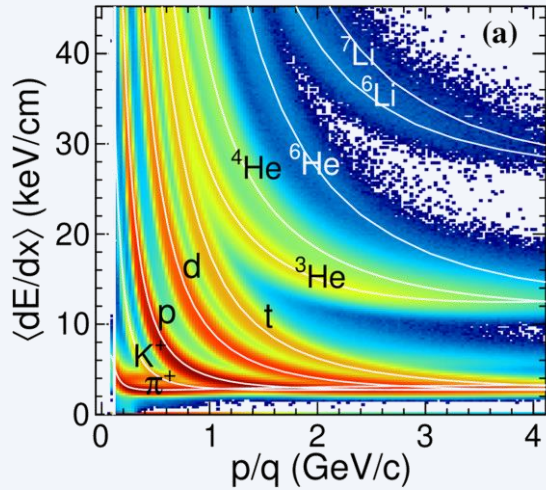
- ❖ $\sqrt{s_{NN}} = 3$ GeV Au+Au collisions $\rightarrow \mu_B \sim 750$ MeV
- ❖ 0~60% centrality, ~ 250 M events (2018)



Fixed Target
 $z = 2$ m

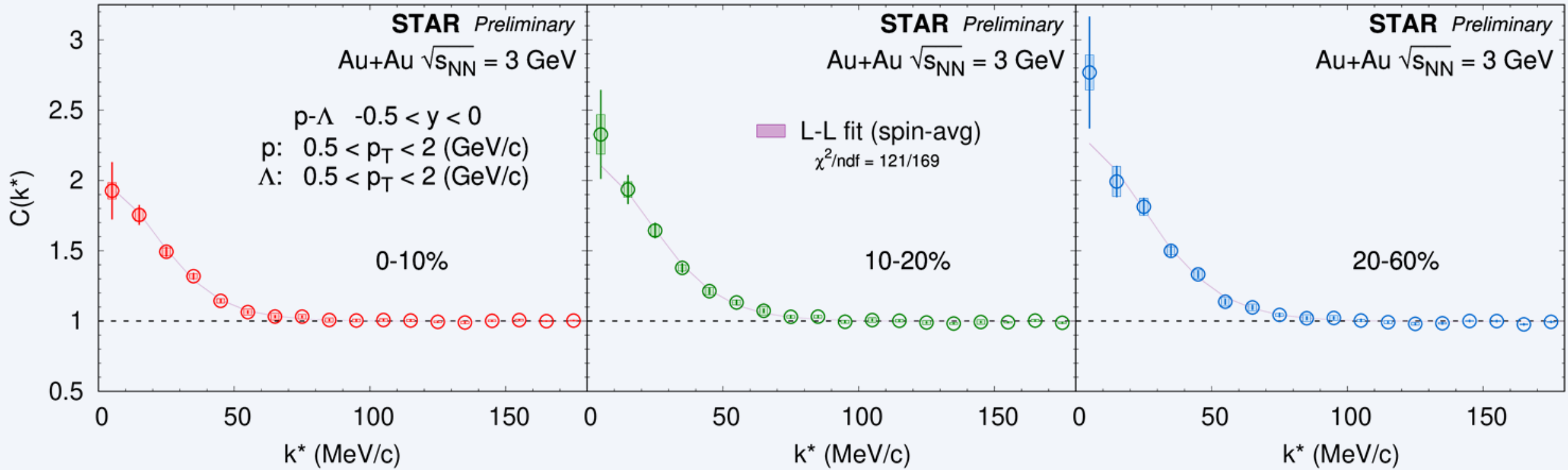


Particle Identification & Reconstruction @ 3 GeV



- ❖ π^- , p , and d particles are identified by TPC and TOF
- ❖ A larger p_T range is used in d - Λ correlation measurement (red) due to statistics

p- Λ Correlation Measurement @ STAR



Corrections

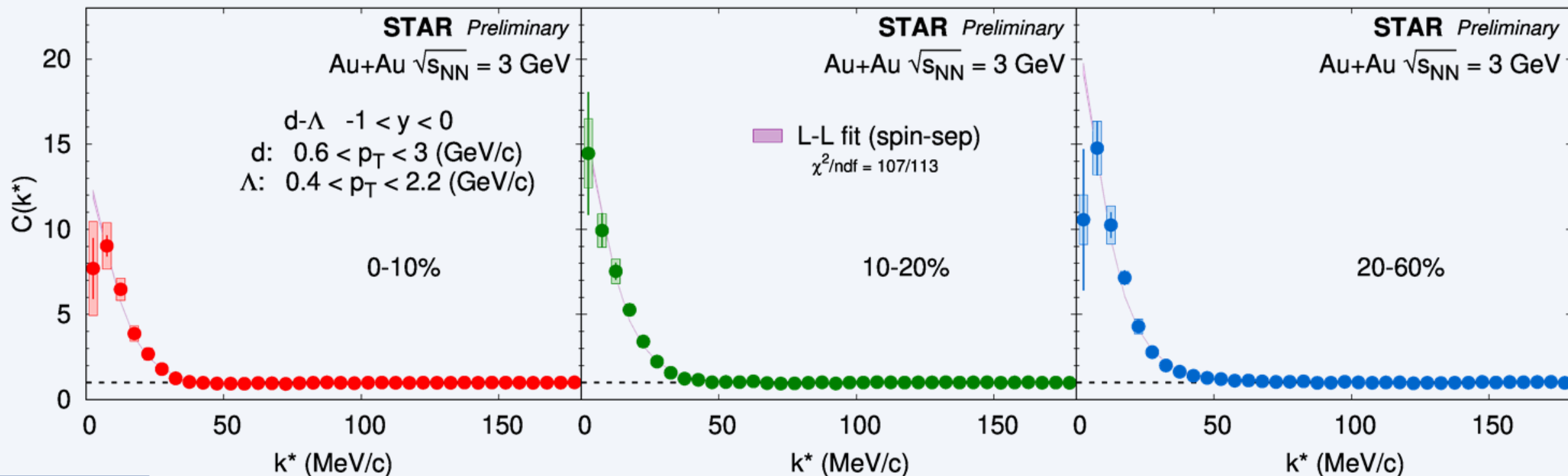
1. Purity correction
2. Λ feed-down correction
3. Track splitting & merging
4. Momentum smearing effect

