

Exploring the deformation of nuclei with $v_n - \langle p_T \rangle$ correlation from STAR

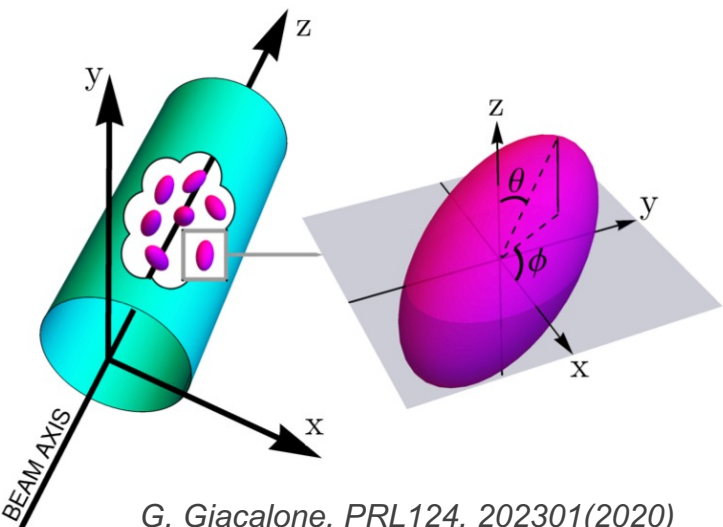
Shengli Huang

Outline:

1. Physics motivations
2. Correlation between v_n and $\langle p_T \rangle$
3. Model comparisons
4. Summary



Deformation and v_2 - $\langle p_T \rangle$ correlation



G. Giacalone, PRL124, 202301(2020)

Nuclear density:
$$\rho(r, \theta) = \frac{\rho_0}{1 + e^{(r-R_0(1+\beta_2 Y_{20}(\theta)))/a}}$$

β_2 of ^{238}U is large

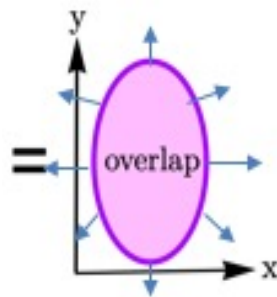
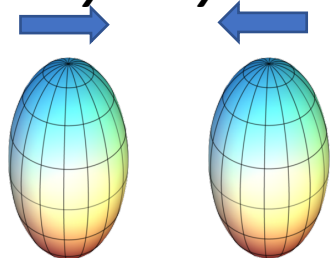
reference	Raman et al.	Löbner et al.	Möller et al.	Möller et al.
method	exp	exp	FRDM	FRLDM
β_2	0.286	0.281	0.215	0.236

β_2 of ^{179}Au is small and can be used as baseline

reference	Möller et al.	Möller et al.	CEA DAM
method	FRDM	FRLDM	HFB
β_2	-0.131	-0.125	-0.10

✓ Deformation is dominated by quadrupole component β_2

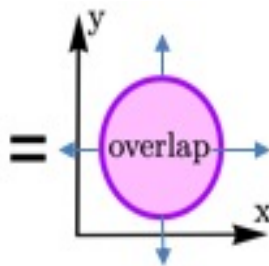
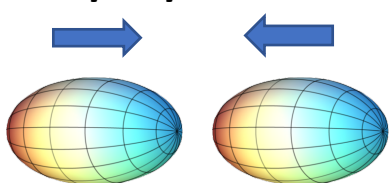
Body-Body



large R , small $\langle p_T \rangle$
large ϵ_2 , large v_2

✓ Deformation has negative contribution on correlation between v_2 and $\langle p_T \rangle$

Tip-Tip

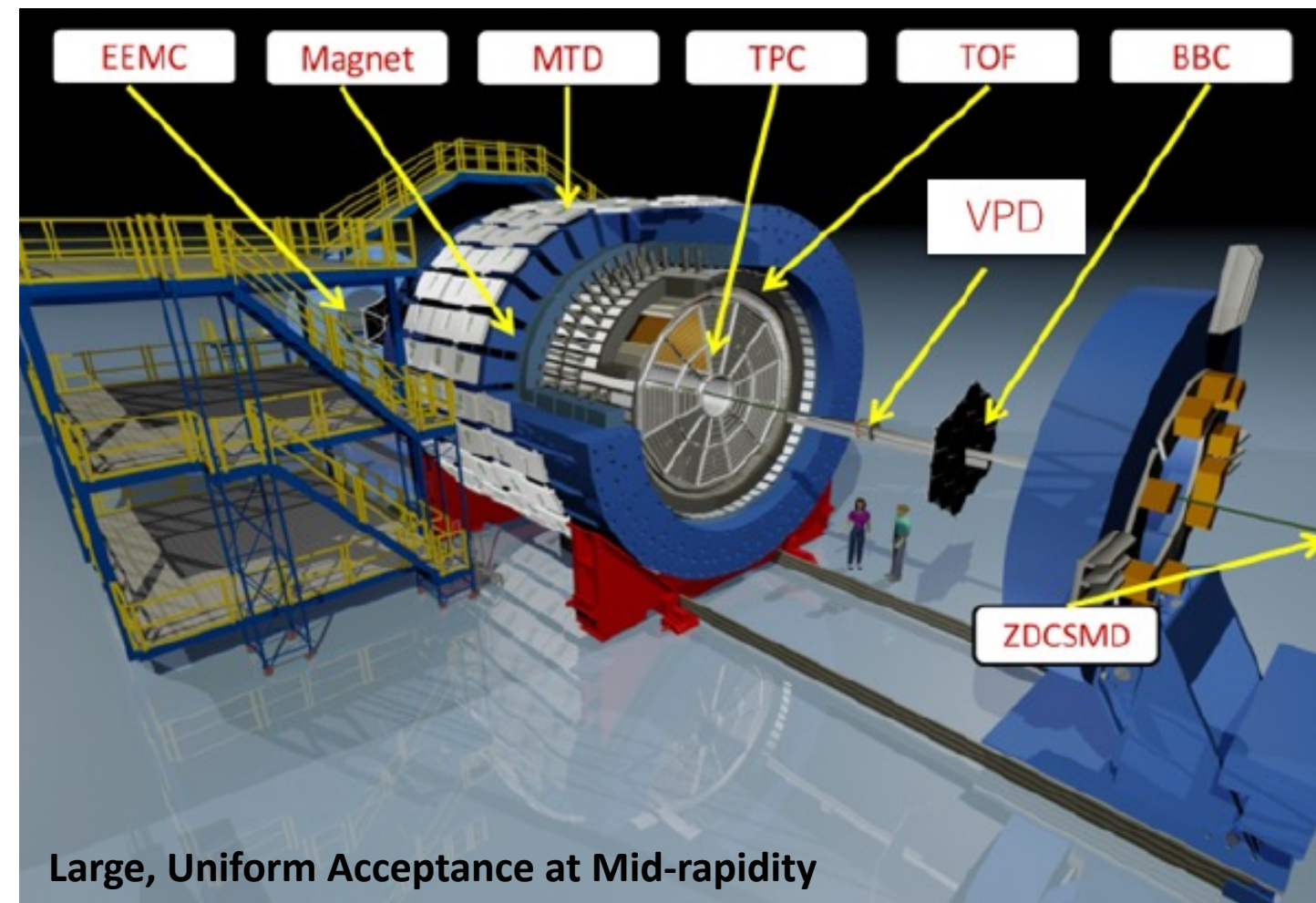


small R , large $\langle p_T \rangle$
small ϵ_2 , small v_2

✓ v_2 - $\langle p_T \rangle$ correlation: A novel tool to reveal the quadrupole deformation at extremely short time scale ($< 10^{-24}\text{s}$).



