

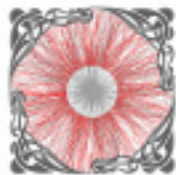


# Systematics of Kinetic Freeze-out Properties in High Energy Collisions from STAR

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## Outline:

- Introduction & Motivation
- STAR Experiment and Particle Identification
- Invariant Yields and Average Transverse Mass
- Blast Wave Fits
- Summary

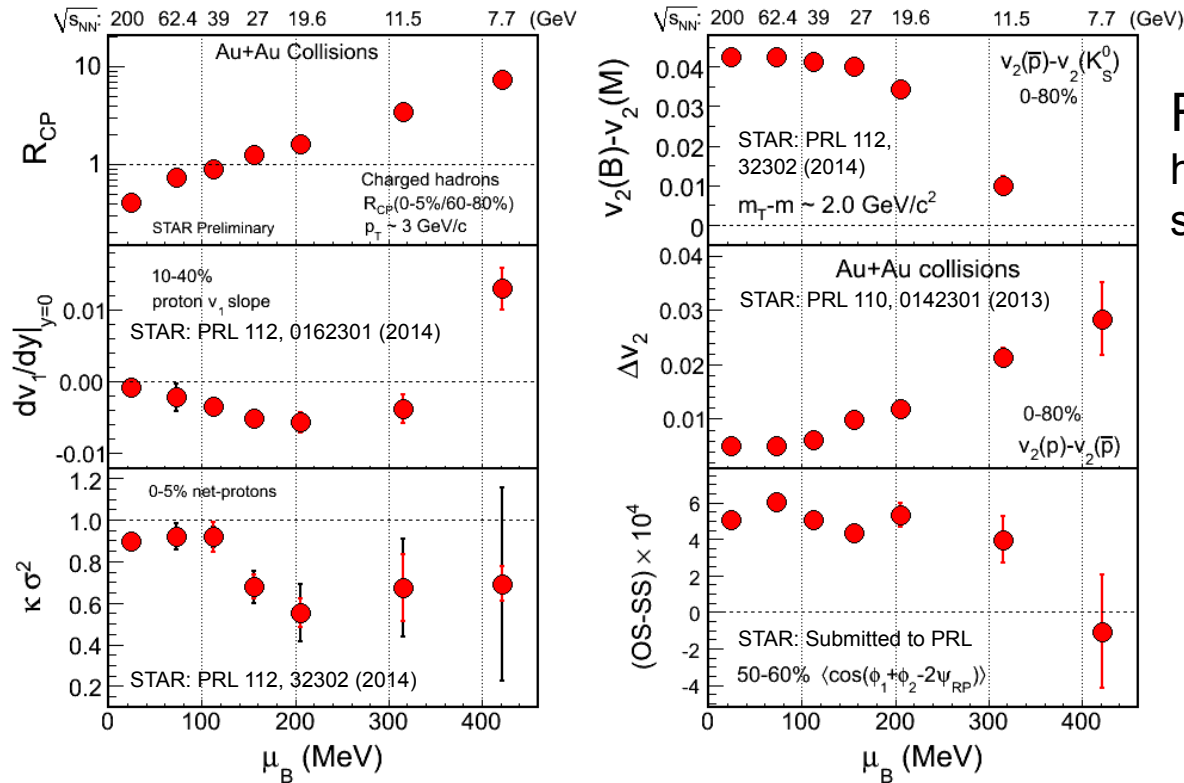


# RHIC BES Program: Motivation

- Explore QCD Phase Diagram: - Search signals of possible phase boundary  
 - Search for softening of EOS  
 - Search for the possible QCD **Critical Point**

## BES-I findings:

Many interesting features as a function of beam energy/chemical potential



Ref: STAR BES white paper  
<https://drupal.star.bnl.gov/STAR/starnotes/public/sn0598>

## This Talk:

Detailed study of kinetic freeze-out parameters



# Freeze-out in Heavy-ion

## Chemical Freeze-out:

Inelastic collisions among particles cease

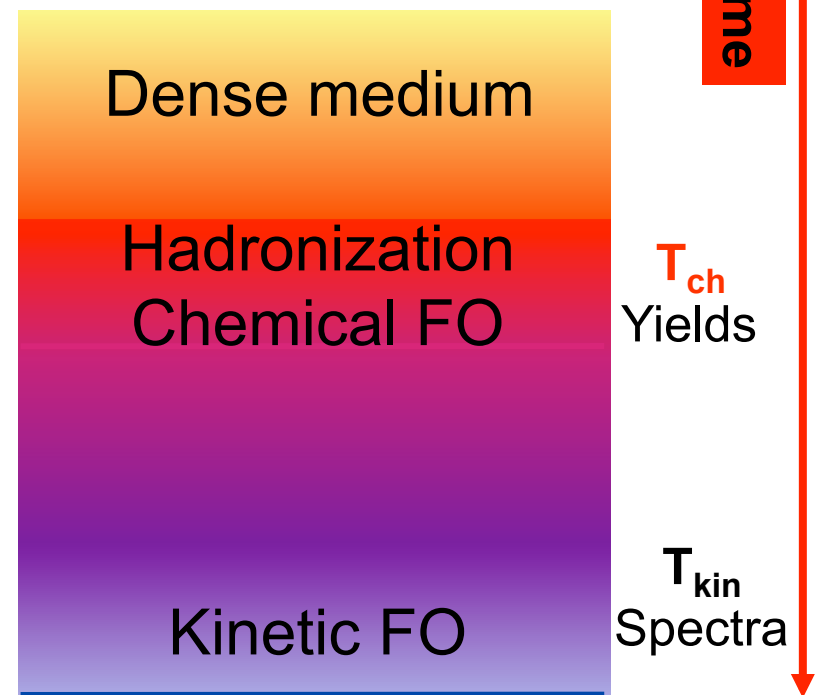
- Particle yields and ratios get fixed
- Chemical freeze-out temperature and baryonic chemical potential

## Kinetic Freeze-out:

Elastic collisions among particles cease

- Particle spectral shapes get fixed
- Kinetic freeze-out temperature and average transverse flow velocity

Single (chemical) freeze-out scenario:

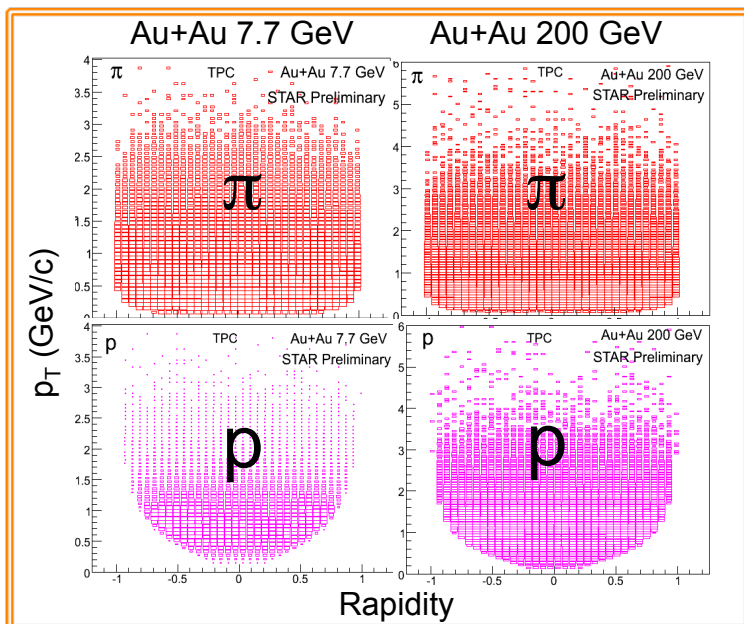
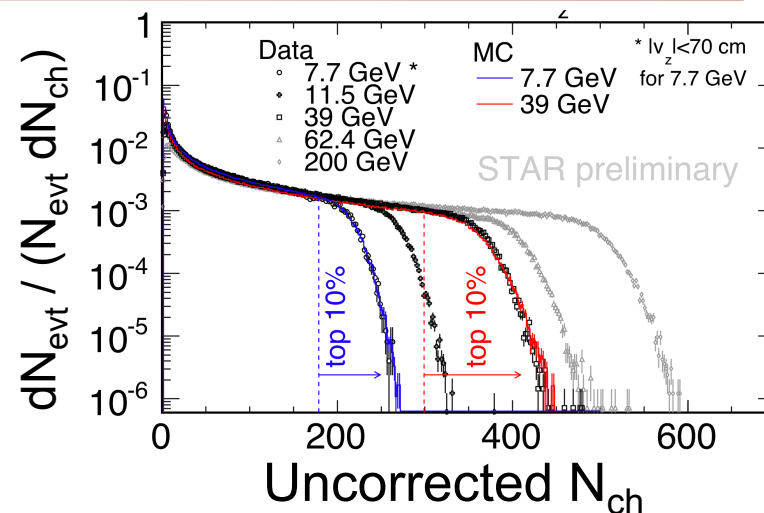
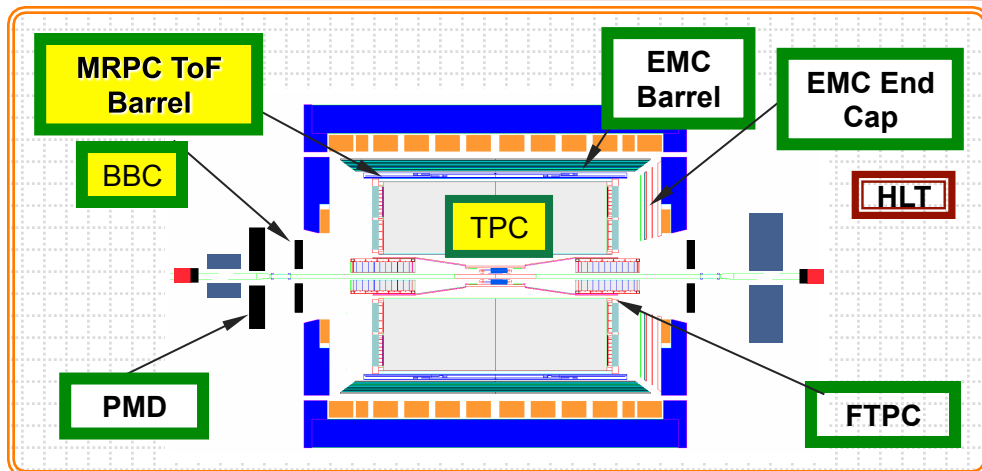