- ❖ Simultaneous fit to data in different centralities/rapidity
 - ❖ R_G^i , **spin-avg** f_0 and d_0 with Lednicky-Lyuboshitz approach
- ❖ Spin-avg scattering length (f_0) and effective range (d_0):

$$f_0 = 2.32^{+0.12}_{-0.11} \text{ fm}$$

$$d_0 = 3.5^{+2.7}_{-1.3} \text{ fm}$$

d- Λ Correlation Measurement @ STAR



Corrections

1. Purity correction
2. Track splitting & merging
3. Contamination from ${}^3\text{H} \rightarrow \pi^- + p + d$ decay

- ❖ First d- Λ correlation measurements in the heavy-ion collision experiment
- ❖ Simultaneous fit to data in different centralities
 - ❖ R_G^i , $f_0(D)$, $d_0(D)$, $f_0(Q)$, and $d_0(Q)$ with Lednicky-Lyuboshitz approach

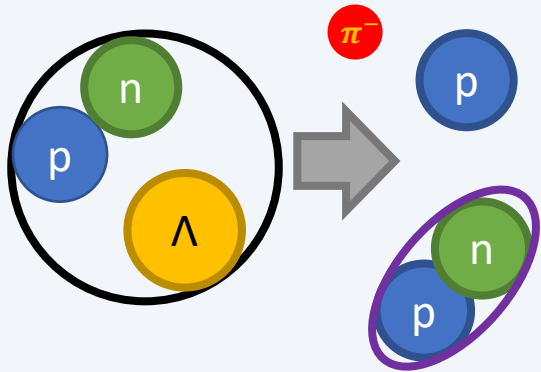
$f_0(D) = -20_{-3}^{+3}$ fm	$d_0(D) = 3_{-1}^{+2}$ fm
$f_0(Q) = 16_{-1}^{+2}$ fm	$d_0(Q) = 2_{-1}^{+1}$ fm

- ❖ Λ feed-down correction not applied due to unknown d- Σ/Ξ correlation
- ❖ Momentum smearing effect negligible

Contamination Correction from ${}^3_{\Lambda}\text{H} \rightarrow p\pi^- + d$ Decay

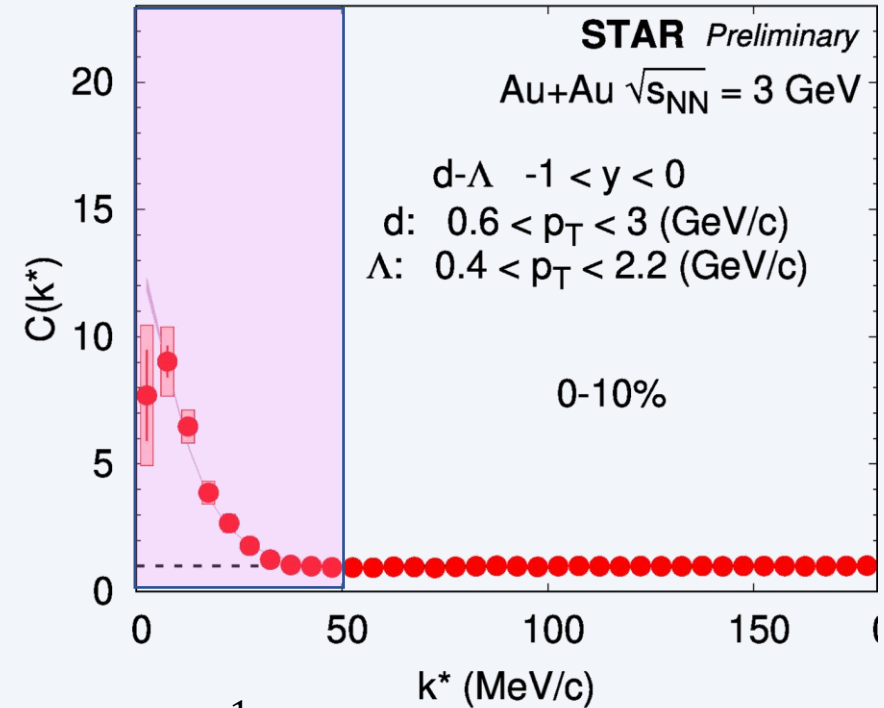
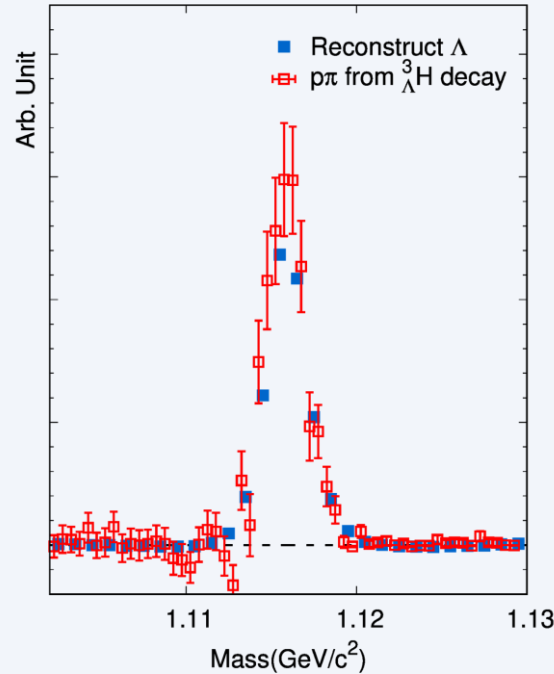
$${}^3_{\Lambda}\text{H} \rightarrow p + \pi^- + d;$$

