

# Measurement of the Collins Asymmetry in Mid-Rapidity Jets at STAR

*Robert Fersch*  
*University of Kentucky*

Presentation for the High- $p_T$  Physics at  
RHIC RBRC Workshop

# **Goals of this Presentation:**

# Goals of this Presentation:

- Present a survey of quark transversity ( $\delta q$ ) and partonic spin degrees of freedom (Motivation)

# Goals of this Presentation:

- Present a survey of quark transversity ( $\delta q$ ) and partonic spin degrees of freedom (Motivation)
- Conduct a relevant overview of the experimental apparatus (STAR) and Jet Reconstruction

# Goals of this Presentation:

- Present a survey of quark transversity ( $\delta q$ ) and partonic spin degrees of freedom (Motivation)
- Conduct a relevant overview of the experimental apparatus (STAR) and Jet Reconstruction
- Relate of  $\delta q$  to the experimentally measurable Collins asymmetry

# Goals of this Presentation:

- Present a survey of quark transversity ( $\delta q$ ) and partonic spin degrees of freedom (Motivation)
- Conduct a relevant overview of the experimental apparatus (STAR) and Jet Reconstruction
- Relate  $\delta q$  to the experimentally measurable Collins asymmetry
- Demonstrate kinematic coverage of the data and physics in terms of  $p_T$

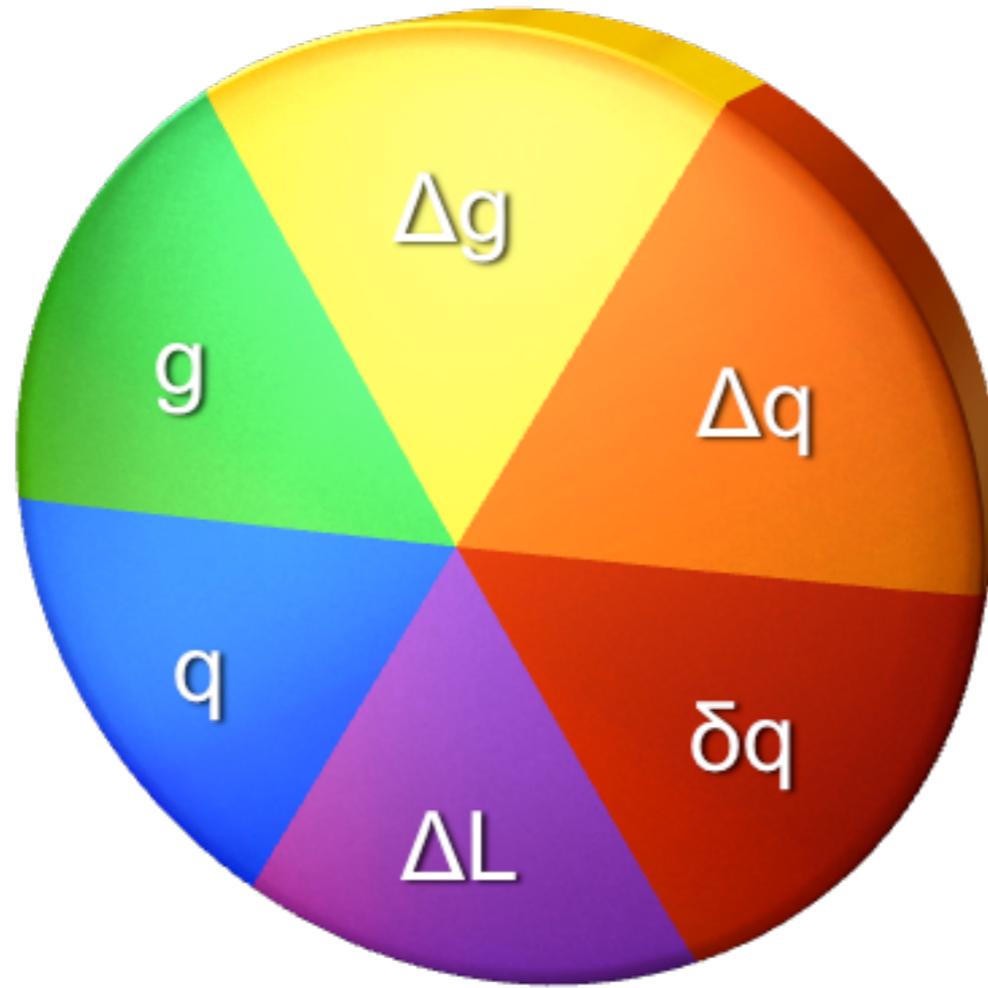
# Goals of this Presentation:

- Present a survey of quark transversity ( $\delta q$ ) and partonic spin degrees of freedom (Motivation)
- Conduct a relevant overview of the experimental apparatus (STAR) and Jet Reconstruction
- Relate  $\delta q$  to the experimentally measurable Collins asymmetry
- Demonstrate kinematic coverage of the data and physics in terms of  $p_T$
- Show statistical expectations of measured asymmetries and summarize systematic concerns

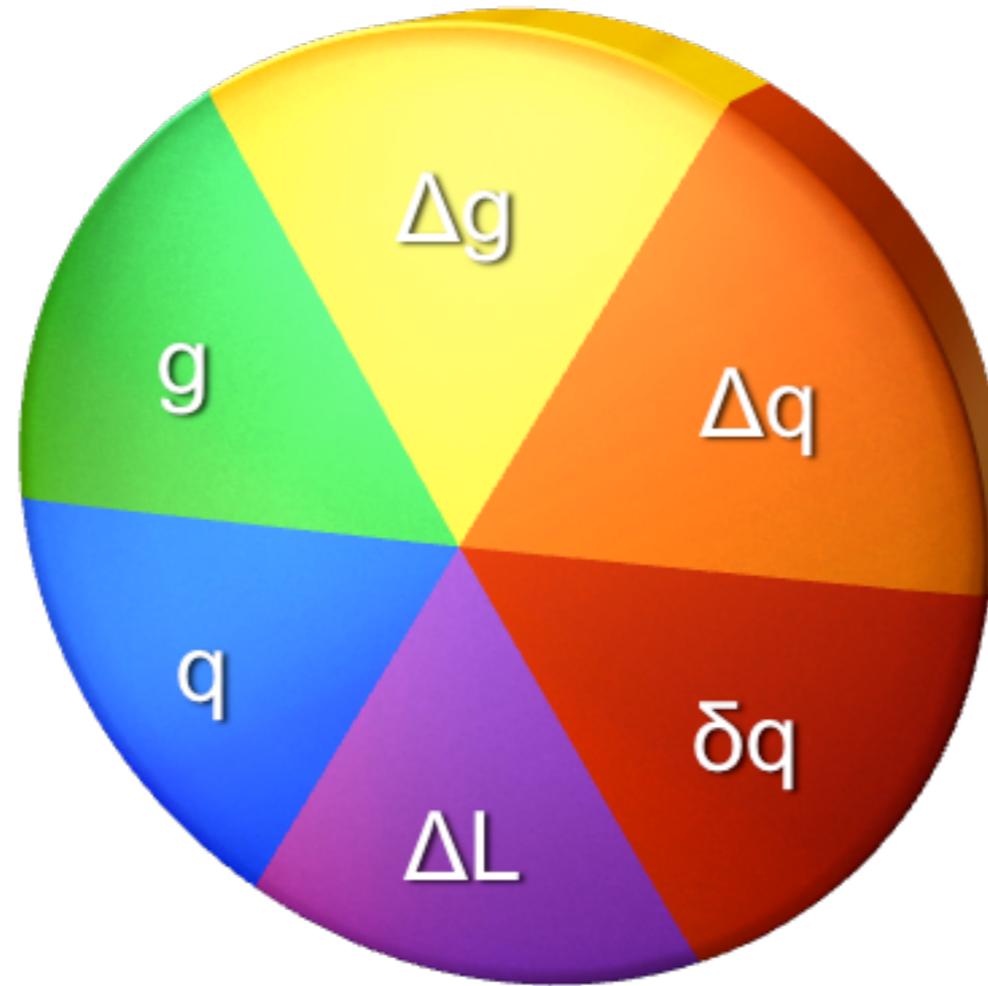
# Goals of this Presentation:

- Present a survey of quark transversity ( $\delta q$ ) and partonic spin degrees of freedom (Motivation)

# Degrees of Freedom in the Proton



# Degrees of Freedom in the Proton

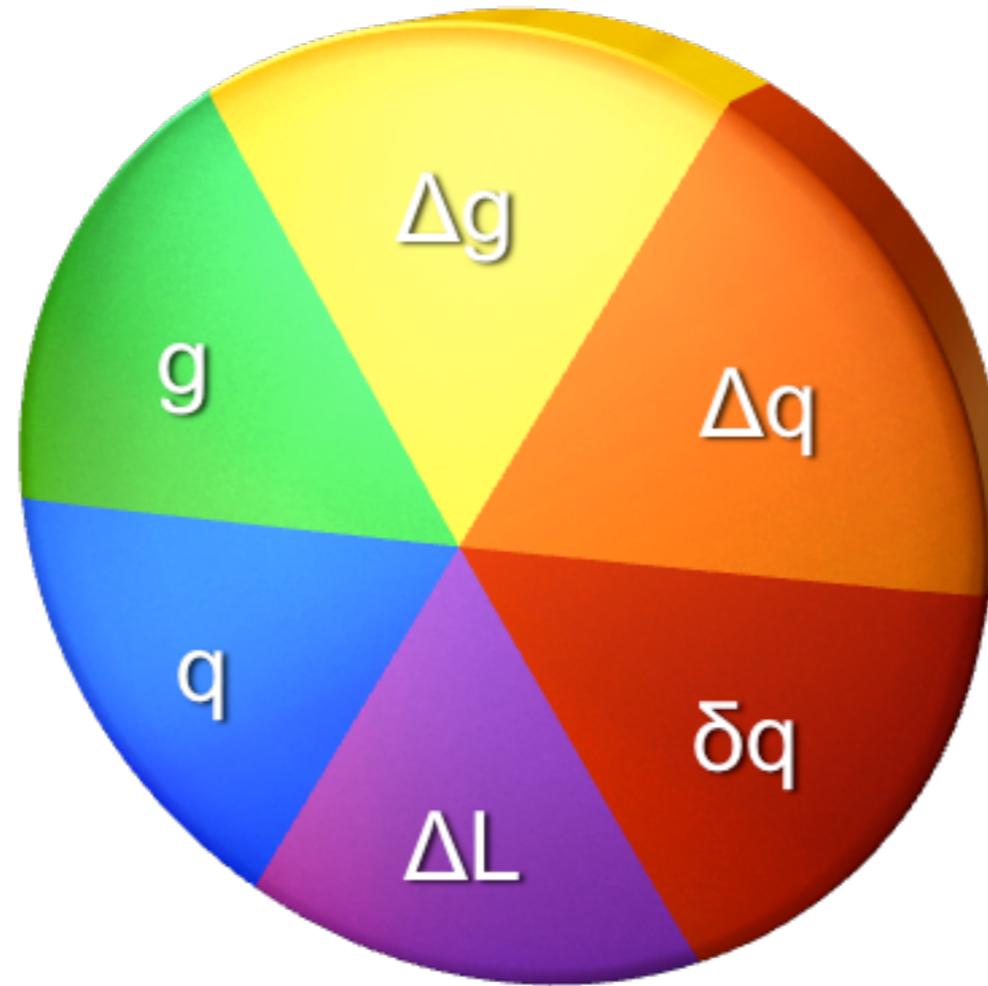


quark density

# Degrees of Freedom in the Proton

gluon density

quark density

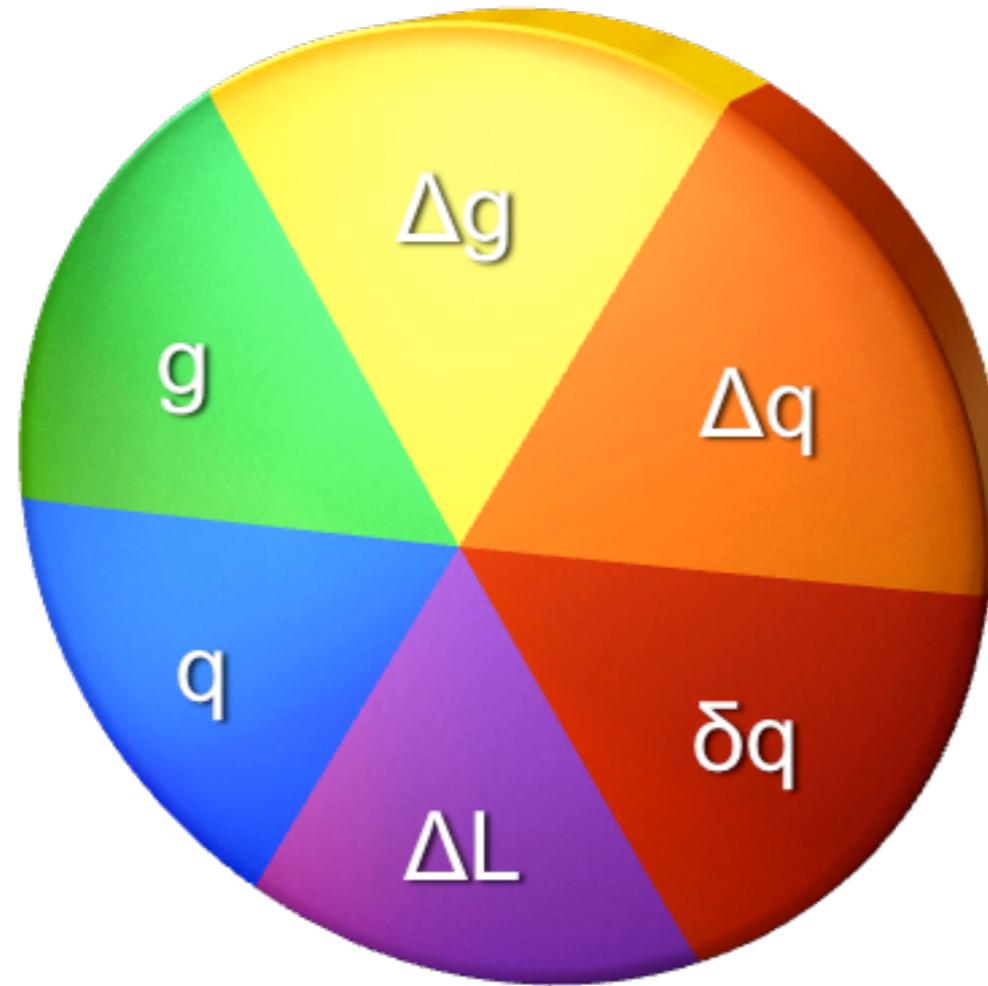


# Degrees of Freedom in the Proton

gluon helicity

gluon density

quark density



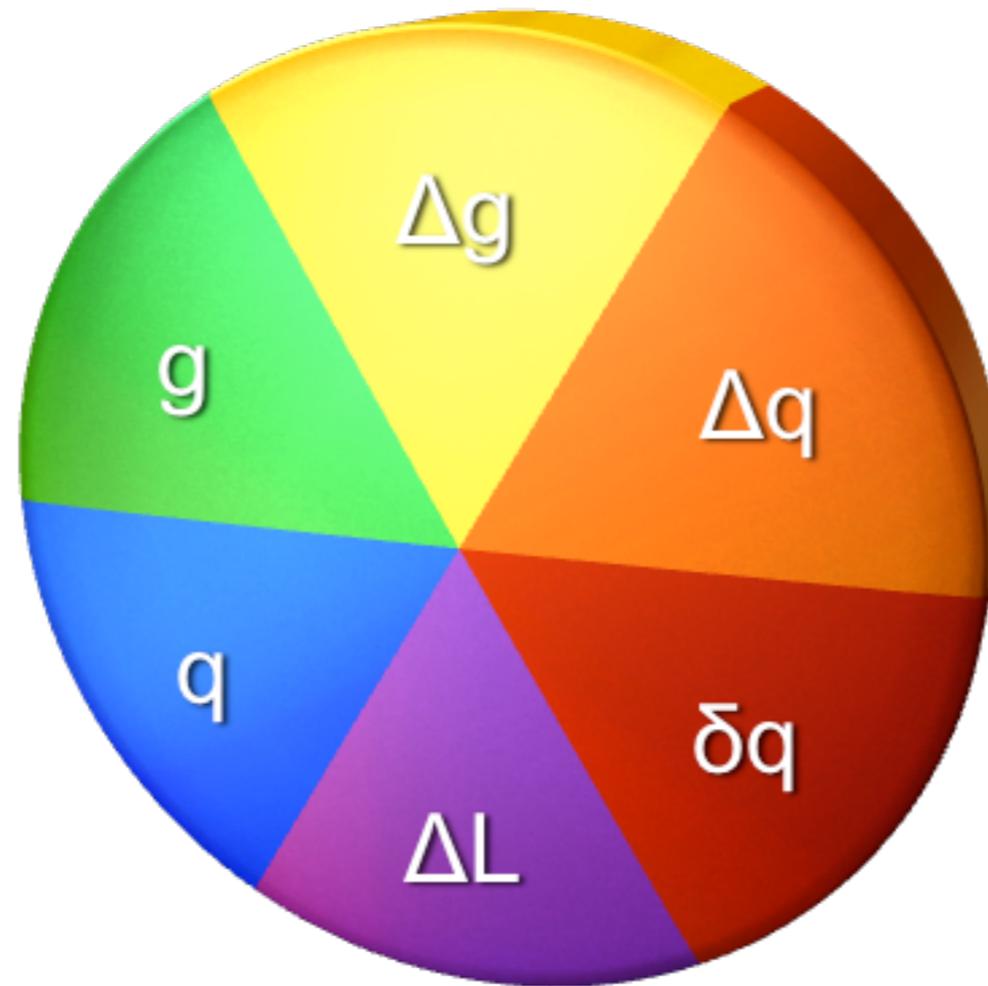
# Degrees of Freedom in the Proton

gluon helicity

gluon density

quark helicity

quark density



# Degrees of Freedom in the Proton

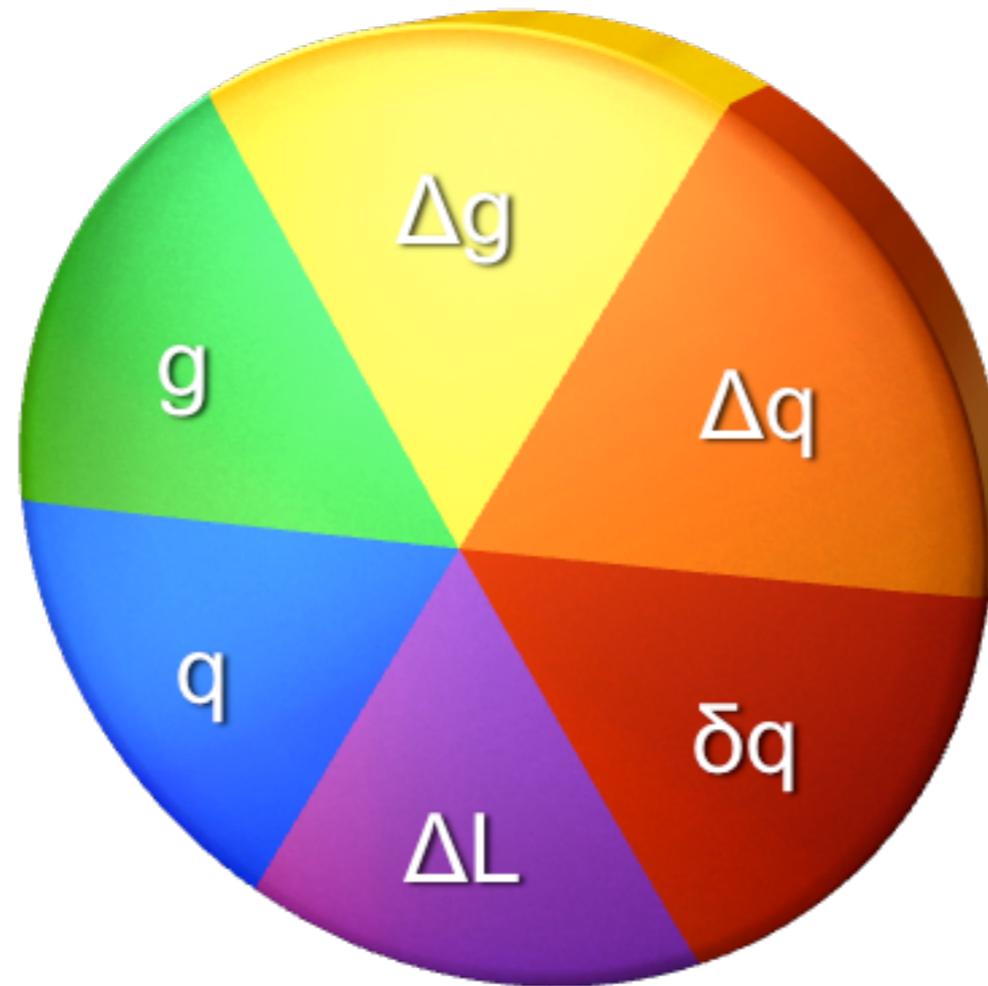
gluon helicity

gluon density

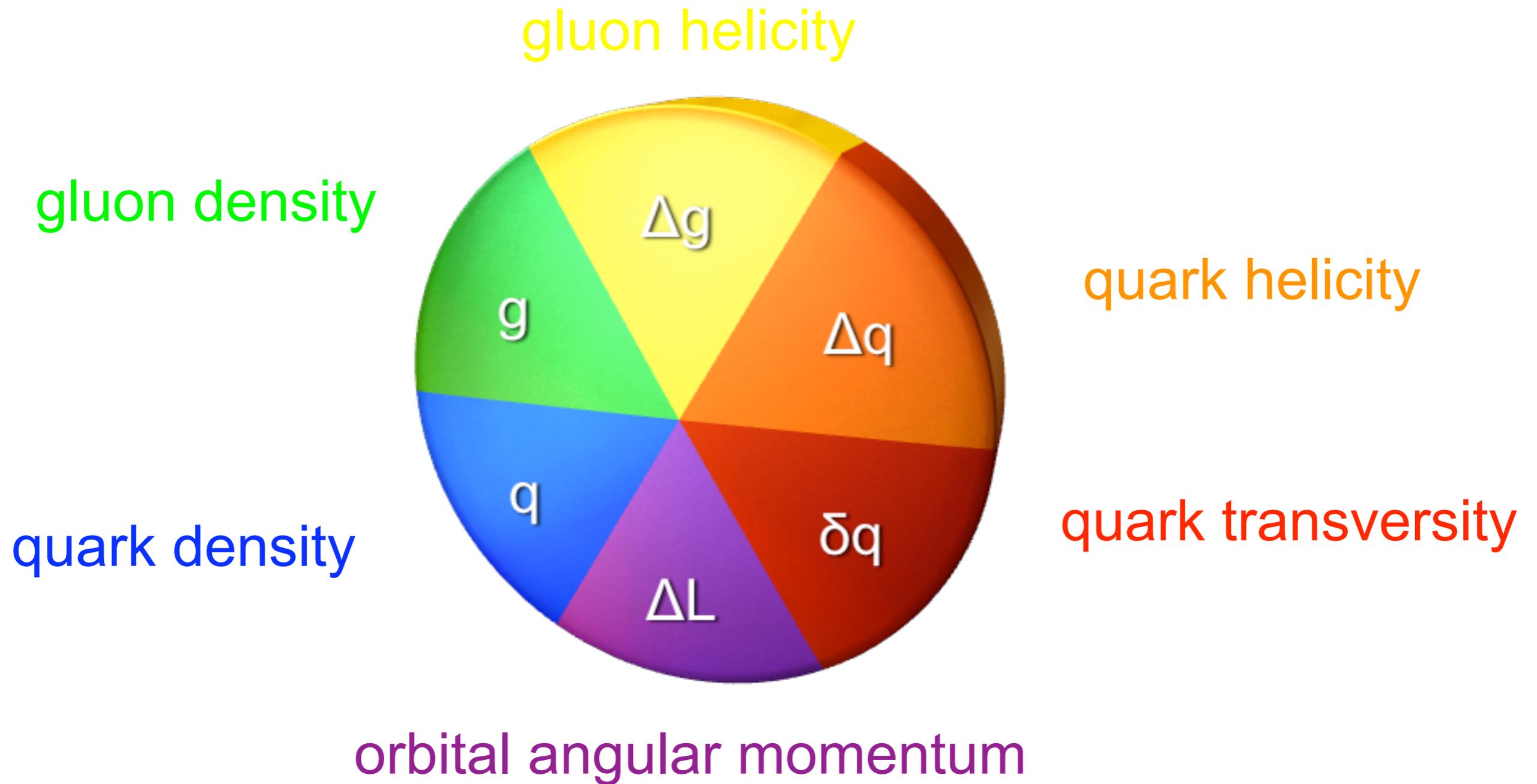
quark helicity

quark density

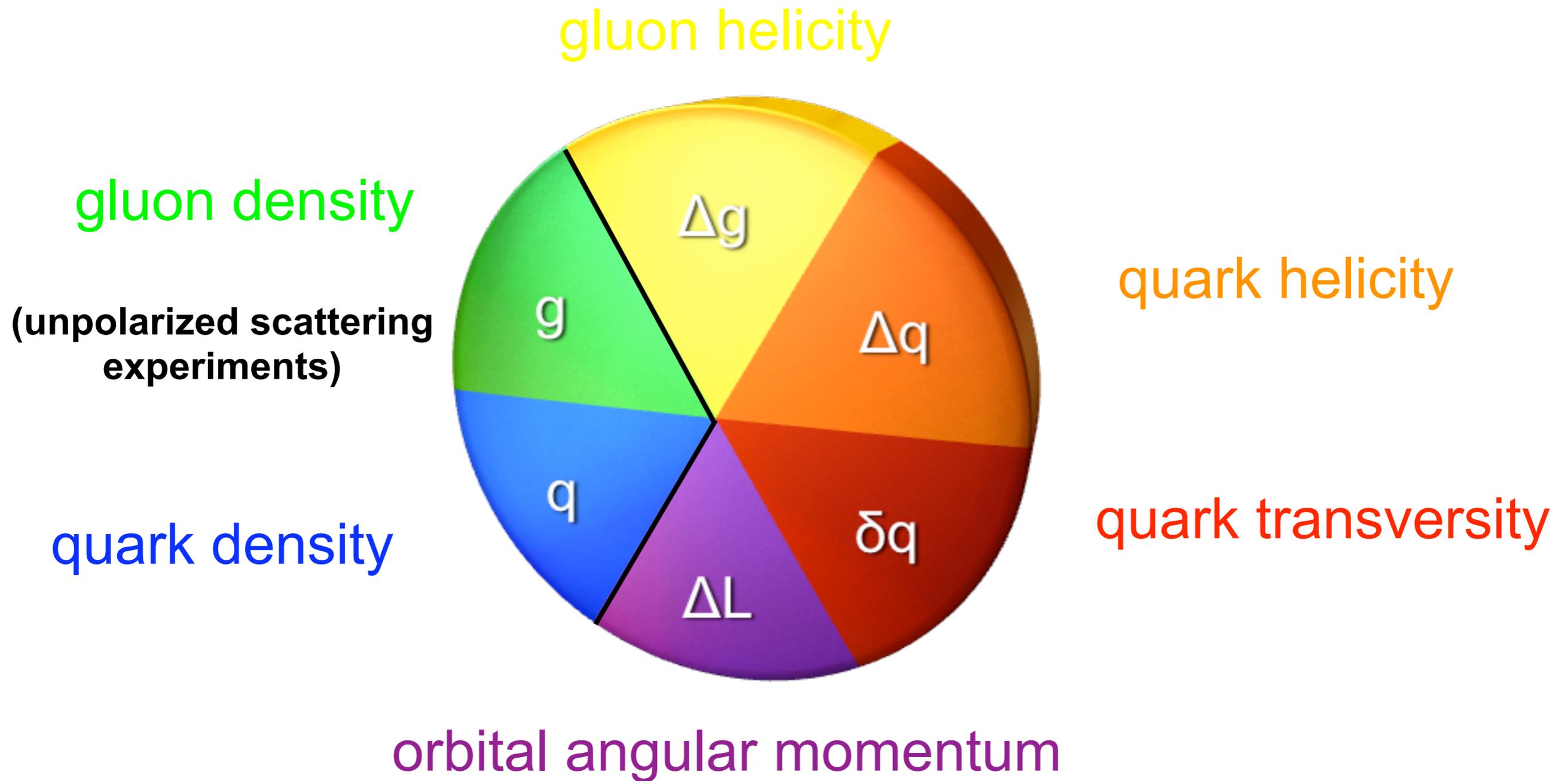
quark transversity



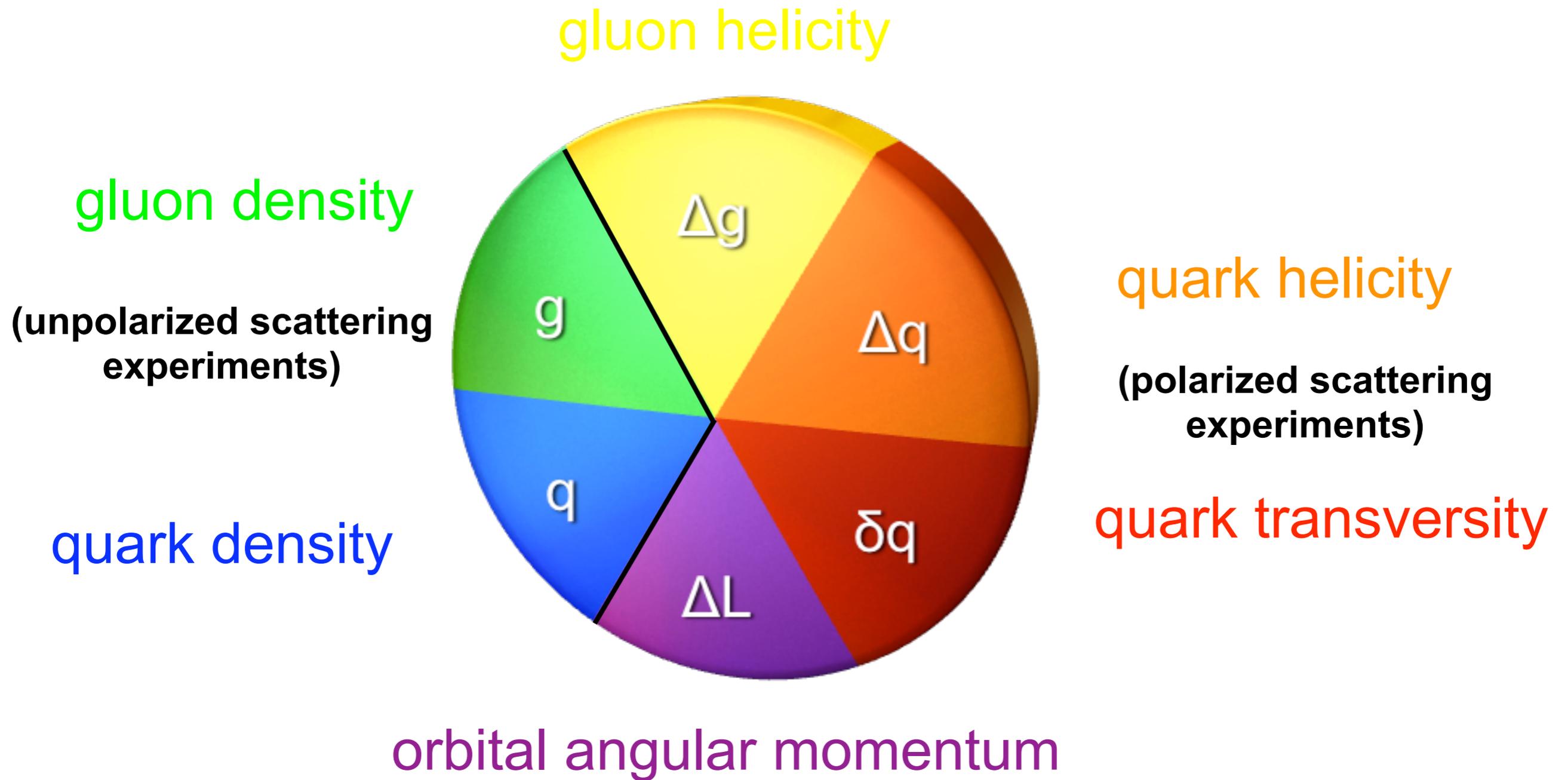
# Degrees of Freedom in the Proton



# Degrees of Freedom in the Proton



# Degrees of Freedom in the Proton



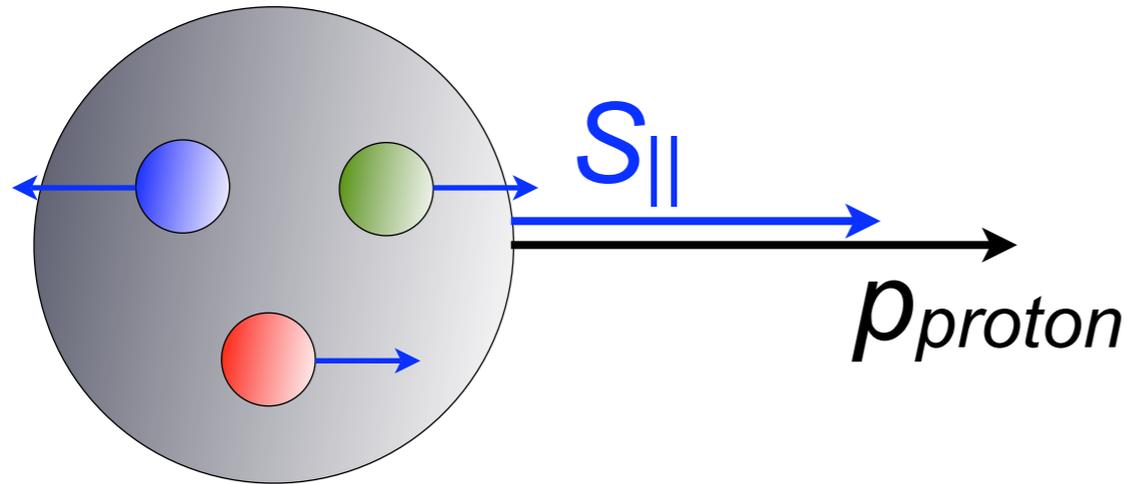
# Quark and Gluon Spin Distributions

# **Quark and Gluon Spin Distributions**

**longitudinal and transverse degrees of freedom**

# Quark and Gluon Spin Distributions

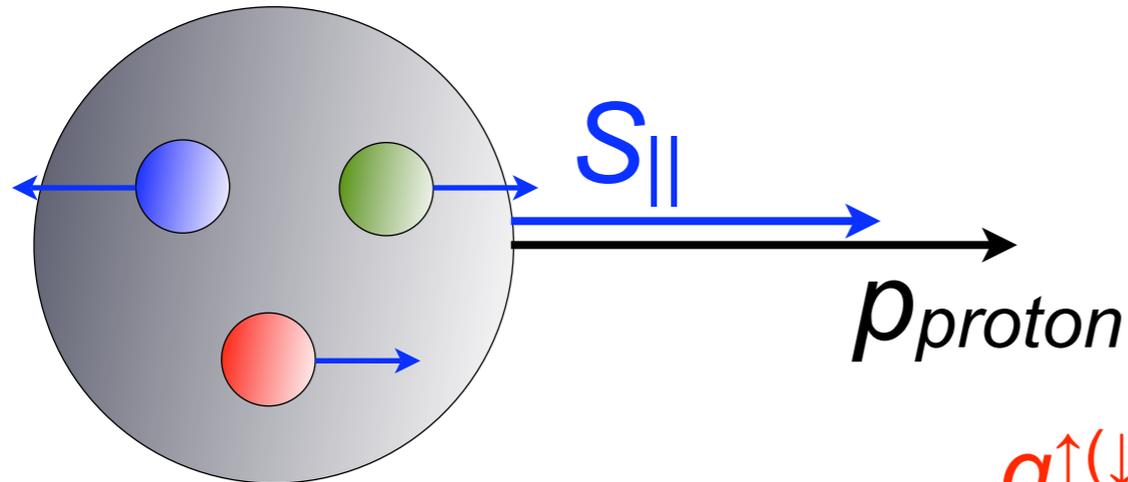
longitudinal and transverse degrees of freedom  
“helicity”



# Quark and Gluon Spin Distributions

longitudinal and transverse degrees of freedom

“helicity”



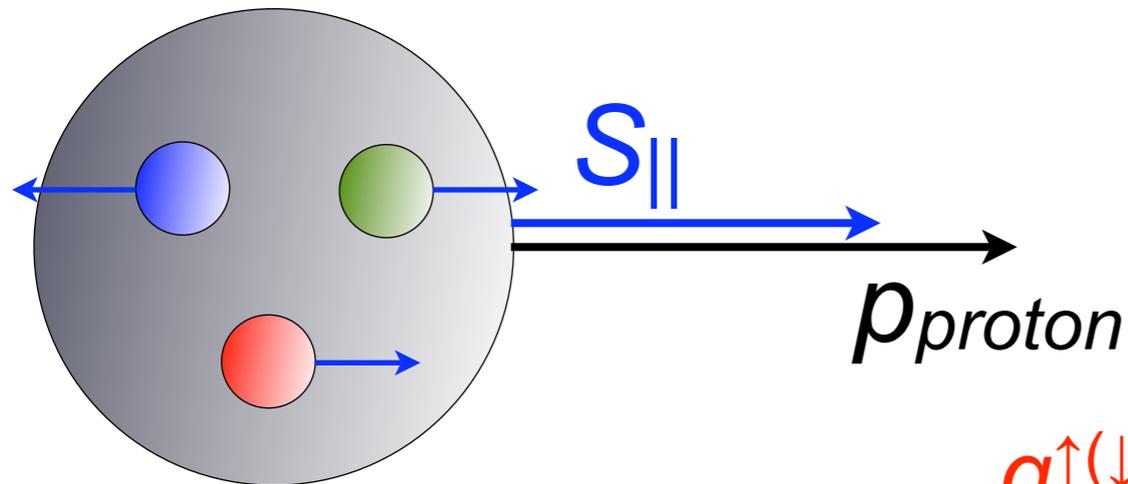
$$\Delta q \equiv q^{\uparrow} - q^{\downarrow}$$

$q^{\uparrow(\downarrow)}$  is the probability of finding a quark with spin equal (opposite) to  $S_{||}$

# Quark and Gluon Spin Distributions

longitudinal and transverse degrees of freedom

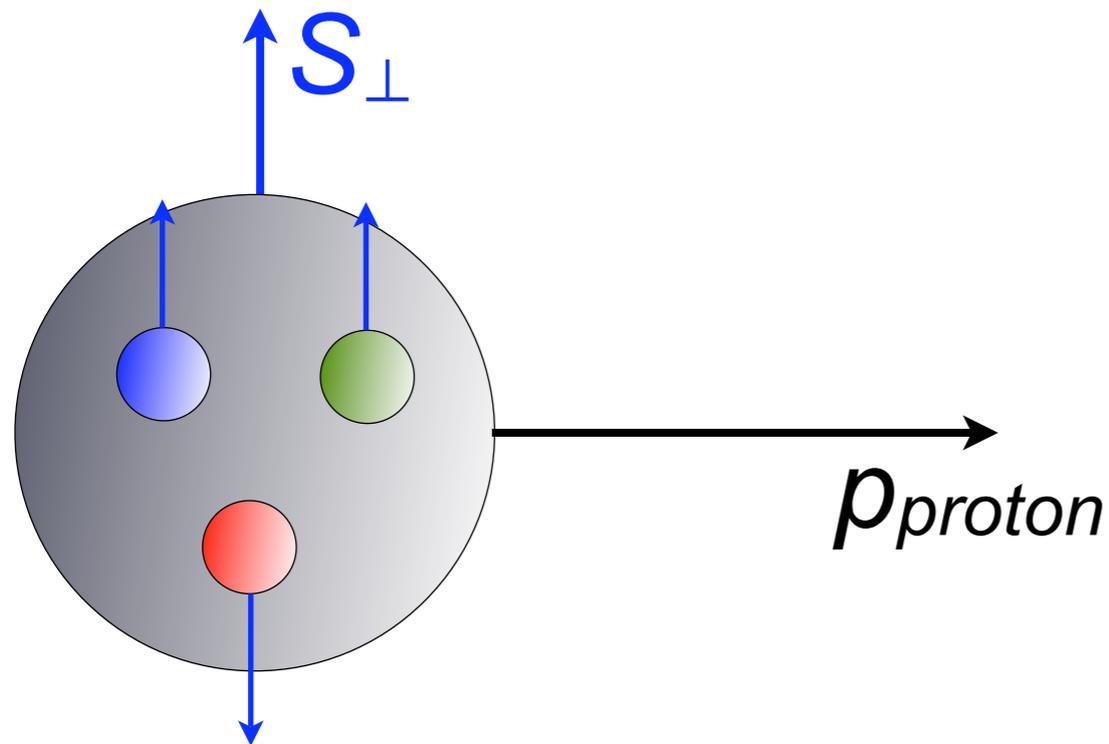
“helicity”



$$\Delta q \equiv q^{\uparrow} - q^{\downarrow}$$

$q^{\uparrow(\downarrow)}$  is the probability of finding a quark with spin equal (opposite) to  $S_{||}$

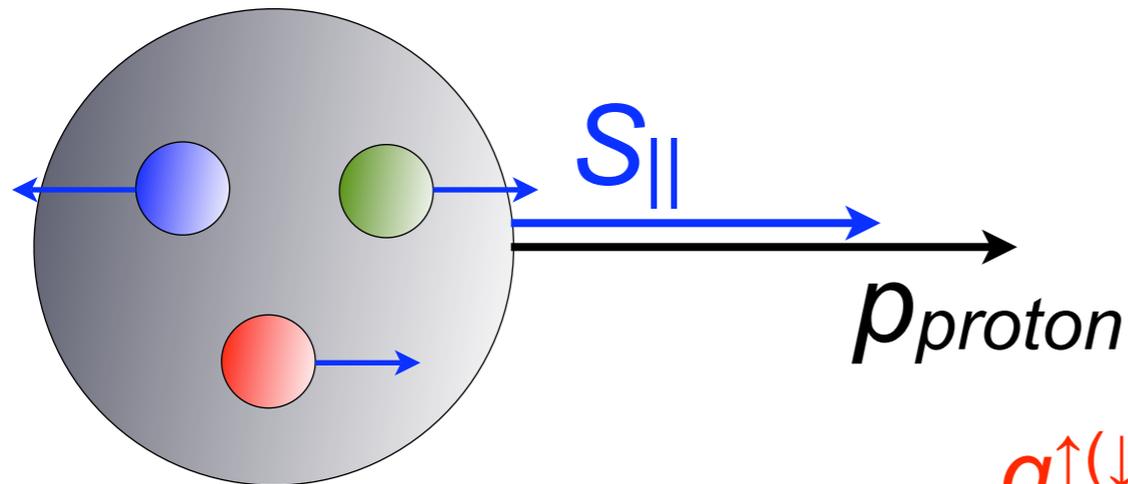
“transversity”



# Quark and Gluon Spin Distributions

longitudinal and transverse degrees of freedom

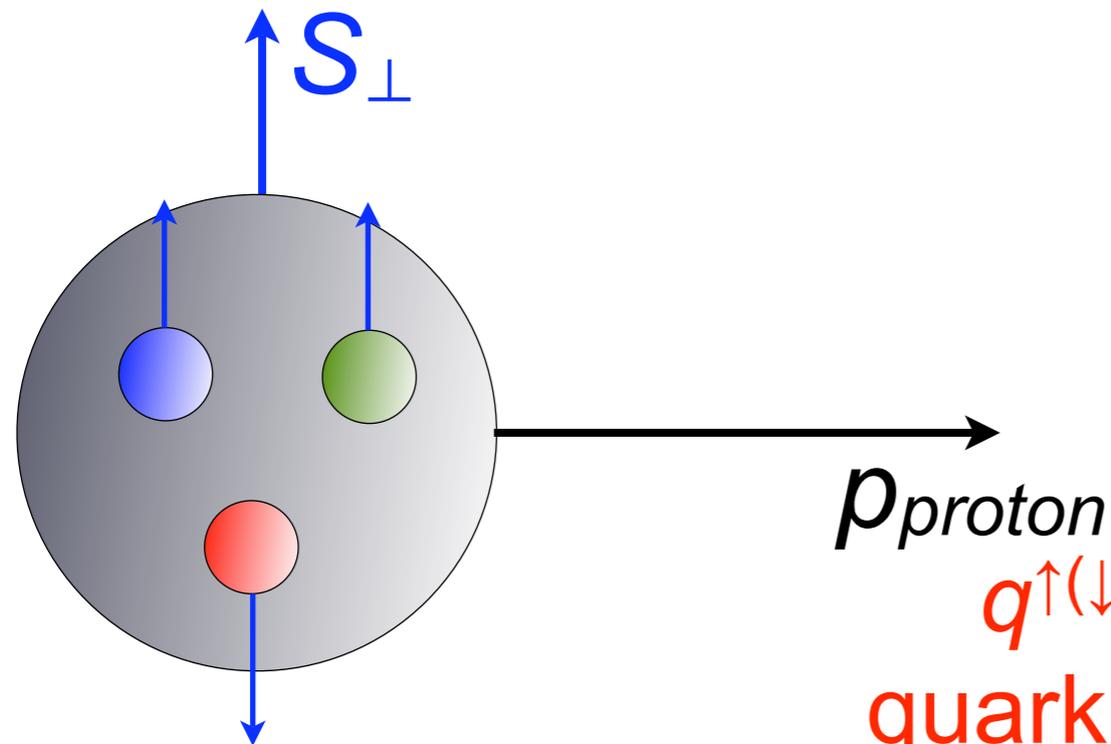
“helicity”



$$\Delta q \equiv q^{\uparrow} - q^{\downarrow}$$

$q^{\uparrow(\downarrow)}$  is the probability of finding a quark with spin equal (opposite) to  $S_{||}$

“transversity”



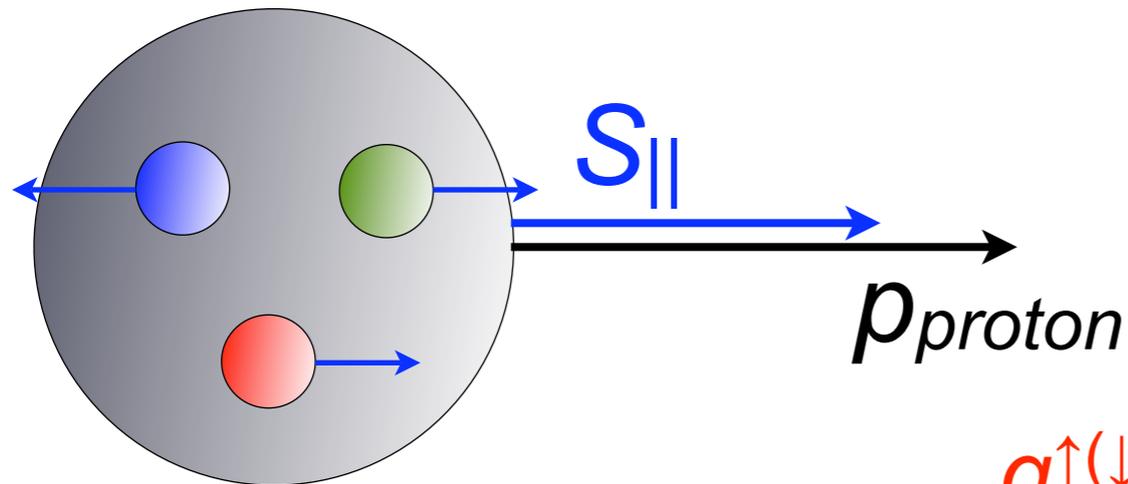
$$\delta q \equiv q^{\uparrow} - q^{\downarrow}$$

$q^{\uparrow(\downarrow)}$  is the probability of finding a quark with spin equal (opposite) to  $S_{\perp}$

# Quark and Gluon Spin Distributions

longitudinal and transverse degrees of freedom

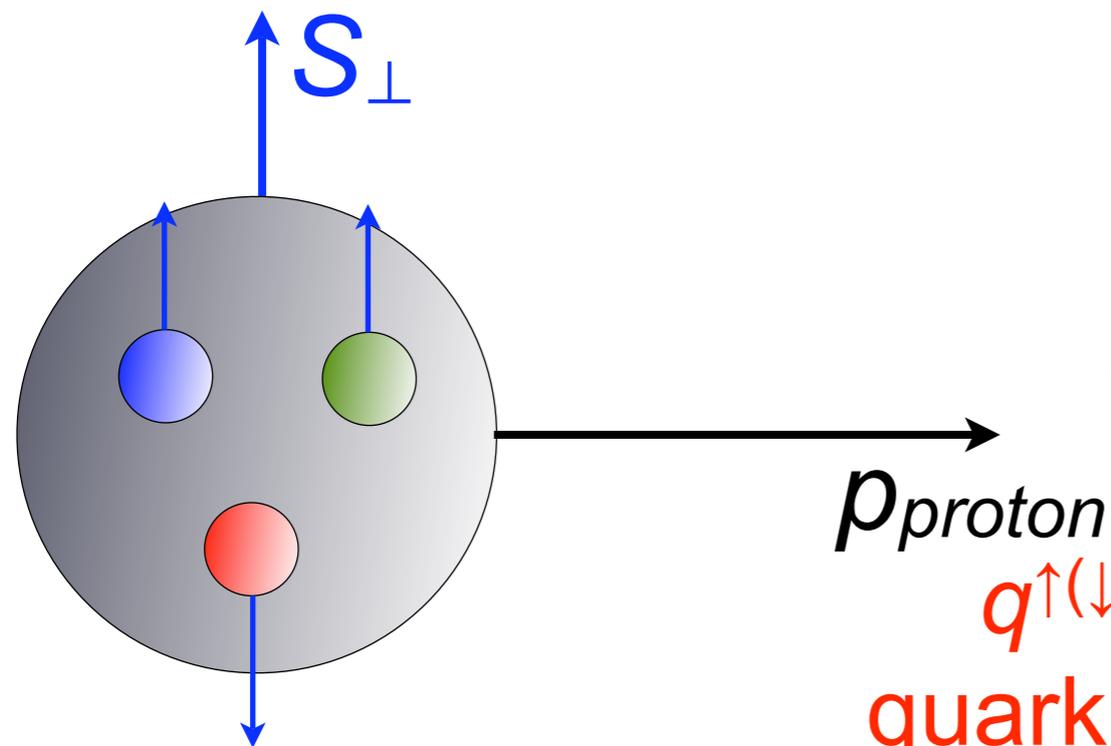
“helicity”



$$\Delta q \equiv q^{\uparrow} - q^{\downarrow}$$

$q^{\uparrow(\downarrow)}$  is the probability of finding a quark with spin equal (opposite) to  $S_{||}$

“transversity”



$$\delta q \equiv q^{\uparrow} - q^{\downarrow}$$

$q$ ,  $\Delta q$ ,  $\delta q$  all required for a complete basis in spin-density matrix representation

$q^{\uparrow(\downarrow)}$  is the probability of finding a quark with spin equal (opposite) to  $S_{\perp}$

# **Existing Measurements of Spin Degrees of Freedom**

# Existing Measurements of Spin Degrees of Freedom

Asymmetries  $\Rightarrow$  Global Analysis  $\Rightarrow$  Parton Distribution Functions (PDFs)

# Existing Measurements of Spin Degrees of Freedom

Asymmetries  $\Rightarrow$  Global Analysis  $\Rightarrow$  Parton Distribution Functions (PDFs)

- Earliest data (polarized beam and targets) collected at SLAC, CERN

# Existing Measurements of Spin Degrees of Freedom

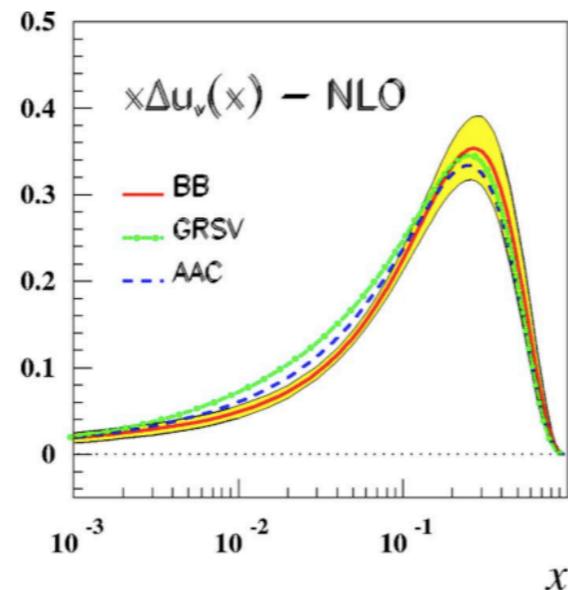
Asymmetries  $\Rightarrow$  Global Analysis  $\Rightarrow$  Parton Distribution Functions (PDFs)

- Earliest data (polarized beam and targets) collected at SLAC, CERN
- Later measurements by Jefferson Lab, DESY greatly increase precision

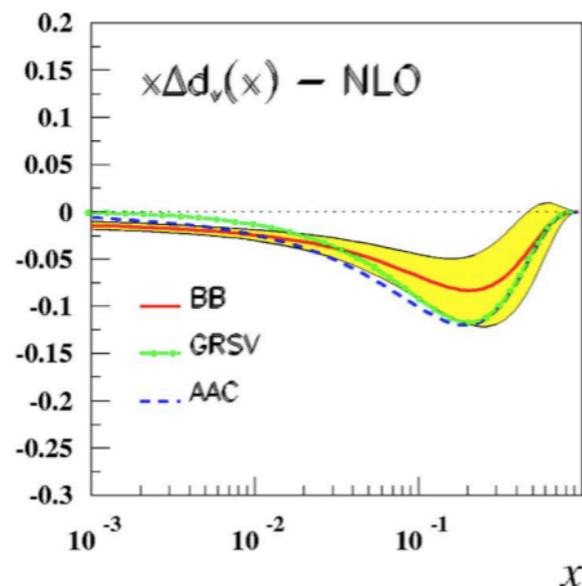
# Existing Measurements of Spin Degrees of Freedom

Asymmetries  $\Rightarrow$  Global Analysis  $\Rightarrow$  Parton Distribution Functions (PDFs)

$x \Delta u$



$x \Delta d$



- Earliest data (polarized beam and targets) collected at SLAC, CERN

- Later measurements by Jefferson Lab, DESY greatly increase precision

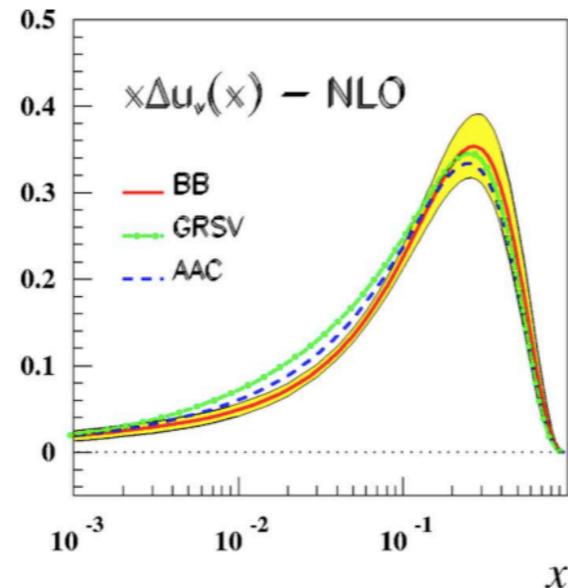
- Global Fits to World Data Shown for constituent quarks

# Existing Measurements of Spin Degrees of Freedom

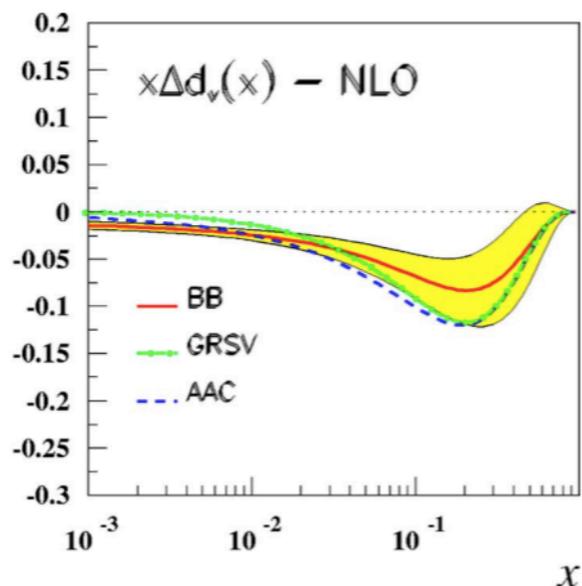
Asymmetries  $\Rightarrow$  Global Analysis  $\Rightarrow$  Parton Distribution Functions (PDFs)

Longitudinal spin  
(helicity)

$x \Delta u$



$x \Delta d$



- Earliest data (polarized beam and targets) collected at SLAC, CERN

- Later measurements by Jefferson Lab, DESY greatly increase precision

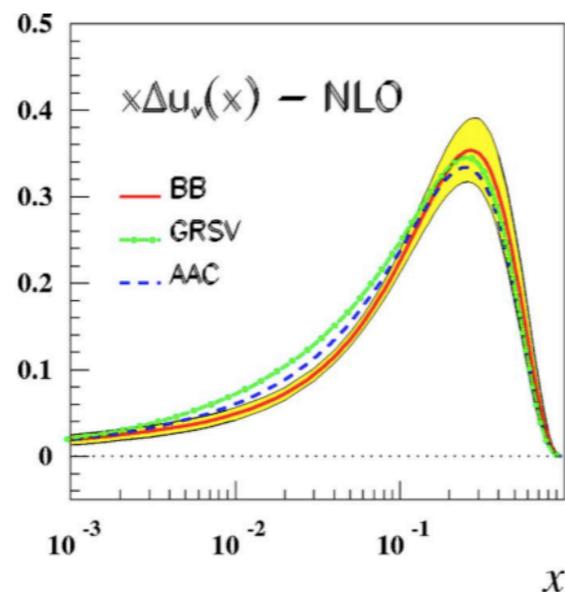
- Global Fits to World Data Shown for constituent quarks

# Existing Measurements of Spin Degrees of Freedom

Asymmetries  $\Rightarrow$  Global Analysis  $\Rightarrow$  Parton Distribution Functions (PDFs)

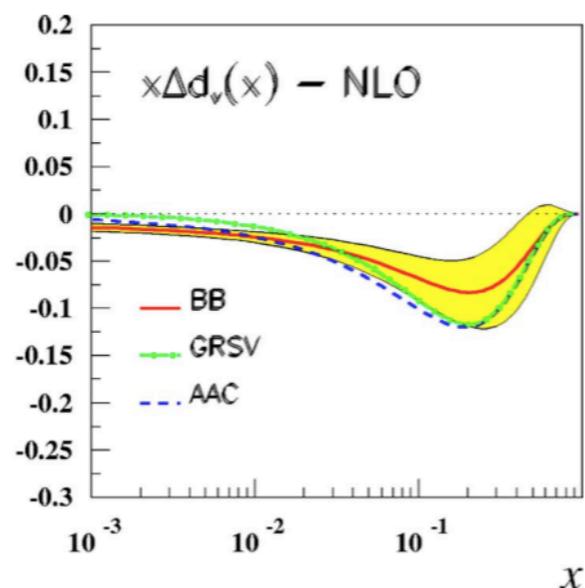
Longitudinal spin  
(helicity)

$x \Delta u$



$x \equiv$  Bjorken  $x$   
( $0 < x < 1$ ); 1 = elastic  
limit

$x \Delta d$



- Earliest data (polarized beam and targets) collected at SLAC, CERN

- Later measurements by Jefferson Lab, DESY greatly increase precision

- Global Fits to World Data Shown for constituent quarks

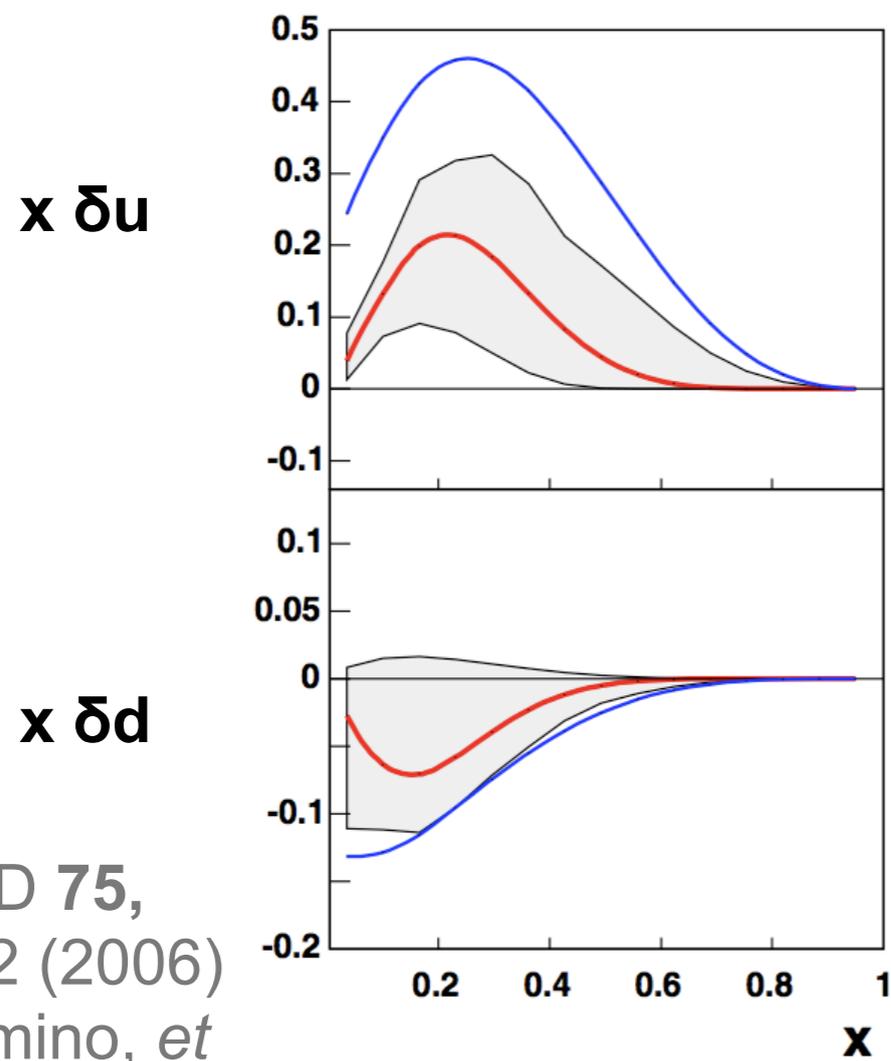
# Existing Measurements of Spin Degrees of Freedom

Asymmetries  $\Rightarrow$  Global Analysis  $\Rightarrow$  Parton Distribution Functions (PDFs)

# Existing Measurements of Spin Degrees of Freedom

Asymmetries  $\Rightarrow$  Global Analysis  $\Rightarrow$  Parton Distribution Functions (PDFs)

Transverse spin  
(transversity)



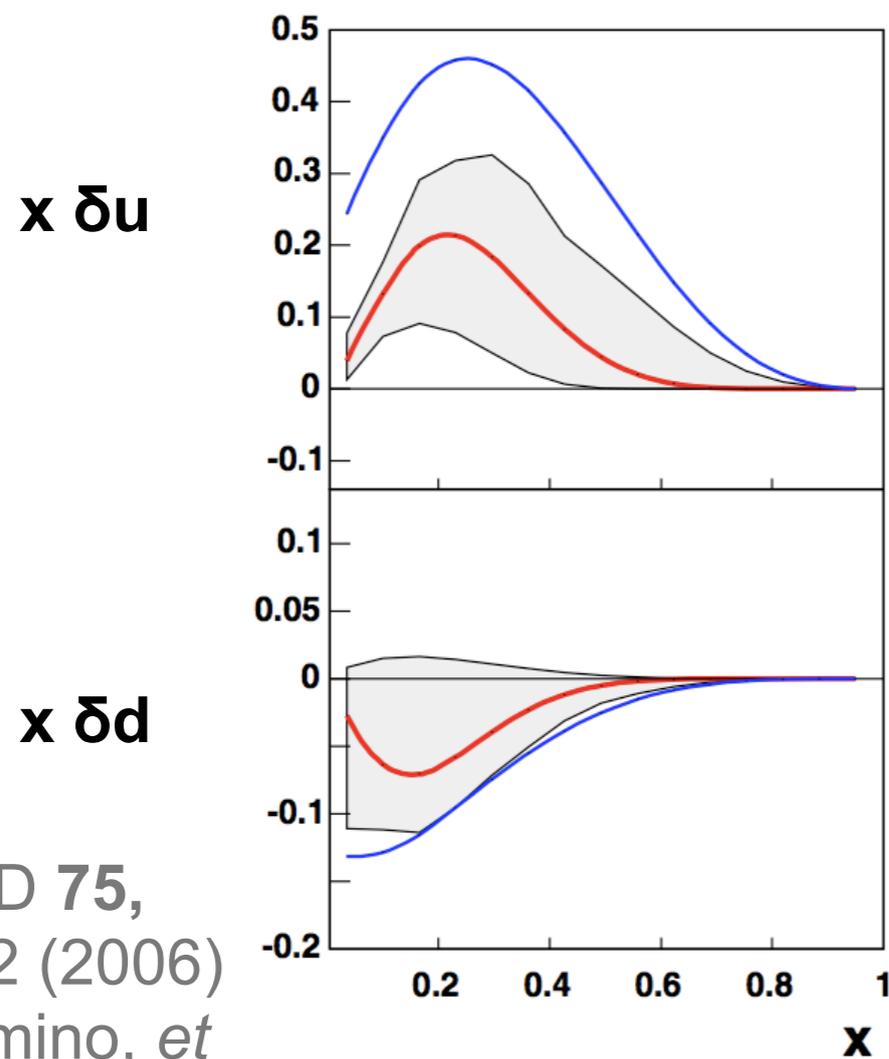
PRD 75,  
054032 (2006)  
Anselmino, *et al.*