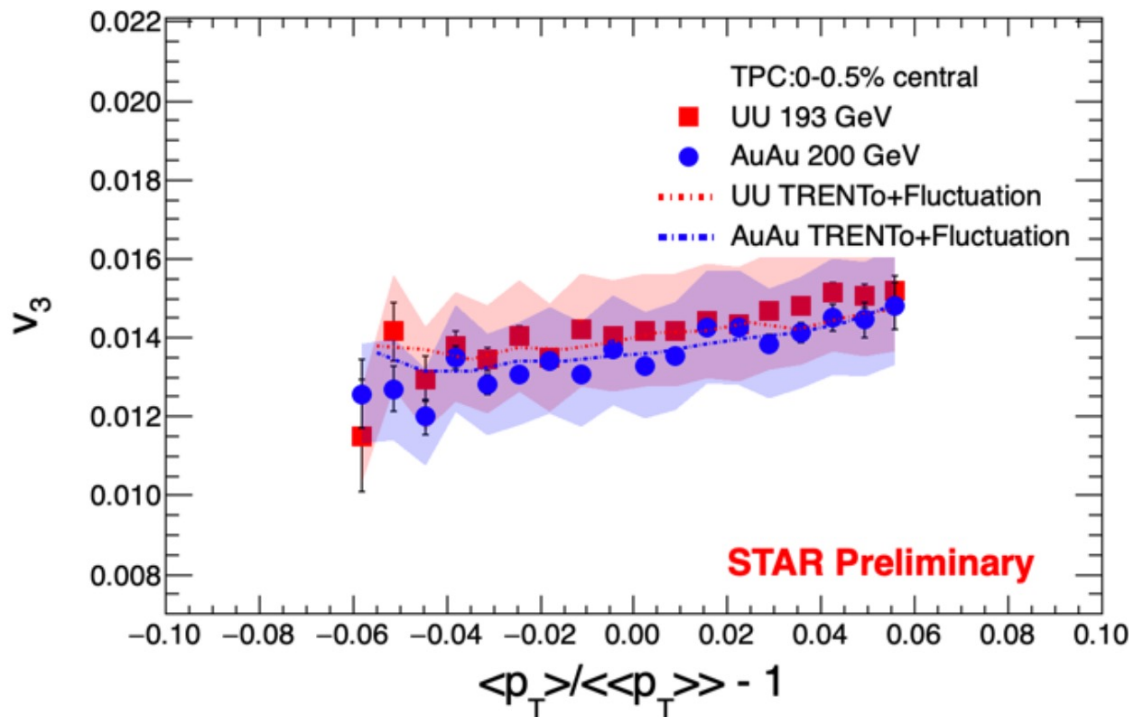
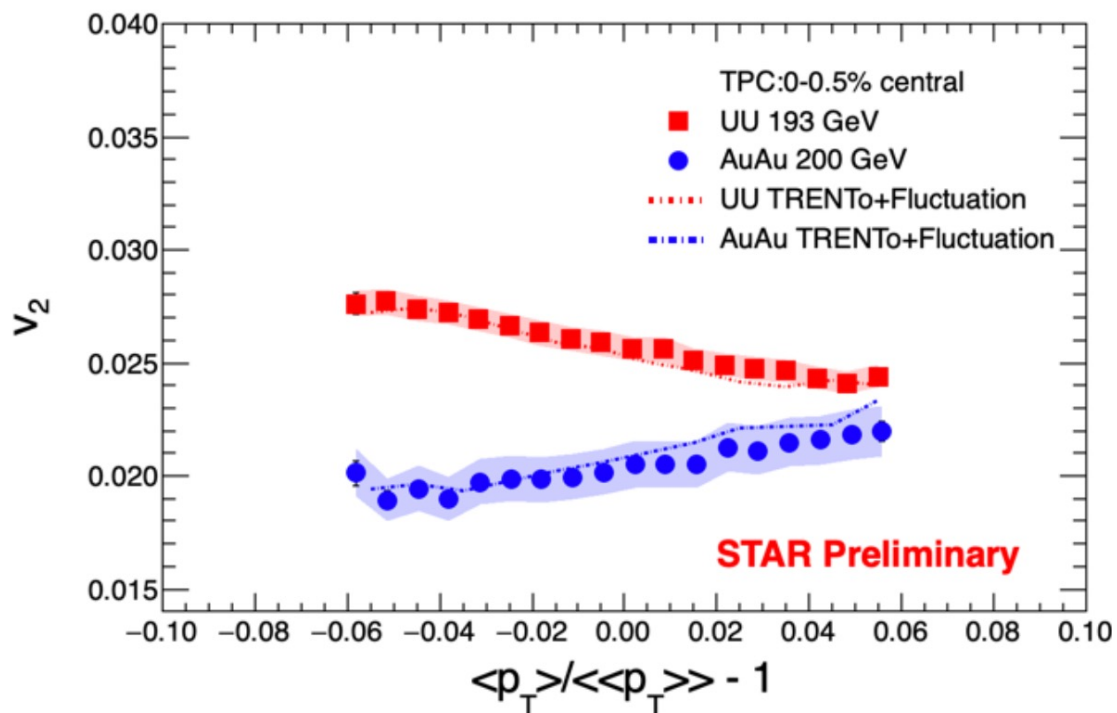
The STAR detector



- $\langle p_T \rangle$ and v_n are measured within $0.2 < p_T < 2.0$ GeV/c and $|\eta| < 1.0$
- Multiplicity are measured within $0.2 < p_T < 2.0$ GeV/c and $|\eta| < 0.5$
- Track efficiency is corrected from embedding data



Event-by-event v_n vs. $\langle p_T \rangle$ in ultra central (0-0.5%) collisions



➤ **Negative correlation** is observed between v_2 and $\langle p_T \rangle$ in central U+U collisions while not in Au+Au \longrightarrow **large deformation in U+U**

➤ $v_3 - \langle p_T \rangle$ correlations are **positive and similar** between Au+Au and U+U

➤ After implementing the statistical fluctuation (due to finite multiplicity), TRENTo model can reproduce the data quantitatively.

v_n	System	slope
v_2	U + U	$-3.5\% \pm 0.1\%$
v_2	Au + Au	$2.6\% \pm 0.2\%$
v_3	U + U	$1.7\% \pm 0.2\%$
v_3	Au + Au	$1.9\% \pm 0.2\%$

**Pearson coefficient: designed to measure dynamical fluctuations**

P. Bozek, PRC93, 044908(2016); B. Schenke et al., PRC102, 034905(2020); G. Giacalone, PRC102, 024901(2020), PRL124, 202301(2020), arXiv:2006.15721; F.G. Gardim et al., PLB809, 135749(2020) ; ATLAS EPJC79, 985(2019)

$$\rho(v_n^2, [p_T]) = \frac{\text{cov}(v_n^2, [p_T])}{\sqrt{\text{Var}(v_n^2)_{\text{dyn}} \langle \delta p_T \delta p_T \rangle}}$$

$$\text{cov}(v_n^2, [p_T]) \equiv \left\langle \frac{\sum_{i \neq j \neq k} w_i w_j w_k e^{in\phi_i} e^{-in\phi_j} (p_{T,k} - \langle p_T \rangle)}{\sum_{i \neq j \neq k} w_i w_j w_k} \right\rangle_{\text{evt}}$$

$$[p_T] \equiv \frac{\sum_i w_i p_{T,i}}{\sum_i w_i}, \langle p_T \rangle \equiv \langle [p_T] \rangle_{\text{evt}}$$

w_i is track weight

$$\text{Var}(v_n^2)_{\text{dyn}} = v_n\{2\}^4 - v_n\{4\}^4$$

$$\langle \delta p_T \delta p_T \rangle = \left\langle \frac{\sum_{i \neq j} w_i w_j (p_{T,i} - \langle p_T \rangle)(p_{T,j} - \langle p_T \rangle)}{\sum_{i \neq j} w_i w_j} \right\rangle_{\text{evt}}$$