$$B.R. \approx 40\sim 50\%$$



$${}^3_{\Lambda}\text{H} \not\rightarrow \Lambda + d$$

Violation of energy conservation



$$k^* = \frac{1}{2} |p_1^* - p_2^*|$$

$$p_1 = \frac{\sqrt{(M^2 + m_1^2 - m_2^2)^2 - 4M^2 m_1^2}}{2M},$$

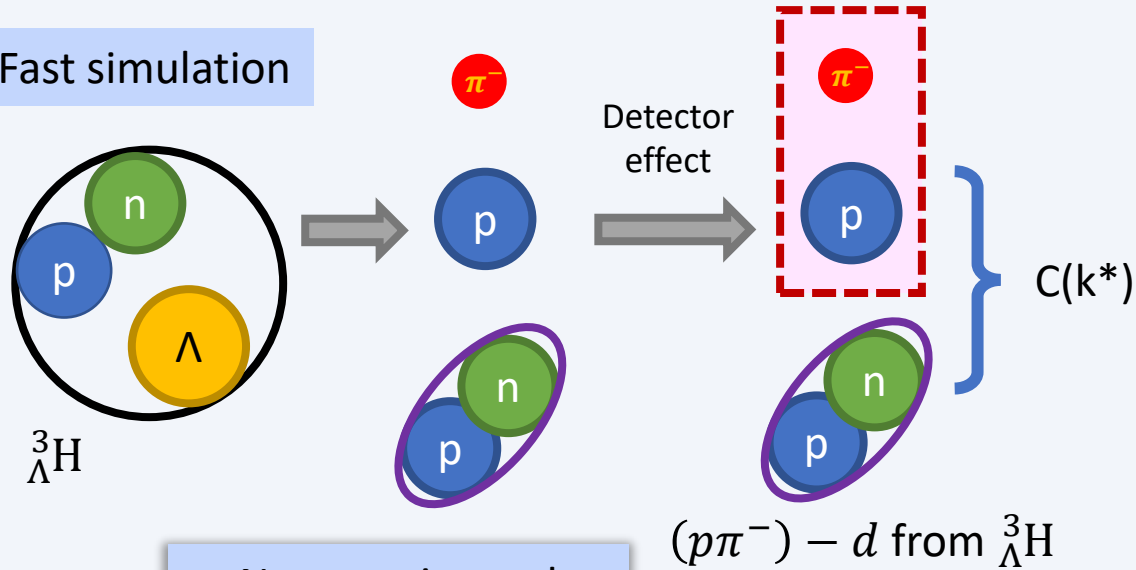
$$p_2 = \frac{\sqrt{(M^2 + m_2^2 - m_1^2)^2 - 4M^2 m_2^2}}{2M}.$$

$$p \approx 20 \text{ MeV/c} \Rightarrow k^* \approx 20 \text{ MeV/c}$$

- ❖ The ${}^3_{\Lambda}\text{H}$ decayed $p + \pi^-$ are **not experimentally distinguishable** with the reconstructed Λ
- ❖ $(p\pi^-) - d$ from ${}^3_{\Lambda}\text{H}$ will affect small k^* region

Contamination Correction from ${}^3_{\Lambda}\text{H} \rightarrow p\pi^- + d$ Decay