# Existing Measurements of Spin Degrees of Freedom

Asymmetries  $\Rightarrow$  Global Analysis  $\Rightarrow$  Parton Distribution Functions (PDFs)

Transverse spin  
(transversity)

- Requires transversely polarized beam(s) and/or target



PRD 75,  
054032 (2006)  
Anselmino, *et al.*

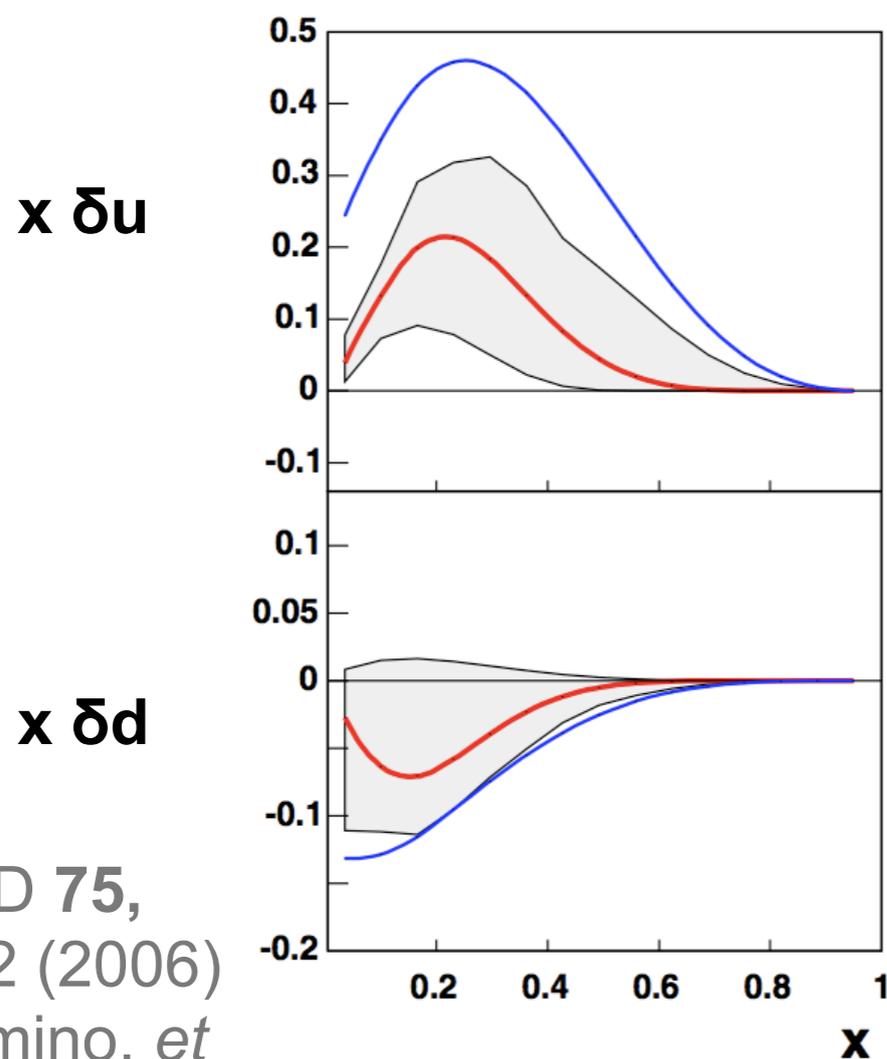
# Existing Measurements of Spin Degrees of Freedom

Asymmetries  $\Rightarrow$  Global Analysis  $\Rightarrow$  Parton Distribution Functions (PDFs)

Transverse spin  
(transversity)

- Requires transversely polarized beam(s) and/or target

- Very limited experimental data  
(Mostly contributed by Belle data)



PRD 75,  
054032 (2006)  
Anselmino, *et al.*

# Existing Measurements of Spin Degrees of Freedom

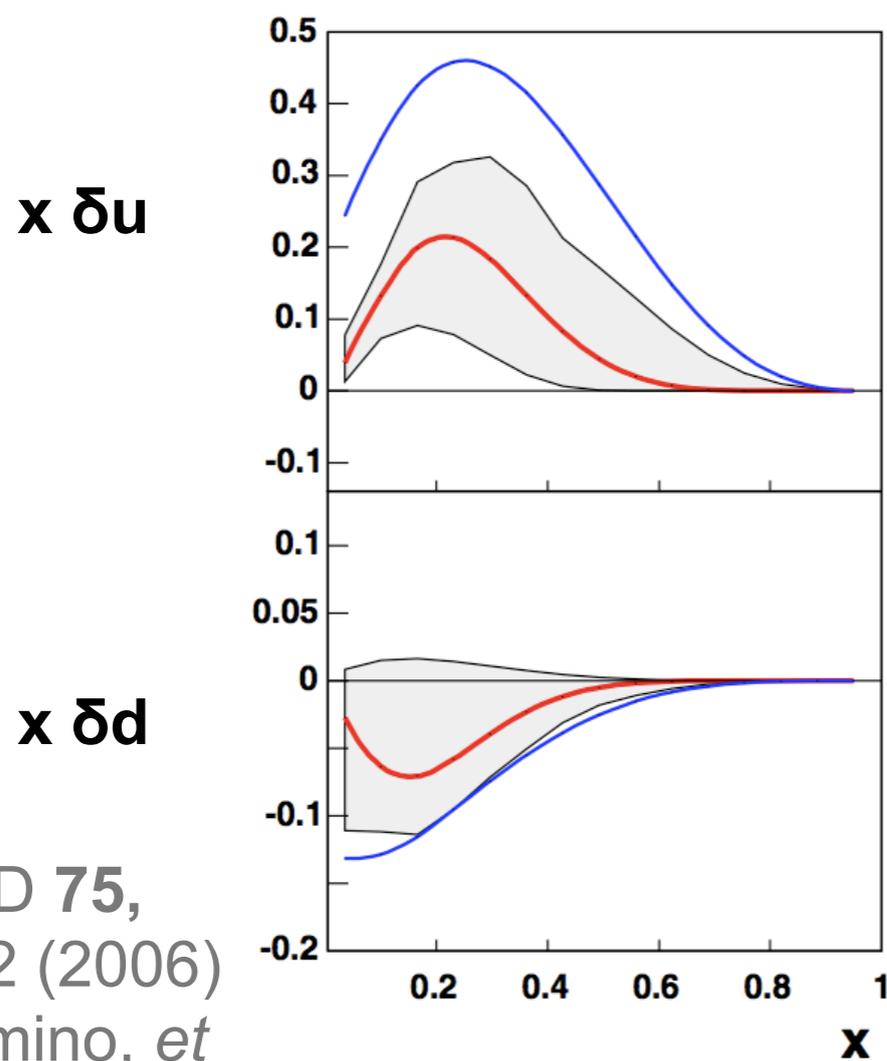
Asymmetries  $\Rightarrow$  Global Analysis  $\Rightarrow$  Parton Distribution Functions (PDFs)

Transverse spin  
(transversity)

- Requires transversely polarized beam(s) and/or target

- Very limited experimental data  
(Mostly contributed by Belle data)

- Chiral-odd effect (i.e. measures correlations between left- and right-handed quarks)



PRD 75,  
054032 (2006)  
Anselmino, *et al.*

# Existing Measurements of Spin Degrees of Freedom

Asymmetries  $\Rightarrow$  Global Analysis  $\Rightarrow$  Parton Distribution Functions (PDFs)

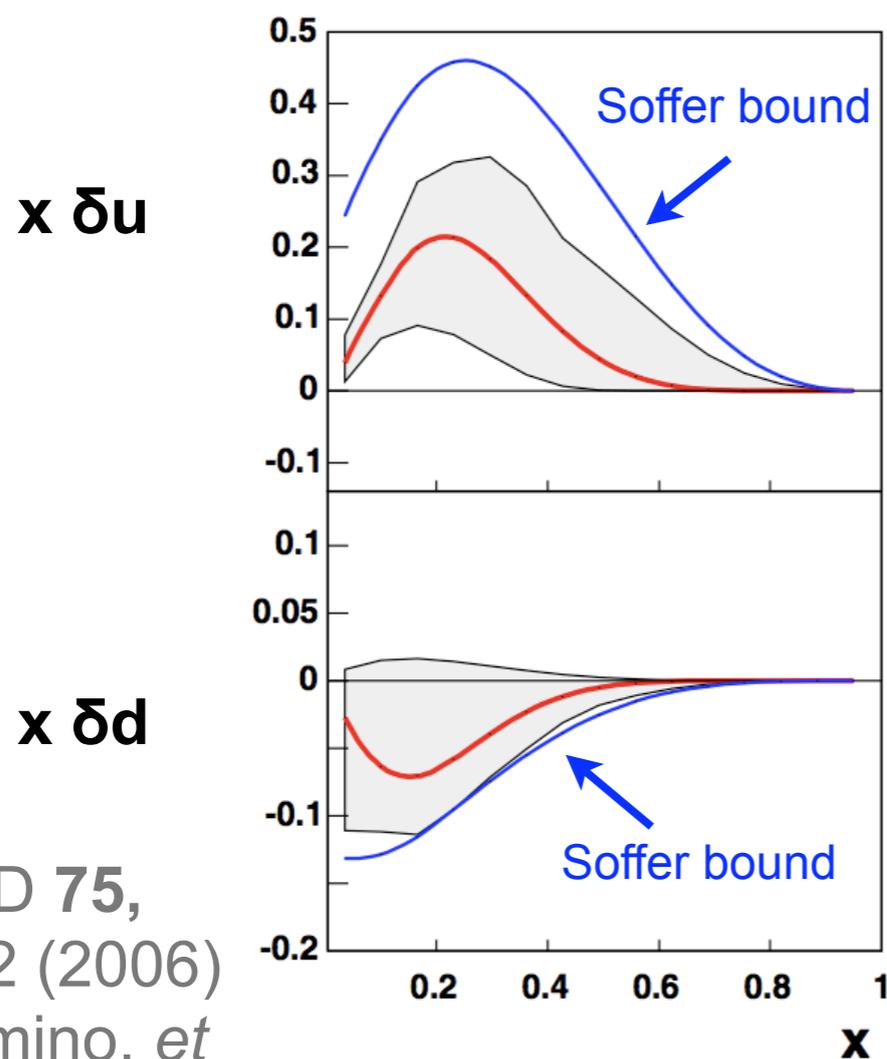
Transverse spin  
(transversity)

- Requires transversely polarized beam(s) and/or target

- Very limited experimental data  
(Mostly contributed by Belle data)

- Chiral-odd effect (i.e. measures correlations between left- and right-handed quarks)

- Constrained by *Soffer bound*:



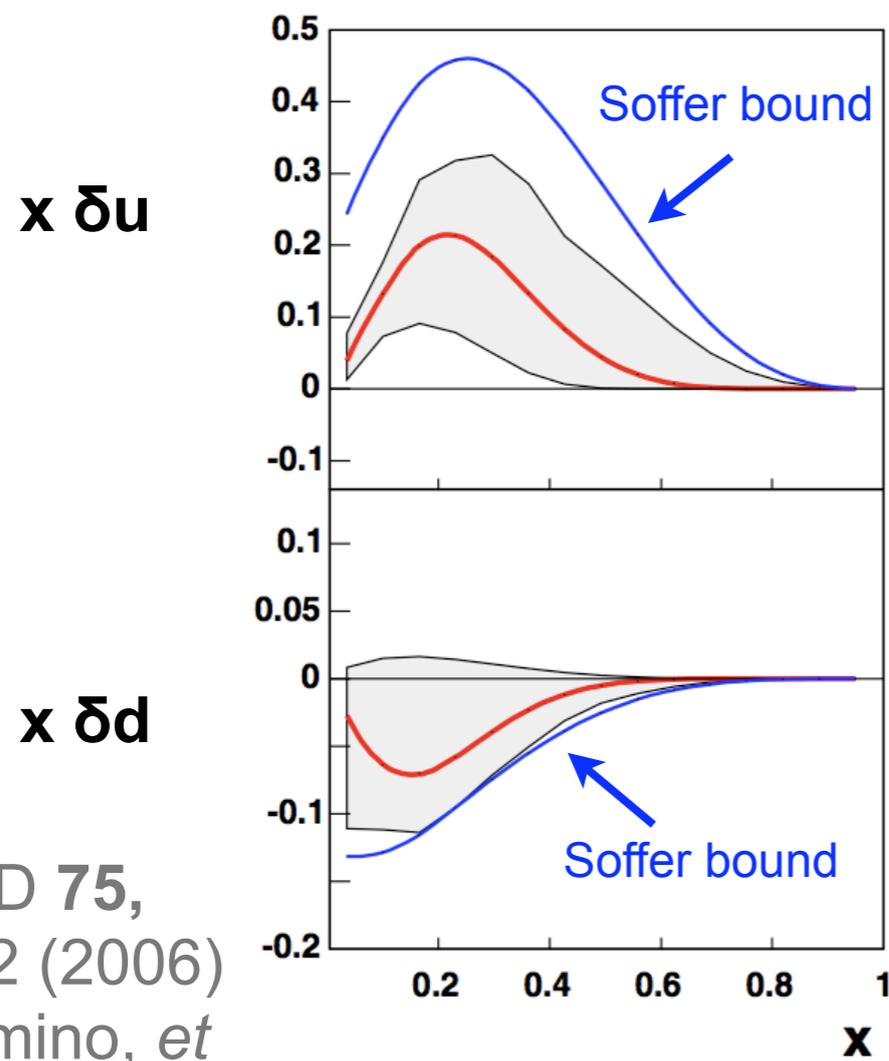
PRD 75,  
054032 (2006)  
Anselmino, *et al.*

# Existing Measurements of Spin Degrees of Freedom

Asymmetries  $\Rightarrow$  Global Analysis  $\Rightarrow$  Parton Distribution Functions (PDFs)

Transverse spin  
(transversity)

- Requires transversely polarized beam(s) and/or target



- Very limited experimental data (Mostly contributed by Belle data)

- Chiral-odd effect (i.e. measures correlations between left- and right-handed quarks)

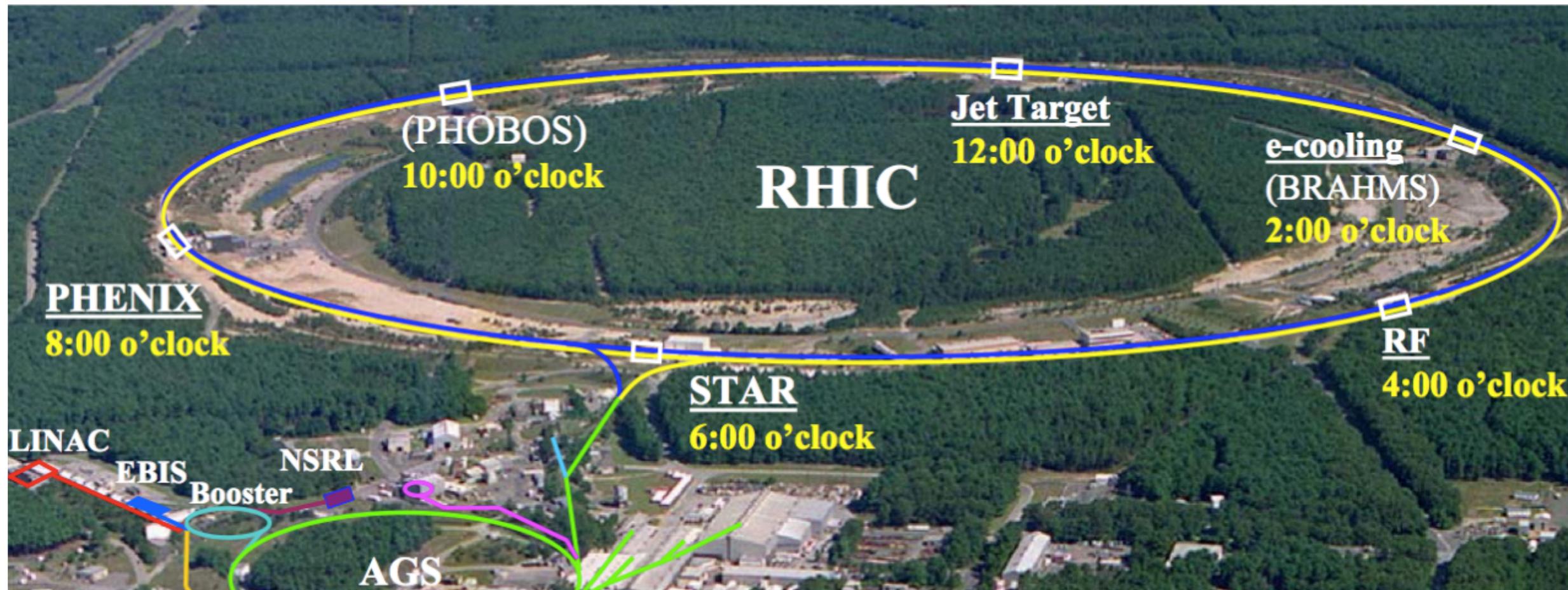
- Constrained by *Soffer bound*:

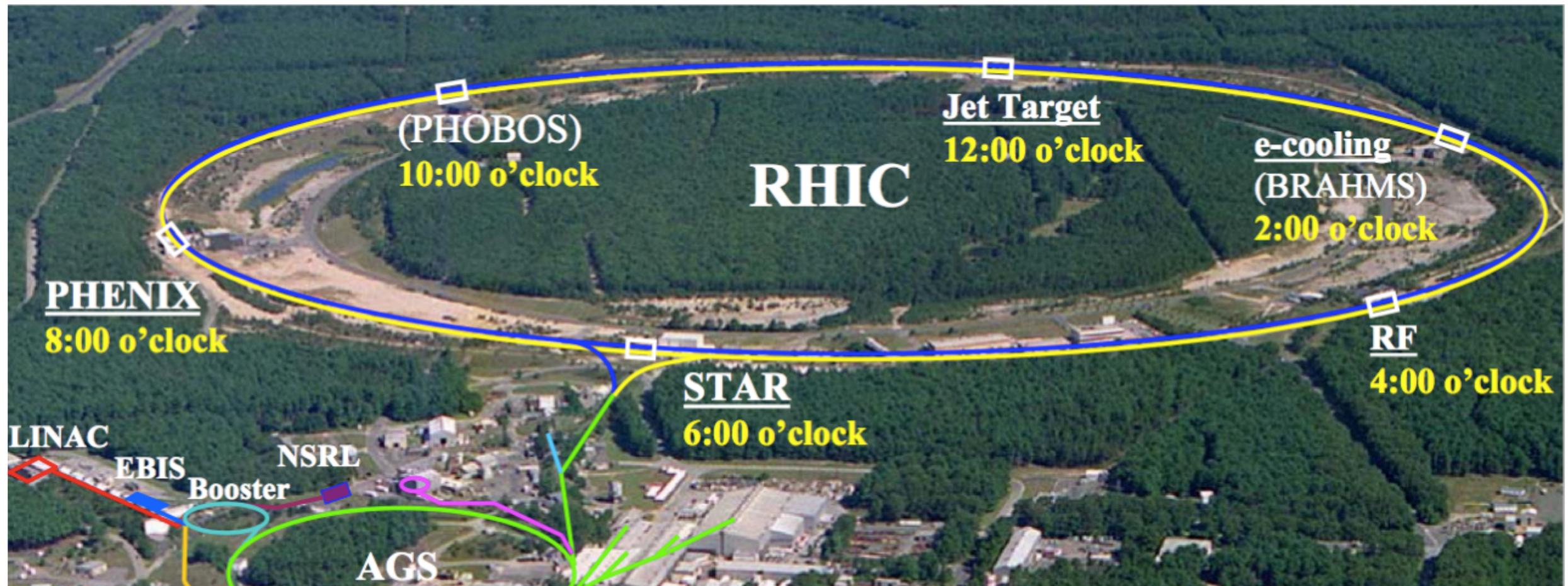
$$|\delta q(x, Q^2)| \leq \frac{1}{2}[q(x, Q^2) + \Delta q(x, Q^2)]$$

PRD 75,  
054032 (2006)  
Anselmino, *et al.*

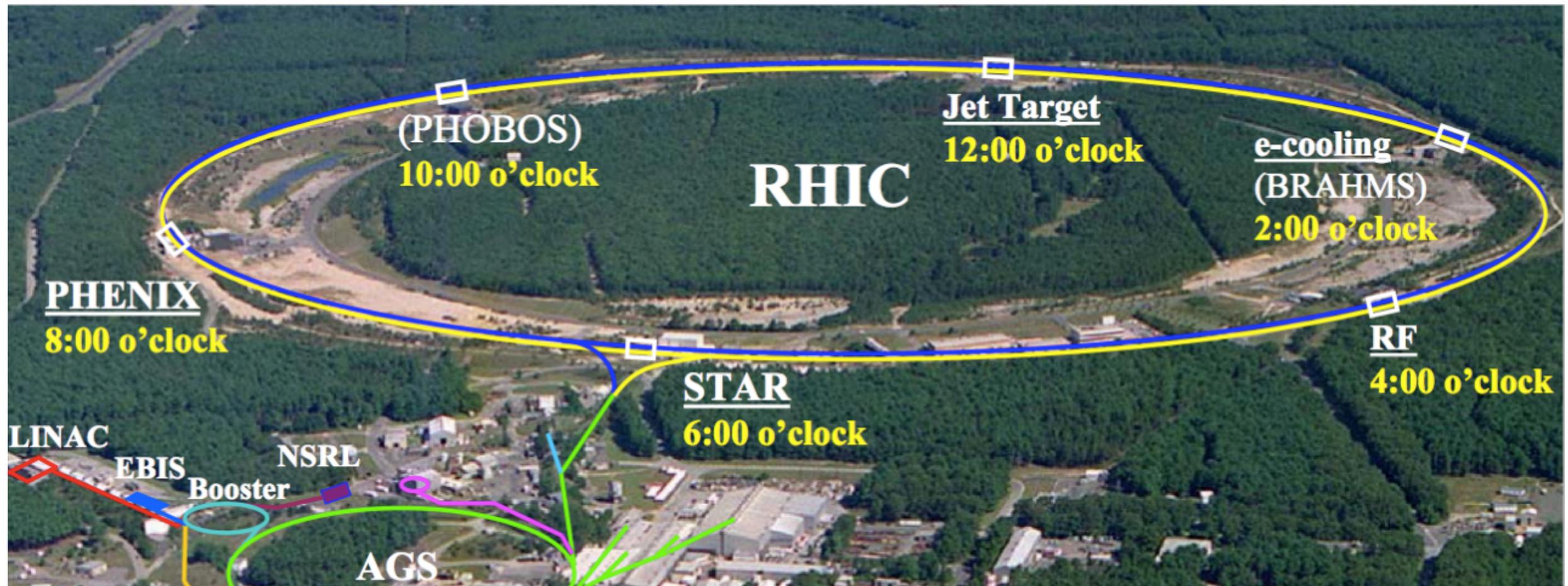
# Goals of this Presentation:

- Conduct a relevant overview of the experimental apparatus (STAR) and Jet Reconstruction



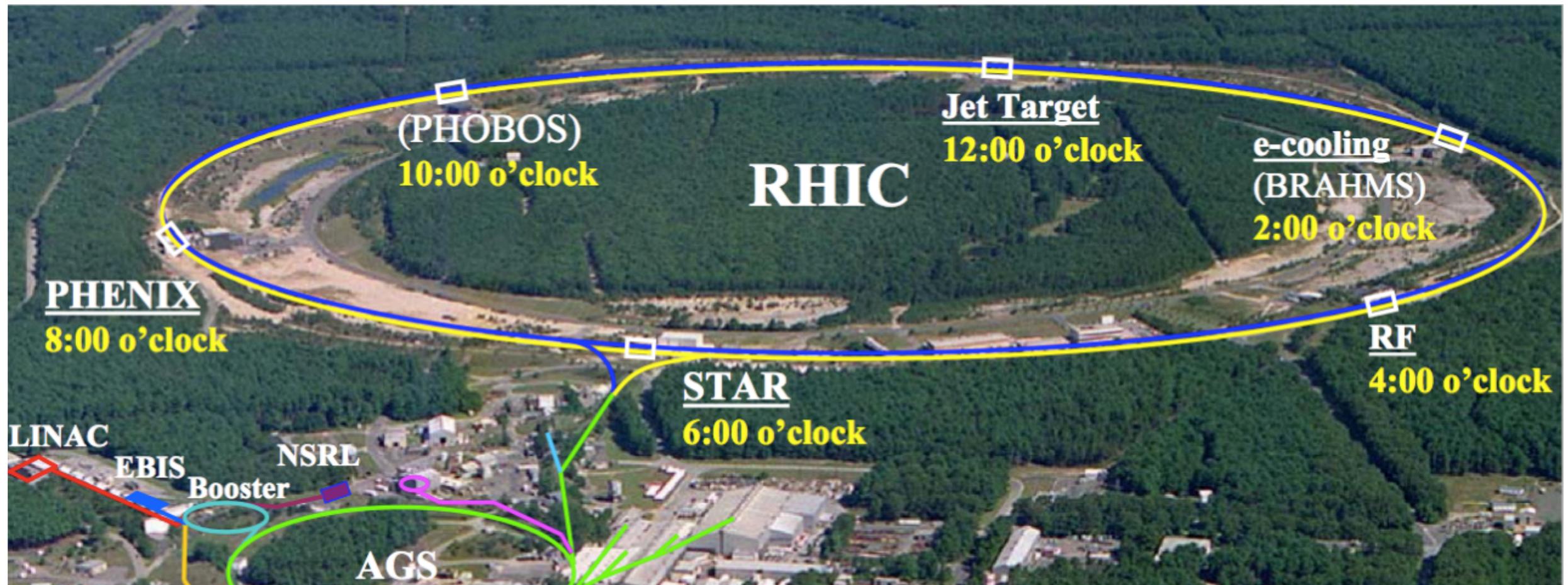


Proton-proton collisions at  $\sqrt{s} = 200$  GeV



Proton-proton collisions at  $\sqrt{s} = 200 \text{ GeV}$

Beam polarizations as high as  $\sim 60\%$



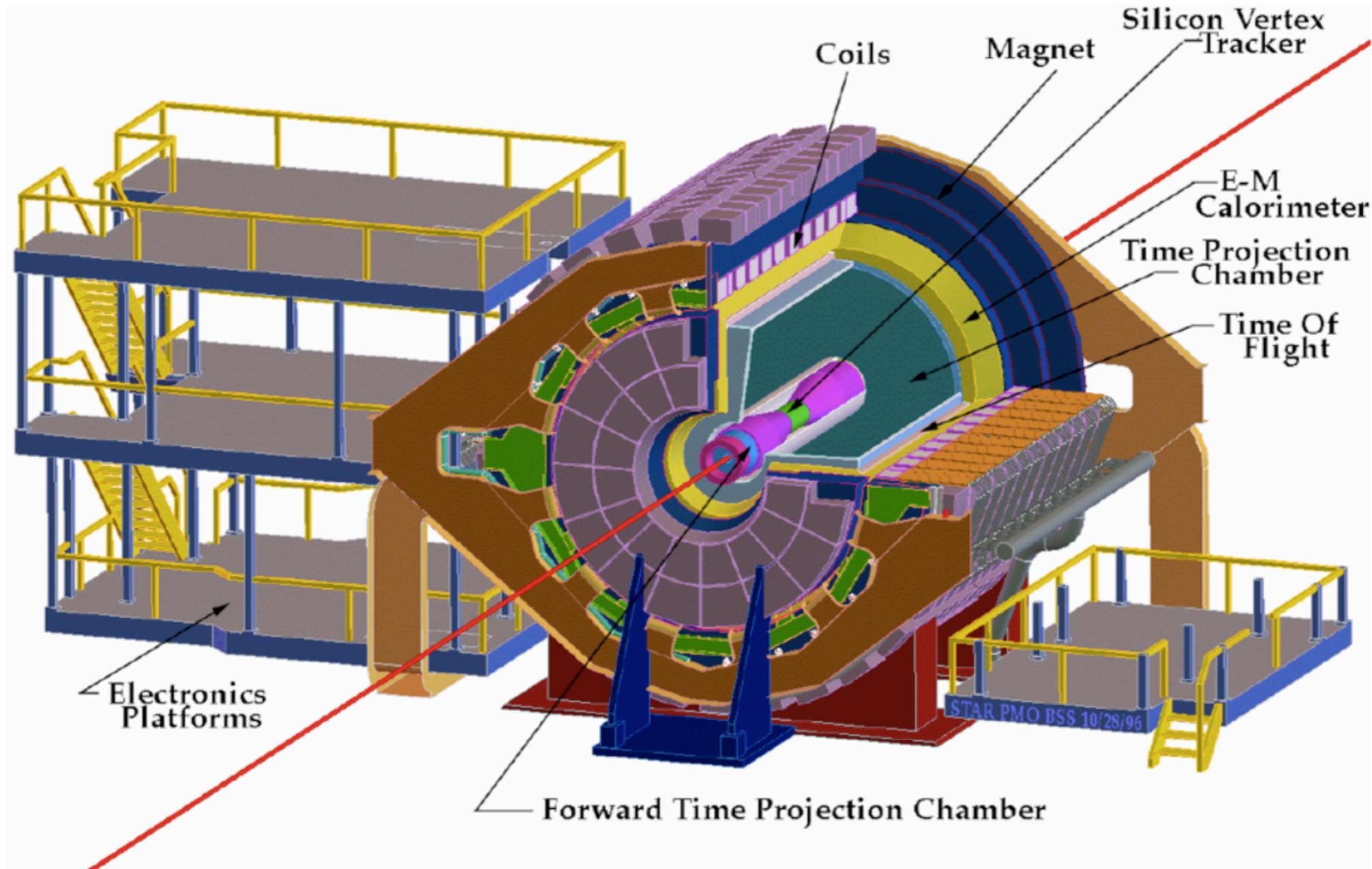
Proton-proton collisions at  $\sqrt{s} = 200 \text{ GeV}$

Beam polarizations as high as  $\sim 60\%$

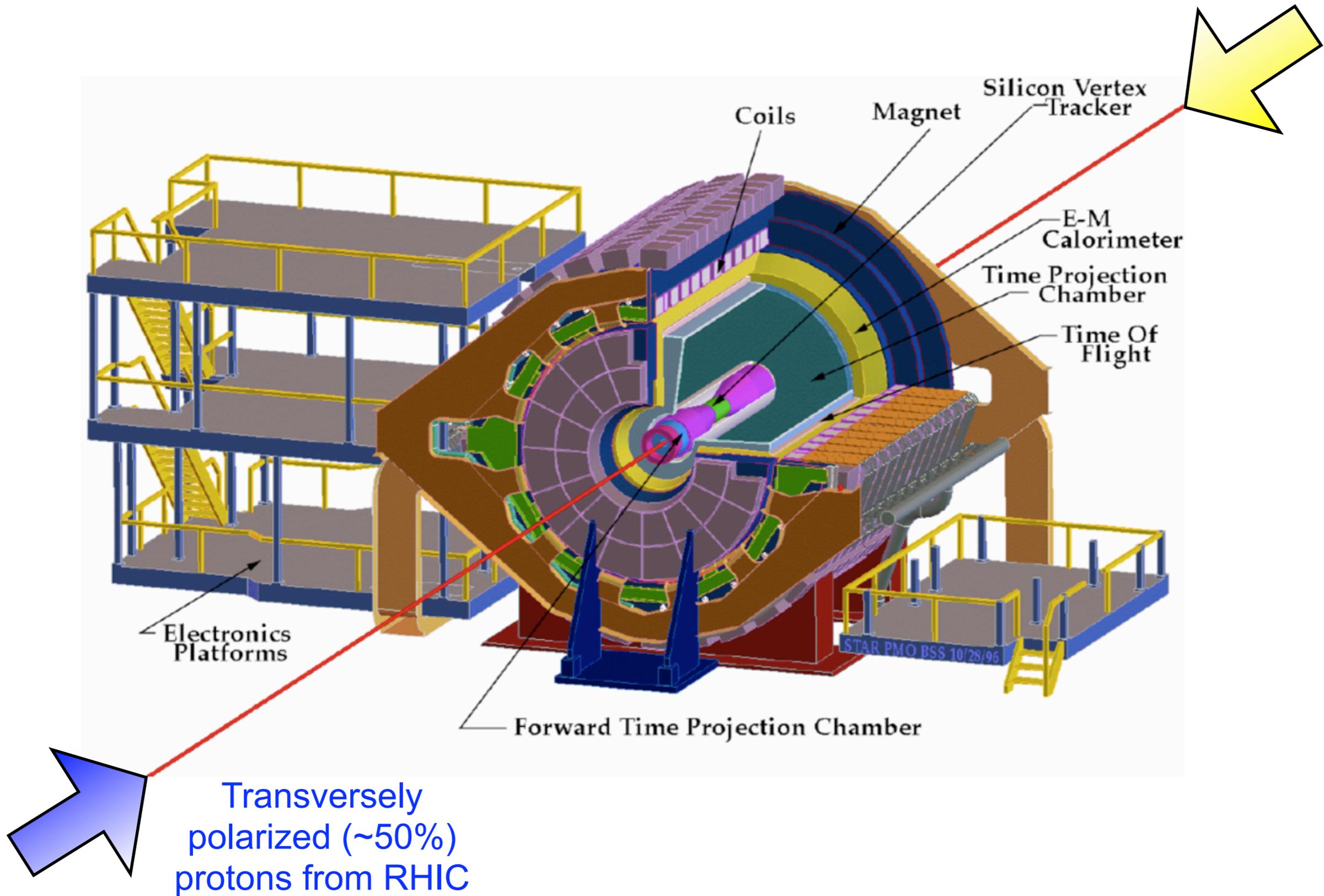
Beam luminosity  $\sim 10^{32} \text{ s}^{-1} \text{ cm}^{-2}$  (1  $\text{pb}^{-1}$  integrated luminosity)

# Experimental Apparatus (S.T.A.R.)

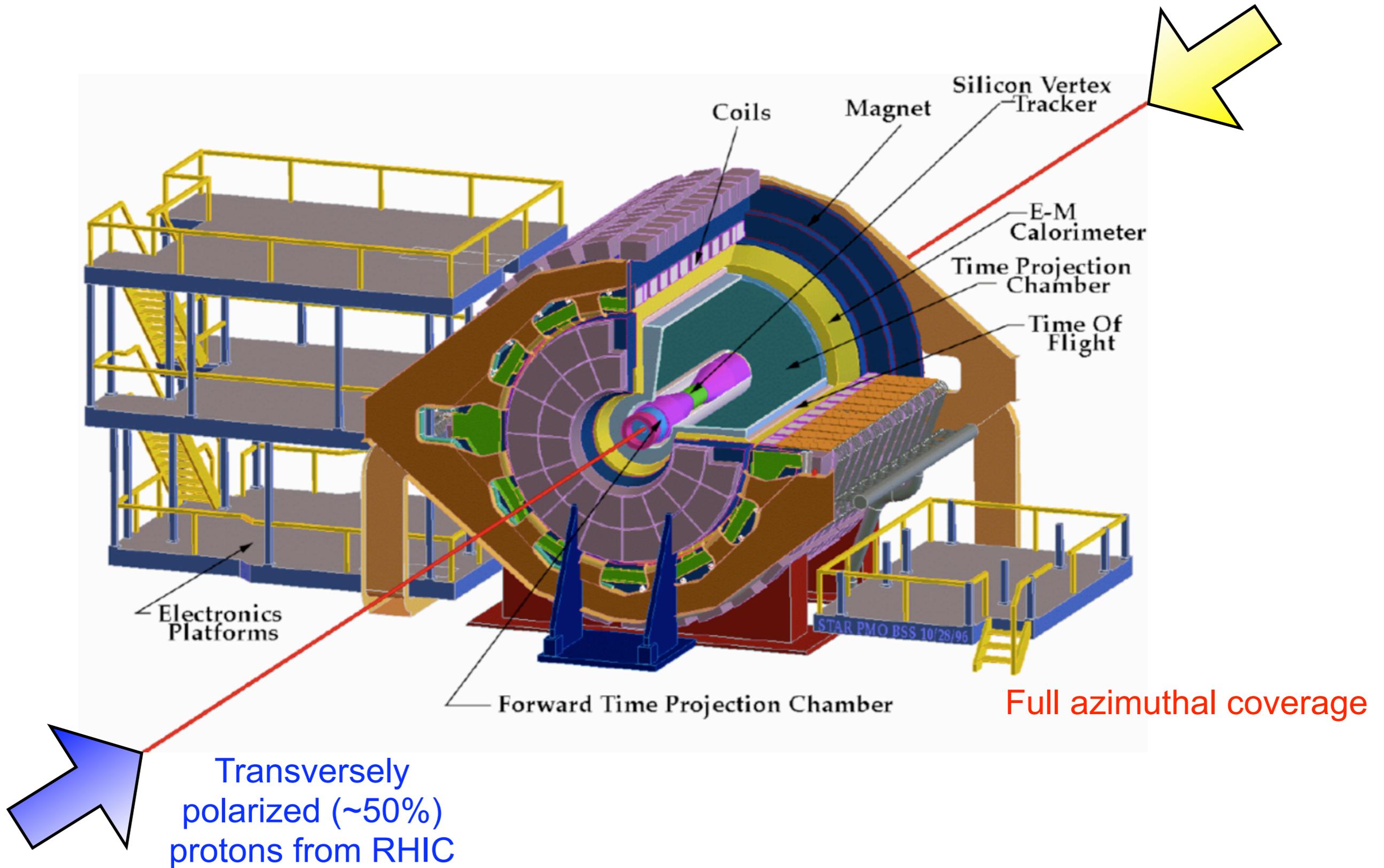
# Experimental Apparatus (S.T.A.R.)



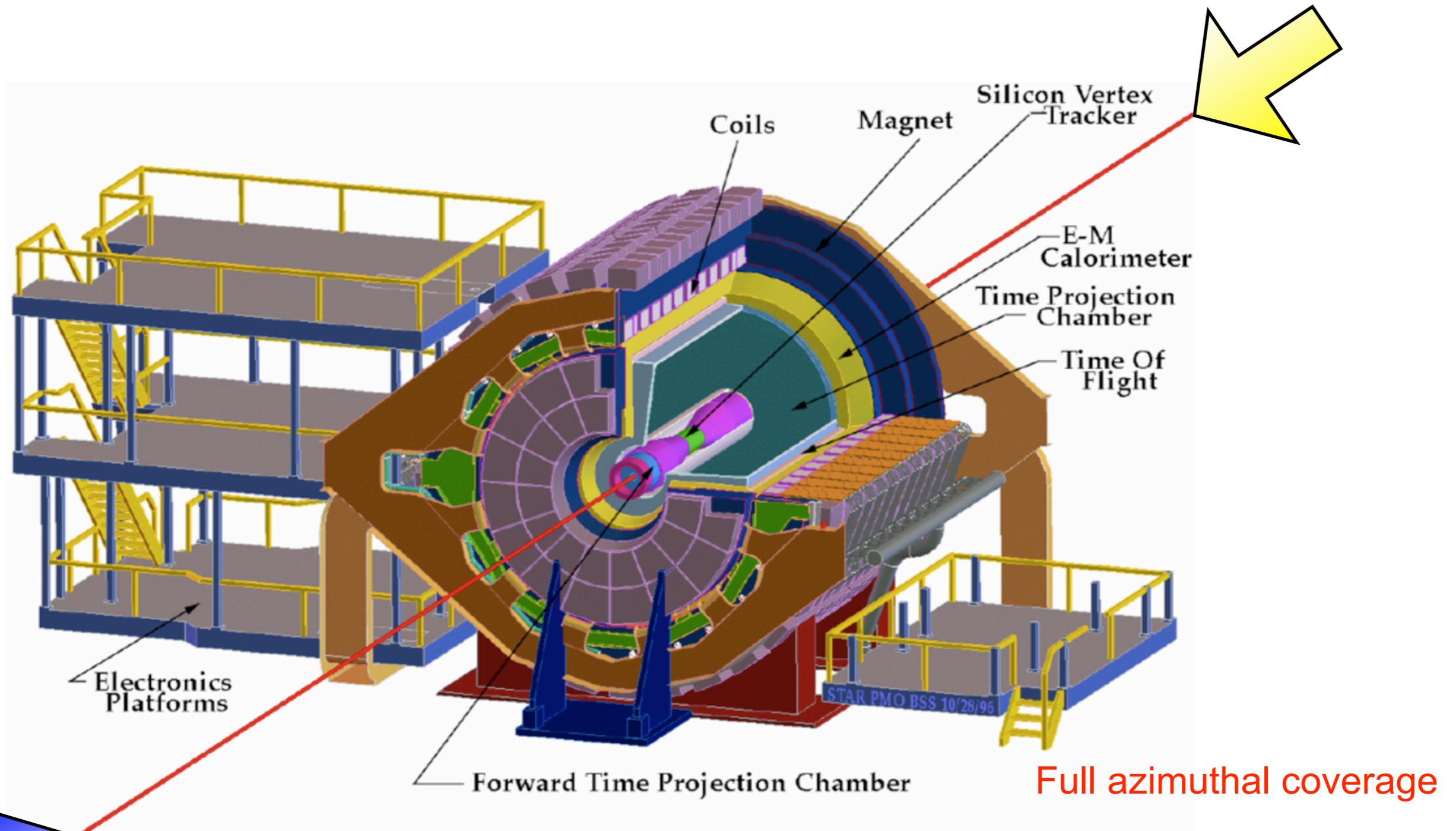
# Experimental Apparatus (S.T.A.R.)



# Experimental Apparatus (S.T.A.R.)



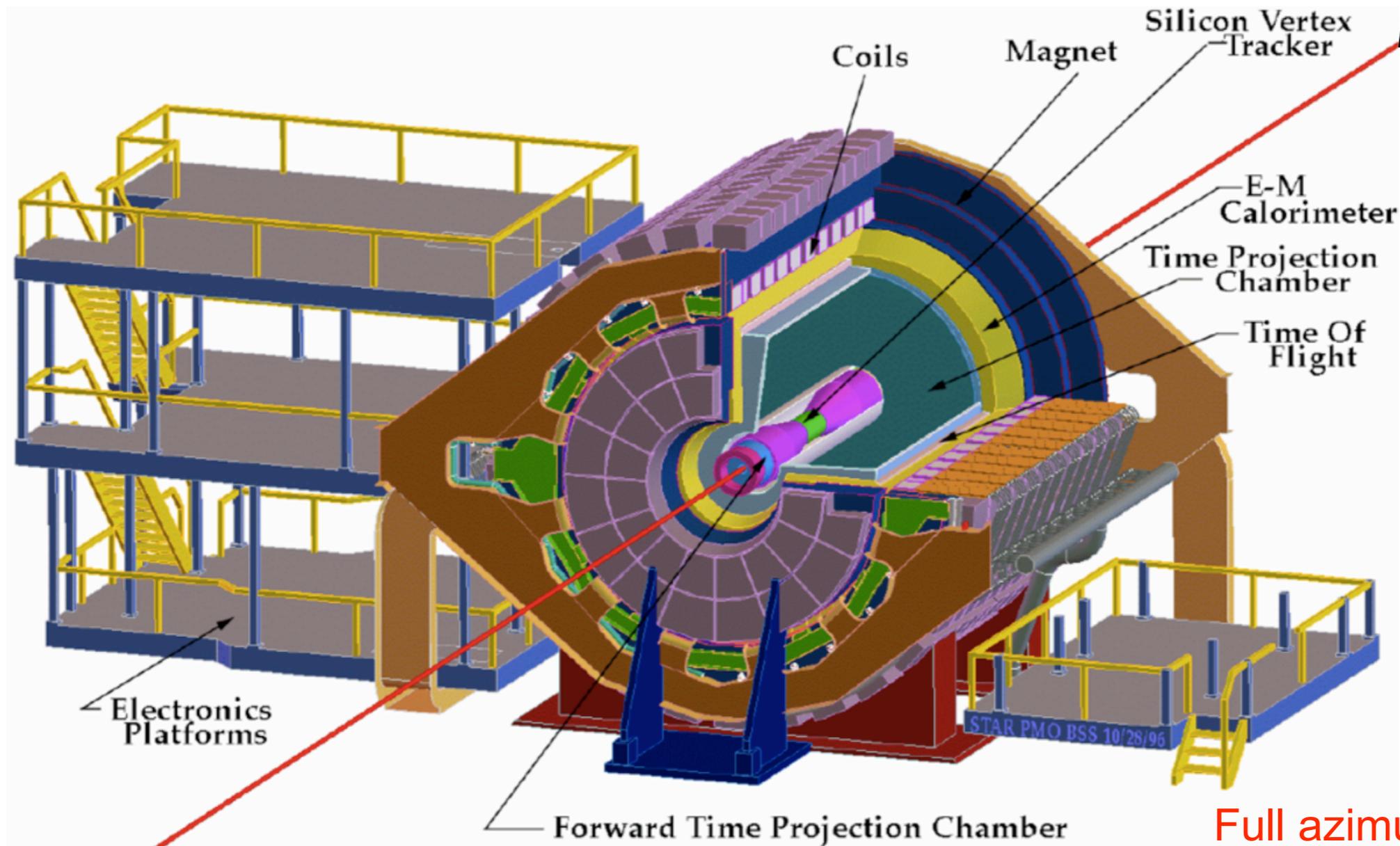
# Experimental Apparatus (S.T.A.R.)



Transversely polarized (~50%) protons from RHIC

Data analyzed at mid-rapidity ( $-1 < \eta < 1$ )

# Experimental Apparatus (S.T.A.R.)

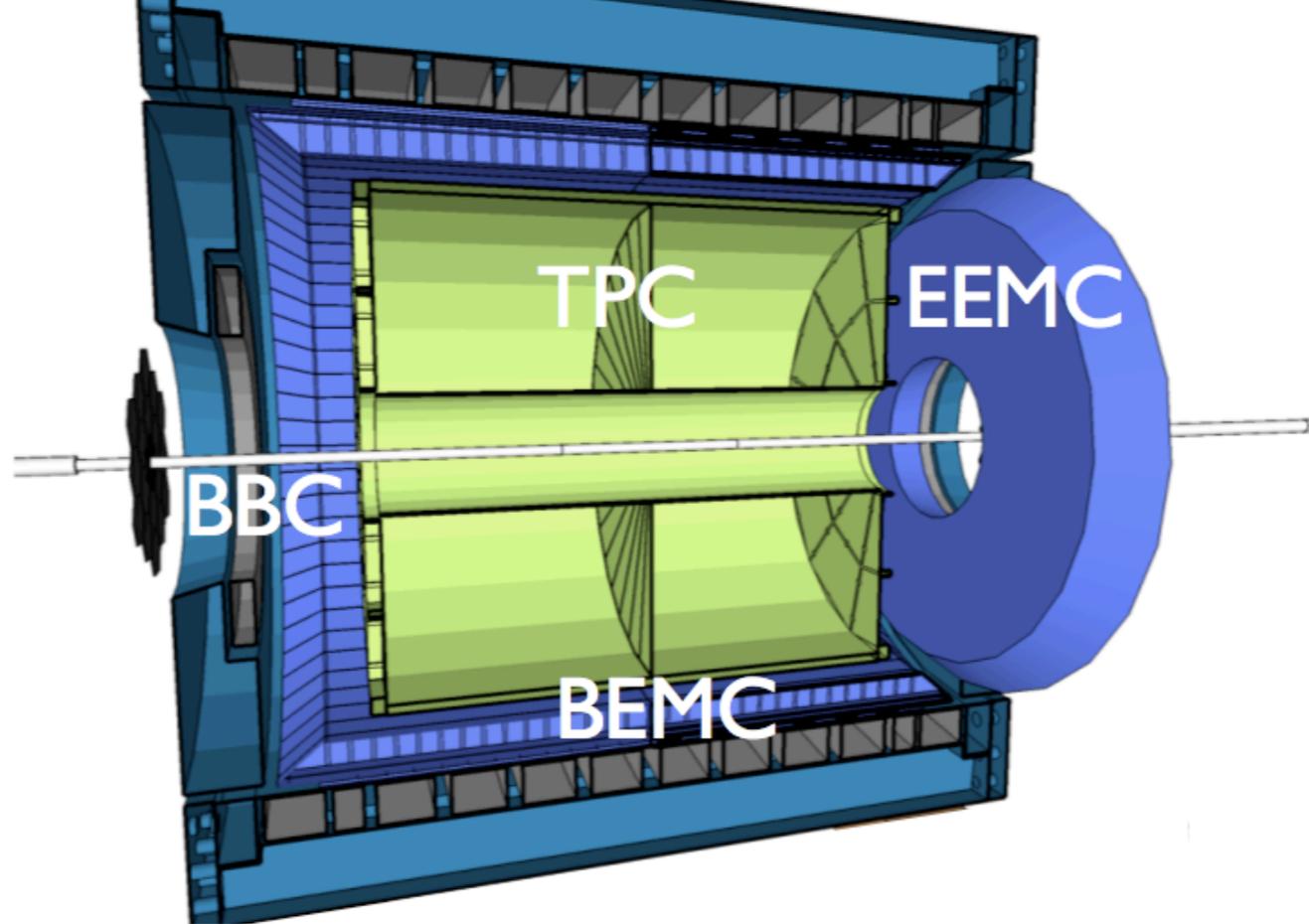


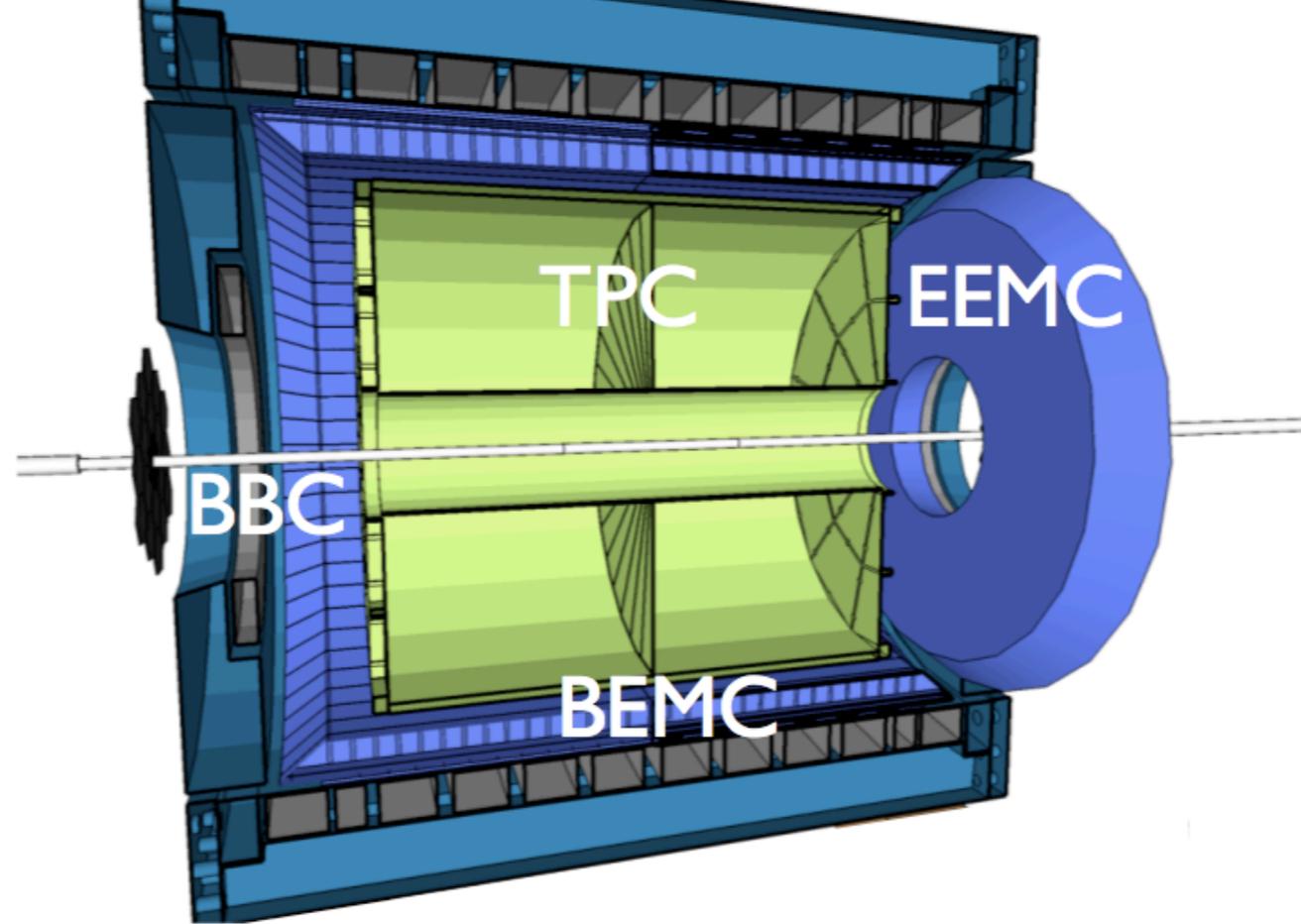
Transversely polarized (~50%) protons from RHIC

Full azimuthal coverage

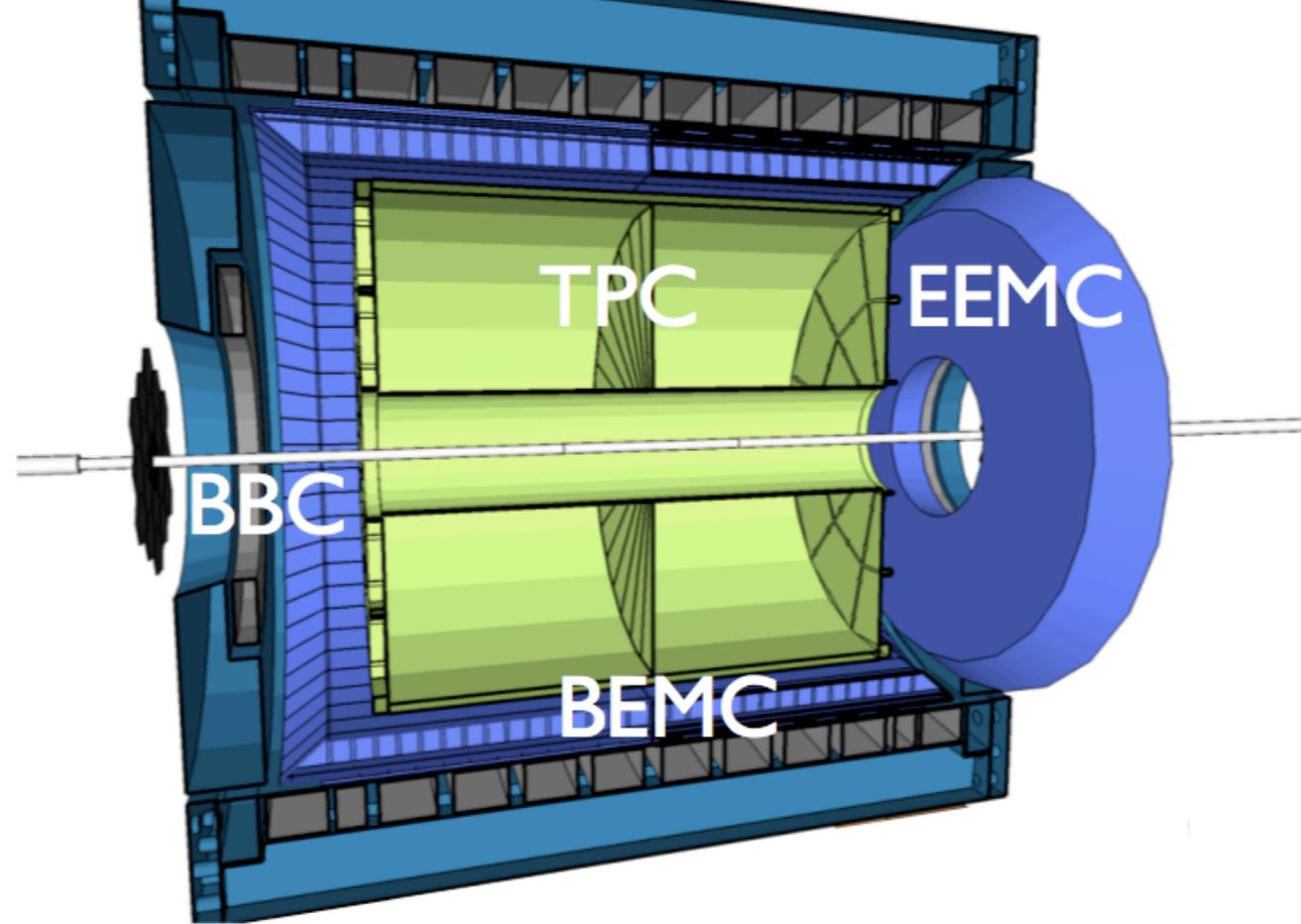
Data analyzed at mid-rapidity ( $-1 < \eta < 1$ )

Reconstruction of jets and component charged particle trajectories reconstructed



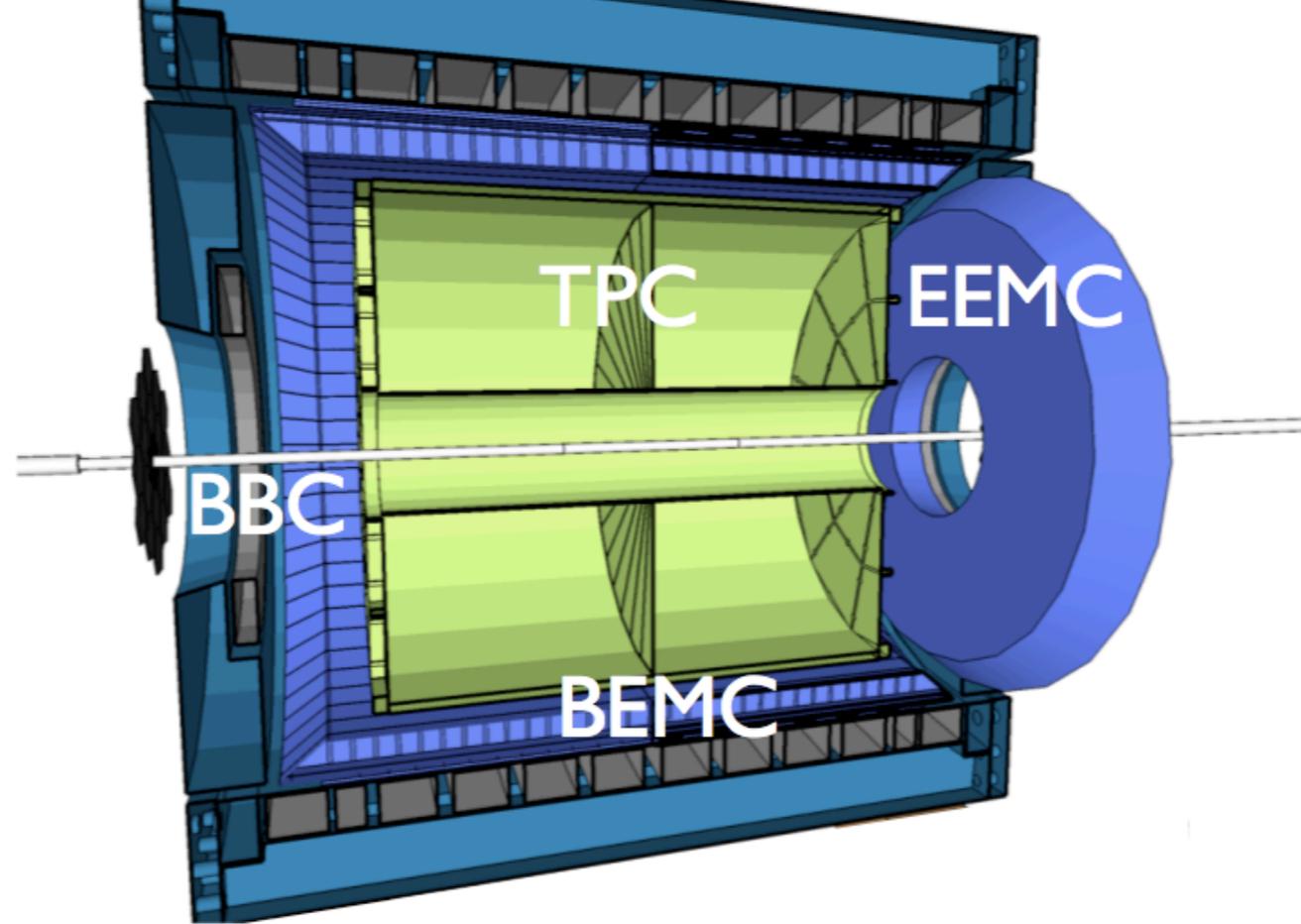


BBC: relative polarization luminosities;  
minimum bias trigger



BBC: relative polarization luminosities;  
minimum bias trigger

TPC: charged particle tracking;  
 $dE/dx$  PID ( $p < 15$  GeV)



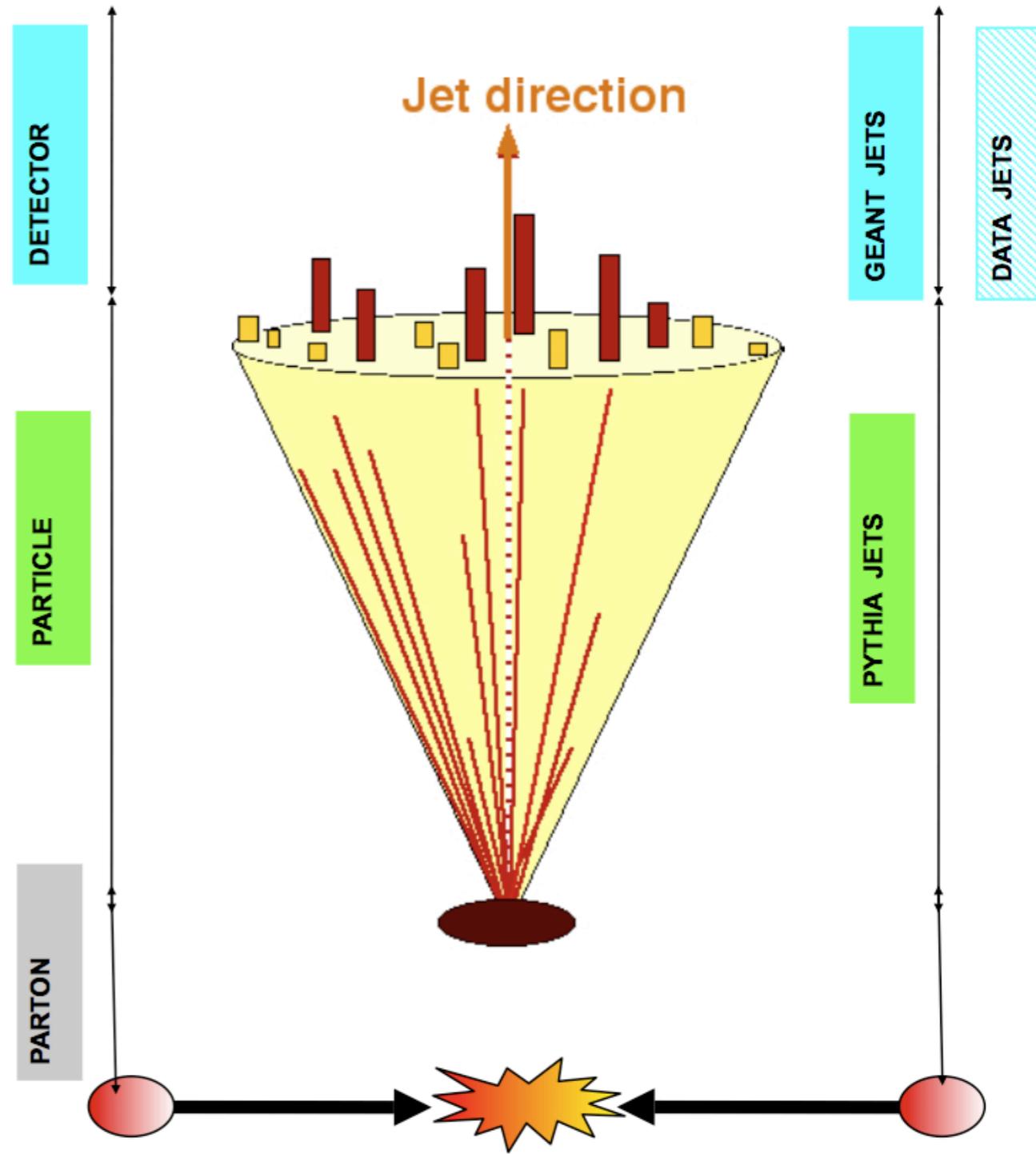
BBC: relative polarization luminosities;  
minimum bias trigger