Beyond single (chemical) freeze-out:

1. J. Steinheimer et al. PRL 110, 042501 (2013)
2. S. Chatterjee et al. PLB 727, 554 (2013)
3. K. Bugaev et al., EPL 104, 22002 (2013)



# STAR Experiment



**Coverage:**  
 $0 < \phi < 2\pi$   
 $|\eta| < 1.0$

**Uniform acceptance:**  
 All energies  
 and particles

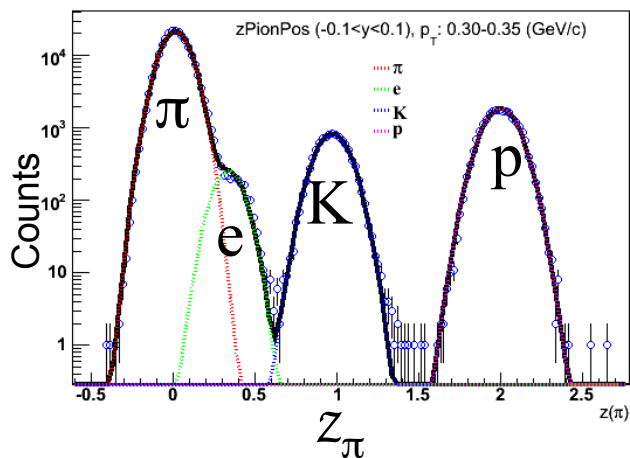
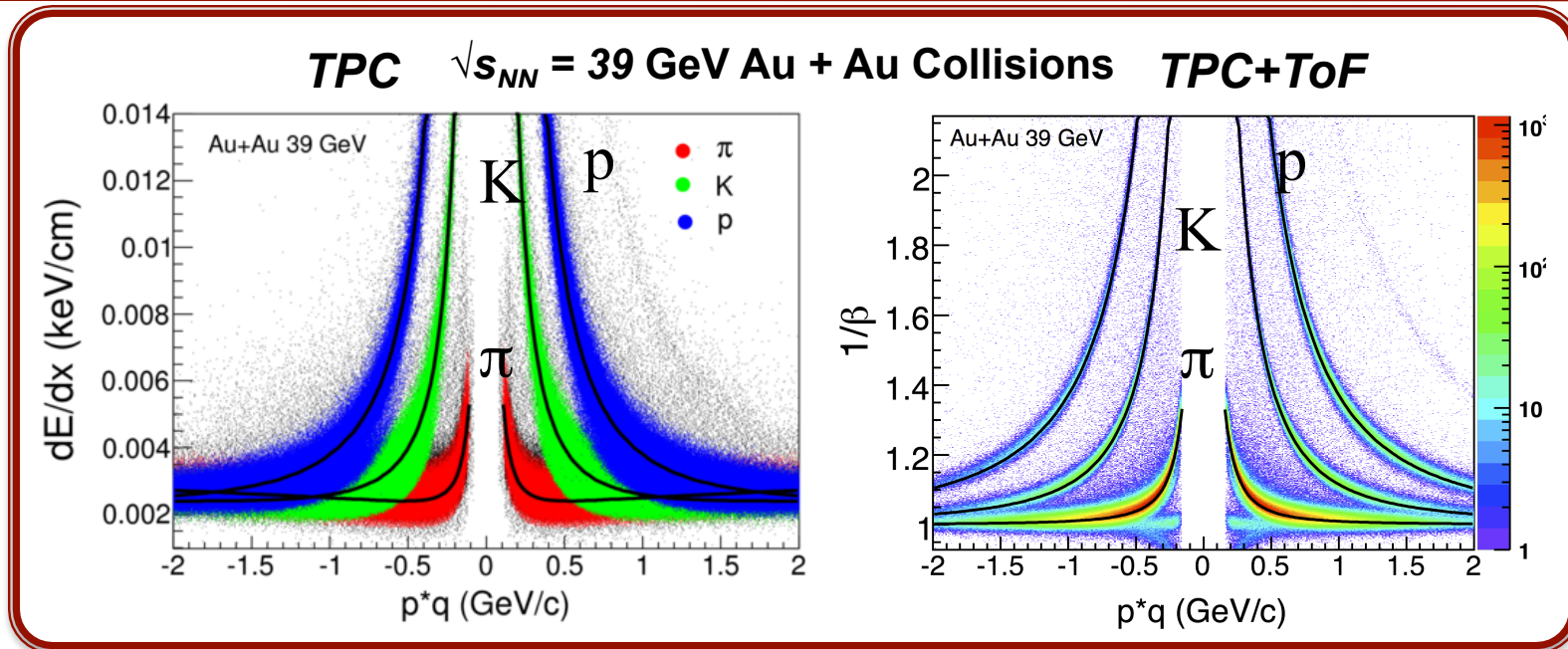
## BES-I Data:

Year	$\sqrt{s_{NN}}$ (GeV)	Events ( $10^6$ )
2010	62.4	67
2010	39	130
2011	27	70
2011	19.6	36
2014	14.5	20*
2010	11.5	12
2010	7.7	5





# Particle Identification

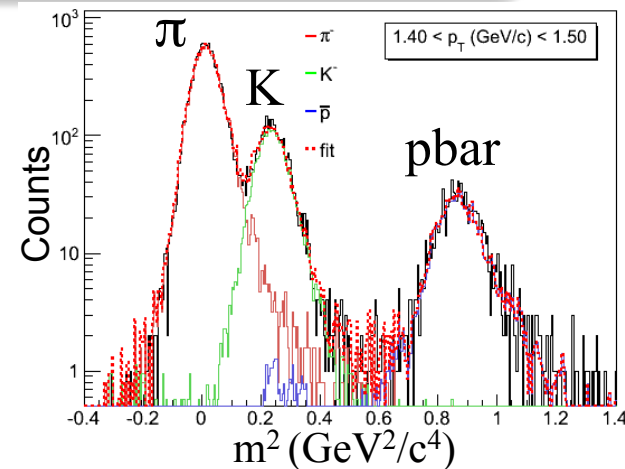


$$z = \log \left( \frac{(dE/dx)_{meas.}}{(dE/dx)_{theory}} \right)$$

H. Bichsel, NIM A. 562 (2006) 154

$$m^2 = p^2 \left( \frac{c^2 t^2}{L^2} - 1 \right)$$

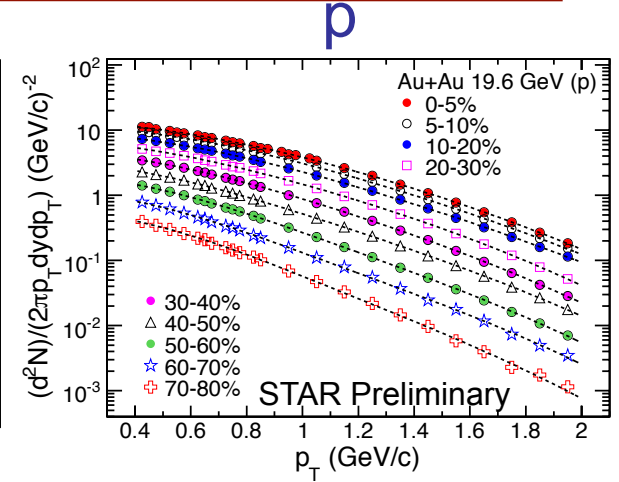
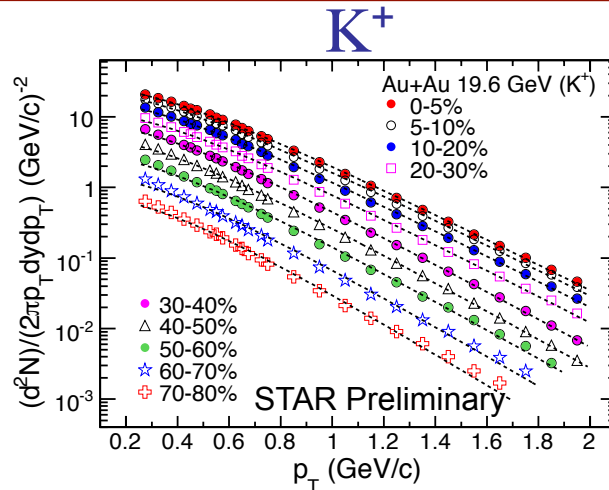
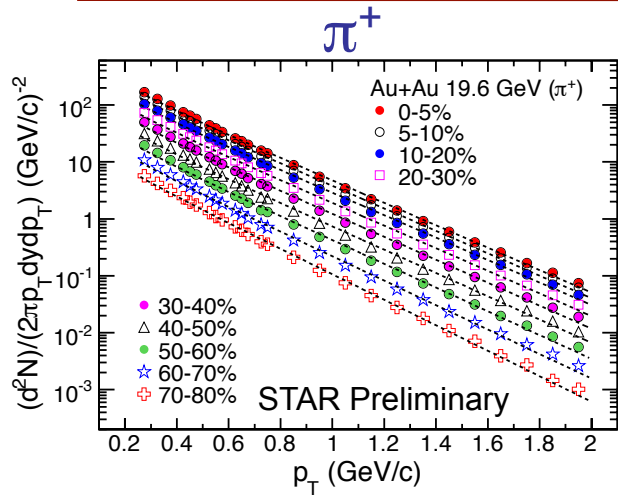
c=velocity of light,  
L=path length