Fast simulation



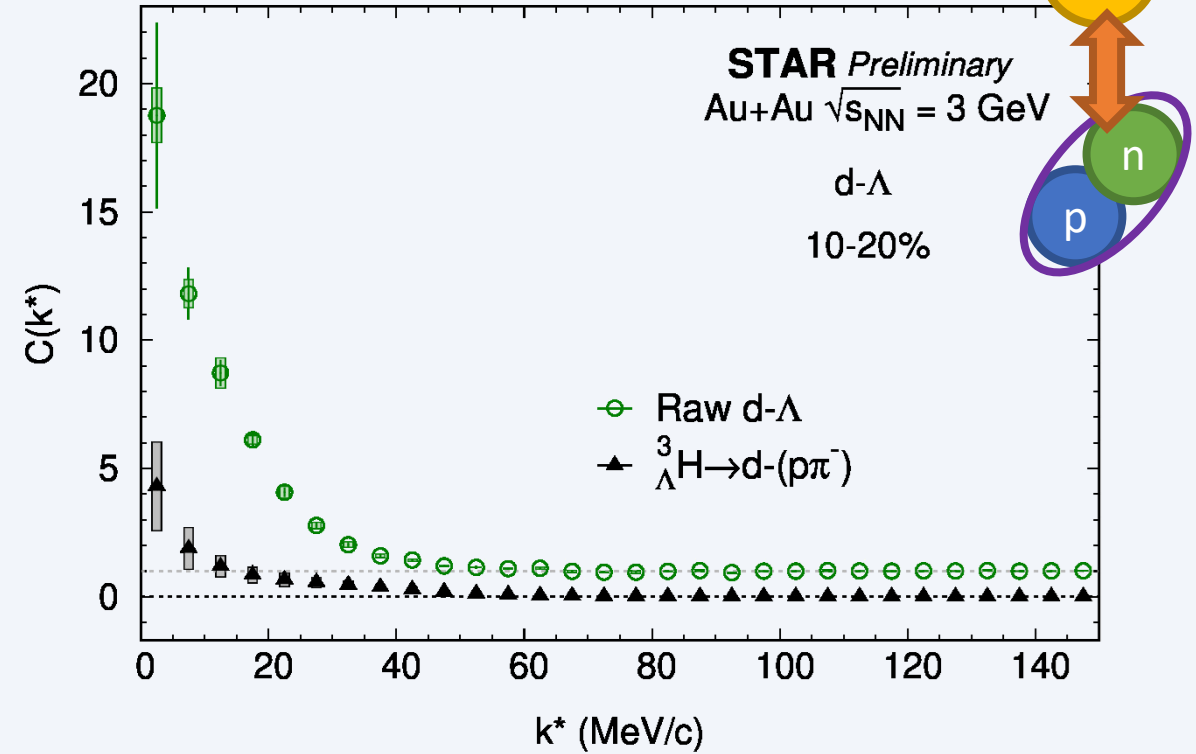
N events in total

Initial $N \cdot \text{Yield} \cdot \text{BR}$ ${}^3_{\Lambda}\text{H}$ in total

Apply different decay kinematics

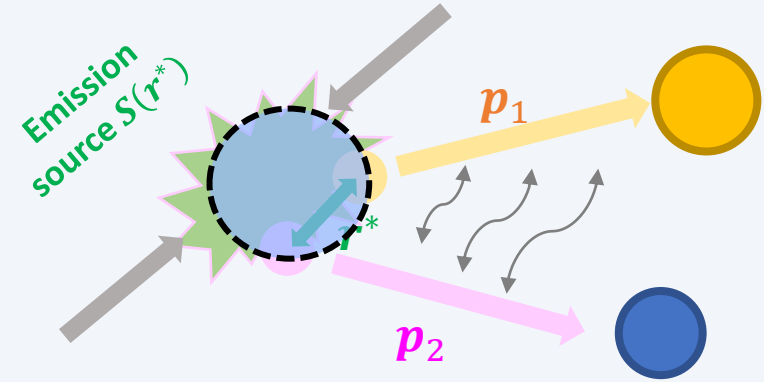
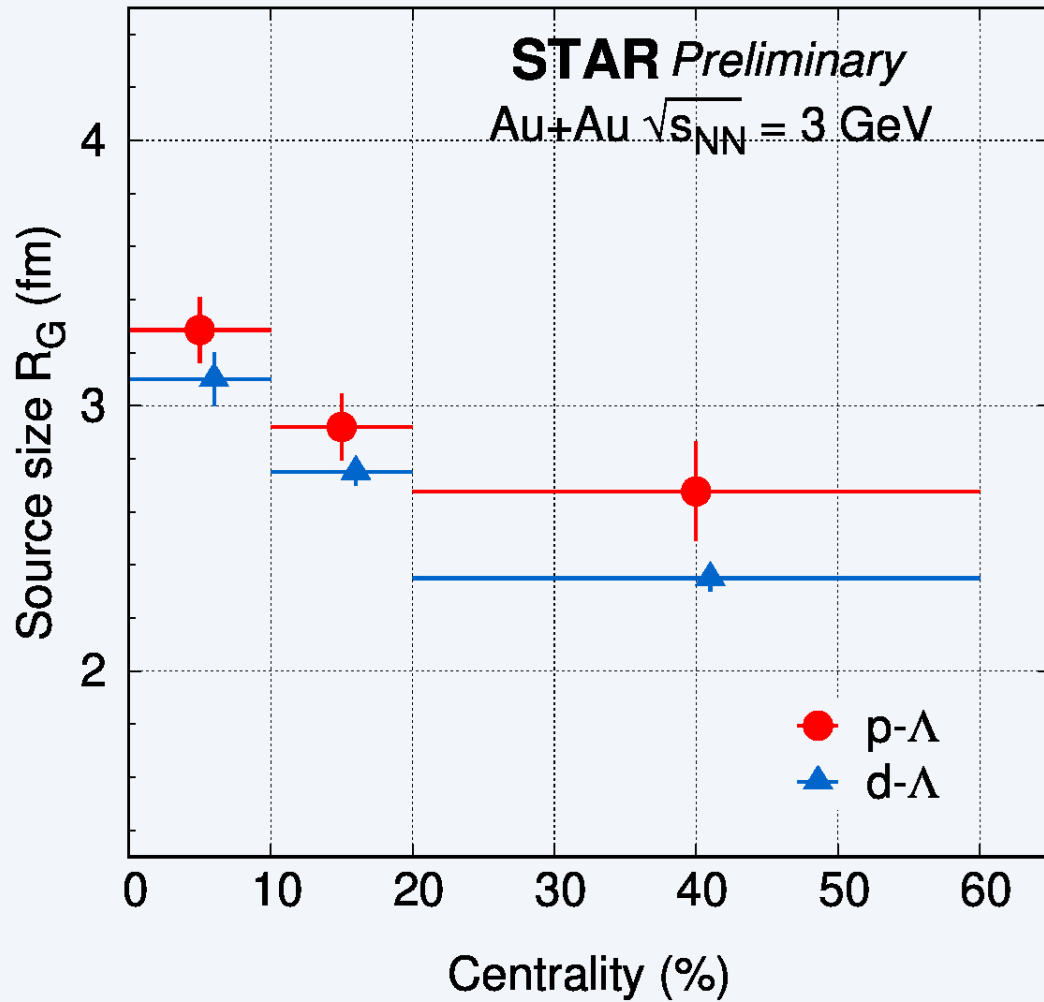
Detector effect, topological cuts,
Acceptance cut...

