# Azimuthal angle dependence of pion femtoscopy in ${ }^{S_{N N}}=200 \mathrm{GeVCu}+A u$ collisions at STAR 

Yota Kawamura<br>for the STAR collaboration<br>October 27th， 2018<br>JPS／APS meeting＠Hawaii

## stai HBT interferometry

- HBT can scope the source size at kinetic freeze-out
$\checkmark$ Measure quantum interference between two identical particles



STAR Collaboration, Phys. Rev. Lett. 87 (2001) 82301

- Experimentally

$$
C(q)=\frac{N(q)}{D(q)} \quad \text { • Event mixing }
$$

N : pair distribution in same event (real)
D: pair distribution in different event (mix)

- Make correlation function as a function of
- Theory

$$
\begin{aligned}
C_{2} & =\frac{P\left(p_{1}, p_{2}\right)}{P\left(p_{1}\right) P\left(p_{2}\right)} \approx 1+\exp \left(-R^{2} Q_{i n v}^{2}\right) \\
\vec{q} & =\overrightarrow{p_{2}}-\overrightarrow{p_{1}} \quad Q_{i n v}=\sqrt{q_{x}^{2}+q_{y}^{2}+q_{z}^{2}-q_{0}^{2}}
\end{aligned}
$$ relative momentum (q)

- We can extract the source radius by fitting with theoretical formula.


## stai 3D HBT radii

- Bertsch-Pratt Parameterization (Phys. Rev. D 33,72 , Phys. Rev. C 37, 1896 (1988) )


$$
\begin{aligned}
& \vec{k}_{T}=\frac{1}{2}\left(\vec{p}_{T 1}+\vec{p}_{T 2}\right) \\
& \vec{q}_{\text {out }} \| \vec{k}_{T} \\
& \vec{q}_{\text {side }} \perp \vec{k}_{T}
\end{aligned}
$$

- 3 dimensional radii use
$\checkmark R_{\text {long }}$ : Source size parallel to the beam direction
$\checkmark$ Rout : Source size parallel to the pair transverse momentum ( $\mathbf{k}_{\mathbf{T}}$ )
$\checkmark R_{\text {side }}$ : Source size perpendicular to $R_{\text {out }}$ and $R_{\text {iong }}$
$\checkmark$ Fitting function:

$$
\begin{aligned}
& C(\vec{q})=N[(1-\lambda)+\lambda K(\vec{q})(1+G(\vec{q}))] \\
& G(\vec{q})=\exp \left(-R_{\text {out }}^{2} q_{o u t}^{2}-R_{\text {side }}^{2} q_{\text {side }}^{2}-R_{\text {long }}^{2} q_{\text {long }}^{2}\right)
\end{aligned}
$$

N : Normalization , $\mathrm{K}(\mathrm{q})$ : Coulomb correction, $\lambda$ : Correlation strength $\checkmark$ Correlation function is expanded to 3 dimensional (out , side and long axis) $\checkmark$ Extract radii parameters 3 dimensionally

## STAR DMPQCTEO TMOM

ALICE Collaboration, Phys. Rev. Lett. 111 (2013) 232302

$\checkmark$ Directed flow is generated by the interaction between spectator and participant particles.
$\checkmark$ Quantified by the 1st harmonic in the Fourier expansion as $\mathbf{v}_{1}$

$$
v_{1}=\left\langle\cos \left(\phi-\Psi_{1}\right)\right\rangle
$$

$\checkmark v_{1}(\eta)$ is crossing 0 by 3 times at around midrapidity, forward and backward rapidity $\checkmark$ The direction of flow have different sign between participant and spectator

