



Results from a modified R_{Ψ_2} observable in isobar collisions at STAR

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Research supported in part by:

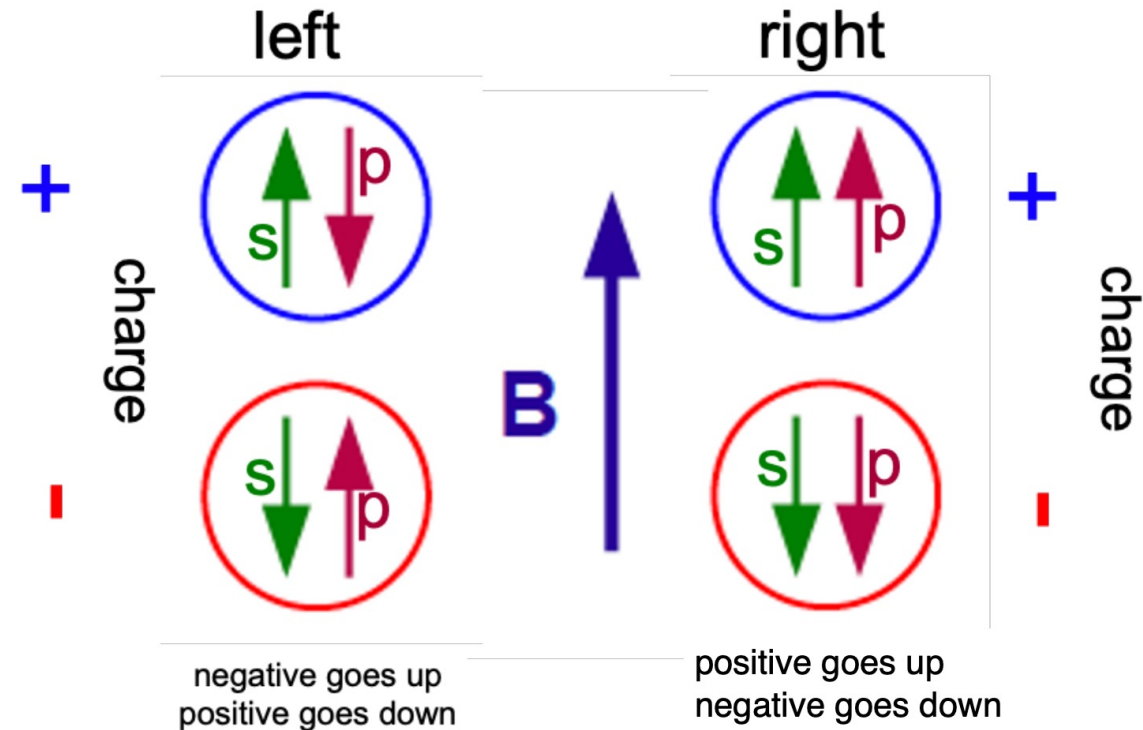


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Chiral Magnetic Effect (CME) Introduction

- **Quantum Chromodynamics (QCD) chiral anomaly can produce an excess of right/left handed quarks in vacuum**
- Charges separate in magnetic field due to spectator protons
- Experimentally, observe **charge separation in final state particles** [1,2]



$$j_V = \frac{N_c e}{2\pi^2} \mu_A B$$

[1] D. Kharzeev, R. Pisarski, and M. H. Tytgat, Phys.Rev.Lett. 81, 512 (1998)

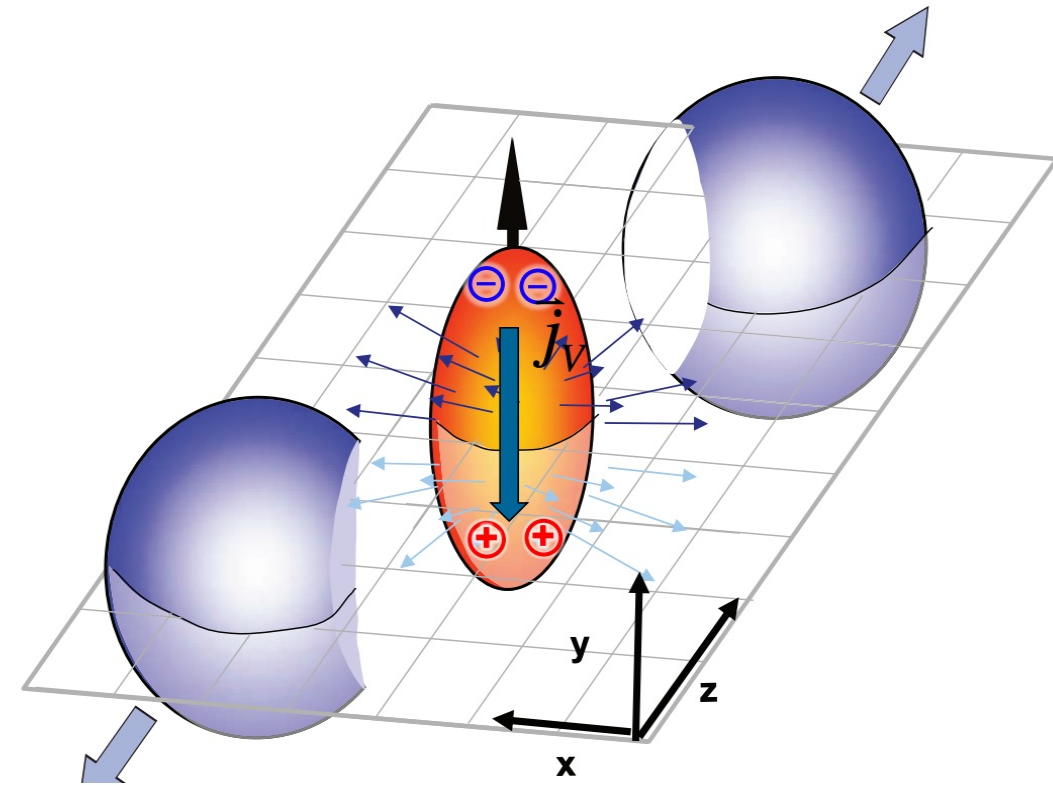
[2] D. E. Kharzeev, L. D. McLerran, and H. J. Warringa, Nucl.Phys. A803, 227 (2008),

CME Introduction

- **B field** and **J** are aligned perpendicular to reaction plane (Ψ_{RP})
- The azimuthal distribution of particles can be expressed as:

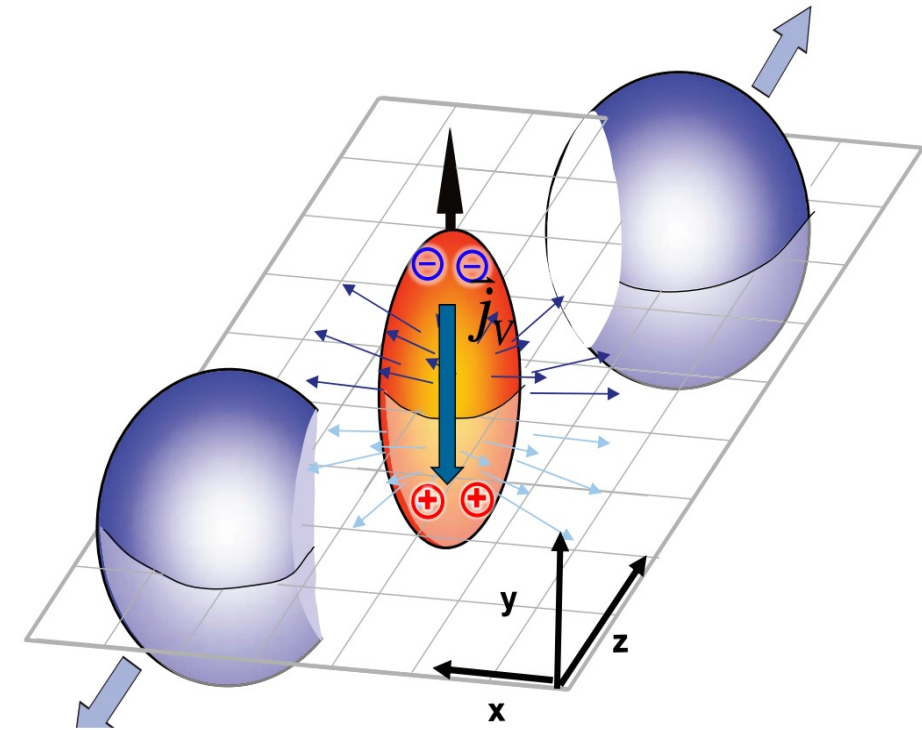
$$\frac{dN^\pm}{d\phi} \propto 1 \pm 2a_1 \sin(\phi - \Psi_{RP}) + 2v_2 \cos 2(\phi - \Psi_{RP}) + \dots$$

