



Stony Brook  
University



# Beam energy and system dependence of rapidity-even dipolar flow

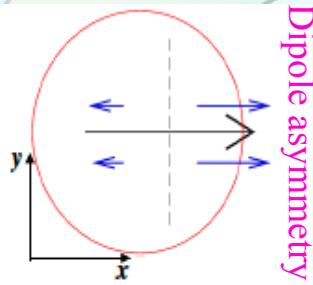
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STAR Collaboration  
Stony Brook University

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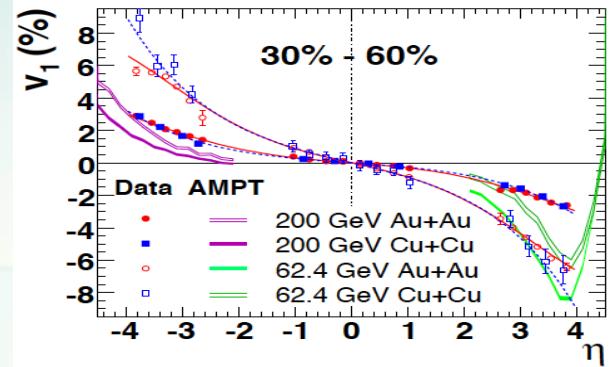


# Directed flow

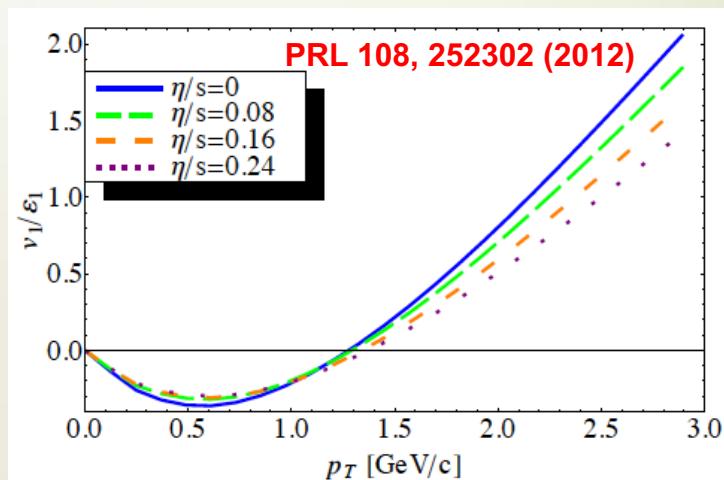
$$v_1(\eta) = v_1^{\text{even}}(\eta) + v_1^{\text{odd}}(\eta)$$



STAR, PRL 101 252301 (2008)



- The rapidity-even directed flow  $v_1^{\text{even}}$  stems from initial-state fluctuations acting in concert with hydrodynamic-like expansion
- The magnitude of  $v_1^{\text{even}}$  is sensitive to:
  - ✓ Initial-state eccentricity & its fluctuations
  - ✓ Transport coefficients ( $\eta/s$ , etc) but with less sensitivity than for higher order harmonics.
- The  $v_1^{\text{even}}$  constitutes a new set of experimental constraints that can help to:
  - ✓ Differentiate between initial-state models
  - ✓ Pin down the temperature dependence of the transport coefficients.

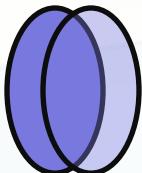


# Datasets

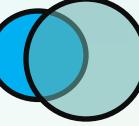
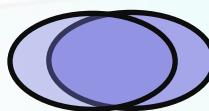
- Collected data for Au+Au at different  $\sqrt{s_{NN}}$
- Collected data for different systems at  $\sqrt{s_{NN}} \approx 200$  GeV;



