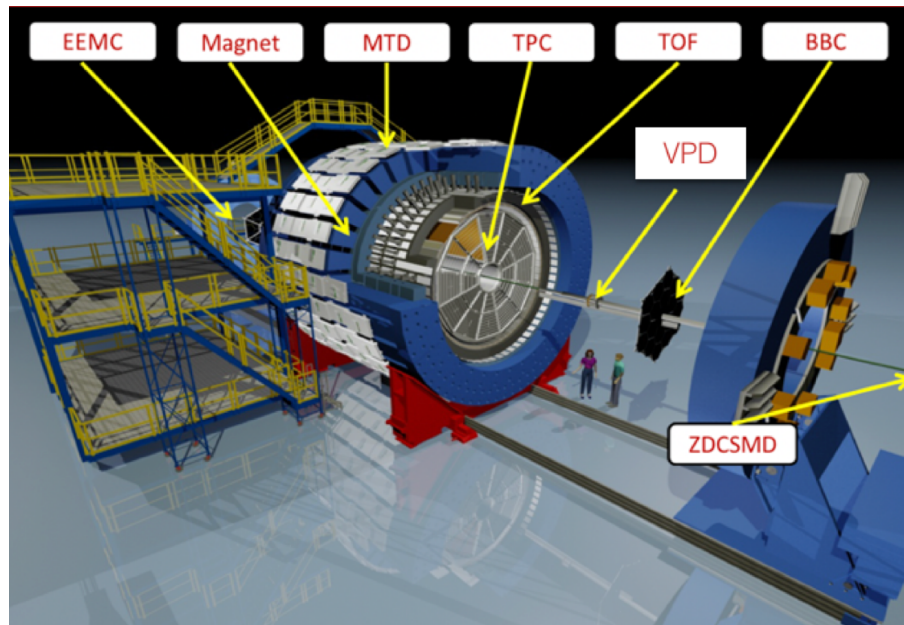


Beam-energy dependence of the longitudinal broadening of two-particle transverse momentum correlations from STAR

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➤ Time Projection Chamber

Tracking of charged particles with:

- ✓ Full azimuthal coverage
- ✓ $|\eta| < 1$ coverage

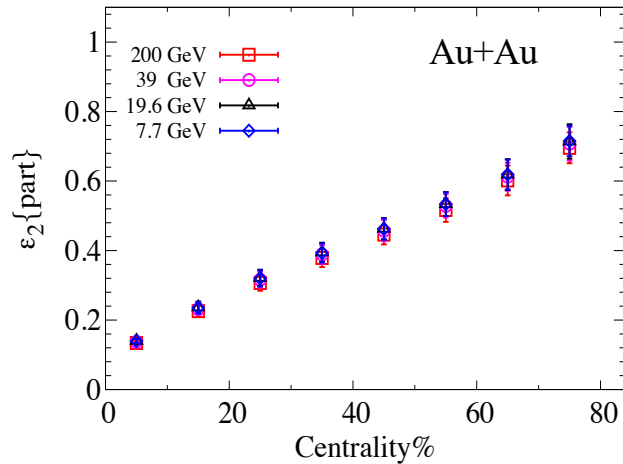
➤ In this analysis we used tracks with:

$$0.2 < p_T < 2 \text{ GeV}/c$$

Motivation:

- The beam-energy dependence of flow and p_T correlations will reflect the respective roles of ϵ_n and its fluctuations and $\frac{\eta}{s}$ as a function of T and μ_B

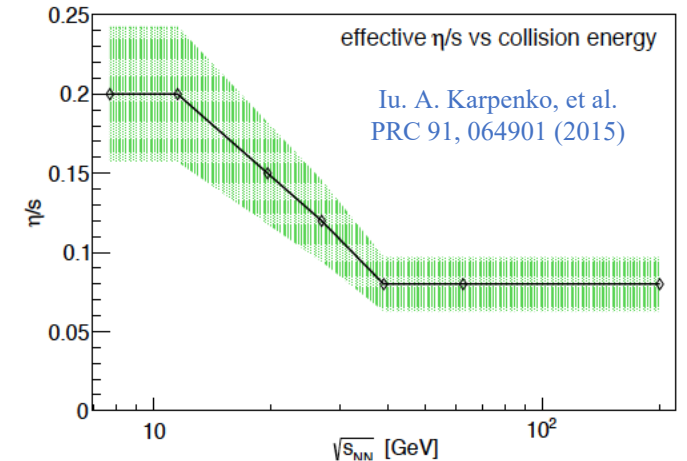
Beam energy dependence for a given collision system:



- Initial-state ϵ_2 is approximately energy independent
- Viscous attenuation ($\propto \frac{\eta}{s}(T)$) is beam energy dependent

Piotr Bozek
PRC 93, 044908 (2016)

Niseem Magdy, Roy Lacey
PLB 821 136625 (2021)

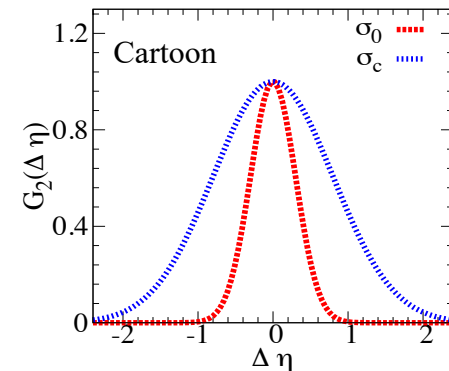


- The Pearson correlation, $v_n - [p_T]$ correlation, coefficient (PCC) is expected to be more susceptible to the initial conditions of heavy-ion collisions.