- a_1 Charge dependent **CME signal**
- v_2 Elliptic flow coefficient
- Ψ_{RP} RP azimuthal angle



R Observable for CME

- Break an event into two subevents (East and West), by $0.1 < |\eta| < 1.0$
 - **Event Plane**, using empirical resolution correction [3]:
 - **POI -- Charge Separation (ΔS)**
- ΔS are calculated **parallel** and **perpendicular** to the **EP**
 - Example: Parallel ΔS for the West subevent
 - $$\Delta S_m^W = \frac{1}{n_w^+} \sum_i^{n_w^+} \sin\left(\frac{m}{2} (\phi_i^+ - \Psi_m^E)\right) - \frac{1}{n_w^-} \sum_i^{n_w^-} \sin\left(\frac{m}{2} (\phi_i^- - \Psi_m^E)\right)$$
- **Can keep ΔS separate or take the average**



R Observable for CME

- The **R observable** is defined as the **ratio** between the **parallel** and **perpendicular ΔS distributions**.

- $$R_{\Psi_m} = \frac{\frac{\Delta S_m}{\Delta S_{m,sh}}}{\frac{\Delta S_m^\perp}{\Delta S_{m,sh}^\perp}} = C e^{\xi x^2 / 2}$$

- Contributions from **CME in R_{Ψ_m}** should be **concave**

- Width of R distribution, from ΔS distributions: $\frac{1}{\sigma^2} = \left(\frac{1}{\sigma_m^2} - \frac{1}{\sigma_{m,sh}^2} \right) - \left(\frac{1}{\sigma_{m\perp}^2} - \frac{1}{\sigma_{m\perp,sh}^2} \right)$

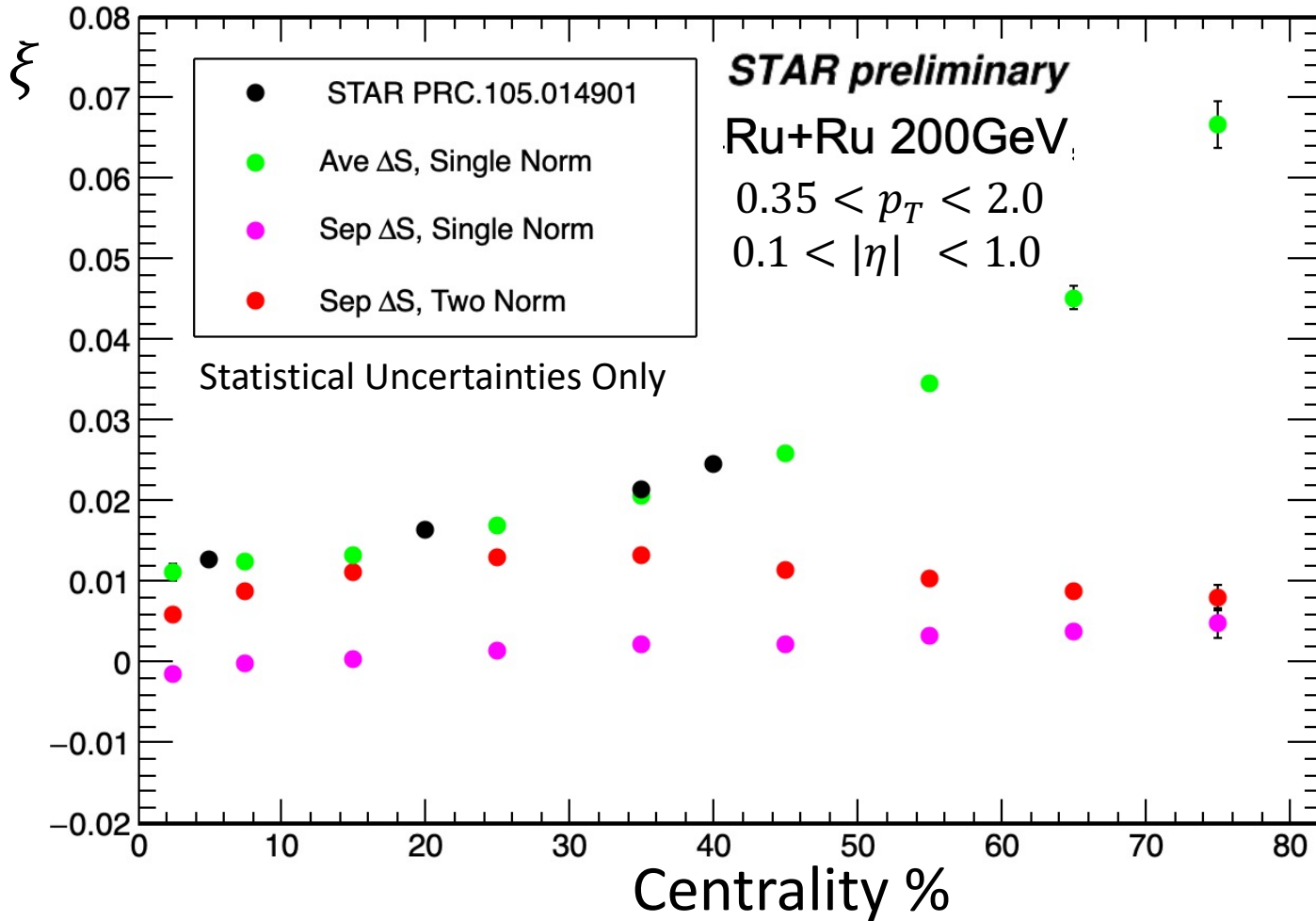
- $\xi = \frac{1}{\sigma'^2} = \left(\frac{\sigma_{m,sh}^2}{\sigma_m^2} - 1 \right) - \left(\frac{\sigma_{m,sh}^2}{\sigma_{m\perp}^2} - \frac{\sigma_{m,sh}^2}{\sigma_{m\perp,sh}^2} \right)$: Single (Shuffled) Normalization

- $\xi = \frac{1}{\sigma'^2} = \left(\frac{\sigma_{m,sh}^2}{\sigma_m^2} - \frac{\sigma_{m\perp,sh}^2}{\sigma_{m\perp}^2} \right)$: Two (Shuffled) Normalization

- “Shuffled” Delta S distributions ($\Delta S_{m,sh}$) are formed by randomly shuffling particle charges

Results

ξ vs. Centrality



- Averaging ΔS between two sub-events can introduce autocorrelation, that is centrality dependent [4]

$$\text{Var}[\Delta S] = \frac{1}{4}\langle \Delta S_E^2 \rangle + \frac{1}{4}\langle \Delta S_W^2 \rangle + \frac{1}{2}\langle \Delta S^E \Delta S^W \rangle$$

- Not expected in separate sub-event ΔS

$$\xi = \frac{1}{\sigma'^2} = \left(\frac{\sigma_{m,sh}^2}{\sigma_m^2} - 1 \right) - \left(\frac{\sigma_{m,sh}^2}{\sigma_{m\perp}^2} - \frac{\sigma_{m,sh}^2}{\sigma_{m\perp,sh}^2} \right)$$