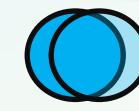
Au + Au



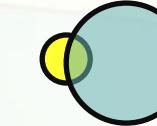
U + U



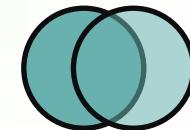
Cu + Au



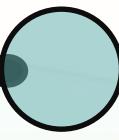
Cu + Cu



d + Au



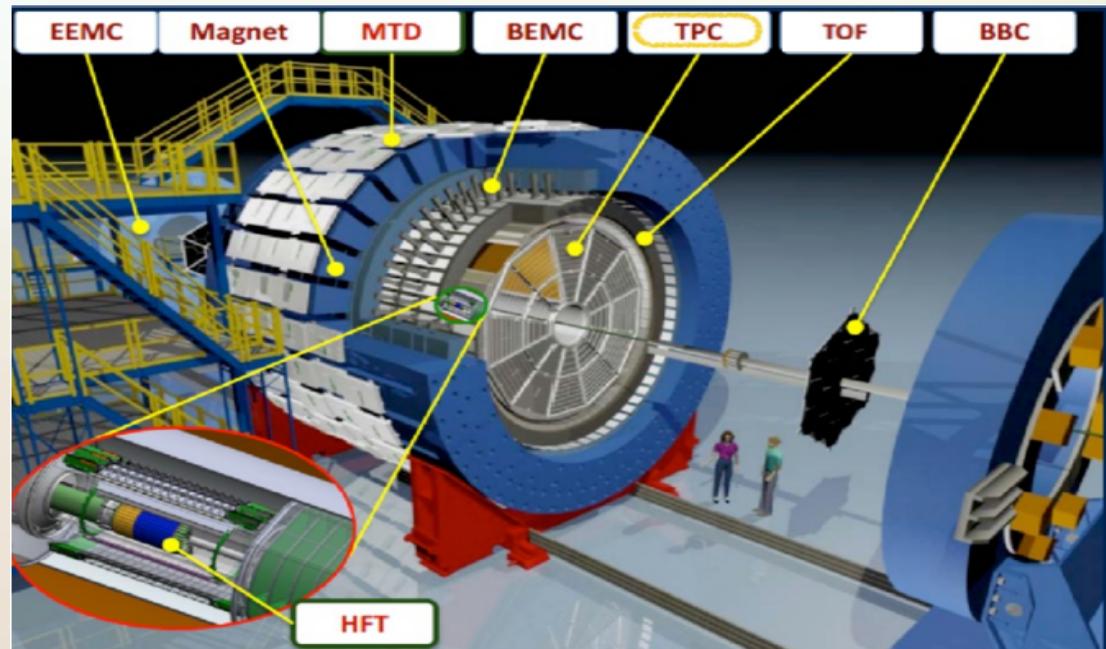
Au + Au



p + Au

## STAR Detector at RHIC

- TPC detector covers  $|\eta| < 1$



# Azimuthal anisotropy measurements

Correlation  
function

Two particle correlation function  $Cr(\Delta\varphi)$ ,

$$Cr(\Delta\varphi) = dN/d\Delta\varphi \quad \text{and} \quad v_{nn} = \frac{\sum_{\Delta\varphi} Cr(\Delta\varphi) \cos(n \Delta\varphi)}{\sum_{\Delta\varphi} Cr(\Delta\varphi)}$$