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# Invariant Yield

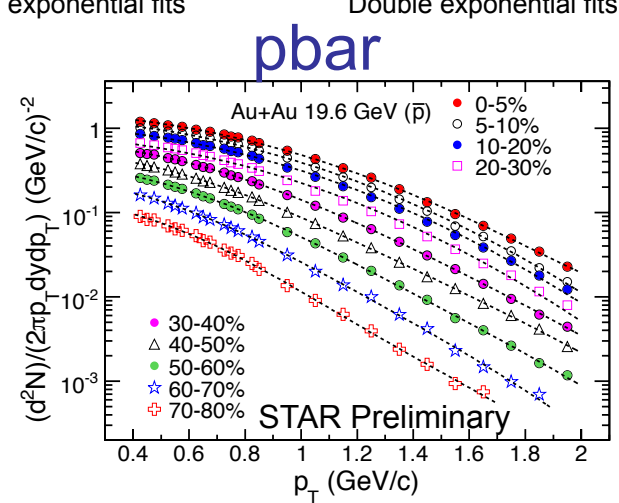
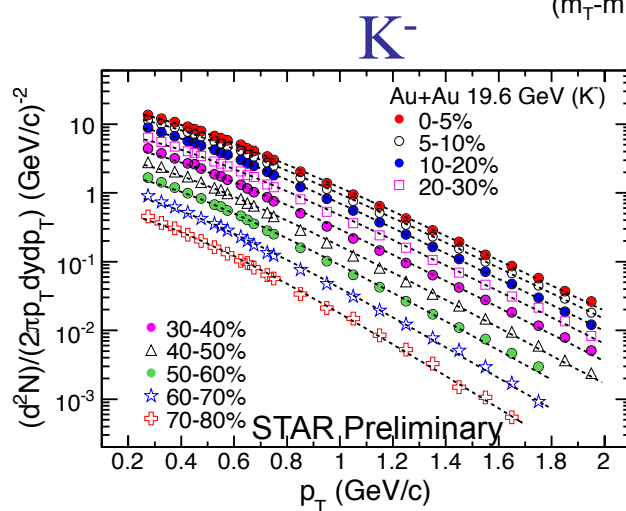
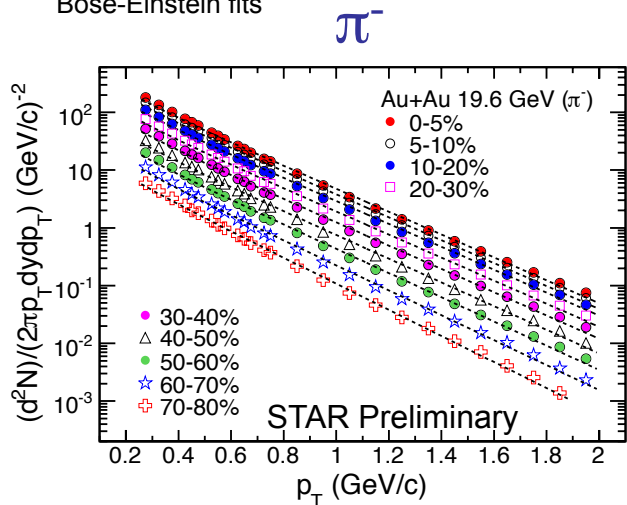


Pion curves:  
Bose-Einstein fits

Au+Au 19.6 GeV

Kaon curves:  
( $m_T-m$ ) exponential fits

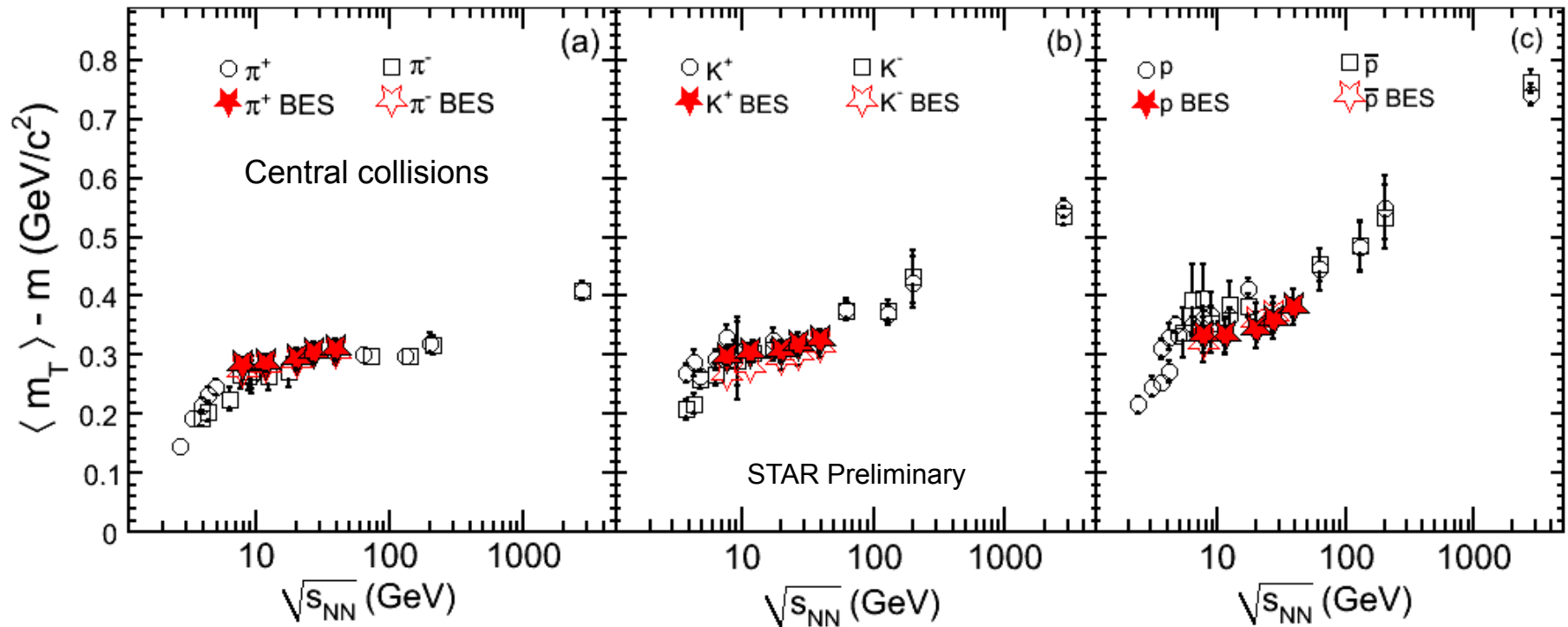
proton curves:  
Double exponential fits



Spectra are characterized by  $dN/dy$  and  $\langle p_T \rangle$  or  $\langle m_T \rangle$



# Average Transverse Mass



NA49 : PRC 66 (2002) 054902, PRC 77 (2008) 024903, PRC 73 (2006) 044910 ;  
 STAR : PRC 79 (2009) 034909, PRC 81, 024911 (2010); E802(AGS) : PRC 58 (1998)  
 3523, PRC 60 (1999) 044904; E877(AGS) : PRC 62 (2000) 024901 E895(AGS) :  
 PRC 68 (2003) 054903; ALICE: PRL109, 252301 (2012), PRC 88, 044910 (2013)

$$m_T = \sqrt{(p_T^2 + m^2)}$$

$\langle m_T \rangle - m$  is almost constant around BES energies for  $\pi$ , K, p

Thermodynamic system:  $T \sim \langle m_T \rangle - m$ , Entropy  $\sim dN/dy \propto \log(\sqrt{s_{NN}})$

L. Van Hove, Phys. Lett. B 118, 138 (1982)





# Kinetic Freeze-out: Blast Wave Model

Elastic collisions among the particles stop and the momentum distribution gets fixed

Blast-Wave (BW) Model:

$$\frac{dN}{p_T dp_T} \propto \int_0^R r dr m_T I_0 \left( \frac{p_T \sinh \rho(r)}{T_{kin}} \right) \times K_1 \left( \frac{m_T \cosh \rho(r)}{T_{kin}} \right)$$

$I_0, K_1$ : Modified Bessel functions

E. Schnedermann, J. Sollfrank, and U. W. Heinz, Phys. Rev. C 48, 2462 (1993).

$\rho(r) = \tanh^{-1}\beta$ ,  $r/R$ : relative radial position;  $R$ : radius of fireball

$\beta$ : transverse radial flow velocity,  $T_{kin}$ : Kinetic freeze-out temperature