- Single (Shuffled) Normalization

- Normalizations can make a difference

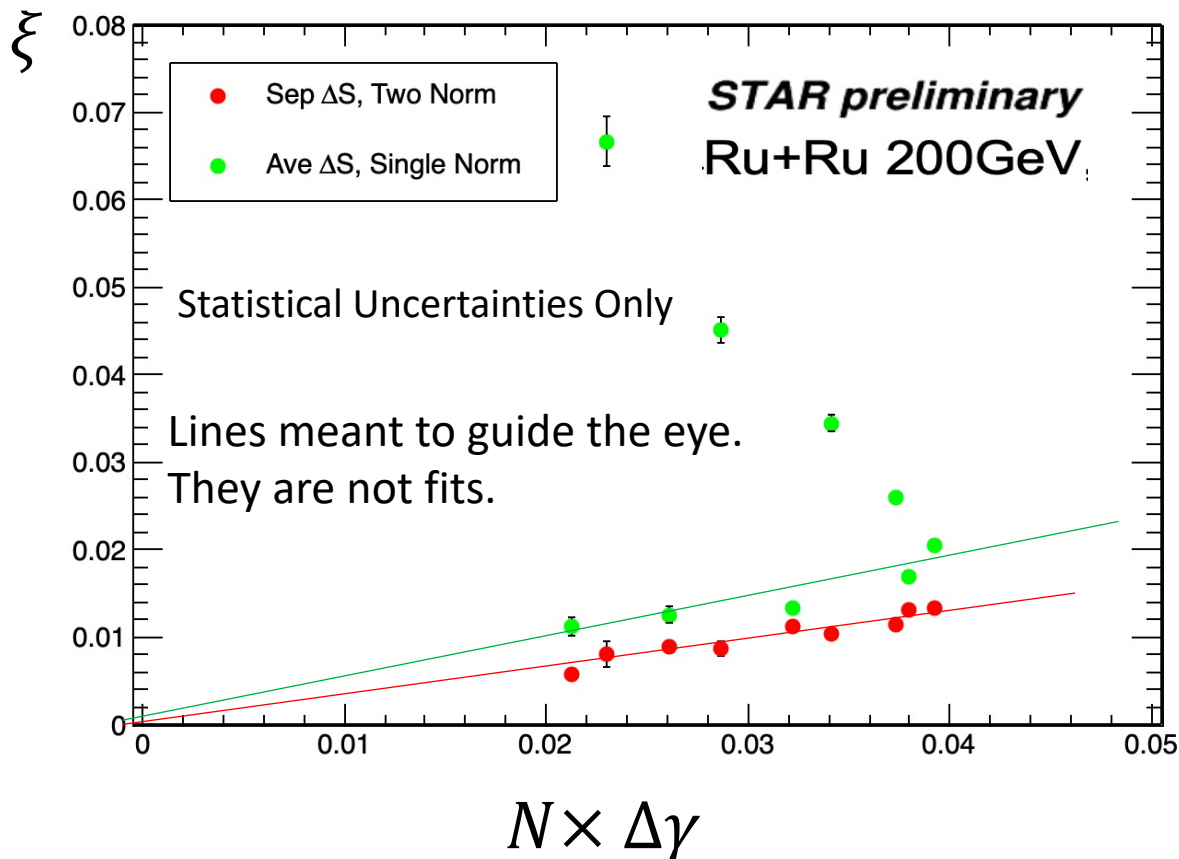
$$\xi = \frac{1}{\sigma'^2} = \left(\frac{\sigma_{m,sh}^2}{\sigma_m^2} - \frac{\sigma_{m\perp,sh}^2}{\sigma_{m\perp}^2} \right)$$

- Two (Shuffled) Normalization

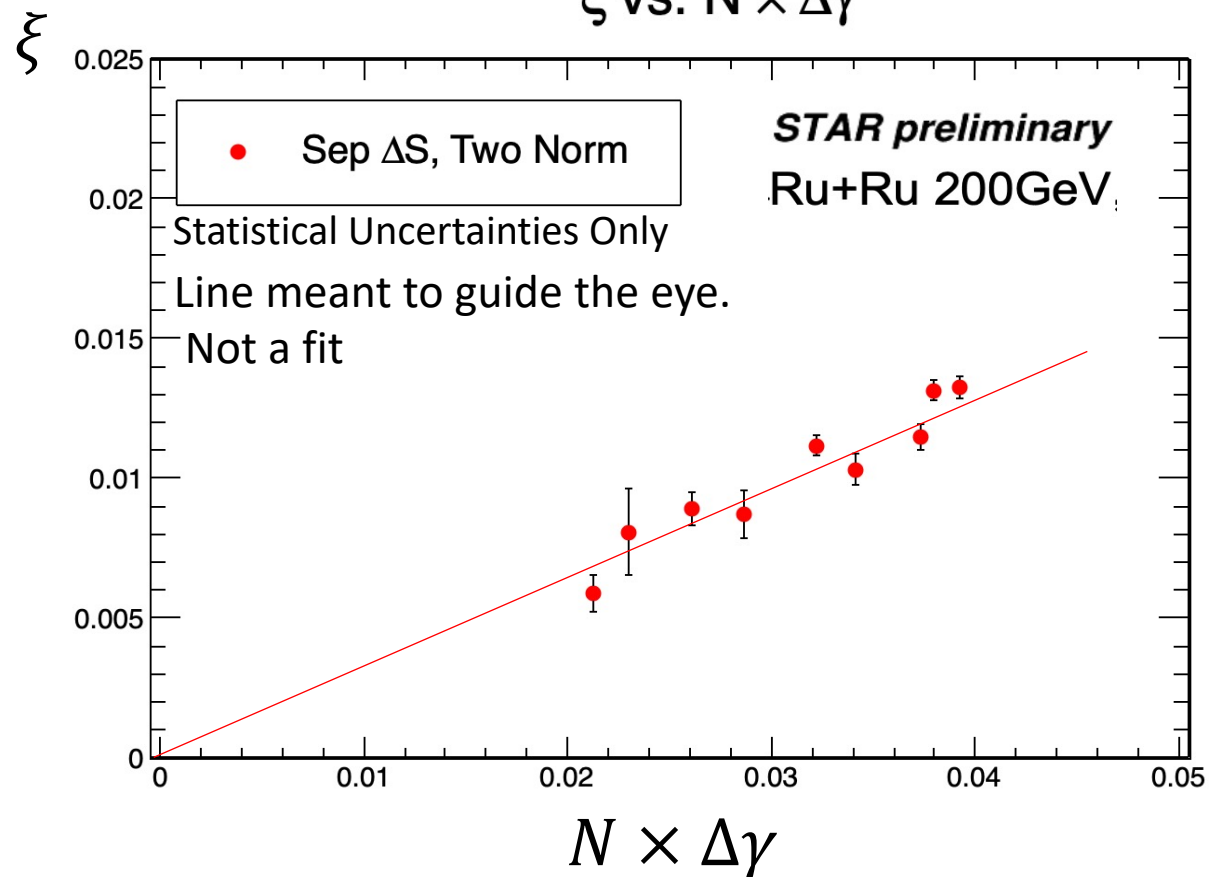
Correlation between ξ and $N \times \Delta\gamma$

Separate or Average ΔS affect the correlation between ξ and $N \times \Delta\gamma$