$$n > 1$$

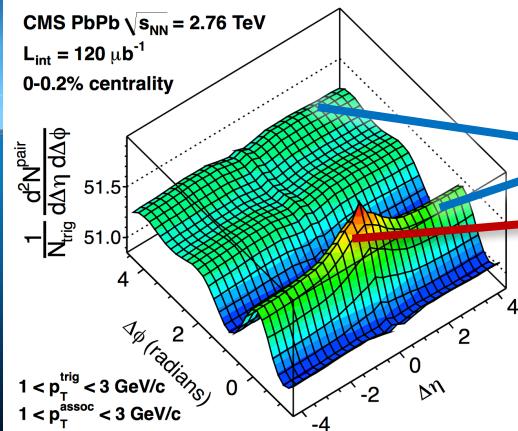
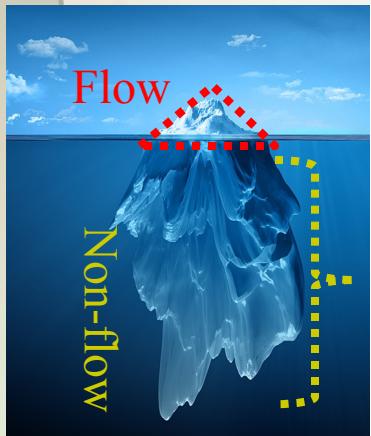
$$v_{nn} = v_n^a v_n^b + \delta_{short}$$

$$n = 1$$

$$v_{11} = v_1^a v_1^b + \delta_{long}$$

Flow

Non-flow



Long – range

Momentum  
Conservation

Di-jets

Short – range

HBT

Decay

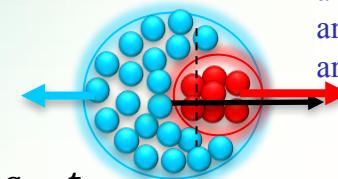
Charge

Non-flow suppression is needed

# Long range non-flow suppression

arXiv:1203.0931  
 arXiv:1203.3410  
 arXiv:1208.1874  
 arXiv:1208.1887  
 arXiv:1211.7162

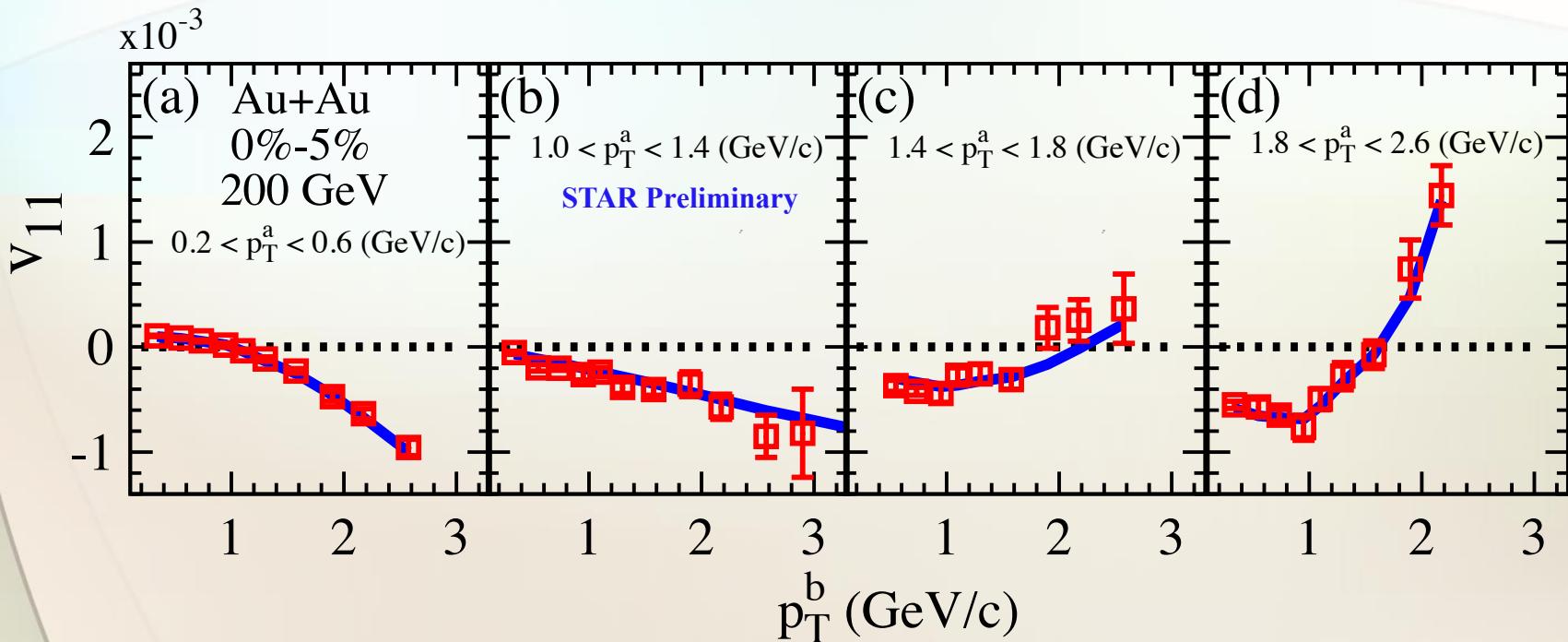
$$v_{11} = v_1^a v_1^b + \delta_{long} \quad n = 1$$