TPC: charged particle tracking;  
 $dE/dx$  PID ( $p < 15$  GeV)

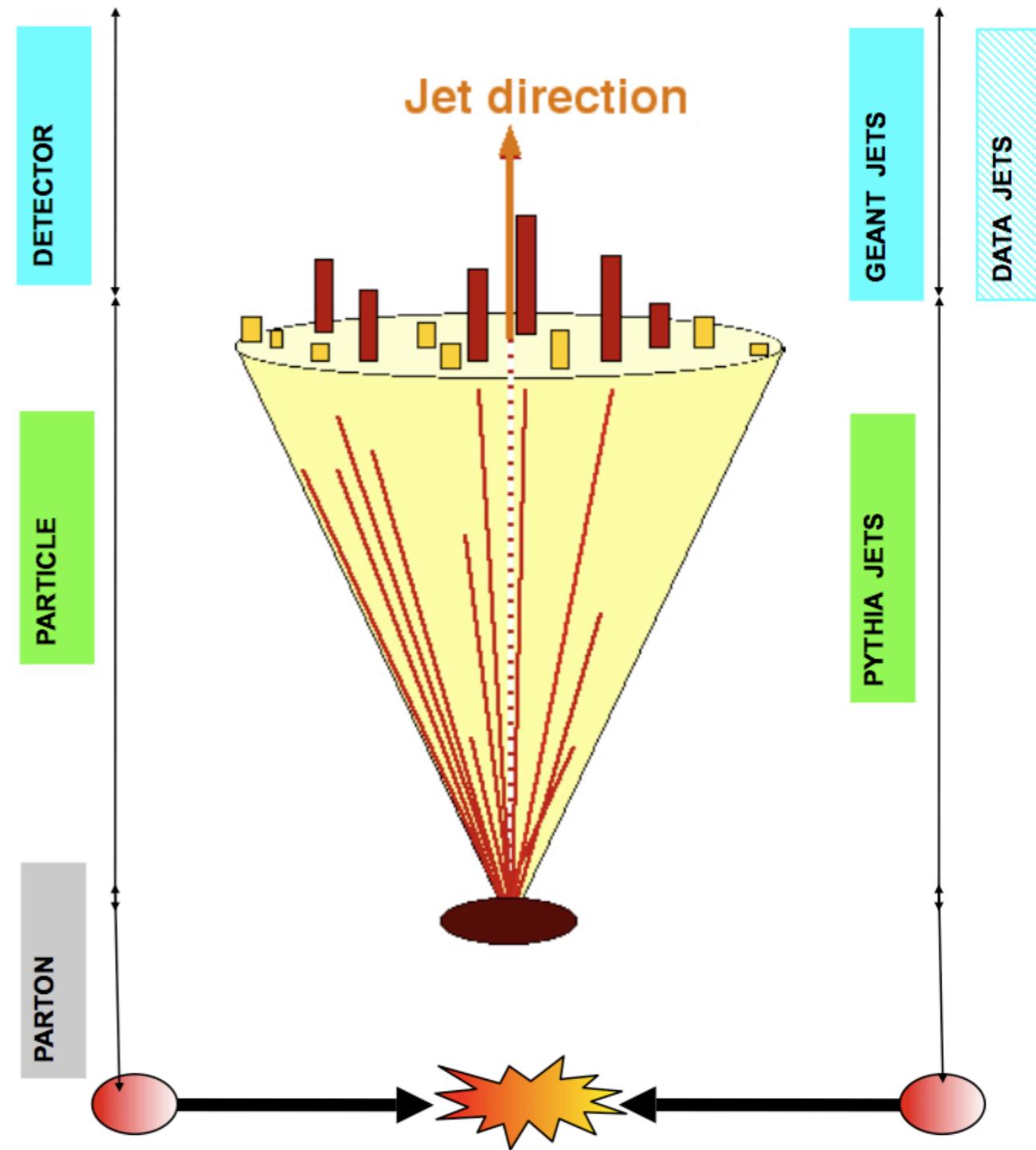
BEMC, EEMC: barrel/endcap calorimeters  
for triggering, jet reconstruction

# Jet Reconstruction

# Jet Reconstruction



# Jet Reconstruction

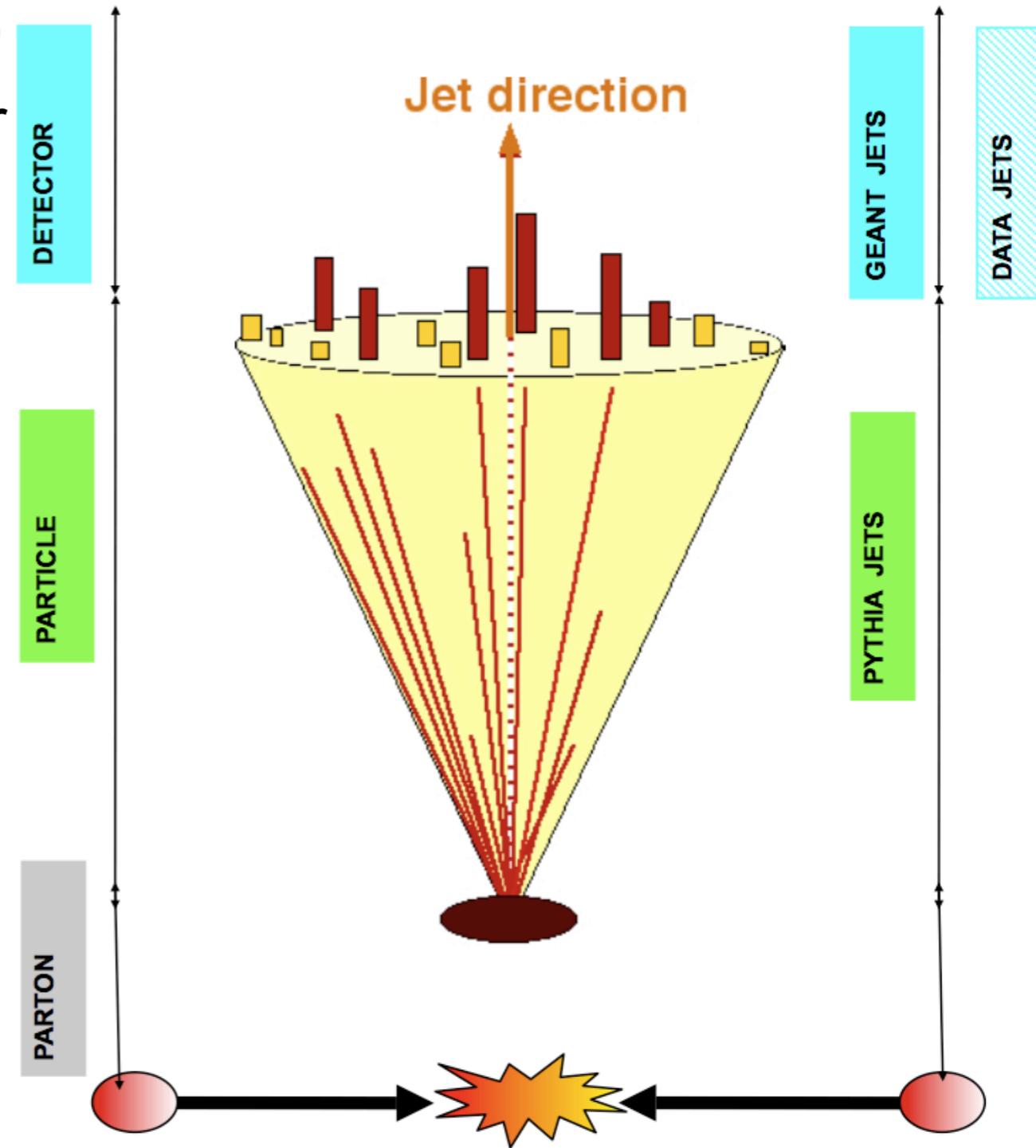


Midpoint Cone Algorithm

([hep-ex/0005012](https://arxiv.org/abs/hep-ex/0005012))

# Jet Reconstruction

- 1) TPC track or EMC tower used as “seed”
- 2) hits inside fixed radius determine cluster energy
- 3) neighboring clusters calculated & merged if energy overlap  $> 50\%$

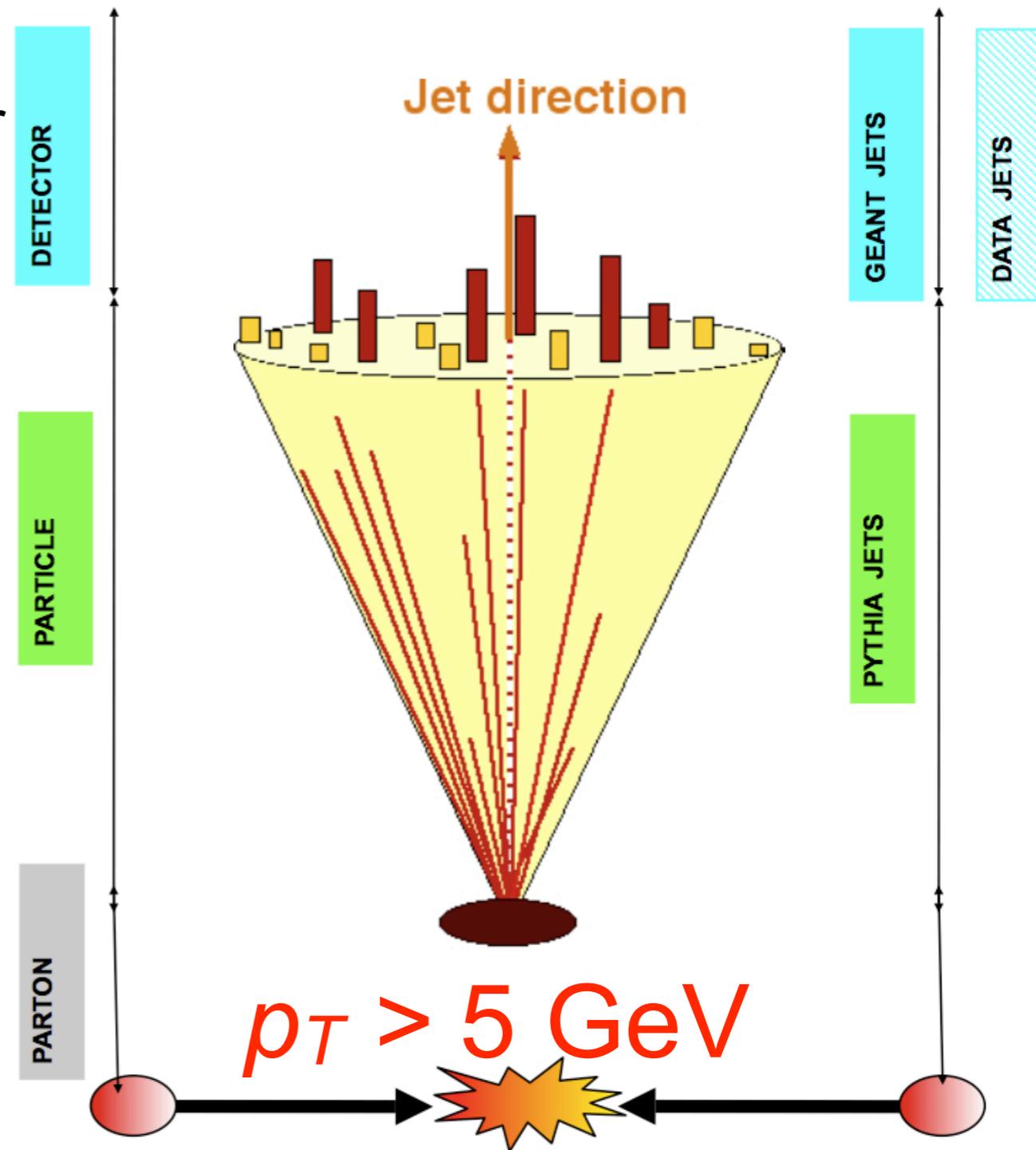


## Midpoint Cone Algorithm

(hep-ex/0005012)

# Jet Reconstruction

- 1) TPC track or EMC tower used as “seed”
- 2) hits inside fixed radius determine cluster energy
- 3) neighboring clusters calculated & merged if energy overlap  $> 50\%$

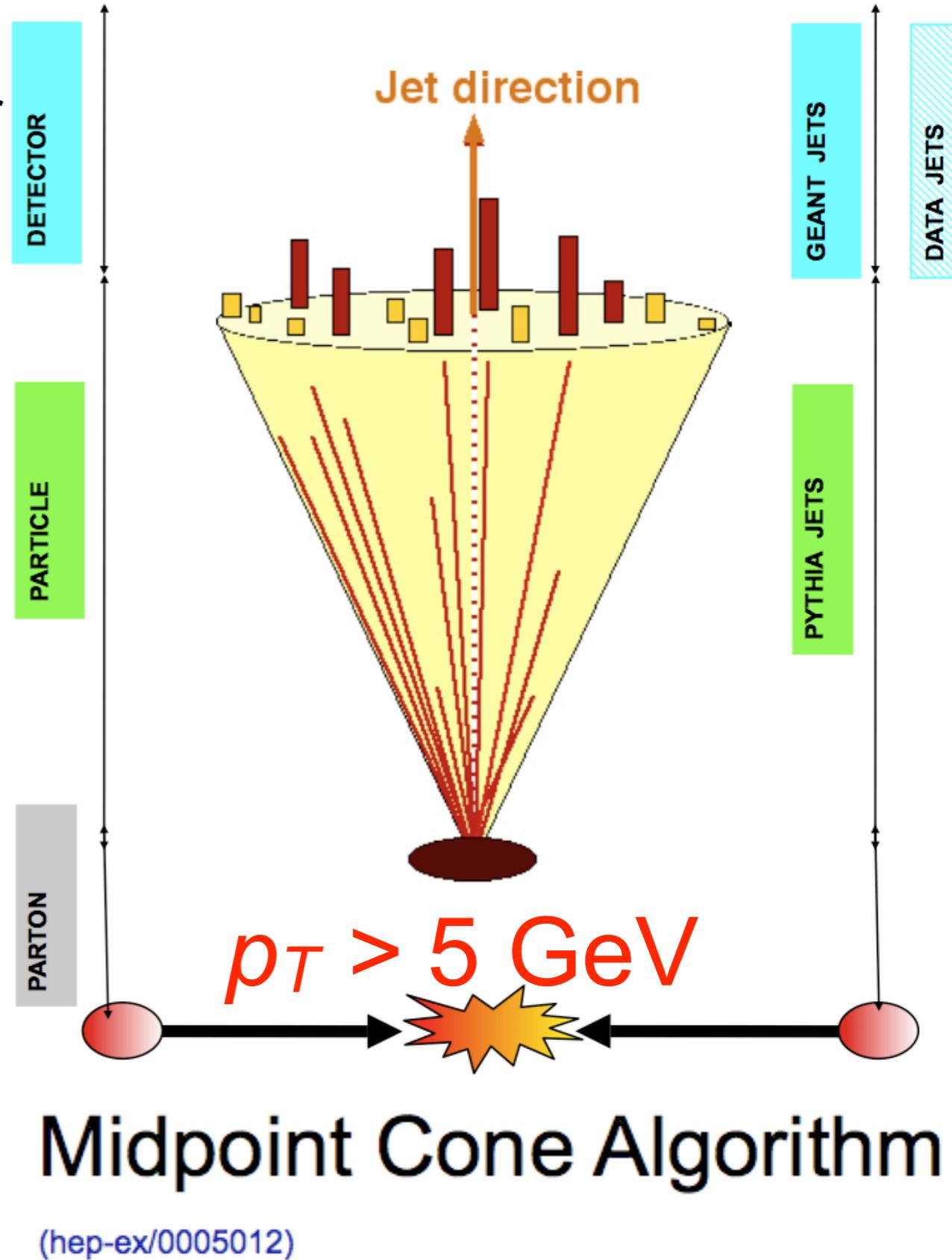
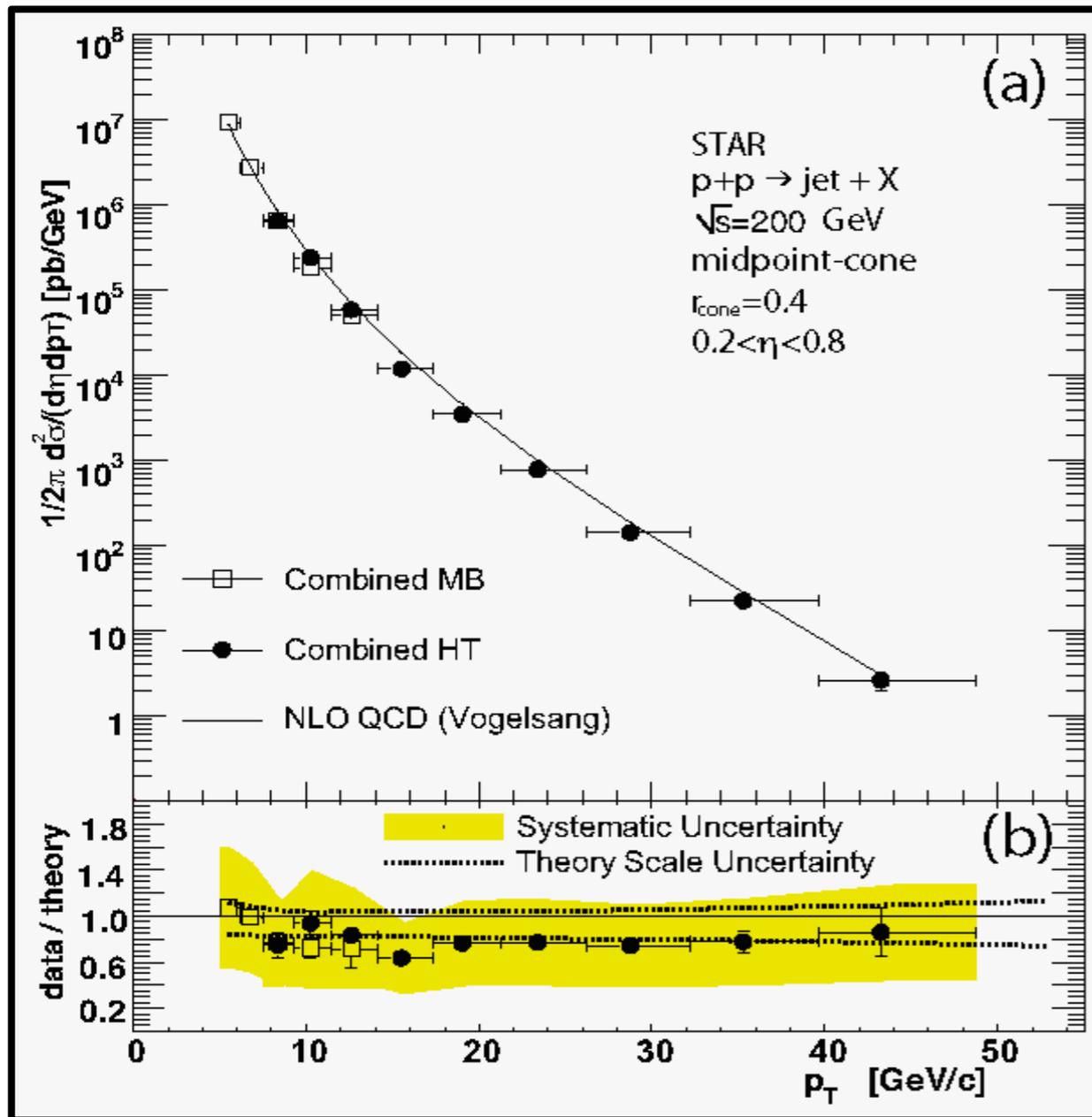


Midpoint Cone Algorithm

(hep-ex/0005012)

# Jet Reconstruction

- 1) TPC track or EMC tower used as “seed”
- 2) hits inside fixed radius determine cluster energy
- 3) neighboring clusters calculated & merged if energy overlap  $> 50\%$



# Goals of this Presentation:

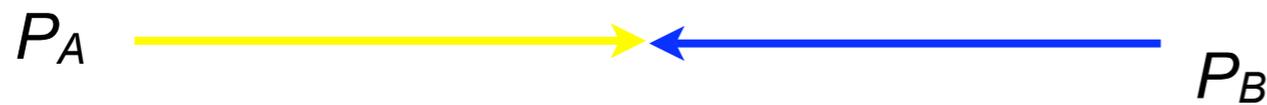
- Relate  $\delta q$  to the experimentally measurable Collins asymmetry

# Experimental access to $\delta q$

# Experimental access to $\delta q$

proton-proton scattering:

$$p(P_A, S_{\perp}) + p(P_B) \rightarrow jet(P_J) + X \rightarrow \pi^{\pm} + X$$

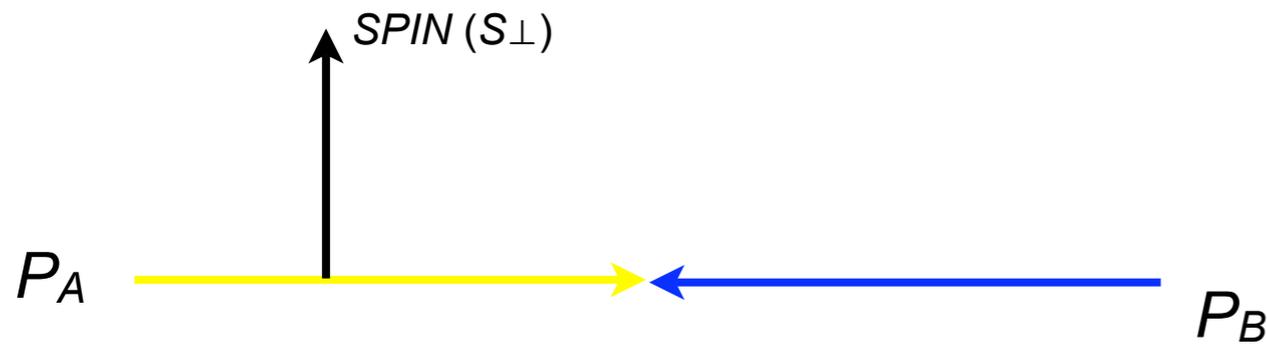


# Experimental access to $\delta q$

proton-proton scattering:

$$p(P_A, S_{\perp}) + p(P_B) \rightarrow jet(P_J) + X \rightarrow \pi^{\pm} + X$$

↑  
one proton polarized



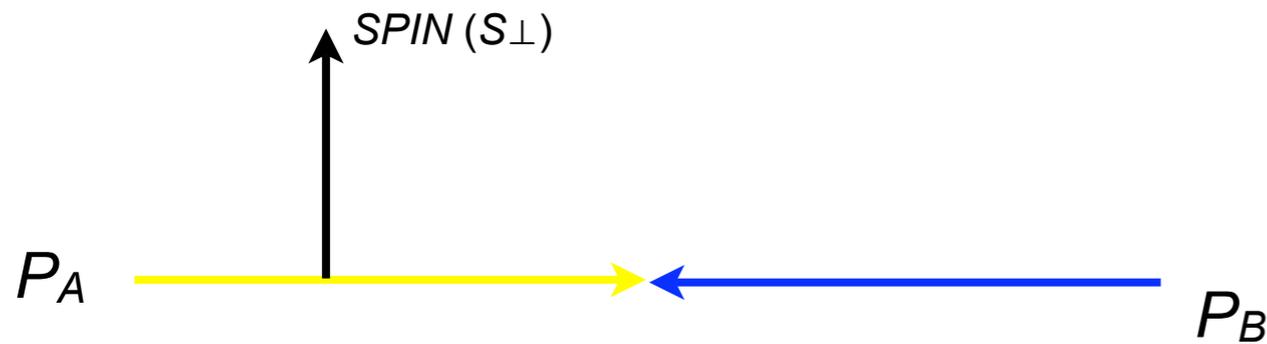
# Experimental access to $\delta q$

proton-proton scattering:

$$p(P_A, S_{\perp}) + p(P_B) \rightarrow \text{jet}(P_J) + X \rightarrow \pi^{\pm} + X$$

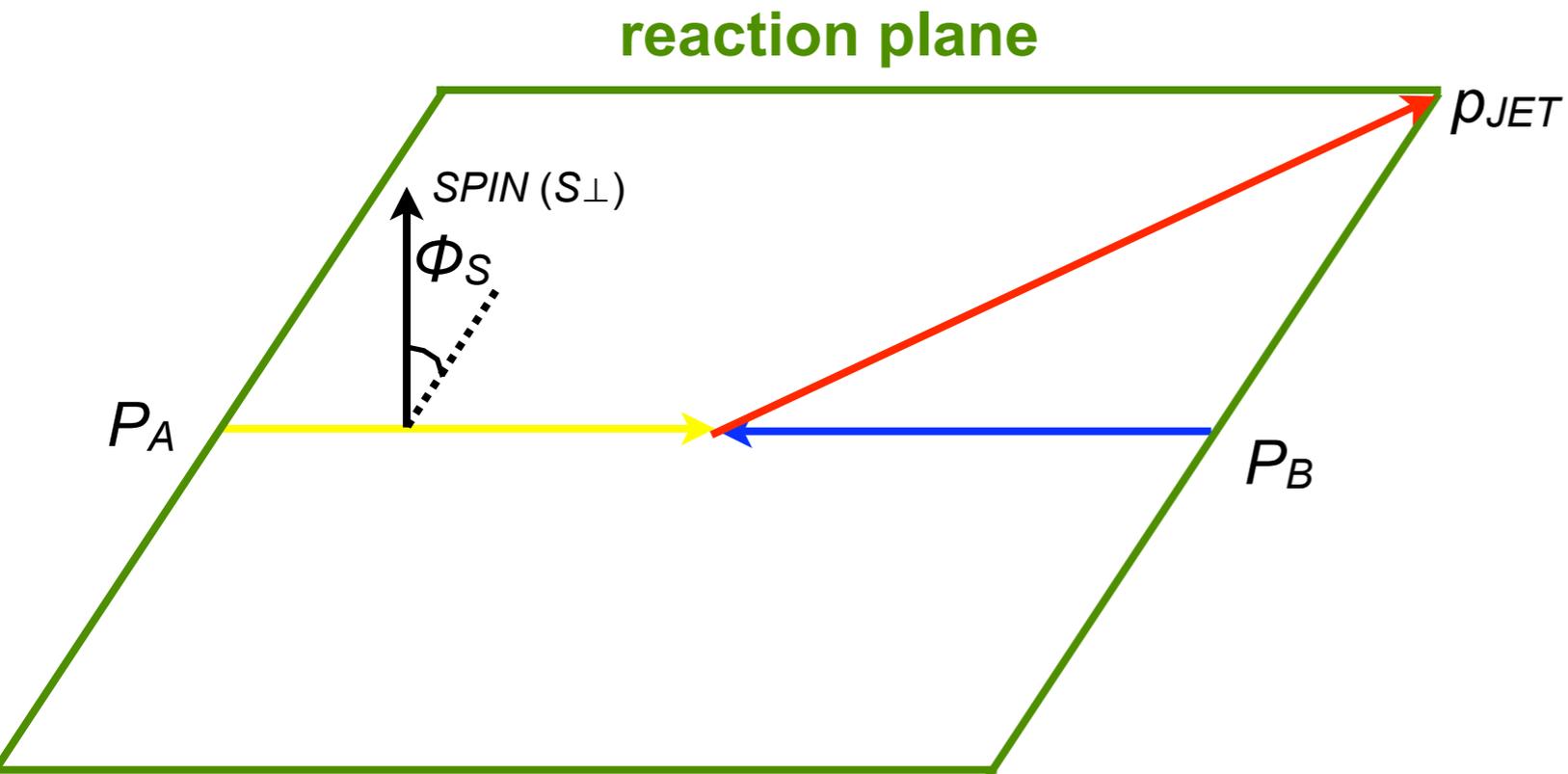
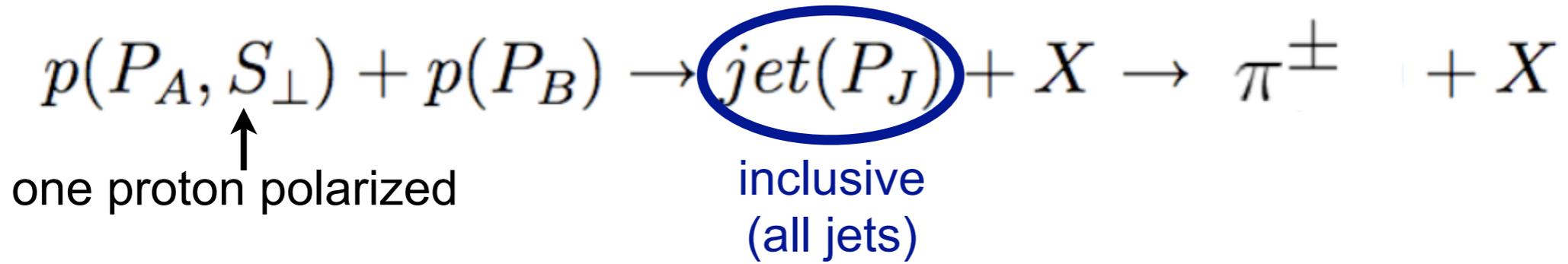
one proton polarized

inclusive  
(all jets)



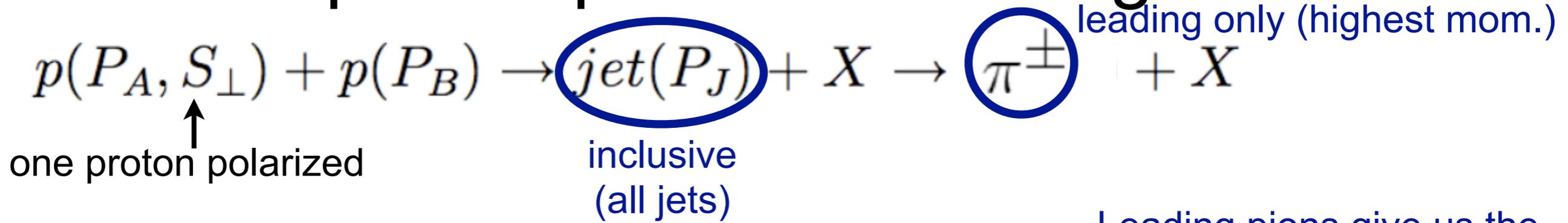
# Experimental access to $\delta q$

proton-proton scattering:

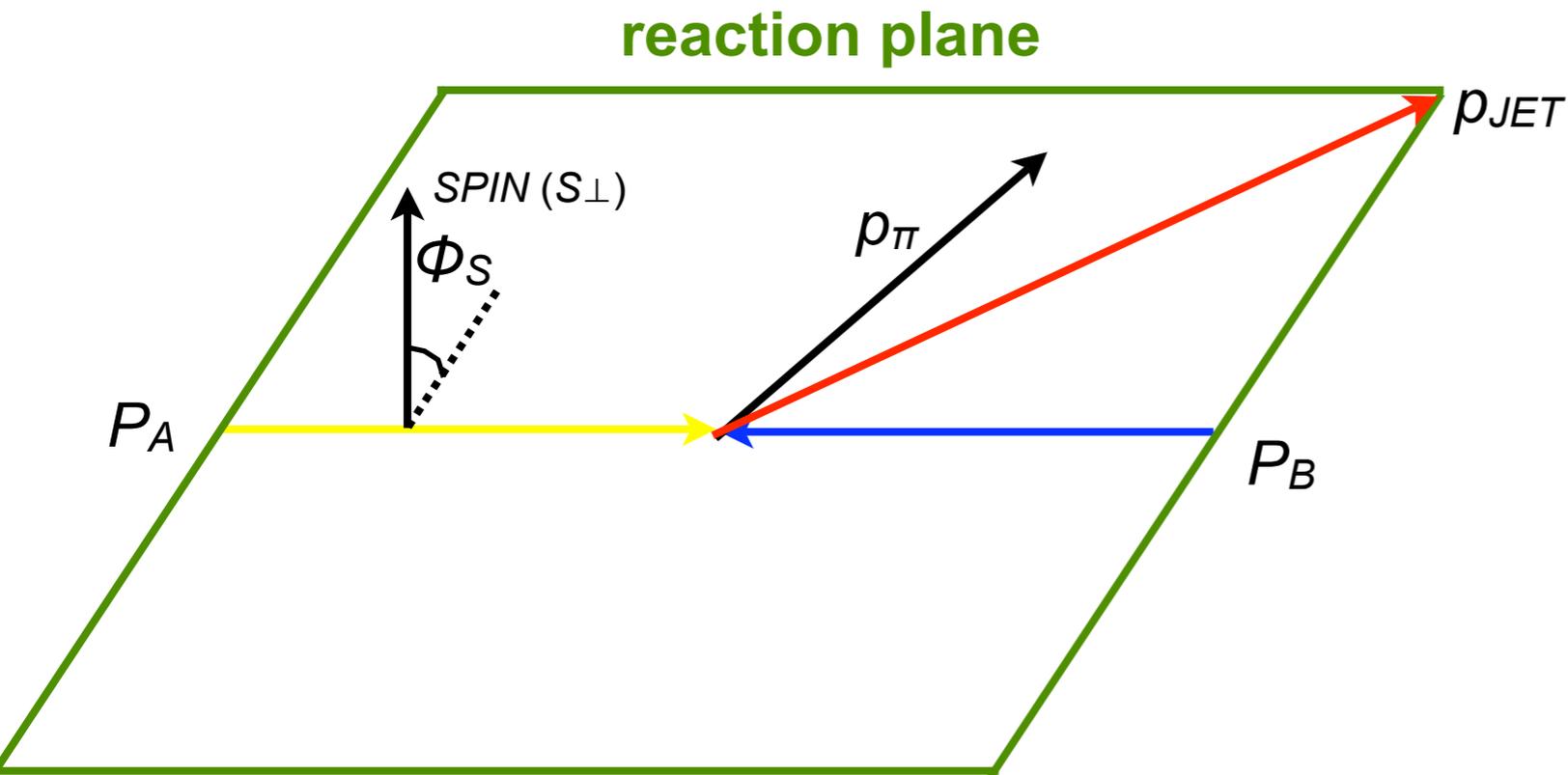


# Experimental access to $\delta q$

proton-proton scattering:

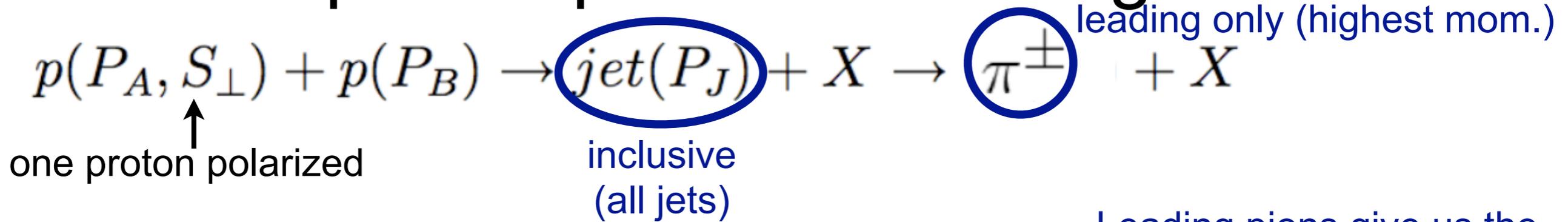


Leading pions give us the most direct access to the quark initiating the event.

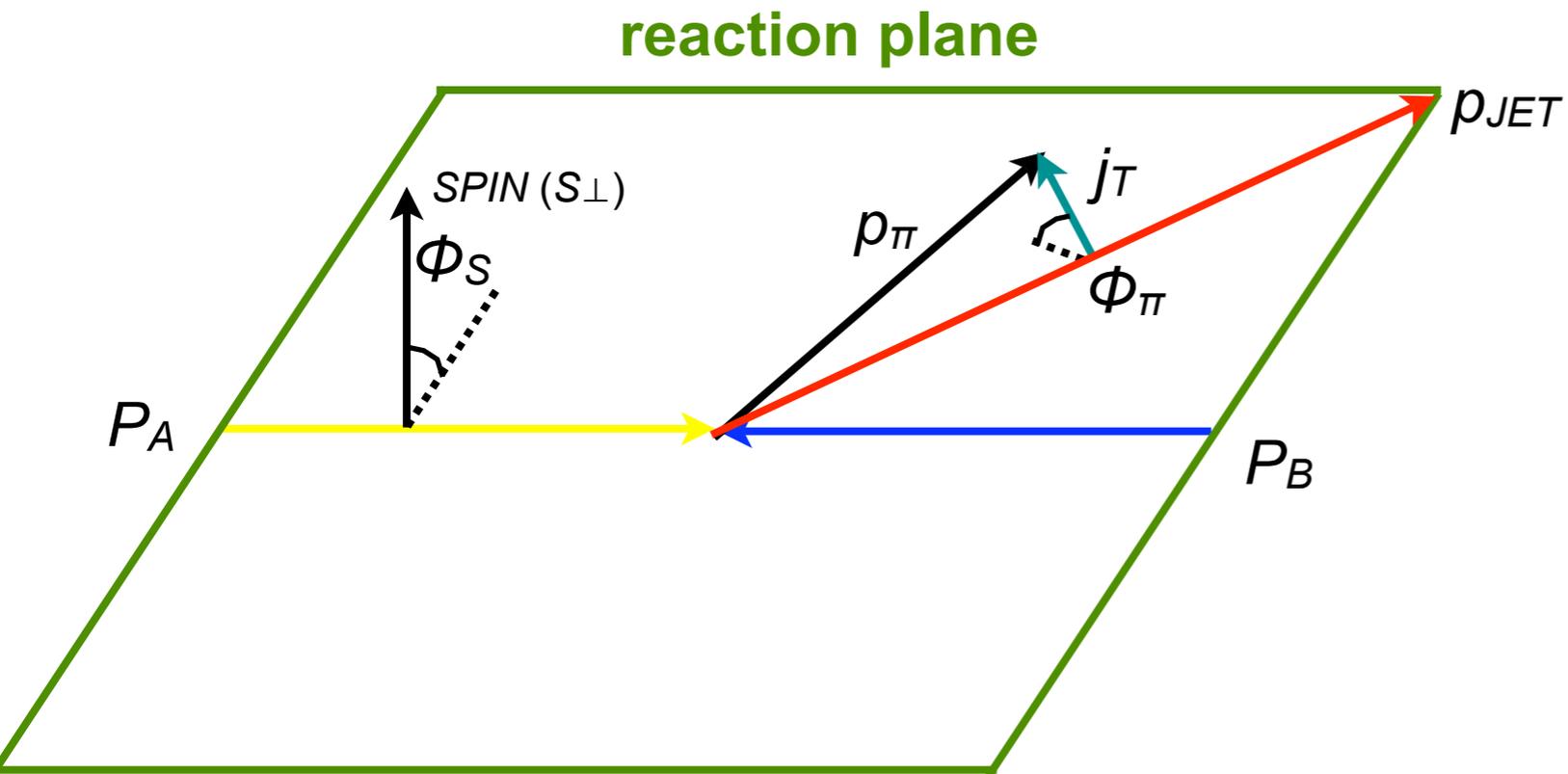


# Experimental access to $\delta q$

proton-proton scattering:

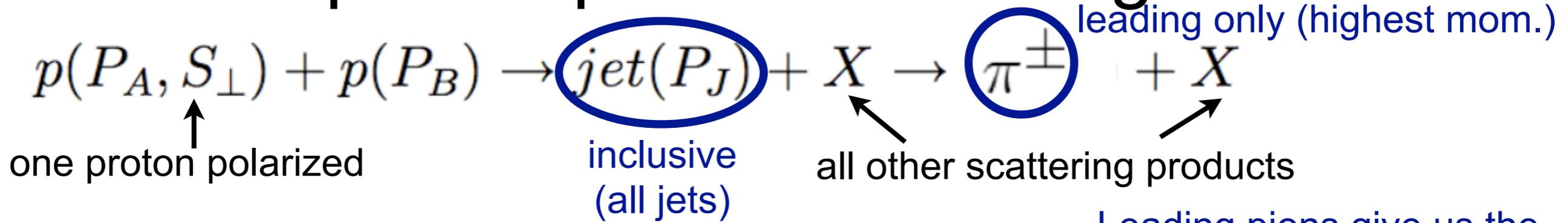


Leading pions give us the most direct access to the quark initiating the event.

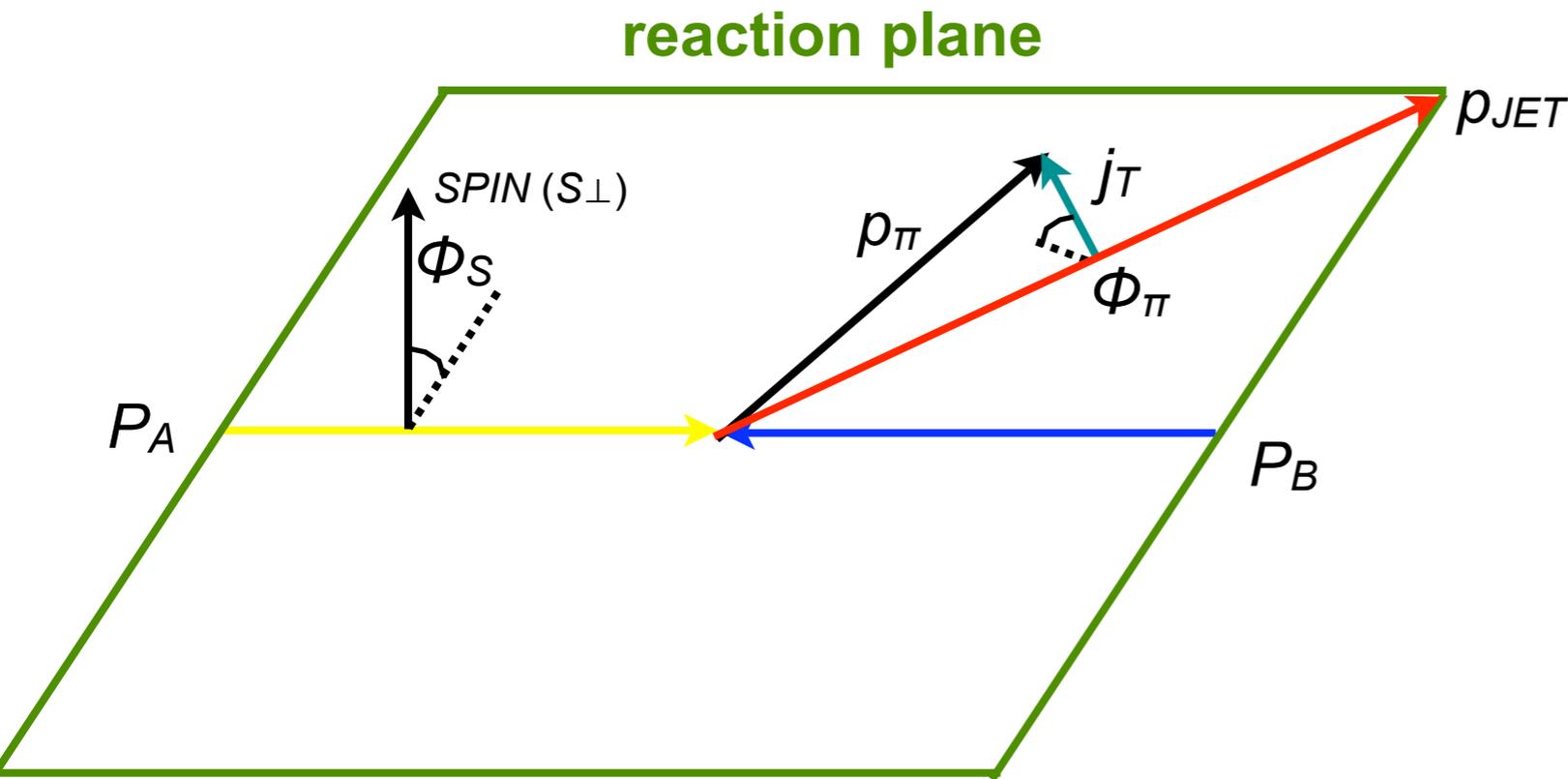


# Experimental access to $\delta q$

proton-proton scattering:

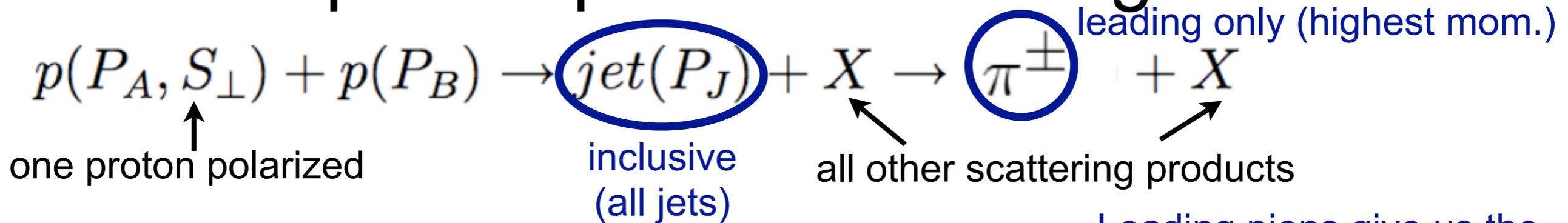


Leading pions give us the most direct access to the quark initiating the event.



# Experimental access to $\delta q$

proton-proton scattering:

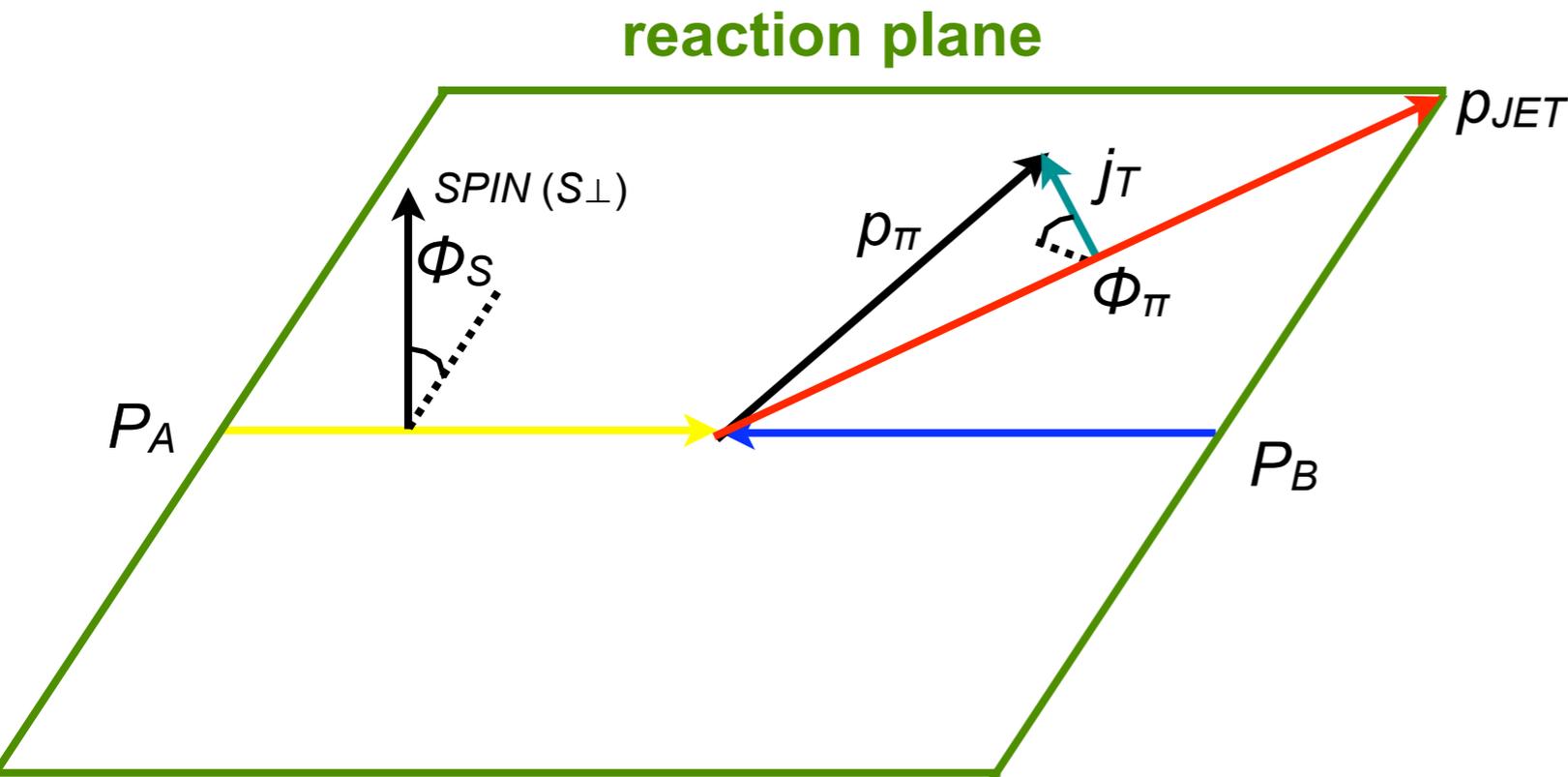


Leading pions give us the most direct access to the quark initiating the event.

**Collins Mechanism:**  
polarized quark  $\rightarrow$  jet  $\Rightarrow$

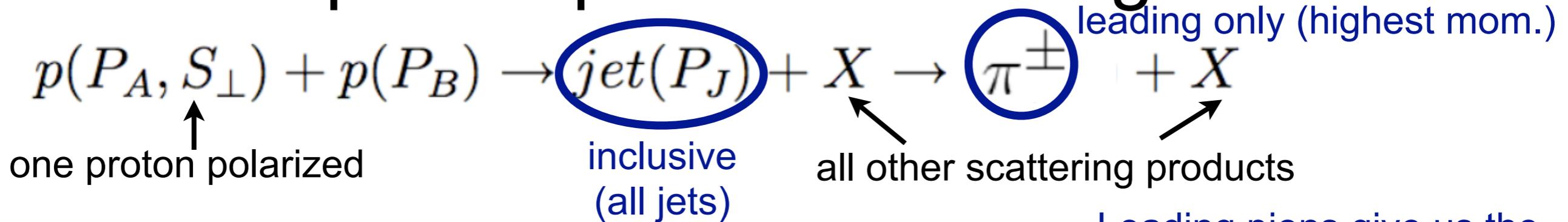
spin-dependence in fragmentation of the polarized quark  $\Rightarrow$

$\Phi_{\pi}$ -dependence of pion production rate, relative to  $S_{\perp}^{\pm}$



# Experimental access to $\delta q$

proton-proton scattering:

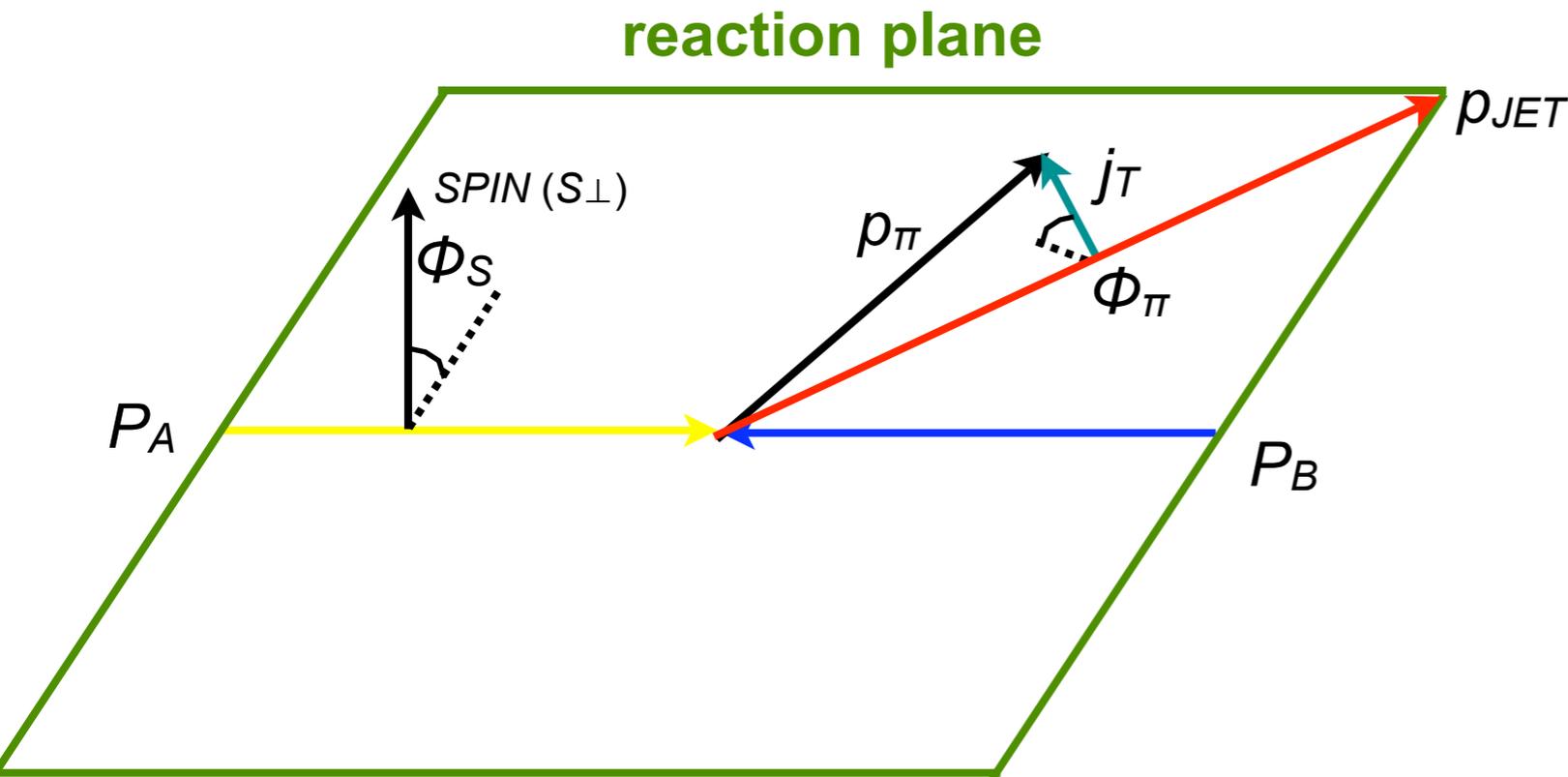


Leading pions give us the most direct access to the quark initiating the event.

**Collins Mechanism:**  
polarized quark  $\rightarrow$  jet  $\Rightarrow$

spin-dependence in fragmentation of the polarized quark  $\Rightarrow$

$\Phi_{\pi}$ -dependence of pion production rate, relative to  $S_{\perp}^{\pm}$



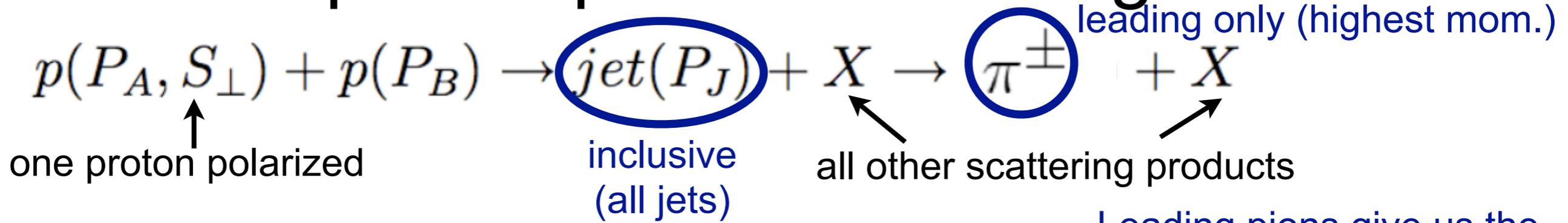
Measured asymmetry

$$z \equiv \rho_{\pi} / \rho_{JET}$$

$$A(z, j_T) = \frac{\langle \sin(\Phi_{\pi} - \Phi_S) \rangle}{N}$$

# Experimental access to $\delta q$

proton-proton scattering:

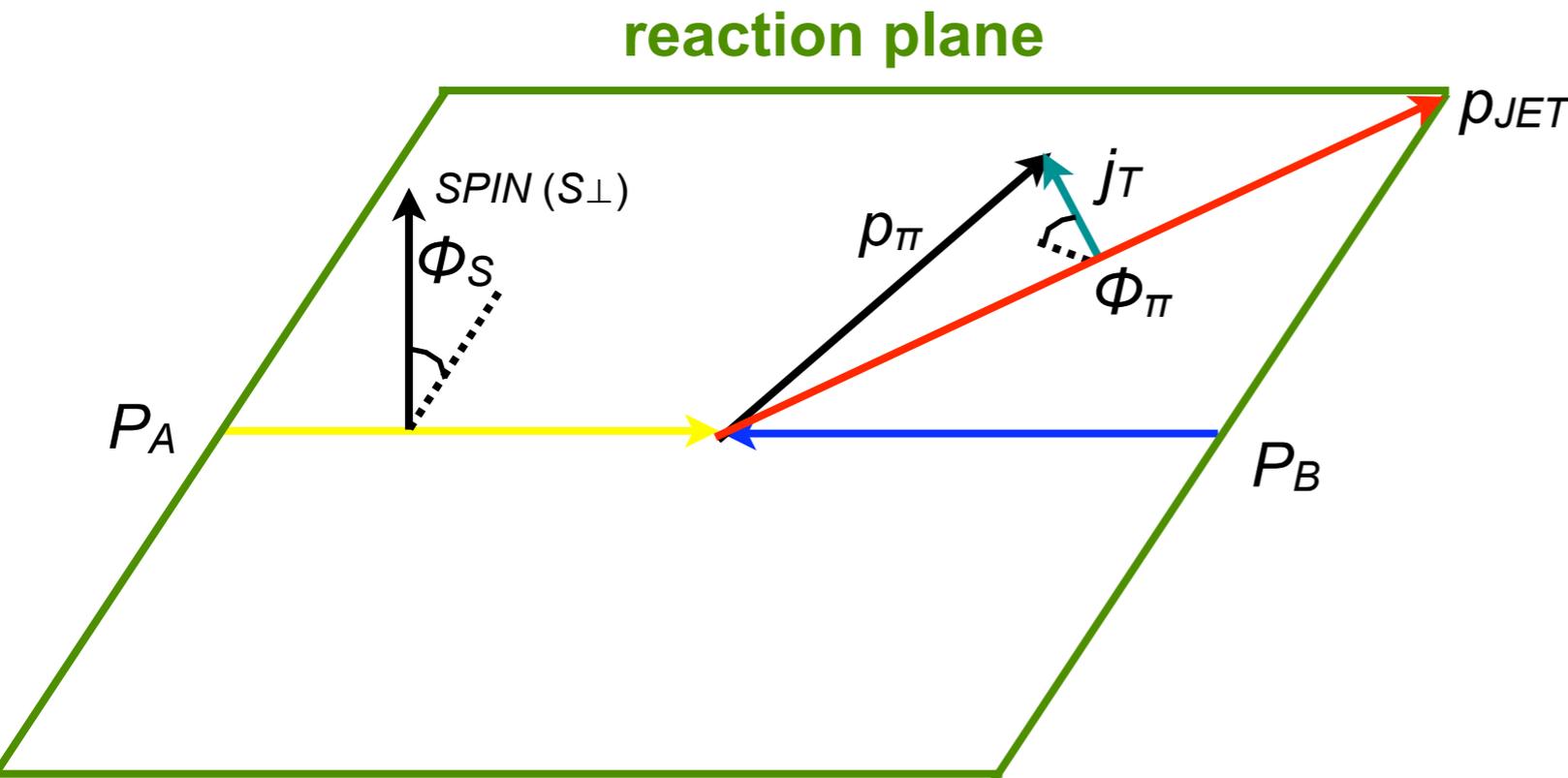


Leading pions give us the most direct access to the quark initiating the event.

**Collins Mechanism:**  
polarized quark  $\rightarrow$  jet  $\Rightarrow$

spin-dependence in fragmentation of the polarized quark  $\Rightarrow$

$\Phi_{\pi}$ -dependence of pion production rate, relative to  $S_{\perp}^{\pm}$



Measured asymmetry

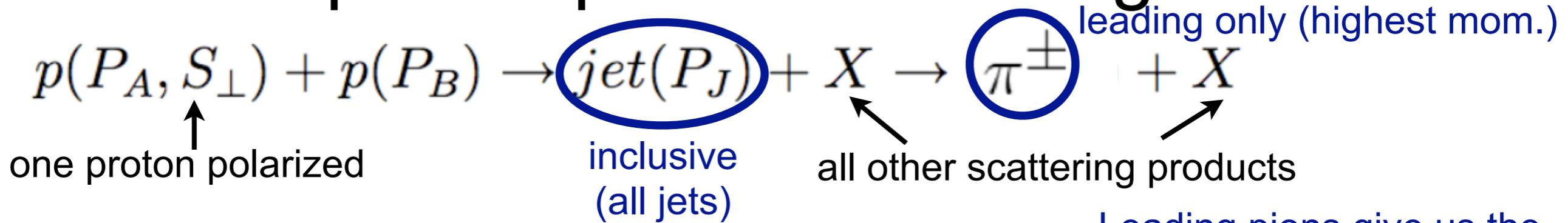
$$z \equiv \rho_{\pi} / \rho_{JET}$$

$$A(z, j_T) = \frac{\langle \sin(\Phi_{\pi} - \Phi_S) \rangle}{N}$$

=0 if distribution of pions within jet symmetric

# Experimental access to $\delta q$

proton-proton scattering:

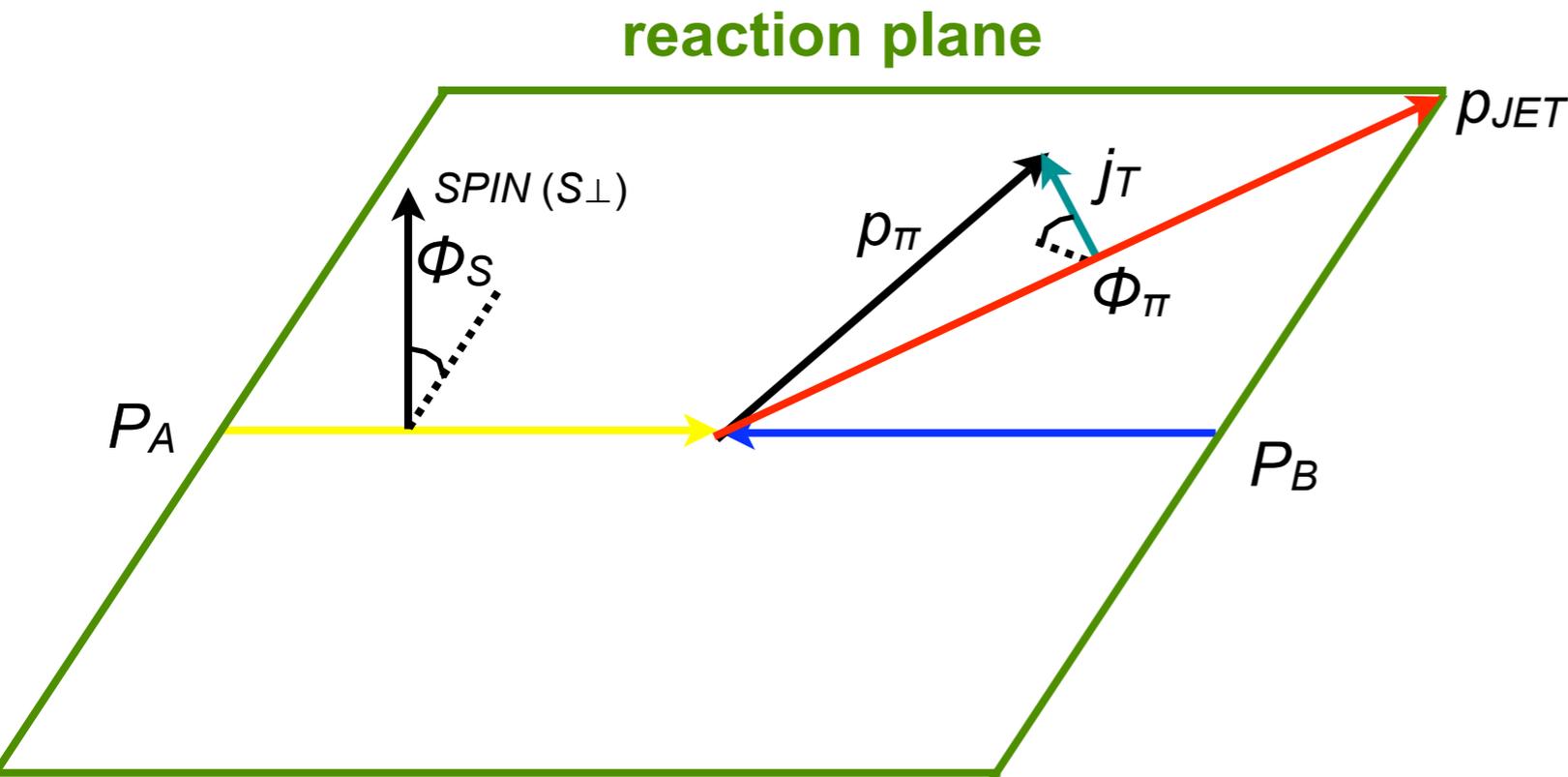


Leading pions give us the most direct access to the quark initiating the event.