Nonflow effect: sub-event method

Standard

$$v_2, p_T \mid \eta \mid < 1.0$$

2-subevent

$$v_2^A \eta < -0.1$$

$$v_2^B \eta > 0.1$$

$$\langle p_T \rangle \mid \eta \mid < 1.0$$

3-subevent

$$v_2^A \eta < -0.35$$

$$\langle p_T \rangle \mid \eta \mid < 0.35$$

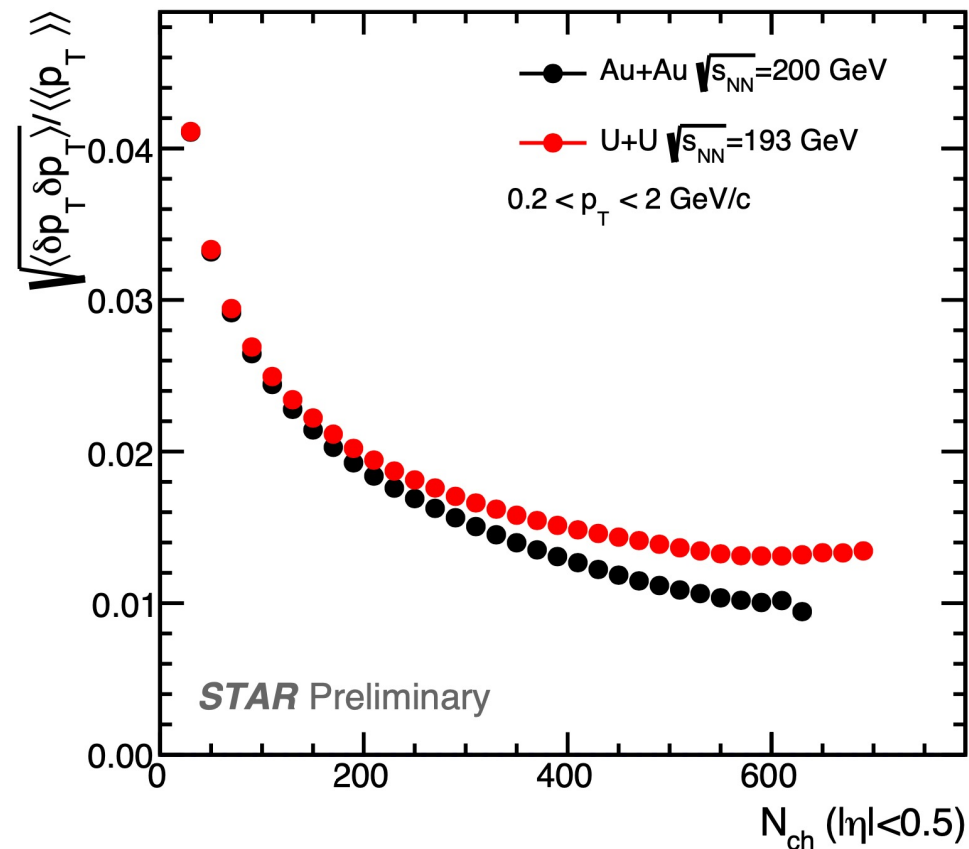
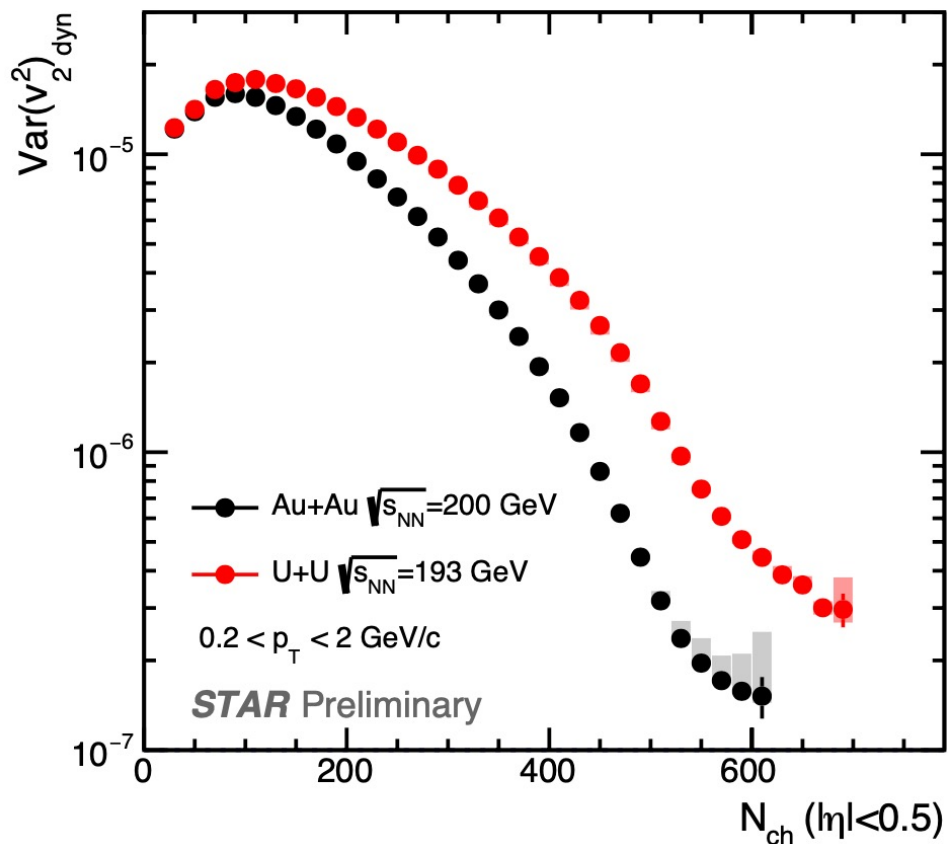
$$v_2^C \eta > 0.35$$



$$\rho(v_n^2, [p_T]) = \frac{\text{cov}(v_n^2, [p_T])}{\sqrt{\text{Var}(v_n^2)_{\text{dyn}} \langle \delta p_T \delta p_T \rangle}}$$

$$\text{Var}(v_n^2)_{\text{dyn}} = v_n\{2\}^4 - v_n\{4\}^4$$

$$\langle \delta p_T \delta p_T \rangle = \left\langle \frac{\sum_{i \neq j} w_i w_j (p_{T,i} - \langle p_T \rangle)(p_{T,j} - \langle p_T \rangle)}{\sum_{i \neq j} w_i w_j} \right\rangle_{\text{evt}}$$