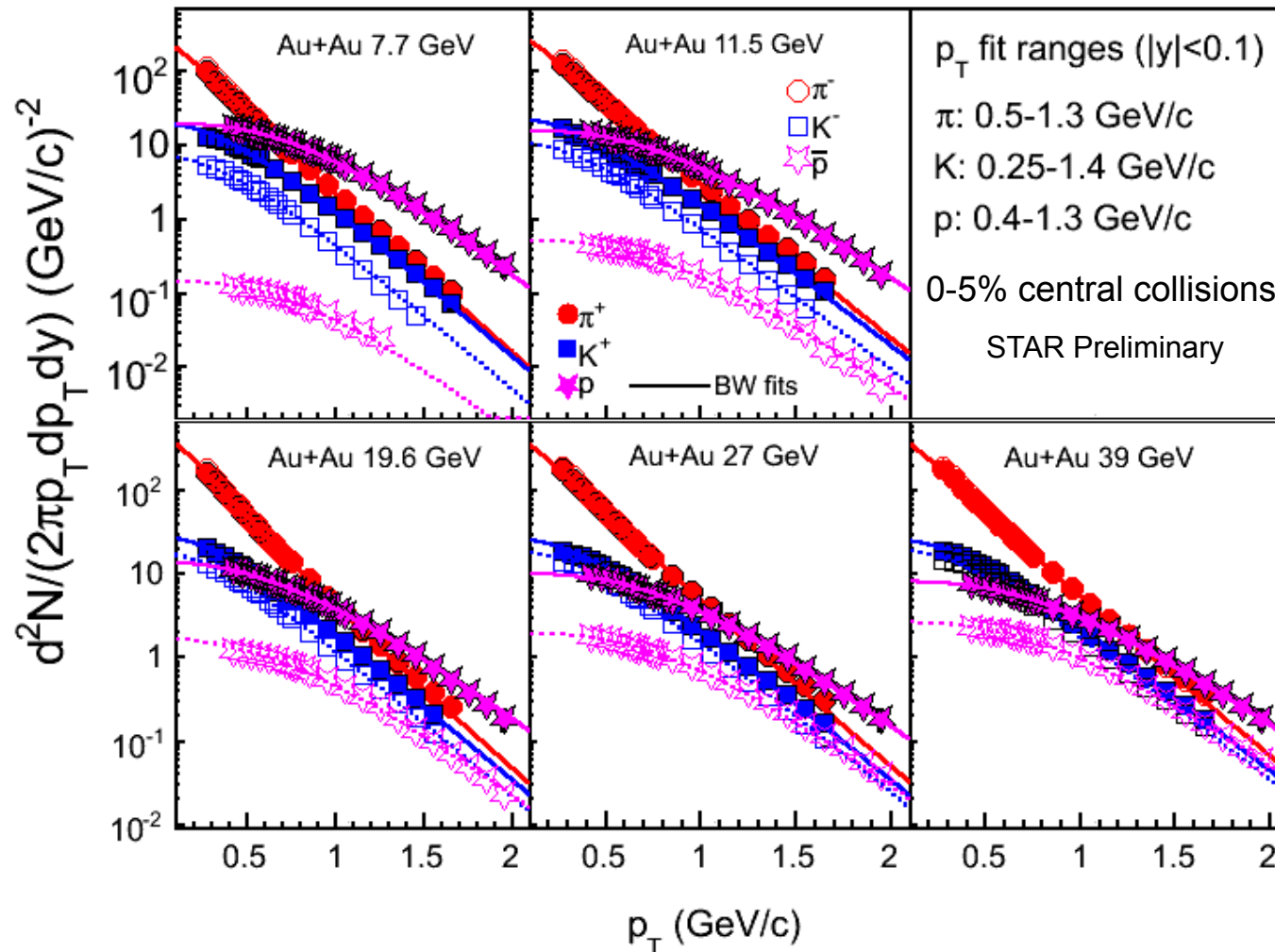
- Hydrodynamic based model
- Assumes particles are locally thermal at a kinetic freeze-out temperature and moving with a common radial flow velocity

✧ Momentum distributions are fitted simultaneously with BW

✧ Two main parameters:  $T_{kin}$  and  $\langle\beta\rangle$



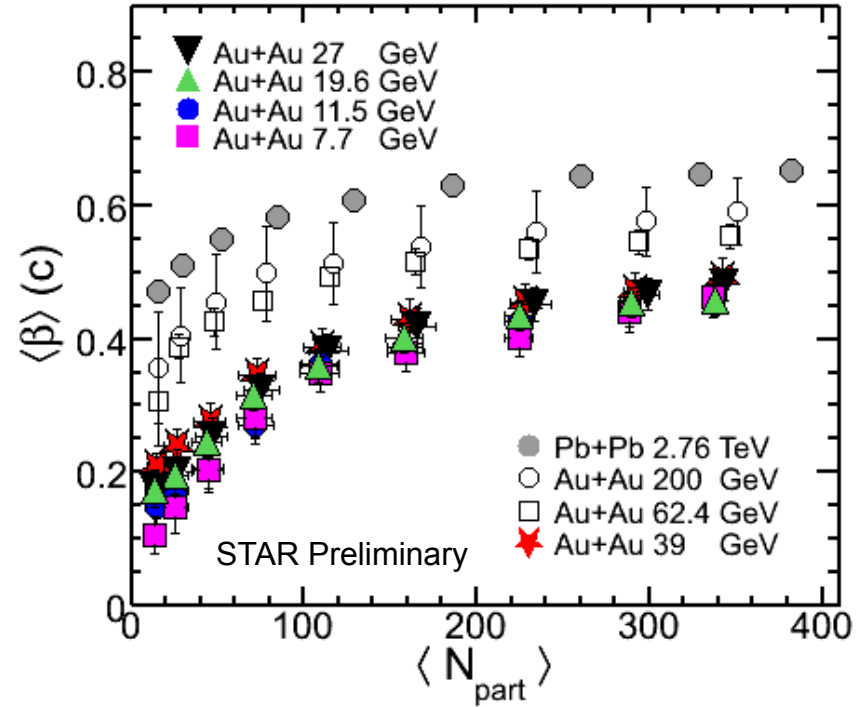
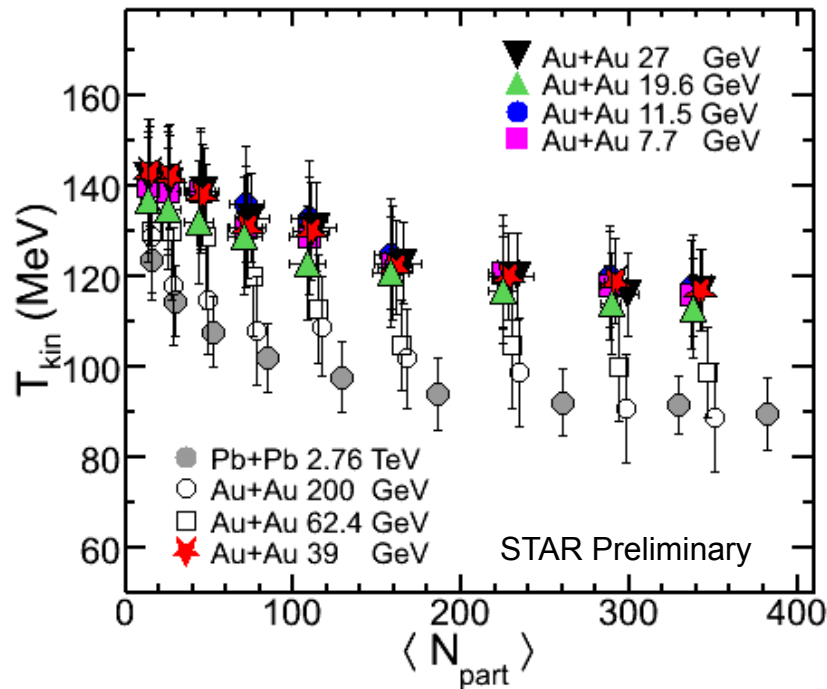
# Blast Wave Fits: $\pi$ , $K$ , $p$



BW well explains the  $\pi$ ,  $K$ ,  $p$  spectra simultaneously



# Centrality Dependence: $T_{kin}$ and $\langle\beta\rangle$



STAR : PRC 79 (2009) 034909; ALICE: PRC 88, 044910 (2013)