S. Gavin and M. Abdel-Aziz
Phys.Rev.Lett. 97 (2006) 162302

The Gavin ansatz:

- The p_T 2-P correlation function is sensitive to the dissipative viscous effects that are ensured during the transverse and longitudinal expansion of the collisions' medium.
- Because such dissipative effects are more prominent for long-lived systems, they lead to longitudinal broadening of p_T 2-P correlation function as collisions become more central.
- A proposed estimate of this broadening, $\Delta\sigma^2$, can be linked to η/s as:



$$\Delta\sigma^2 = \sigma_c^2 - \sigma_0^2 = \frac{4}{T_c} \frac{\eta}{s} \left(\frac{1}{\tau_0} - \frac{1}{\tau_{c,f}} \right)$$



J. Jia, M. Zhou, A. Trzupek,
PRC 96 034906 (2017)

ATLAS Collaboration,
Eur. Phys. J. C 79, 985 (2019)

Piotr Bozek
PRC 93, 044908 (2016)

Niseem Magdy, Roy Lacey
PLB 821 136625 (2021)

Motivation:

❖ Transverse momentum-flow correlations:

$$\text{cov}(v_n^2, [p_T]) = \text{Re} \left(\left\langle \frac{\sum_{a,c} w_a w_c e^{in(\phi_a - \phi_c)} ([p_T] - \langle [p_T] \rangle)_b}{\sum_{a,c} w_a w_c} \right\rangle \right)$$

$$\rho(v_n^2, [p_T]) = \frac{\text{cov}(v_n^2, [p_T])}{\sqrt{\text{Var}(v_n^2)_{\text{dyn}} C_{\{k\}}}}$$

$\Delta\eta_{b\hat{b}} > 0.2$

$$C_k = \left\langle \frac{\sum_b \sum_{b'} w_b w_{b'} (p_{T,b} - \langle [p_T] \rangle) (p_{T,b'} - \langle [p_T] \rangle)}{(\sum_b w_b)^2 - \sum_b (w_b)^2} \right\rangle$$

$$\text{Var}(v_n^2)_{\text{dyn}} = v_n^4 \{2\} - v_n^4 \{4\}$$

The Pearson correlation coefficient (PCC) measures the strength of the $v_n, [p_T]$ correlation.

❖ The p_T 2-P correlator:

$$G_2(\eta_1, \varphi_1, \eta_2, \varphi_2) = \frac{\langle \sum_i^{n_1} \sum_{j \neq i}^{n_2} p_{T,i} p_{T,j} \rangle}{\langle n_1 \rangle \langle n_2 \rangle} - \langle p_{T,1} \rangle_{\eta_1, \varphi_1} \langle p_{T,2} \rangle_{\eta_2, \varphi_2}$$

- $r_{1,2}$ is a number correlation, it will be unity when the particle pairs are independent
- The $r_{1,2}$ correlations can be impacted by the centrality definition

$$\frac{\left\langle \frac{\sum_i^{n_1} \sum_{j \neq i}^{n_2} p_{T,i} p_{T,j}}{\langle n_1 \rangle \langle n_2 \rangle} \right\rangle}{\left\langle \frac{\sum_i^{n_1} \sum_{j \neq i}^{n_2} n_i n_j}{\langle n_1 \rangle \langle n_2 \rangle} \right\rangle} = \frac{\left\langle \frac{\sum_i^{n_1} \sum_{j \neq i}^{n_2} p_{T,i} p_{T,j}}{\langle n_1 \rangle \langle n_2 \rangle} \right\rangle}{\left\langle \frac{\sum_i^{n_1} \sum_{j \neq i}^{n_2} n_i n_j}{\langle n_1 \rangle \langle n_2 \rangle} \right\rangle} r_{1,2}$$

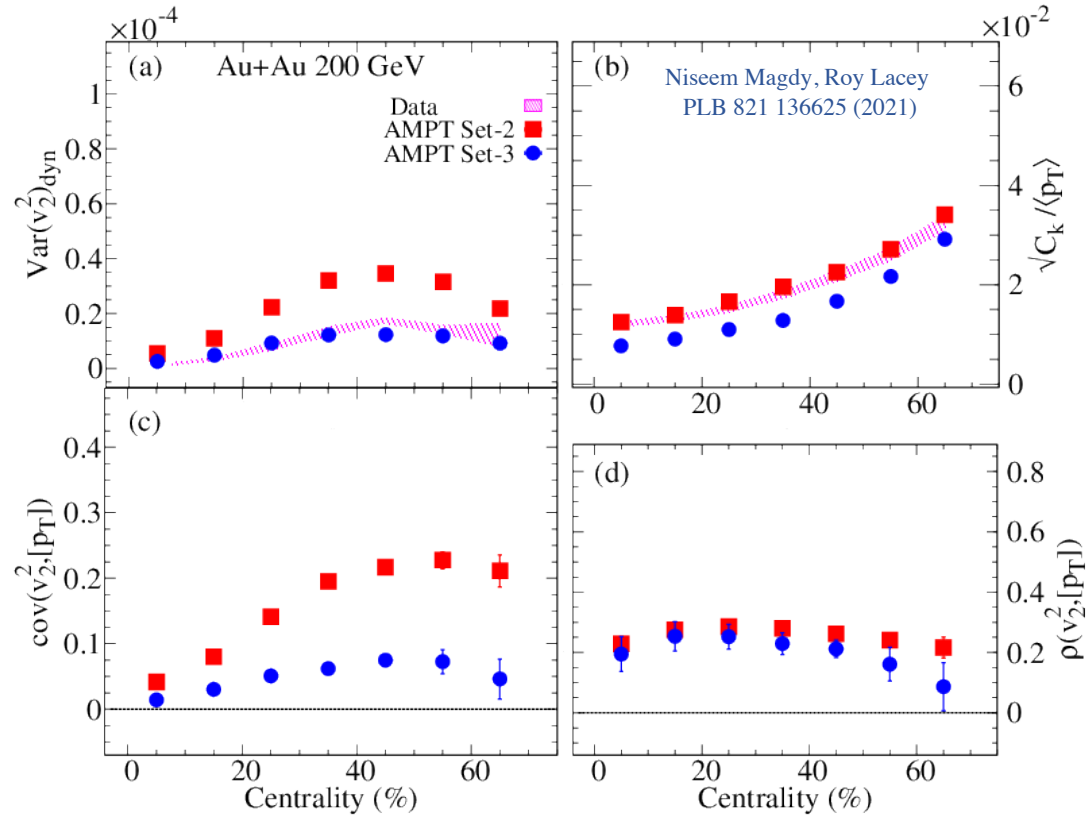
Excluding the POI from the collision centrality definition, helps reduce the possible self-correlations.