ξ vs. $N \times \Delta\gamma$



ξ vs. $N \times \Delta\gamma$



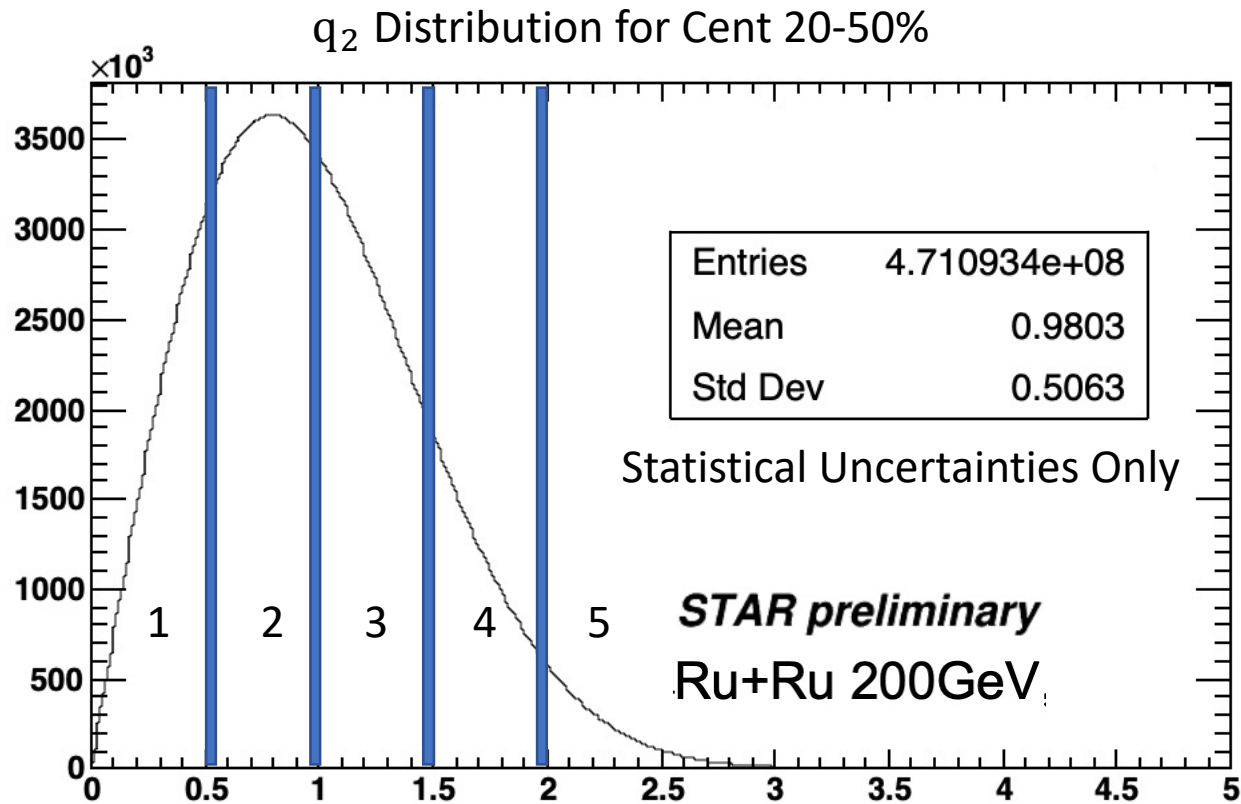
Now, onto to Event Shape Engineering (ESE) Analysis^[5]

- ξ is expected to be similar to $N \times \Delta\gamma$, which is proportional to v_2 ^[6]
 - ξ was **observed to be roughly independent of v_2 with non-zero intercept**^[3]
 - Want to **examine modified ξ vs. v_2 in ESE**

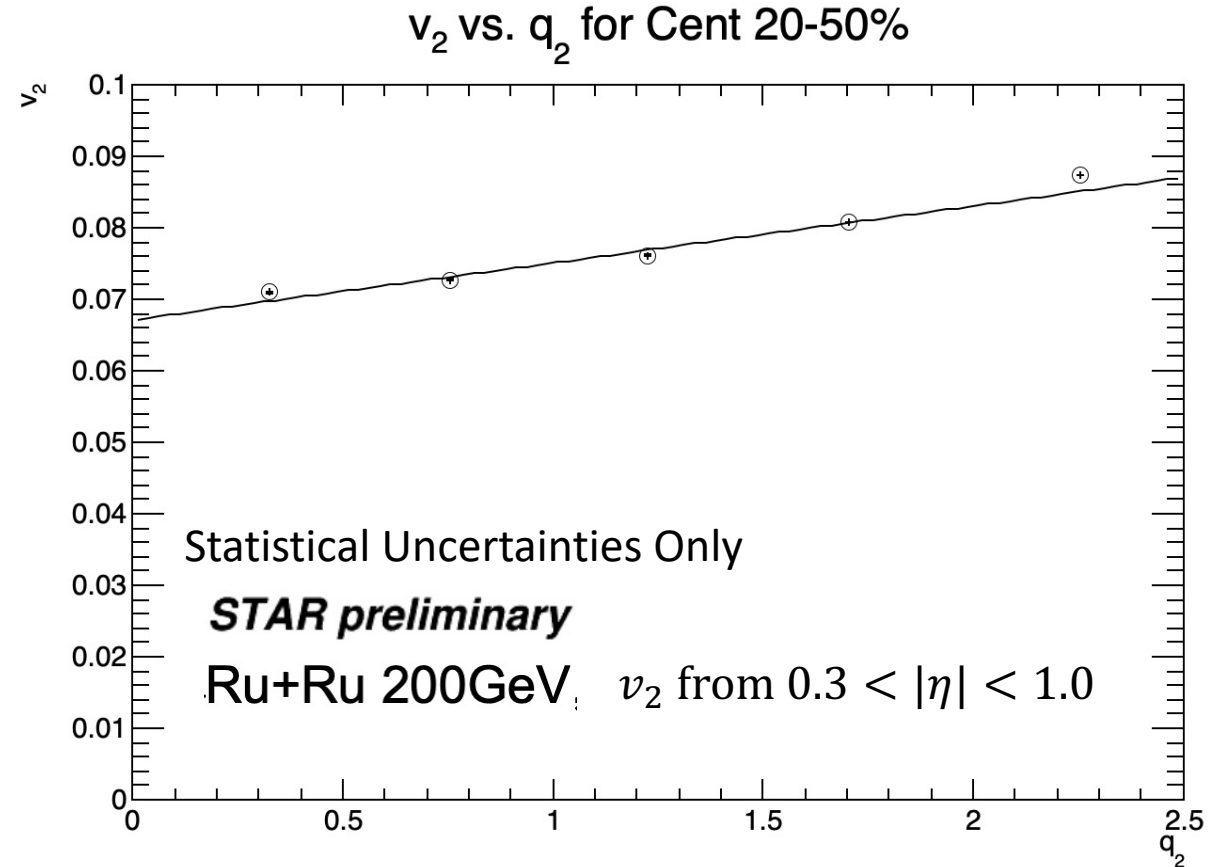
[5] J. Schukraft, A. Timmins, and S. A. Voloshin,
Ultrarelativistic nuclear collisions: event shape engineering, Phys. Lett. B719, 394 (2013)

[6] S. Choudhury et al. , Investigation of experimental observables in search of the chiral magnetic effect in heavy-ion collisions in the STAR experiment, Chinese Phys. C 46 014101 (2022)