$T_{kin}$  decreases from peripheral to central collisions

-- Longer lived fireball in central collisions

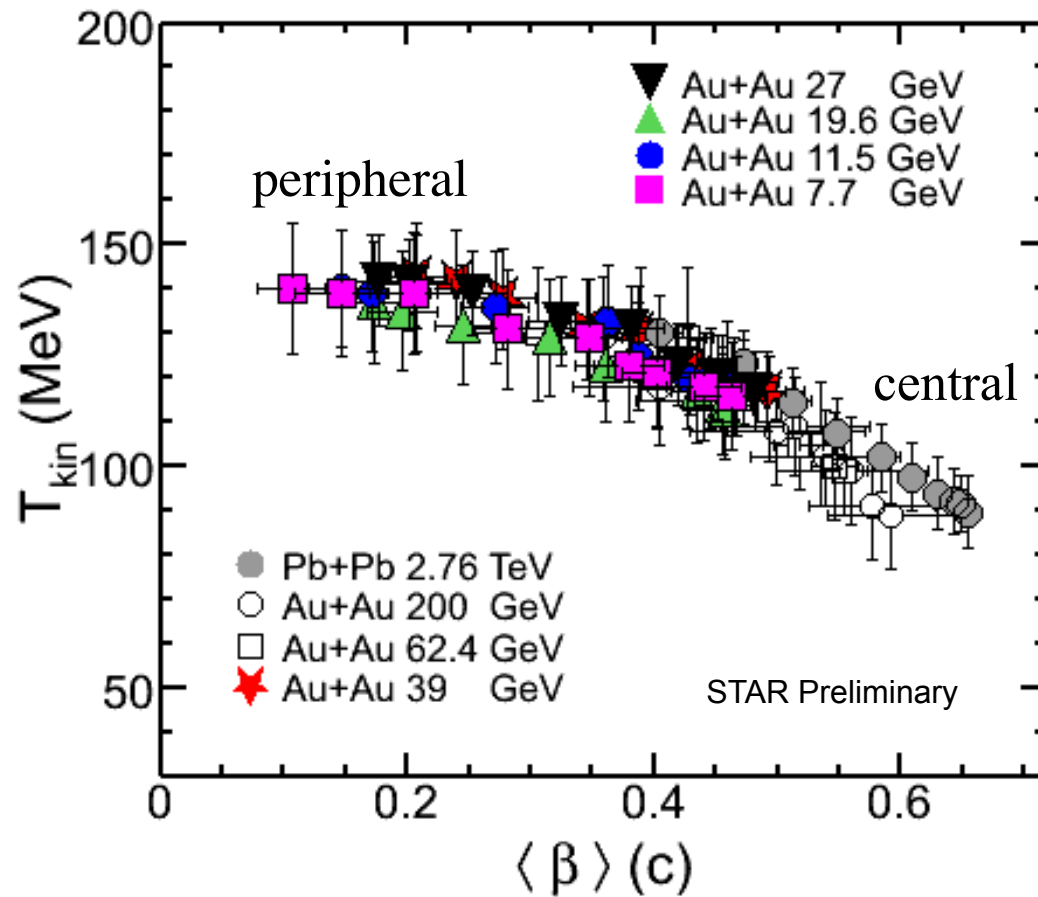
$\langle\beta\rangle$  increases from peripheral to central collisions

-- More rapid expansion in central collisions





# $T_{kin}$ versus $\langle \beta \rangle$



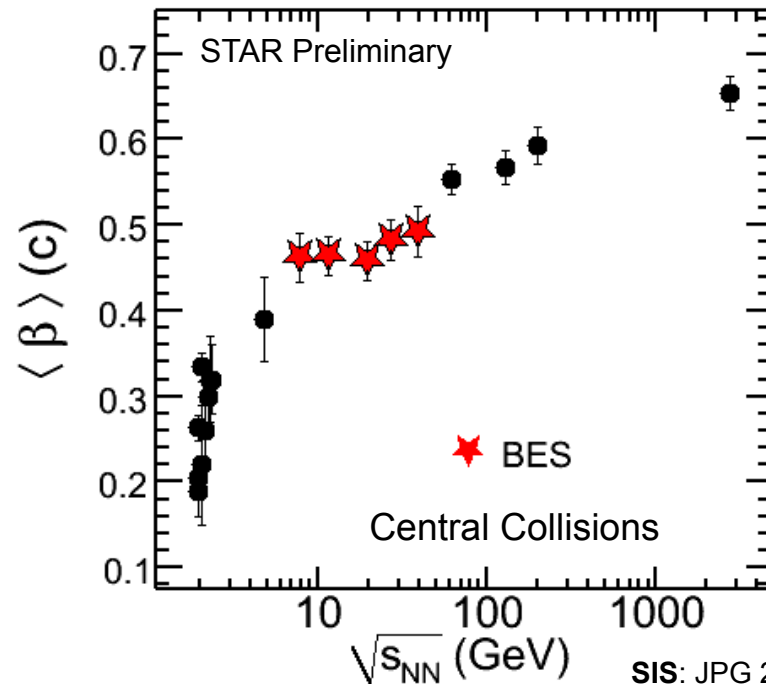
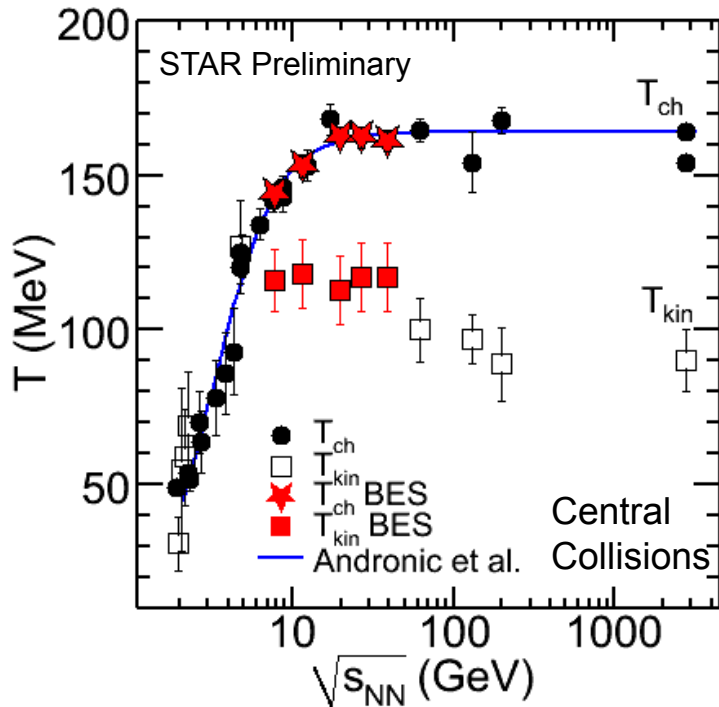
STAR : PRC 79 (2009) 034909; ALICE: PRC 88, 044910 (2013)

Anti-correlation:  $T_{kin}$  increases,  $\langle \beta \rangle$  decreases and vice-versa





# Energy Dependence: $T_{kin}$ and $\langle\beta\rangle$



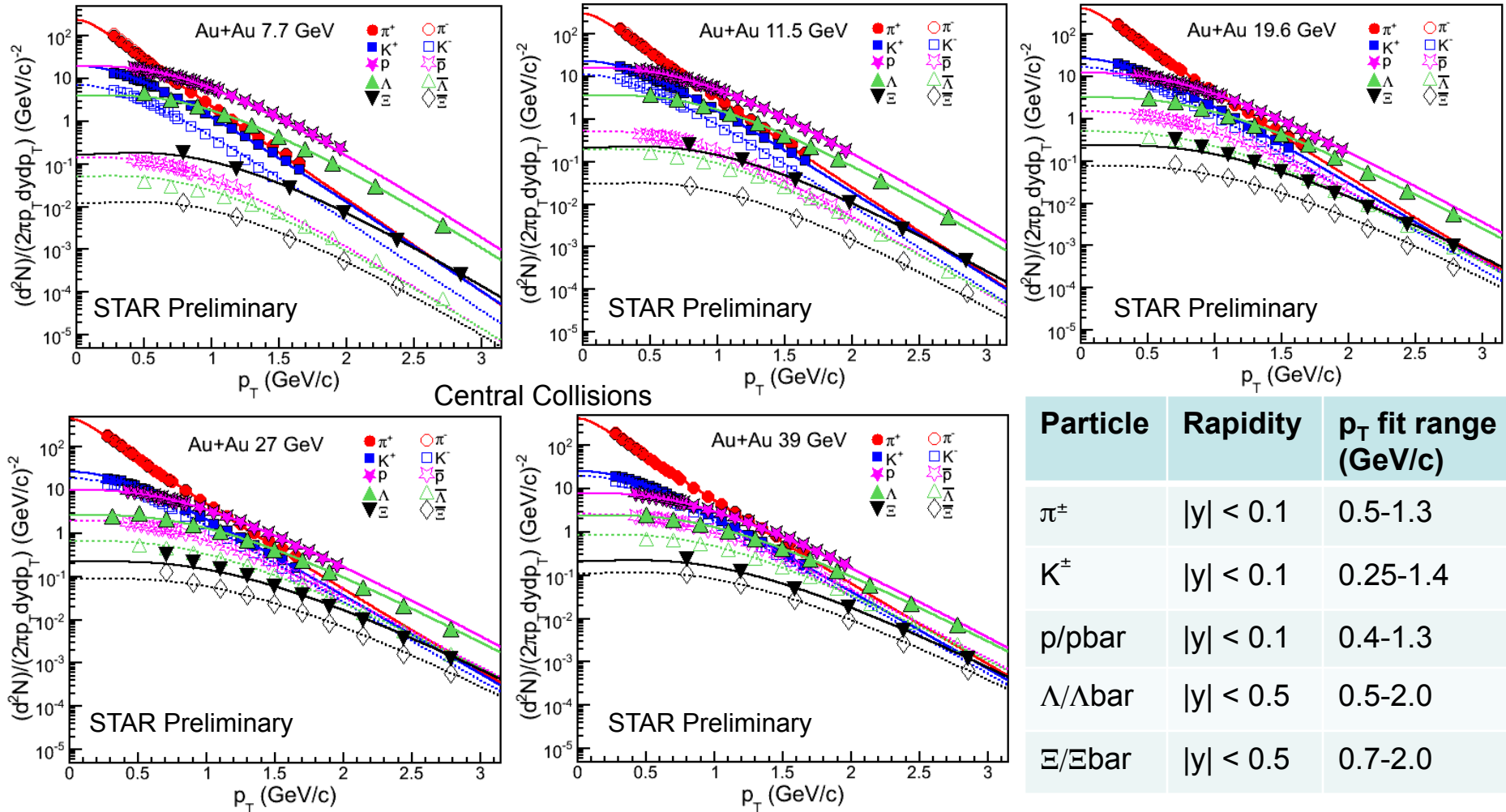
**FOPI:** NPA 612, 493 (1997);  
**EOS:** PRL 75, 2662 (1995);  
**E866:** arXiv:nucl-ex/9806002;  
**STAR :** PRC 79 (2009) 034909;  
**ALICE:** PRC 88, 044910 (2013); PRL 109, 252301 (2012).