Niseem Magdy, Roy Lacey
PRC 104 1, 014907 (2021)

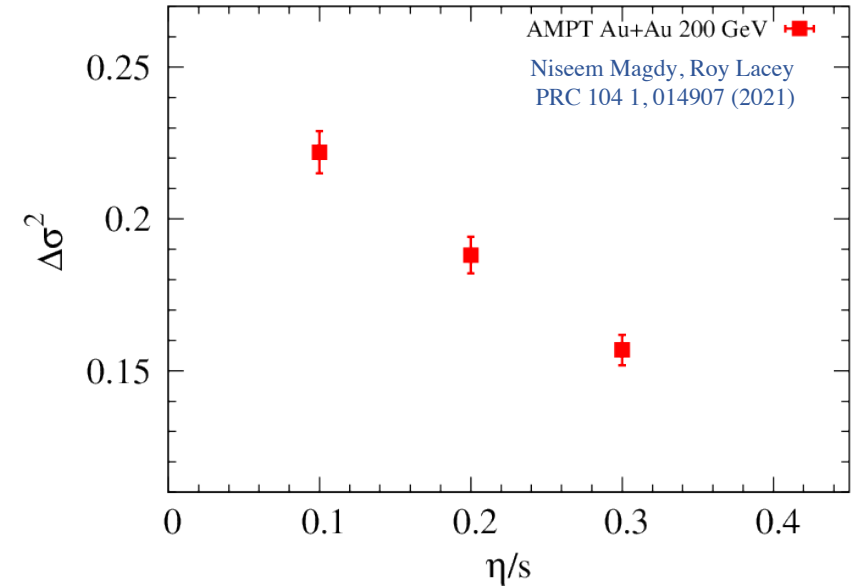
STAR Collaboration
PLB 704 (2011) 467–473

Motivation:

AMPT-set	η/s	String Melting Mechanism
Set-1	0.1	OFF
Set-2	0.1	ON
Set-3	0.3	ON



$$\Delta\sigma^2 = \sigma_c^2 - \sigma_0^2 = \frac{4}{T_c} \frac{\eta}{s} \left(\frac{1}{\tau_0} - \frac{1}{\tau_{c,f}} \right)$$