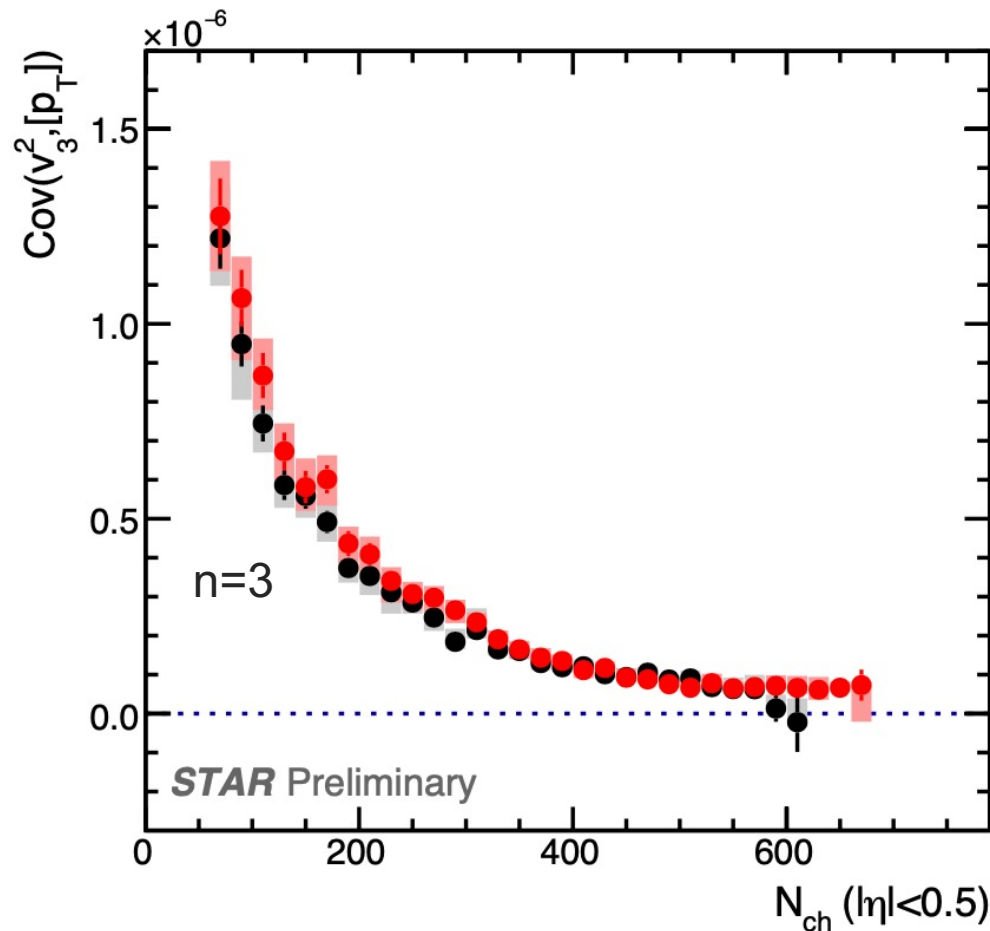
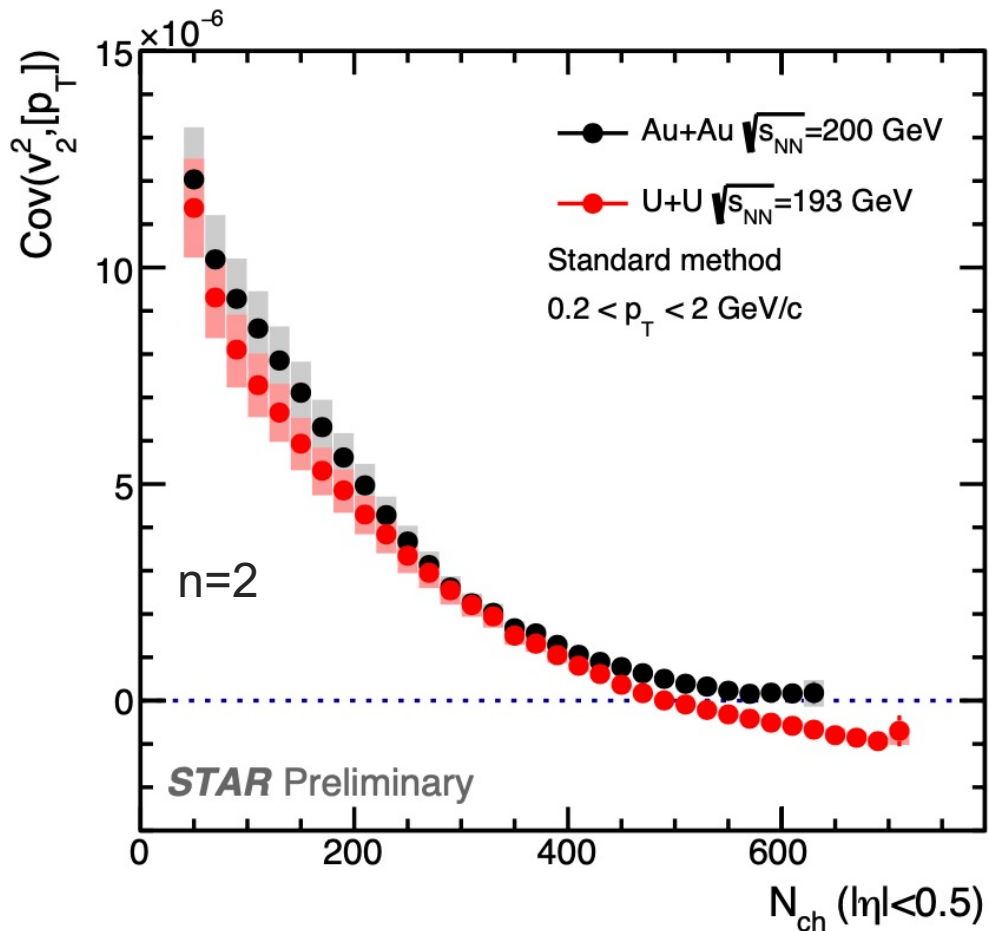
Both flow and $\langle p_T \rangle$ fluctuations affected by nuclear deformation



Covariance $\text{Cov}(v_n^2, [p_T])$

$$\rho(v_n^2, [p_T]) = \frac{\text{cov}(v_n^2, [p_T])}{\sqrt{\text{Var}(v_n^2)_{\text{dyn}} \langle \delta p_T \delta p_T \rangle}} \longrightarrow$$