Normalize by the experimental
mixed event



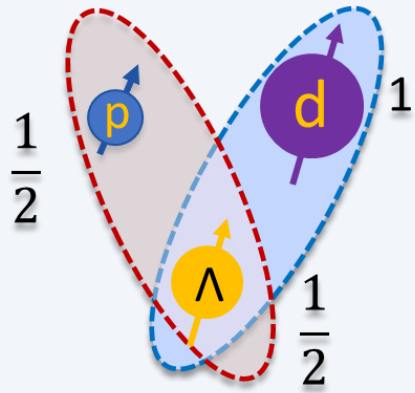
- ❖ Simulation based on STAR ${}^3_{\Lambda}\text{H}$ yield measurement:
4~8% of d- Λ entries from ${}^3_{\Lambda}\text{H}$ decay at $k^* < 100$ MeV/c in
10~20% centrality
- ❖ Contamination subtracted from inclusive d- Λ correlation

Source Size with L-L approach



- ❖ R_G : **spherical Gaussian source of pairs** by Lednicky-Lyuboshits approach
- ❖ Separation of emission source from final state interaction
- ❖ Collision dynamics as expected:
 - ❖ $R_G^{\text{central}} > R_G^{\text{peripheral}}$
 - ❖ $R_G(p - \Lambda) > R_G(d - \Lambda)$