## stai HBT radii w.r.t. $\Psi_{1}$

M A Lisa et al. New J. Phys. 13 (2011) 065006


- One can predict one of the origin of directed flow is the "tilt of the medium"
- HBT measurement w.r.t. $\Psi_{1}$ can scope directly this "tilt" by including cross terms in fit function.
$\checkmark$ Fit function with cross term:

$$
\begin{aligned}
& C(\vec{q})=N[(1-\lambda)+\lambda K(\vec{q})(1+G(\vec{q}))] \\
& G(\vec{q})=\exp \left(-R_{\text {out }}^{2} q_{\text {out }}^{2}-R_{\text {side }}^{2} q_{\text {side }}^{2}-R_{\text {long }}^{2} q_{\text {long }}^{2}-2 R_{\text {os }}^{2} q_{o u t} q_{\text {side }}-2 R_{\text {ol }}^{2} q_{\text {out }} q_{\text {long }}-2 R_{\text {sl }}^{2} q_{\text {side }} q_{\text {long }}\right)
\end{aligned}
$$

- Important parameters: $\mathrm{R}_{\mathrm{ol}}, \mathrm{R}_{\mathrm{sl}}$
- If final source is tilted, $\mathrm{R}_{\mathrm{o}}$ and $\mathrm{R}_{\mathrm{sl}}$ cross terms will have oscillation w.r.t. $\boldsymbol{\Psi}_{1}$


## sTAR Motivation

## $\checkmark$ Low energy


$\checkmark$ High energy expectation



Is there a signal?
M A Lisa et al. New J. Phys. 13 (2011) 065006
Tilt angle

$$
\theta_{s}=\frac{1}{2} \tan ^{-1}\left(\frac{-4 R_{s l, 1}^{2}}{R_{l, 0}^{2}-R_{s, 0}^{2}+2 R_{s, 2}^{2}}\right)
$$

- Fit function:

$$
\begin{aligned}
& \mathbf{R}^{2}{ }_{\mu, 0}+2 \mathbf{R}^{2}{ }_{\mu, 1} \cos \left(\varphi-\Psi_{1}\right)+2 \mathbf{R}^{2}{ }_{\mu, 2} \cos \left(2\left(\varphi-\Psi_{1}\right)\right),(\mu=0, s, o l) \\
& \mathbf{R}_{\mu, 0}+2 \mathbf{R}_{\mu, 1}^{2} \sin \left(\varphi-\Psi_{1}\right)+2 \mathbf{R}_{\mu, 2} \sin \left(2\left(\varphi-\Psi_{1}\right)\right),(\mu=o s, s l)
\end{aligned}
$$

- Experimentally, source tilt has been only measured at low energies.
- Tilt angle is inversely proportional to the beam energy
- In RHIC energy ( 200 GeV ), source tilt value is expected nearly 0 or signal is very small. $\checkmark$ Measure HBT w.r.t $\Psi_{1}$ and scope tilt signal using both $A u+A u$ and $C u+A u$ in 200 GeV $\checkmark \mathrm{Cu}+\mathrm{Au}$ have initial density asymmetry...
-> How does it affect HBT measurement?


## star The STAR detector



Time Projection Chamber (TPC)

- Main tracking detector, $|\boldsymbol{\eta}|<1.0$, full azimuth

Zero Degree Calorimeter (ZDC)

- $|n|>6.3$
- Measure spectator neutron
- event plane reconstruction using spectator neutrons

TOF \& TPC detector $\checkmark$ Use PID (particle identification) TPC ( $\mathrm{dE} / \mathrm{dx}$ ) STAR Preliminary


TOF (time of flight)
STAR Preliminary

$\checkmark$ Pion selected Beam-Beam Counters (BBC)

- $3.3<|\eta|<5$
- event plane reconstruction using participants


## sTAR Analysis

- Cu+Au 200 GeV, Au+Au 200 GeV
- Number of events: $\mathrm{Cu}+\mathrm{Au}$ ~ 45 M
$A u+A u \sim 200$ M
- Correlation function

$$
N(q) \quad N: \text { Nair distribution (real) } \quad \begin{array}{llll} 
& -0.1 & 0 & q_{\text {out }}(\mathrm{GeV} / \mathrm{c})
\end{array}
$$