**Collins Mechanism:**  
polarized quark  $\rightarrow$  jet  $\Rightarrow$

spin-dependence in fragmentation of the polarized quark  $\Rightarrow$

$\Phi_{\pi}$ -dependence of pion production rate, relative to  $S_{\perp}^{\pm}$



Measured asymmetry

$$z \equiv \rho_{\pi} / \rho_{JET}$$

$$A(z, j_T) = \frac{\langle \sin(\Phi_{\pi} - \Phi_S) \rangle}{N}$$

=0 if distribution of pions within jet symmetric

total number of jets

How is  $\Delta u$ ,  $\Delta d$  constrained by this asymmetry?

Measured asymmetry

$$A = \frac{\langle \sin(\Phi_{\pi} - \Phi_S) \rangle}{N}$$

# How is $\Delta u$ , $\Delta d$ constrained by this asymmetry?

Measured asymmetry

$$A = \frac{\langle \sin(\Phi_\pi - \Phi_S) \rangle}{N}$$

$$A \approx \left[ \frac{\delta q(x)}{f_q(x)} \frac{\Delta^N D_q(z, j_T)}{D_q^h(z, j_T)} \frac{H_{qb \rightarrow qb}^{\text{Collins}}}{H_{qb \rightarrow cd}} \right]_{\text{favored } q} + \left[ \frac{\delta q(x)}{f_q(x)} \frac{\Delta^N D_q(z, j_T)}{D_q^h(z, j_T)} \frac{H_{qb \rightarrow qb}^{\text{Collins}}}{H_{qb \rightarrow cd}} \right]_{\text{unfavored } q}$$

# How is $\Delta u$ , $\Delta d$ constrained by this asymmetry?

Measured asymmetry

$$A = \frac{\langle \sin(\Phi_\pi - \Phi_S) \rangle}{N}$$

$$A \approx \left[ \frac{\delta q(x)}{f_q(x)} \frac{\Delta^N D_q(z, j_T)}{D_q^h(z, j_T)} \frac{H_{qb \rightarrow qb}^{\text{Collins}}}{H_{qb \rightarrow cd}} \right]_{\text{favored } q} + \left[ \frac{\delta q(x)}{f_q(x)} \frac{\Delta^N D_q(z, j_T)}{D_q^h(z, j_T)} \frac{H_{qb \rightarrow qb}^{\text{Collins}}}{H_{qb \rightarrow cd}} \right]_{\text{unfavored } q}$$

$\pi^+$ : favored =  $u$ , unfavored =  $d$   
 $\pi^-$ : favored =  $d$ , unfavored =  $u$

# How is $\Delta u$ , $\Delta d$ constrained by this asymmetry?

Measured asymmetry

$$A = \frac{\langle \sin(\Phi_\pi - \Phi_S) \rangle}{N}$$

$$A \approx \left[ \frac{\delta q(x)}{f_q(x)} \frac{\Delta^N D_q(z, j_T)}{D_q^h(z, j_T)} \frac{H_{qb \rightarrow qb}^{\text{Collins}}}{H_{qb \rightarrow cd}} \right]_{\text{favored } q} + \left[ \frac{\delta q(x)}{f_q(x)} \frac{\Delta^N D_q(z, j_T)}{D_q^h(z, j_T)} \frac{H_{qb \rightarrow qb}^{\text{Collins}}}{H_{qb \rightarrow cd}} \right]_{\text{unfavored } q}$$

**unpolarized quark distribution**

$\pi^+$ : favored =  $u$ , unfavored =  $d$

$\pi^-$ : favored =  $d$ , unfavored =  $u$

# How is $\Delta u$ , $\Delta d$ constrained by this asymmetry?

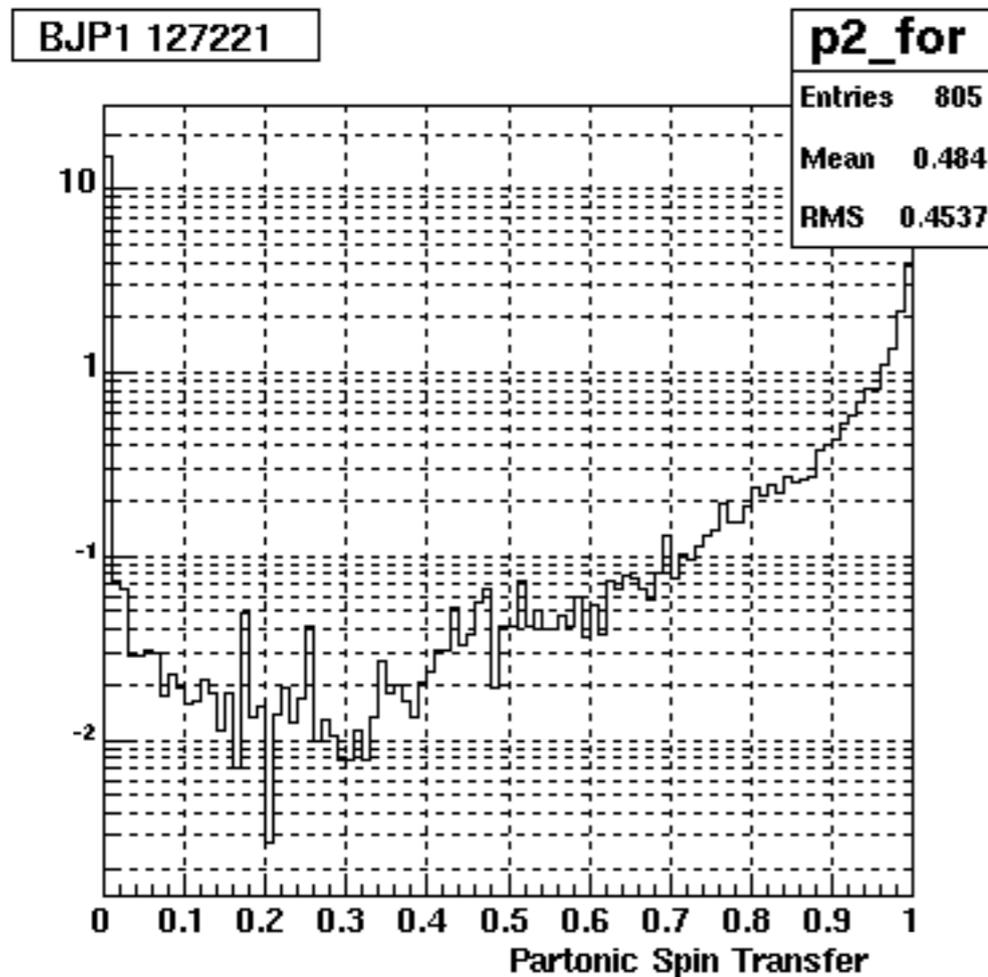
Measured asymmetry

$$A = \frac{\langle \sin(\Phi_\pi - \Phi_S) \rangle}{N}$$

$$A \approx \left[ \frac{\delta q(x)}{f_q(x)} \frac{\Delta^N D_q(z, j_T)}{D_q^h(z, j_T)} \frac{H_{qb \rightarrow qb}^{\text{Collins}}}{H_{qb \rightarrow cd}} \right]_{\text{favored } q} + \left[ \frac{\delta q(x)}{f_q(x)} \frac{\Delta^N D_q(z, j_T)}{D_q^h(z, j_T)} \frac{H_{qb \rightarrow qb}^{\text{Collins}}}{H_{qb \rightarrow cd}} \right]_{\text{unfavored } q}$$

Spin transfer coefficient  $\downarrow$  unpolarized quark distribution

$\pi^+$ : favored =  $u$ , unfavored =  $d$   
 $\pi^-$ : favored =  $d$ , unfavored =  $u$



(GEANT + PYTHIA) simulation

# How is $\Delta u, \Delta d$ constrained by this asymmetry?

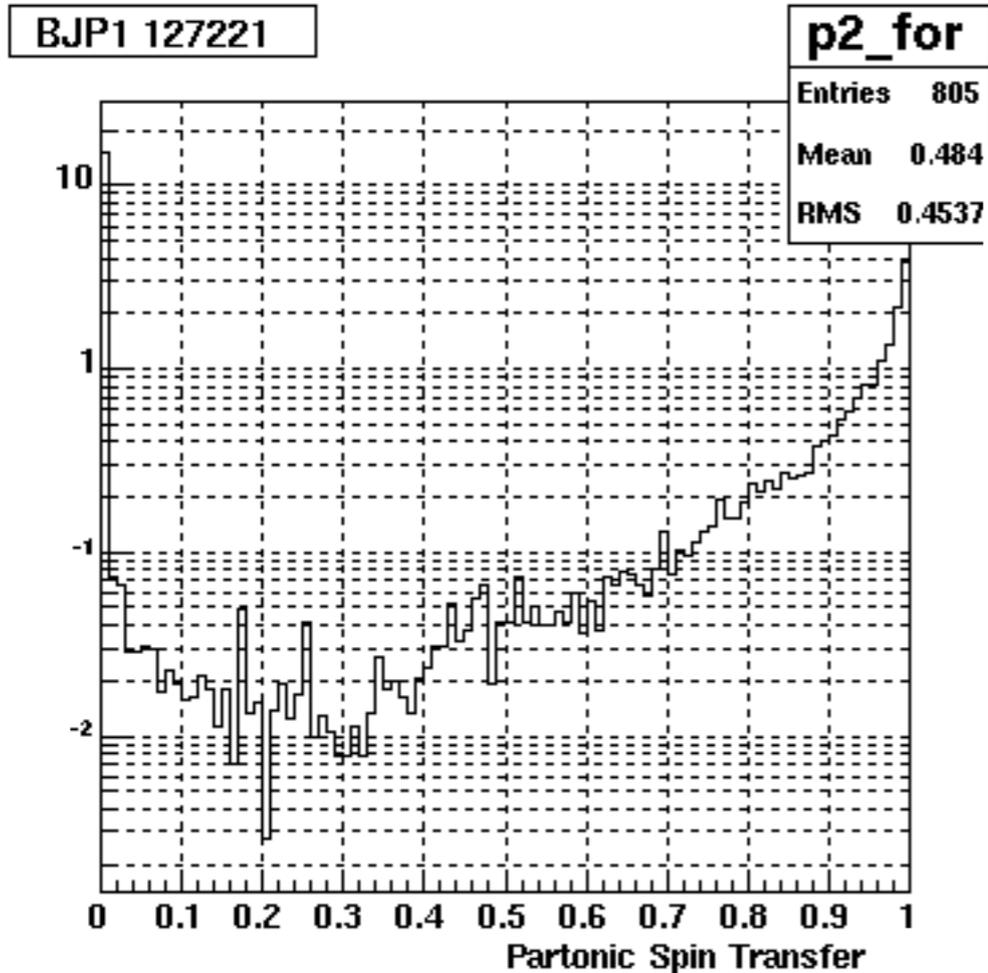
Measured asymmetry

$$A = \frac{\langle \sin(\Phi_{\pi} - \Phi_S) \rangle}{N}$$

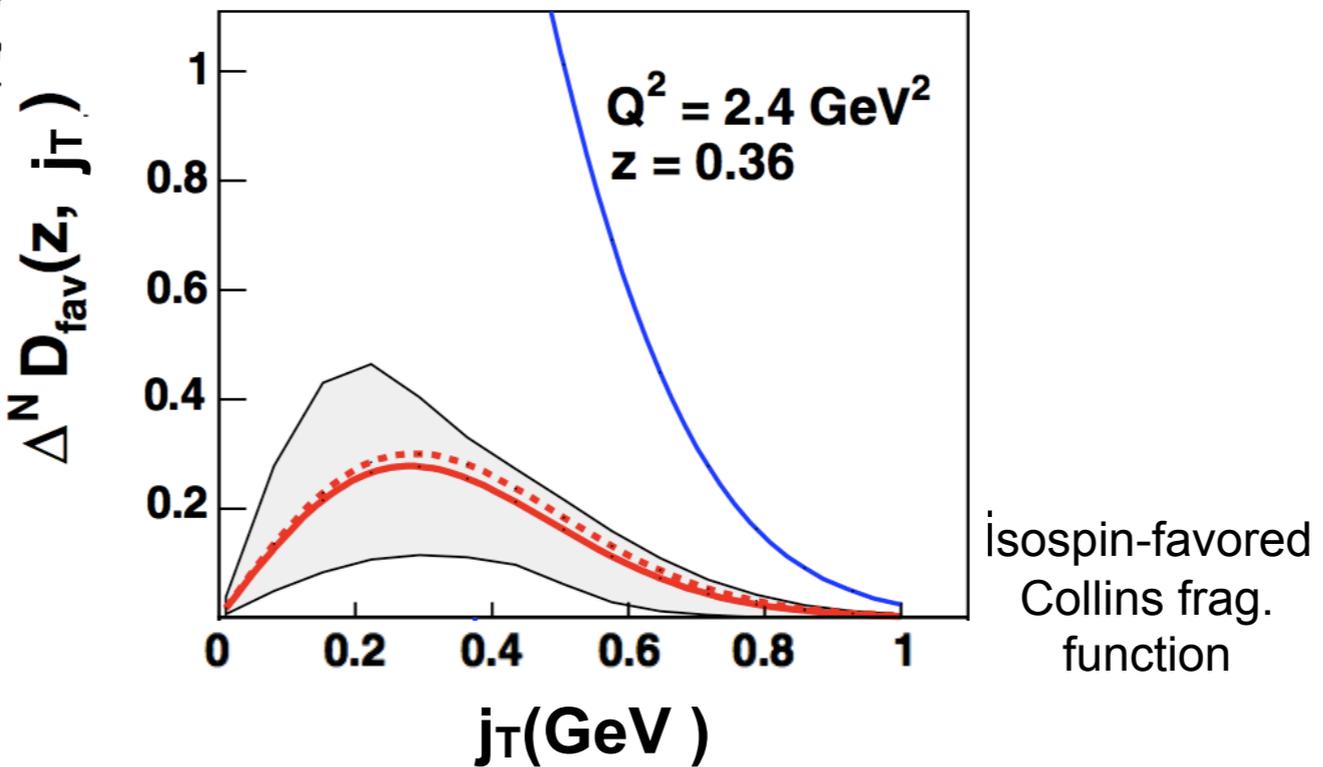
$$A \approx \left[ \frac{\delta q(x)}{f_q(x)} \frac{\Delta^N D_q(z, j_T)}{D_q^h(z, j_T)} \frac{H_{qb \rightarrow qb}^{\text{Collins}}}{H_{qb \rightarrow cd}} \right]_{\text{favored } q} + \left[ \frac{\delta q(x)}{f_q(x)} \frac{\Delta^N D_q(z, j_T)}{D_q^h(z, j_T)} \frac{H_{qb \rightarrow qb}^{\text{Collins}}}{H_{qb \rightarrow cd}} \right]_{\text{unfavored } q}$$

Spin transfer coefficient      unpolarized quark distribution      Collins, Sivers fragmentation functions

$\pi^+$ : favored =  $u$ , unfavored =  $d$   
 $\pi^-$ : favored =  $d$ , unfavored =  $u$



(GEANT + PYTHIA) simulation



# How is $\Delta u, \Delta d$ constrained by this asymmetry?

Measured asymmetry

$$A = \frac{\langle \sin(\Phi_\pi - \Phi_S) \rangle}{N}$$

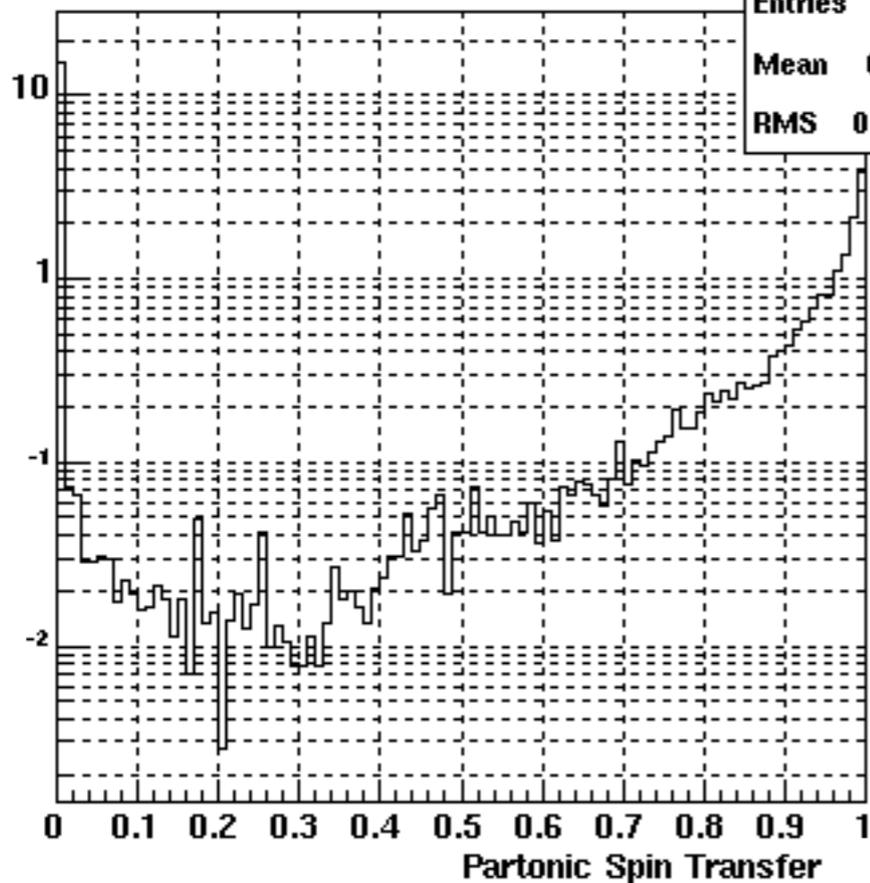
$$A \approx \left[ \frac{\delta q(x)}{f_q(x)} \frac{\Delta^N D_q(z, j_T)}{D_q^h(z, j_T)} \frac{H_{qb \rightarrow qb}^{\text{Collins}}}{H_{qb \rightarrow cd}} \right]_{\text{favored } q} + \left[ \frac{\delta q(x)}{f_q(x)} \frac{\Delta^N D_q(z, j_T)}{D_q^h(z, j_T)} \frac{H_{qb \rightarrow qb}^{\text{Collins}}}{H_{qb \rightarrow cd}} \right]_{\text{unfavored } q}$$

Spin transfer coefficient      unpolarized quark distribution      Collins, Sivers fragmentation functions

$\pi^+$ : favored =  $u$ , unfavored =  $d$   
 $\pi^-$ : favored =  $d$ , unfavored =  $u$

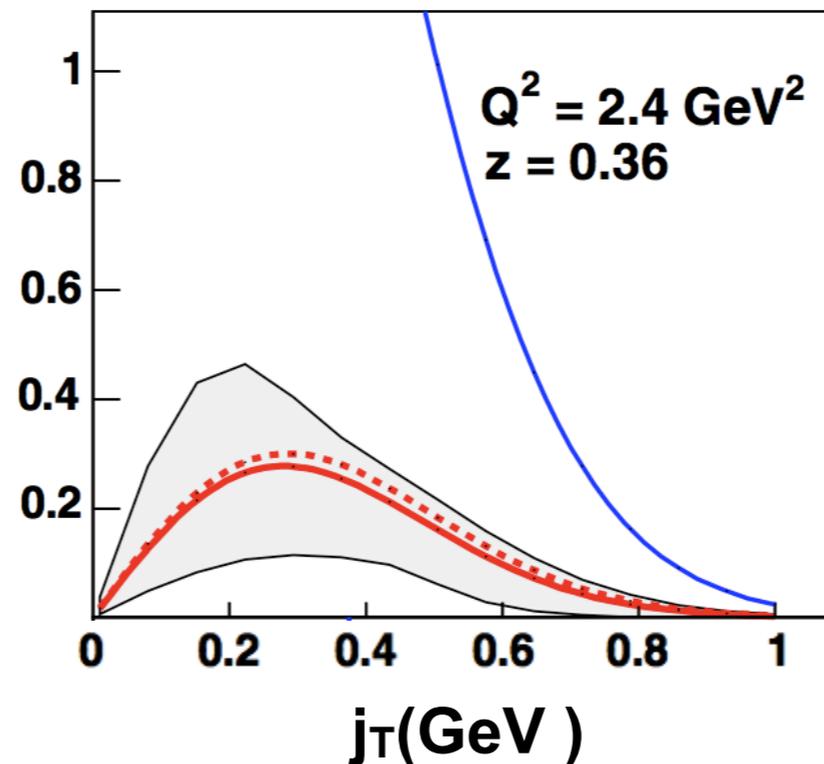
BJP1 127221

p2\_for  
 Entries 805  
 Mean 0.484  
 RMS 0.4537



(GEANT + PYTHIA) simulation

$\Delta^N D_{\text{fav}}(z, j_T)$



Extraction of Collins fragmentation function from fit to SIDIS data (HERMES, COMPASS) and Belle Collab. data (KEK) (Anselmino, *et al.*, 2008)

isospin-favored Collins frag. function

# How is $\Delta u, \Delta d$ constrained by this asymmetry?

Measured asymmetry

$$A = \frac{\langle \sin(\Phi_{\pi} - \Phi_S) \rangle}{N}$$

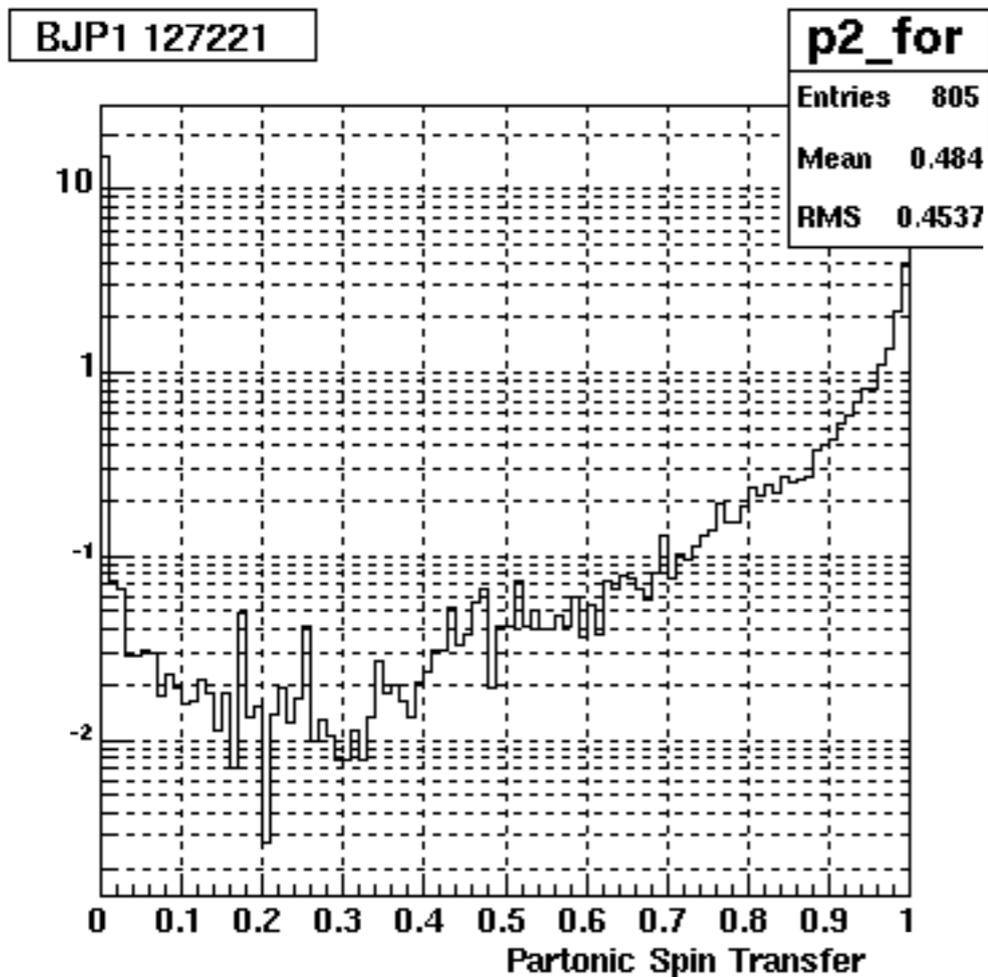
$$A \approx \left[ \frac{\delta q(x)}{f_q(x)} \frac{\Delta^N D_q(z, j_T)}{D_q^h(z, j_T)} \frac{H_{qb \rightarrow qb}^{\text{Collins}}}{H_{qb \rightarrow cd}} \right]_{\text{favored } q} + \left[ \frac{\delta q(x)}{f_q(x)} \frac{\Delta^N D_q(z, j_T)}{D_q^h(z, j_T)} \frac{H_{qb \rightarrow qb}^{\text{Collins}}}{H_{qb \rightarrow cd}} \right]_{\text{unfavored } q}$$

Spin transfer coefficient

unpolarized quark distribution

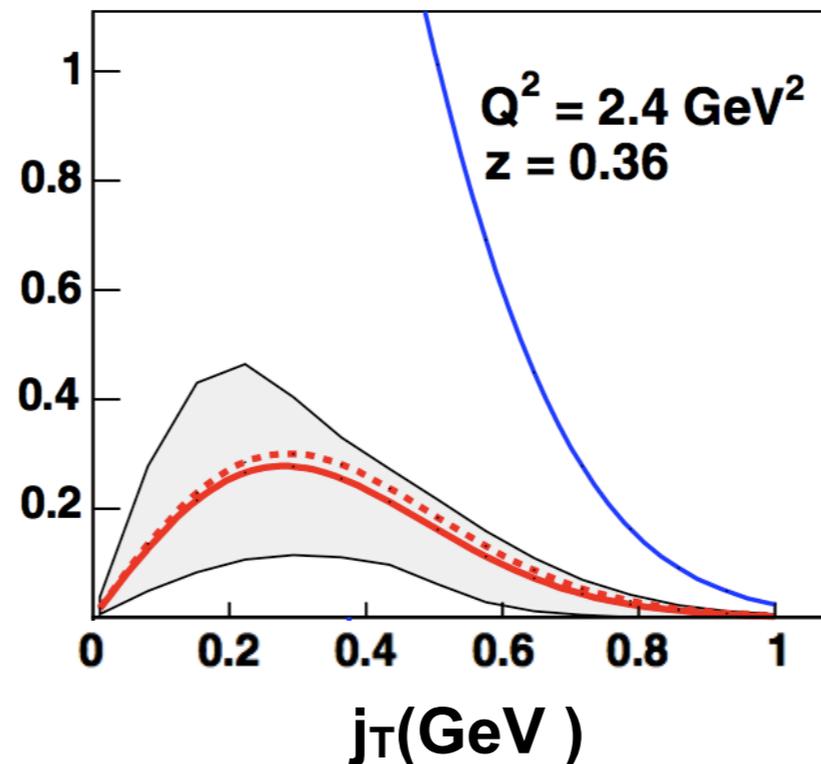
Collins, Siverson fragmentation functions

$\pi^+$ : favored =  $u$ , unfavored =  $d$   
 $\pi^-$ : favored =  $d$ , unfavored =  $u$



(GEANT + PYTHIA) simulation

$\Delta^N D_{\text{fav}}(z, j_T)$



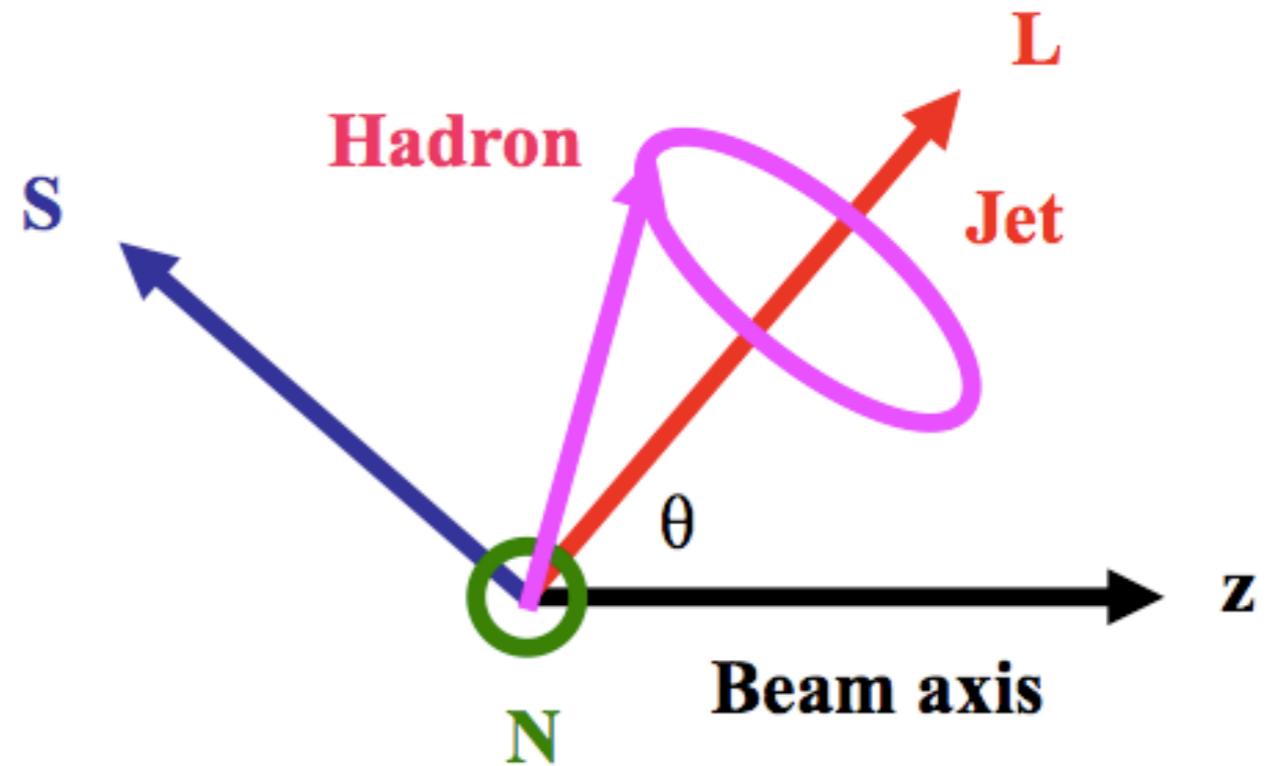
Extraction of Collins fragmentation function from fit to SIDIS data (HERMES, COMPASS) and Belle Collab. data (KEK) (Anselmino, *et al.*, 2008)

Prediction (estimate):  $A(\pi^\pm) \approx \pm 0.03$

# The Collins Asymmetry

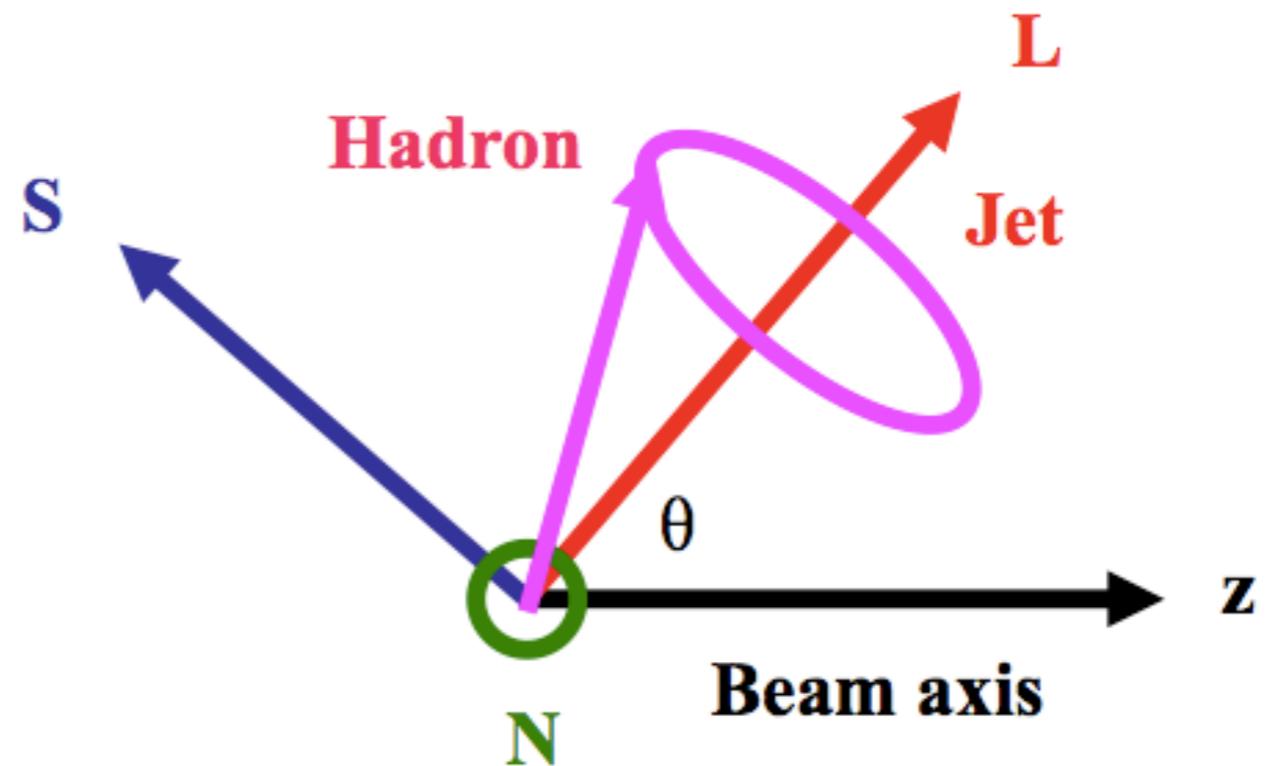
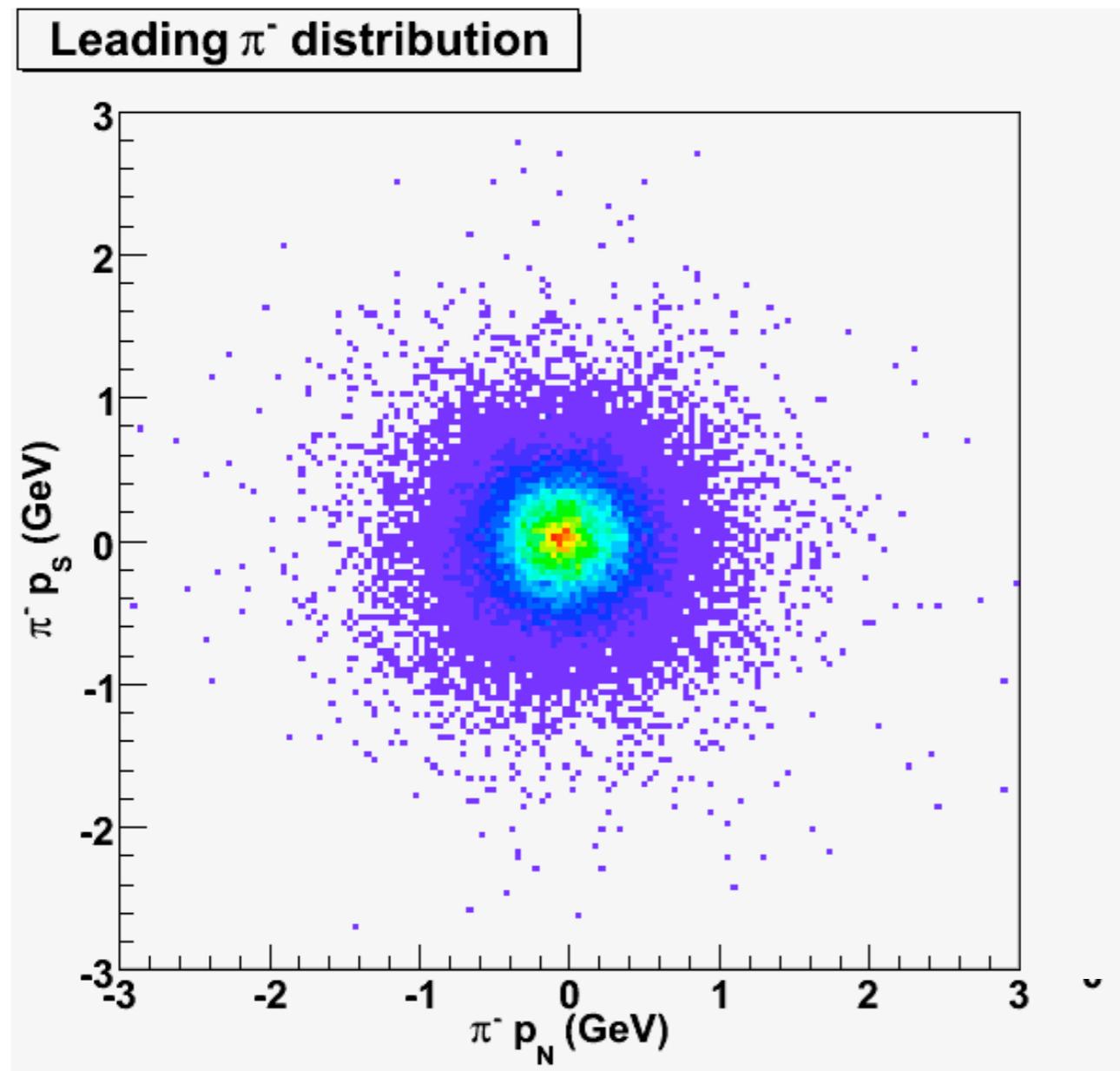
# The Collins Asymmetry

$\Phi_{\pi}$  is defined in NLS coordinates



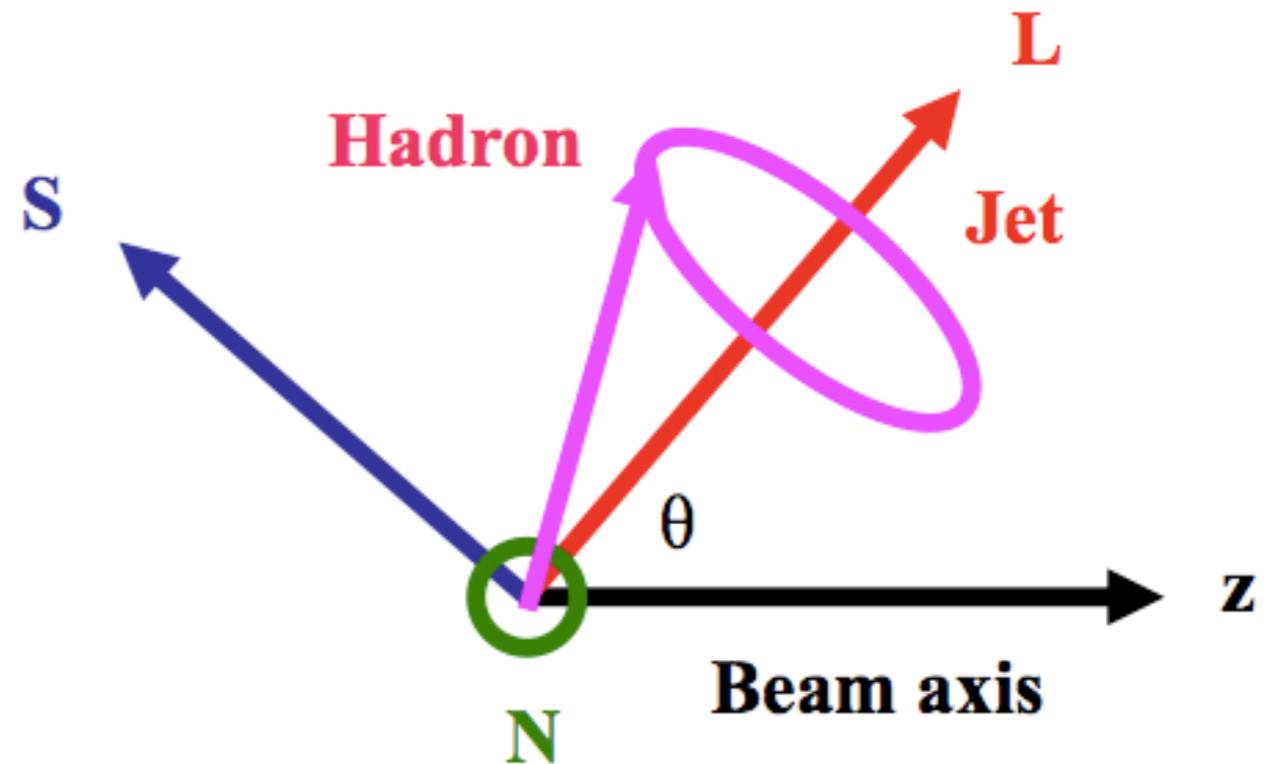
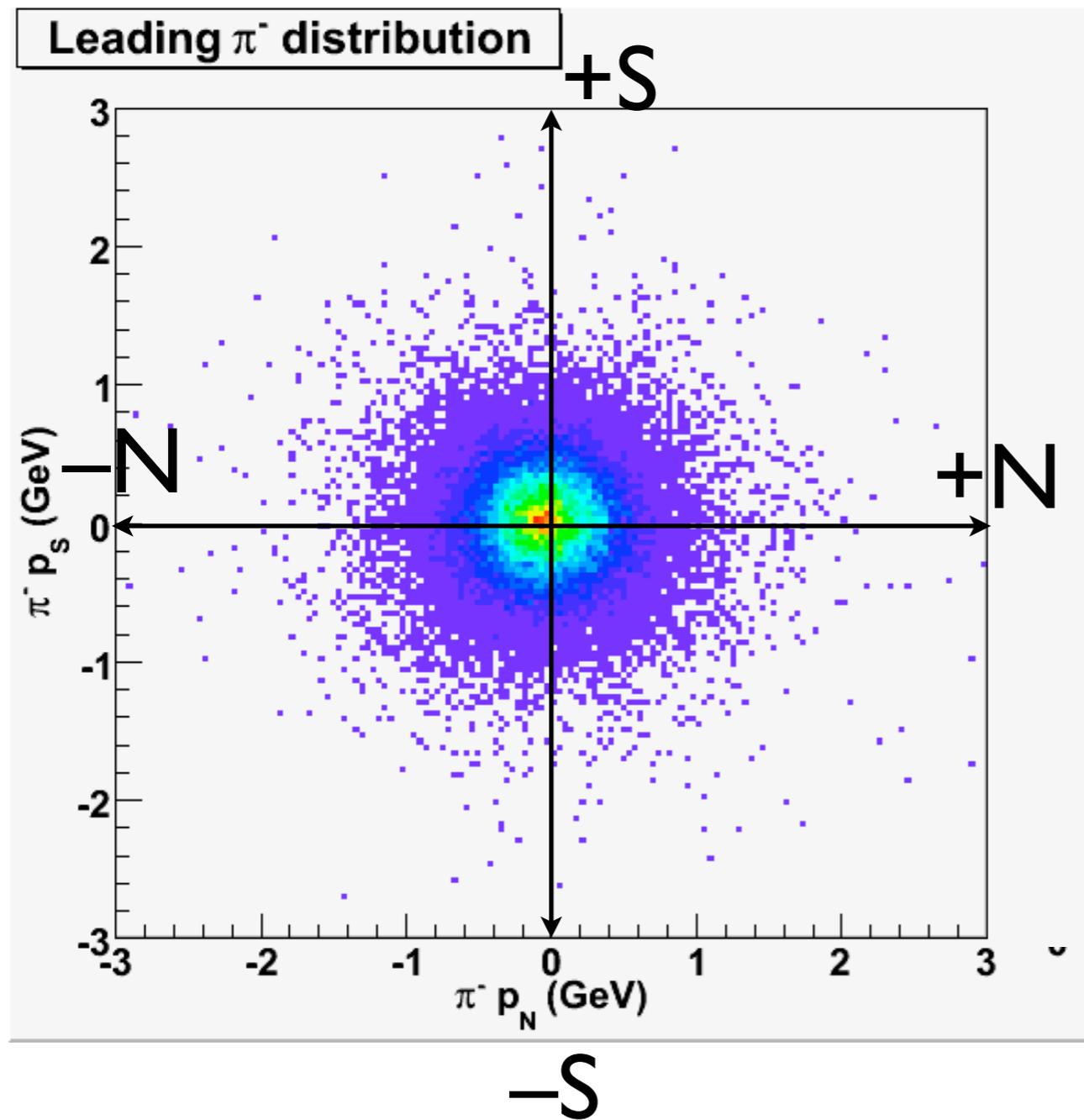
# The Collins Asymmetry

$\Phi_{\pi}$  is defined in NLS coordinates



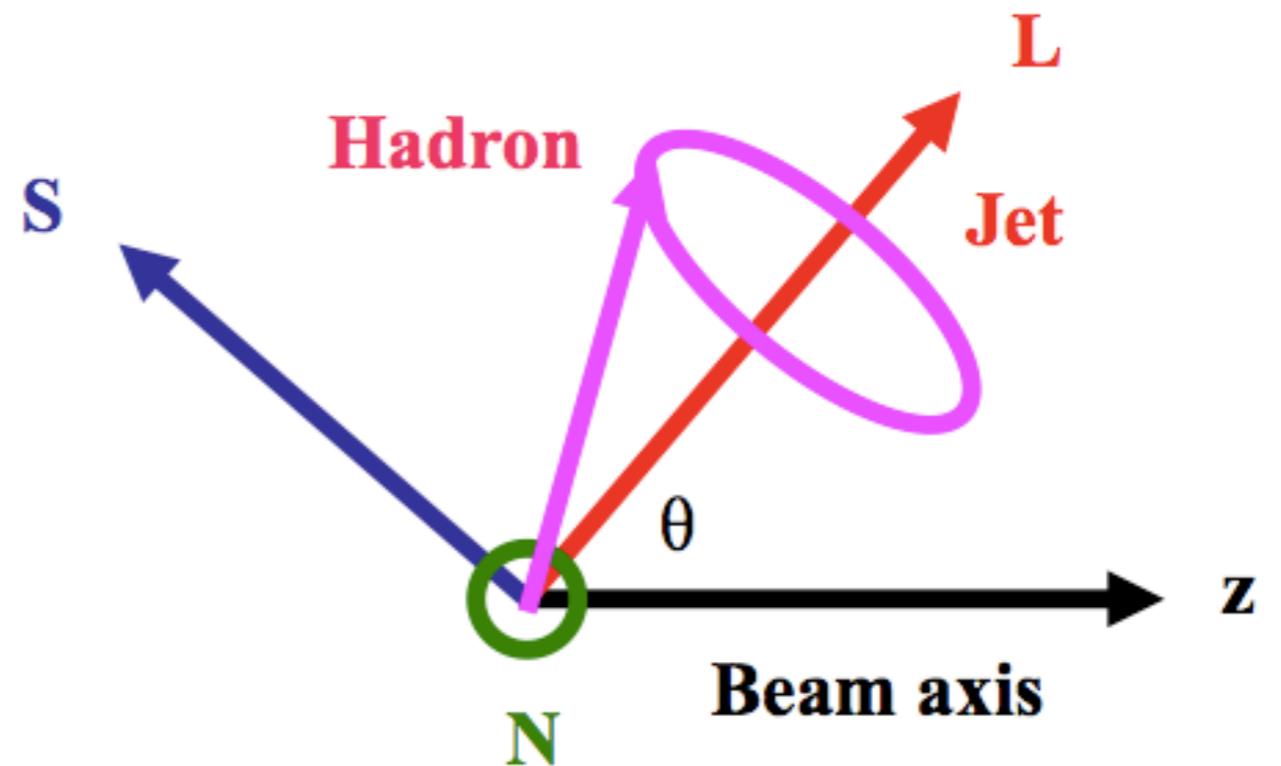
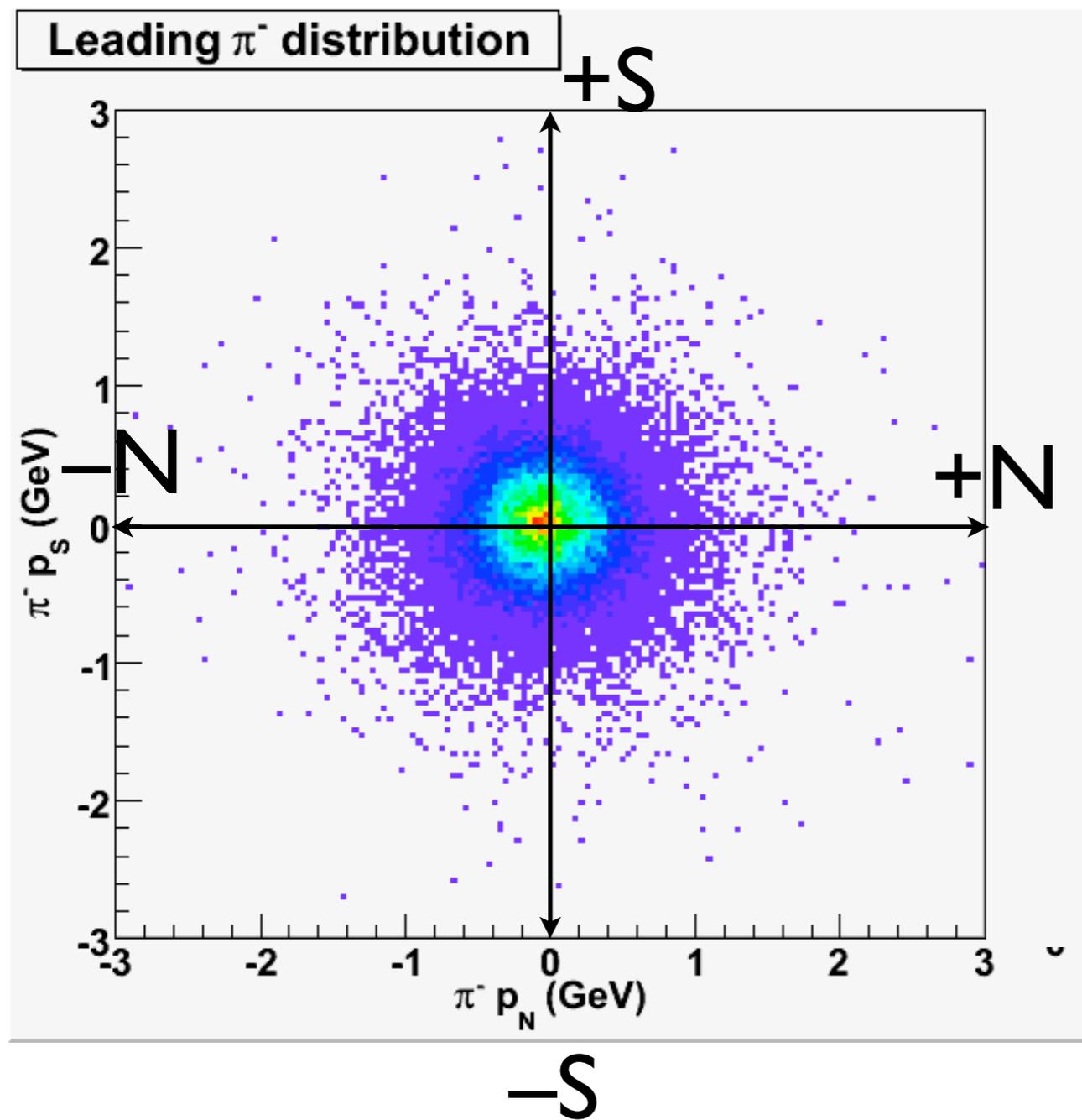
# The Collins Asymmetry

$\Phi_{\pi}$  is defined in NLS coordinates



# The Collins Asymmetry

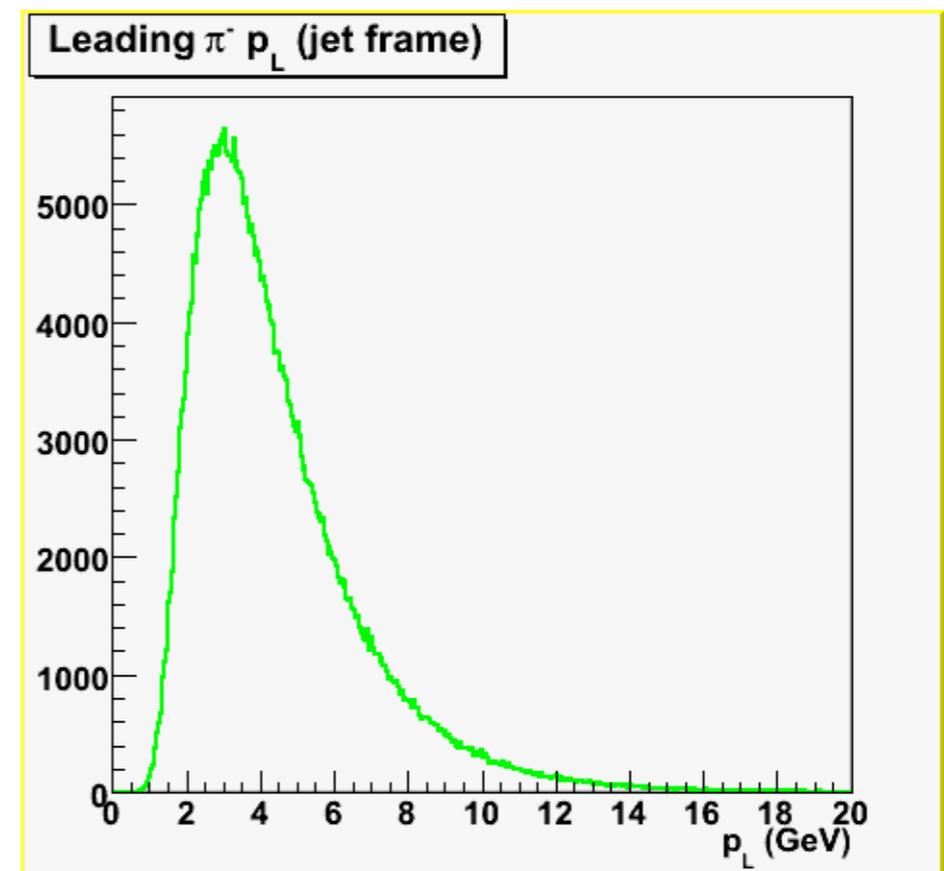
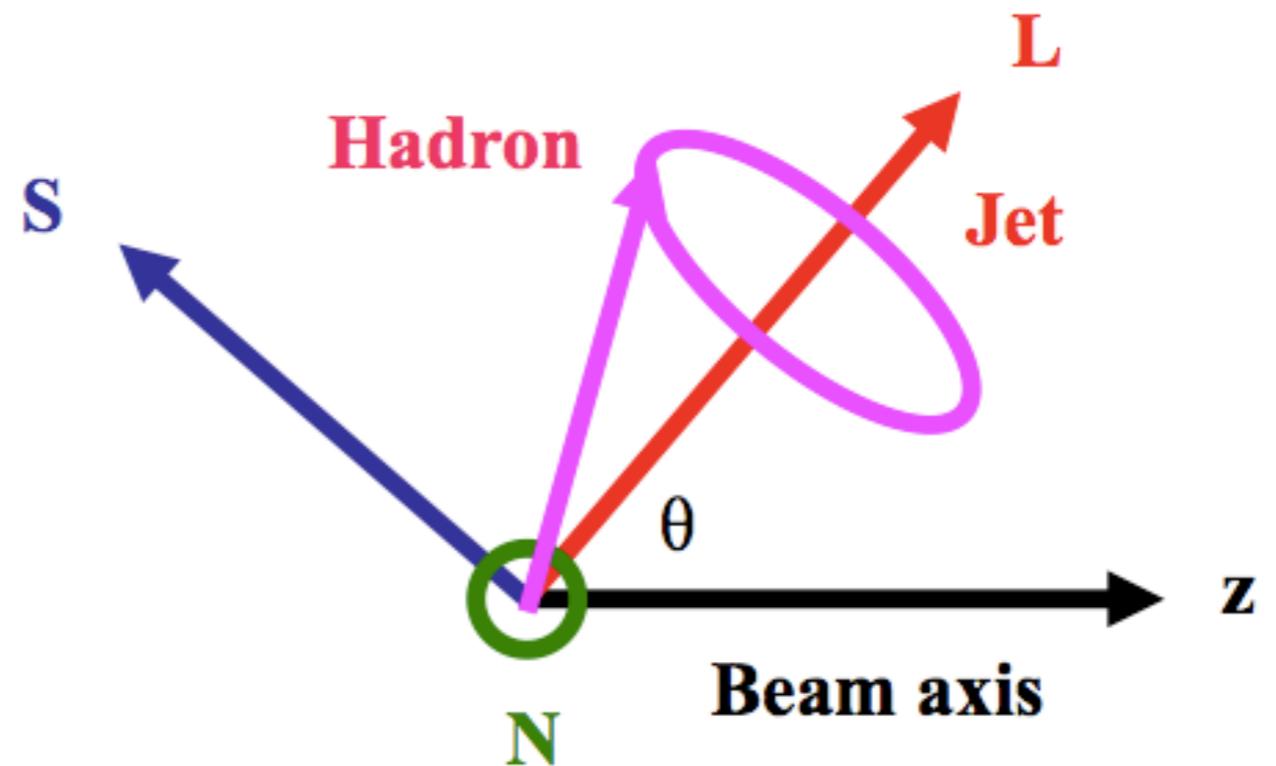
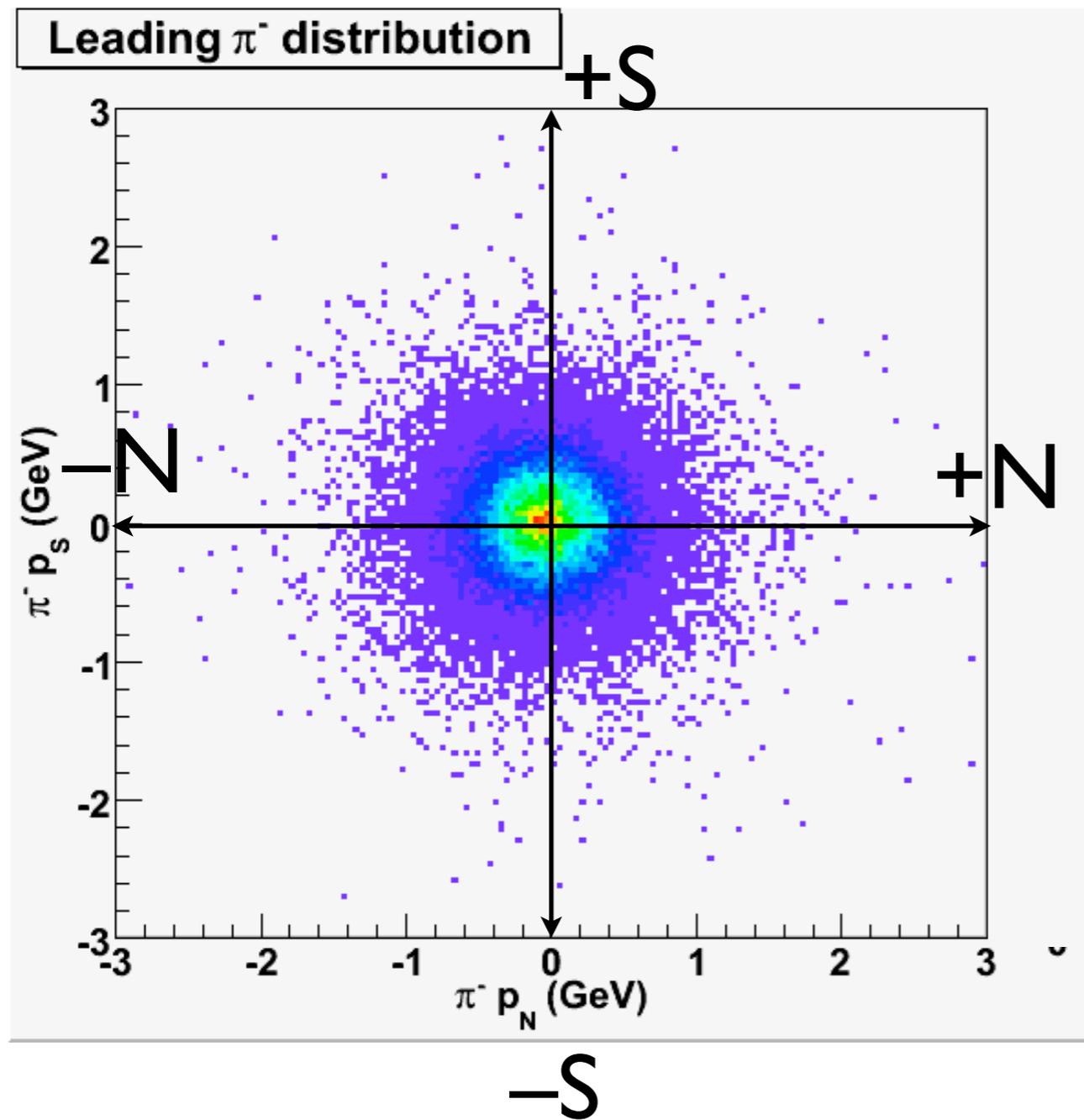
$\Phi_{\pi}$  is defined in NLS coordinates



(L is 3rd axis;  $L = S \times N$ )