**SIS:** JPG 25, 281 (1999); PRC 57, 3319 (1998);  
**AGS:** PLB 344, 43 (1995); PLB 365, 1 (1996); PRC 67, 015205 (2003);  
**SPS:** PLB 365, 1 (1996); PLB 465, 15 (1999); PRC 67, 015205 (2003); JPG 28, 1861 (2002); PRC 64, 024901 (2001); PRC 73, 034905 (2006); NPA 772, 167 (2006) ;

- Systematic study of chemical and kinetic freeze-out in heavy-ion collisions
- $\langle\beta\rangle$  similar at low BES energies and then increases for higher energies up to LHC



# BW Fits: Including $\Lambda$ and $\Xi$

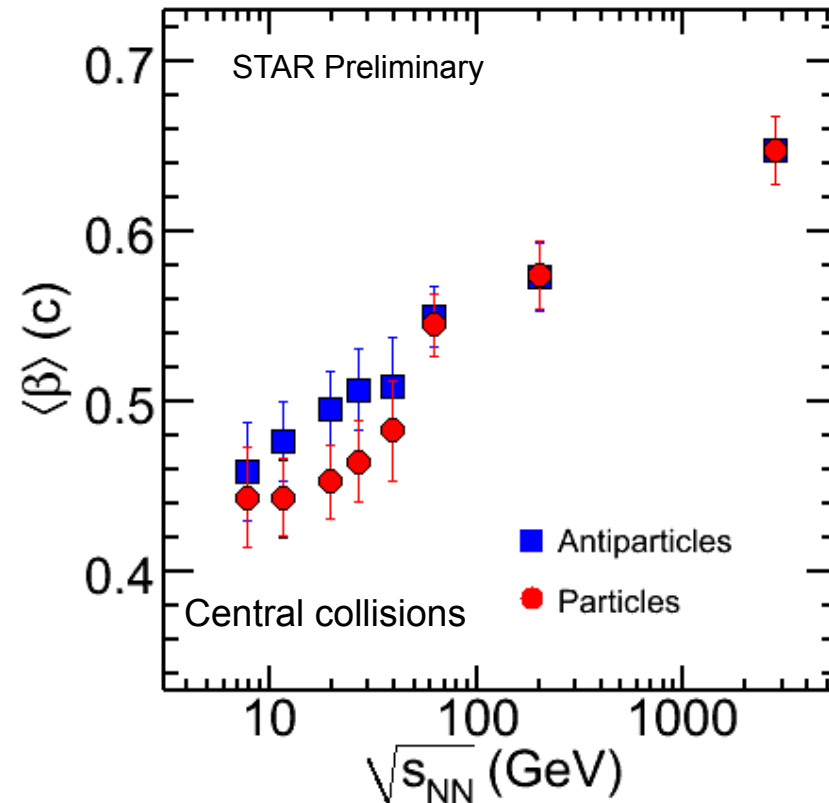
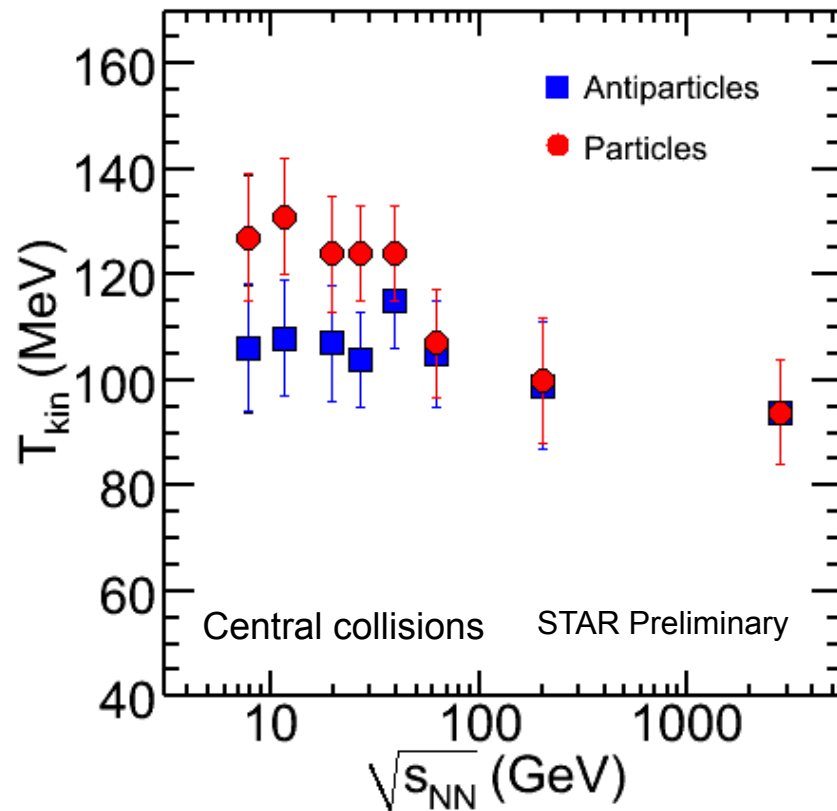


- ✧ Strange particles ( $\Lambda$ ,  $\Xi$ ) are fitted well simultaneously with  $\pi, K, p$  in Blast wave
- ✧  $T_{kin}$  and  $\langle \beta \rangle$  extracted are similar as from fits to  $\pi, K, p$  spectra only



# BW Fits: Particle-Antiparticle

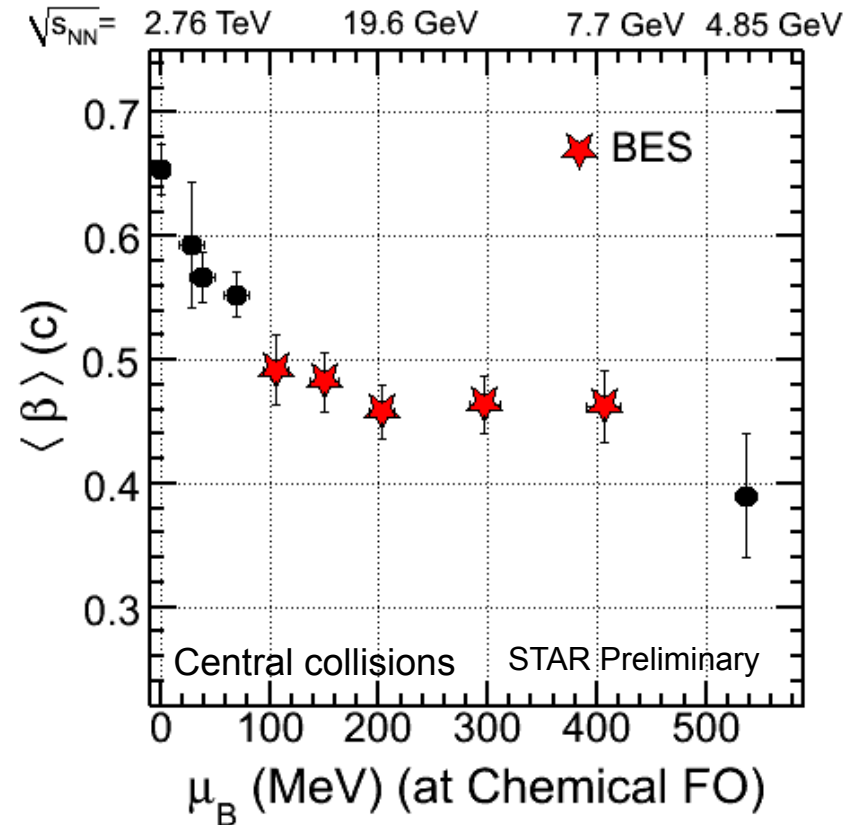
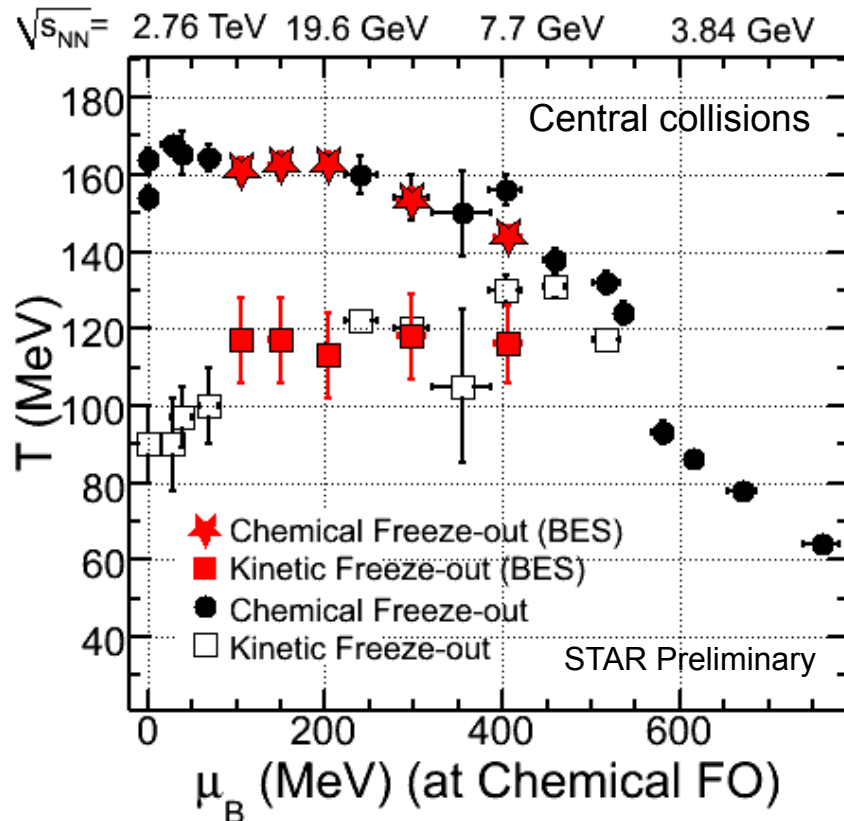
Particles:  $\pi^+$ ,  $K^+$ ,  $p$ ,  $\Lambda$ ,  $\Xi^-$ ; Antiparticles:  $\pi^-$ ,  $K^-$ ,  $pbar$ ,  $\Lambdabar$ ,  $\Xi^+$



