

# 1 Multi-dimensional measurements of parton shower 2 in $p+p$ collisions at RHIC

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Jets, collimated sprays of hadrons, serve as an experimental tool for studying parton shower evolution. Differential measurements of jet substructure observables enable the exploration of perturbative and non-perturbative QCD processes. The SoftDrop grooming technique is based on removing soft wide-angle radiation and products of this procedure are substructure observables, such as the shared momentum fraction ( $z_g$ ) and groomed jet radius ( $R_g$ ). We present fully corrected correlations between the  $z_g$  and  $R_g$  at the first split for jets of varying momenta in  $p+p$  collisions at the center of mass energy  $\sqrt{s} = 200$  GeV. To study the evolution along the jet shower, we also present the  $z_g$  and  $R_g$  observables at the first, second, and third splits for various jet momenta. As these novel measurements are presented in three dimensions, we outline the correction procedure so that it can be used as a template for future multi-differential measurements across all experiments.

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## 11 1. Introduction

12 Hard scattered partons in high energy collisions evolve via parton showering and hadroniza-  
 13 tion. Collimated sprays of hadrons created during this evolution are called jets and can  
 14 be defined using jet clustering algorithms. Algorithms used in our analysis are anti- $k_T$   
 15 [1] and Cambridge/Aachen (C/A) [2]. Jet substructure describes the dynamics of quarks  
 16 and gluons inside the jet. Study of jet substructure help us understand the perturbative  
 17 (parton shower) and non-perturbative (hadronization) processes and can be accessed using  
 18 grooming techniques such as SoftDrop [3]. This technique removes wide-angle radiation  
 19 based on the following SoftDrop condition:

$$z_g = \frac{\min(p_{T,1}, p_{T,2})}{p_{T,1} + p_{T,2}} > z_{\text{cut}} \left( \frac{R_g}{R} \right)^\beta, \quad (1)$$

20 where  $p_{T,i}$  is the transverse momentum of the corresponding subjet,  $R$  is the resolution  
 21 parameter of the jet, and  $R_g$  is the distance between the two subjets. There are two free  
 22 parameters in Eq. 1, which we set in our analysis to  $\beta = 0$  and  $z_{\text{cut}} = 0.1$ , where  $z_{\text{cut}}$  is  
 23 momentum fraction cut that reduces sensitivity to non-perturbative effects.

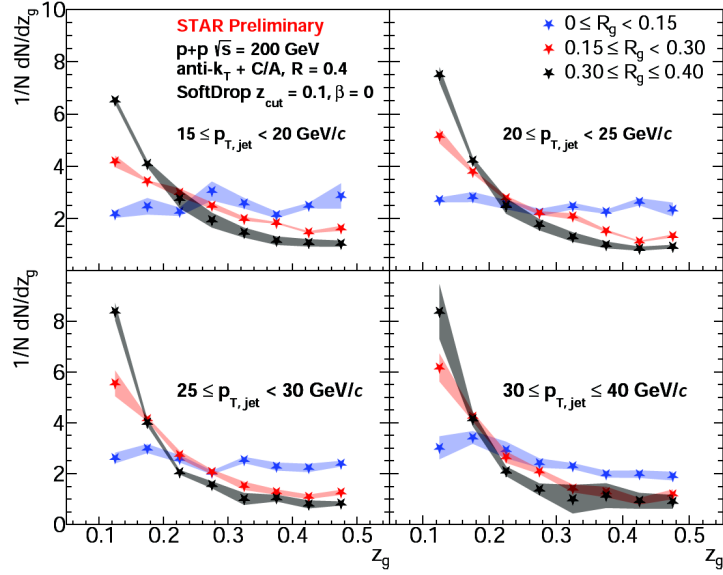
24 Products of the SoftDrop procedure are two observables called the shared momentum  
 25 fraction ( $z_g$ ) and groomed radius ( $R_g$ ). We present two ways to study parton shower using  
 26 these two observables: correlation between  $z_g$  and  $R_g$  at the first split, and the evolution  
 27 of the substructure observables at the first, second, and third splits.

## 28 2. Correlation between $z_g$ and $R_g$ at the first split

29 Data used in this analysis were collected in  $p+p$  collisions at  $\sqrt{s} = 200$  GeV by the  
 30 STAR experiment [4] in 2012. A detailed description of the data and analysis cuts can be  
 31 found in Ref. [5].

32 We need to correct the data for the finite instrumental resolution in order to obtain  
 33 the true particle-level distributions. Our observables lie in 3-dimensional ( $p_{T,\text{jet}}, z_g, R_g$ )  
 34 space, requiring usage of multi-dimensional unfolding techniques. First, we unfold  $z_g$  vs.  
 35  $R_g$  spectra using the 2D Iterative Bayesian unfolding [6] for each detector-level bin in jet  
 36 transverse momentum,  $p_{T,\text{jet}}$ . Then we use the  $p_{T,\text{jet}}$  response matrix where on the x-axis is  
 37 the particle-level  $p_{T,\text{jet}}$  and on the y-axis is the detector-level  $p_{T,\text{jet}}$  to perform the projection  
 38 of each particle-level  $p_{T,\text{jet}}$  bin onto detector-level  $p_{T,\text{jet}}$  bins. We obtain weights from these  
 39 projections and use them for weighting the 2D unfolded  $z_g$  vs.  $R_g$  spectra which are then  
 40 summed. Additional corrections for trigger and jet finding efficiencies are applied as well.