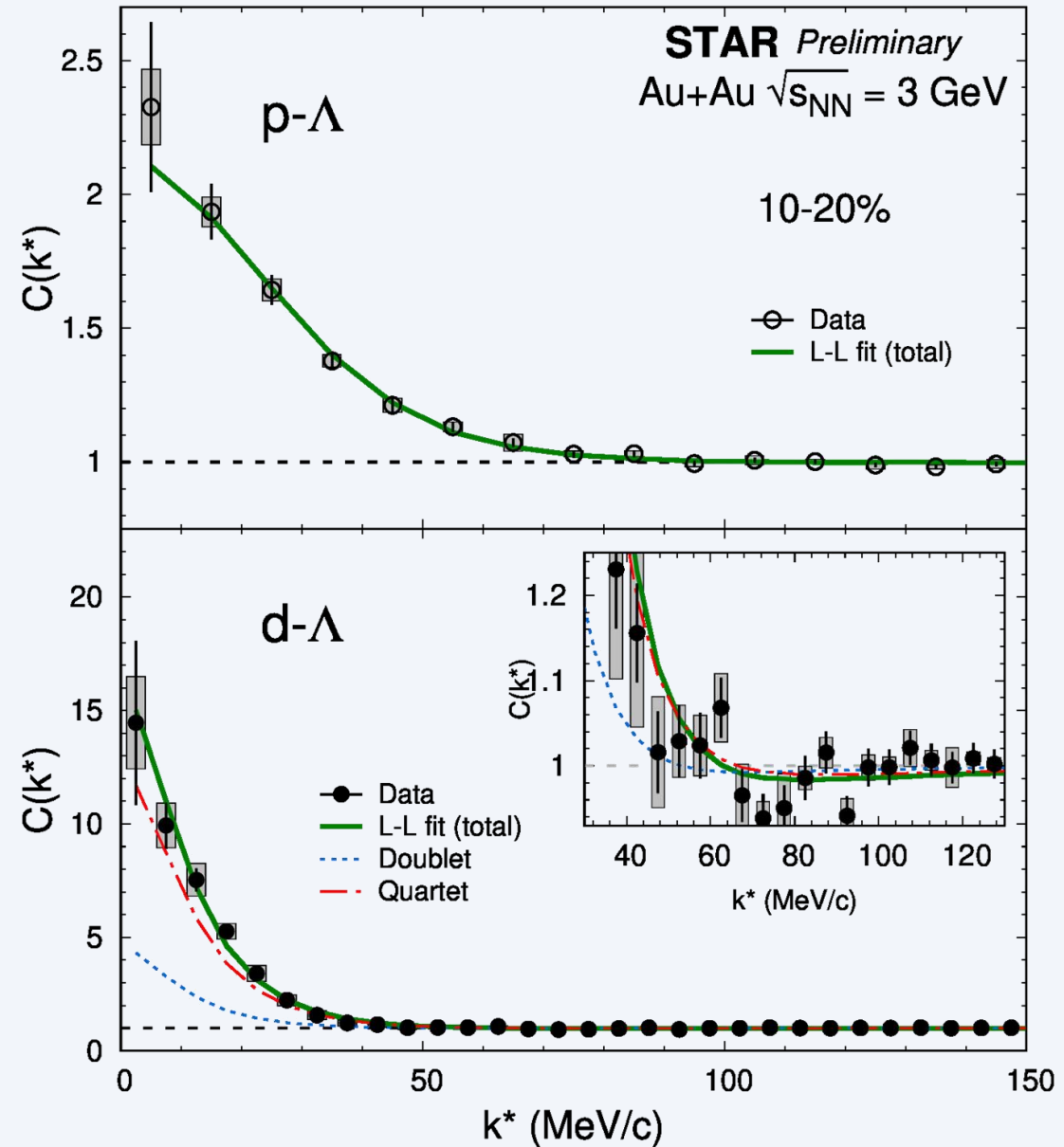
Correlation Function & Spin States



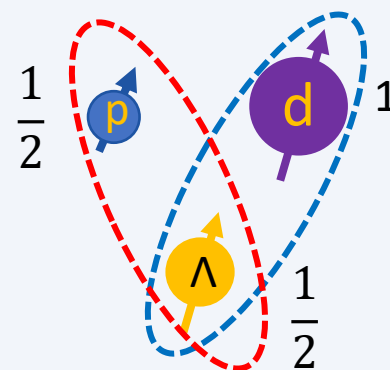
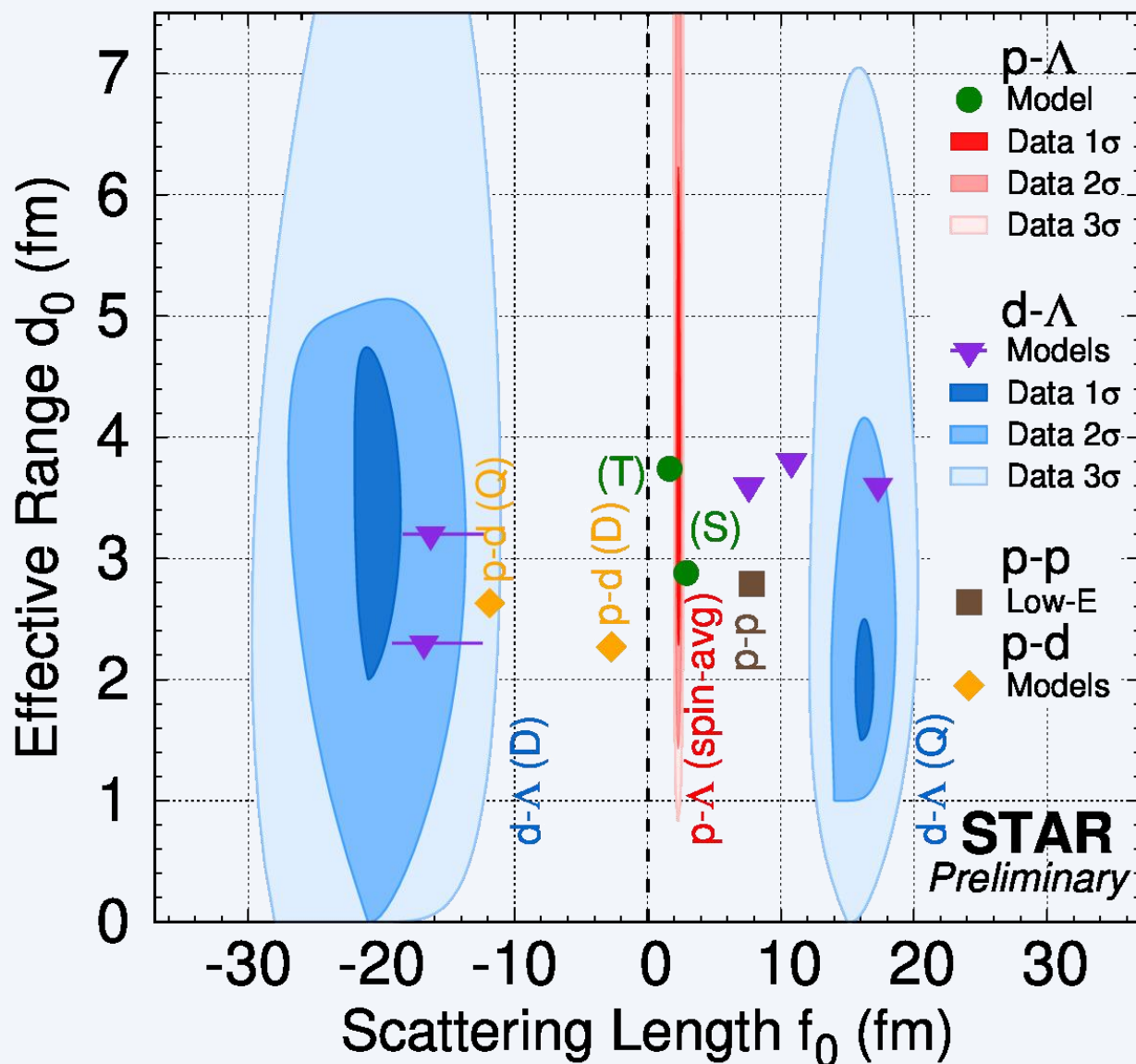
Singlet State	1S_0	(S)
Triplet State	3S_1	(T)
Doublet State	$^2S_{1/2}$	(D)
Quartet State	$^4S_{3/2}$	(Q)