- ◇ Interesting trends at lower energies but errors are large
- ◇ More detailed studies underway...



# Current Status of Phase Diagram



- ✧ Covering large portion of QCD phase diagram
- ✧ Difference between  $T_{kin}$  and  $T_{ch}$  increases for lower  $\mu_B$  : Effect of hadronic interactions between chemical and kinetic freeze-out
- ✧  $\langle \beta \rangle$  is almost similar from  $\mu_B$  200-400 MeV



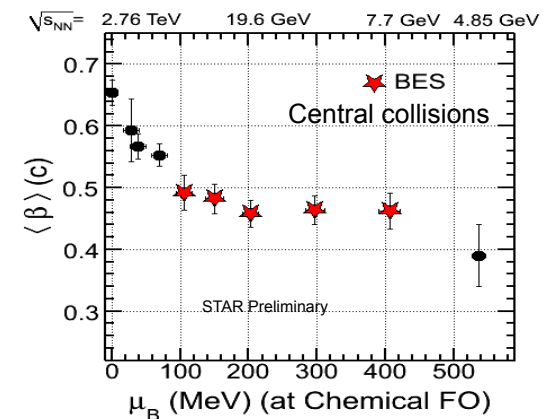
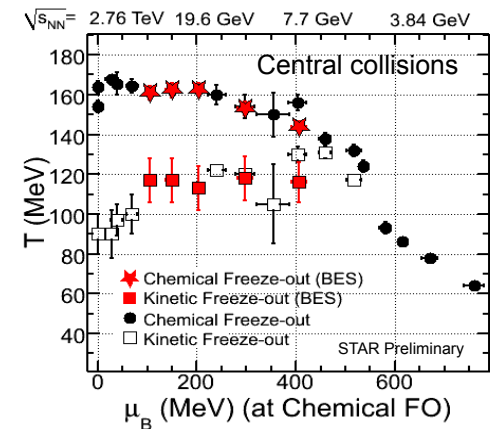
# Summary

❑ Systematic study of kinetic freeze-out properties in heavy-ion collisions ( $\mu_B$  : 20-400 MeV)

❑  $T_{kin}$  and  $\langle\beta\rangle$  show anti-correlation:  
-  $T_{kin}$  decreases towards central collisions  
-- longer lived fireball  
-  $\langle\beta\rangle$  increases towards central collisions  
-- more rapid expansion

❑  $T_{kin}$  is similar at low BES energies  
- Decreases for higher energies  
- Difference b/w  $T_{ch}$  and  $T_{kin}$  is large at lower  $\mu_B$   
-- effect of hadronic interactions b/w chemical and kinetic FO

❑  $\langle\beta\rangle$  is almost constant for lower BES energies and increases for higher energies :  $\langle m_T \rangle - m$  for  $\pi$ , K, p also shows similar behavior







# Thanks to STAR Collaboration

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Back up





# Chemical Freeze-out

Statistical-Thermal Model (THERMUS):

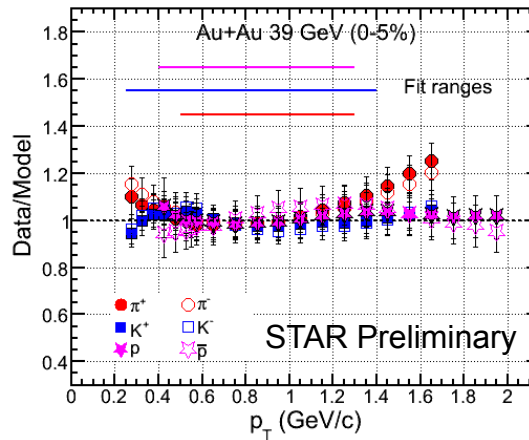
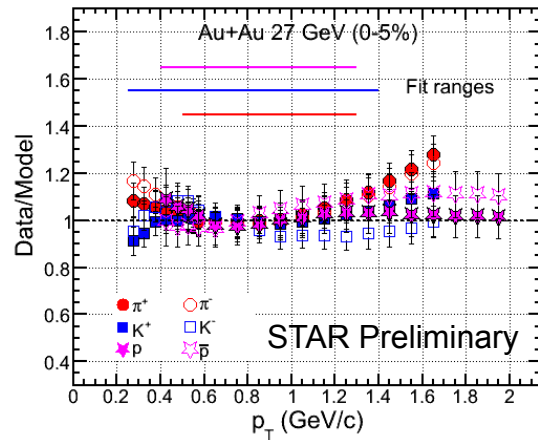
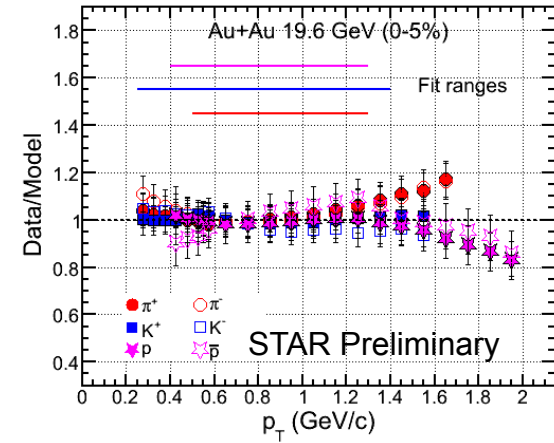
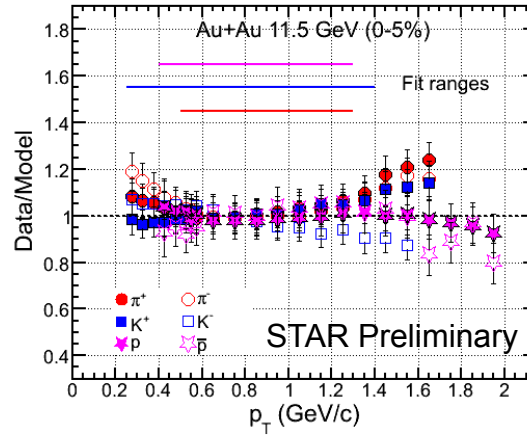
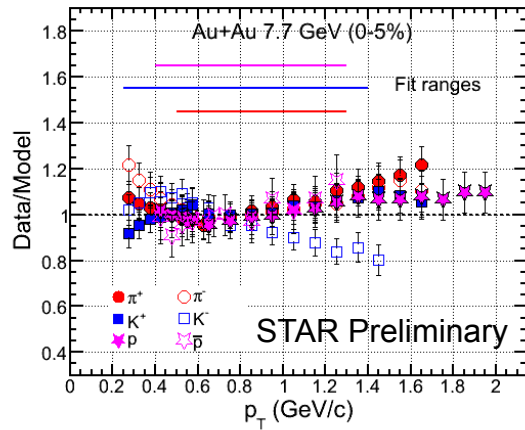
$$n = \frac{1}{V} \frac{\partial(T \ln Z)}{\partial \mu} = \frac{VT m_i^2 g_i}{2\pi^2} \sum_{k=1}^{\infty} \frac{(\pm 1)^{k+1}}{k} \left( e^{\beta k \mu_i} \right) K_2 \left( \frac{k m_i}{T} \right)$$

$\beta=1/T$ ; -1(+1) for fermions (bosons),  
Z=partition function;  
 $m_i$  = mass of hadron species i;  
V = volume; T = Temperature;  
 $K_2$ = 2<sup>nd</sup> order Bessel function;  
 $g_i$  = degeneracy;  $\mu_i$  = chemical potential

- Fitted particle ratios with THERMUS
- Used grand-canonical approach
- Two main parameters:  $T_{ch}$  and  $\mu_B$