# The Collins Asymmetry

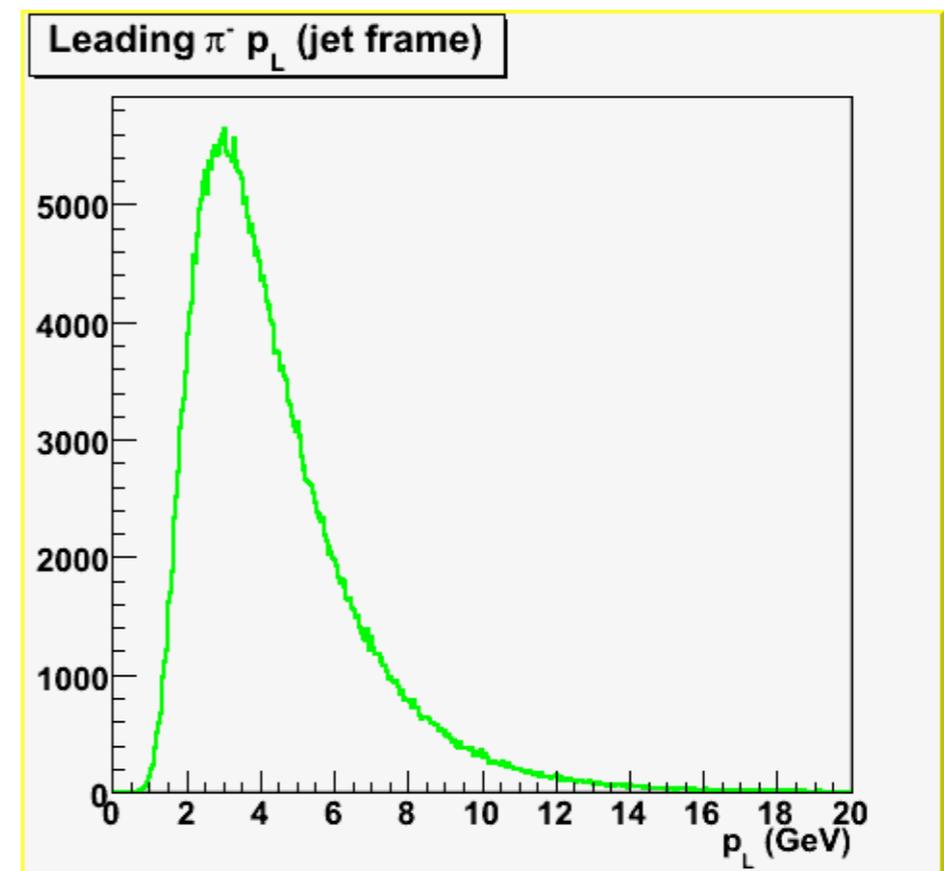
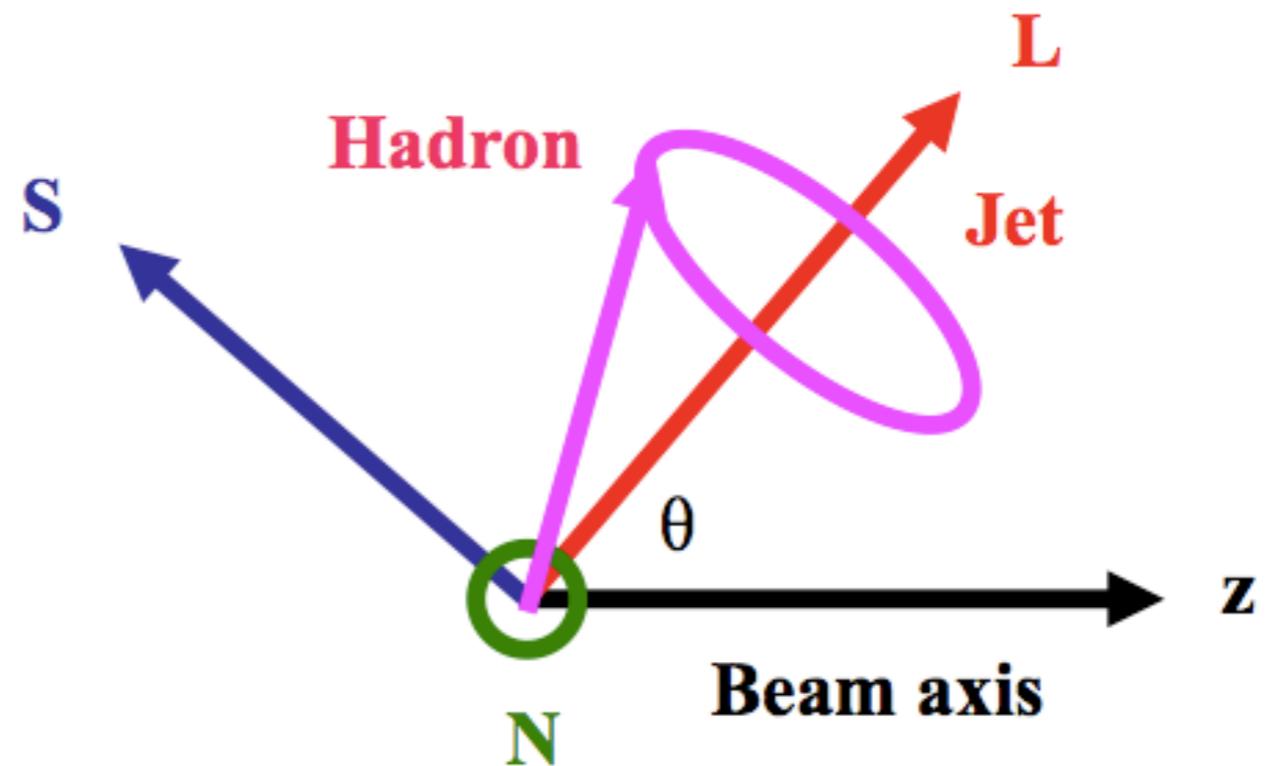
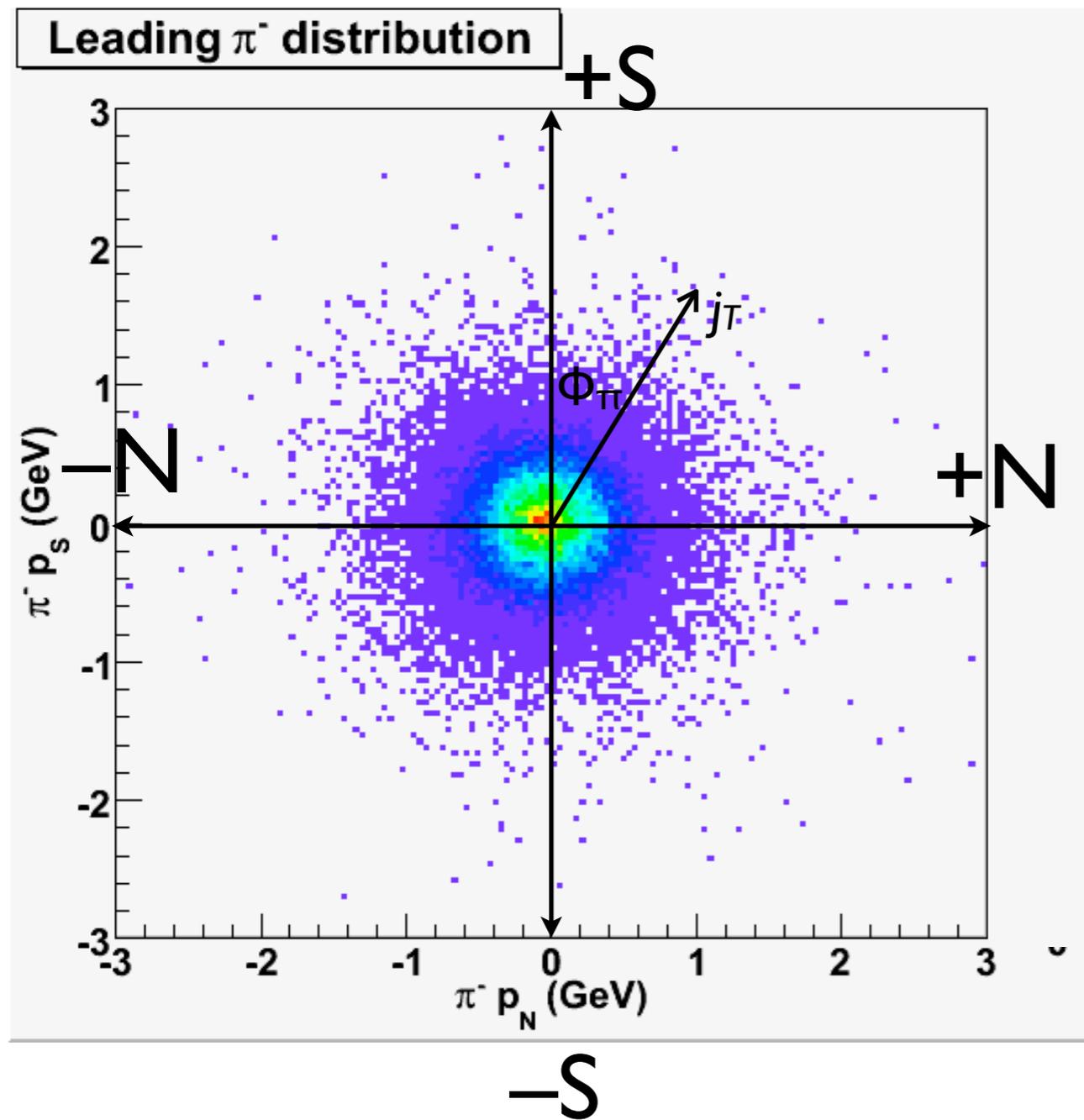
$\Phi_{\pi}$  is defined in NLS coordinates



( $L$  is 3rd axis;  $L = S \times N$ )

# The Collins Asymmetry

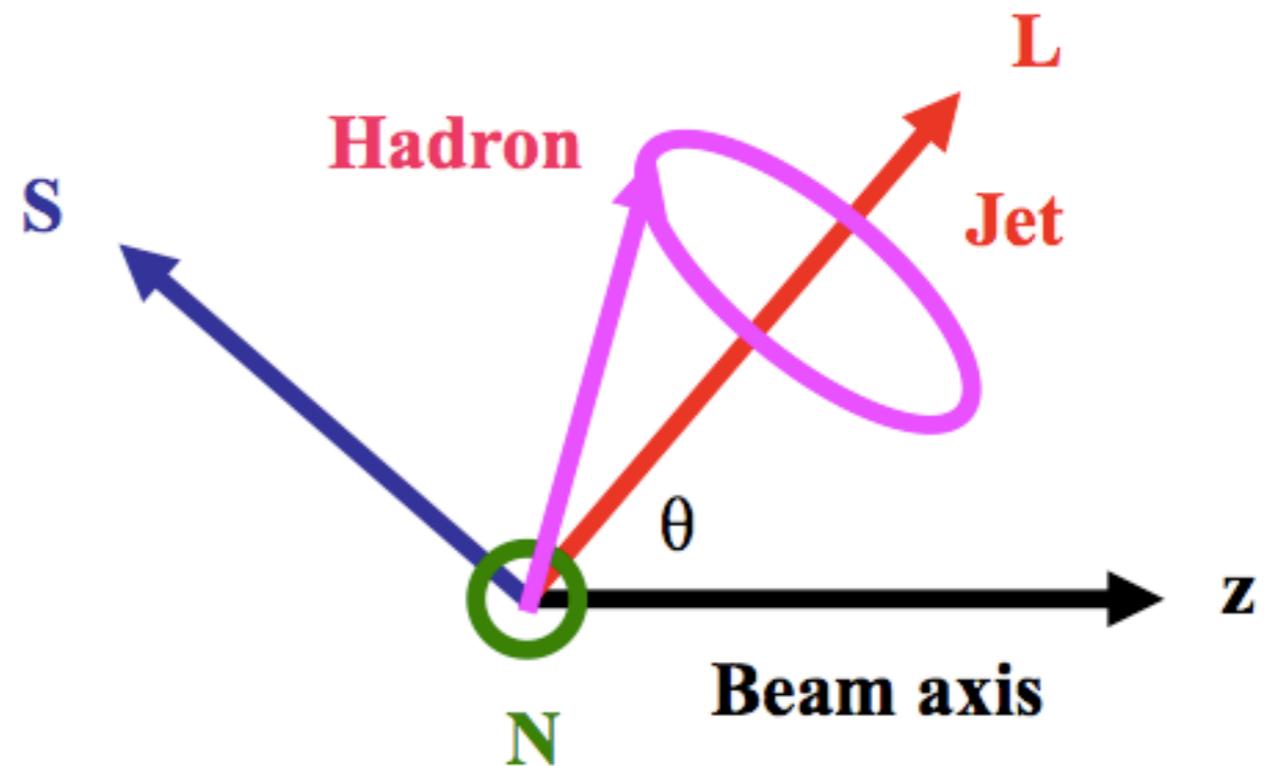
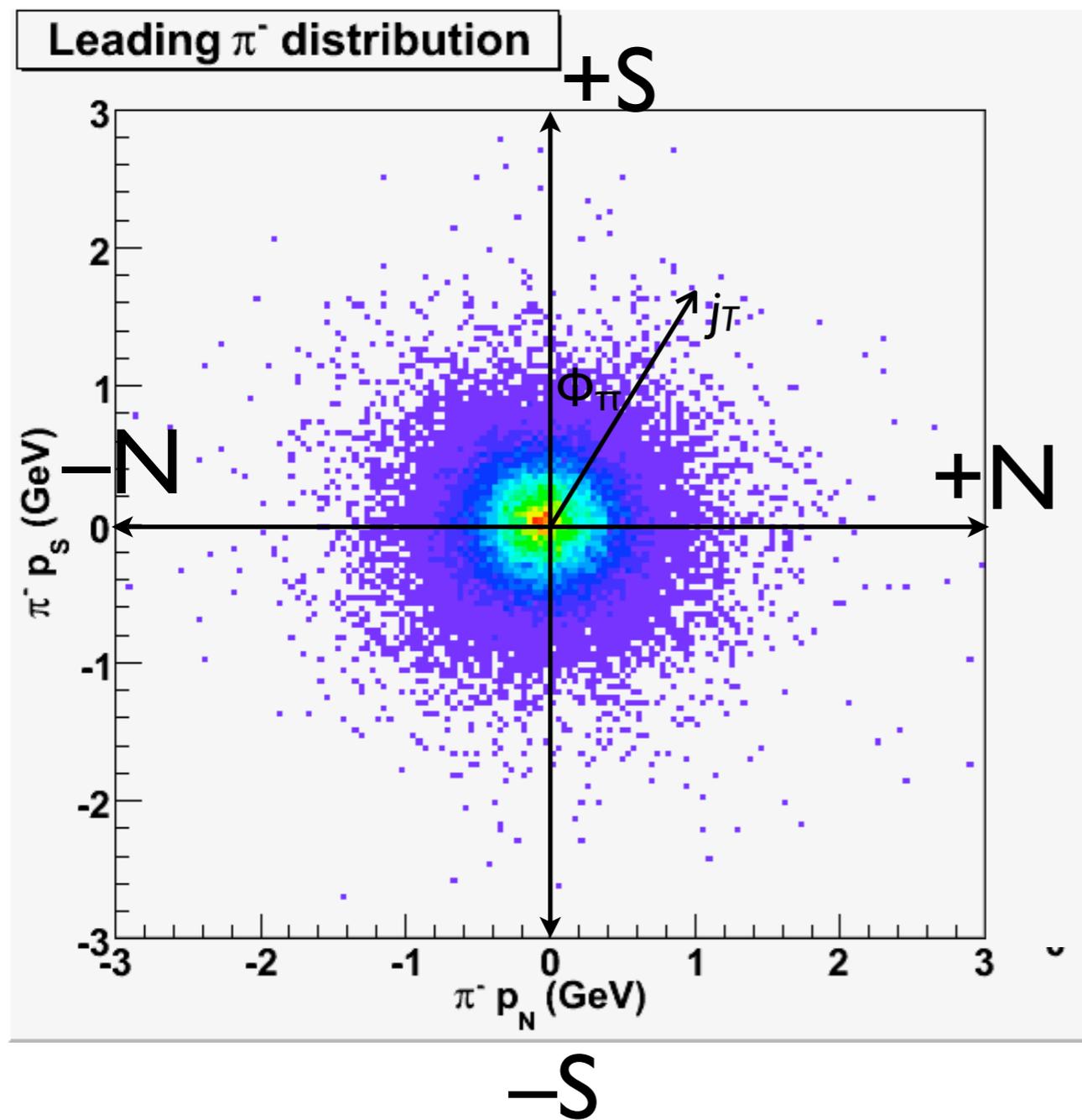
$\Phi_{\pi}$  is defined in NLS coordinates



( $L$  is 3rd axis;  $L = S \times N$ )

# The Collins Asymmetry

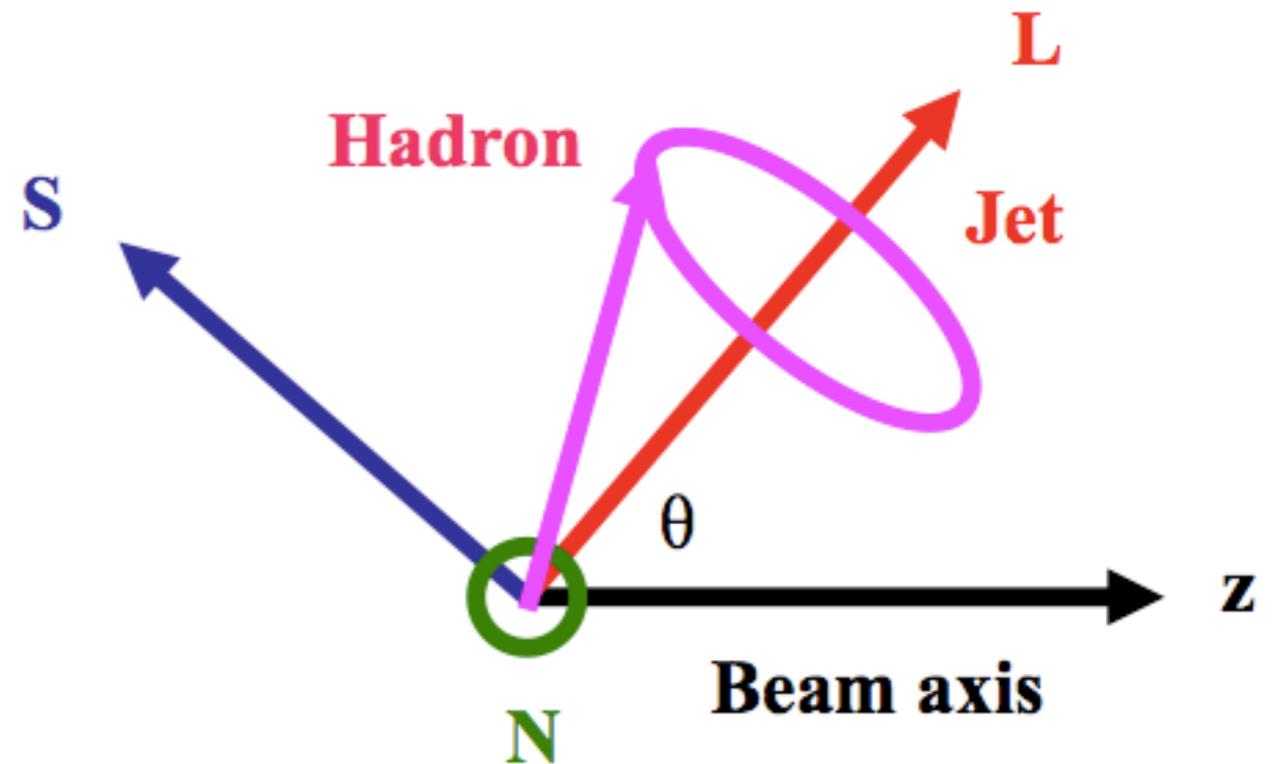
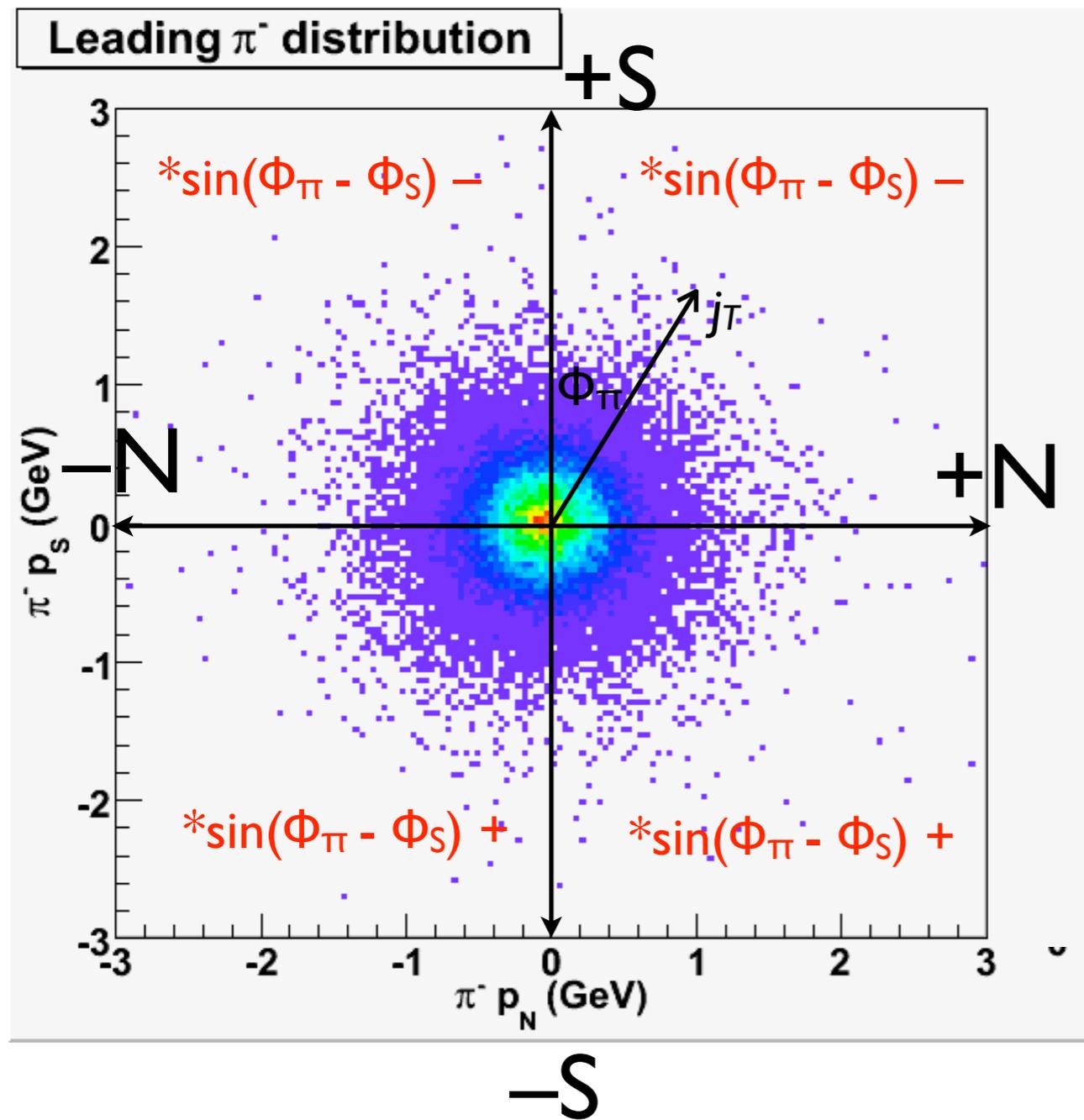
$\Phi_{\pi}$  is defined in NLS coordinates



(L is 3rd axis;  $L = S \times N$ )

# The Collins Asymmetry

$\Phi_{\pi}$  is defined in NLS coordinates

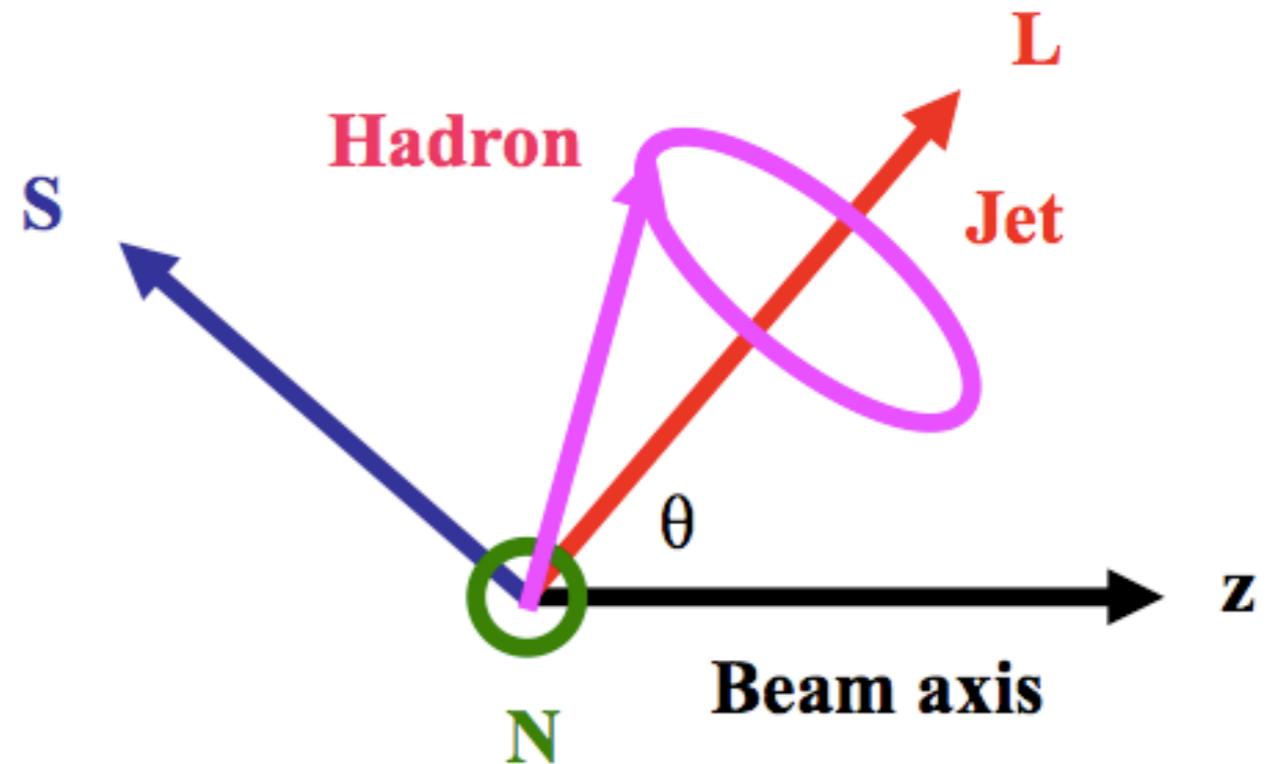
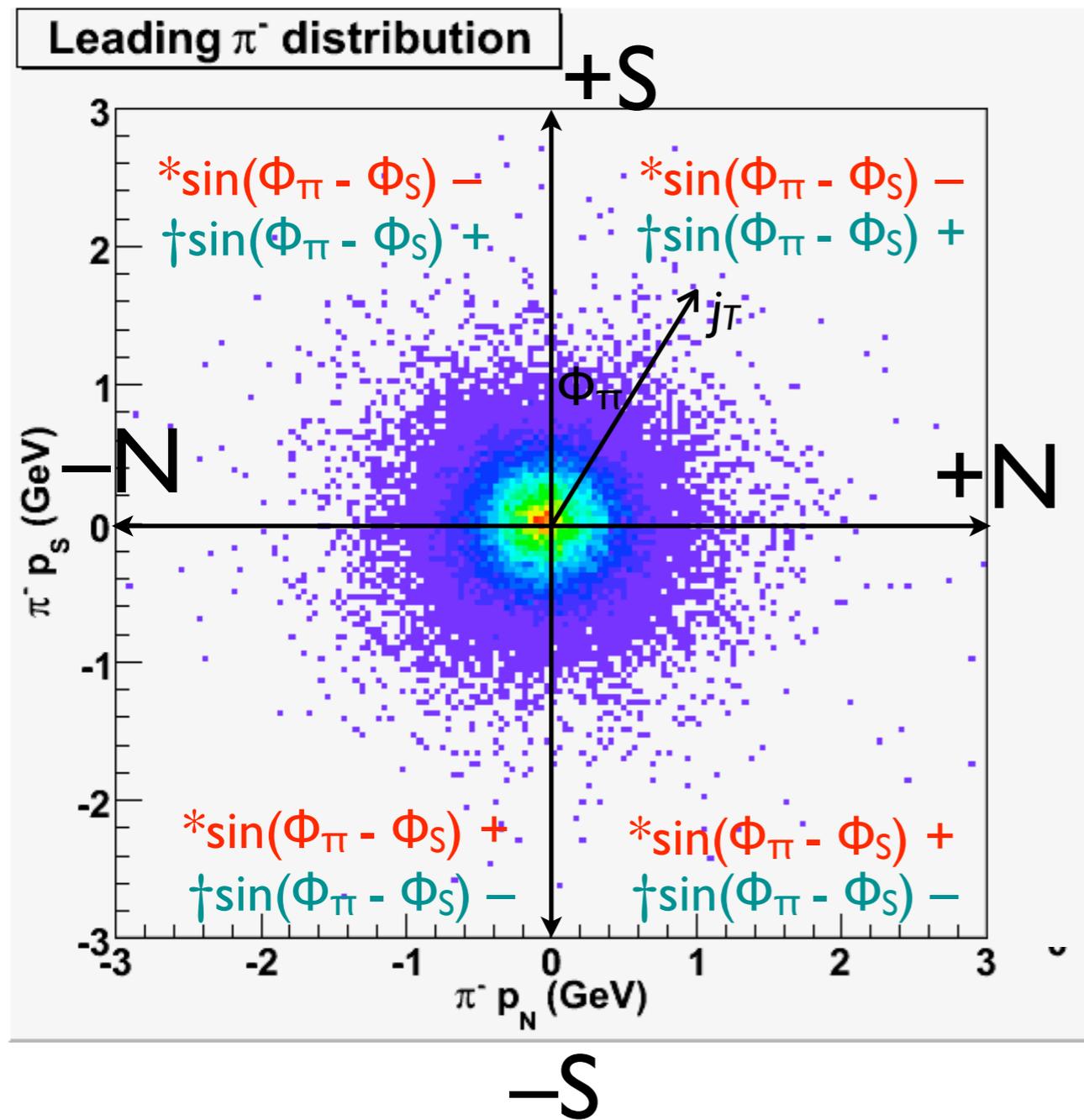


\*For proton spin  $\uparrow \uparrow$  N axis,  
 $\Phi_S = 90^\circ$

(L is 3rd axis;  $L = S \times N$ )

# The Collins Asymmetry

$\Phi_{\pi}$  is defined in NLS coordinates

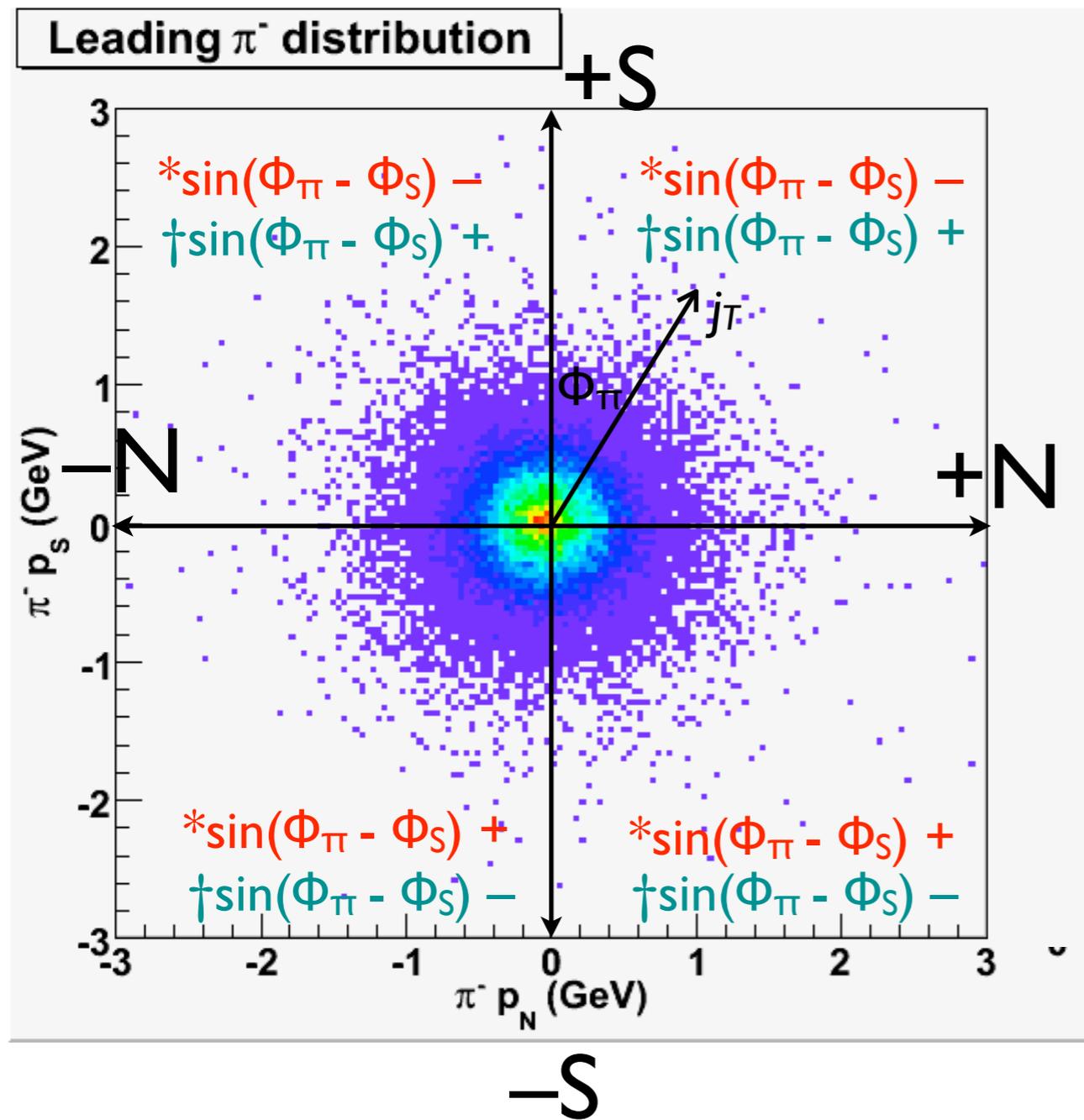


- \*For proton spin  $\uparrow \uparrow$  N axis,  
 $\Phi_S = 90^\circ$
- †For proton spin  $\uparrow \downarrow$  N axis,  
 $\Phi_S = -90^\circ$

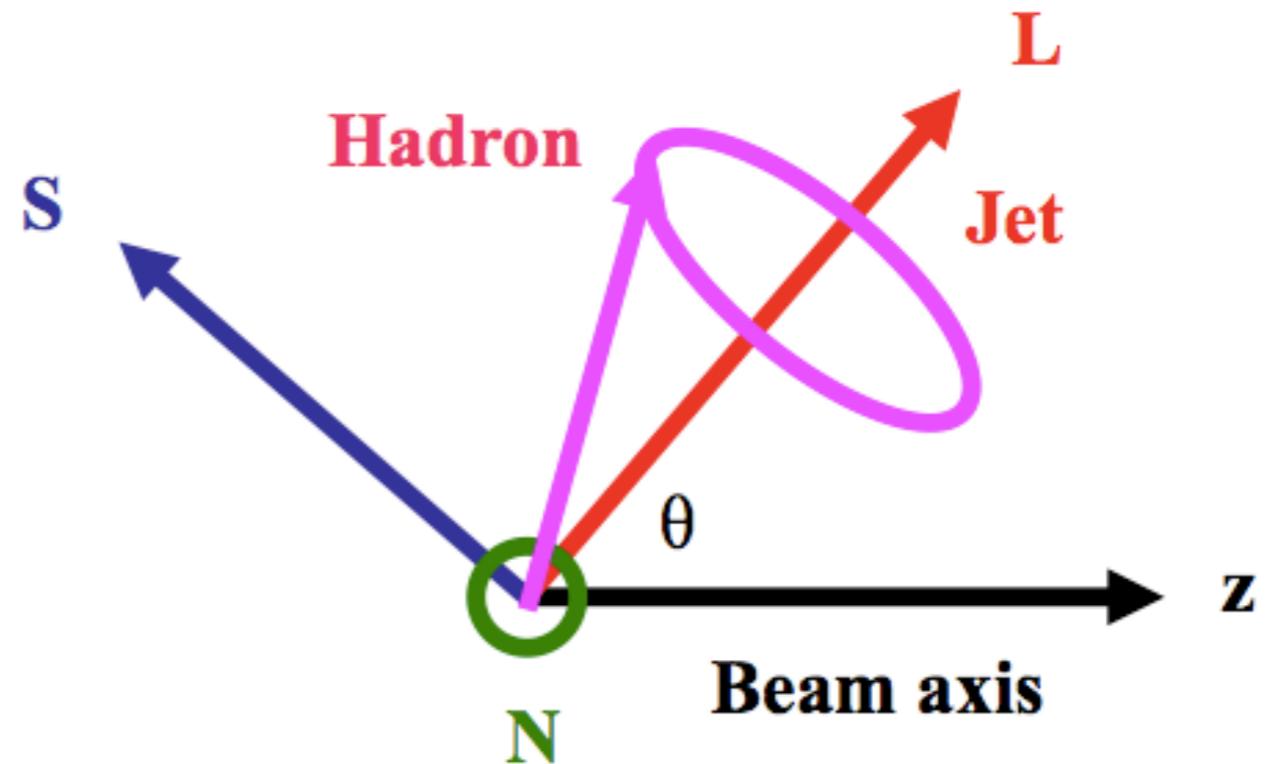
(L is 3rd axis;  $L = S \times N$ )

# The Collins Asymmetry

$\Phi_{\pi}$  is defined in NLS coordinates



(L is 3rd axis;  $L = S \times N$ )

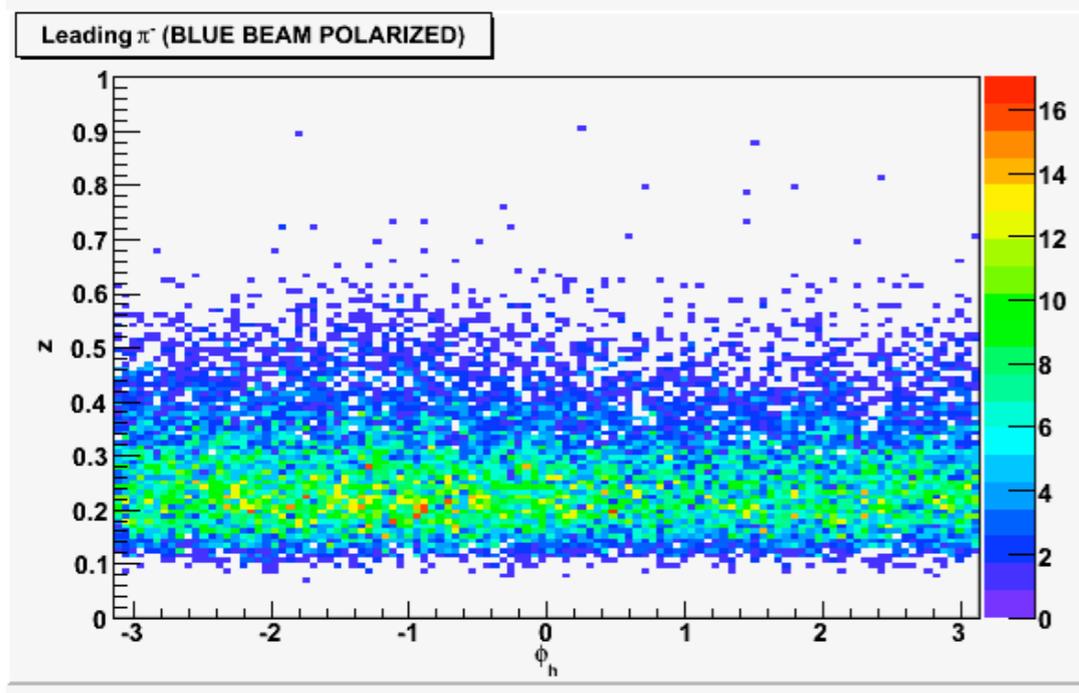
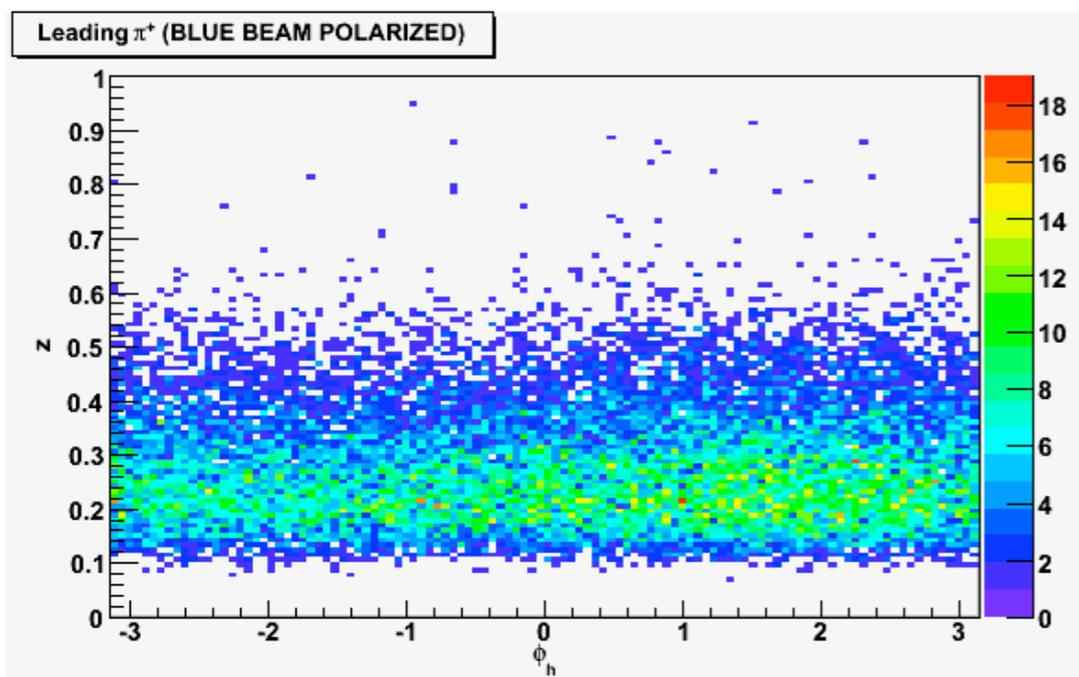


- \*For proton spin  $\uparrow \uparrow$  N axis,  
 $\Phi_S = 90^\circ$
- †For proton spin  $\uparrow \downarrow$  N axis,  
 $\Phi_S = -90^\circ$

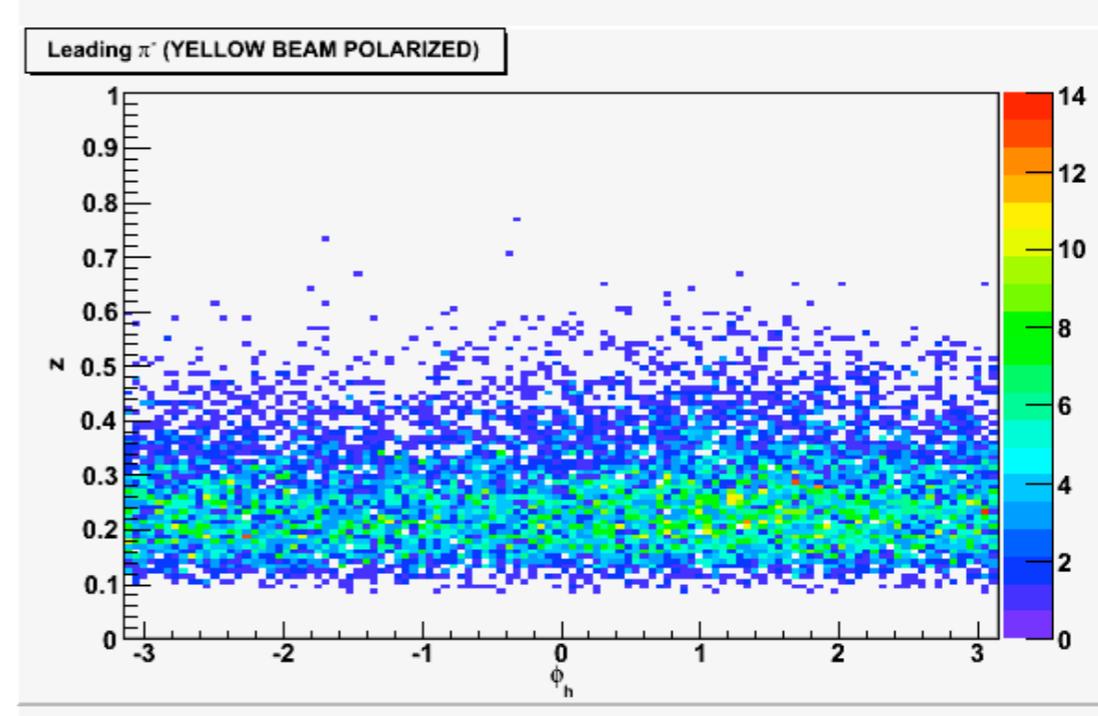
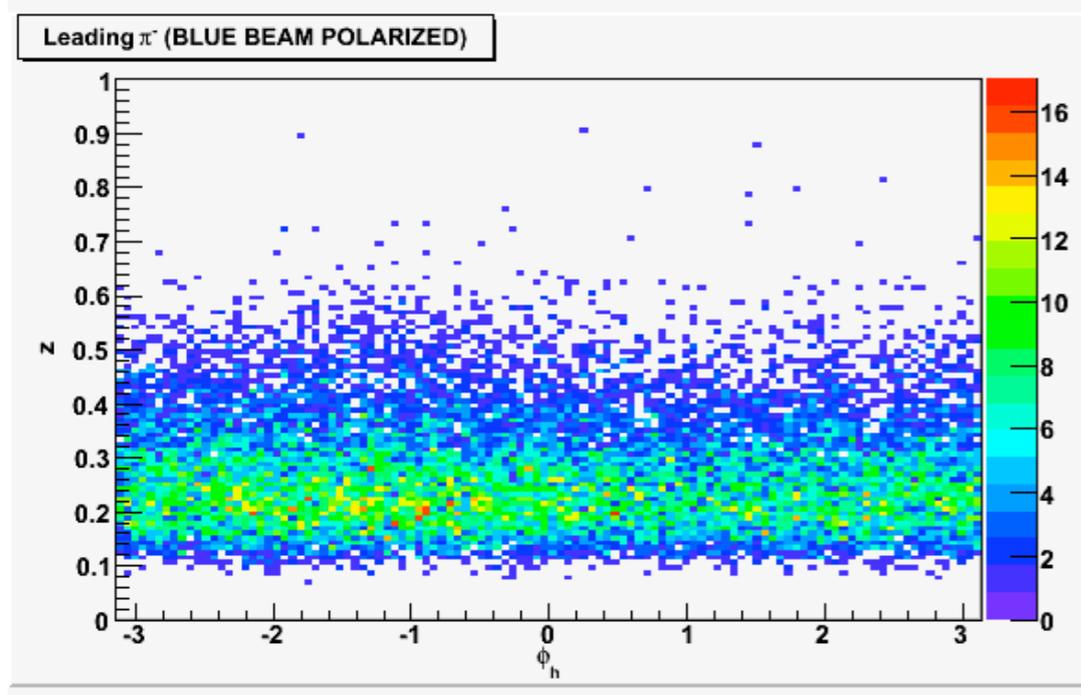
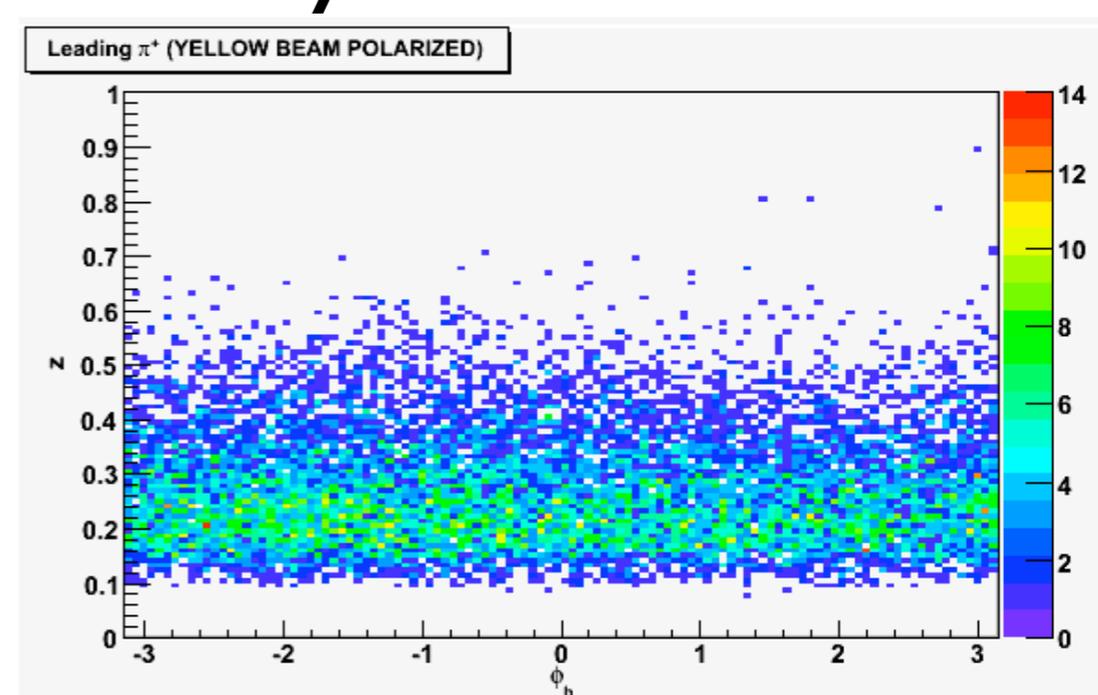
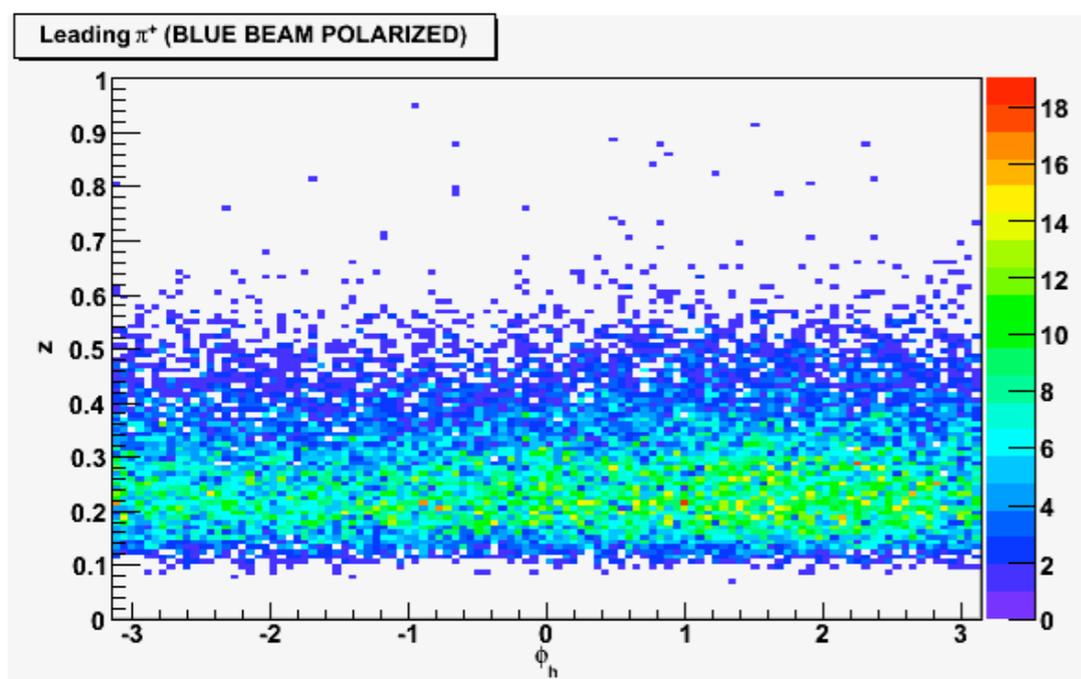
Geometry dictates these cancel along the N-axis; leaving a possible top-bottom asymmetry A along the S-axis

Data analyzed separately for **blue** and **yellow** beams in forward hemisphere only:

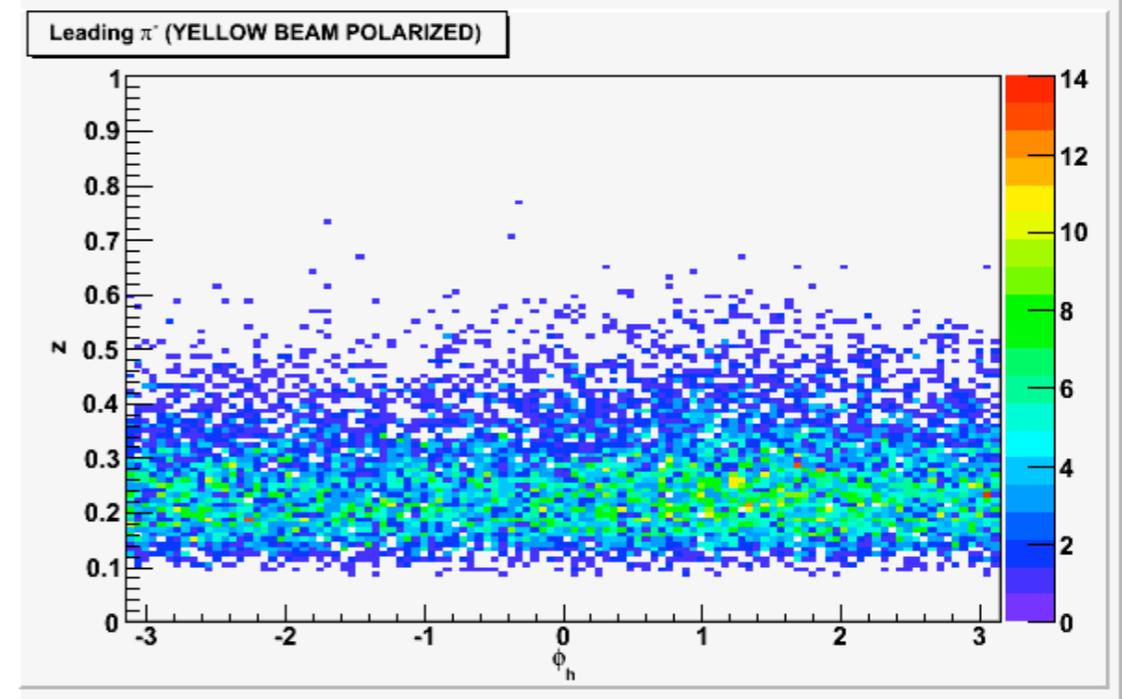
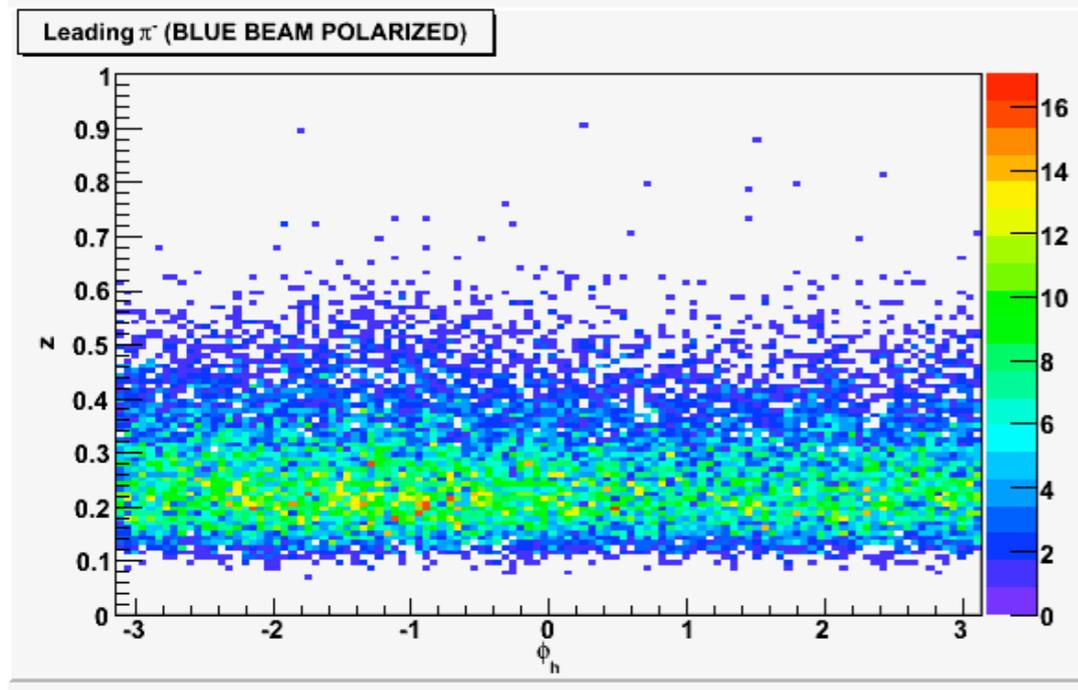
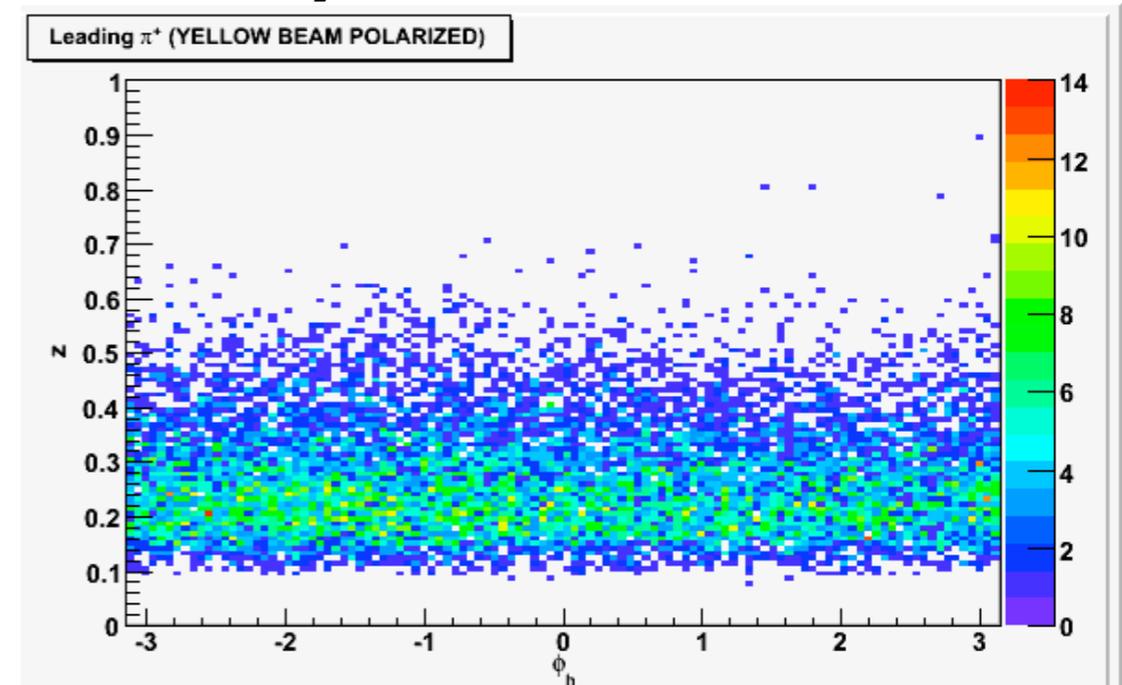
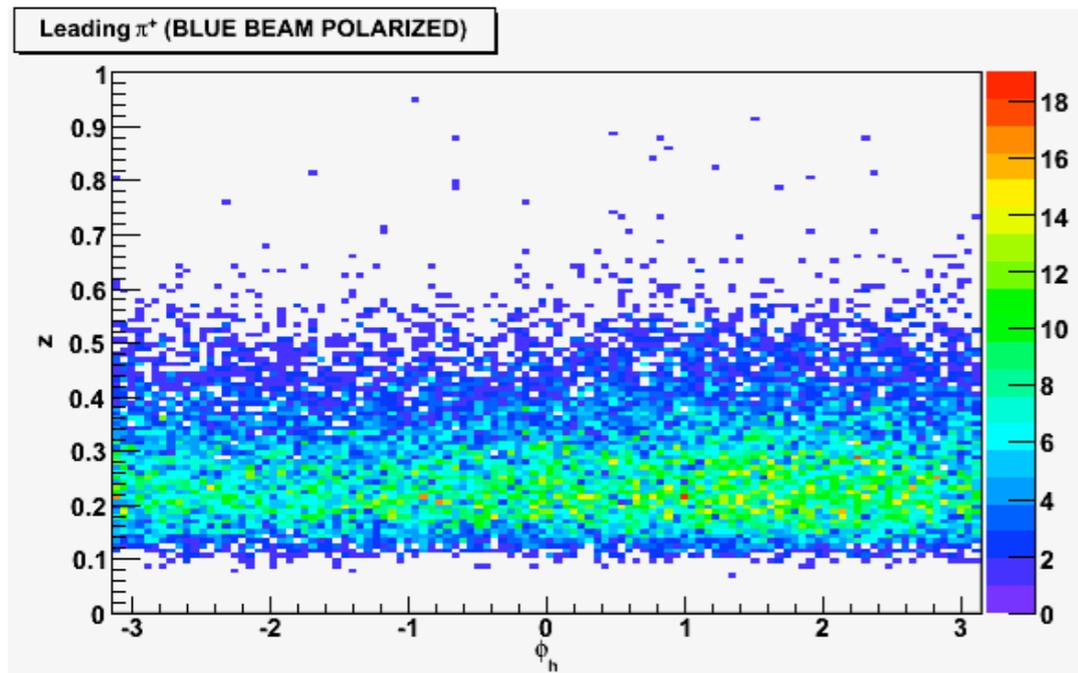
# Data analyzed separately for blue and yellow beams in forward hemisphere only:



# Data analyzed separately for blue and yellow beams in forward hemisphere only:



# Data analyzed separately for blue and yellow beams in forward hemisphere only:

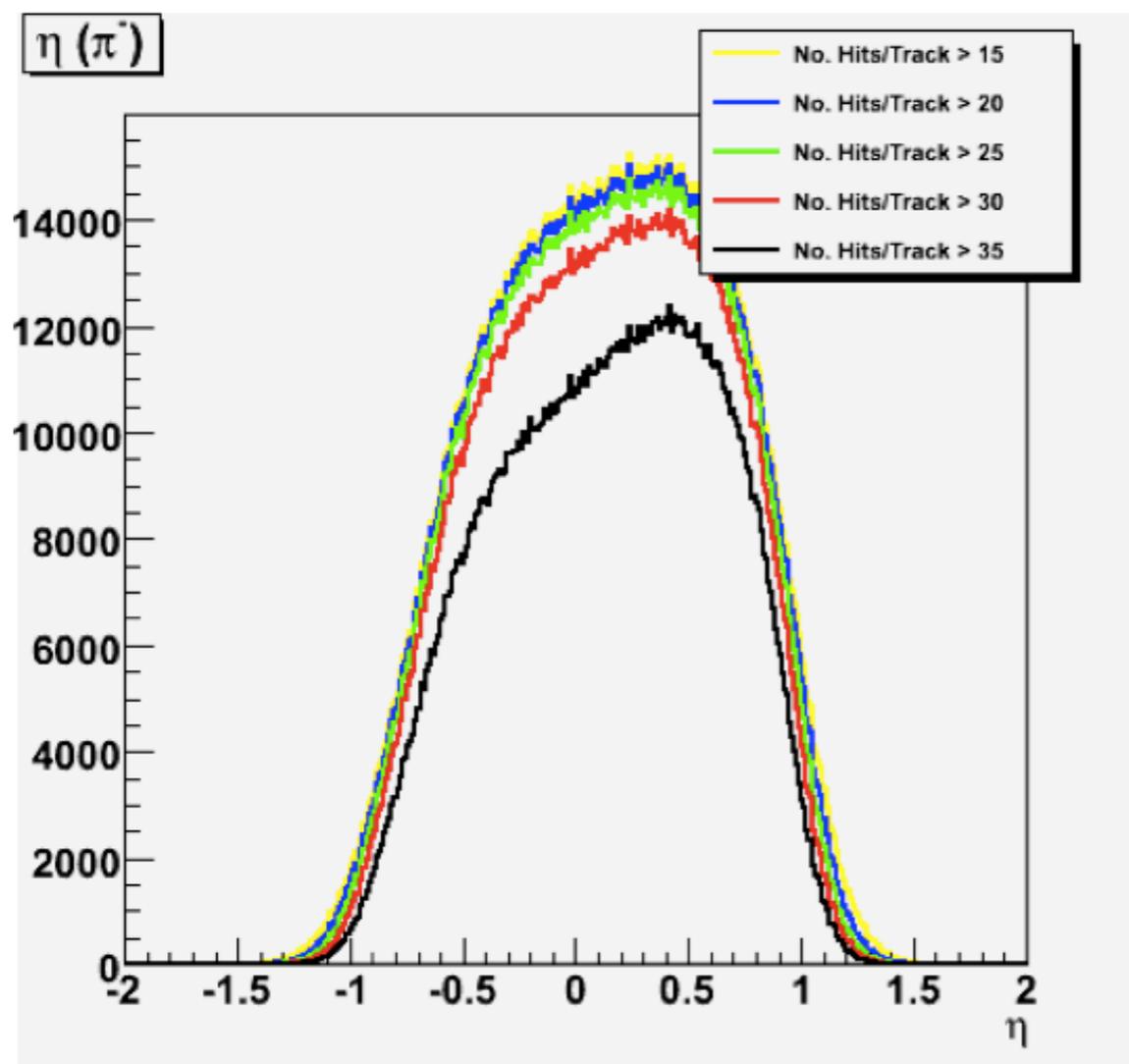


\* Asymmetric distributions shown here are NOT a result of the Collins Asymmetry, they are a relic of track curvatures between TPC sectors; they are opposite for blue, yellow beam measurements & are symmetric with respect to the S-axis