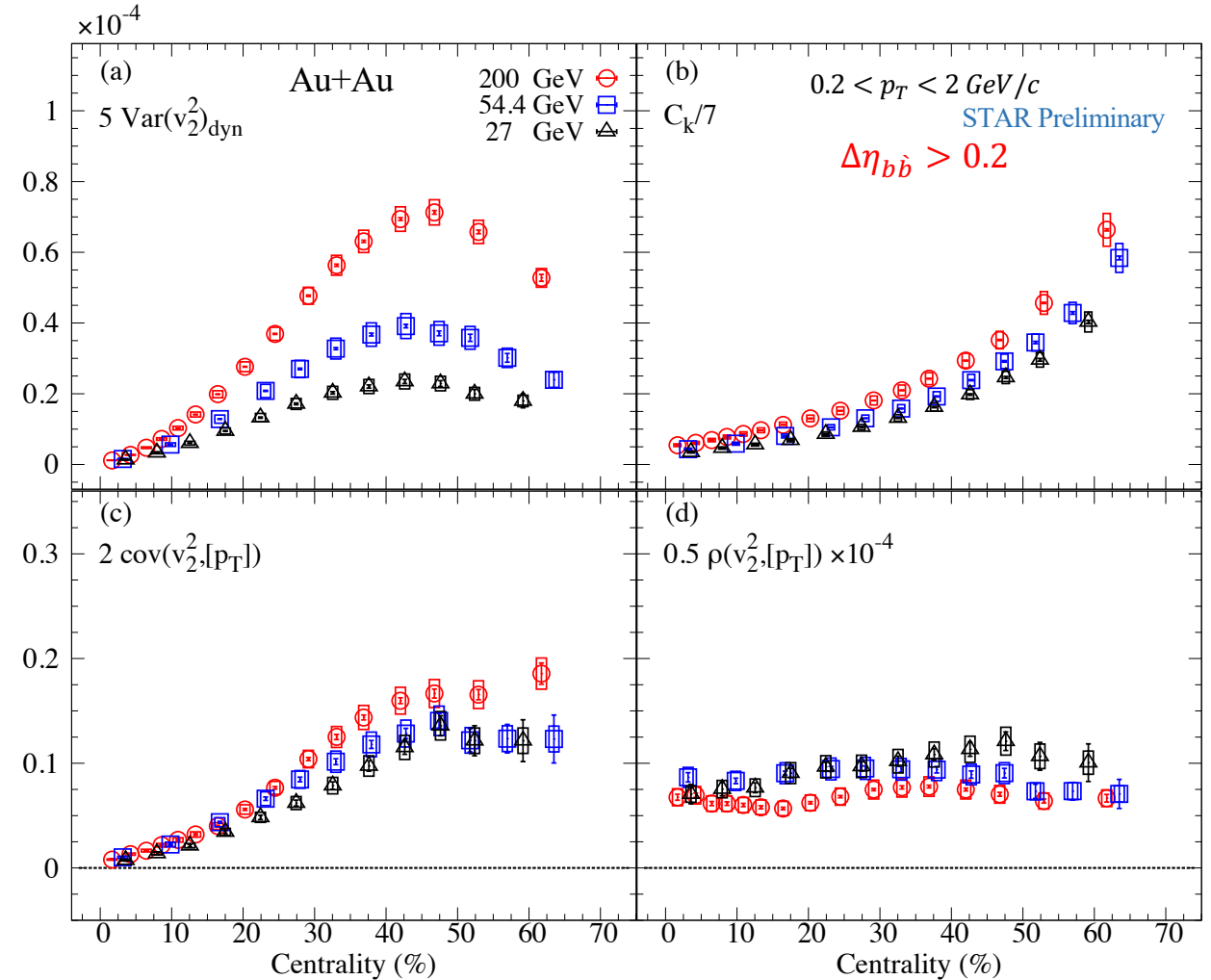
➤ $\rho(v_2^2, [p_T])$ values show little, if any, change with η/s , suggesting that $\rho(v_2^2 - [p_T])$ is dominated by initial state effects

➤ $\Delta\sigma^2$ values show a strong η/s sensitivity

❖ Transverse momentum-flow correlations:

The beam-energy dependence of the transverse momentum-flow correlations

- $Var(v_2^2)_{dyn}$ decreases with beam-energy
- C_k decreases with beam-energy
- $cov(v_2^2, [p_T])$ decreases with beam-energy

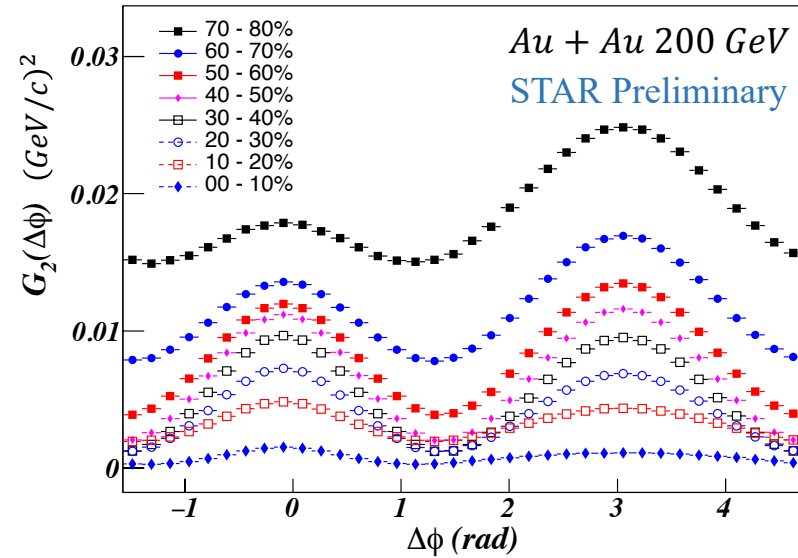


- The Pearson correlation, $\rho(v_2^2, [p_T])$, increases with decreasing the beam-energy