- Estimate coulomb interaction correction factor


## K(q) : coulomb correction

- Fit correlation function and extract radii parameters

$$
C(\vec{q})=N[(1-\lambda)+\lambda K(q)(1+G(\vec{q}))]
$$


$\checkmark$ Azimuthally-integrated analysis $G(\vec{q})=\exp \left(-R_{\text {out }}^{2} q_{\text {out }}^{2}-R_{\text {side }}^{2} q_{\text {side }}^{2}-R_{\text {long }}^{2} q_{\text {long }}^{2}\right)$
$\checkmark$ Azimuthal-angle-dependent HBT analysis
$G(\vec{q})=\exp \left(-R_{\text {out }}^{2} q_{\text {out }}^{2}-R_{\text {side }}^{2} q_{\text {side }}^{2}-R_{\text {long }}^{2} q_{\text {long }}^{2}-2 R_{\text {os }}^{2} q_{o u t} q_{\text {side }}-2 R_{\text {ol }}^{2} q_{o u t} q_{l o n g}-2 R_{\text {sl }}^{2} q_{\text {side }} q_{l o n g}\right)$

- Event plane reconstruction $\checkmark$ ZDC east + west plane used $\checkmark$ ZDC east + west plane is defined based of the sign of ZDC west ( $\eta>0$ ) (with flipped sign of ZDC east ( $\eta<0$ ))



## star $N_{\text {part }}$ dependence

$\checkmark \mathrm{Cu}+\mathrm{Au} 200 \mathrm{GeV}$


$\checkmark$ Comparison of System size



$0.15<k_{\mathrm{T}}<0.25 \mathrm{GeV} / c$

- $\mathrm{Cu}+\mathrm{Au} \sqrt{\mathrm{s}_{N N}}=200 \mathrm{GeV}$
$\star \mathrm{Au}+\mathrm{Au} \sqrt{\mathrm{s}_{N N}}=200 \mathrm{GeV}$
(STAR) Phys. Rev. C 80 (2009) 24905
- $\mathrm{Cu}+\mathrm{Cu} \sqrt{\mathrm{s}_{N N}}=200 \mathrm{GeV}$
(STAR) Phys. Rev. C 80 (2009) 24905
- $\mathrm{N}_{\text {part }}{ }^{1 / 3}$ corresponds to the source radius at the collision time.
- Checked HBT radii $\propto \mathbf{N}_{\text {part }}{ }^{1 / 3}$
- HBT radii have an approximate common linear dependence on $\mathbf{N a r t}^{1 / 3}$ regardless of system size differences.


## star HBT radii w.r.t. $\Psi_{1}$ in $A u+A u$







$\mathrm{Au}+\mathrm{Au} \sqrt{\mathrm{s}_{\mathrm{NN}}}=200 \mathrm{GeV}$ $|\eta|<1$
Centrality 10-50\% $0.15<k_{\mathrm{T}}<0.6 \mathrm{GeV} / \mathrm{c}$ $\pi^{+} \pi^{+}$and $\pi^{-\pi} \pi^{-}$combined

- E.P. resolution correction is not applied
- $\mathbf{R}_{\text {out }}, \mathbf{R}_{\text {side }}$ and $\mathbf{R}_{\text {os }}$ have a $2 n d$-order oscillation due to the elliptic source shape with respect to $\Psi_{1}$
- Small ( but $\neq 0$ ) 1st-order oscillation can be found in $R_{\text {ol }}$ and $R_{\text {sl }}$ due to source tilt signal.
- These results indicate that the source shape at freeze-out is tilted even at top RHIC energy.