$$v_{11}(p_T^a, p_T^b) = v_1^{even}(p_T^a)v_1^{even}(p_T^b) - C p_T^a p_T^b \quad C \propto 1/\langle p_T^2 \rangle < Mult >$$

1

$v_{11}$  Eq(1) represents NxM matrix which we fit with N+1 parameters



- Good simultaneous fit ( $\frac{\chi^2}{ndf} \sim 1.1$ ) obtained with fit function Eq(1)
- $v_{11}$  characteristic behavior gives a good constraint for  $v_1^{even}(p_T)$  extraction

Long – range

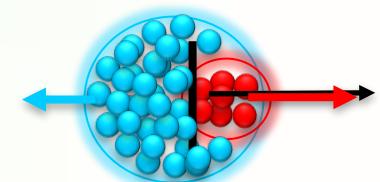
Momentum  
Conservation

## Long range non-flow suppression

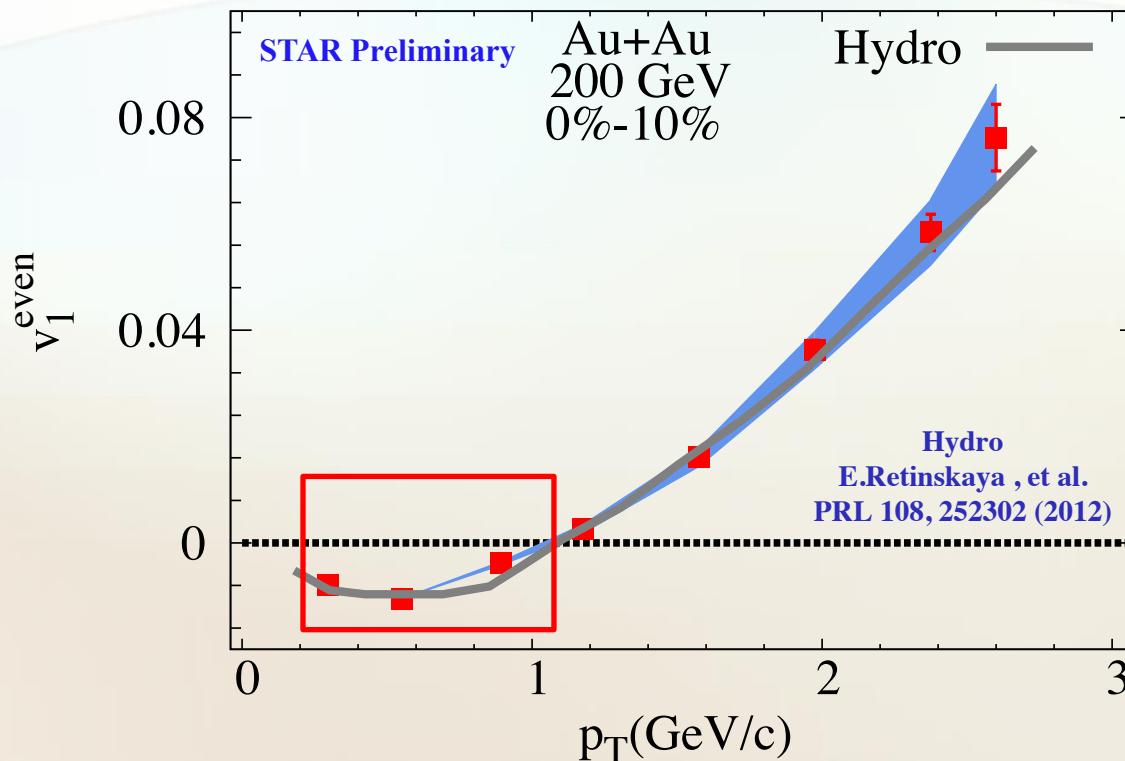
$|\eta| < 1$  and  $|\Delta\eta| > 0.7$

$$v_{11}(p_T^a, p_T^t) = v_1^{even}(p_T^a)v_1^{even}(p_T^t) - c p_T^a p_T^t$$

Dipolar nature requires that  $\int_0^\infty \frac{dN}{dp_T} p_T v_1^{even} = 0$



The extracted  $v_1^{even}(p_T)$  at 200 GeV and 0%-10% centrality



- The characteristic behavior of  $v_1^{even}(p_T)$  agrees with hydrodynamic expectations.