# Goals of this Presentation:

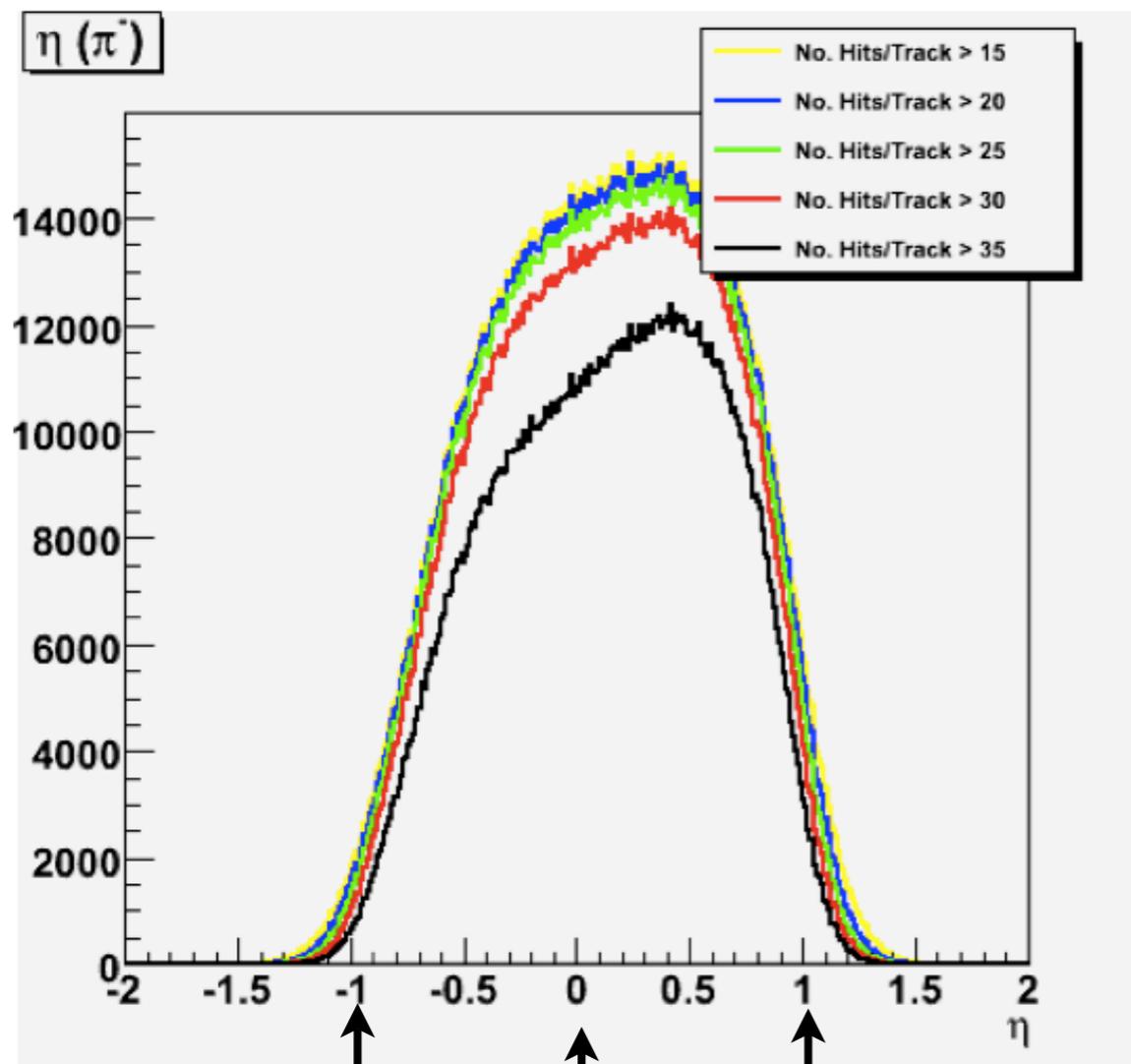
- Demonstrate kinematic coverage of the data and physics in terms of  $p_T$

# Charged $\pi^\pm$ reconstruction



# Charged $\pi^\pm$ reconstruction

# Charged $\pi^\pm$ reconstruction

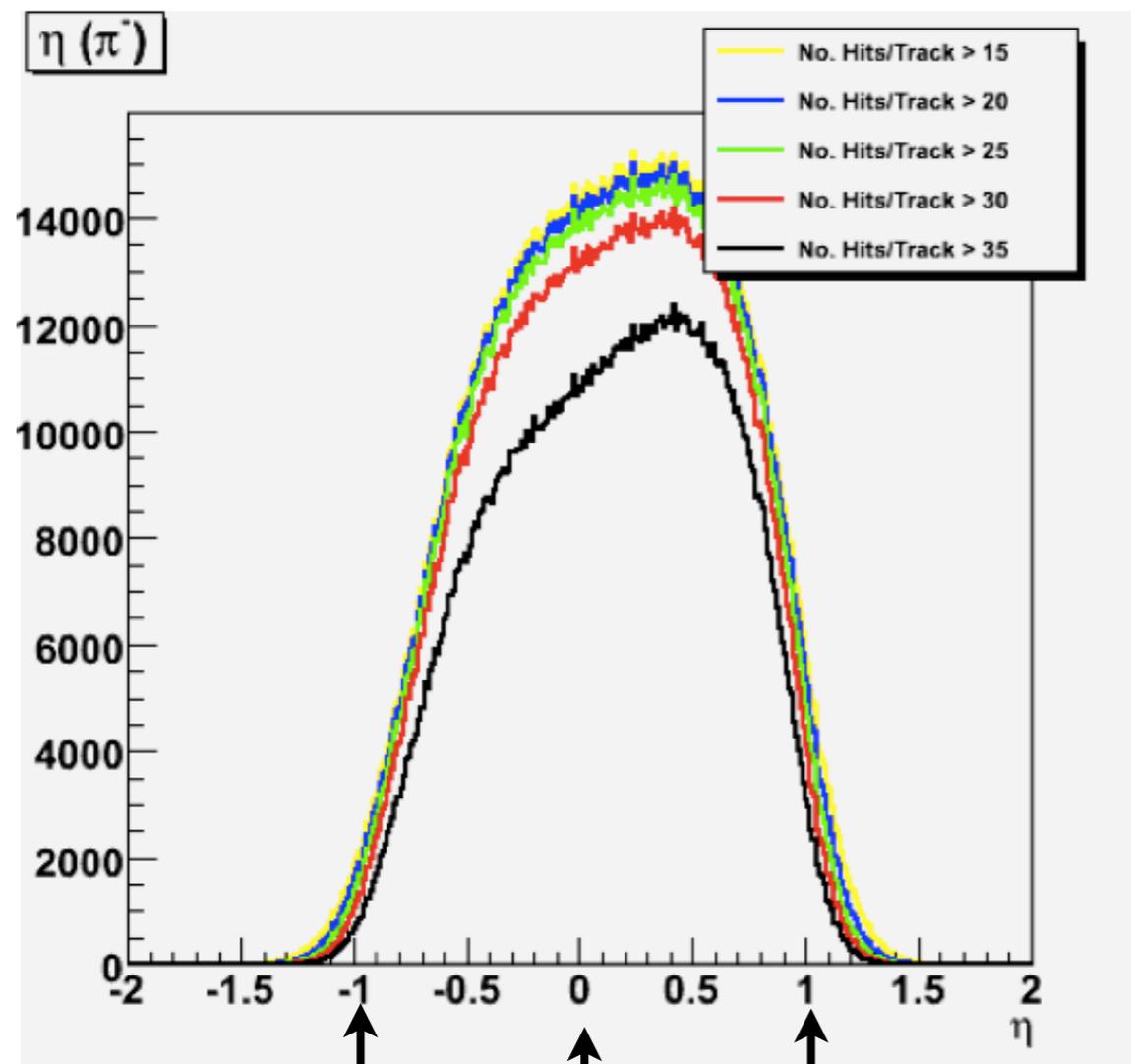


backward  
BEMC, TPC  
edge

$90^\circ$

forward  
BEMC, TPC  
edge

# Charged $\pi^\pm$ reconstruction



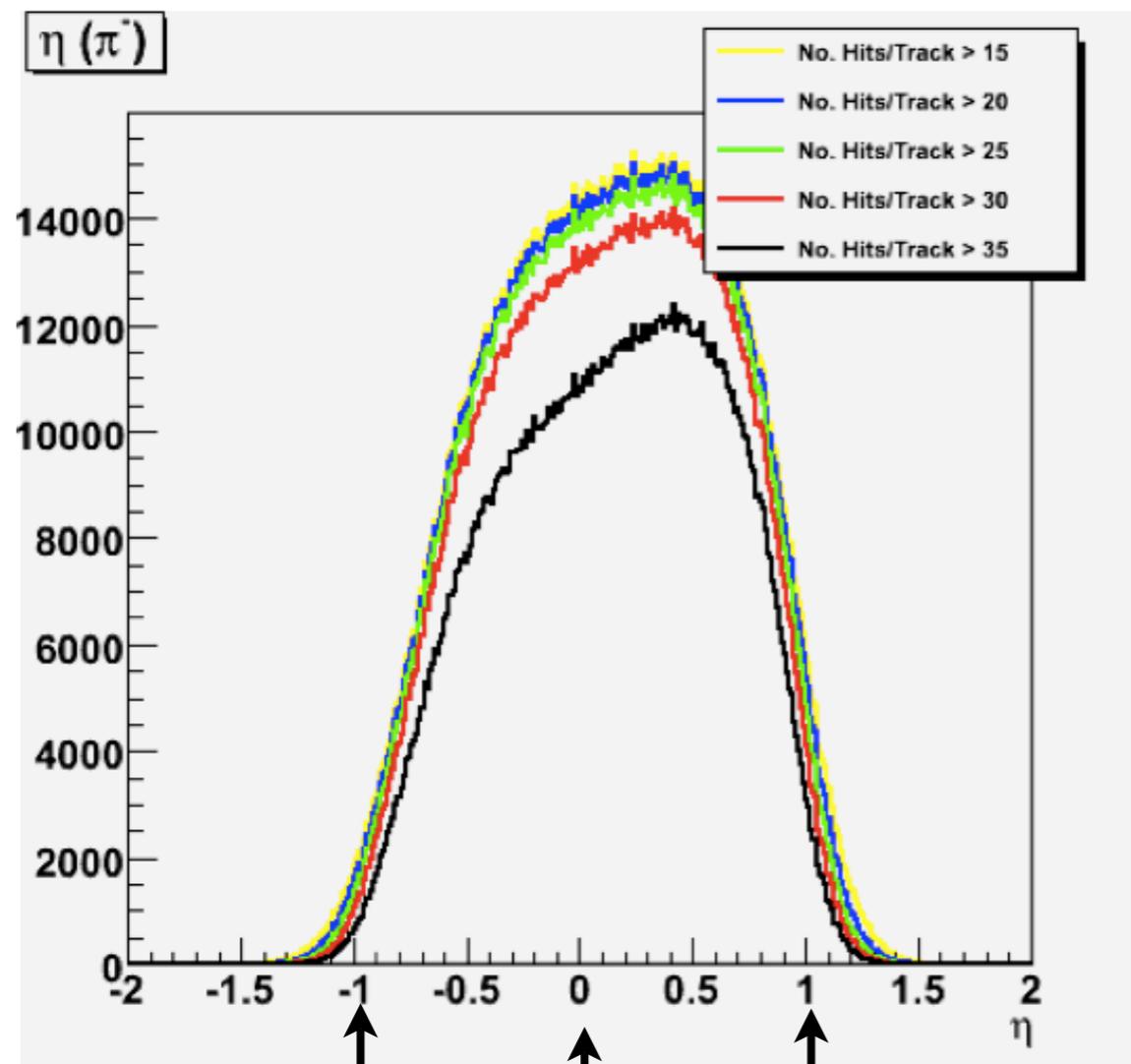
backward  
BEMC, TPC  
edge

$90^\circ$

forward  
BEMC, TPC  
edge

**Determined by  
momentum and  $dE/dx$  in  
the TPC ( $\geq 25$  fit points  
required)**

# Charged $\pi^\pm$ reconstruction



backward  
BEMC, TPC  
edge

$90^\circ$

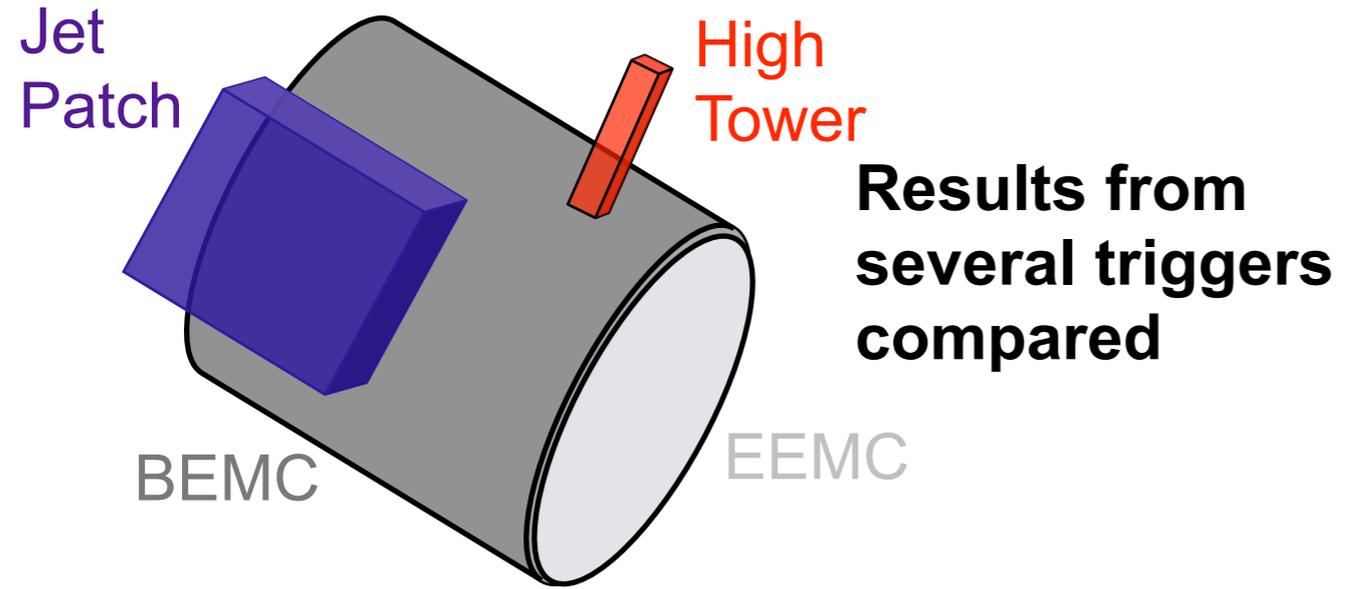
forward  
BEMC, TPC  
edge

**Determined by  
momentum and  $dE/dx$  in  
the TPC ( $\geq 25$  fit points  
required)**

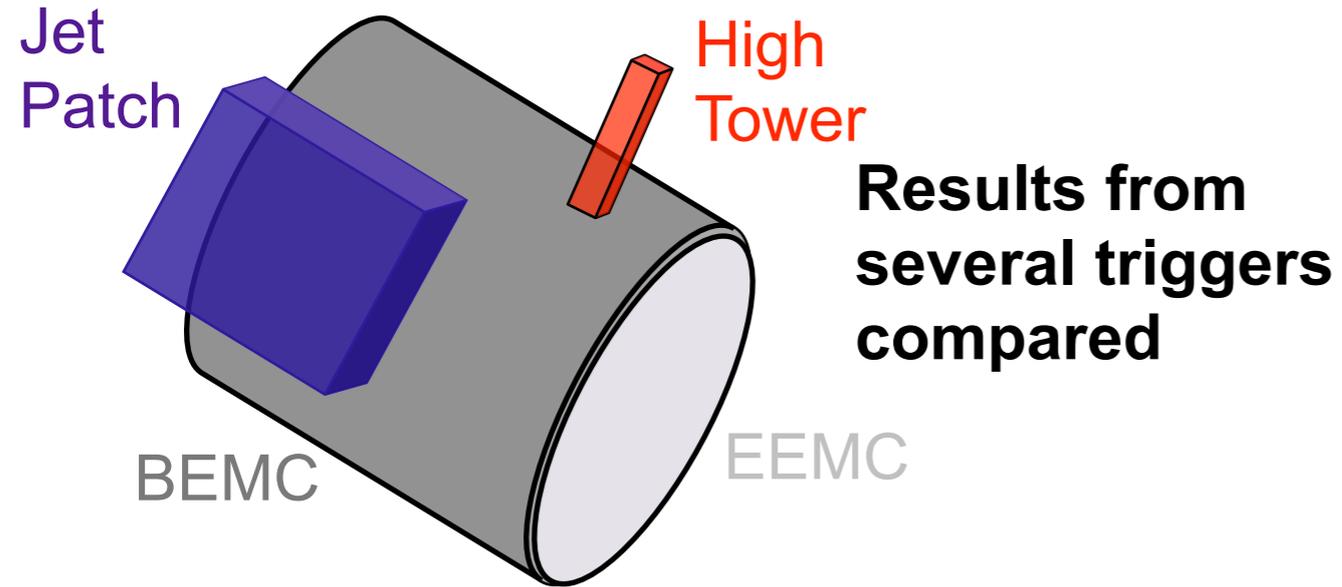
**Only *Leading* pions (highest  
momentum fraction  $z$ ) are  
kept**

# Jet reconstruction

# Jet reconstruction



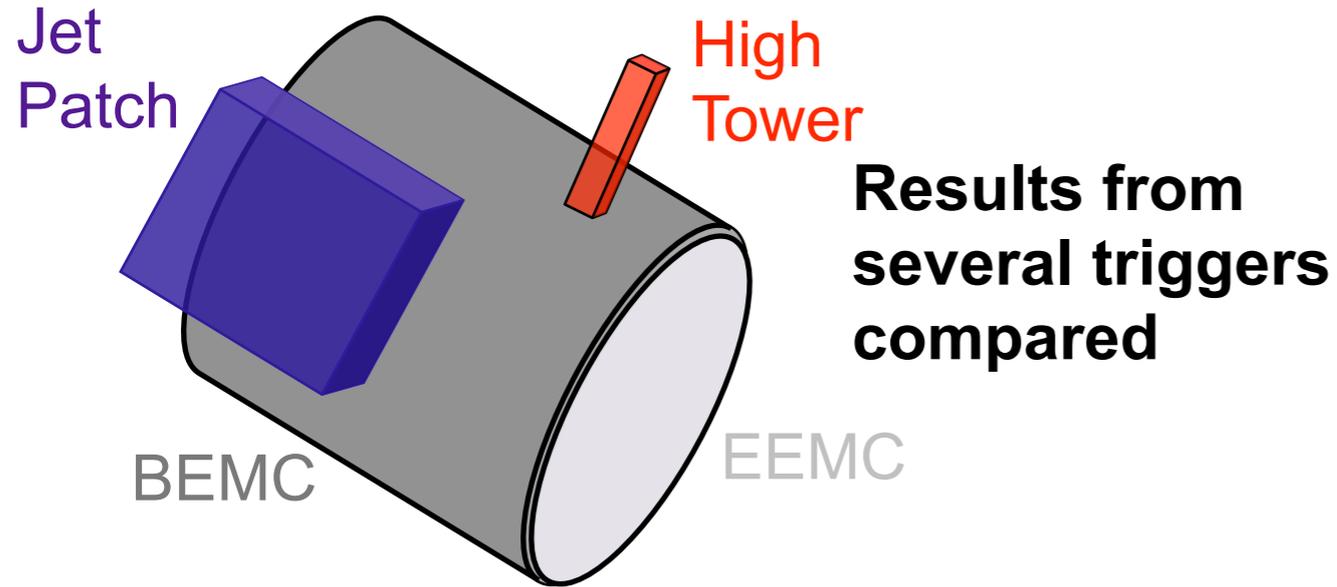
# Jet reconstruction



## Jet Patch trigger:

Requires sum of 400 localized "patches" above a threshold as a cluster for soft fragmentation (total coverage  $\Delta\phi = \Delta\eta = 1$ )

# Jet reconstruction



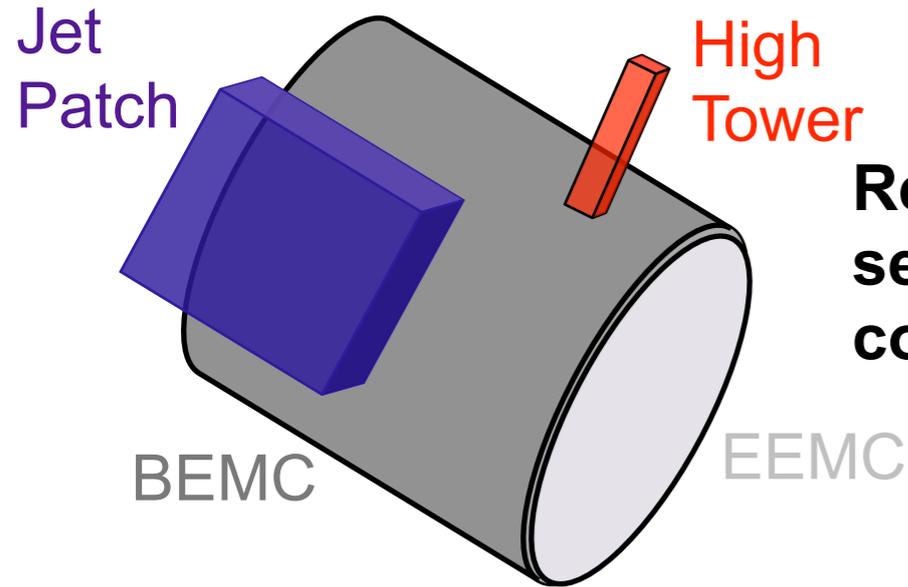
## Jet Patch trigger:

Requires sum of 400 localized “patches” above a threshold as a cluster for soft fragmentation (total coverage  $\Delta\Phi = \Delta\eta = 1$ )

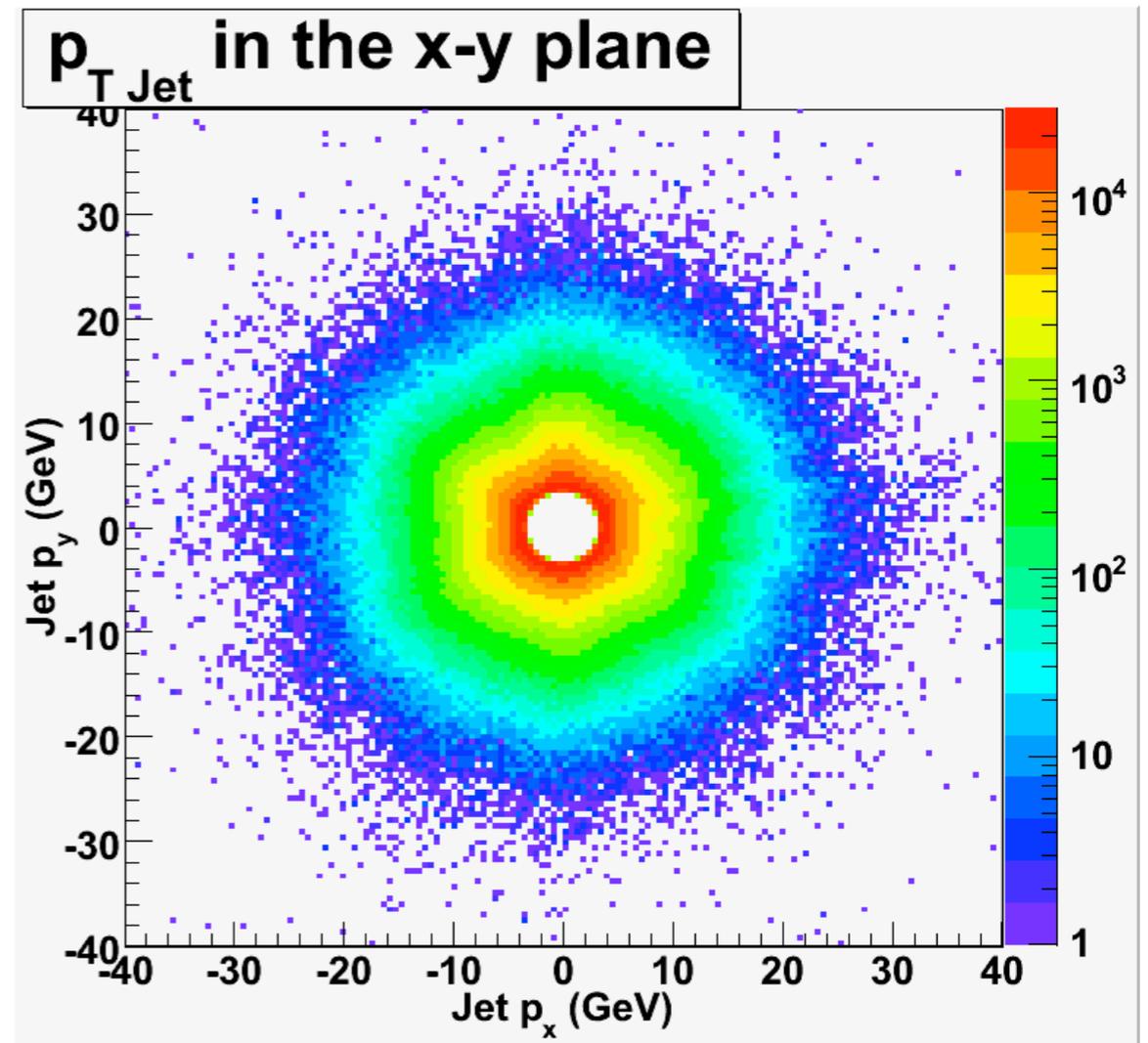
## High Tower trigger:

Uses a single ADC channel as a jet “seed” and totals energy in surrounding trigger “patch”

# Jet reconstruction



Results from  
several triggers  
compared



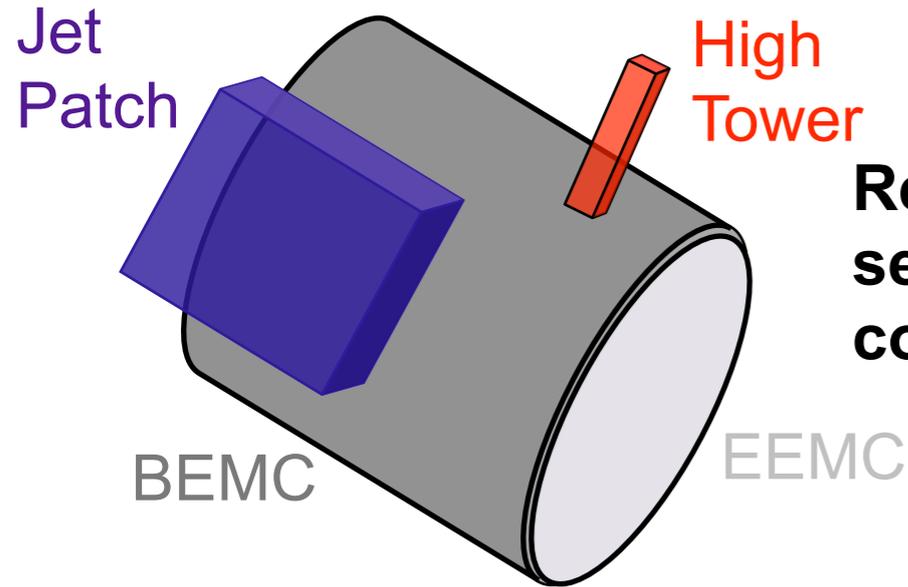
## Jet Patch trigger:

Requires sum of 400 localized "patches" above a threshold as a cluster for soft fragmentation (total coverage  $\Delta\phi = \Delta\eta = 1$ )

## High Tower trigger:

Uses a single ADC channel as a jet "seed" and totals energy in surrounding trigger "patch"

# Jet reconstruction



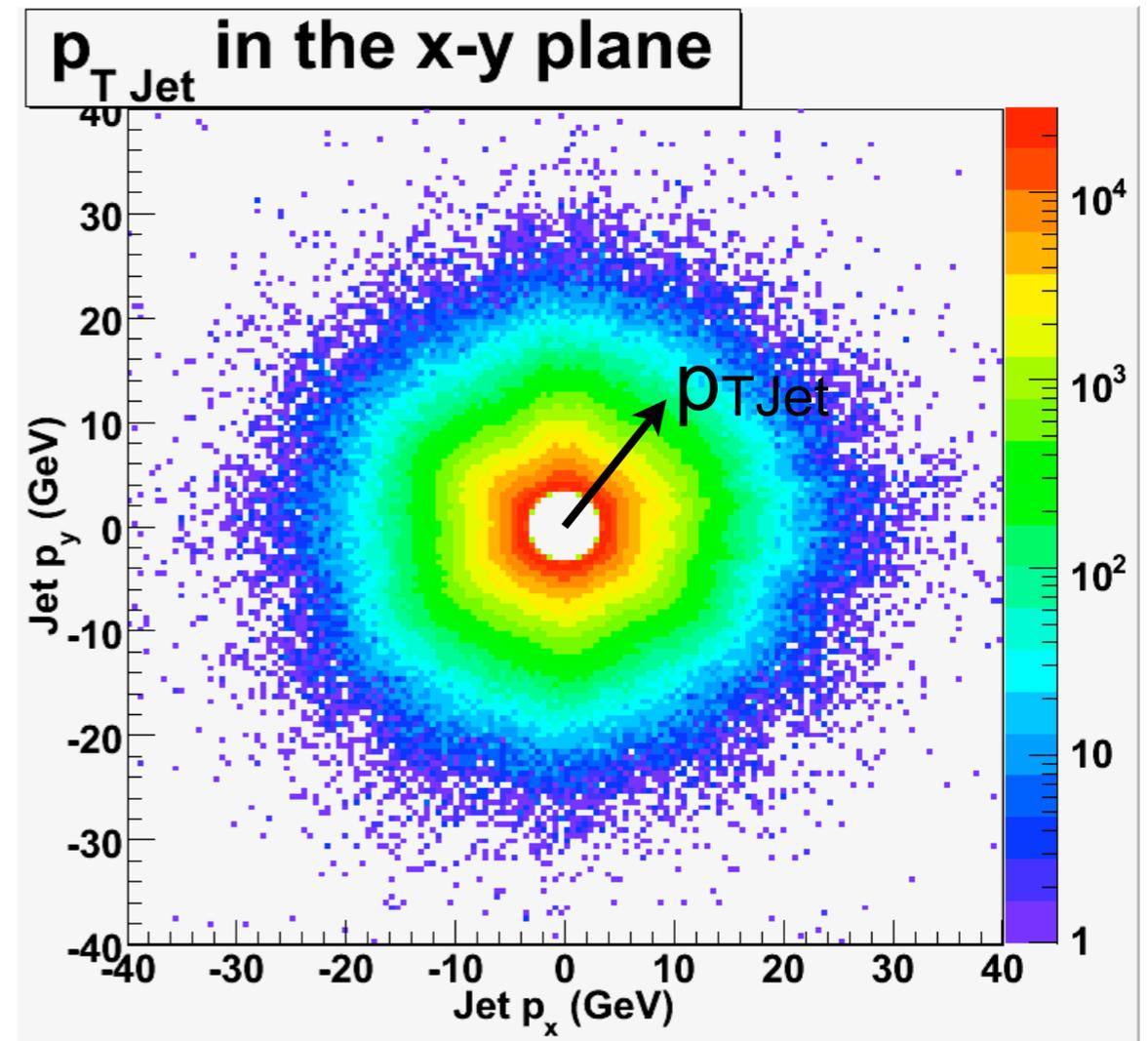
Results from several triggers compared

## Jet Patch trigger:

Requires sum of 400 localized “patches” above a threshold as a cluster for soft fragmentation (total coverage  $\Delta\Phi = \Delta\eta = 1$ )

## High Tower trigger:

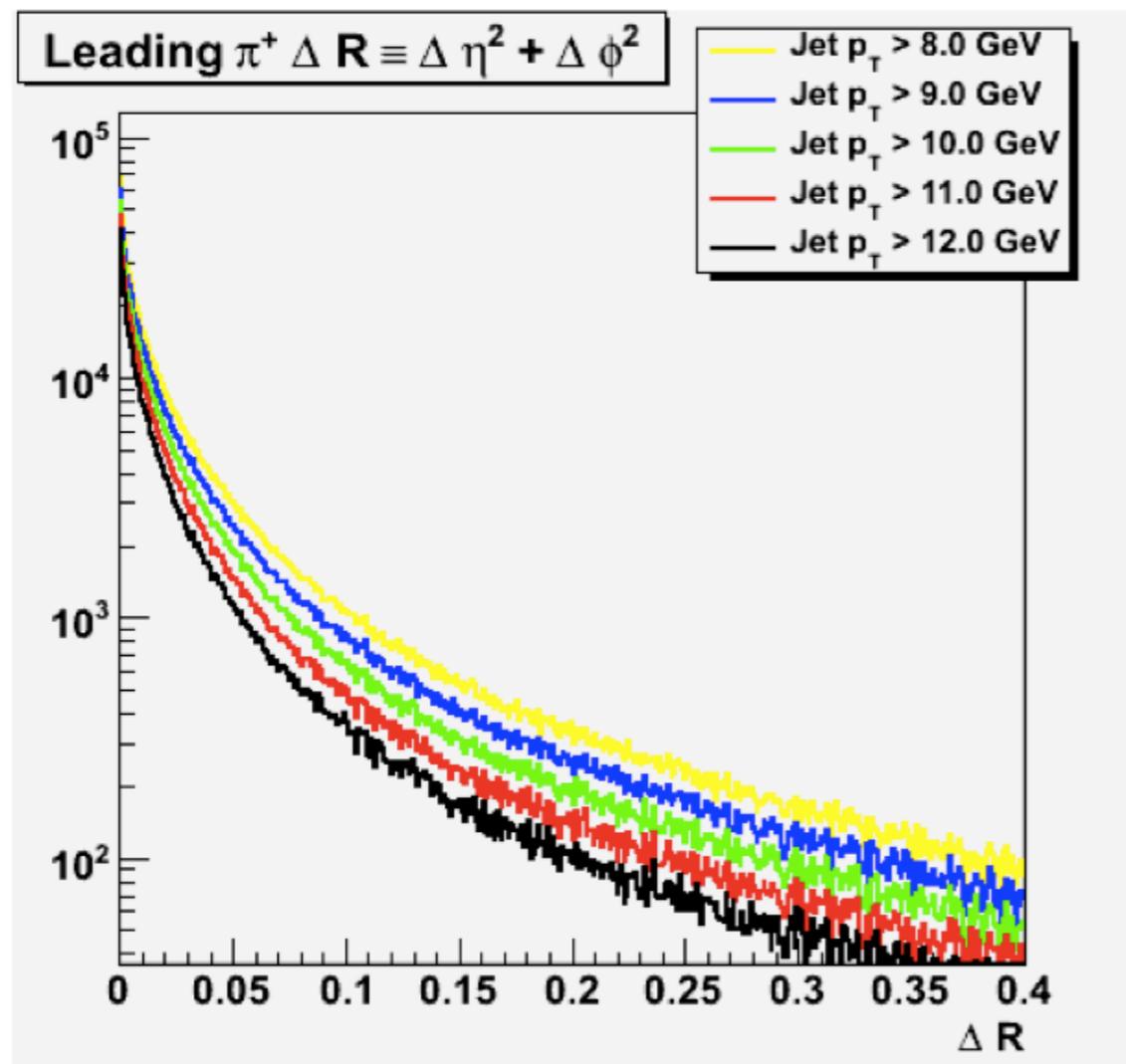
Uses a single ADC channel as a jet “seed” and totals energy in surrounding trigger “patch”



full azimuthal ( $\Phi$ ) coverage

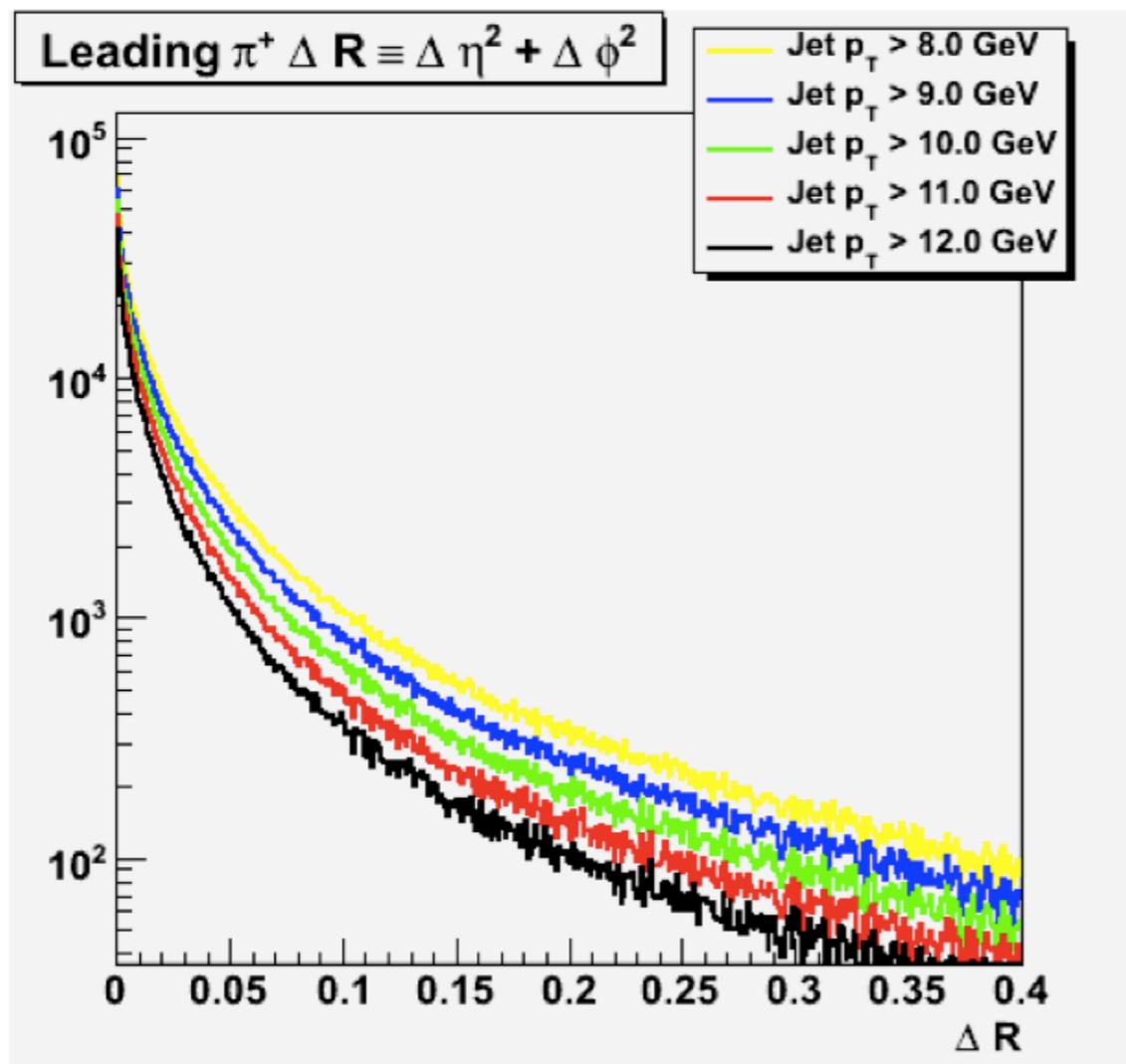
# Jet physics in terms of $p_T$

# Jet physics in terms of $p_T$



$\Delta R$  measures collimation  
of particles within jet

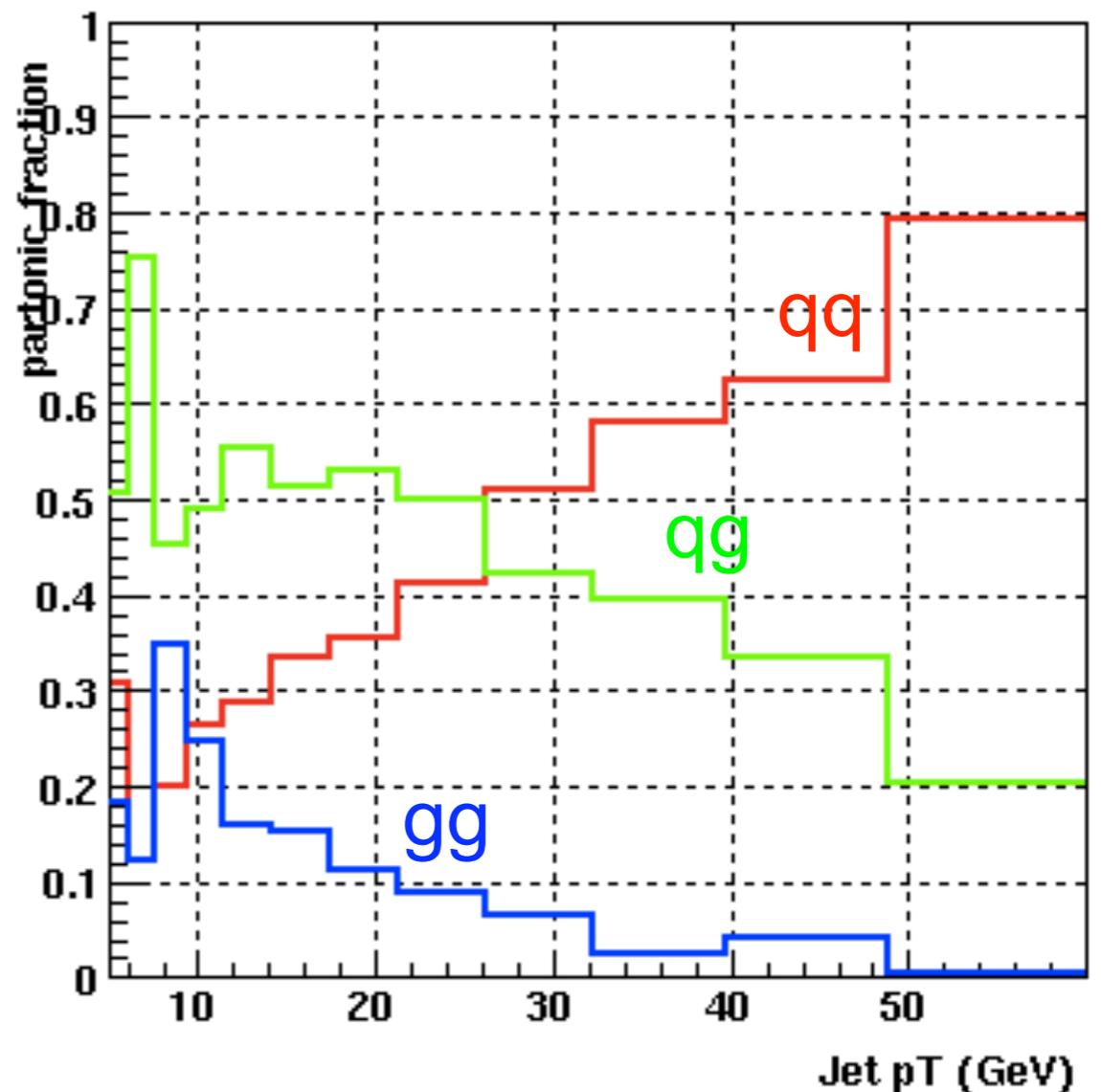
# Jet physics in terms of $p_T$



$\Delta R$  measures collimation of particles within jet

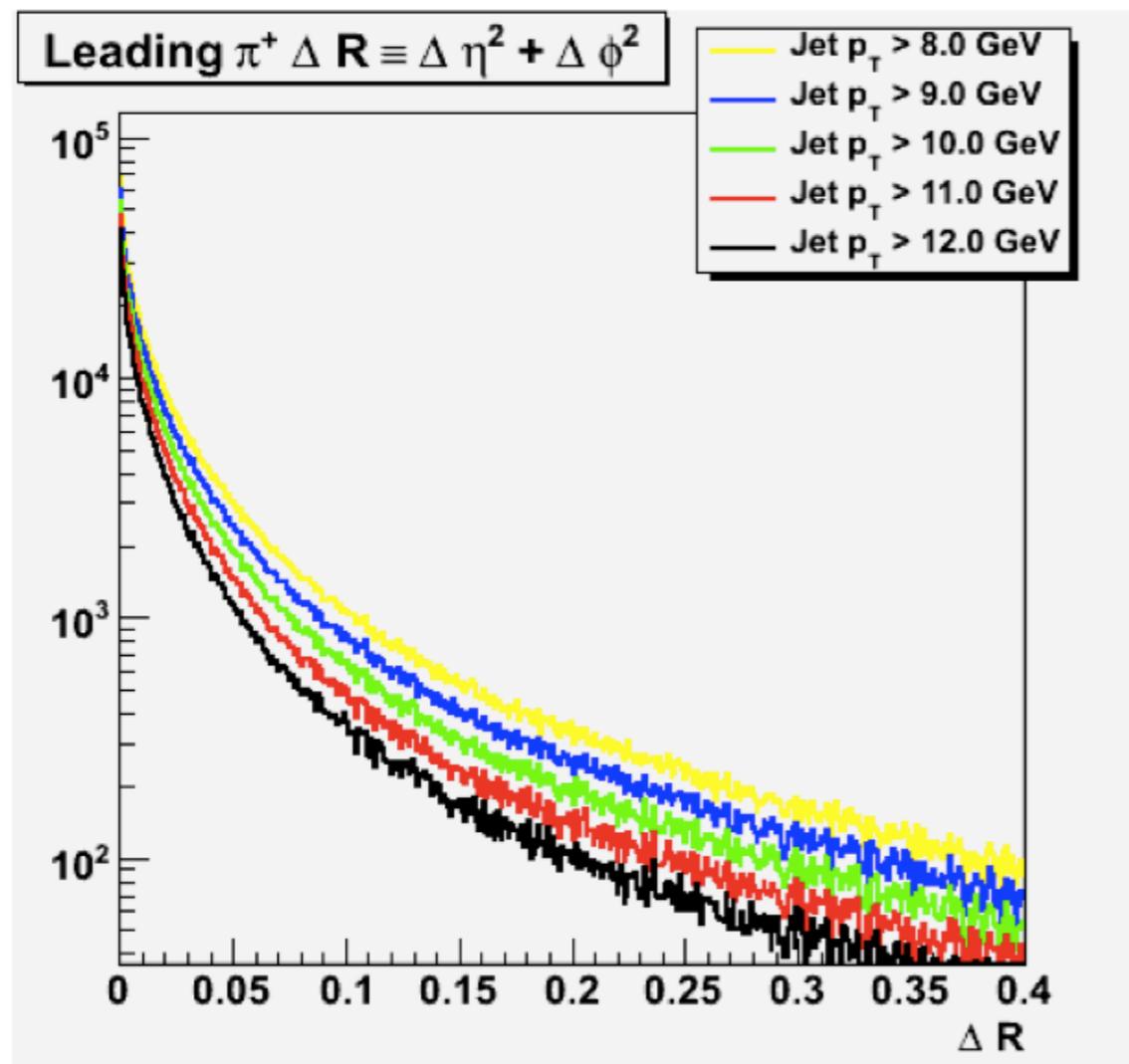
Lower  $p_T$  cut is a tradeoff between statistics and gluon event contamination:

BJP1 -127221



STAR simulation (PYTHIA + GEANT) at  $\sqrt{s} = 200$  GeV

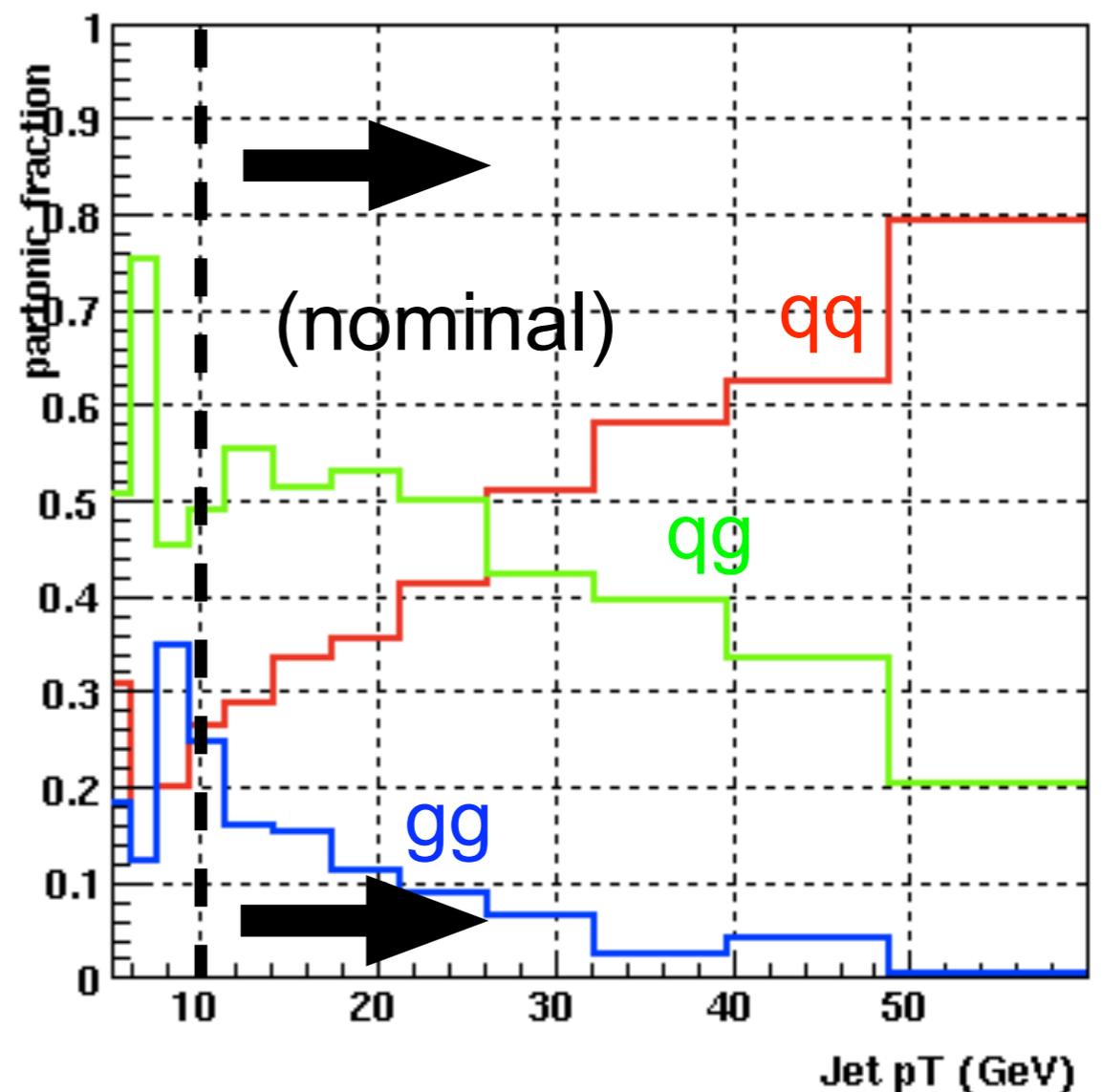
# Jet physics in terms of $p_T$



$\Delta R$  measures collimation of particles within jet

Lower  $p_T$  cut is a tradeoff between statistics and gluon event contamination:

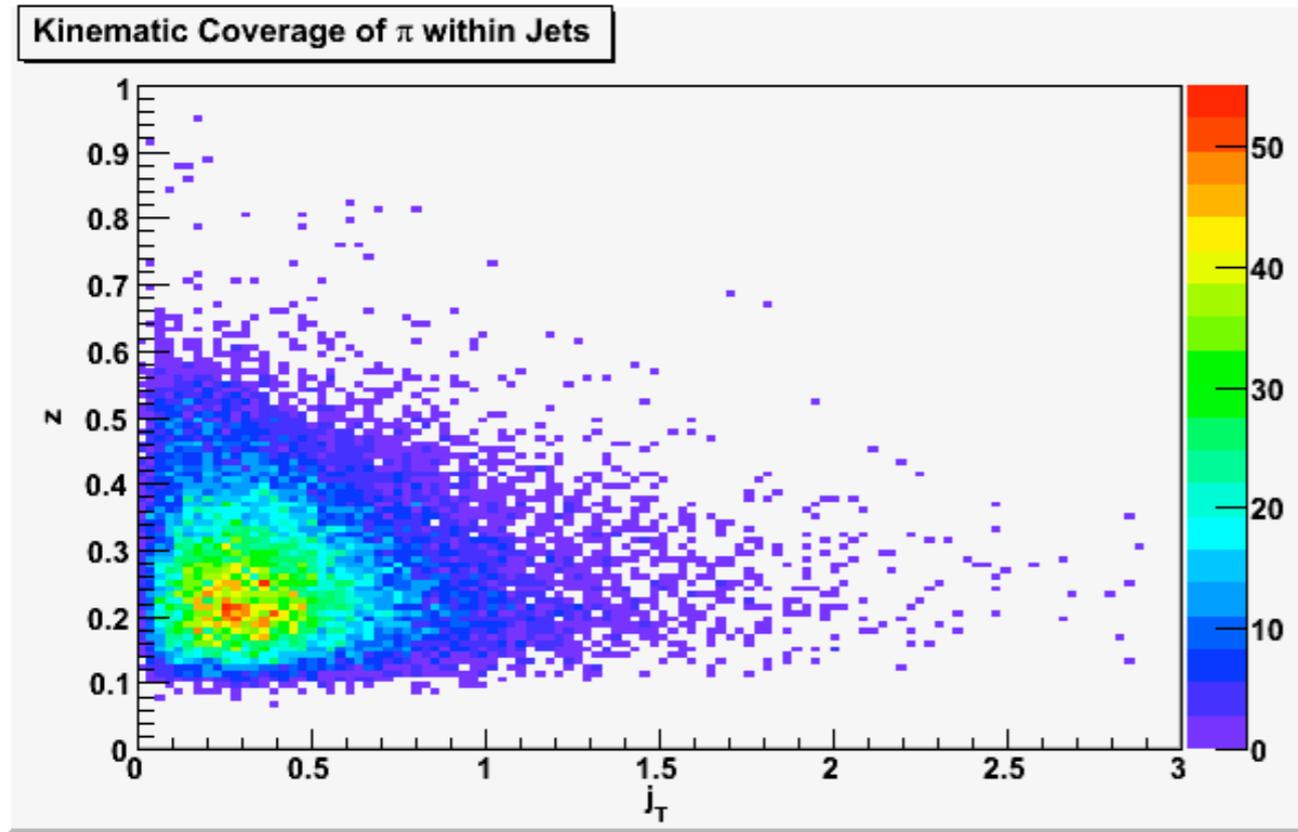
BJP1 -127221



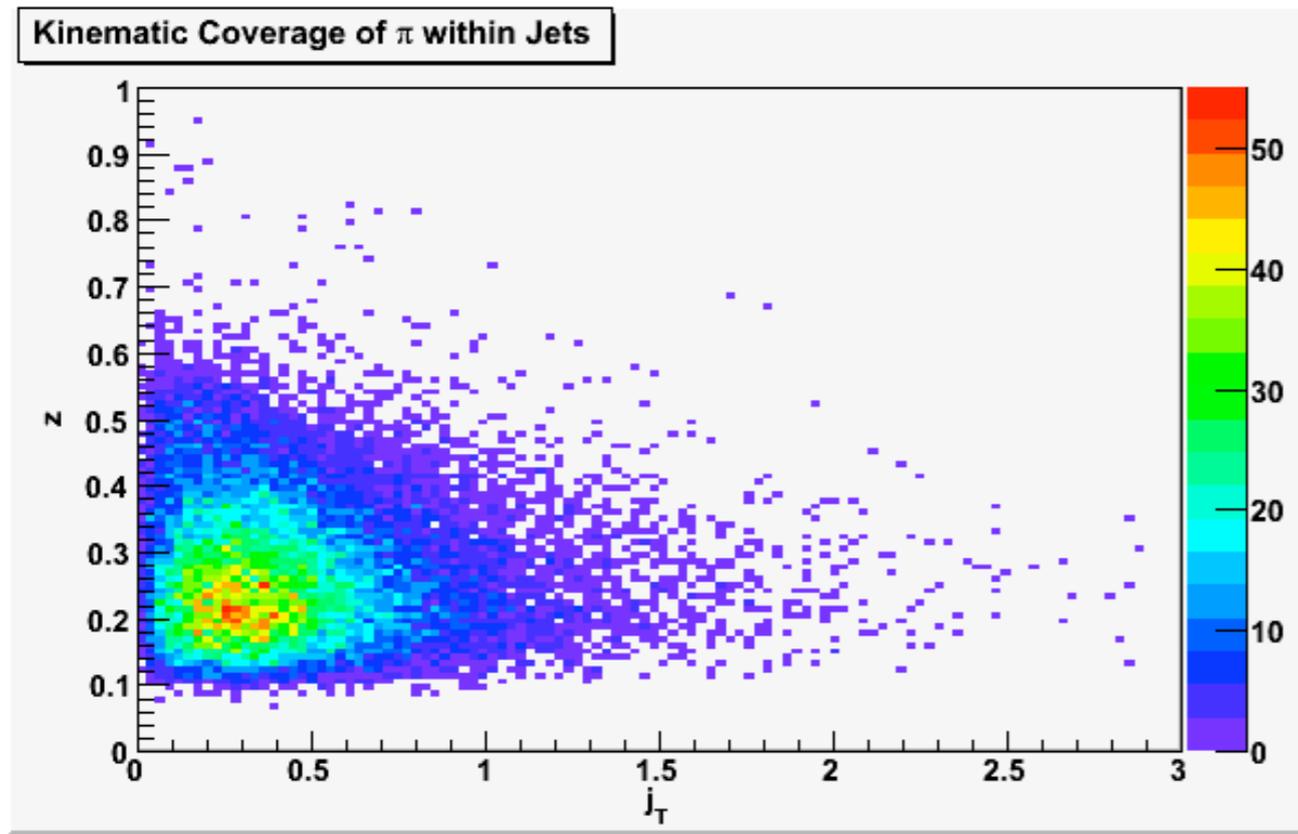
STAR simulation (PYTHIA + GEANT) at  $\sqrt{s} = 200$  GeV



# Data separated by $z$ and $j_T$ ;

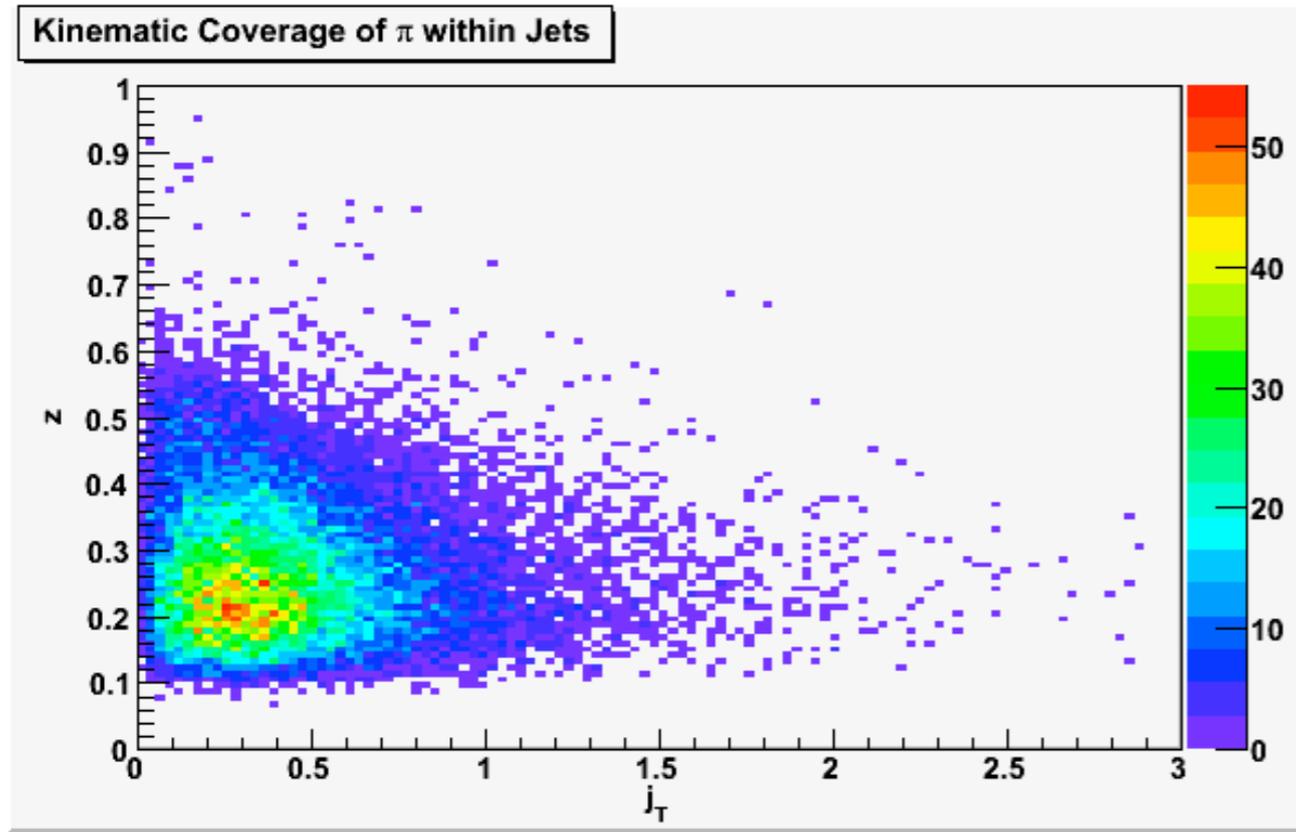


# Data separated by $z$ and $j_T$ ;

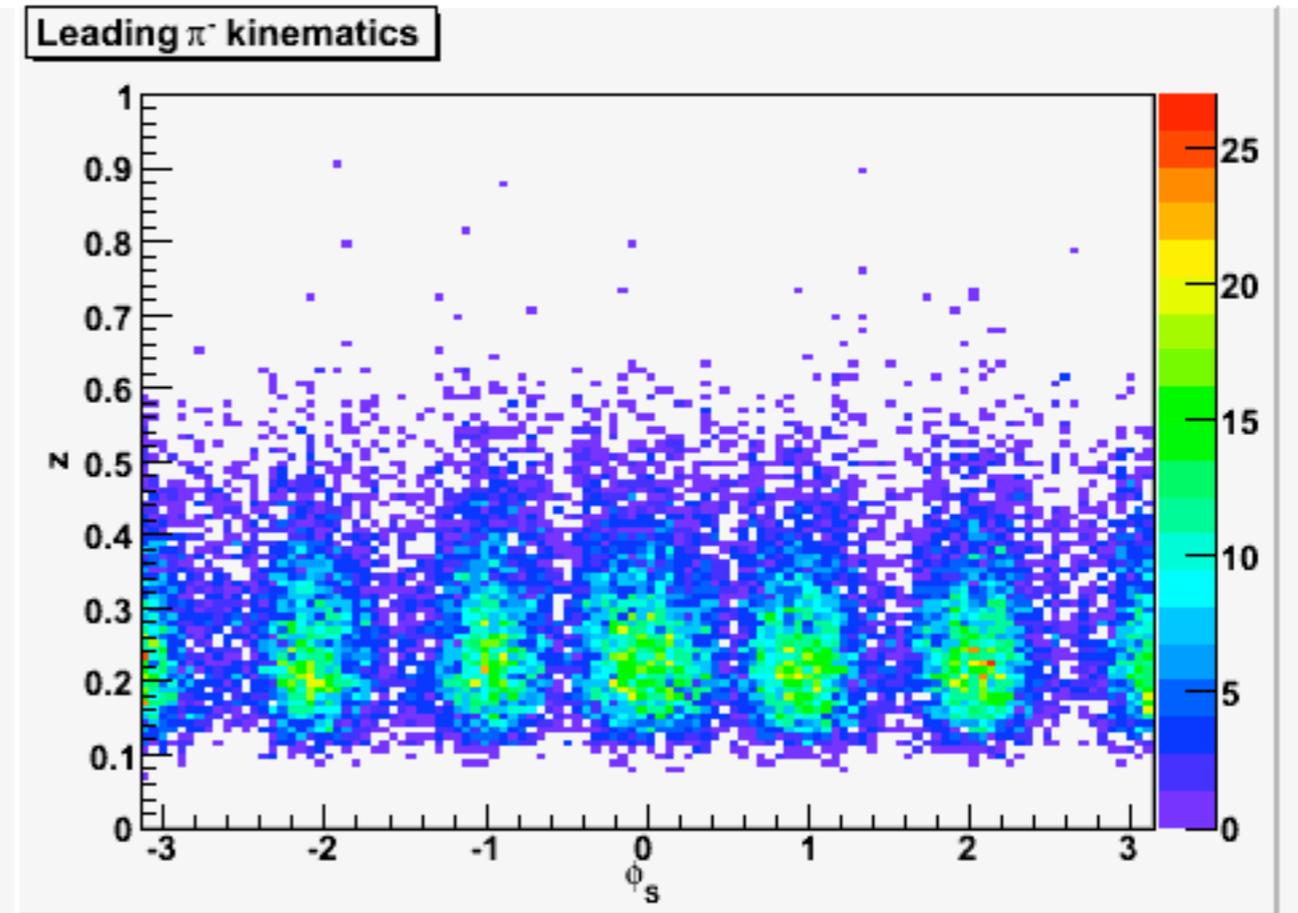
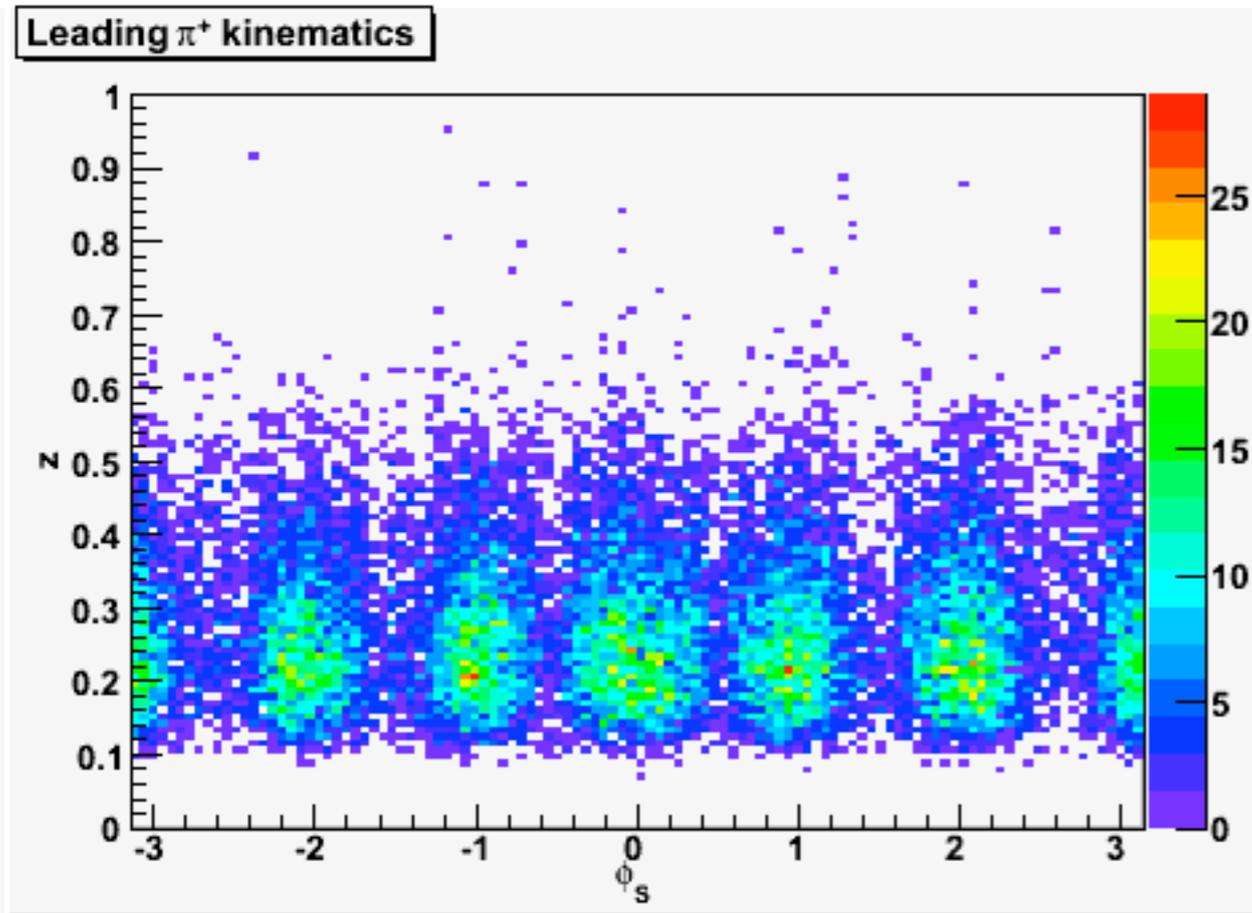