Investigations of the $p_T - p_T$ correlations from STAR

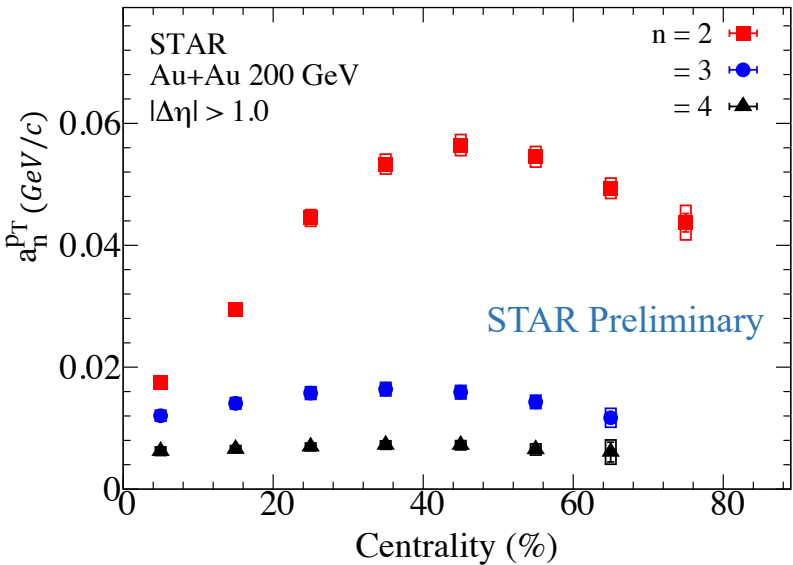
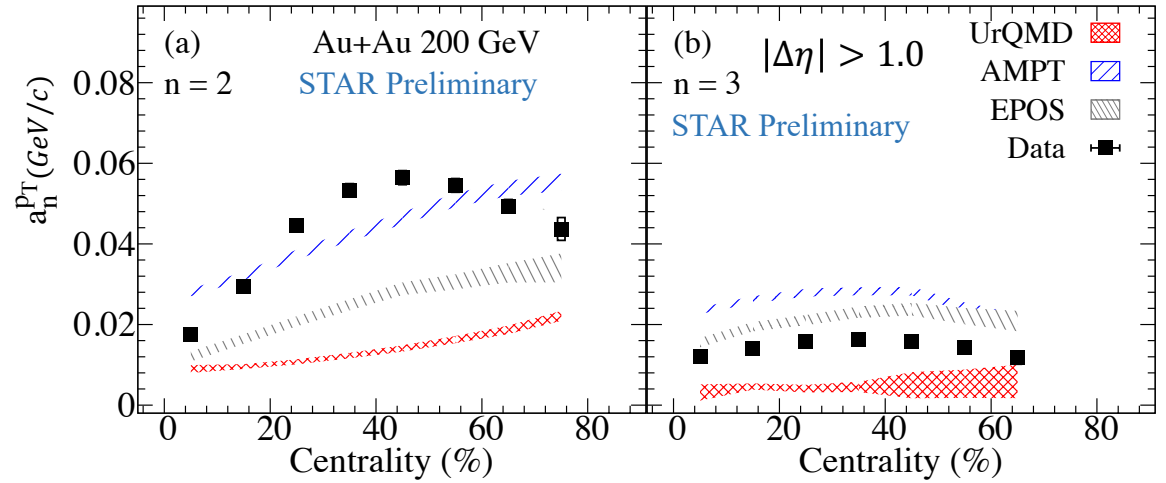
➤ The azimuthal correlations for Au+Au at 200 GeV

$$G_2(\Delta\phi) = A_0^{pT} + 2 \sum_{n=1}^6 A_n^{pT} \cos(n \Delta\phi) \quad a_n^{pT} = \sqrt{A_n^{pT}}$$



➤ The extracted a_n^{pT} :

- ✓ Decrease with harmonic order
- ✓ Models do not describe the data
- ✓ Event shape dependent

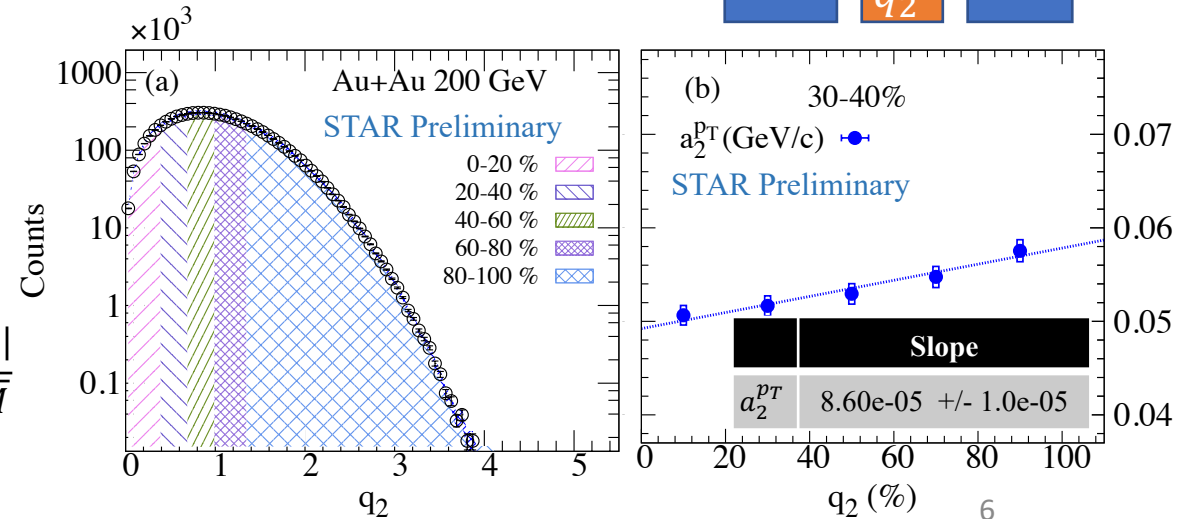
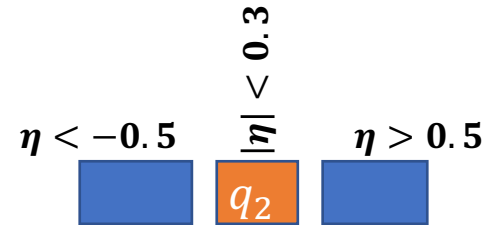