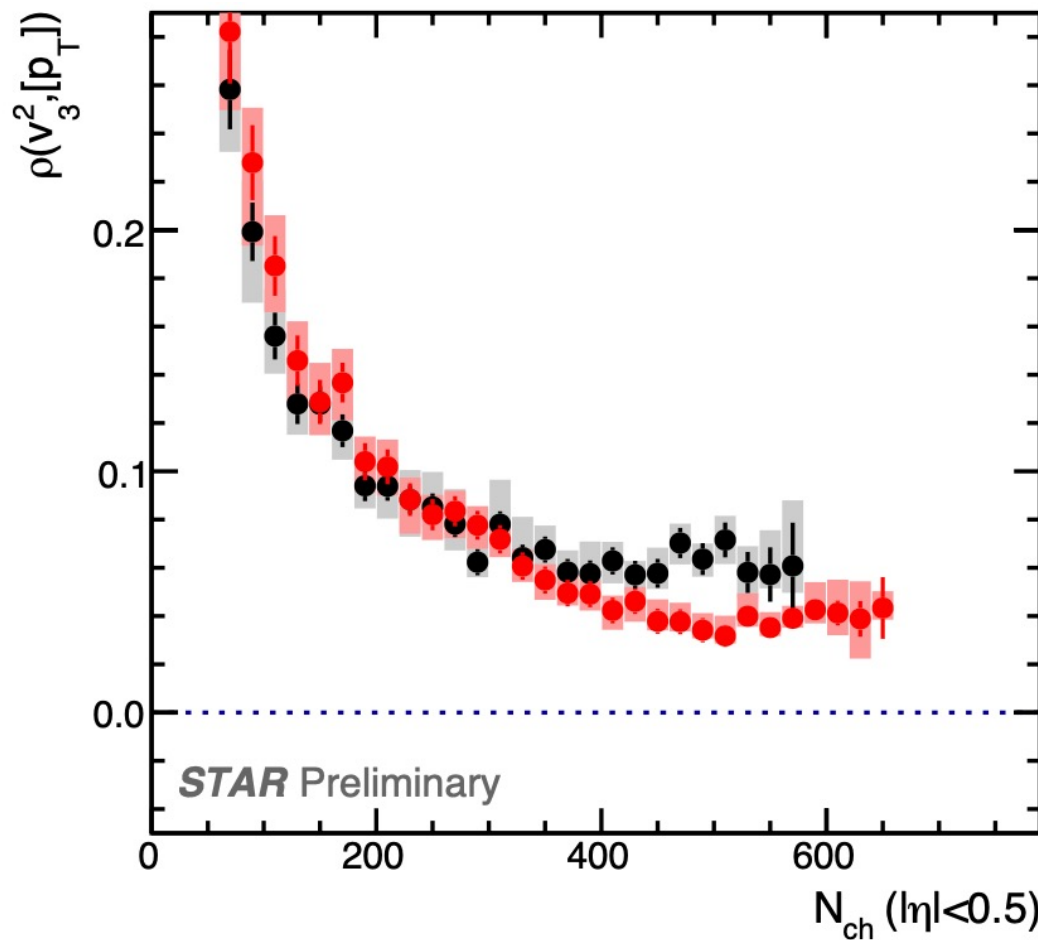
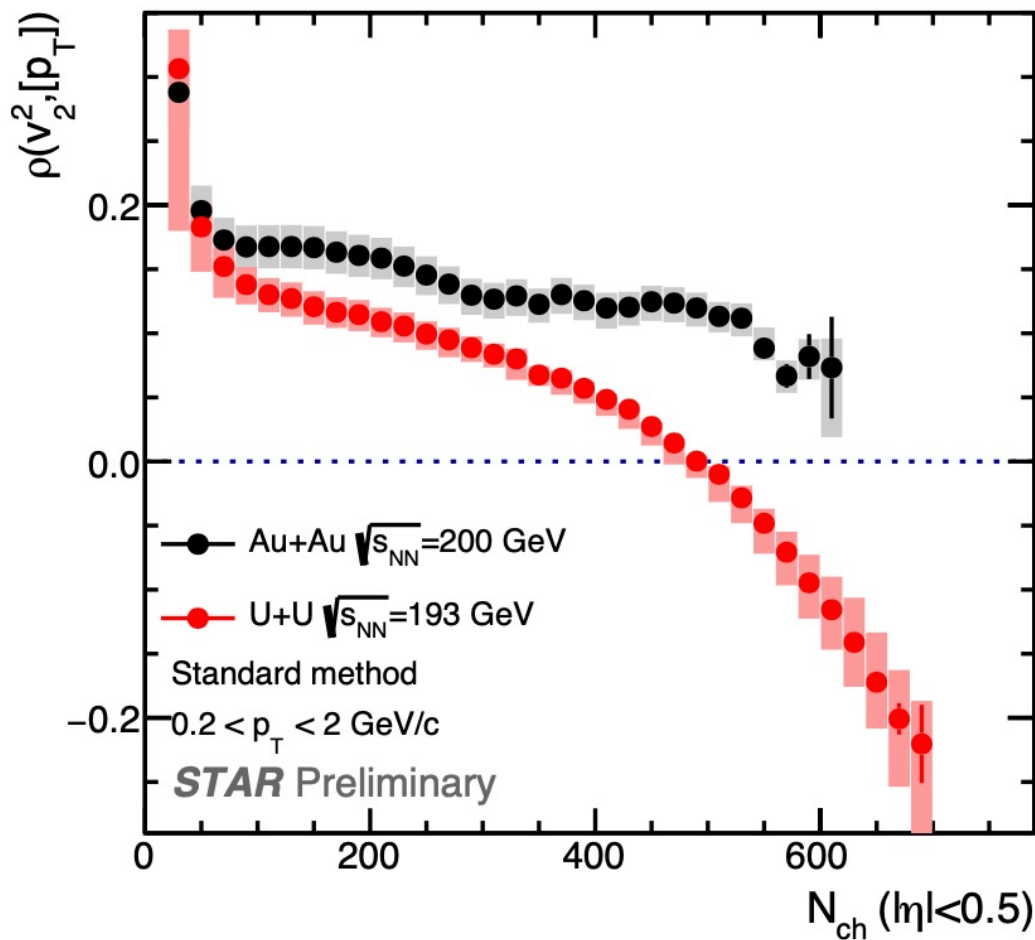
$$\text{cov}(v_n^2, [p_T]) \equiv \left\langle \frac{\sum_{i \neq j \neq k} w_i w_j w_k e^{in\phi_i} e^{-in\phi_j} (p_{T,k} - \langle p_T \rangle)}{\sum_{i \neq j \neq k} w_i w_j w_k} \right\rangle_{\text{evt}}$$



Sign-change for $\text{cov}(v_2^2, [p_T])$ in central U+U as expected from deformation



Pearson coefficient $\rho(v_n^2, [p_T])$

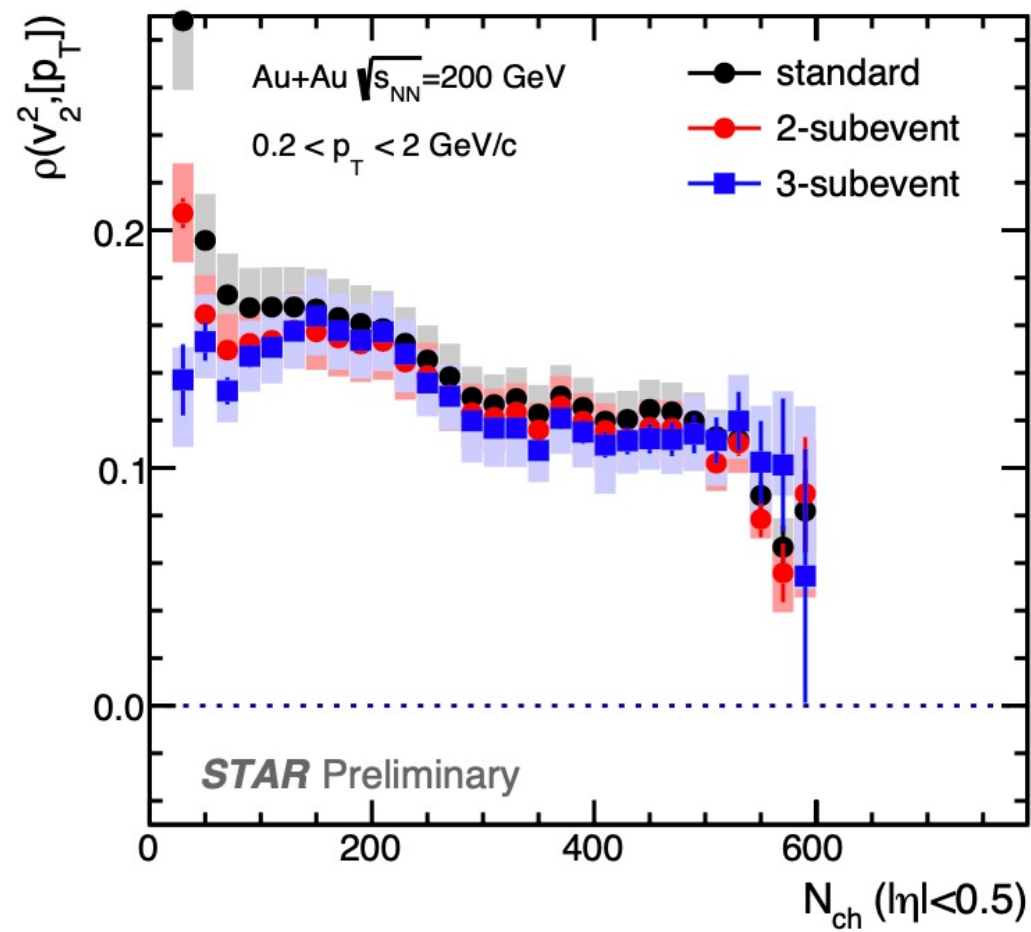
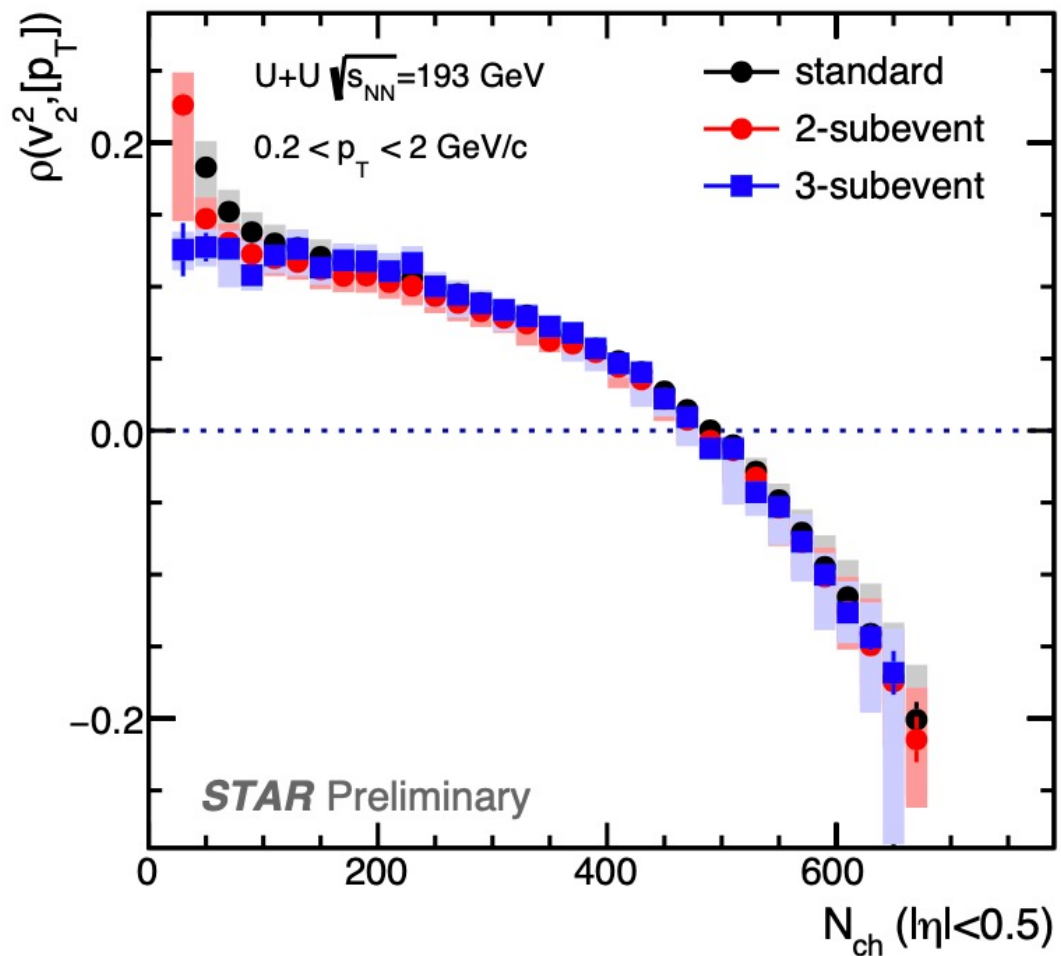