v_2 vs. q_2



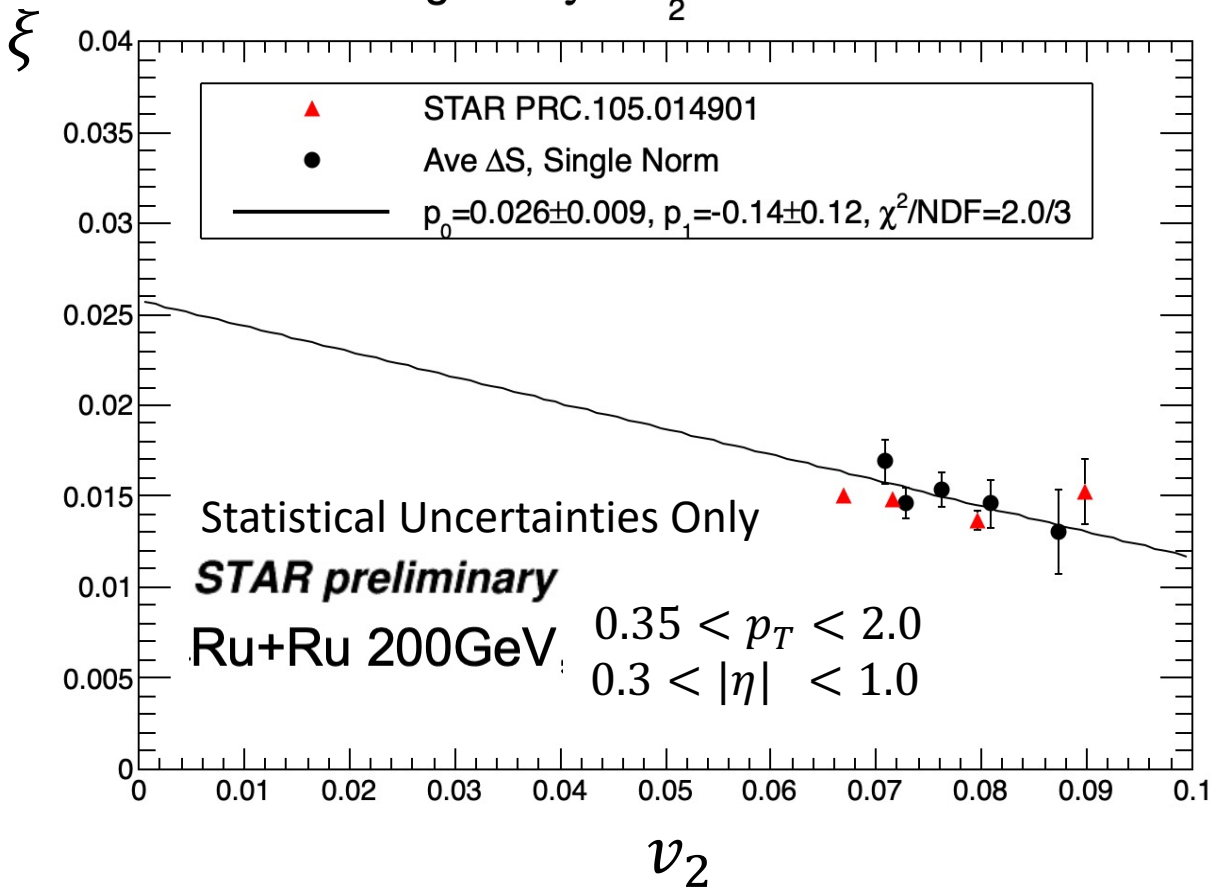
q_2 calculated from middle subevent $|\eta| < 0.3$ with particles satisfying $0.2 < p_T < 2.0$



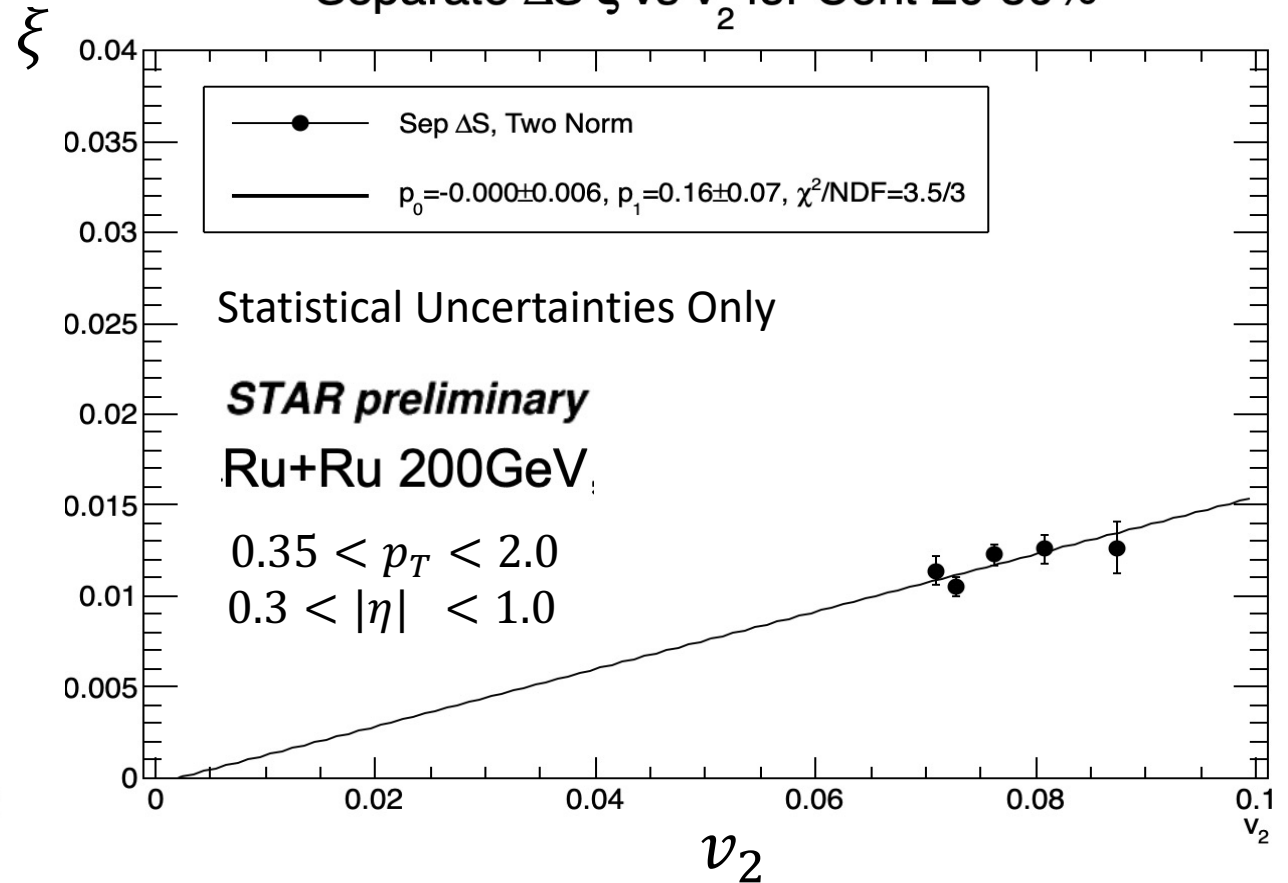
Weighted average of q_2 , and v_2 over the Centrality 20-50% range, each weighted by the number of events

ξ vs v_2 for Cent 20-50%

Average ΔS ξ vs v_2 for Cent 20-50%



Separate ΔS ξ vs v_2 for Cent 20-50%



The Average ΔS introduces an autocorrelation yielding a non-zero intercept. This intercept is not present in the Separate ΔS case.

Conclusions

A modified R-observable developed for CME search.

- In previous analyses, STAR data are normalized using a **single shuffled distribution**
 - Normalizing by **both perpendicular and parallel** shuffled distributions **makes a difference**
- STAR data **average** the **ΔS distributions** of the subevents
 - This averaging introduces an **autocorrelation** which **increases signal**
 - Yields a **non-zero intercept** in ESE analysis
- Our results (separate subevents, two shuffled normalizations) indicate **weak centrality dependence** of the modified ξ , similar to v_2 . Modified ξ observed to be proportional to $N \times \Delta\gamma$

Backup

ESE Analysis Procedure

- 1) 3 separate centrality bins: 20-30%, 30-40%, 40-50%
- 2) Event Shape Engineering (ESE) procedure: Each event is split into three subevents east ($-1 < \eta < -0.3$), middle ($-0.3 < \eta < 0.3$), and west ($0.3 < \eta < 1.0$)
- 3) $q_2 = \sqrt{[(\sum_i^M \cos(2\phi_i))^2 + (\sum_i^M \sin(2\phi_i))^2] / M}$ calculated from the middle subevent (M is the number of particles). Each centrality bin has 5 equal width q_2 bins (q_2 cuts are the same for all centralities).
- 4) Accumulate $\cos(2(\phi_1 - \phi_2))$. One phi from $-1 < \eta < -0.3$ and the other is from $0.3 < \eta < 1.0$
- 5) Event Plane (EP) from $-1 < \eta < -0.3$ and four ΔS distributions (real event, shuffled, both perpendicular and parallel to RP) using POI from $0.3 < \eta < 1.0$, and vice versa
- 6) EP Resolution from $\sqrt{\langle \cos(2(\Psi_1 - \Psi_2)) \rangle}$