$$Q_{2,x} = \sum_{i=1}^M \cos(2 \varphi_i)$$

$$Q_{2,y} = \sum_{i=1}^M \sin(2 \varphi_i)$$

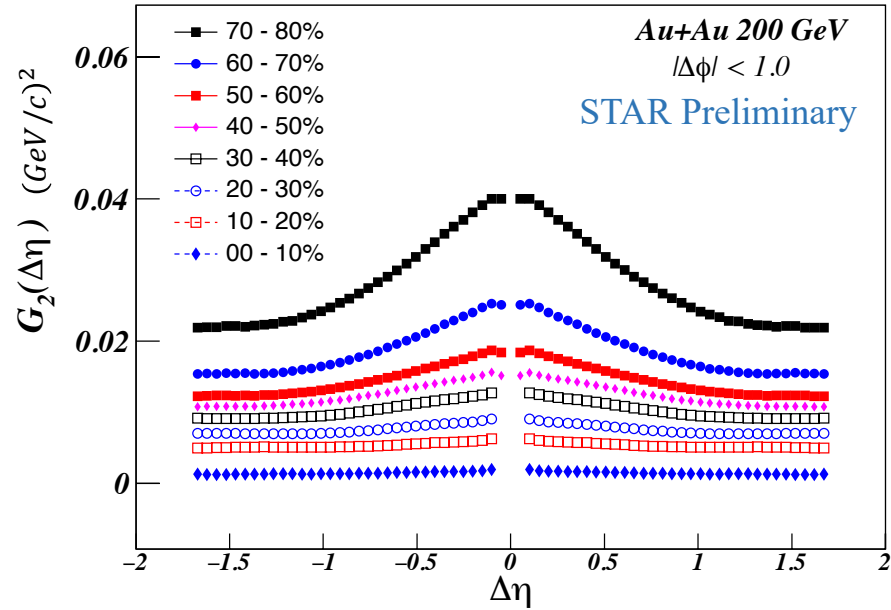
$$|Q_2| = \sqrt{Q_{2,x}^2 + Q_{2,y}^2} \quad q_2 = \frac{|Q_2|}{\sqrt{M}}$$

➤ q_2 is separated from particle of interest



Investigations of the $p_T - p_T$ correlations from STAR

➤ The longitudinal correlations for Au+Au at 200 GeV

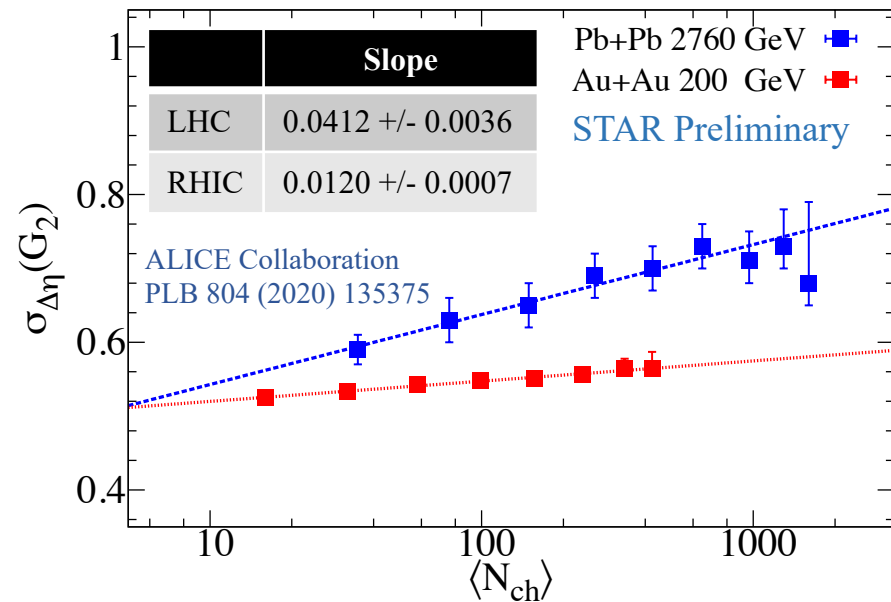
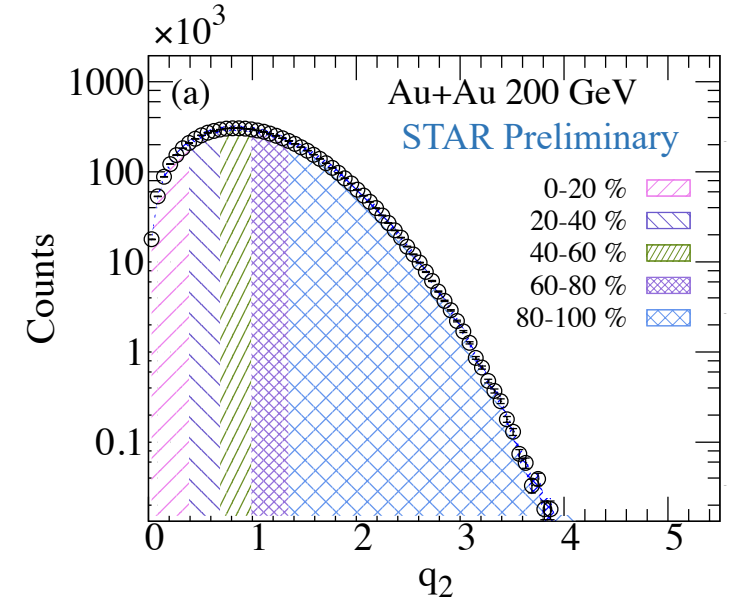