✓ $\rho(v_2^2, [p_T])$ is quite different between central U+U(negative) and Au+Au(positive)

✓ $\rho(v_3^2, [p_T])$ is similar and always positive in Au+Au and U+U collisions



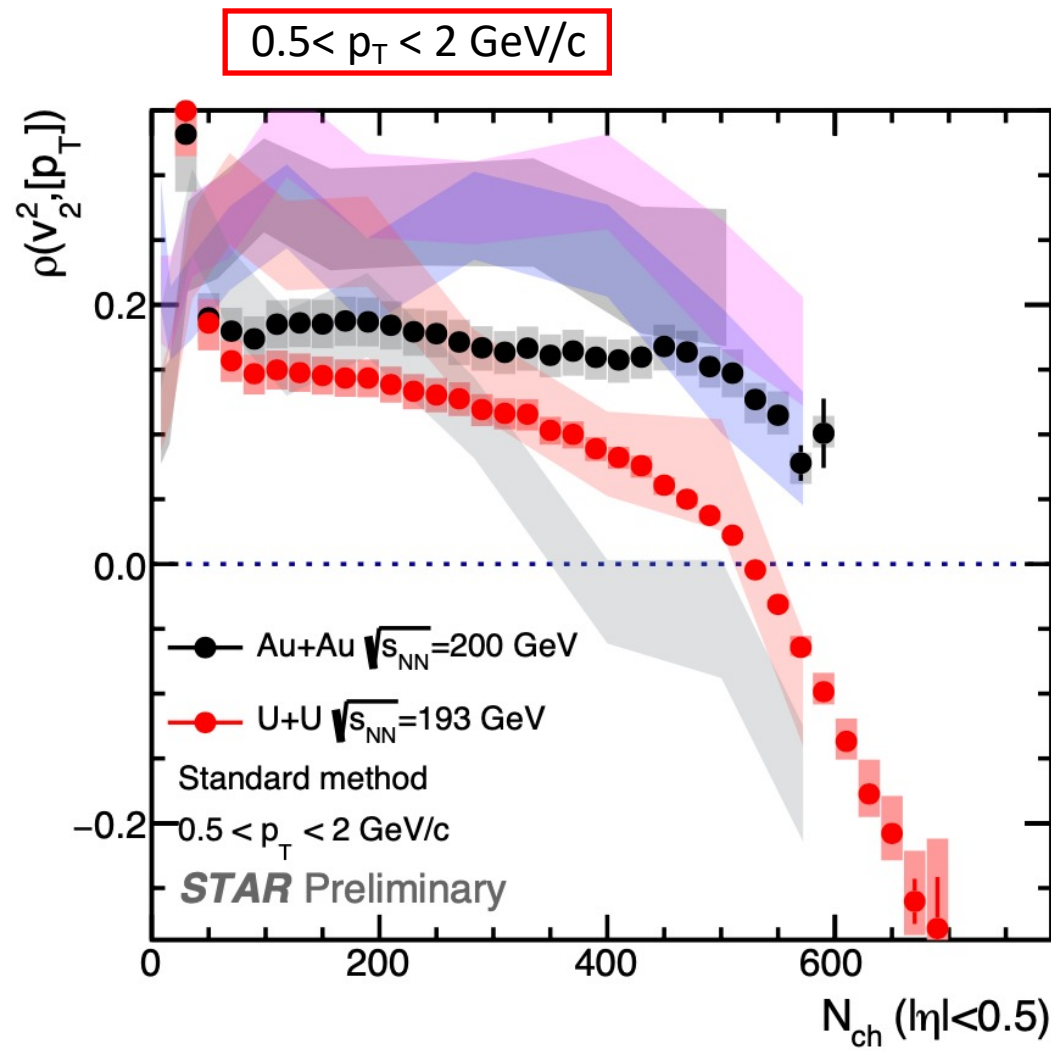
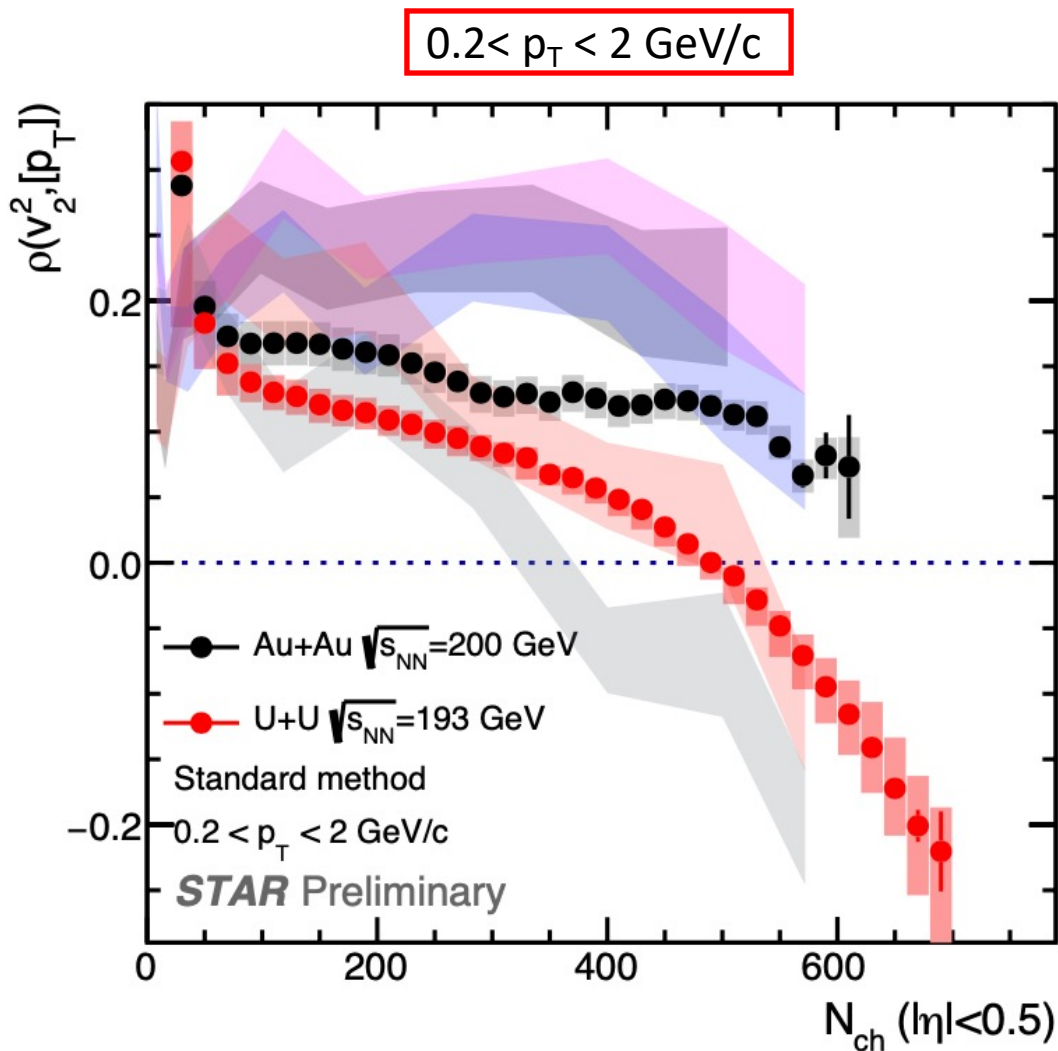
$\rho(v_n^2, [p_T])$ from Sub-Event Method