## star HBT radii w.r.t. $\Psi_{1}$ in $C u+A u$







$\mathrm{Cu}+\mathrm{Au} \sqrt{\mathrm{s}_{N N}}=200 \mathrm{GeV}$ $|\eta|<1$
Centrality 10-50 \% $0.15<k_{\mathrm{T}}<0.6 \mathrm{GeV} / \mathrm{c}$ $\pi^{+} \pi^{+}$and $\pi^{-} \pi^{-}$combined

- E.P. resolution correction is not applied

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- For all extra radii, oscillation is small as compared to Au+Au results due to poor event plane resolution
- In $\mathrm{R}_{\mathrm{ol}}$, average magnitude is shifted from $\mathbf{0}$ because center of mass rapidity is not $\mathbf{0}$ ( shift to Au-going side ( $\boldsymbol{\eta}<0$ ) )
- Trends are similar to those from Au+Au collisions


## star HBT radii w.r.t. $\Psi_{1}$

$\checkmark \eta$ dependence in $\mathrm{Au}+\mathrm{Au} 200 \mathrm{GeV}$


$\mathrm{Au}+\mathrm{Au} \sqrt{\mathrm{s}_{N N}}=200 \mathrm{GeV}$ Centrality 10-50 \%
$0.15<k_{\mathrm{T}}<0.6 \mathrm{GeV} / c$
$\pi^{+} \pi^{+}$and $\pi^{-} \pi^{-}$combined

- E.P. resolution correction is not applied
- Average $\mathrm{R}_{\mathrm{ol}}$ value has $\boldsymbol{\eta}$ dependence (similar effect is seen in $\mathrm{Cu}+\mathrm{Au}$ results).
- The 1st-order oscillation amplitude does not have significant dependence on $\eta$ -> 1st-order oscillations have same sign in all eta region.
$\checkmark$ Difference between participant and spectator $\Psi_{1}$ planes in Cu+Au 200 GeV


- The 1st-order oscillation sign is opposite
-> The same relation to $\mathrm{v}_{1}$ measurement could be seen.
$\mathrm{Cu}+\mathrm{Au} \sqrt{\mathrm{s}_{N N}}=200 \mathrm{GeV}$
Centrality 10-50\%
$0.2<k_{\mathrm{T}}<1.0 \mathrm{GeV} / \mathrm{c}$
$\pi^{+} \pi^{+}$and $\pi^{-} \pi^{-}$combined
- ZDC east+west
- BBC east+west
- E.P. resolution correction is not applied
- BBC: $v_{1}$ sign is negative ( $3.3<\eta<5$ )
- ZDC: $v_{1}$ sign is positive $(\eta>6.3)$


## star Summary

- Azimuthally integrated HBT radii
$\checkmark$ HBT radii seems to be proportional to $\mathbf{N}_{\text {part }}{ }^{1 / 3}$.
- Azimuthal angle dependence of HBT radii w.r.t. $\Psi_{1}$
$\checkmark$ Source tilt signal has been measured at 200 GeV .
$\checkmark$ Average Rol value can be shifted in case of non-zero center-of-mass rapidity $\checkmark$ The 1st-order oscillation shows opposite sign between event planes defined by participants and spectators


## Outlook

- Perform event plane resolution correction and evaluate tilt angle
- Comparison between Au+Au and Cu+Au collisions quantitatively in azimuthal-angledependent HBT analysis
- Examine beam energy dependence in BES-II with high statistics and good event plane resolution due to installation of Event Plane Detector (EPD)

Back up

## star Data set

## Au+Au 200 GeV using Data set

- Run11 minimum bias
- Events ~ 200 M

Event selection

- $\left|\mathrm{v}_{\mathrm{z}}\right|<25 \mathrm{~cm}$
- $\left|v_{r}\right|<2 \mathbf{c m}$
- $\left|\mathbf{v}_{\mathbf{z}}-\mathbf{v z}_{\mathbf{z}}^{\mathrm{vpd}}\right|<3 \mathrm{~cm}$

Track selection

- $0.15<\mathrm{p}_{\mathrm{T}}<0.8 \mathrm{GeV} / \mathrm{c}$
- $|\eta|<1.0$
- nHitsFit >= 15
- nHitsFit/nHitsPoss >= 0.52
- DCA < 3 cm