[Steps 4, 5, 6 are done for each q_2 bin in each centrality]

ESE Analysis Procedure II

7) Add $\cos(2(\phi_1 - \phi_2))$ for each q2 bin over the 3 centrality bins and calculate

$$v_2 = \sqrt{\langle \cos(2(\phi_1 - \phi_2)) \rangle}$$

8) For each q2 bin in each centrality calculate $\xi = \frac{1}{\sigma'^2}$ via RMS method

- $\xi = \frac{1}{\sigma'^2} = \left(\frac{\sigma_{m,sh}^2}{\sigma_m^2} - 1 \right) - \left(\frac{\sigma_{m,sh}^2}{\sigma_{m\perp}^2} - \frac{\sigma_{m\perp,sh}^2}{\sigma_{m\perp}^2} \right)$: Single (Shuffled) Normalization

- $\xi = \frac{1}{\sigma'^2} = \left(\frac{\sigma_{m,sh}^2}{\sigma_m^2} - \frac{\sigma_{m\perp,sh}^2}{\sigma_{m\perp}^2} \right)$: Two (Shuffled) Normalization

9) Correct by EP resolution (δ_{rm}^2): $\xi^{Cor} = \xi \times \frac{-1}{\delta_{rm}^2}$

10) For each q2 bin, take the average ξ^{Cor} over the three centrality bins weighted by the number of events. This is for the ξ^{Cor} vs. v_2 plot.

11) All ξ 's on all plots are already corrected for EP Resolution, so we only use ξ^{Cor} for backup slides discussing EP Resolution Correction

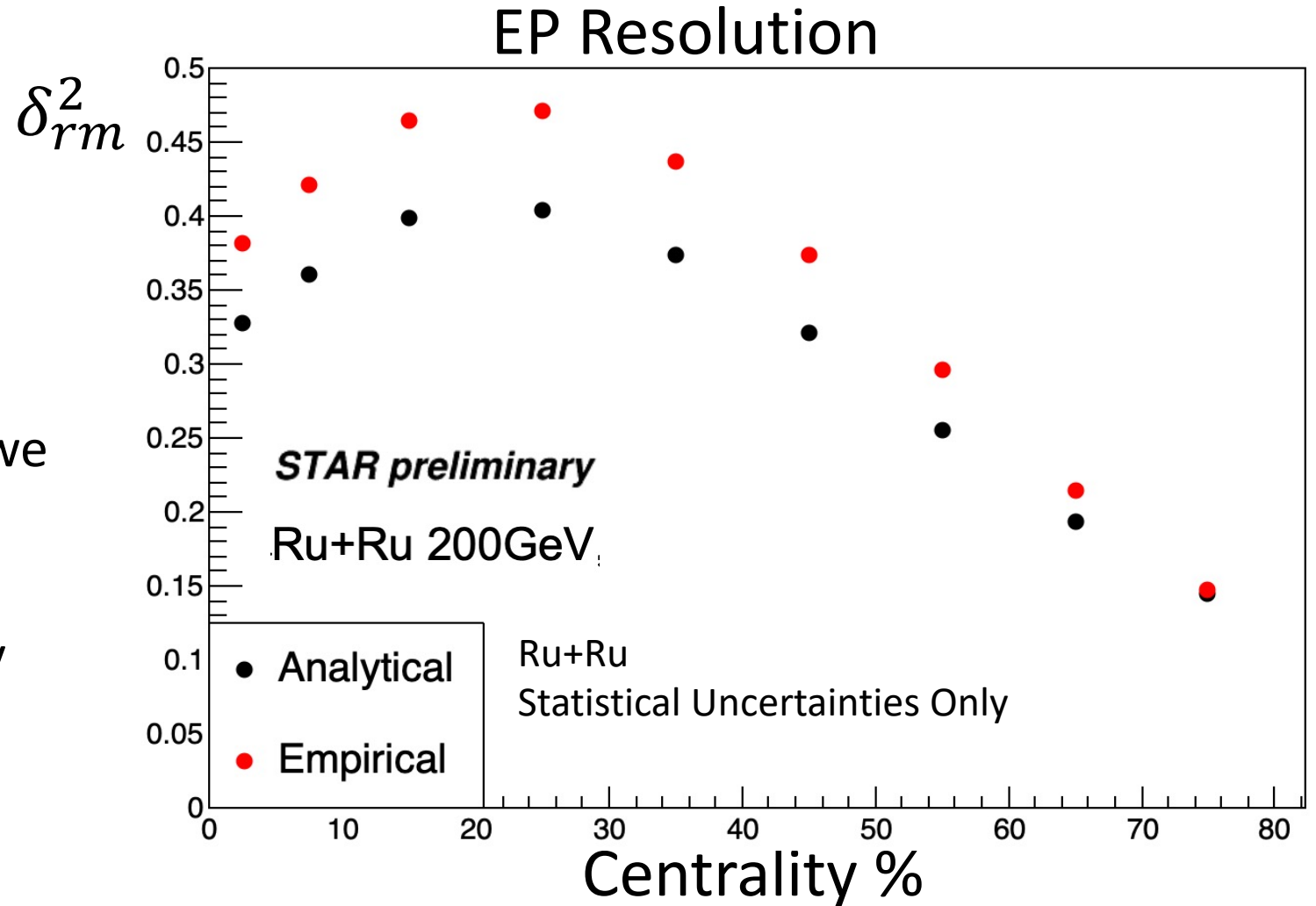
Event Plane Resolution Correction

- ξ also affected by EP Resolution (δ_{rm}^2):

- $\xi^{Cor} = \xi \times \frac{-1}{\delta_{rm}^2}$

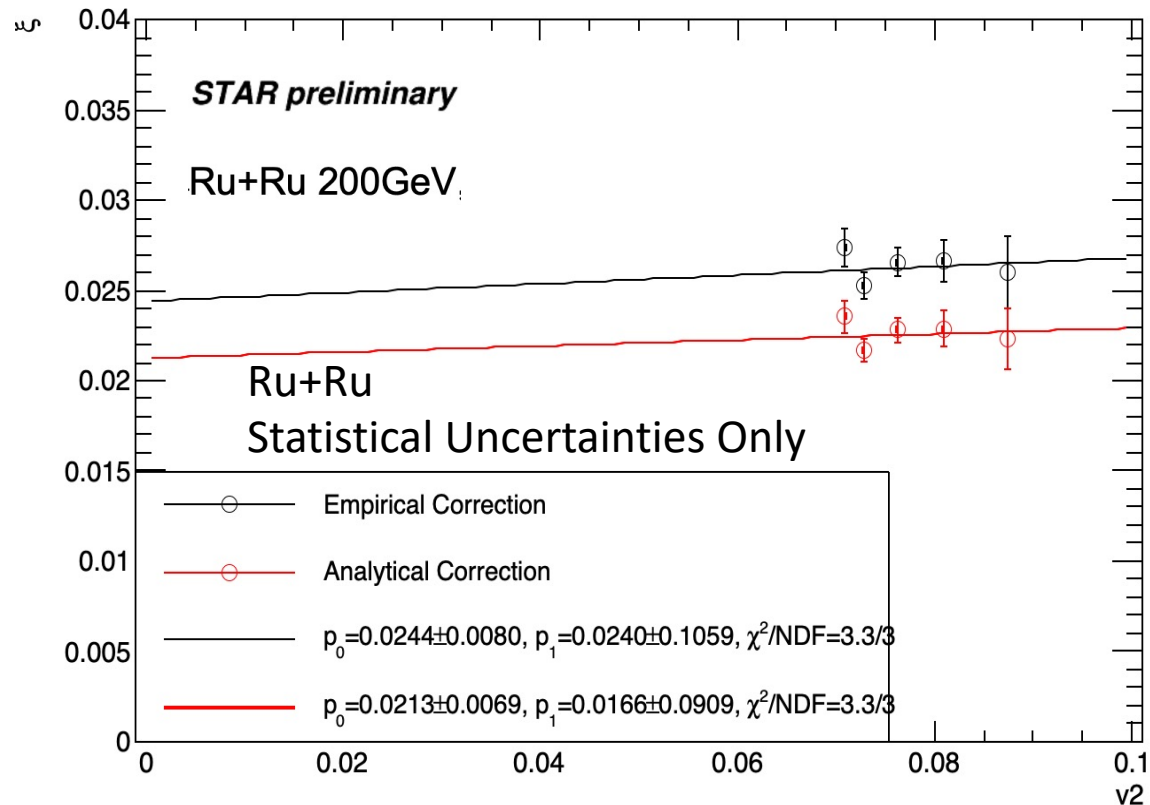
- 2 ways to get EP Resolution, we use empirical in this study