$$\text{d-}\Lambda: |\psi(r, k)|^2 \rightarrow \frac{1}{3} |\psi_{1/2}(r, k)|^2 + \frac{2}{3} |\psi_{3/2}(r, k)|^2$$

- ❖ Different spin states with different f_0 and d_0 parameters
- ❖ **p-Λ correlation:** current statistics is not enough to separate two spin states → **spin-averaged fit**
- ❖ **d-Λ correlation:** very different f_0 for (D) and (Q) are predicted → **Spin-separated fit**



Scattering Length (f_0) and Effective Range (d_0)



$$\frac{1}{f(k)} \approx \frac{1}{f_0} + \frac{d_0 k^2}{2} - ik$$

❖ The constraint on the effective range (d_0) is weaker

- ❖ The measurement is done at freeze-out
- ❖ Spin-avg for f_0 & d_0 p- Λ system

$$f_0 = 2.32^{+0.12}_{-0.11} \text{ fm}$$

$$d_0 = 3.5^{+2.7}_{-1.3} \text{ fm}$$

- ❖ Successfully separate two spin states in d- Λ

$$f_0(D) = -20^{+3}_{-3} \text{ fm}$$

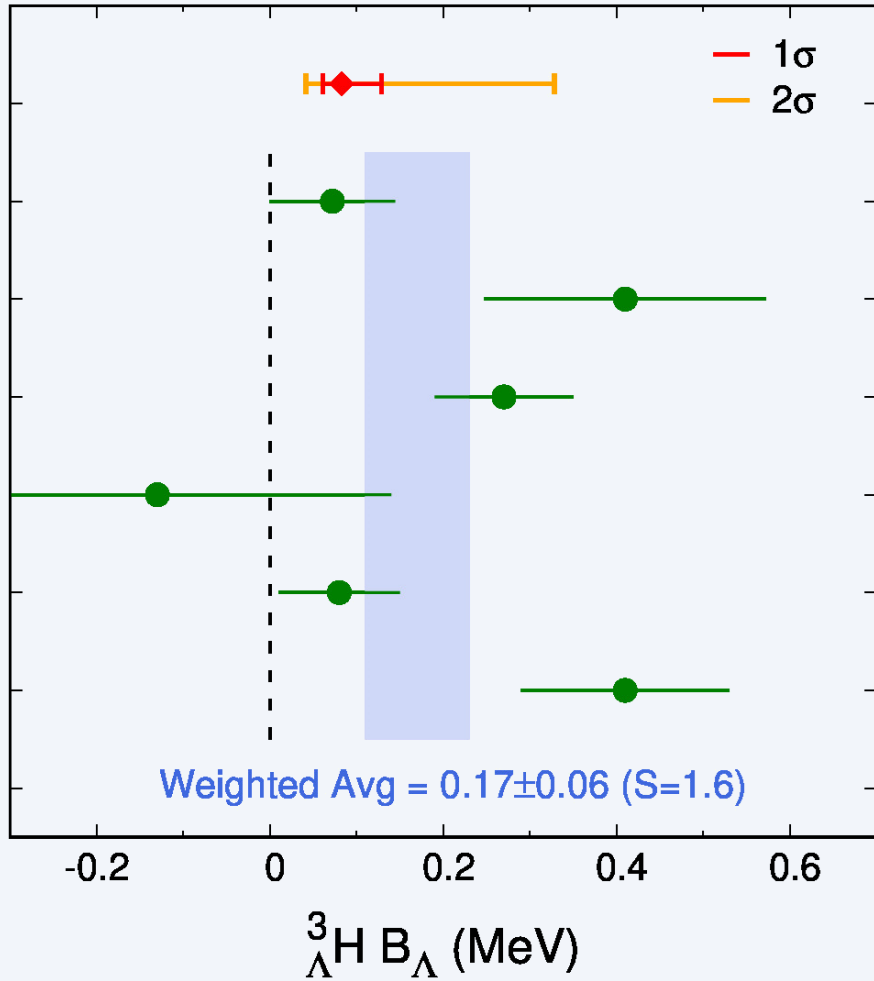
$$d_0(D) = 3^{+2}_{-1} \text{ fm}$$

$$f_0(Q) = 16^{+2}_{-1} \text{ fm}$$

$$d_0(Q) = 2^{+1}_{-1} \text{ fm}$$

- ❖ Constraint fit for d- Λ , require $f_0(D) < 0$
- ❖ Edge of d- Λ contours are shown with Bezier smooth to improve the visibility