$$\sigma_{\Delta\eta}(G_2) = \text{RMS}[G_2(\Delta\eta)]$$

➤ The slope of $\sigma_{\Delta\eta}(G_2)$ is softer for RHIC

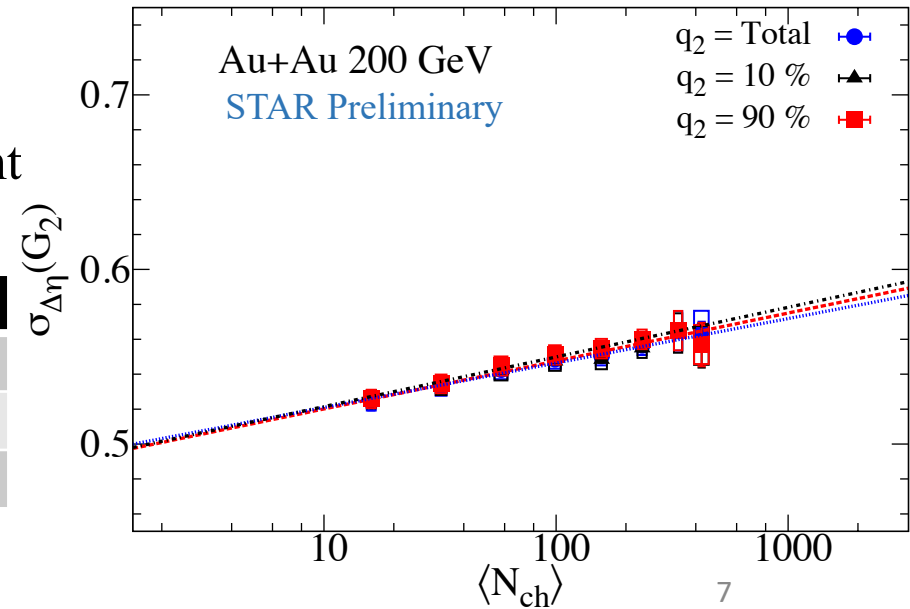
✓ Smaller η/s for RHIC

P. Alba et al.
PRC 98, 034909 (2018)



➤ The $\sigma_{\Delta\eta}(G_2)$ is event shape independent

Slope	
Total	0.0120 +/- 0.0007
10 %	0.0119 +/- 0.0009
90 %	0.0110 +/- 0.0012



Conclusions

We studied the transverse momentum-flow correlations as well as the transverse momentum 2-P correlations;

- Transverse momentum-flow correlations:
 - ✓ The $cov(v_2^2, [p_T])$ increases with beam energy
 - ✓ The normalized $\rho(v_2^2, [p_T])$:
Weakly increases with decreasing the beam-energy

These measurements compared to viscous hydrodynamic model calculation will provide constraints on the initial conditions and $\frac{\eta}{s}(T)$

- The extracted a_n^{pT} :
 - ✓ Decrease with harmonic order
 - ✓ Models don't describe the a_n^{pT} data
 - ✓ Event shape dependent a_2^{pT}

- The slope of $\sigma_{\Delta\eta}(G_2)$ vs multiplicity is:
 - ✓ Softer for RHIC (indicating smaller η/s for RHIC) than LHC
 - ✓ Event shape independent

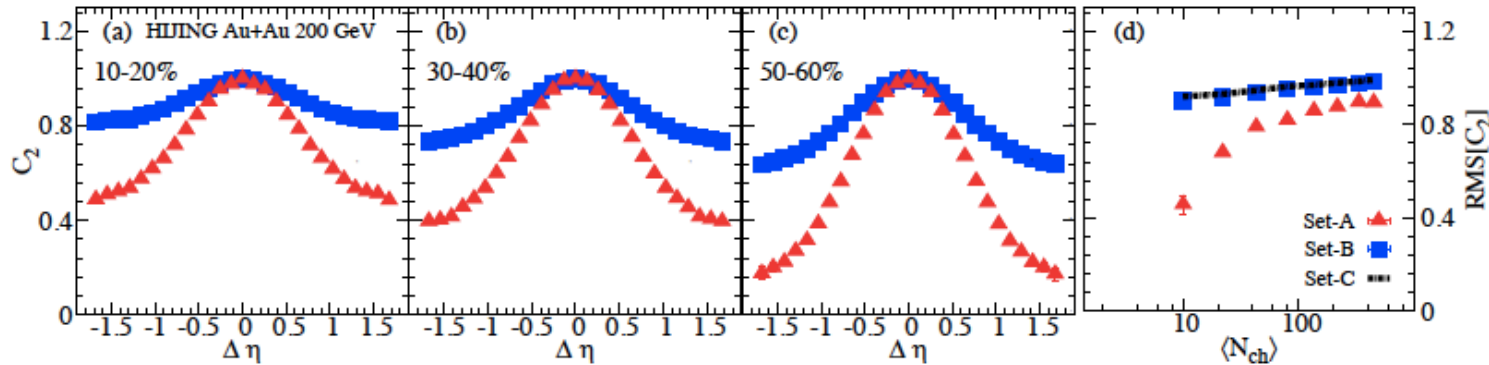
These comparisons are reflecting the efficacy of the $G_2(\Delta\eta, \Delta\varphi)$ correlator to differentiate among theoretical models as well as to constrain the η/s .

Thank You

- The p_T 2-P correlator is given as: $G_2(\eta_1, \varphi_1, \eta_2, \varphi_2) = \frac{\left\langle \sum_i^{n_1} \sum_{j \neq i}^{n_2} p_{T,i} p_{T,j} \right\rangle}{\langle n_1 \rangle \langle n_2 \rangle} - \langle p_{T,1} \rangle_{\eta_1, \varphi_1} \langle p_{T,2} \rangle_{\eta_2, \varphi_2}$
- The first term can be given as:

$$\frac{\left\langle \sum_i^{n_1} \sum_{j \neq i}^{n_2} p_{T,i} p_{T,j} \right\rangle}{\langle n_1 \rangle \langle n_2 \rangle} = \frac{\left\langle \sum_i^{n_1} \sum_{j \neq i}^{n_2} p_{T,i} p_{T,j} \right\rangle}{\left\langle \sum_i^{n_1} \sum_{j \neq i}^{n_2} n_i n_j \right\rangle} r_{1,2}, \quad \longrightarrow \quad r_{1,2} = \frac{\left\langle \sum_i^{n_1} \sum_{j \neq i}^{n_2} n_i n_j \right\rangle}{\langle n_1 \rangle \langle n_2 \rangle}.$$

- $r_{1,2}$ is a number correlation, it will be 1 when the particle pairs are independent.
- The $r_{1,2}$ correlations can be impacted by the centrality definition.