Asymmetry can be measured in terms of either  $z$  or  $j_T$

# Data separated by $z$ and $j_T$ ; azimuthal angles calculated:



Asymmetry can be measured in terms of either  $z$  or  $j_T$



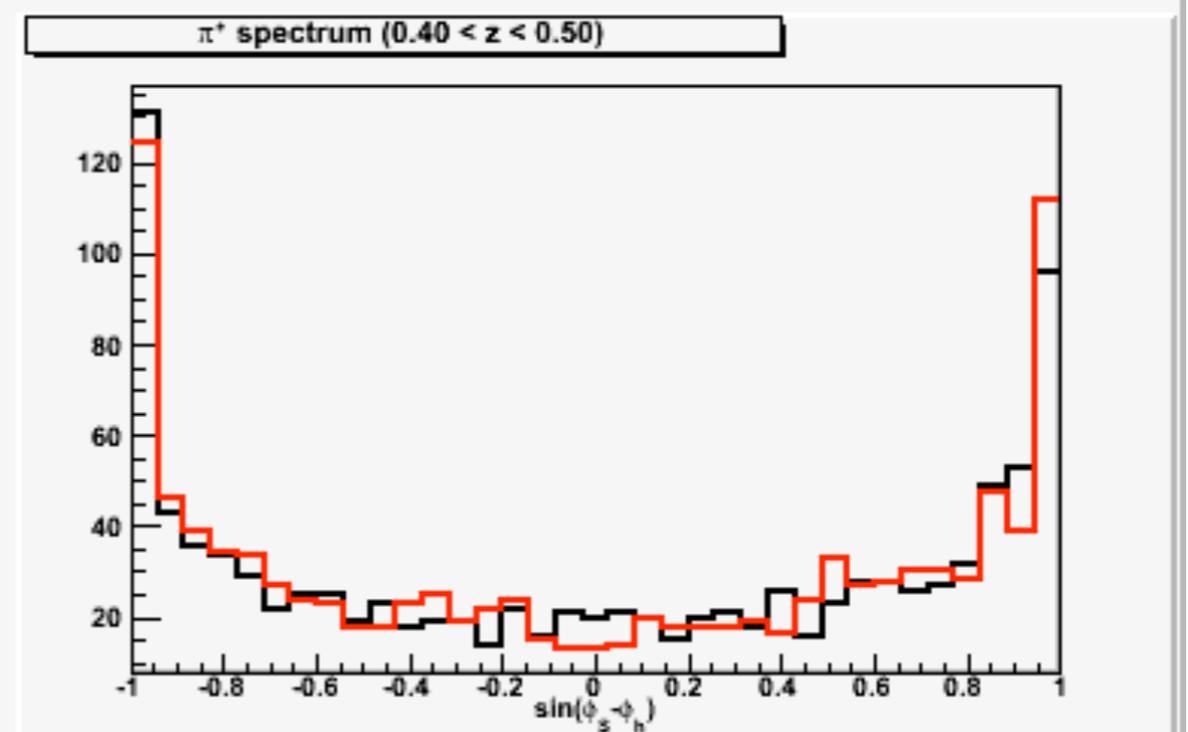
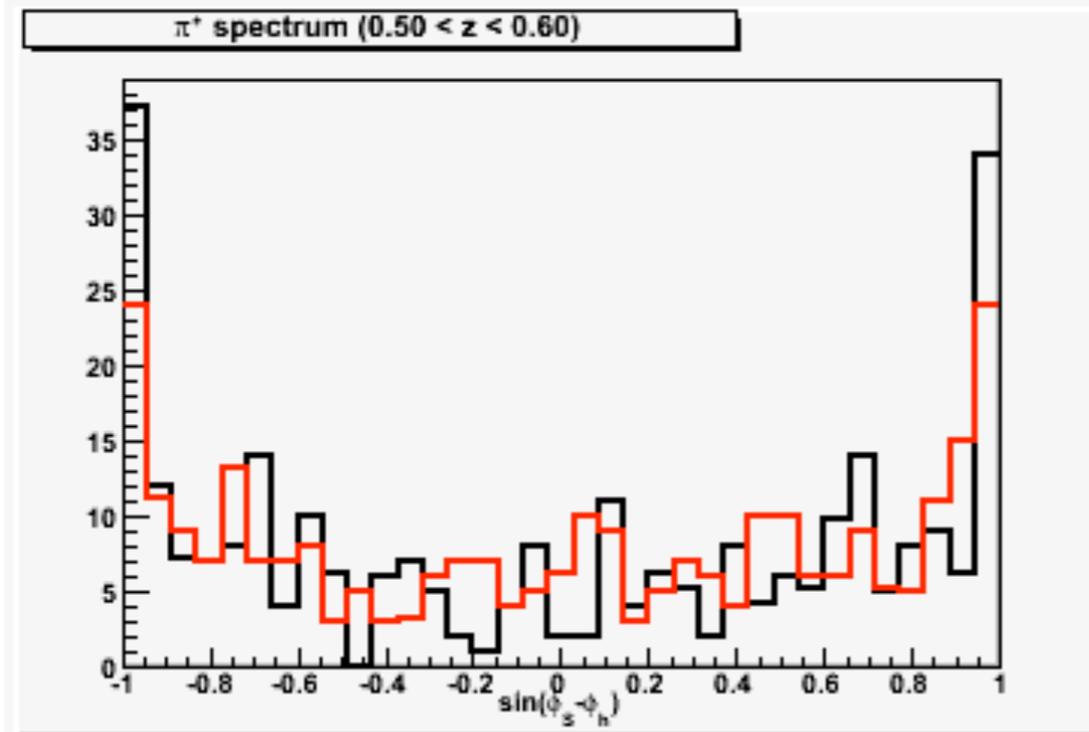
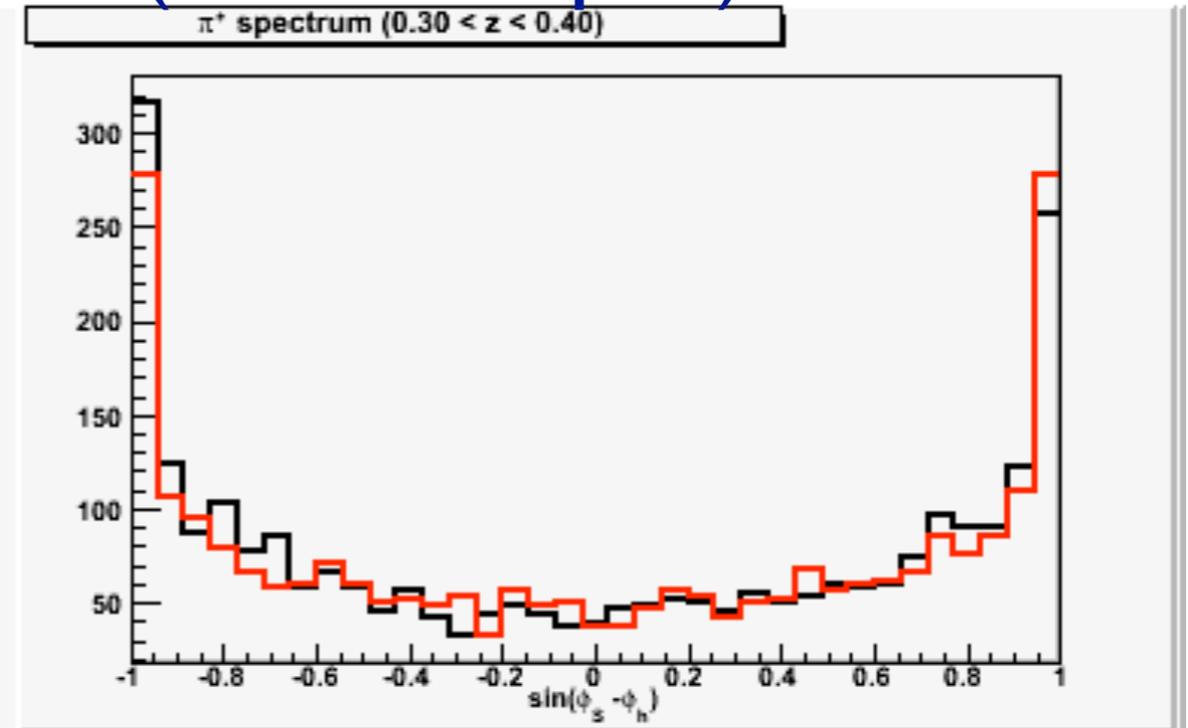
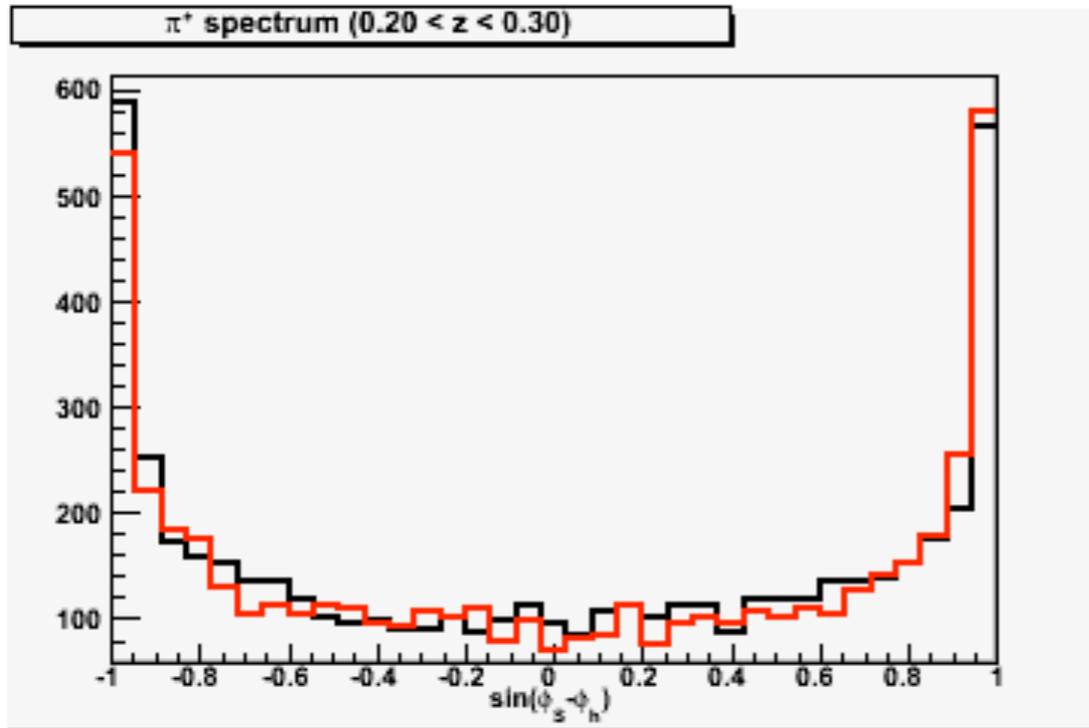
# Goals of this Presentation:

- Show statistical expectations of measured asymmetries and summarize systematic concerns

**$\sin(\phi_s - \phi_\pi)$  spectrum**

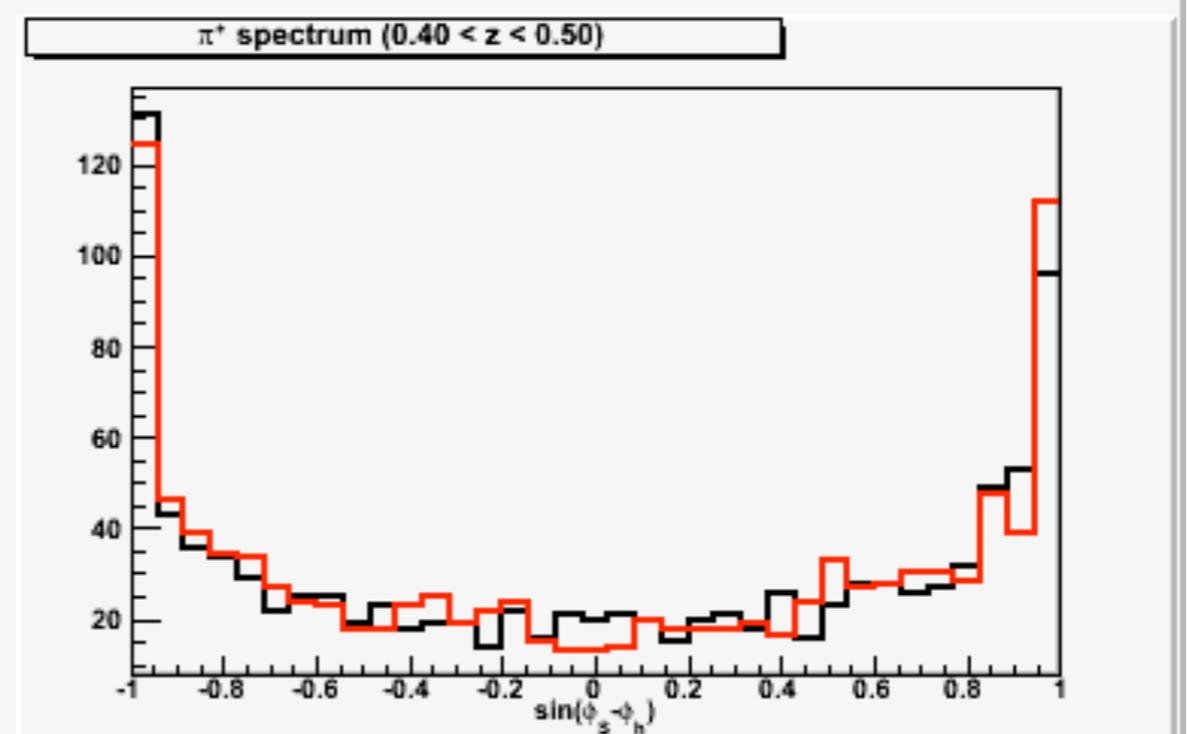
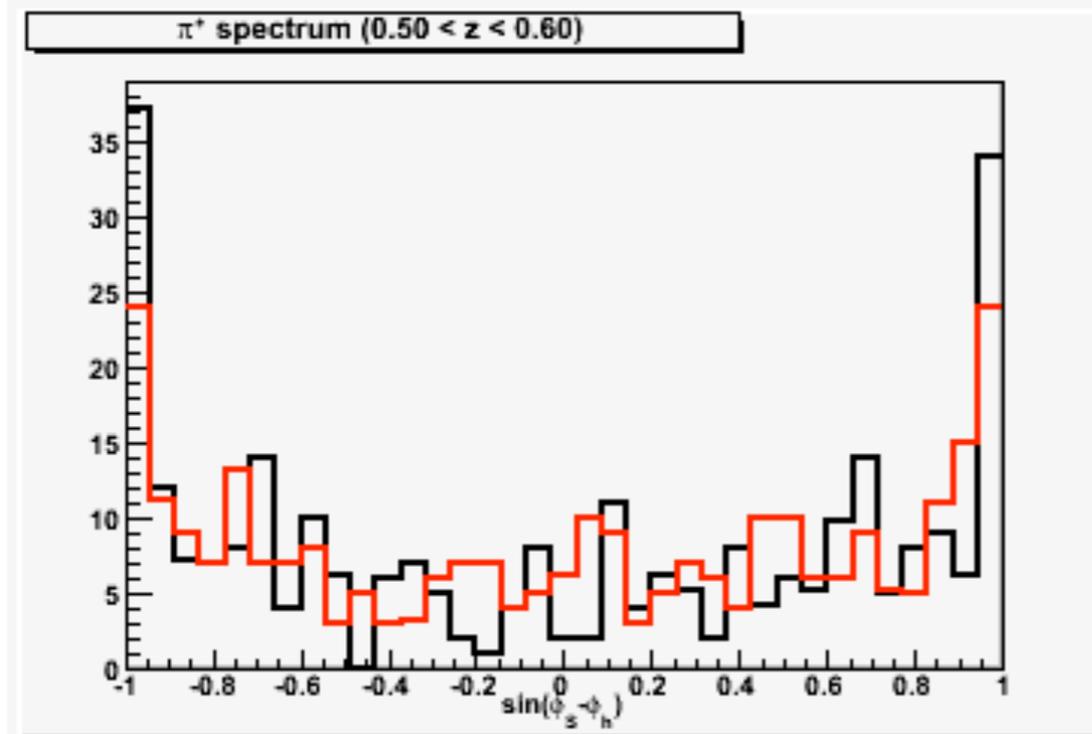
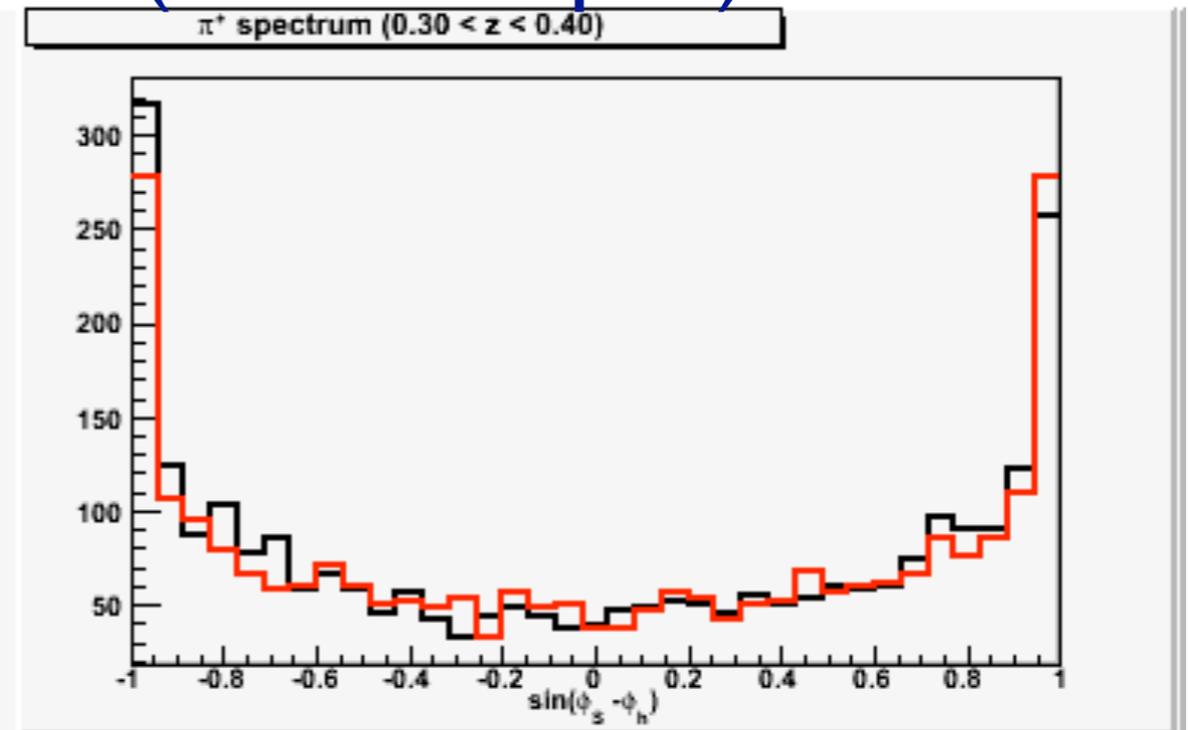
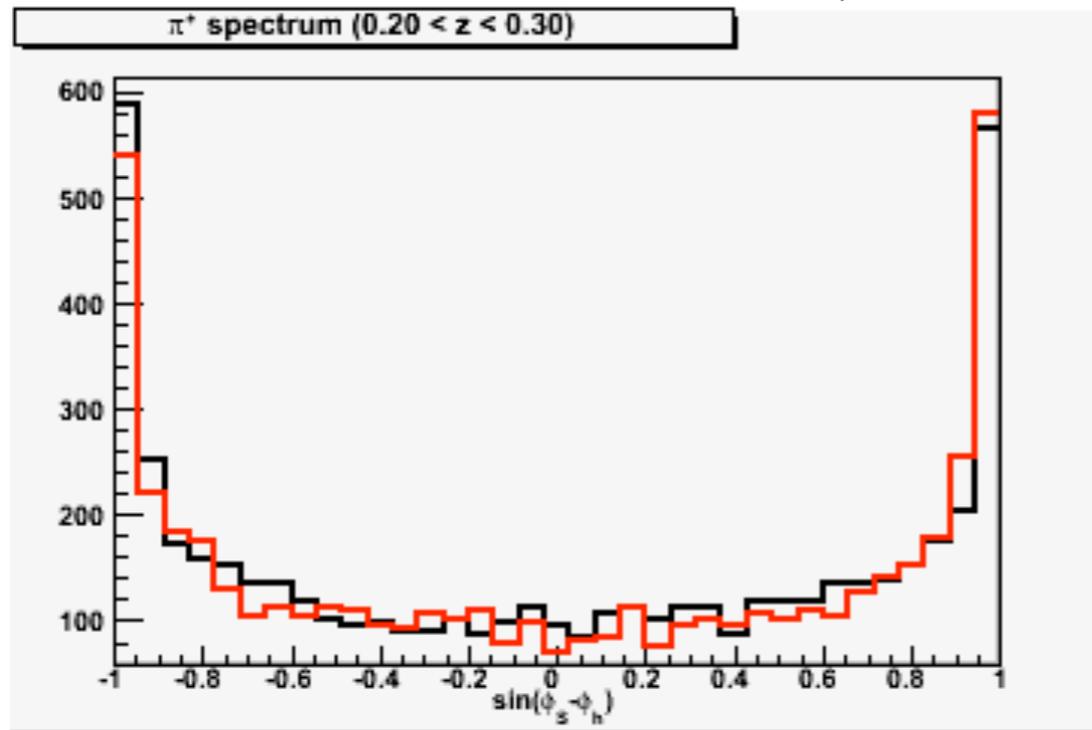
# $\sin(\Phi_S - \Phi_\pi)$ spectrum

Red =  $\uparrow$ , Black =  $\downarrow$  (lab frame pol.)



# $\sin(\Phi_S - \Phi_\pi)$ spectrum

Red =  $\uparrow$ , Black =  $\downarrow$  (lab frame pol.)

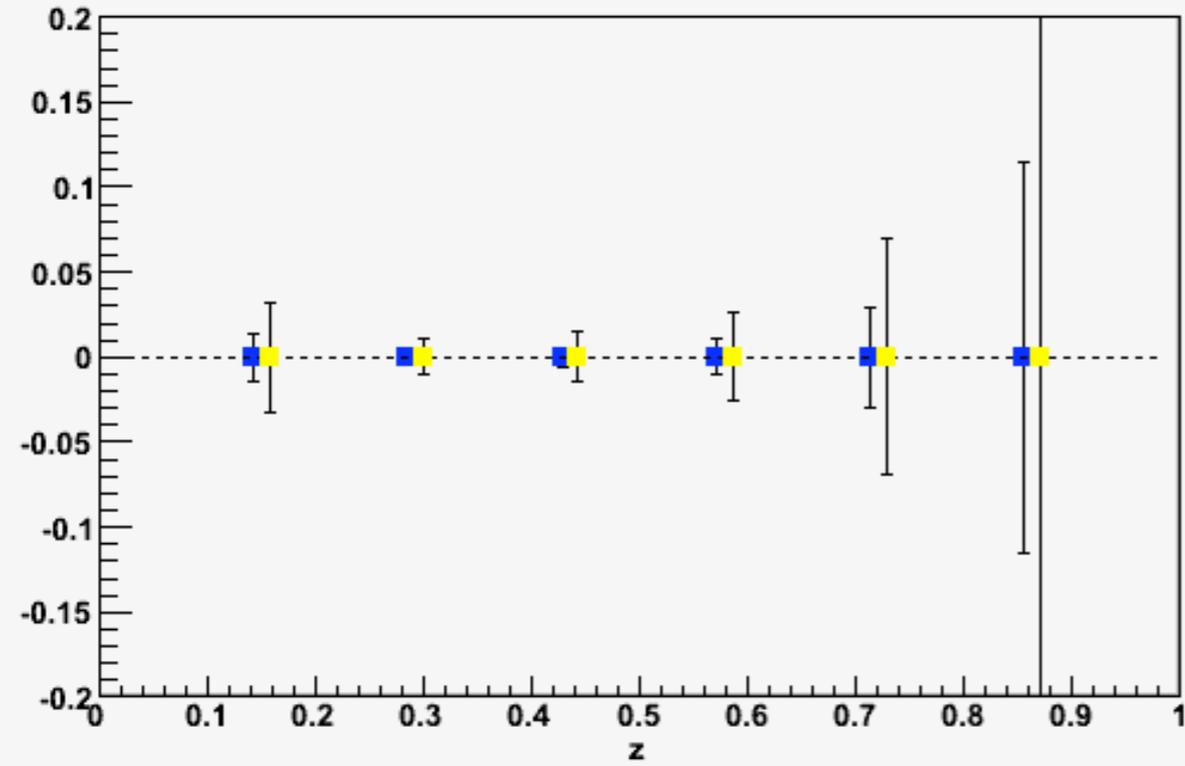


*(Use of opposing polarizations, weighted by beam luminosity, ensures that detector acceptances cancel in the asymmetry.)*

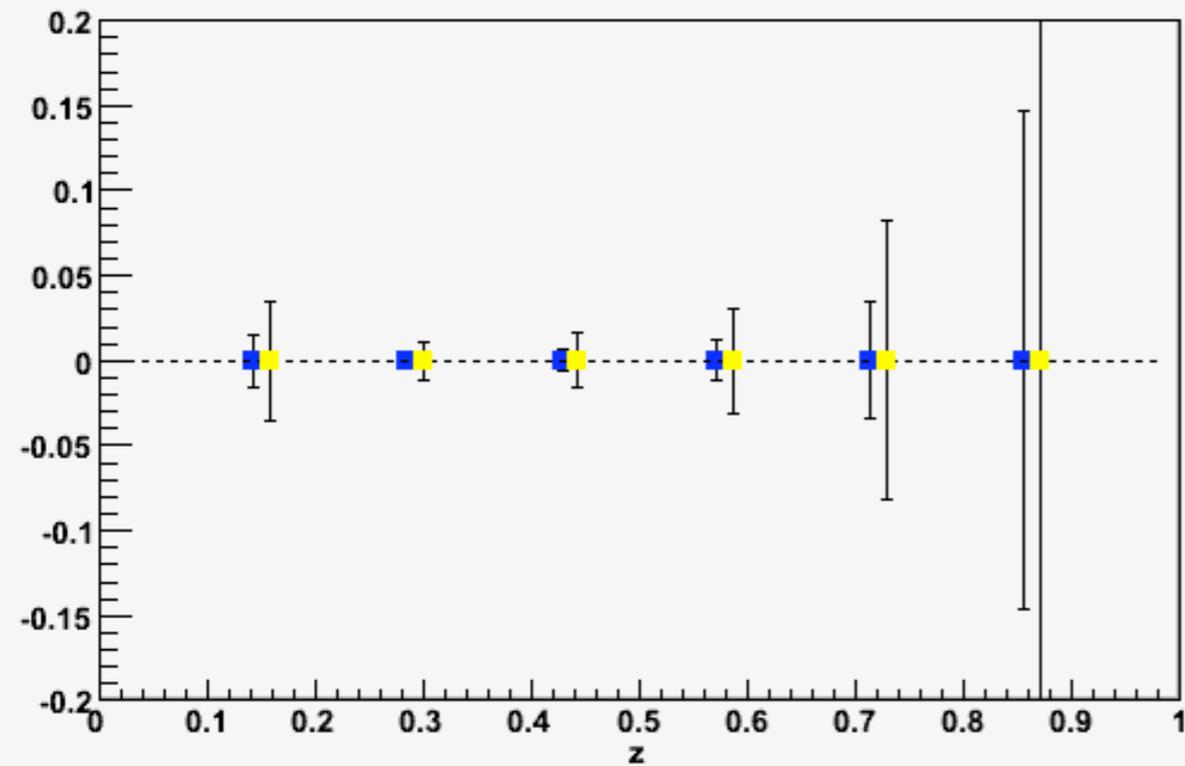
# **Asymmetry Statistics**

# Asymmetry Statistics

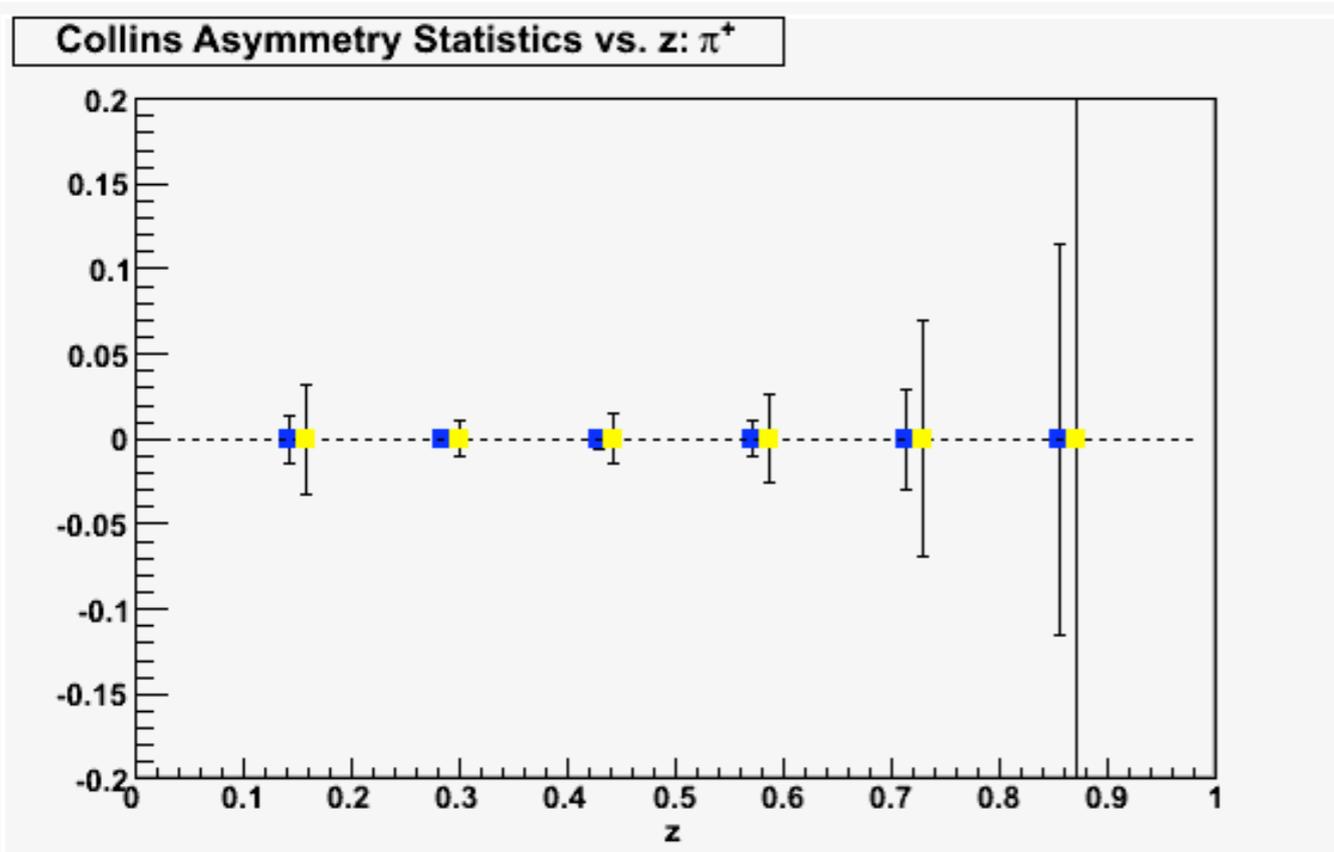
Collins Asymmetry Statistics vs.  $z: \pi^+$



Collins Asymmetry Statistics vs.  $z: \pi^-$



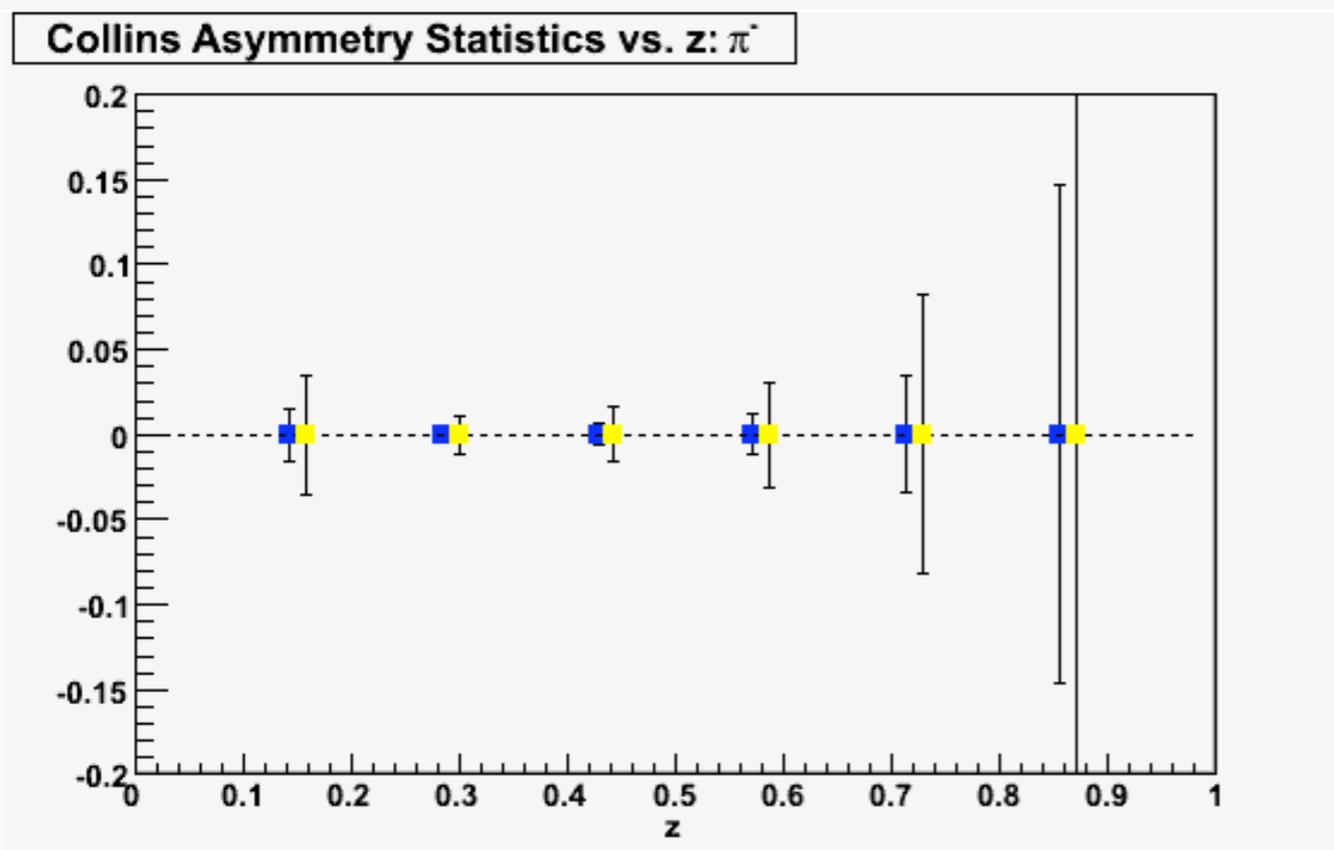
# Asymmetry Statistics



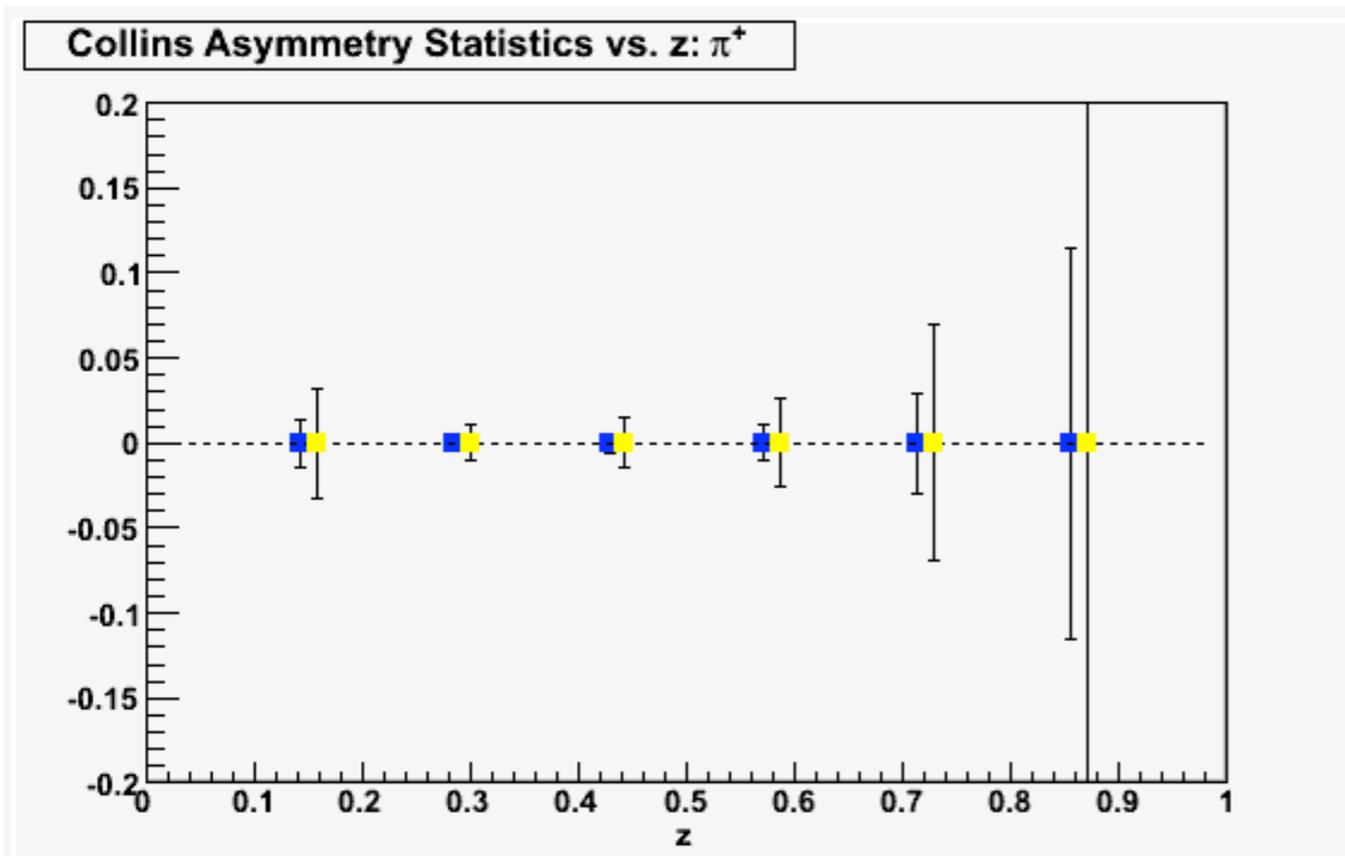
“blue” beam polarized

“yellow” beam polarized

(jets in forward hemisphere of each beam analyzed)



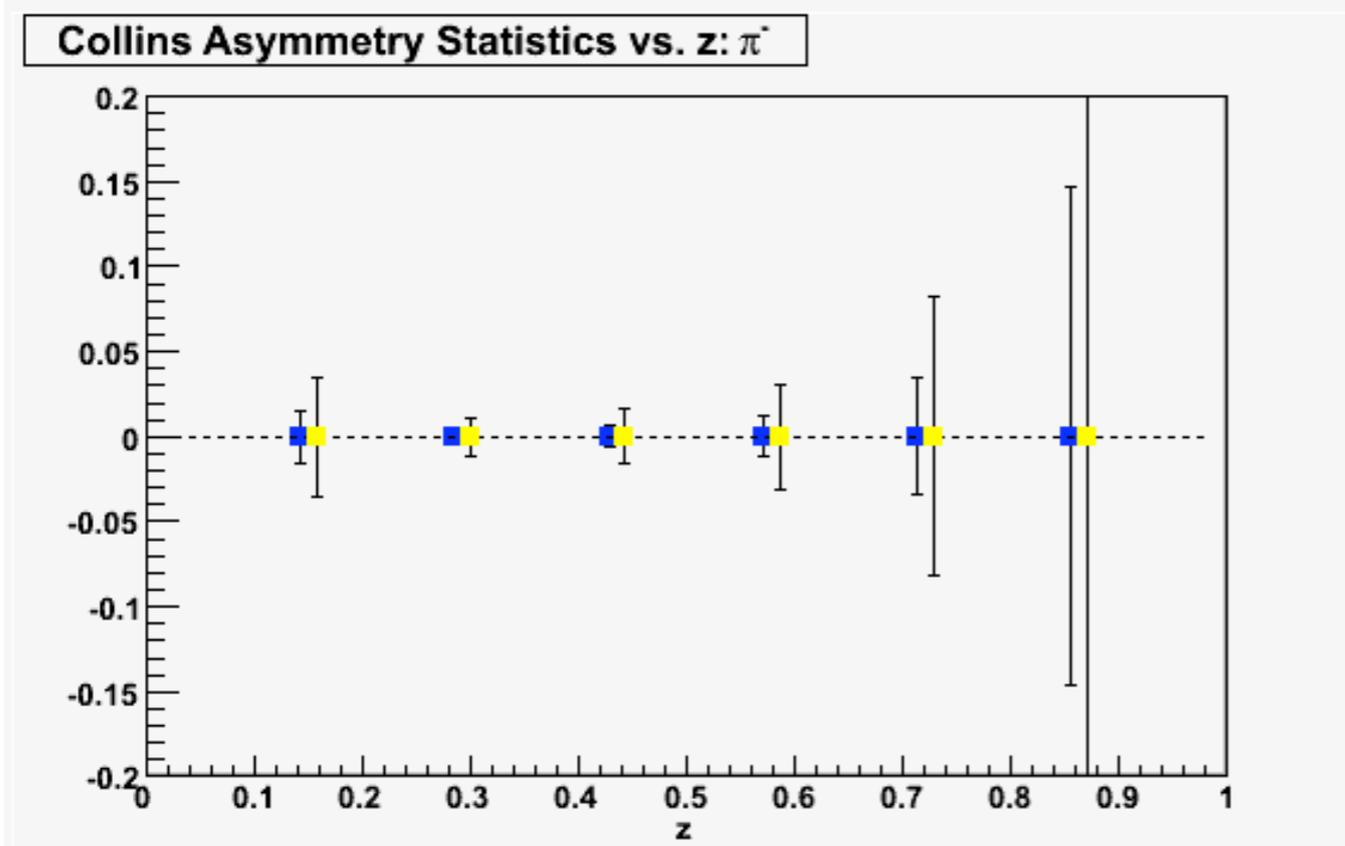
# Asymmetry Statistics



“blue” beam polarized

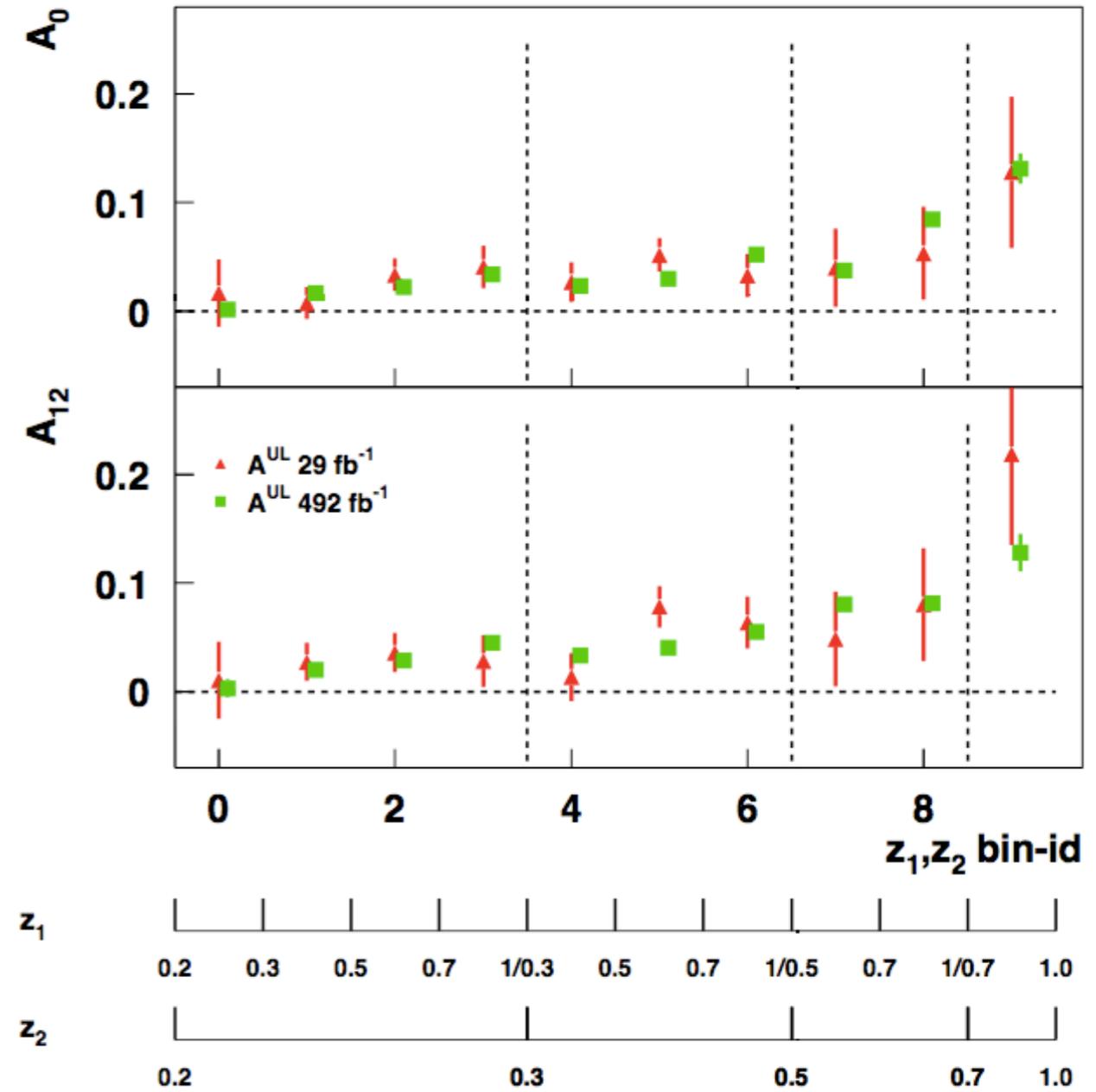
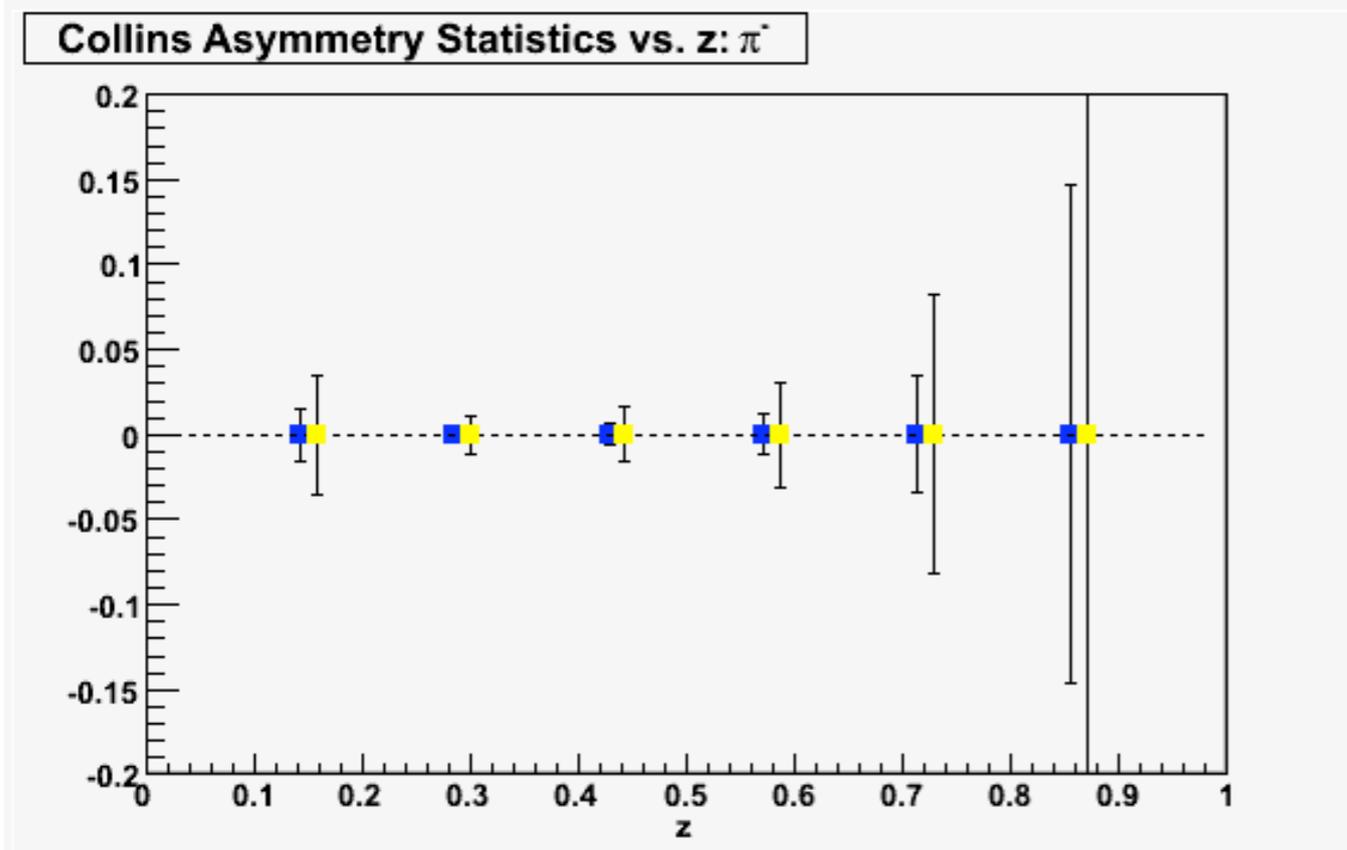
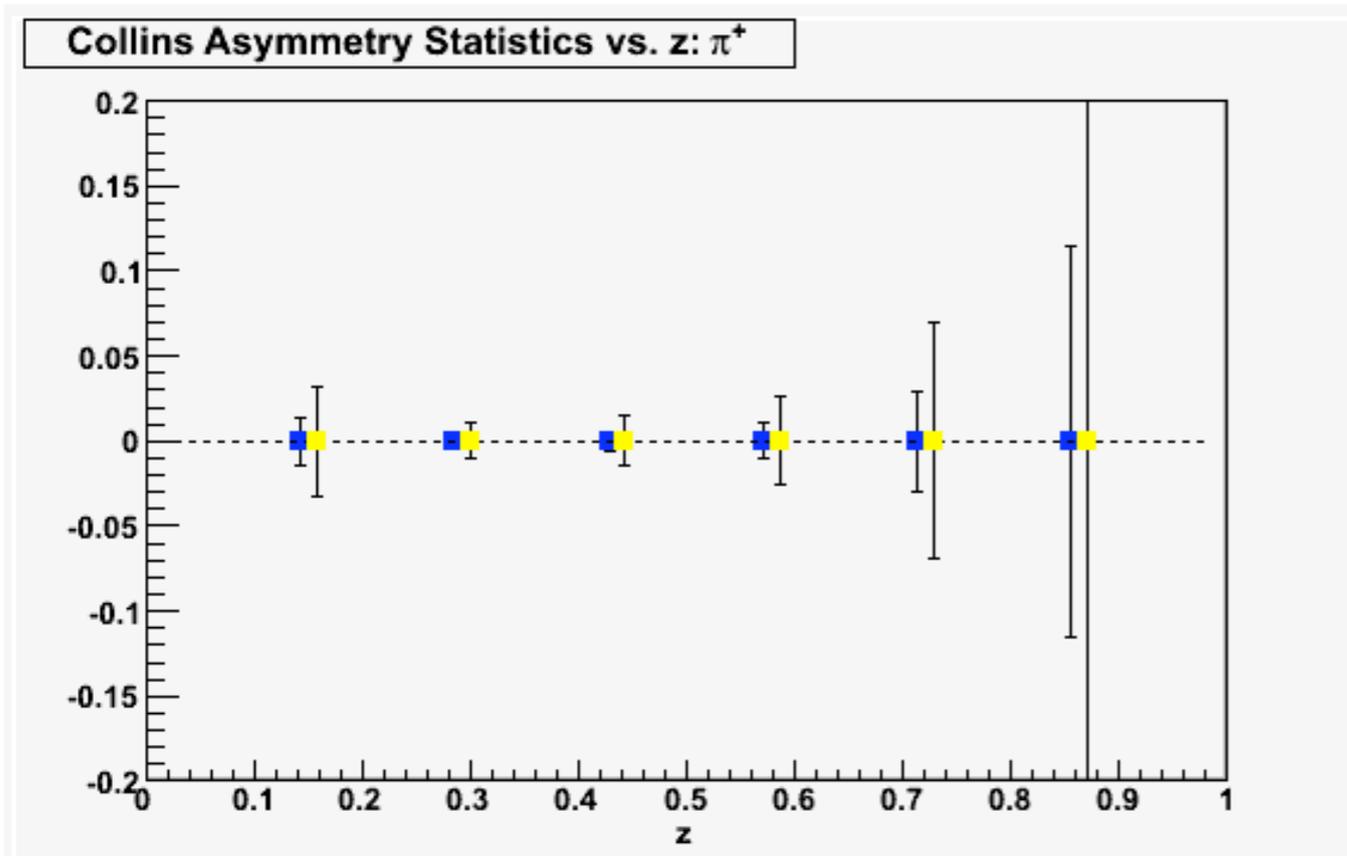
“yellow” beam polarized

(jets in forward hemisphere of each beam analyzed)



**Asymmetry should be opposite in sign for + vs. - pions**

# Asymmetry Statistics



Published  $e^+e^-$  results  
from Belle

# Upcoming: Systematic Errors

# Upcoming: Systematic Errors

- TRIGGER BIAS  $\Rightarrow$  accurate determination of leading pions; natural  $\langle z \rangle$  distribution (need PYTHIA simulation)

# Upcoming: Systematic Errors

- TRIGGER BIAS  $\Rightarrow$  accurate determination of leading pions; natural  $\langle z \rangle$  distribution (need PYTHIA simulation)
- $\pi^0$  (and  $K^0$ ) contribution to leading particles

# Upcoming: Systematic Errors

- TRIGGER BIAS  $\Rightarrow$  accurate determination of leading pions; natural  $\langle z \rangle$  distribution (need PYTHIA simulation)
- $\pi^0$  (and  $K^0$ ) contribution to leading particles
- $K^\pm$  contamination

# Upcoming: Systematic Errors

- TRIGGER BIAS  $\Rightarrow$  accurate determination of leading pions; natural  $\langle z \rangle$  distribution (need PYTHIA simulation)
- $\pi^0$  (and  $K^0$ ) contribution to leading particles
- $K^\pm$  contamination
- Track efficiency

# Upcoming: Systematic Errors

- TRIGGER BIAS  $\Rightarrow$  accurate determination of leading pions; natural  $\langle z \rangle$  distribution (need PYTHIA simulation)
- $\pi^0$  (and  $K^0$ ) contribution to leading particles
- $K^\pm$  contamination
- Track efficiency
- Accuracy of both jet and  $\pi$  kinematics

# Upcoming: Systematic Errors

- TRIGGER BIAS  $\Rightarrow$  accurate determination of leading pions; natural  $\langle z \rangle$  distribution (need PYTHIA simulation)
- $\pi^0$  (and  $K^0$ ) contribution to leading particles
- $K^\pm$  contamination
- Track efficiency
- Accuracy of both jet and  $\pi$  kinematics
- Polarization direction and magnitude

# Upcoming: Systematic Errors

- TRIGGER BIAS  $\Rightarrow$  accurate determination of leading pions; natural  $\langle z \rangle$  distribution (need PYTHIA simulation)
- $\pi^0$  (and  $K^0$ ) contribution to leading particles
- $K^\pm$  contamination
- Track efficiency
- Accuracy of both jet and  $\pi$  kinematics
- Polarization direction and magnitude
- Relative luminosity error

# Conclusion and Status of Research

The Collins mechanism yields sensitivity to transverseity in polarized  $p \uparrow p$  jet production.

Analysis of 2006 transverse data at mid-rapidity is well under way.

The aforementioned systematic effects are now being studied.

# Conclusion and Status of Research

The Collins mechanism yields sensitivity to transverseity in polarized  $p \uparrow p$  jet production.

Analysis of 2006 transverse data at mid-rapidity is well under way.

The aforementioned systematic effects are now being studied.

# Conclusion and Status of Research

The Collins mechanism yields sensitivity to transverseity in polarized  $p \uparrow p$  jet production.

Analysis of 2006 transverse data at mid-rapidity is well under way.

The aforementioned systematic effects are now being studied.

# Conclusion and Status of Research

The Collins mechanism yields sensitivity to transverseity in polarized  $p \uparrow p$  jet production.

Analysis of 2006 transverse data at mid-rapidity is well under way.

The aforementioned systematic effects are now being studied.

# Conclusion and Status of Research

The Collins mechanism yields sensitivity to transverseity in polarized  $p \uparrow p$  jet production.

Analysis of 2006 transverse data at mid-rapidity is well under way.

The aforementioned systematic effects are now being studied.

# Conclusion and Status of Research

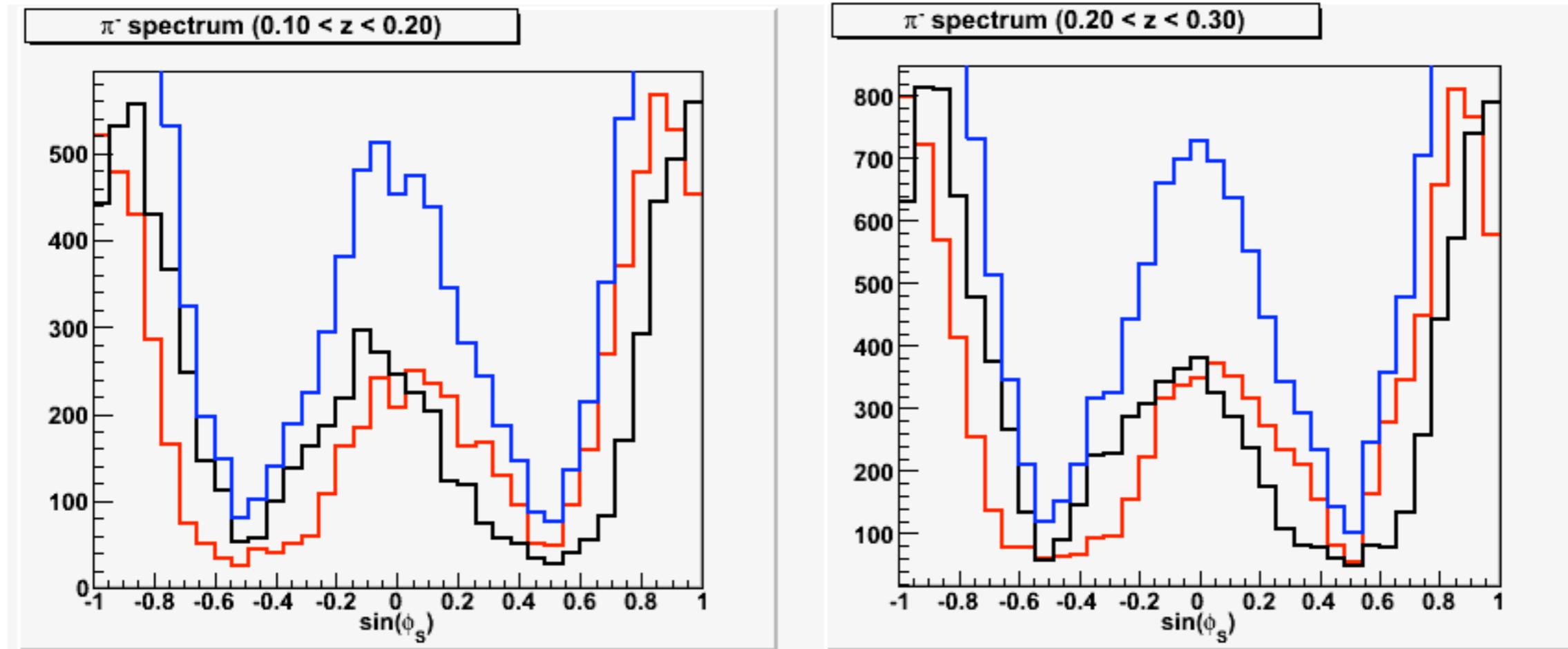
The Collins mechanism yields sensitivity to transverseity in polarized  $p \uparrow p$  jet production.

Analysis of 2006 transverse data at mid-rapidity is well under way.

The aforementioned systematic effects are now being studied.

# Extra Reference Slides

...after acceptances cancel when  
↑ and ↓ polarizations are added



red = up pol., black =  
down pol., blue = added

# Quantifying the Asymmetry

# Quantifying the Asymmetry

$$A = \frac{\langle \sin(\Phi_s - \Phi_h) \Delta \sigma^{TU} \rangle}{\langle \sigma^{UU} \rangle}$$

# Quantifying the Asymmetry

$$A = \frac{\langle \sin(\Phi_s - \Phi_h) \Delta \sigma^{TU} \rangle}{\langle \sigma^{UU} \rangle}$$

How do we get the cross-sections from particle counts in the detector?