${}^3_{\Lambda}\text{H}$ Binding Energy



Estimated from
STAR Preliminary
d- Λ Correlation

ALICE 2022

STAR 2020

NPB52 1973

PRD1 1970

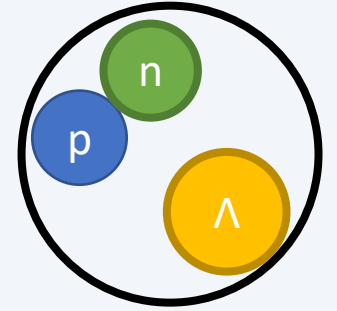
NPB4 1968

NPB1 1967

HIC
InvM
Stopped K^-
Chamber / emulsion

${}^3_{\Lambda}\text{H}$ binding energy (B_{Λ}):

- ❖ Bethe formula from Effective Range Expansion (ERE) parameters $f_0(D)$ & $d_0(D)$



$$\frac{1}{-f_0} = \gamma - \frac{1}{2}d_0\gamma^2$$

- ❖ $B_{\Lambda} = \frac{\gamma^2}{2\mu_{d\Lambda}}$

- ❖ $\mu_{d\Lambda}$: reduced mass

- ❖ γ : binding momentum

- ❖ ${}^3_{\Lambda}\text{H } B_{\Lambda} = [0.04, 0.33] \text{ (MeV) @ 95\% CL}$

Consistent with the world average

- ❖ A new way to constrain the ${}^3_{\Lambda}\text{H}$ structure

Summary and outlook

- ❖ The first d- Λ correlation function measurements in heavy-ion collisions
- ❖ Successfully separated emission source size from final state interactions in d- Λ correlation functions

- $R_G^{\text{central}} > R_G^{\text{peripheral}}$ and $R_G(p - \Lambda) > R_G(d - \Lambda)$
- d- Λ correlation spin-sep:

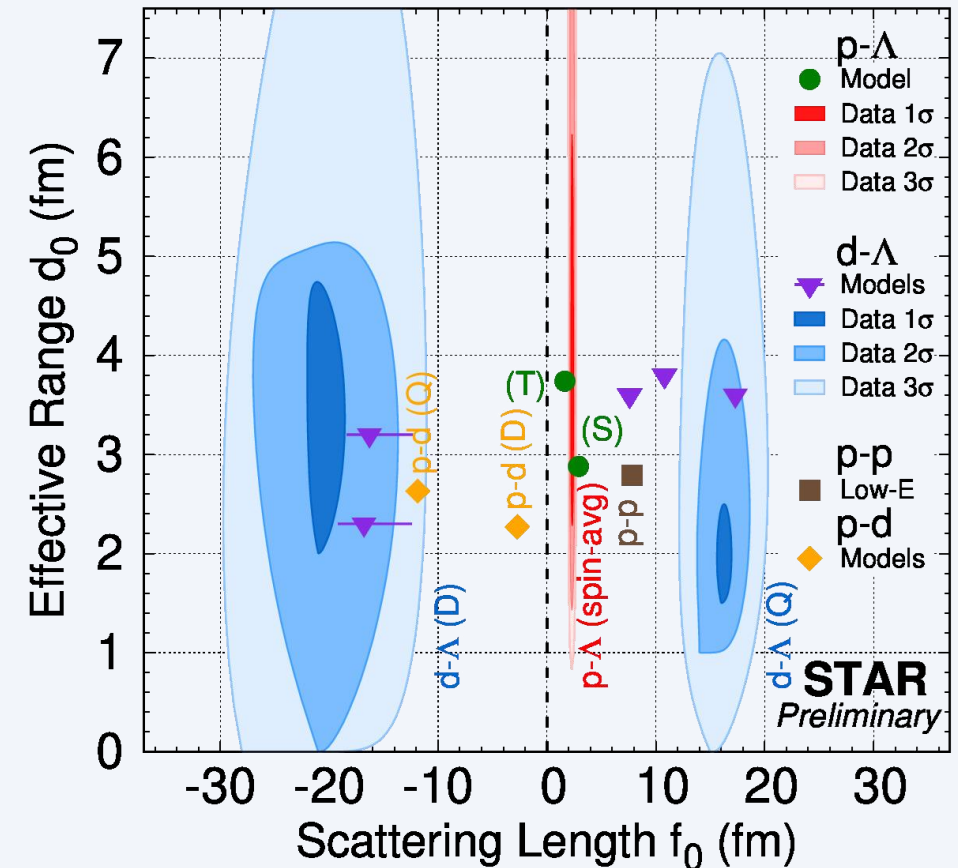
$$f_0(D) = -20_{-3}^{+3} \text{ fm} \quad d_0(D) = 3_{-1}^{+2} \text{ fm}$$

$$f_0(Q) = 16_{-1}^{+2} \text{ fm} \quad d_0(Q) = 2_{-1}^{+1} \text{ fm}$$
- ${}^3\text{H } B_\Lambda = [0.04, 0.33] \text{ (MeV)}$ @ 95% CL from d- Λ correlation (D)

Outlook:

More than 10 times statistics from BES-II

- ❖ Emission source size vs. energy, rapidity...
- ❖ Baryon correlations with different species





Thank you!