## Cu+Au 200 GeV using Data set

- Run12 minimum bias
- Events: ~ 45 M

Event Selection

- $\left|\mathrm{v}_{\mathbf{z}}\right|<30 \mathrm{~cm}$
- $\left|v_{r}\right|<2$ cm
- $\left|\mathbf{v}_{\mathbf{z}}-\mathbf{v}_{\mathbf{z}}^{\mathrm{vpd}}\right|<3 \mathrm{~cm}$ Track selection
- $0.15<\mathrm{Pt}<2 \mathrm{GeV} / \mathrm{c}$ (for $\mathrm{N}_{\text {part }}$ dependence)
- $0.15<\mathrm{Pt}<0.8 \mathrm{GeV} / \mathrm{c}$ (for $\Psi_{1}$ dependence)
- $|\boldsymbol{n}|<1$
- nHitsFit >= 15
- nHitsdEdx >= 10
- nHitsFit/nHitsPoss >= 0.52
- DCA $<\mathbf{3 c m}$


## star $C u+A u$ collisions

STAR Collaboration, Phys. Rev. C 98 (2018) 14915

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    Directed flow
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Participant
Phys. Rev. C 98, 014915

(b) tilted source

+ asymmetric density gradient

(c) tilted source
+ asymmetric participants

$\checkmark \mathrm{Cu}+\mathrm{Au}$ has asymmetric density gradient and it arise "dipole flow".
-> It dump up directed flow signals. (Fig. (b))
$\checkmark$ In addition, $\mathrm{Cu}+\mathrm{Au}$ collisions have a different number of participant between forward and backward directions.
-> It shifts directed flow to the center of mass rapidity (Fig.(c))


## stais Event plane resolution correction

$$
\begin{align*}
& N\left(\boldsymbol{q}, \Phi_{j}\right)=N_{\exp }\left(\boldsymbol{q}, \Phi_{j}\right)+2 \sum_{n=1}^{n_{\text {bin }}} \zeta_{n, m}(\Delta)\left[N_{c, n}^{\exp }(\boldsymbol{q}) \cos \left(n \Phi_{j}\right)\right. \\
& \left.+N_{s, n}^{\exp }(\boldsymbol{q}) \sin \left(n \Phi_{j}\right)\right],  \tag{44}\\
& \zeta_{n, m}(\Delta)=\frac{n \Delta / 2}{\sin (n \Delta / 2)\left\langle\cos \left(n\left(\psi_{m}-\psi_{R}\right)\right)\right\rangle_{p}}-1 . \quad(45) \underset{\operatorname{Res}\left\{\Psi_{\mathrm{m}}\right\}}{ } \mathrm{e} \\
& N_{s, n}^{\exp }(\boldsymbol{q}) \equiv\left\langle N_{\exp }(\boldsymbol{q}, \Phi) \sin (n \Phi)\right\rangle \\
& =\frac{1}{n_{\text {bin }}} \sum_{j=1}^{n_{\text {bin }}} N_{\text {exp }}\left(\boldsymbol{q}, \Phi_{j}\right) \sin \left(n \Phi_{j}\right), \quad=\frac{1}{n_{\text {bin }}} \sum_{j=1}^{n_{\text {bin }}} N_{\exp }\left(\boldsymbol{q}, \Phi_{j}\right) \cos \left(n \Phi_{j}\right), \\
& \text { - The correction is performed to } \\
& q \text { distribution } \\
& \text { ( } \mathrm{N} \text { denotes the count of each qbin) } \\
& N_{c, n}^{\exp }(\boldsymbol{q}) \equiv\left\langle N_{\exp }(\boldsymbol{q}, \Phi) \cos (n \Phi)\right\rangle
\end{align*}
$$

- Correlation of event planes with different orders (e.g. 1st - 2nd ) should be taken into account.