Comparison of the $C_2(\Delta\eta)$ correlators ($|\Delta\varphi| < 1$) obtained from 10-20%, 30-40% and 50-60% central HIJING events for Au+Au collisions at 200 GeV.

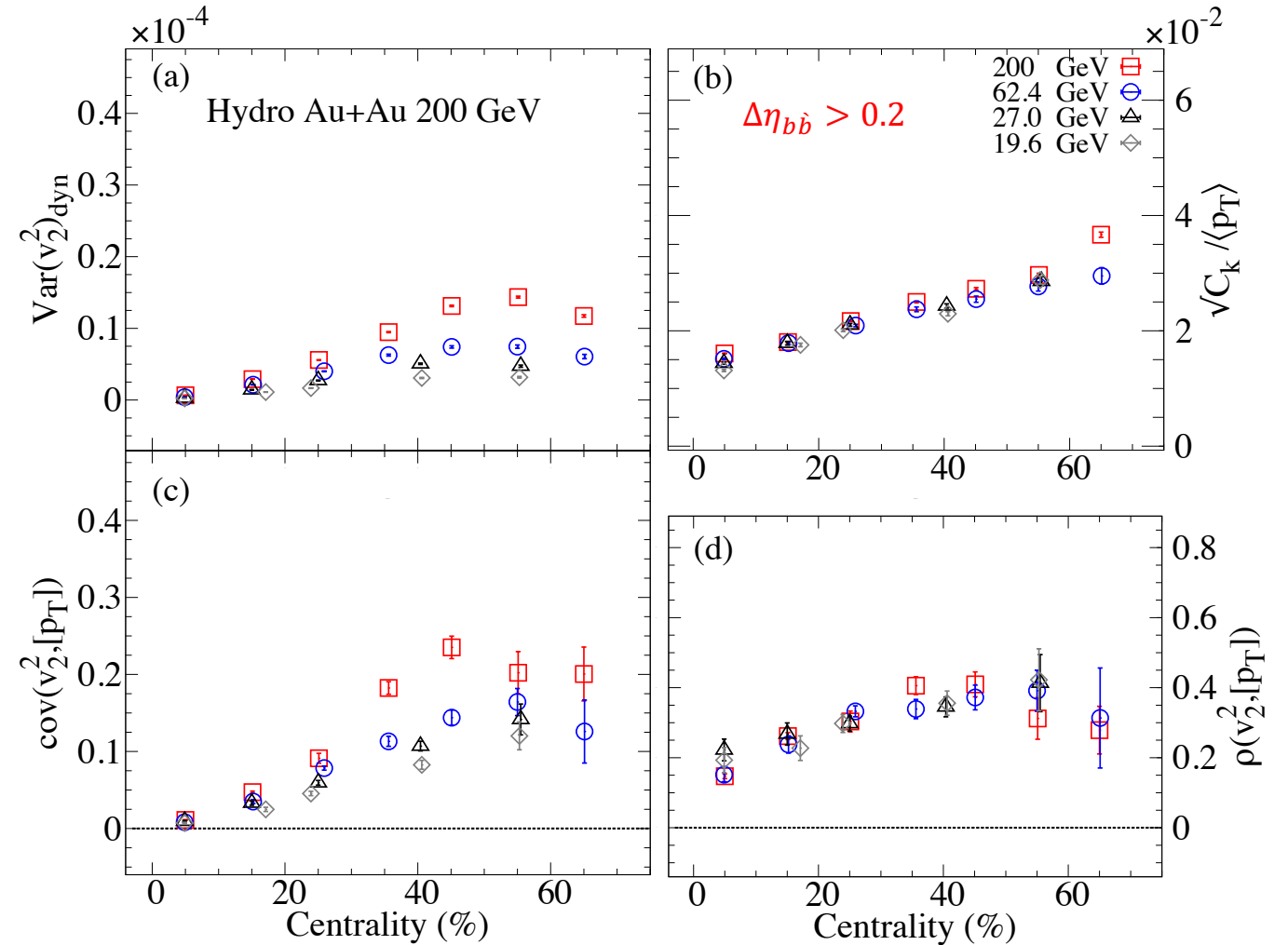
- (i) Set-A: with centrality defined using all charged particles in an event,
- (ii) Set-B: with centrality defined using random sampling of charged particles in an event
- (iii) Set-C: with centrality defined using the impact parameter distribution.

- Excluding the POI from the collision centrality definition, serves to reduce the possible self-correlations.

❖ Transverse momentum-flow correlations:

The beam-energy dependence of the transverse momentum-flow correlations using hydro model

- $Var(v_2^2)_{dyn}$ decreases with beam-energy
- C_k decreases with beam-energy
- $cov(v_2^2, [p_T])$ decreases with beam-energy



➤ The Pearson correlation, $\rho(v_2^2, [p_T])$, increases with decreasing the beam-energy