# Beam-energy dependence of the azimuthal anisotropic flow from RHIC

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**Abstract:** Recent STAR measurements of the anisotropic flow coefficients  $(v_n)$  are presented for Au+Au collisions spanning the beam energy range  $\sqrt{s_{NN}} = 7.7 - 200$  GeV. The measurements indicate dependences on the harmonic number (n), transverse momentum  $(p_T)$ , pseudorapidity  $(\eta)$ , collision centrality and beam energy  $(\sqrt{s_{NN}})$  which could serve as important constraints to test different initial-state models and to aid precision extraction of the temperature dependence of the specific shear viscosity.

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# I. INTRODUCTION

A major aim of the heavy-ion experimental program at the Relativistic Heavy Ion Collider (RHIC) is to study the properties of the quark-gluon plasma (QGP) created in ion-ion collisions. Recently, several studies have highlighted the use of anisotropic flow measurements to investigate the transport properties of the QGP [1–7]. An essential question in many of these studies has been the role of initial-state fluctuations and their impact on the uncertainties associated with the extraction of  $\eta/s$  for the QGP [8, 9].

In this work, we present a new measurement for the anisotropic flow coefficients,  $v_n(n > 1)$  [10–12], and the rapidity-even dipolar flow coefficient,  $v_1^{even}$  [13, 14], with an eye toward providing a new constraint which could assist the distinction between different initial-state models and therefore, facilitate a more accurate extraction of the specific shear viscosity,  $\eta/s$  [15, 16].

The anisotropic flow is described by the coefficients,  $v_n$ , obtained from a Fourier expansion of the azimuthal angle ( $\phi$ ) distribution of the particles emitted in the collisions [17]:

$$\frac{dN}{d\phi} \propto 1 + 2\sum_{n=1} \mathbf{v}_n \cos(n(\phi - \Psi_n)),\tag{1}$$

where  $\Psi_n$  denotes the azimuthal angle of the  $n^{th}$ -order event plane; the coefficients,  $v_1$ ,  $v_2$  and  $v_3$  define directed, elliptic, and triangular flow, respectively. The flow coefficients,  $v_n$ , are linked to the two-particle Fourier coefficients,  $v_{n,n}$ , as:

$$\mathbf{v}_{\mathbf{n},\mathbf{n}}(p_{\mathrm{T}}^{a}, p_{\mathrm{T}}^{b}) = \mathbf{v}_{\mathbf{n}}(p_{\mathrm{T}}^{a})\mathbf{v}_{\mathbf{n}}(p_{\mathrm{T}}^{b}) + \delta_{\mathrm{NF}},\tag{2}$$

where a and b are particles with  $p_{\rm T}^a$  and  $p_{\rm T}^b$ , respectively, and  $\delta_{\rm NF}$  is the non-flow (NF) term, which involves potential short-range contributions from resonance decays, Bose-Einstein correlation, near-side jets, and long-range contributions from the global momentum conservation (GMC) [18–20]. The short-range nonflow contributions can be reduced by applying a pseudorapidity gap,  $\Delta\eta$ , between  $\eta^a$  and  $\eta^b$ . However, the impacts of the GMC must be explicitly considered. For the current analysis, a simultaneous fitting method [13], outlined below, was used to account for the GMC.

#### II. MEASUREMENTS

The correlation function method was used to measure the two-particle  $\Delta \phi$  correlations:

$$C_r(\Delta\phi,\Delta\eta) = \frac{(dN/d\Delta\phi)_{same}}{(dN/d\Delta\phi)_{mixed}},\tag{3}$$

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FIG. 1.  $v_{1,1}$  vs.  $p_T^b$  for several selections of  $p_T^a$  for 0-5% central Au+Au collisions at  $\sqrt{s_{NN}} = 200$  GeV. The dashed curves show the result of the simultaneous fit with Eq. 5. Figure are taking from Ref [13].

where  $(dN/d\Delta\phi)_{same}$  denotes the normalized azimuthal distribution of particle pairs from the same event and  $(dN/d\Delta\phi)_{mixed}$  denotes the normalized azimuthal distribution for particle pairs in which each member is selected from a different events but with a similar classification for the collision vertex location, centrality, etc. The pseudorapidity gap requirement  $|\Delta\eta| > 0.7$  was applied to track pairs to reduce the non-flow contributions associated with the short-range correlations.

The two-particle Fourier coefficients,  $v_{n,n}$ , are extracted from the correlation function as:

$$\mathbf{v}_{\mathbf{n},\mathbf{n}} = \frac{\sum_{\Delta\phi} C_r(\Delta\phi, \Delta\eta) \cos(n\Delta\phi)}{\sum_{\Delta\phi} C_r(\Delta\phi, \Delta\eta)},\tag{4}$$

and then the two-particle Fourier coefficients,  $v_{n,n}$ , are used to extract  $v_1^{even}$  via a simultaneous fit of  $v_{1,1}$  as a function of  $p_T^{\rm b}$ , for several selections of  $p_T^{\rm a}$  with Eq. 2:

$$\mathbf{v}_{1,1}(p_{\rm T}^a, p_{\rm T}^b) = \mathbf{v}_1^{\rm even}(p_{\rm T}^a)\mathbf{v}_1^{\rm even}(p_{\rm T}^b) - Cp_{\rm T}^a p_{\rm T}^b.$$
(5)

Here,  $C \propto 1/(\langle Mult \rangle \langle p_T^2 \rangle)$  takes into account the non-flow correlations caused by a global momentum conservation [20, 21] and  $\langle Mult \rangle$  is the mean multiplicity. For a particular centrality selection, the left-hand side of Eq. 5 describes the  $N \times N$  matrix which we fit with the right-hand side using N + 1 parameters; N values of  $v_1^{even}(p_T)$  and one additional parameter C, accounting for the momentum conservation [22].