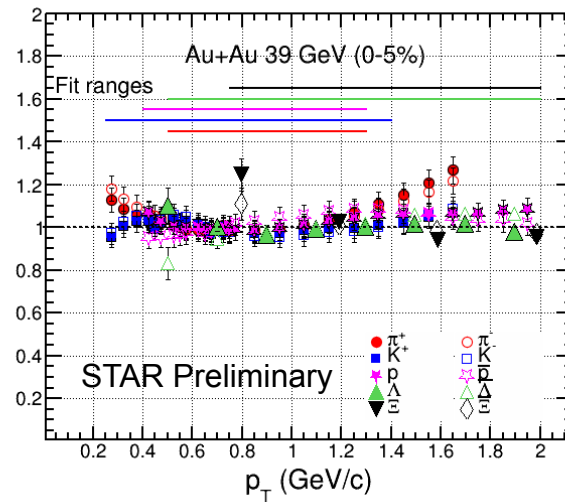
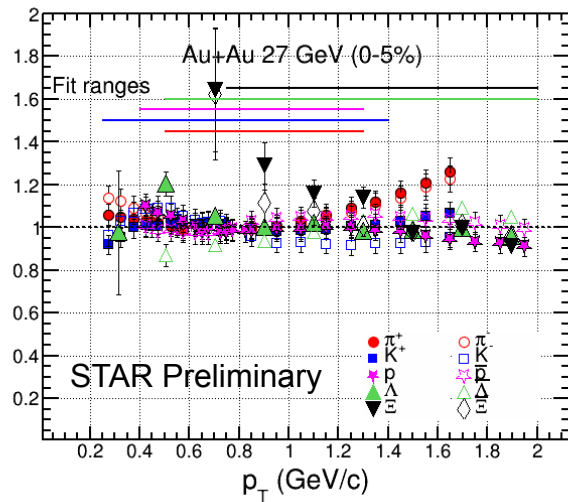
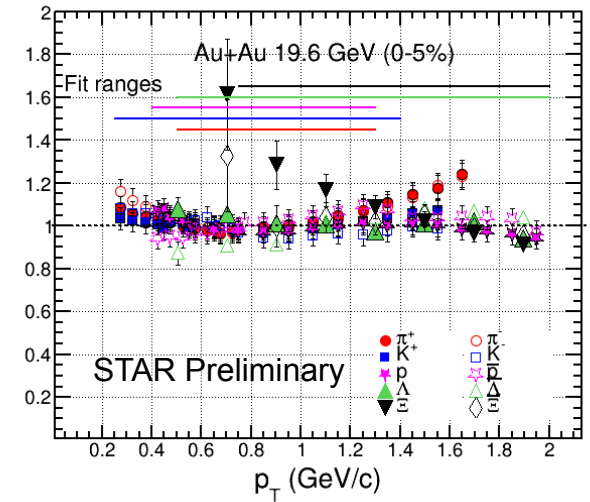
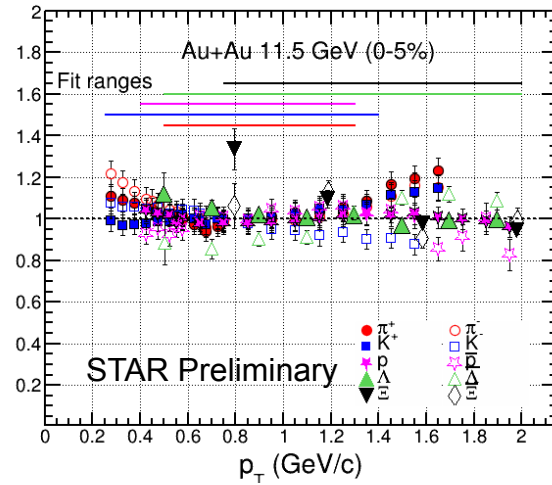
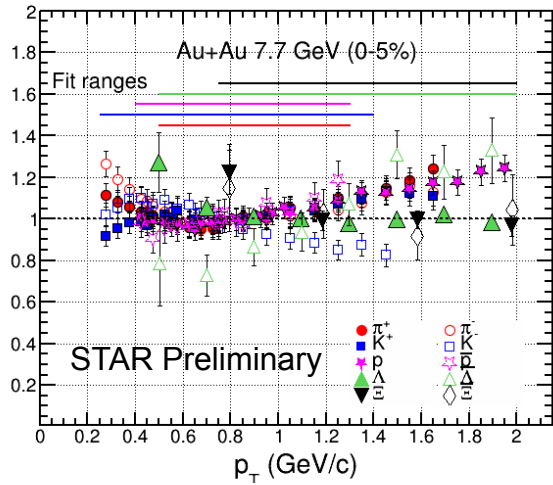
# BW fits (data/model)



$\pi$ ,  $K$ ,  $p$   
and antiparticles



# BW fits (data/model)



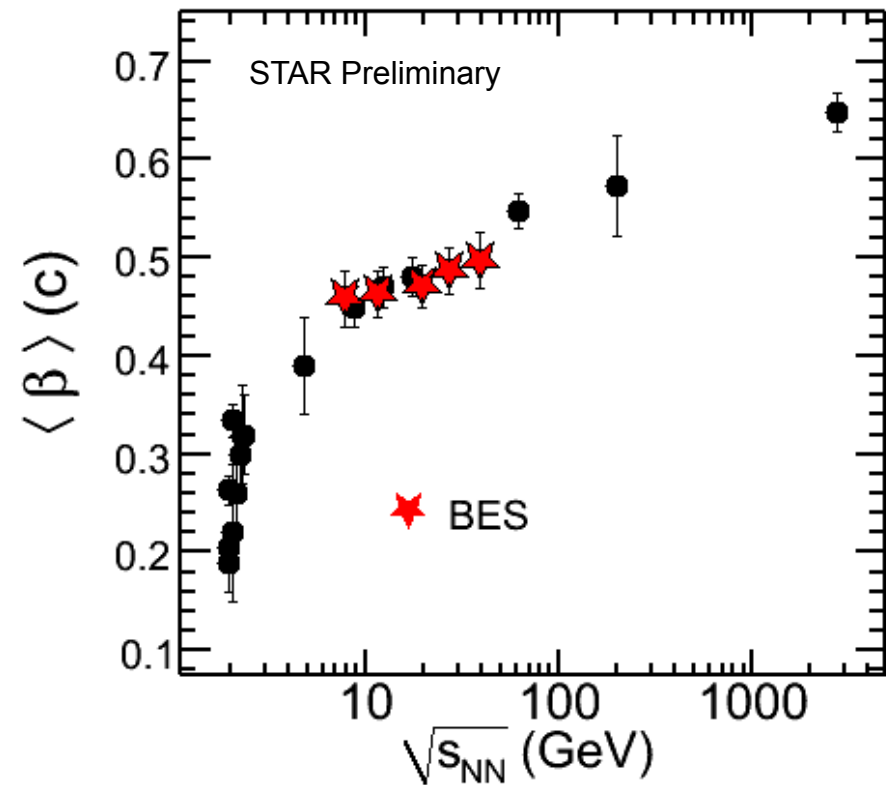
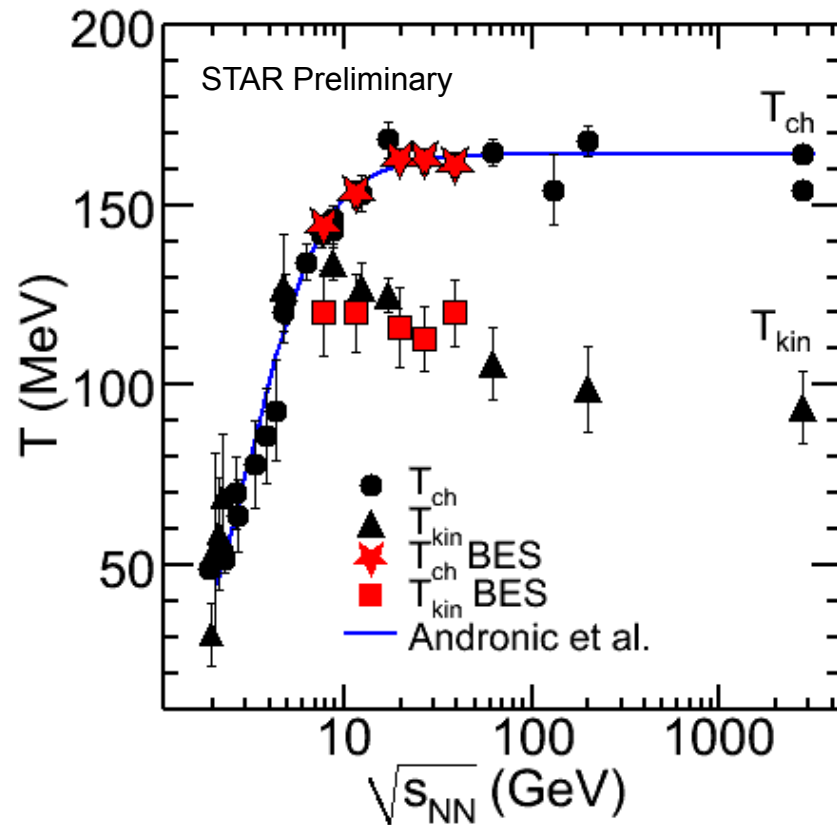
$\pi$ ,  $K$ ,  $p$ ,  $\Lambda$ ,  $\Xi$   
and antiparticles





# Energy dependence: fits with $\Lambda$ and $\Xi$

BW fits include:  $\pi$ ,  $K$ ,  $\rho$ ,  $\Lambda$ ,  $\Xi$  and corresponding antiparticles





# BW Fits: Particle-Antiparticle

BW fits include:  $\pi$ , K, p only and corresponding antiparticles