Sub-event methods indicate non-flow effect is negligible in central AA collisions



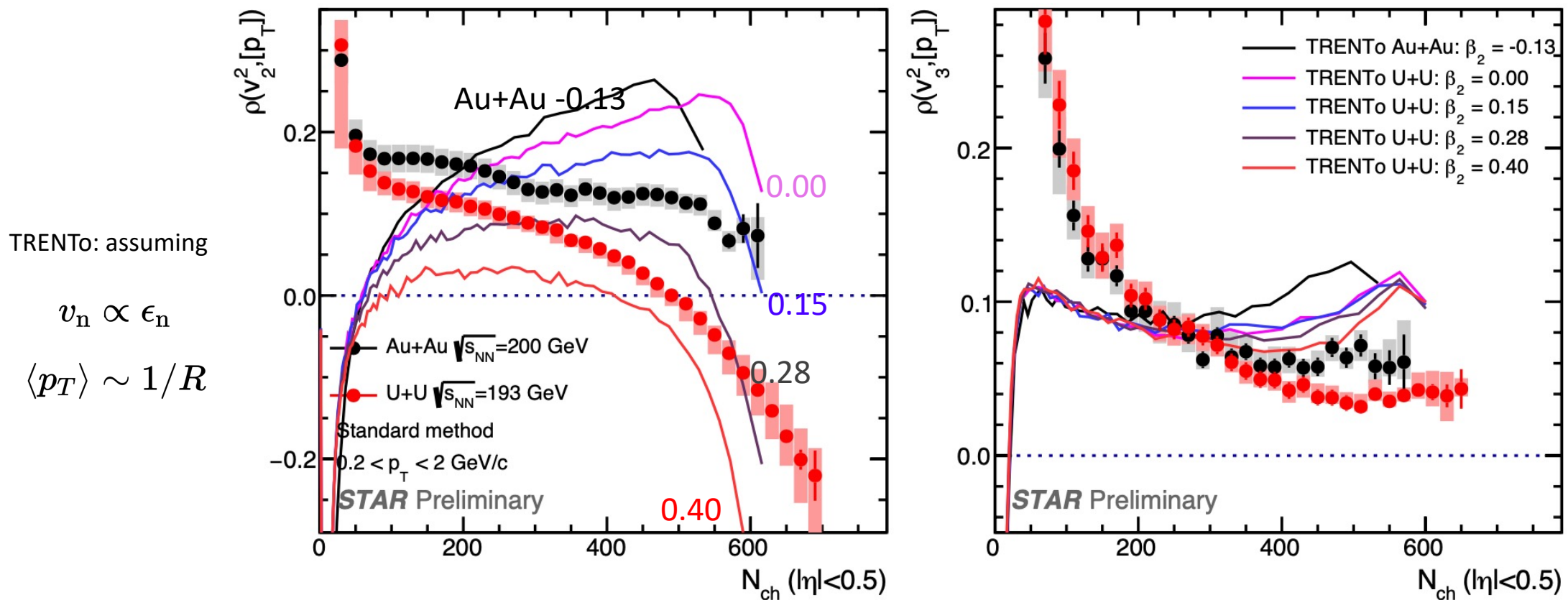
IP-Glasma+Hydro: private calculation provided by Bjoern Schenke (based on B. Schenke, C. Shen, P. Tribedy, PRC102, 044905(2020))



Features for $0.5 < p_T < 2 \text{ GeV}/c$ are same as $0.2 < p_T < 2 \text{ GeV}/c$.



TRENTo: private calculation provided by Giuliano Giacalone (based on PRC102, 024901(2020), PRL124, 202301(2020))



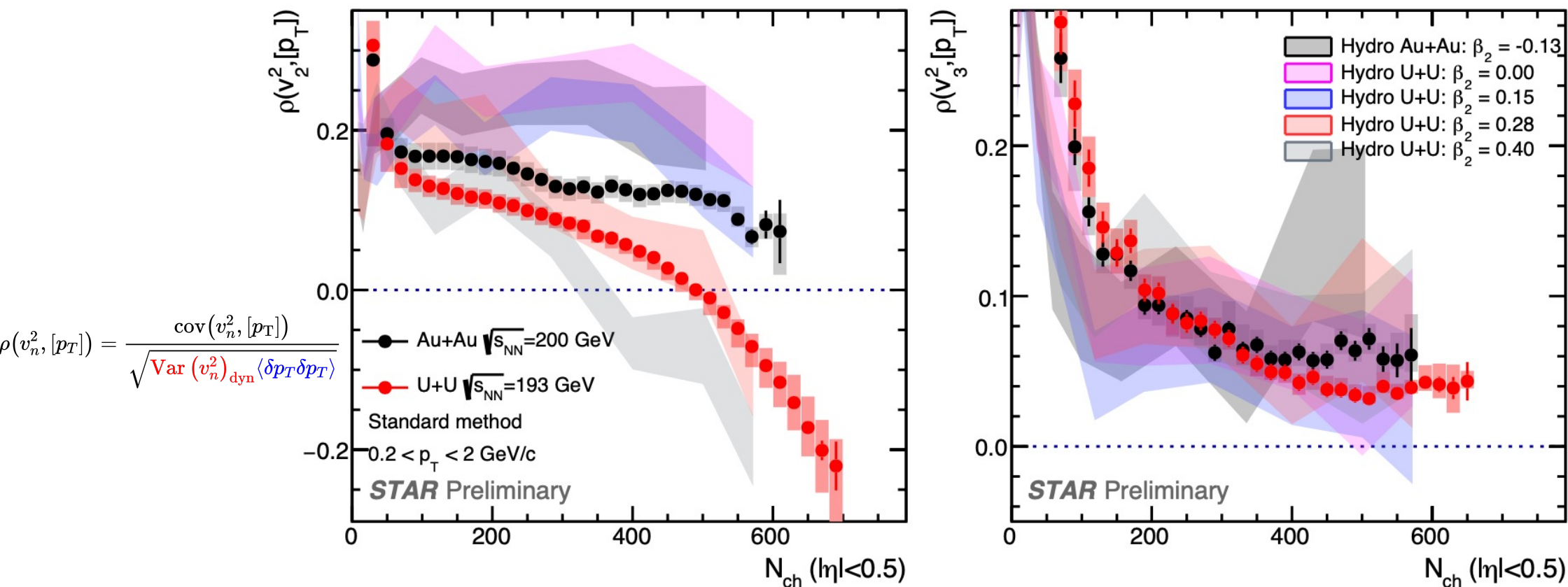
TRENTo fails to describe the STAR data but shows a hierarchical β_2 dependence in U+U collisions.