# Quantifying the Asymmetry

$$A = \frac{\langle \sin(\Phi_s - \Phi_h) \Delta\sigma^{\text{TU}} \rangle}{\langle \sigma^{\text{UU}} \rangle}$$

How do we get the cross-sections from particle counts in the detector?

We sum over both  $\uparrow$  and  $\downarrow$  polarizations\* and exploit symmetry

\*weighted by relative luminosities

# Quantifying the Asymmetry

$$A = \frac{\langle \sin(\Phi_s - \Phi_h) \Delta\sigma^{TU} \rangle}{\langle \sigma^{UU} \rangle}$$

How do we get the cross-sections from particle counts in the detector?

We sum over both  $\uparrow$  and  $\downarrow$  polarizations\* and exploit symmetry

For  $0 < \Phi_s - \Phi_h < 180^\circ$ :

\*weighted by relative luminosities

Azimuthal symmetry requires that

$$N(\Phi_s - \Phi_h) \uparrow = N(\Phi_s - \Phi_h + 180^\circ) \downarrow + \Delta N$$

$$N(\Phi_s - \Phi_h) \downarrow = N(\Phi_s - \Phi_h + 180^\circ) \uparrow + \Delta N$$

# Quantifying the Asymmetry

$$A = \frac{\langle \sin(\Phi_s - \Phi_h) \Delta\sigma^{TU} \rangle}{\langle \sigma^{UU} \rangle}$$

How do we get the cross-sections from particle counts in the detector?

We sum over both  $\uparrow$  and  $\downarrow$  polarizations\* and exploit symmetry

For  $0 < \Phi_s - \Phi_h < 180^\circ$ :

Azimuthal symmetry requires that

$$N^+ \uparrow = N^- \downarrow + \Delta N$$

$$N^+ \downarrow = N^- \uparrow + \Delta N$$

\*weighted by relative luminosities

# Quantifying the Asymmetry

$$A = \frac{\langle \sin(\Phi_s - \Phi_h) \Delta \sigma^{TU} \rangle}{\langle \sigma^{UU} \rangle}$$

How do we get the cross-sections from particle counts in the detector?

We sum over both  $\uparrow$  and  $\downarrow$  polarizations\* and exploit symmetry

For  $0 < \Phi_s - \Phi_h < 180^\circ$ :

\*weighted by relative luminosities

Azimuthal symmetry requires that

$$N^+ \uparrow = N^- \downarrow + \Delta N$$

$$N^+ \downarrow = N^- \uparrow + \Delta N$$

Weighting and summing over opposite detector sides yields

$$A = \frac{N^+ \uparrow [\sin(\Phi_s - \Phi_h)] + N^- \downarrow [\sin(\Phi_s - \Phi_h + 180^\circ)] + N^+ \downarrow [\sin(\Phi_s - \Phi_h)] + N^- \uparrow [\sin(\Phi_s - \Phi_h + 180^\circ)] + 2\Delta N}{\Sigma N}$$

# Quantifying the Asymmetry

$$A = \frac{\langle \sin(\Phi_s - \Phi_h) \Delta\sigma^{TU} \rangle}{\langle \sigma^{UU} \rangle}$$

How do we get the cross-sections from particle counts in the detector?

We sum over both  $\uparrow$  and  $\downarrow$  polarizations\* and exploit symmetry

For  $0 < \Phi_s - \Phi_h < 180^\circ$ :

\*weighted by relative luminosities

Azimuthal symmetry requires that

$$N^+\uparrow = N^-\downarrow + \Delta N$$

$$N^+\downarrow = N^-\uparrow + \Delta N$$

Weighting and summing over opposite detector sides yields

$$\begin{aligned} A &= \frac{N^+\uparrow [\sin(\Phi_s - \Phi_h)] + N^-\downarrow [\sin(\Phi_s - \Phi_h + 180^\circ)] + N^+\downarrow [\sin(\Phi_s - \Phi_h)] + N^-\uparrow [\sin(\Phi_s - \Phi_h + 180^\circ)] + 2\Delta N}{\Sigma N} \\ &= \frac{N^+\uparrow [\sin(\Phi_s - \Phi_h)] - N^-\downarrow [\sin(\Phi_s - \Phi_h)] + N^+\downarrow [\sin(\Phi_s - \Phi_h)] - N^-\uparrow [\sin(\Phi_s - \Phi_h)] + 2\Delta N}{\Sigma N} \end{aligned}$$

# Quantifying the Asymmetry

$$A = \frac{\langle \sin(\Phi_s - \Phi_h) \Delta\sigma^{TU} \rangle}{\langle \sigma^{UU} \rangle}$$

How do we get the cross-sections from particle counts in the detector?

We sum over both  $\uparrow$  and  $\downarrow$  polarizations\* and exploit symmetry

For  $0 < \Phi_s - \Phi_h < 180^\circ$ :

\*weighted by relative luminosities

Azimuthal symmetry requires that

$$N^+ \uparrow = N^- \downarrow + \Delta N$$

$$N^+ \downarrow = N^- \uparrow + \Delta N$$

Weighting and summing over opposite detector sides yields

$$\begin{aligned} A &= \frac{N^+ \uparrow [\sin(\Phi_s - \Phi_h)] + N^- \downarrow [\sin(\Phi_s - \Phi_h + 180^\circ)] + N^+ \downarrow [\sin(\Phi_s - \Phi_h)] + N^- \uparrow [\sin(\Phi_s - \Phi_h + 180^\circ)] + 2\Delta N}{\Sigma N} \\ &= \frac{N^+ \uparrow [\sin(\Phi_s - \Phi_h)] - N^- \downarrow [\sin(\Phi_s - \Phi_h)] + N^+ \downarrow [\sin(\Phi_s - \Phi_h)] - N^- \uparrow [\sin(\Phi_s - \Phi_h)] + 2\Delta N}{\Sigma N} \\ &= \frac{2\Delta N}{\Sigma N} \end{aligned}$$

# Quantifying the Asymmetry

$$A = \frac{\langle \sin(\Phi_s - \Phi_h) \Delta\sigma^{TU} \rangle}{\langle \sigma^{UU} \rangle}$$

How do we get the cross-sections from particle counts in the detector?

We sum over both  $\uparrow$  and  $\downarrow$  polarizations\* and exploit symmetry

For  $0 < \Phi_s - \Phi_h < 180^\circ$ :

\*weighted by relative luminosities

Azimuthal symmetry requires that

$$N^+ \uparrow = N^- \downarrow + \Delta N$$

$$N^+ \downarrow = N^- \uparrow + \Delta N$$

Weighting and summing over opposite detector sides yields

$$\begin{aligned} A &= \frac{N^+ \uparrow [\sin(\Phi_s - \Phi_h)] + N^- \downarrow [\sin(\Phi_s - \Phi_h + 180^\circ)] + N^+ \downarrow [\sin(\Phi_s - \Phi_h)] + N^- \uparrow [\sin(\Phi_s - \Phi_h + 180^\circ)] + 2\Delta N}{\Sigma N} \\ &= \frac{N^+ \uparrow [\sin(\Phi_s - \Phi_h)] - N^- \downarrow [\sin(\Phi_s - \Phi_h)] + N^+ \downarrow [\sin(\Phi_s - \Phi_h)] - N^- \uparrow [\sin(\Phi_s - \Phi_h)] + 2\Delta N}{\Sigma N} \\ &= \frac{2\Delta N}{\Sigma N} \end{aligned}$$

Acceptances cancel if opposing polarizations summed

# Quantifying the Asymmetry

$$A = \frac{N_{\sin(\Phi_S - \Phi_H)}^{\uparrow} + N_{\sin(\Phi_S - \Phi_H)}^{\downarrow}}{N^{\uparrow} + N^{\downarrow}}$$

How do we get the cross-sections from particle counts in the detector?

We sum over both  $\uparrow$  and  $\downarrow$  polarizations\* and exploit symmetry

For  $0 < \Phi_S - \Phi_H < 180^\circ$ :

\*weighted by relative luminosities

Azimuthal symmetry requires that

$$N^{+\uparrow} = N^{-\downarrow} + \Delta N$$

$$N^{+\downarrow} = N^{-\uparrow} + \Delta N$$

Weighting and summing over opposite detector sides yields

$$\begin{aligned} A &= \frac{N^{+\uparrow} [\sin(\Phi_S - \Phi_H)] + N^{-\downarrow} [\sin(\Phi_S - \Phi_H + 180^\circ)] + N^{+\downarrow} [\sin(\Phi_S - \Phi_H)] + N^{-\uparrow} [\sin(\Phi_S - \Phi_H + 180^\circ)] + 2\Delta N}{\Sigma N} \\ &= \frac{N^{+\uparrow} [\sin(\Phi_S - \Phi_H)] - N^{-\downarrow} [\sin(\Phi_S - \Phi_H)] + N^{+\downarrow} [\sin(\Phi_S - \Phi_H)] - N^{-\uparrow} [\sin(\Phi_S - \Phi_H)] + 2\Delta N}{\Sigma N} \\ &= \frac{2\Delta N}{\Sigma N} \end{aligned}$$

Acceptances cancel if opposing polarizations summed

# Quantifying the Asymmetry

$$A = \frac{N_{\sin(\Phi_s - \Phi_h)}^{\uparrow}(z, j_T) + N_{\sin(\Phi_s - \Phi_h)}^{\downarrow}(z, j_T)}{N^{\uparrow}(z, j_T) + N^{\downarrow}(z, j_T)}$$

How do we get the cross-sections from particle counts in the detector?

We sum over both  $\uparrow$  and  $\downarrow$  polarizations\* and exploit symmetry

For  $0 < \Phi_s - \Phi_h < 180^\circ$ :

\*weighted by relative luminosities

Azimuthal symmetry requires that

$$N^{+\uparrow} = N^{-\downarrow} + \Delta N$$

$$N^{+\downarrow} = N^{-\uparrow} + \Delta N$$

Weighting and summing over opposite detector sides yields

$$\begin{aligned} A &= \frac{N^{+\uparrow}[\sin(\Phi_s - \Phi_h)] + N^{-\downarrow}[\sin(\Phi_s - \Phi_h + 180^\circ)] + N^{+\downarrow}[\sin(\Phi_s - \Phi_h)] + N^{-\uparrow}[\sin(\Phi_s - \Phi_h + 180^\circ)] + 2\Delta N}{\Sigma N} \\ &= \frac{N^{+\uparrow}[\sin(\Phi_s - \Phi_h)] - N^{-\downarrow}[\sin(\Phi_s - \Phi_h)] + N^{+\downarrow}[\sin(\Phi_s - \Phi_h)] - N^{-\uparrow}[\sin(\Phi_s - \Phi_h)] + 2\Delta N}{\Sigma N} \\ &= \frac{2\Delta N}{\Sigma N} \end{aligned}$$

Acceptances cancel if opposing polarizations summed

# Extraction of $\delta q$

F. Yuan, arXiv:0804.3047 [hep-ph] (2008)

$$\frac{d\sigma}{dy_1 dy_2 dp_T^2 dz d^2 j_T} \equiv \frac{d\sigma}{d\mathbf{P.S.}} = \frac{d\sigma_{UU}}{d\mathbf{P.S.}} + |S_\perp| \frac{|j_T|}{m_\pi} \sin(\phi_\pi - \phi_S) \frac{d\sigma_{TU}}{d\mathbf{P.S.}}$$

# Extraction of $\delta q$

F. Yuan, arXiv:0804.3047 [hep-ph] (2008)

$$\frac{d\sigma}{dy_1 dy_2 dp_T^2 dz d^2 j_T} \equiv \frac{d\sigma}{d\mathbf{P.S.}} = \frac{d\sigma_{UU}}{d\mathbf{P.S.}} + |S_\perp| \frac{|j_T|}{m_\pi} \sin(\phi_\pi - \phi_S) \frac{d\sigma_{TU}}{d\mathbf{P.S.}}$$

phase space

# Extraction of $\delta q$

F. Yuan, arXiv:0804.3047 [hep-ph] (2008)

$$\frac{d\sigma}{dy_1 dy_2 dp_T^2 dz d^2 j_T} \equiv \frac{d\sigma}{d\mathbf{P.S.}} = \frac{d\sigma_{UU}}{d\mathbf{P.S.}} + \underset{\substack{\uparrow \\ \text{polarization}}}{|S_{\perp}|} \frac{|j_T|}{m_{\pi}} \sin(\phi_{\pi} - \phi_S) \frac{d\sigma_{TU}}{d\mathbf{P.S.}}$$

phase space

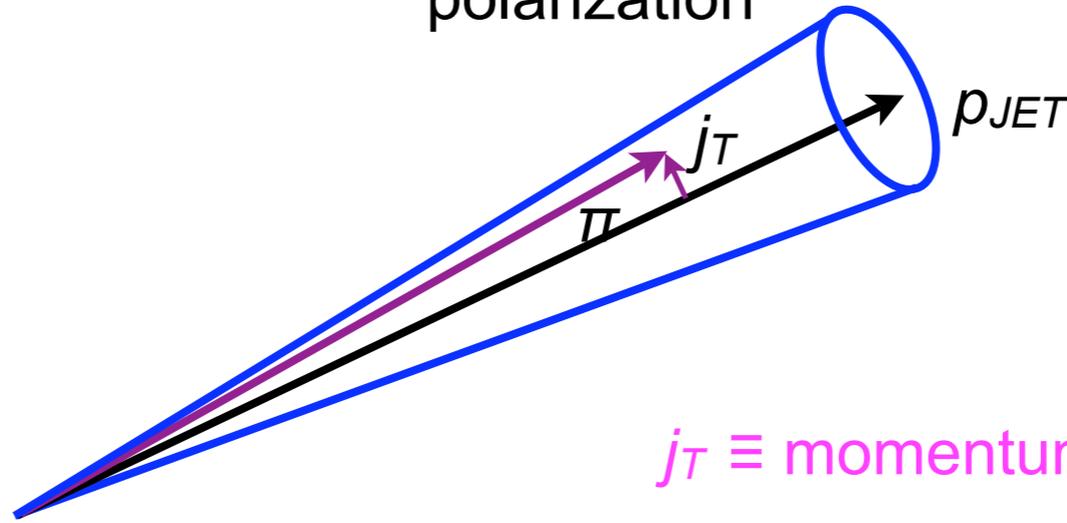
# Extraction of $\delta q$

F. Yuan, arXiv:0804.3047 [hep-ph] (2008)

$$\frac{d\sigma}{dy_1 dy_2 dp_T^2 dz d^2 j_T} \equiv \frac{d\sigma}{d\mathbf{P.S.}} = \frac{d\sigma_{UU}}{d\mathbf{P.S.}} + |S_{\perp}| \frac{j_T}{m_{\pi}} \sin(\phi_{\pi} - \phi_S) \frac{d\sigma_{TU}}{d\mathbf{P.S.}}$$

phase space

polarization



$j_T \equiv$  momentum of  $\pi$  transverse to jet

# Extraction of $\delta q$

F. Yuan, arXiv:0804.3047 [hep-ph] (2008)

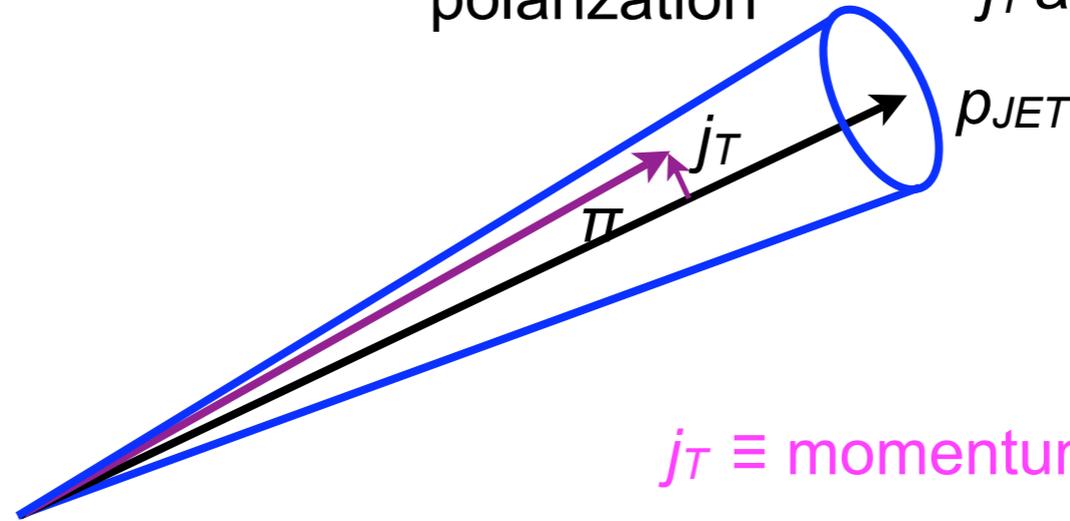
$$\frac{d\sigma}{dy_1 dy_2 dp_T^2 dz d^2 j_T} \equiv \frac{d\sigma}{d\mathbf{P.S.}} = \frac{d\sigma_{UU}}{d\mathbf{P.S.}} + |S_{\perp}| \frac{j_T}{m_{\pi}} \sin(\phi_{\pi} - \phi_S) \frac{d\sigma_{TU}}{d\mathbf{P.S.}}$$

phase space

polarization

$j_T$  angle

pol. angle



$j_T \equiv$  momentum of  $\pi$  transverse to jet

# Extraction of $\delta q$

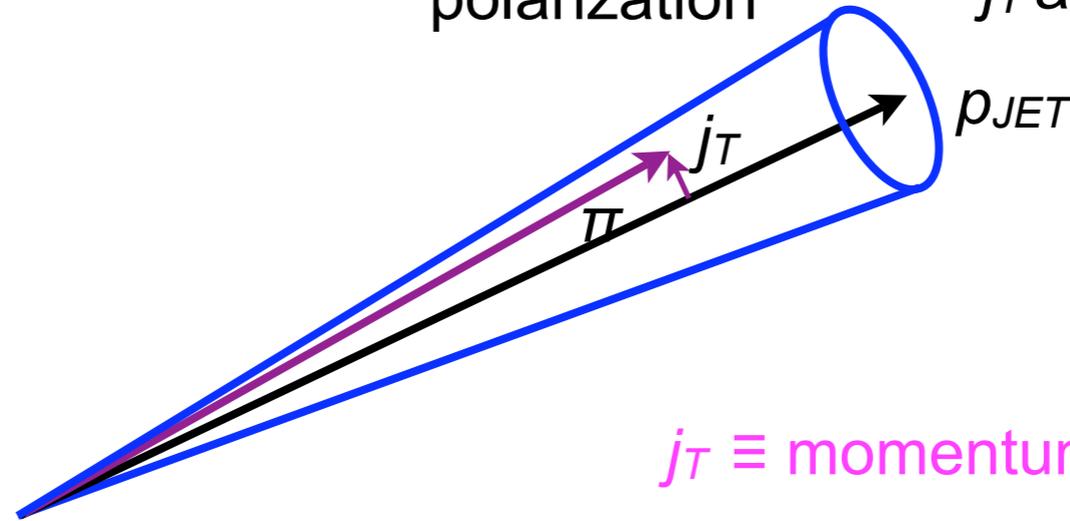
F. Yuan, arXiv:0804.3047 [hep-ph] (2008)

unpolarized, polarized cross-sections

$$\frac{d\sigma}{dy_1 dy_2 dp_T^2 dz d^2 j_T} \equiv \frac{d\sigma}{d\mathbf{P.S.}} = \frac{d\sigma_{UU}}{d\mathbf{P.S.}} + |S_{\perp}| \frac{j_T}{m_{\pi}} \sin(\phi_{\pi} - \phi_S) \frac{d\sigma_{TU}}{d\mathbf{P.S.}}$$

↑ polarization
↑  $j_T$  angle
↑ pol. angle

phase space



$j_T \equiv$  momentum of  $\pi$  transverse to jet

$$\frac{d\sigma_{UU}}{d\mathbf{P.S.}} = \sum_{a,b,c} x' f_b(x') x f_a(x) D_c^h(z, j_T) H_{ab \rightarrow cd}$$

$$\frac{d\sigma_{TU}}{d\mathbf{P.S.}} = \sum_{b,q} x' f_b(x') x \delta q(x) \Delta^N D_q(z, j_T) H_{qb \rightarrow qb}^{\text{Collins}}$$

# Extraction of $\delta q$

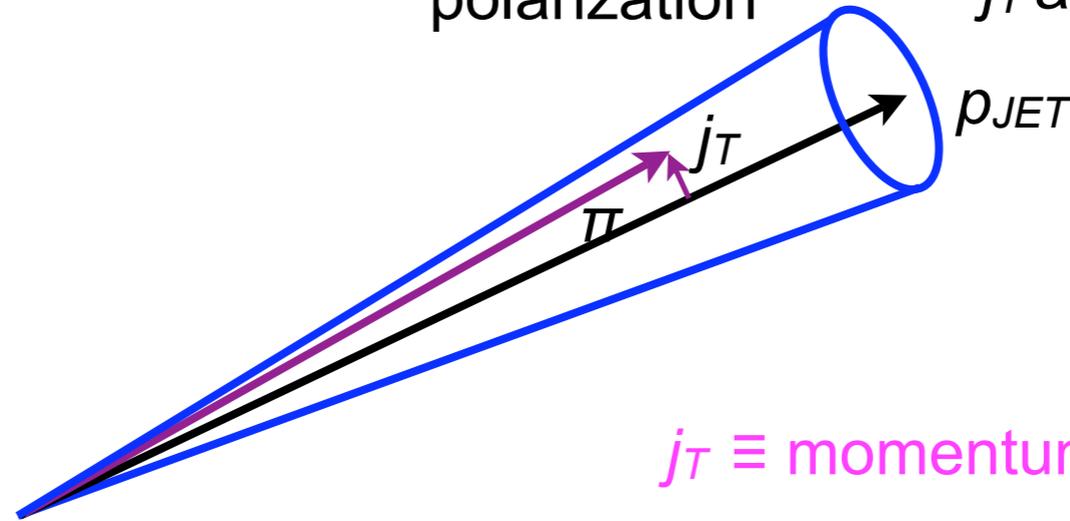
F. Yuan, arXiv:0804.3047 [hep-ph] (2008)

unpolarized, polarized cross-sections

$$\frac{d\sigma}{dy_1 dy_2 dp_T^2 dz d^2 j_T} \equiv \frac{d\sigma}{d\mathbf{P.S.}} = \frac{d\sigma_{UU}}{d\mathbf{P.S.}} + |S_\perp| \frac{j_T}{m_\pi} \sin(\phi_\pi - \phi_S) \frac{d\sigma_{TU}}{d\mathbf{P.S.}}$$

↑ polarization
↑  $j_T$  angle
↑ pol. angle

phase space



$j_T \equiv$  momentum of  $\pi$  transverse to jet

$$\frac{d\sigma_{UU}}{d\mathbf{P.S.}} = \sum_{a,b,c} x' f_b(x') x f_a(x) D_c^h(z, j_T) H_{ab \rightarrow cd}$$

$$\frac{d\sigma_{TU}}{d\mathbf{P.S.}} = \sum_{b,q} x' f_b(x') x \delta q(x) \Delta^N D_q(z, j_T) H_{qb \rightarrow qb}^{\text{Collins}}$$

(Unpolarized) quark distributions at  $x \approx 0.2$

# Extraction of $\delta q$

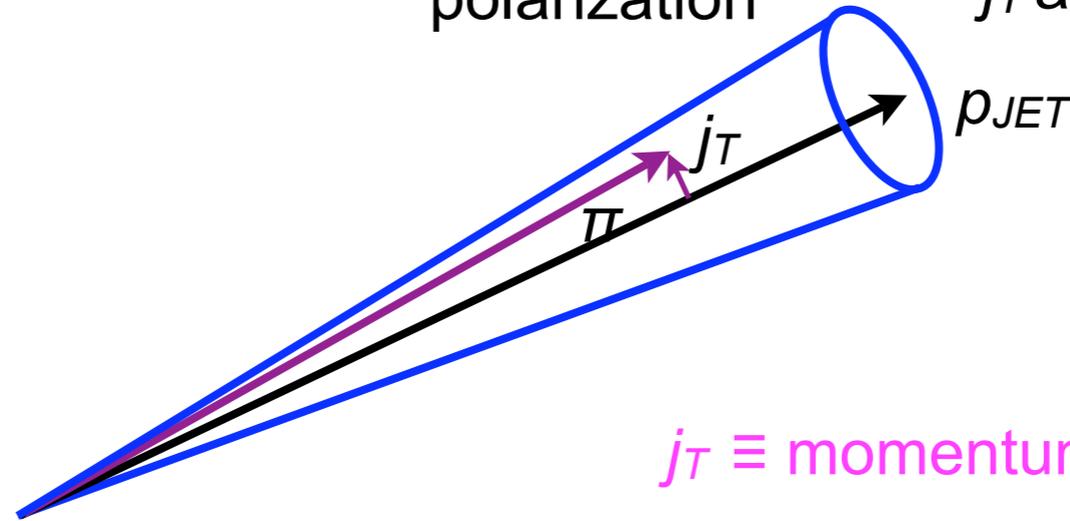
F. Yuan, arXiv:0804.3047 [hep-ph] (2008)

unpolarized, polarized cross-sections

$$\frac{d\sigma}{dy_1 dy_2 dp_T^2 dz d^2 j_T} \equiv \frac{d\sigma}{d\mathbf{P.S.}} = \frac{d\sigma_{UU}}{d\mathbf{P.S.}} + |S_{\perp}| \frac{j_T}{m_{\pi}} \sin(\phi_{\pi} - \phi_S) \frac{d\sigma_{TU}}{d\mathbf{P.S.}}$$

↑ polarization
↑  $j_T$  angle
↑ pol. angle

phase space



$j_T \equiv$  momentum of  $\pi$  transverse to jet

$$\frac{d\sigma_{UU}}{d\mathbf{P.S.}} = \sum_{a,b,c} x' f_b(x') x f_a(x) D_c^h(z, j_T) H_{ab \rightarrow cd}$$

$$\frac{d\sigma_{TU}}{d\mathbf{P.S.}} = \sum_{b,q} x' f_b(x') x \delta q(x) \Delta^N D_q(z, j_T) H_{qb \rightarrow qb}^{\text{Collins}}$$

(Unpolarized) quark distributions at  $x \approx 0.2$

**Fragmentation functions (Collins, Sivers)**

# Extraction of $\delta q$

F. Yuan, arXiv:0804.3047 [hep-ph] (2008)

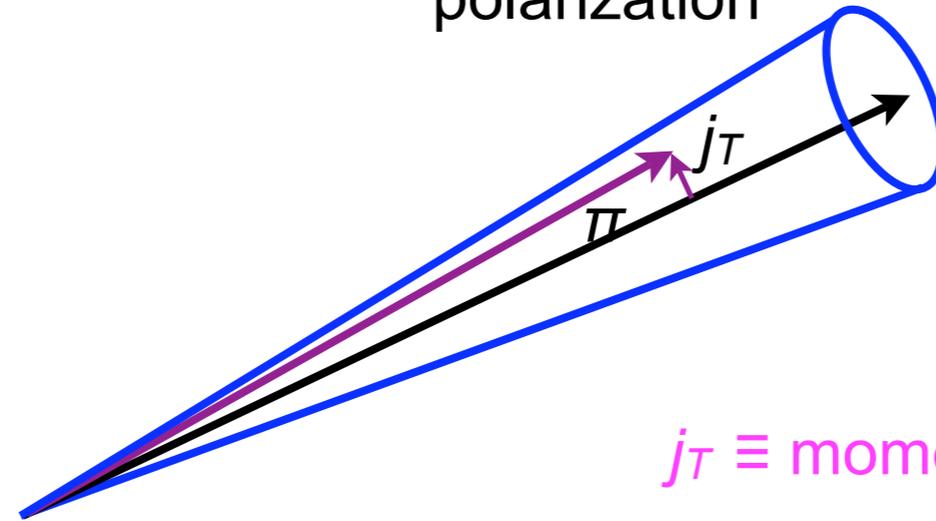
unpolarized, polarized cross-sections

$$\frac{d\sigma}{dy_1 dy_2 dp_T^2 dz d^2 j_T} \equiv \frac{d\sigma}{d\mathbf{P.S.}} = \frac{d\sigma_{UU}}{d\mathbf{P.S.}} + |S_{\perp}| \frac{j_T}{m_{\pi}} \sin(\phi_{\pi} - \phi_S) \frac{d\sigma_{TU}}{d\mathbf{P.S.}}$$

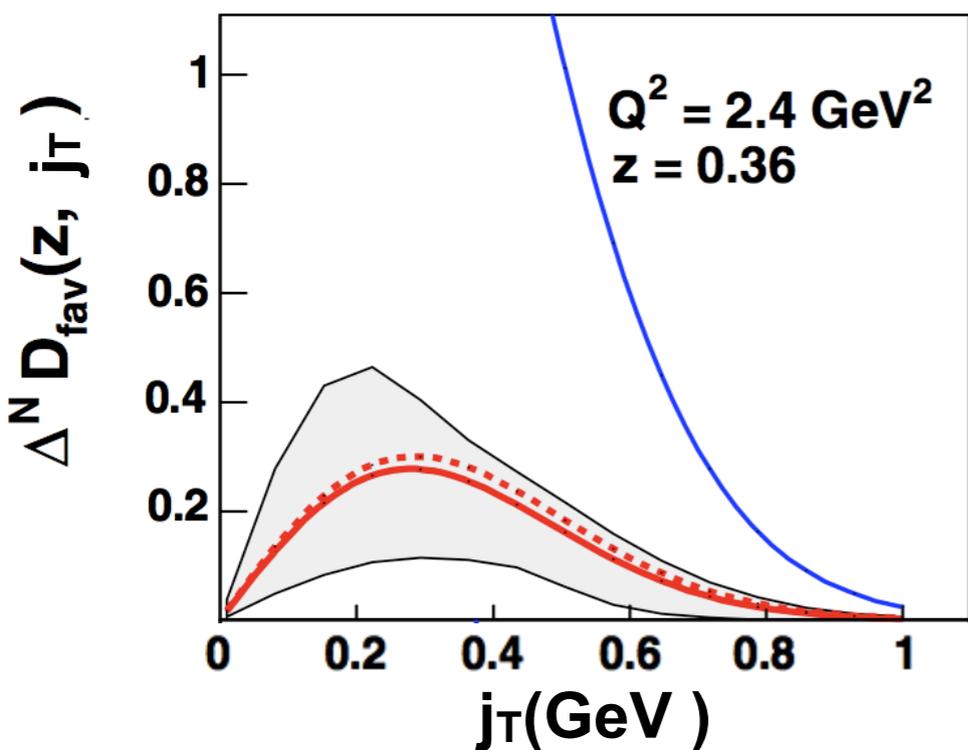
↑ polarization
↑  $j_T$  angle
↑ pol. angle

phase space

Extraction of Collins fragmentation function from fit to SIDIS data (HERMES, COMPASS) and Belle Collab. data (KEK) (Anselmino, *et al.*, 2008)



$j_T \equiv$  momentum of  $\pi$  transverse to jet



$$\frac{d\sigma_{UU}}{d\mathbf{P.S.}} = \sum_{a,b,c} x' f_b(x') x f_a(x) D_c^h(z, j_T) H_{ab \rightarrow cd}$$

$$\frac{d\sigma_{TU}}{d\mathbf{P.S.}} = \sum_{b,q} x' f_b(x') x \delta q(x) \Delta^N D_q(z, j_T) H_{qb \rightarrow qb}^{\text{Collins}}$$

(Unpolarized) quark distributions at  $x \approx 0.2$

**Fragmentation functions (Collins, Sivers)**

← Isospin-favored Collins frag. function

# Extraction of $\delta q$

F. Yuan, arXiv:0804.3047 [hep-ph] (2008)

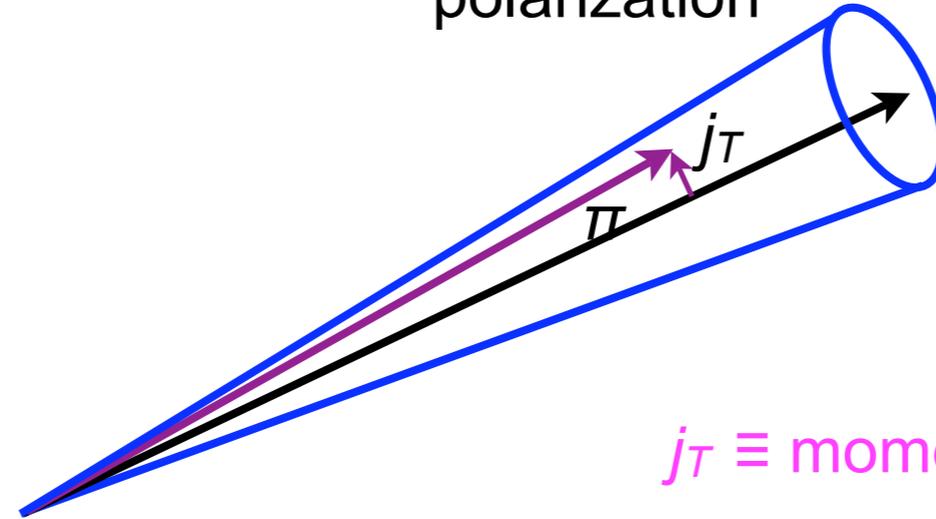
unpolarized, polarized cross-sections

$$\frac{d\sigma}{dy_1 dy_2 dp_T^2 dz d^2 j_T} \equiv \frac{d\sigma}{d\mathbf{P.S.}} = \frac{d\sigma_{UU}}{d\mathbf{P.S.}} + |S_\perp| \frac{j_T}{m_\pi} \sin(\phi_\pi - \phi_S) \frac{d\sigma_{TU}}{d\mathbf{P.S.}}$$

↑ polarization
↑  $j_T$  angle
↑ pol. angle

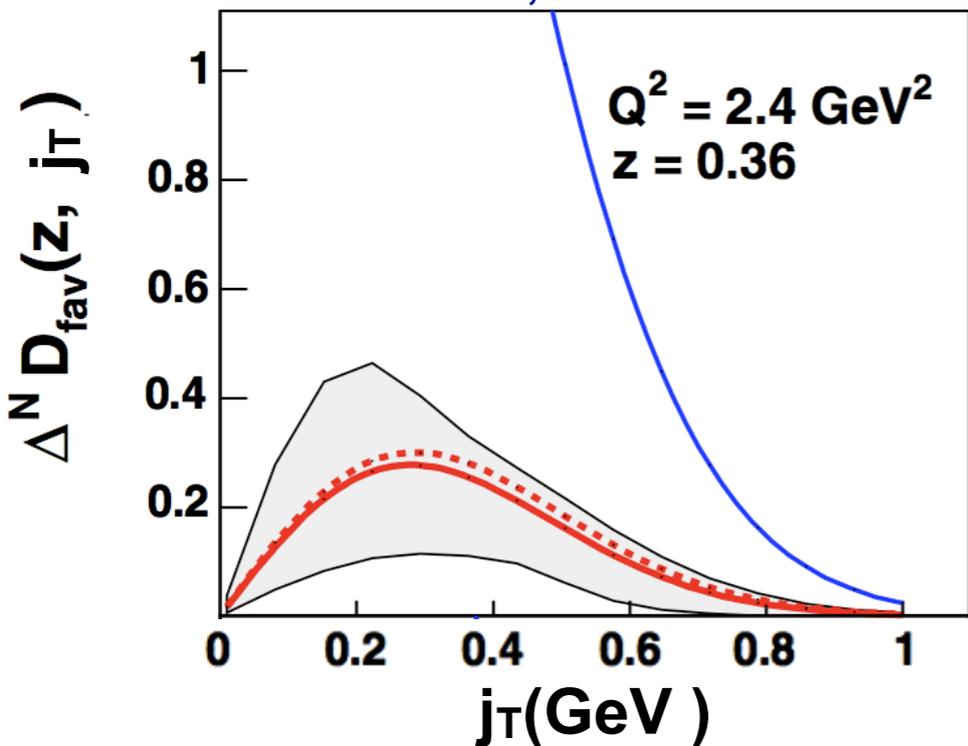
phase space

Extraction of Collins fragmentation function from fit to SIDIS data (HERMES, COMPASS) and Belle Collab. data (KEK) (Anselmino, *et al.*, 2008)



$j_T \equiv$  momentum of  $\pi$  transverse to jet

$\pi^+$ : favored =  $u$ , unfavored =  $d$   
 $\pi^-$ : favored =  $d$ , unfavored =  $u$



Isospin-favored Collins frag. function

$$\frac{d\sigma_{UU}}{d\mathbf{P.S.}} = \sum_{a,b,c} x' f_b(x') x f_a(x) D_c^h(z, j_T) H_{ab \rightarrow cd}$$

$$\frac{d\sigma_{TU}}{d\mathbf{P.S.}} = \sum_{b,q} x' f_b(x') x \delta q(x) \Delta^N D_q(z, j_T) H_{qb \rightarrow qb}^{\text{Collins}}$$

(Unpolarized) quark distributions at  $x \approx 0.2$

Fragmentation functions (Collins, Sivers)

# Extraction of $\delta q$

F. Yuan, arXiv:0804.3047 [hep-ph] (2008)

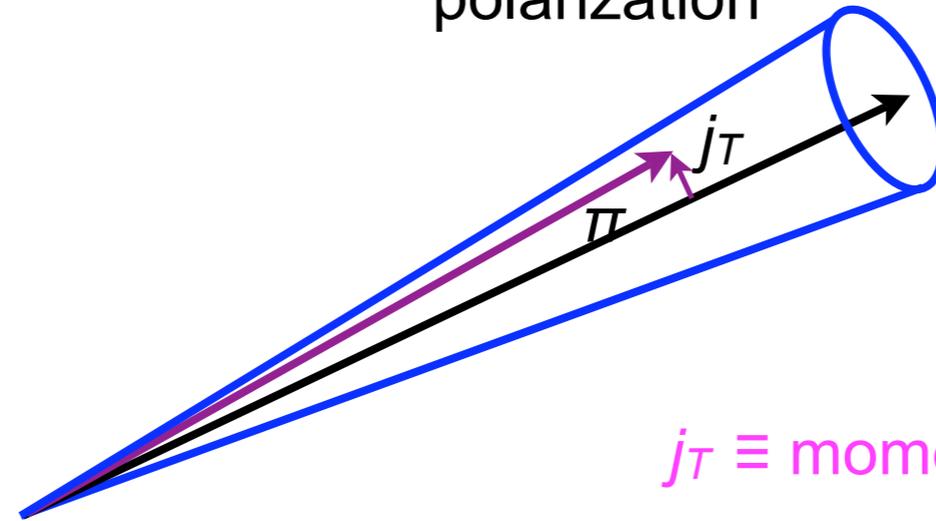
unpolarized, polarized cross-sections

$$\frac{d\sigma}{dy_1 dy_2 dp_T^2 dz d^2 j_T} \equiv \frac{d\sigma}{d\mathbf{P.S.}} = \frac{d\sigma_{UU}}{d\mathbf{P.S.}} + |S_{\perp}| \frac{j_T}{m_{\pi}} \sin(\phi_{\pi} - \phi_S) \frac{d\sigma_{TU}}{d\mathbf{P.S.}}$$

↑ polarization
↑  $j_T$  angle
↑ pol. angle

phase space

Extraction of Collins fragmentation function from fit to SIDIS data (HERMES, COMPASS) and Belle Collab. data (KEK) (Anselmino, *et al.*, 2008)



$j_T \equiv$  momentum of  $\pi$  transverse to jet

$\pi^+$ : favored =  $u$ , unfavored =  $d$   
 $\pi^-$ : favored =  $d$ , unfavored =  $u$

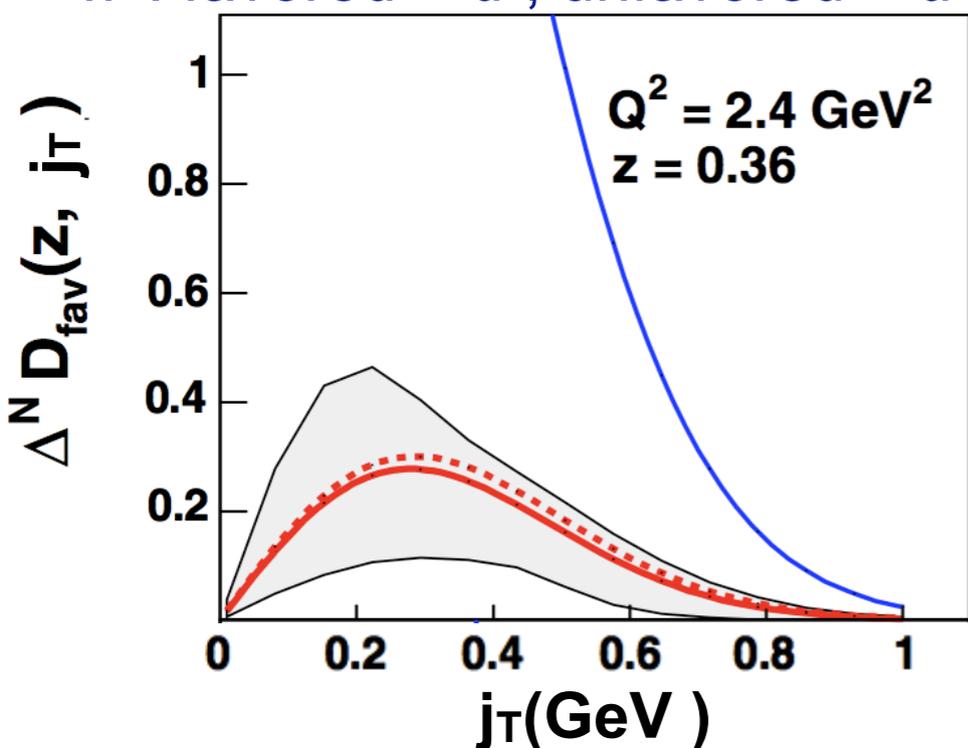
$$\frac{d\sigma_{UU}}{d\mathbf{P.S.}} = \sum_{a,b,c} x' f_b(x') x f_a(x) D_c^h(z, j_T) H_{ab \rightarrow cd}$$

$$\frac{d\sigma_{TU}}{d\mathbf{P.S.}} = \sum_{b,q} x' f_b(x') x \delta q(x) \Delta^N D_q(z, j_T) H_{qb \rightarrow qb}^{\text{Collins}}$$

(Unpolarized) quark distributions at  $x \approx 0.2$

Fragmentation functions (Collins, Sivers)

Hard scattering term  $\sim 0.4-0.5$



Isospin-favored Collins frag. function

# Extraction of $\delta q$

F. Yuan, arXiv:0804.3047 [hep-ph] (2008)

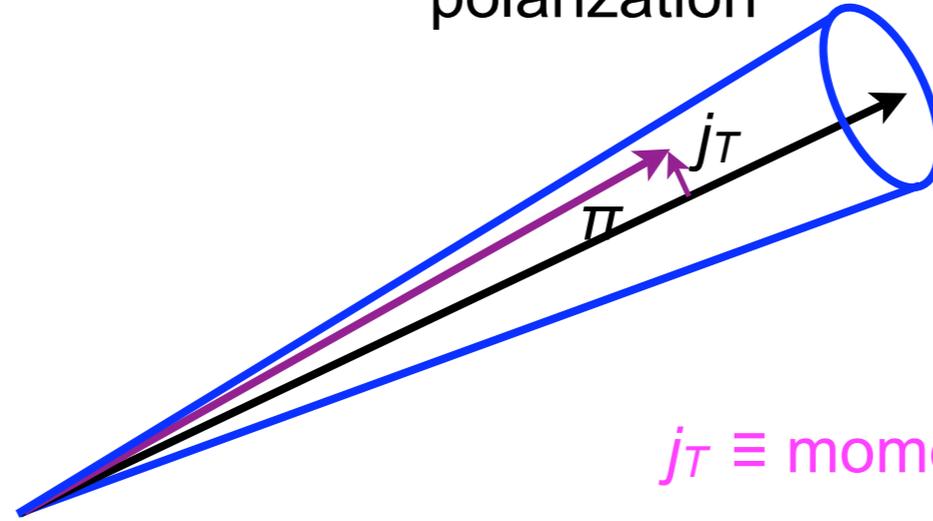
unpolarized, polarized cross-sections

$$\frac{d\sigma}{dy_1 dy_2 dp_T^2 dz d^2 j_T} \equiv \frac{d\sigma}{d\mathbf{P.S.}} = \frac{d\sigma_{UU}}{d\mathbf{P.S.}} + |S_{\perp}| \frac{j_T}{m_{\pi}} \sin(\phi_{\pi} - \phi_S) \frac{d\sigma_{TU}}{d\mathbf{P.S.}}$$

↑ polarization
↑  $j_T$  angle
↑ pol. angle

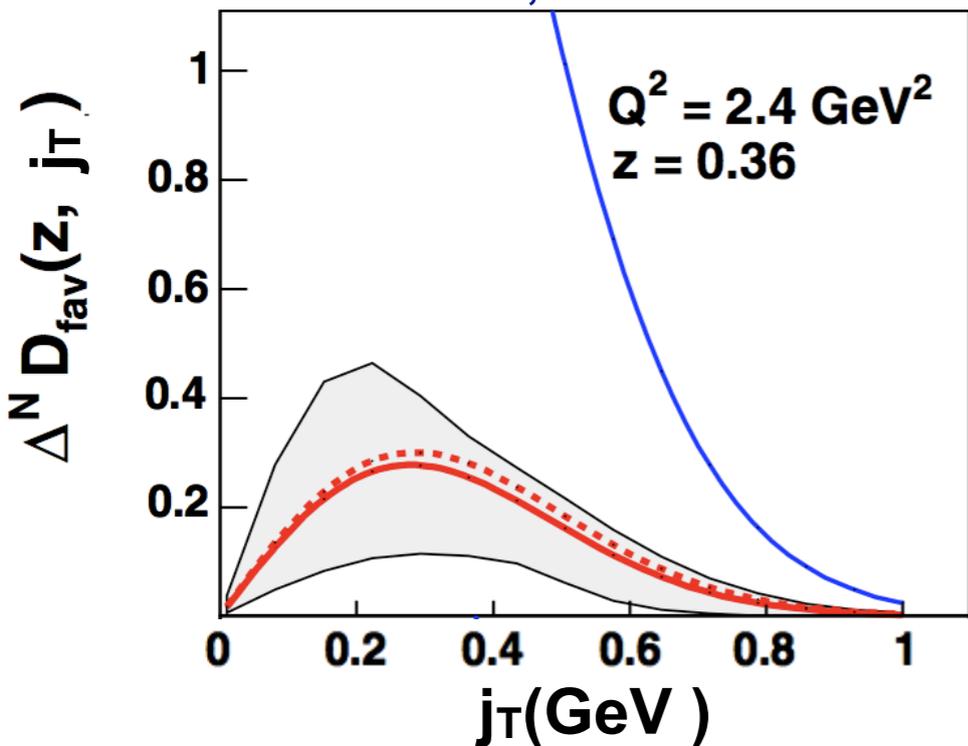
phase space

Extraction of Collins fragmentation function from fit to SIDIS data (HERMES, COMPASS) and Belle Collab. data (KEK) (Anselmino, *et al.*, 2008)



$j_T \equiv$  momentum of  $\pi$  transverse to jet

$\pi^+$ : favored =  $u$ , unfavored =  $d$   
 $\pi^-$ : favored =  $d$ , unfavored =  $u$



$$\frac{d\sigma_{UU}}{d\mathbf{P.S.}} = \sum_{a,b,c} x' f_b(x') x f_a(x) D_c^h(z, j_T) H_{ab \rightarrow cd}$$

$$\frac{d\sigma_{TU}}{d\mathbf{P.S.}} = \sum_{b,q} x' f_b(x') x \delta q(x) \Delta^N D_q(z, j_T) H_{qb \rightarrow qb}^{\text{Collins}}$$

(Unpolarized) quark distributions at  $x \approx 0.2$

Fragmentation functions (Collins, Sivers)

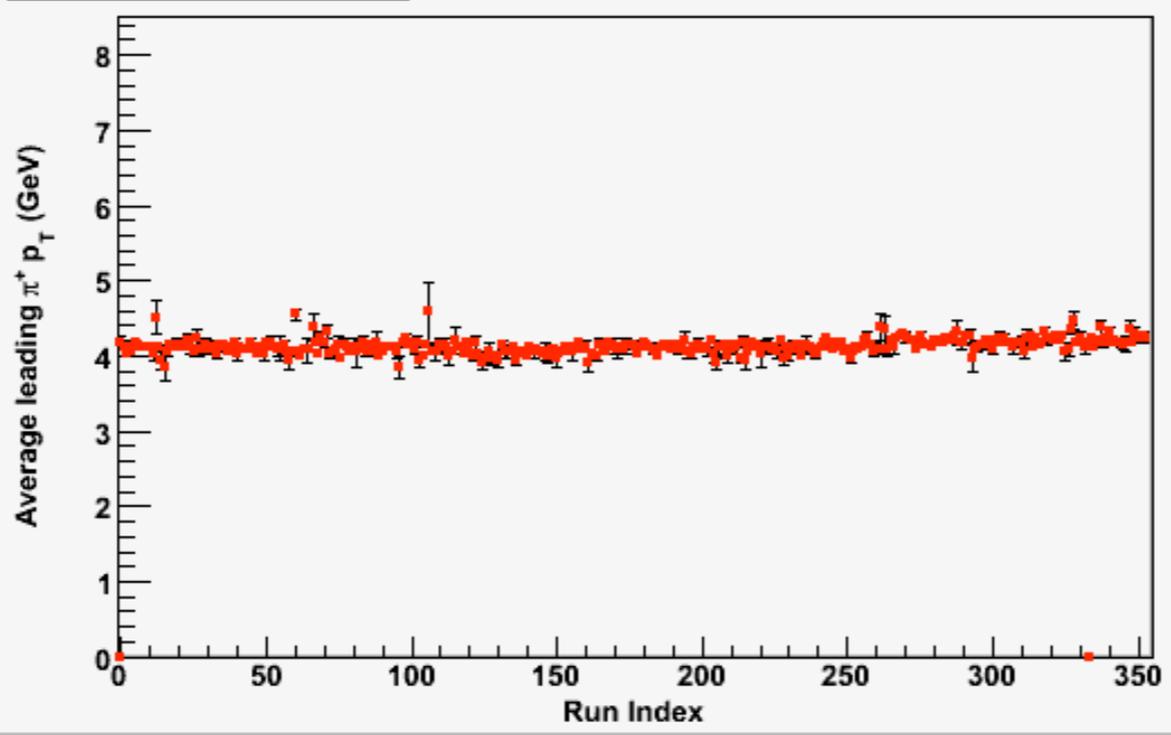
Isospin-favored Collins frag. function

Hard scattering term  $\sim 0.4-0.5$

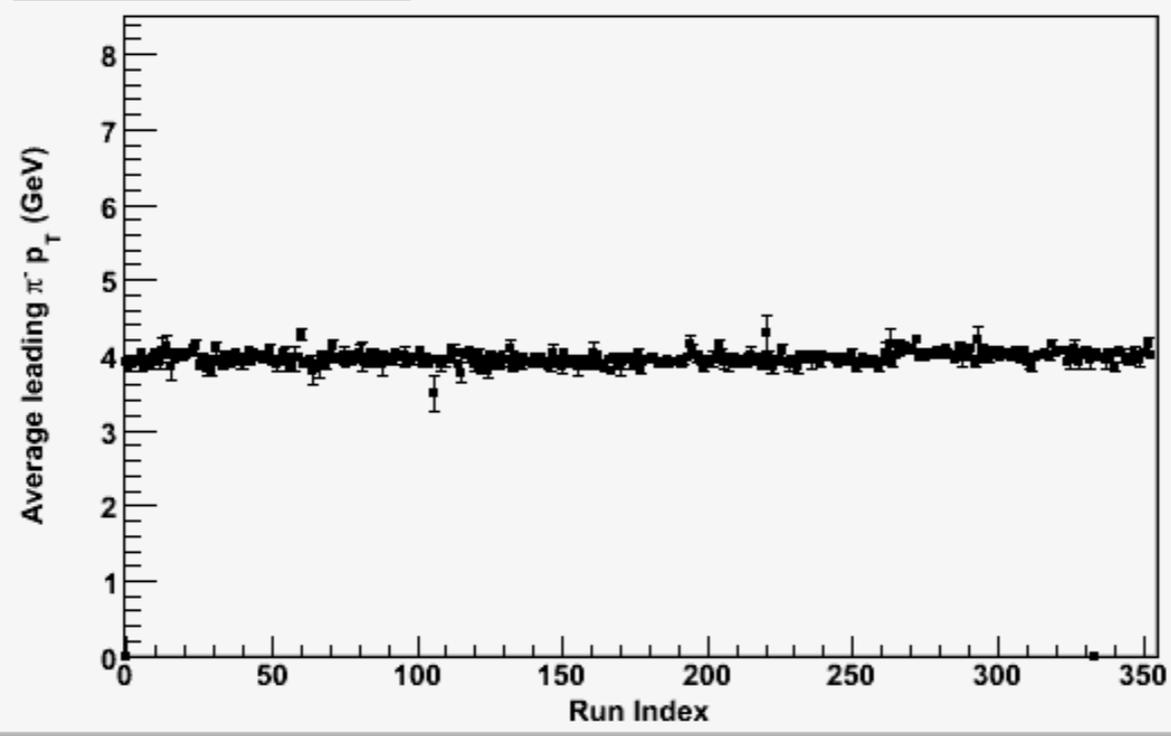
Quark transversity

# Quality Assessment:

Leading  $\pi^+$   $p_T$  by Run

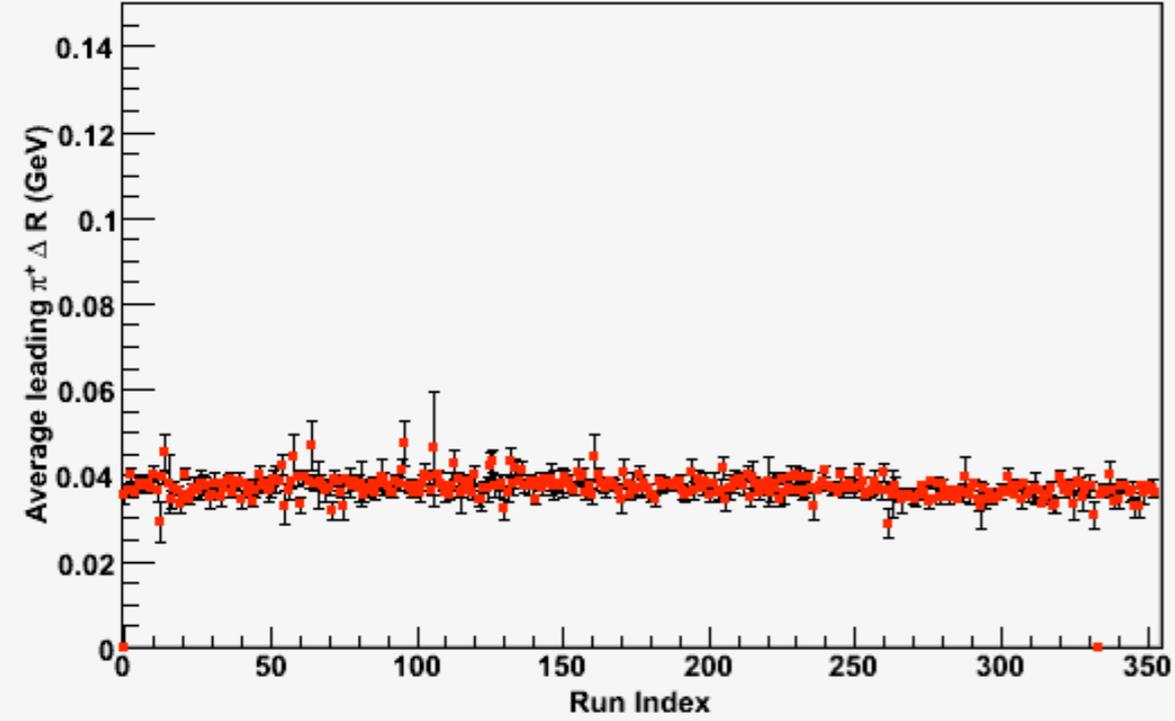


Leading  $\pi^-$   $p_T$  by Run

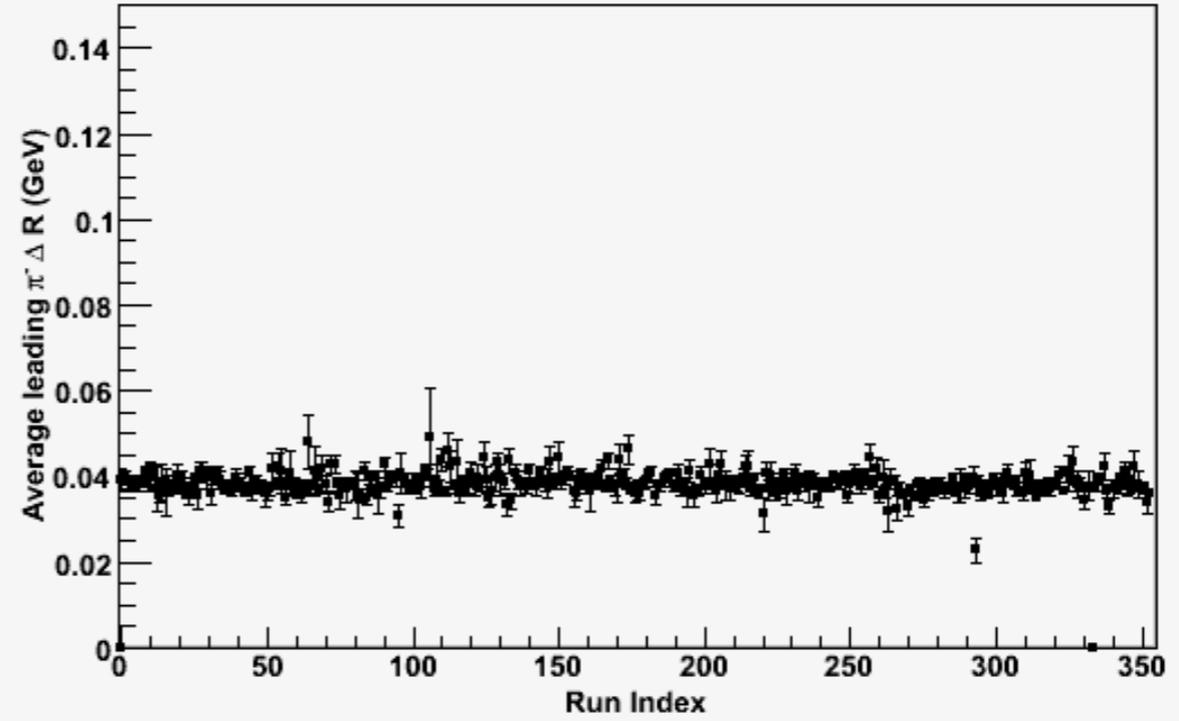


# Quality Assessment:

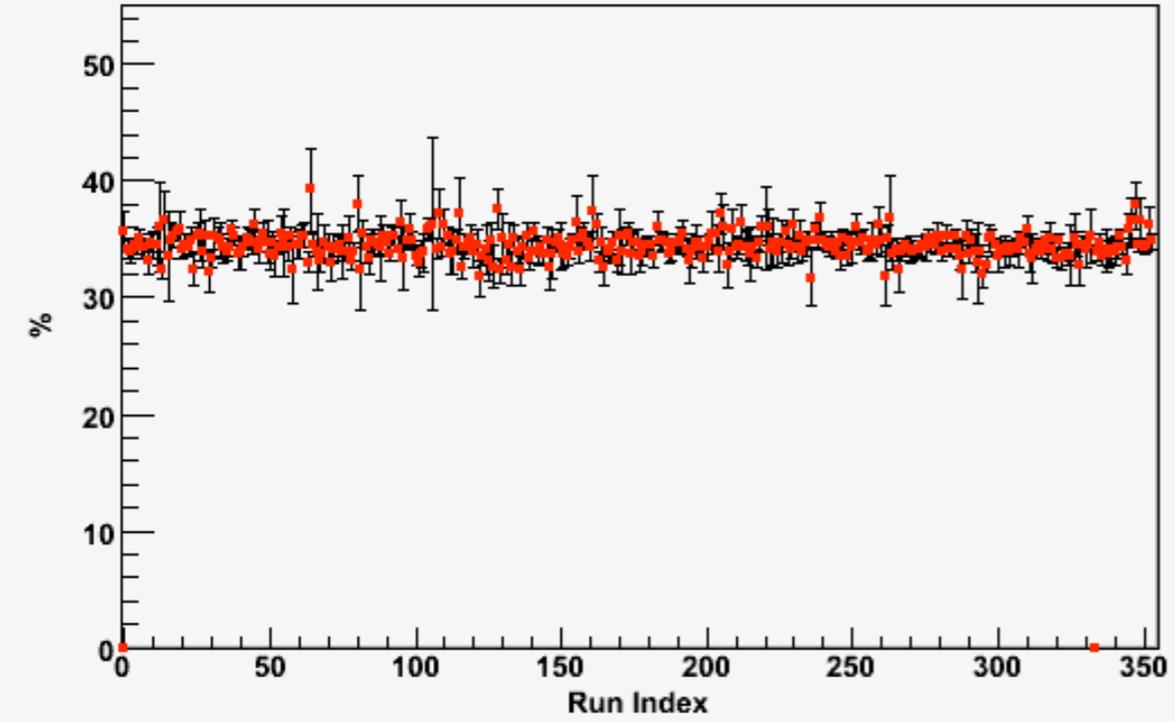
$\pi^+ \Delta R \equiv \Delta \eta^2 + \Delta \phi^2$  by Run



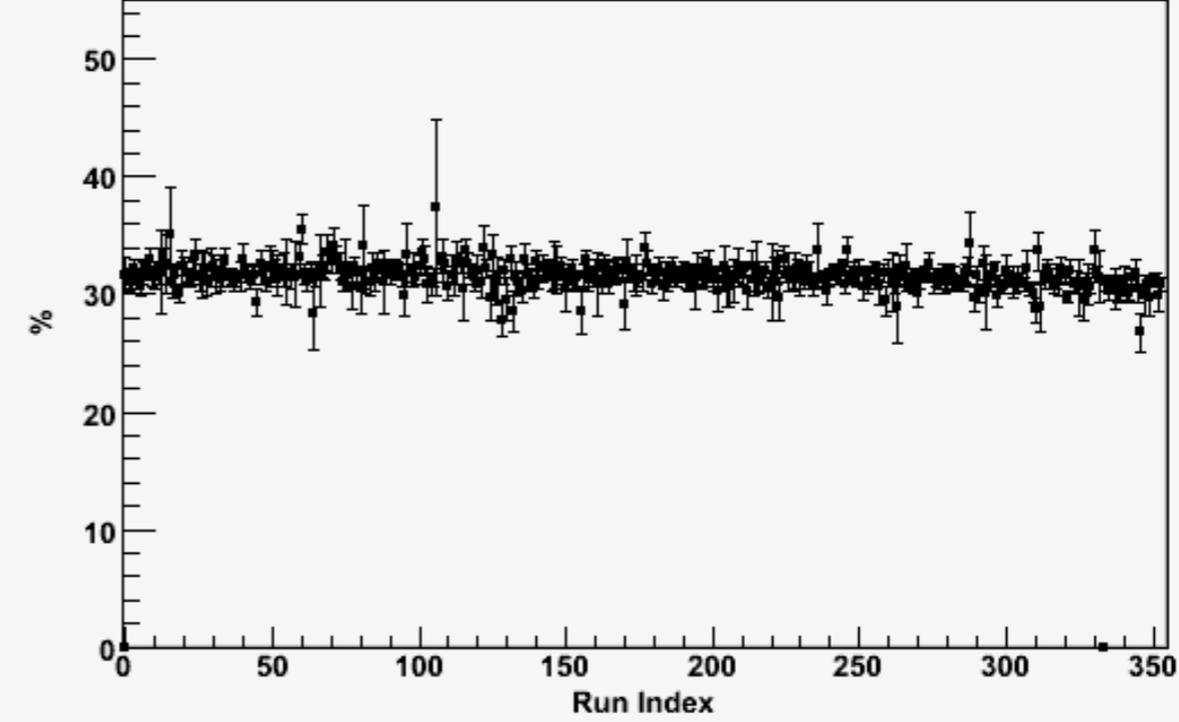
$\pi^- \Delta R \equiv \Delta \eta^2 + \Delta \phi^2$  by Run



% of jets with leading  $\pi^+$



% of jets with leading  $\pi^-$



# Effect on z due to triggering on neutral particles