- All ξ 's on all plots are already corrected for EP Resolution

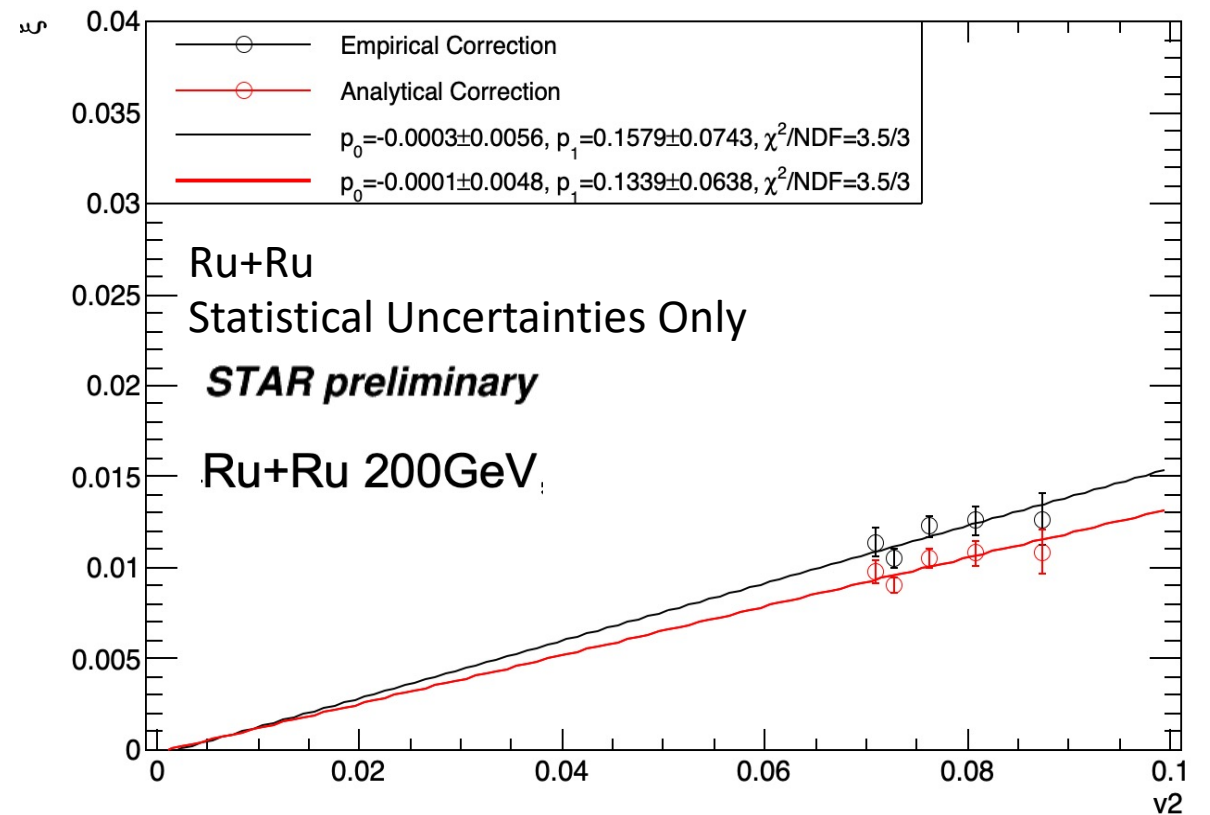


EP Resolution Correction Comparison: ξ vs v_2 for Cent 20-50%

Average Subevent ξ vs v_2 for Cent 20-50%

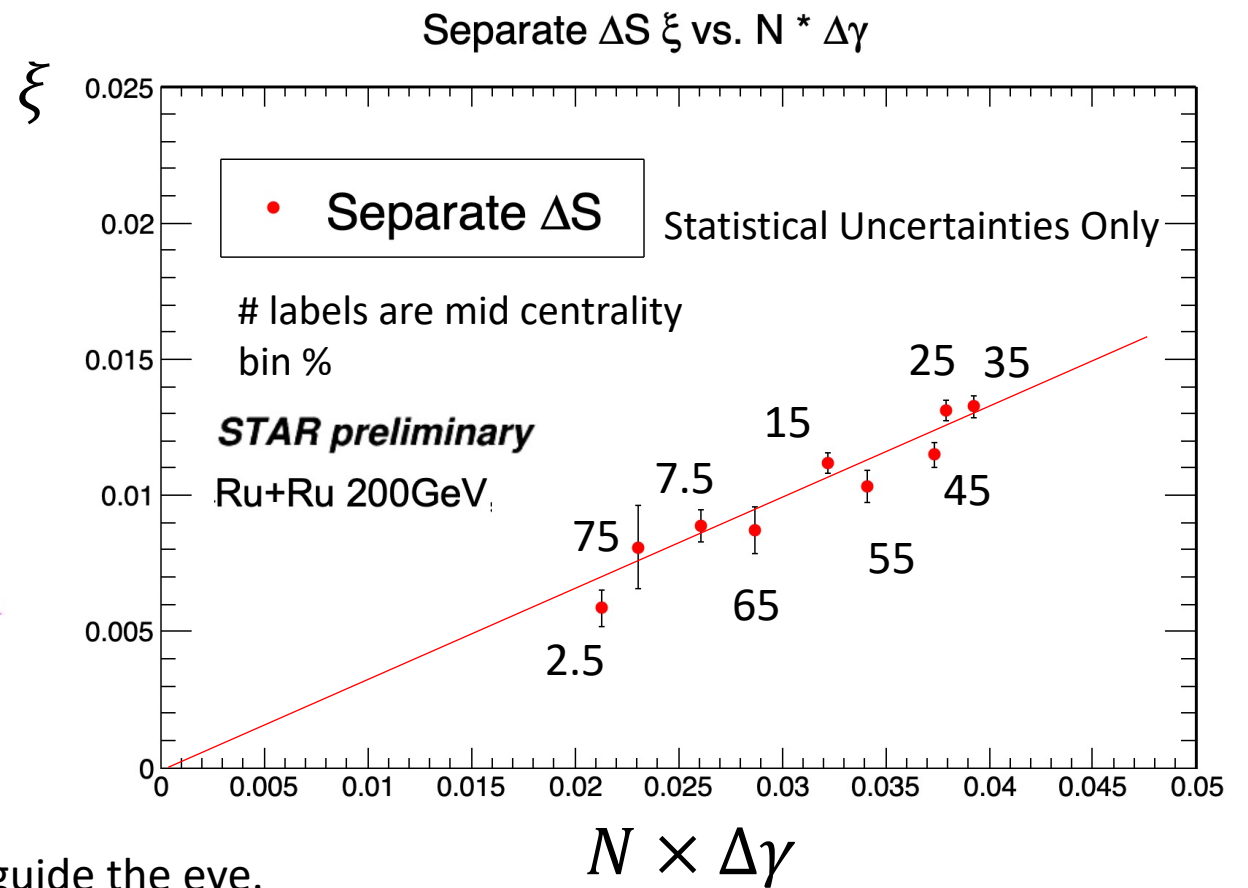
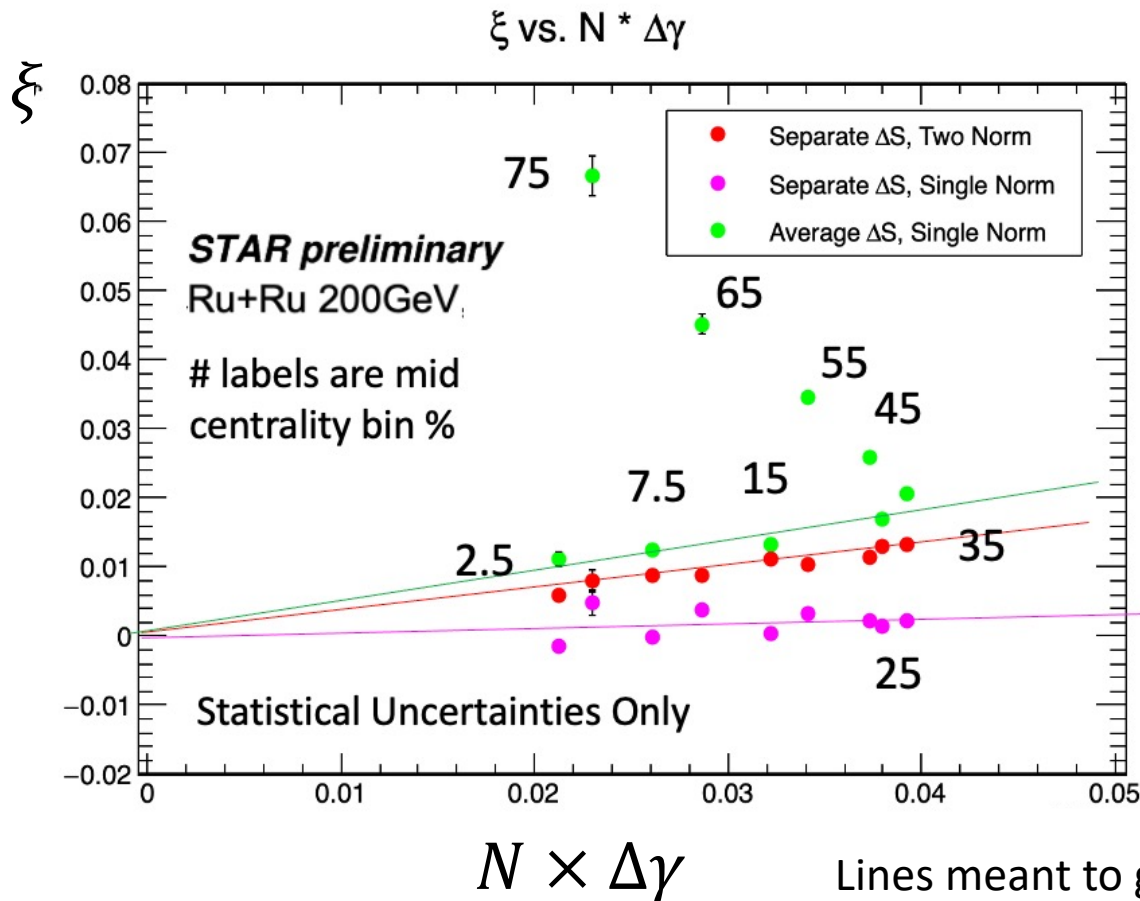


Separate Subevent ξ vs v_2 for Cent 20-50%



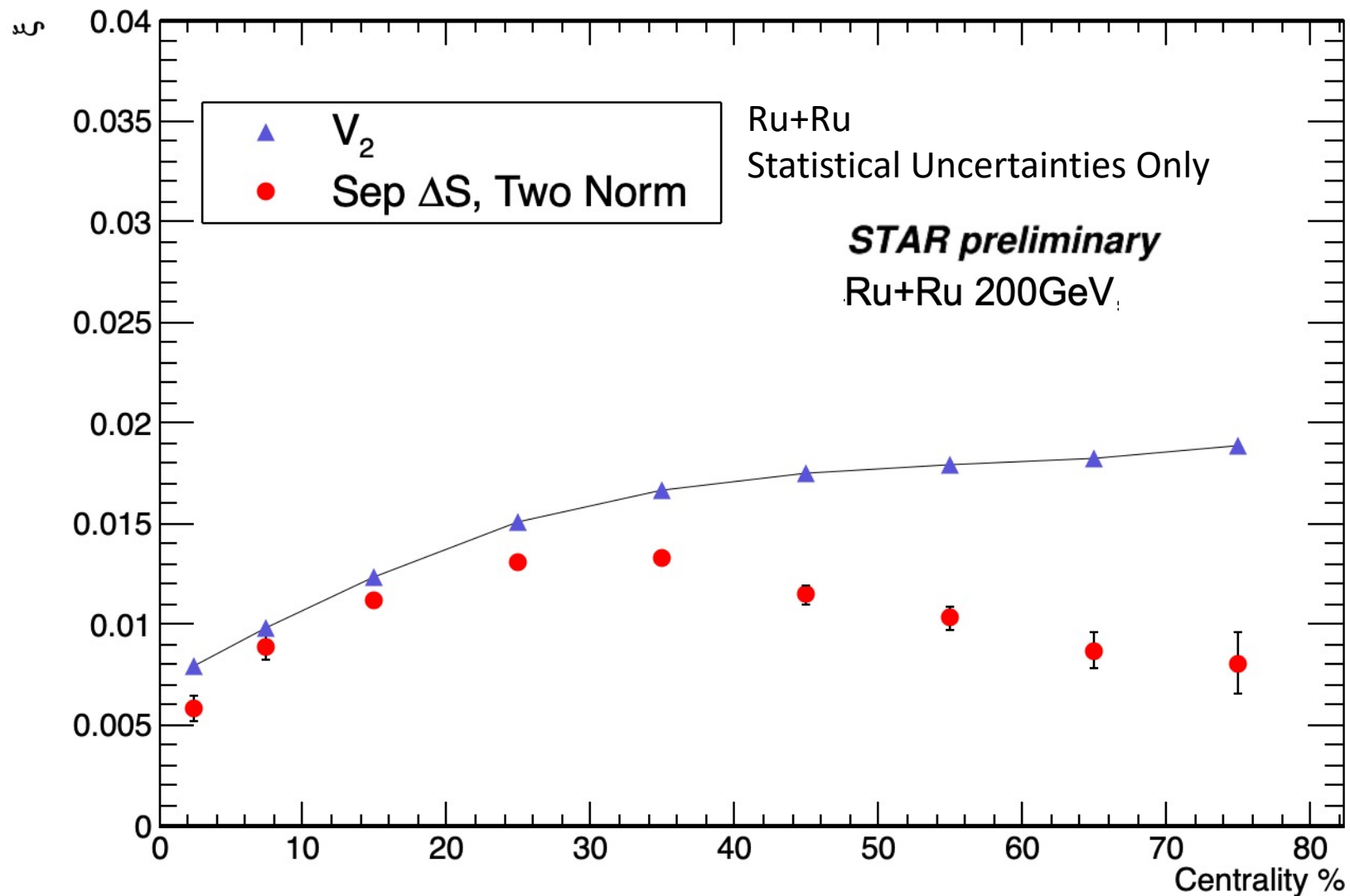
ξ vs $\langle N_{offline} \rangle \times \Delta\gamma$ Check

Separate ΔS and different treatments of normalization affect the correlation between ξ and $N * \Delta\gamma$



Lines meant to guide the eye.
They are not fits.

ξ and v_2 vs. Centrality



v_2 scaled by 0.25 to plot on same scale with ξ

Only interested in shape of v_2 and ξ vs. centrality in this plot

Normalization and EP Resolution effects on ξ