TRENTo suggests this sign-change in the central collisions could be due to deformation effect.

TRENTo prefers the β_2 value between 0.28 to 0.4 for Uranium



IP-Glasma+Hydro: private calculation provided by Bjoern Schenke (based on B. Schenke, C. Shen, P. Tribedy, PRC102, 044905(2020))

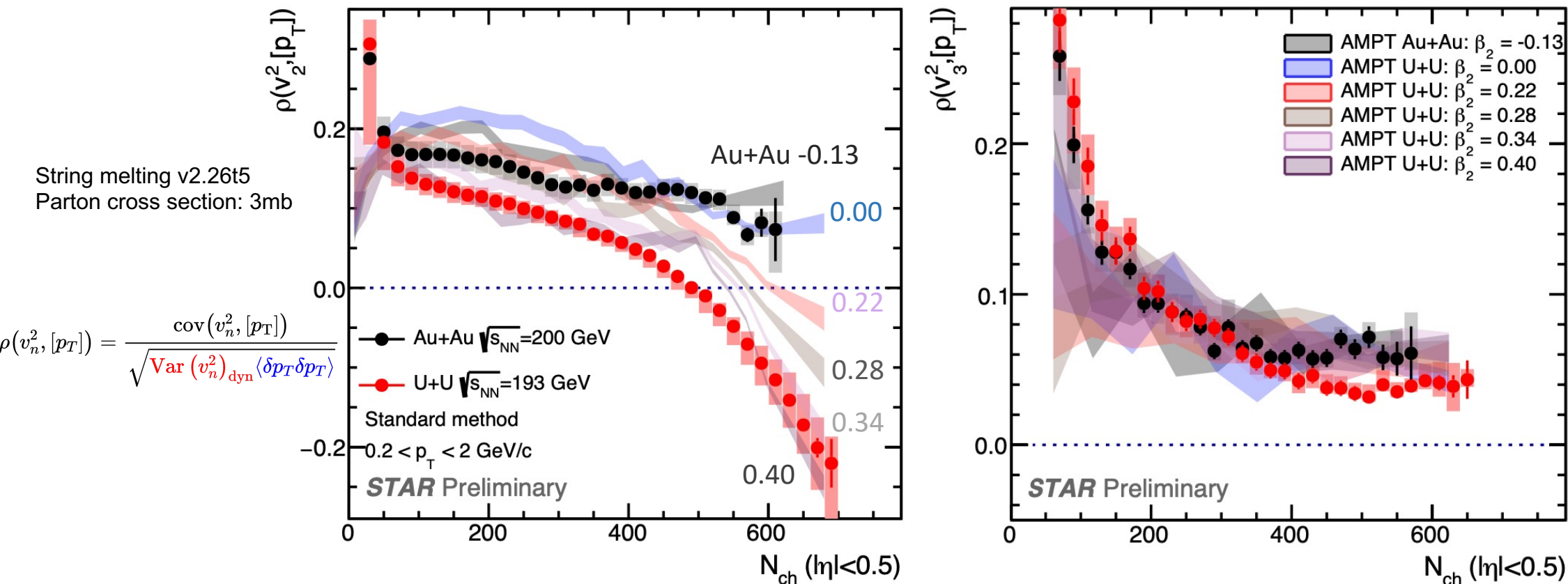


A hierarchical β_2 dependence for $\rho(v_2^2, [p_T])$ while not for $\rho(v_3^2, [p_T])$ in U+U in IP-Glasma

Data comparable to $\beta_2 \sim 0.28$ with IP-Glasma but with large uncertainty

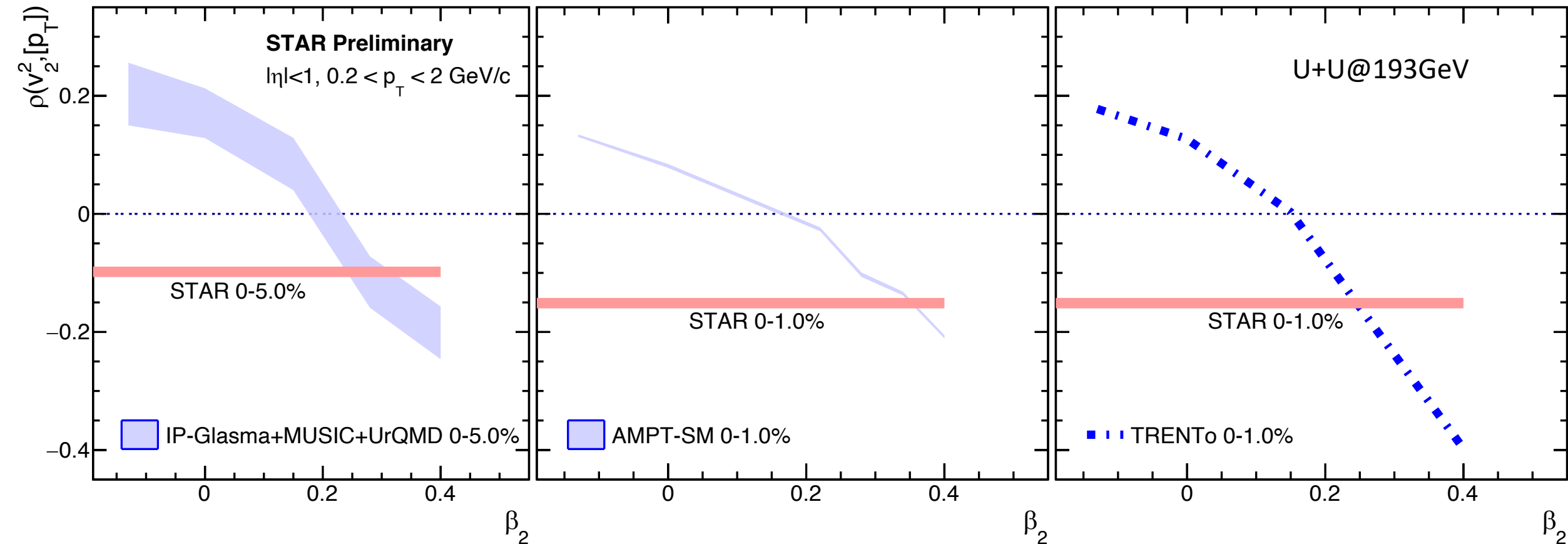


AMPT-SM: Chunjian Zhang, Jianguong Jia et al., arXiv:2105.05713



✓ AMPT allows more precise calculation due to large statistics

✓ β_2 value around 0.34-0.40 by comparing with AMPT



- ✓ β_2 is around 0.2-0.4 for U+U by comparing with three models in central collisions
- ✓ First extraction of the quadrupole deformation at extremely short time scale ($< 10^{-24}\text{s}$) in heavy-ion collisions.



Summary



A sign change of v_2 - p_T correlation is observed in central U+U while not in Au+Au collisions

Nonflow has been studied via sub-event methods and found to be negligible in central collisions

Comparison with several model calculations constrains β_2 in the range of 0.2-0.4 for Uranium

First constraints on quadrupole deformation at extremely short time scale ($< 10^{-24}$ s) accessible through heavy-ion collisions.