Figure 1 [13] shows the result of this fitting method for 0 - 5% central Au+Au collisions at  $\sqrt{s_{NN}} = 200$  GeV. The dashed curve (produced with Eq. 5) in each panel represents the effectiveness of the simultaneous fits, as well as the data constraining power. That is,  $v_{1,1}(p_T^b)$  grows from negative to positive values as the selection range for  $p_T^a$  is increased.

### III. RESULTS

Representative set of STAR measurements for  $v_1^{even}$  and  $v_n (n \ge 2)$  for Au+Au collisions at several different collision energies are summarized in Figs. 2, 3, 4 and 5.

The extracted values of  $v_1^{even}(p_T)$  for 0-10%, 10-20% and 20-30% centrality selections are shown in Fig. 2; the solid line in panel (a) indicates the hydrodynamic calculations [21], that in good agreement with our measurements, the inset displays the results of the associated momentum conservation coefficient, C, obtained for several centralities at  $\sqrt{s_{NN}} = 200$  GeV. The  $v_1^{even}(p_T)$  values show the characteristic pattern of a change from negative  $v_1^{even}(p_T)$  at low  $p_T$  to positive  $v_1^{even}(p_T)$  for  $p_T > 1$  GeV/c, with a crossing point that slowly shifts with  $\sqrt{s_{NN}}$ . They also indicate that  $v_1^{even}$  increases as the collisions become more peripheral, as might be expected from the centrality dependence of  $\varepsilon_1$ .

Figure 2 shows the  $p_T$  dependence of the  $v_n (n \ge 2)$  measurements for 0-40% centrality selection for a representative set of beam energies. Fig. 2 shows the  $v_n$  dependence on  $p_T$  and the harmonic number, n, with similar trends for each beam energy.

The centrality dependence of  $v_n (n \ge 2)$  is indicated in Fig. 4 for the same representative set of beam energies. Our measurements indicate a soft centrality dependence for the higher-order flow harmonics,



FIG. 2. The extracted values of  $v_1^{even}$  vs.  $p_T$  for different centrality selections (0-10%, 10-20% and 20-30%) of Au+Au collisions for several values of  $\sqrt{s_{_{NN}}}$ . The  $v_1^{even}$  values are obtained via fits with Eq. (5). The solid line in panel (a) shows the result from a hydrodynamic calculations with  $\eta/s = 0.16$  [21]. The inset in panel (a) shows a representative set of the associated values of C vs. the corrected mean multiplicity for  $|\eta| < 0.5$  ( $\langle Mult \rangle^{-1}$ ). The extracted  $v_1^{even}$  for  $\sqrt{s_{_{NN}}} = 200$ , 39 and 19.6 GeV are shown in panels a, b and c respectively.



FIG. 3. The  $v_n(p_T)$  as a function of  $p_T$  for charged particles in 0-40% central Au+Au collisions. The shaded bands represent the systematic uncertainty. The measured  $v_n(p_T)$  for  $\sqrt{s_{NN}} = 200$ , 27 and 11.5 GeV are shown in panels a, b and c respectively.

which all decrease with decreasing the  $\sqrt{s_{\text{NN}}}$ . These  $v_n$  patterns may be related to the dependence of the viscous effects in the created medium, which lead to attenuation of  $v_n$  magnitude.

Figure 5 gives the excitation functions for the  $p_T$ -integrated v<sub>2</sub>, v<sub>3</sub> and v<sub>4</sub> for 0 - 40% central Au+Au collisions. They indicate monotonic trend for v<sub>n</sub> with  $\sqrt{s_{NN}}$ , as might be expected for a temperature increase with  $\sqrt{s_{NN}}$ .



FIG. 4. The  $v_n$  as a function of Au+Au collision centrality for charged particles with  $0.2 < p_T < 4$  GeV/c. The shaded bands represent the systematic uncertainty. The measured  $v_n$  (Centrality%) for  $\sqrt{s_{NN}} = 200$ , 27 and 11.5 GeV are shown in panels a, b and c respectively.



FIG. 5. The  $v_n(\sqrt{s_{NN}})$  for charged particles with  $0.2 < p_T < 4 \text{ GeV/c}$  and 0-40% central Au+Au collisions. The shaded bands represent the systematic uncertainty. The dashed line at  $v_n = 0$  is to guide the eye.

## IV. CONCLUSION

In summary, we have presented a comprehensive set of STAR anisotropic flow measurements for Au+Au collisions at  $\sqrt{s_{\rm NN}} = 7.7-200$  GeV. The measurements use the two-particle correlation method to obtain the Fourier coefficients,  $v_n(n > 1)$ , and the rapidity-even dipolar flow coefficient,  $v_1^{even}$ . The rapidity-even dipolar flow measurements indicate the characteristic patterns of an evolution from negative  $v_1^{even}(p_{\rm T})$  for  $p_{\rm T} < 1$  GeV/c to positive  $v_1^{even}(p_{\rm T})$  for  $p_{\rm T} > 1$  GeV/c, expected when initial-state geometric fluctuations act along with the hydrodynamic-like expansion to generate rapidity-even dipolar flow. The  $v_n(n > 1)$  measurements show a rich set of dependences on harmonic number n,  $p_T$  and centrality for several collision energies. This set of measurements may provide additional constraints to test different initial-state models and to aid accuracy extraction of the temperature dependence of the specific shear viscosity.

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