41 Figure 1 shows fully unfolded  $z_g$  distributions for different  $p_{T,\text{jet}}$  bins and  $R = 0.4$ .  
 42 Each color corresponds to different  $R_g$  bin and bands around the data points represent  
 43 systematic uncertainties. We observe a strong dependence of  $z_g$  on  $R_g$  and only a mild  
 44 dependence on  $p_{T,\text{jet}}$ . The  $z_g$  distributions become steeper with larger  $R_g$  which means  
 45 that softer wide-angle splitting is enhanced.



**Figure 1:** Fully unfolded  $z_g$  distributions for three  $R_g$  bins for jets with  $R = 0.4$  in  $p+p$  collisions at  $\sqrt{s} = 200$  GeV. Individual panels correspond to different  $p_{T,\text{jet}}$  intervals (see legend).

### 3. Evolution of the splitting kinematics along the jet shower

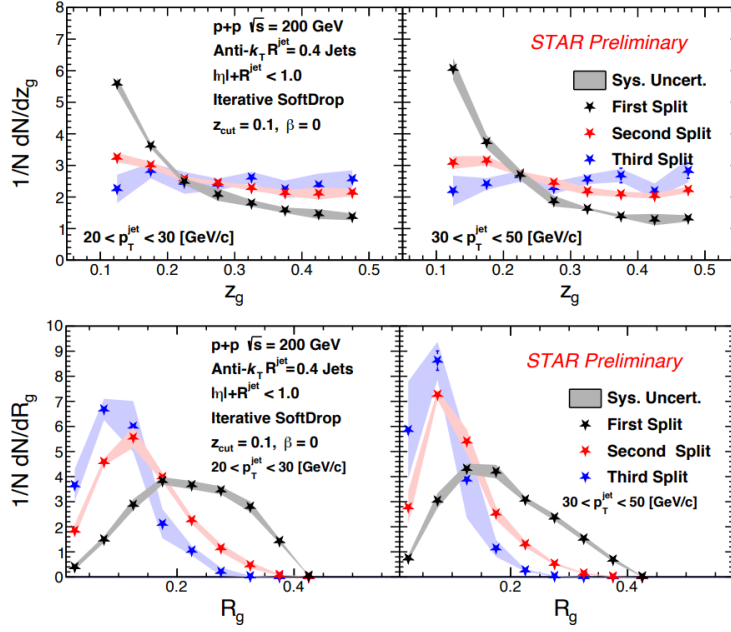
In the second part of our analysis, the evolution of the substructure observables at the first, second, and third splits is studied. The data sample is the same as described in Sec. 2. To study more splits than only the first one we need to use a special variant of the SoftDrop technique called iterative SoftDrop [7].

As in previous case, we need to unfold the data in the 3-dimensional space. In this case, the dimensions are  $z_g$  vs.  $p_{T,\text{jet}}$  vs. split number and  $R_g$  vs.  $p_{T,\text{jet}}$  vs. split number. We use the 2D Iterative Bayesian unfolding to unfold  $z_g$  or  $R_g$  vs.  $p_{T,\text{jet}}$  and then we reconstruct a hierarchy matrix with particle-level splits on the x-axis and detector-level splits on the y-axis. Unfolded distributions are then weighted according to the splitting matching hierarchy and summed.

Fully unfolded  $z_g$  and  $R_g$  distributions for  $R = 0.4$  jets in two different  $p_{T,\text{jet}}$  bins are shown in Fig. 2. Each color corresponds to a different split and bands around the data points represent systematic uncertainties. We observe that the splitting becomes harder and more collinear with increasing split number. As in the previous section, we observe only a mild dependence on  $p_{T,\text{jet}}$ .

### 4. Conclusions

We presented fully unfolded  $z_g$  vs.  $R_g$  as a function of  $p_{T,\text{jet}}$  at the first split, and  $z_g$  and  $R_g$  distributions as a function of  $p_{T,\text{jet}}$  for the first, second, and third splits. We observe that the  $z_g$  distribution at the first split with small  $R_g$  has a similar trend as the  $z_g$  distribution at the third split. We plan to extend our studies to correlations of other



**Figure 2:** Fully unfolded  $z_g$  (top) and  $R_g$  (bottom) distributions for different splits of jets with  $R = 0.4$  in  $p+p$  collisions at  $\sqrt{s} = 200$  GeV. The top and bottom panels are differential in jet  $p_T$  for two bins  $20 < p_T^{\text{jet}} < 30$  GeV/ $c$  (left) and  $30 < p_T^{\text{jet}} < 50$  GeV/ $c$  (right).

67 substructure observables at the first split and  $z_g$  and  $R_g$  observables for various initiator  
 68 prong transverse momentum at the first, second, and third splits.

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