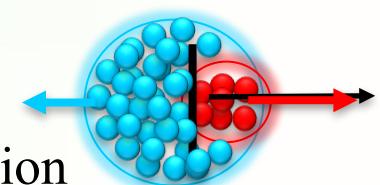
Long – range

Momentum  
Conservation

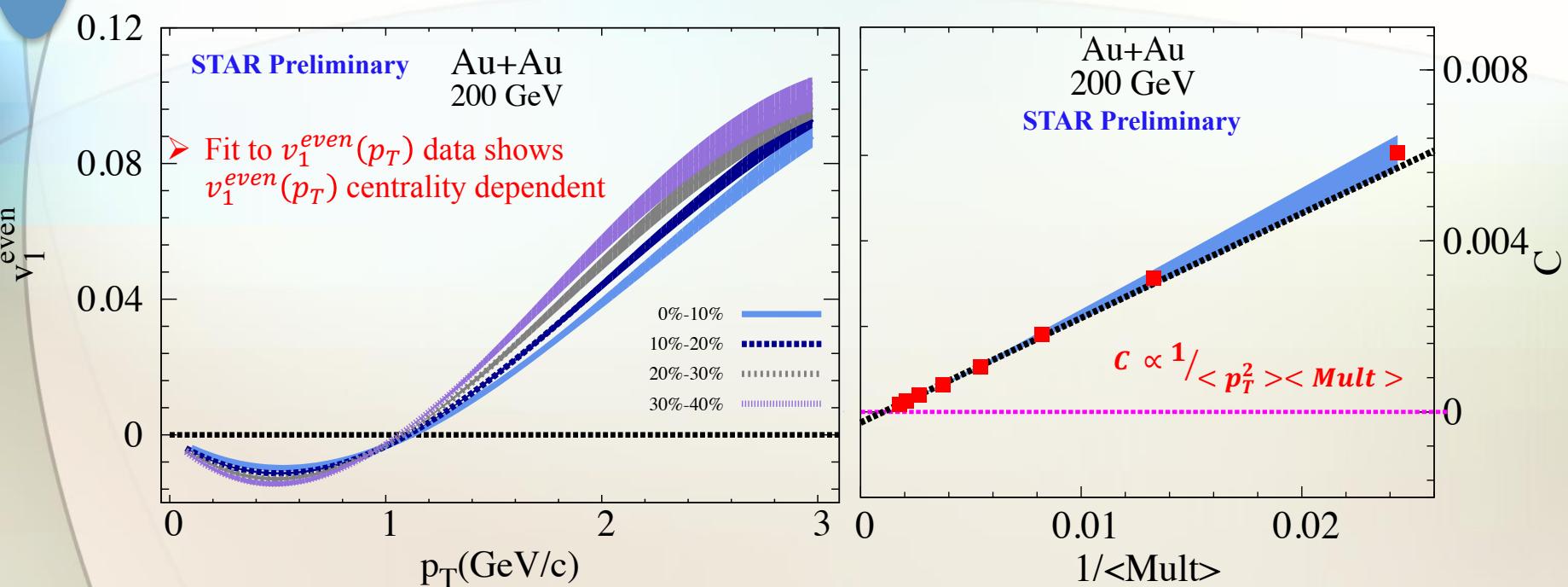
## Long range non-flow suppression

$|\eta| < 1$  and  $|\Delta\eta| > 0.7$

$$v_{11}(p_T^a, p_T^t) = v_1^{even}(p_T^a)v_1^{even}(p_T^t) - C p_T^a p_T^t$$



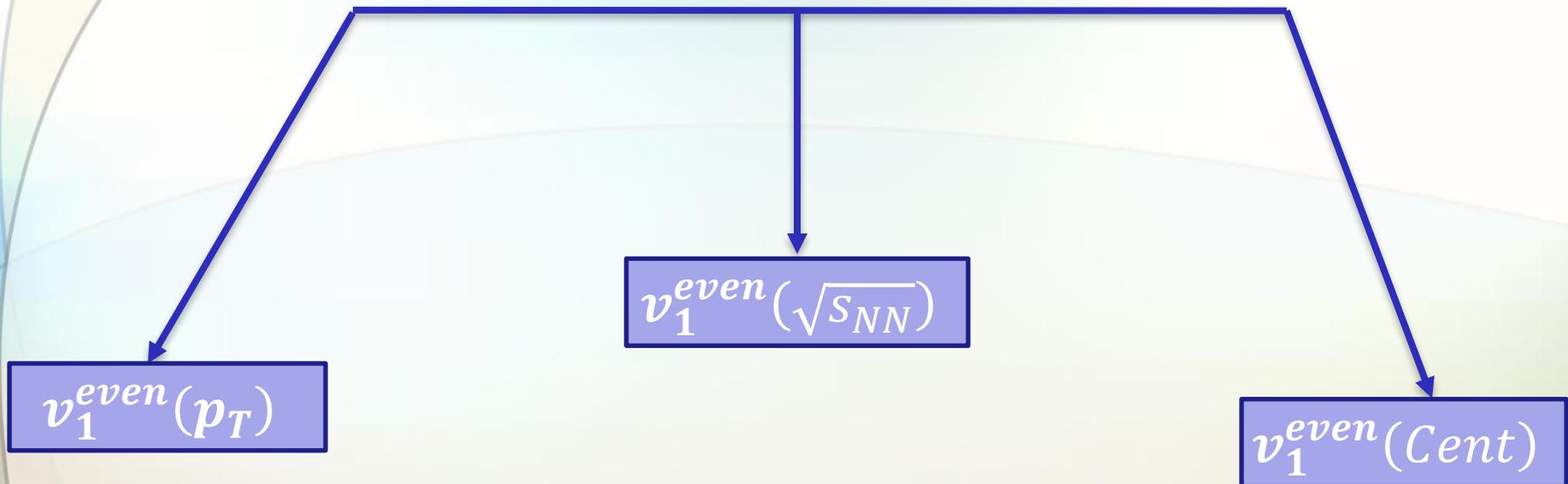
The extracted  $v_1^{even}(p_T)$  and the momentum conservation parameter  $C$  at 200 GeV



➤ The characteristic behavior of  $v_1^{even}(p_T)$  shows a weak centrality dependence

➤ The momentum conservation parameter  $C$  scales as  $\langle \text{Mult} \rangle^{-1}$

## Rapidity-even dipolar flow



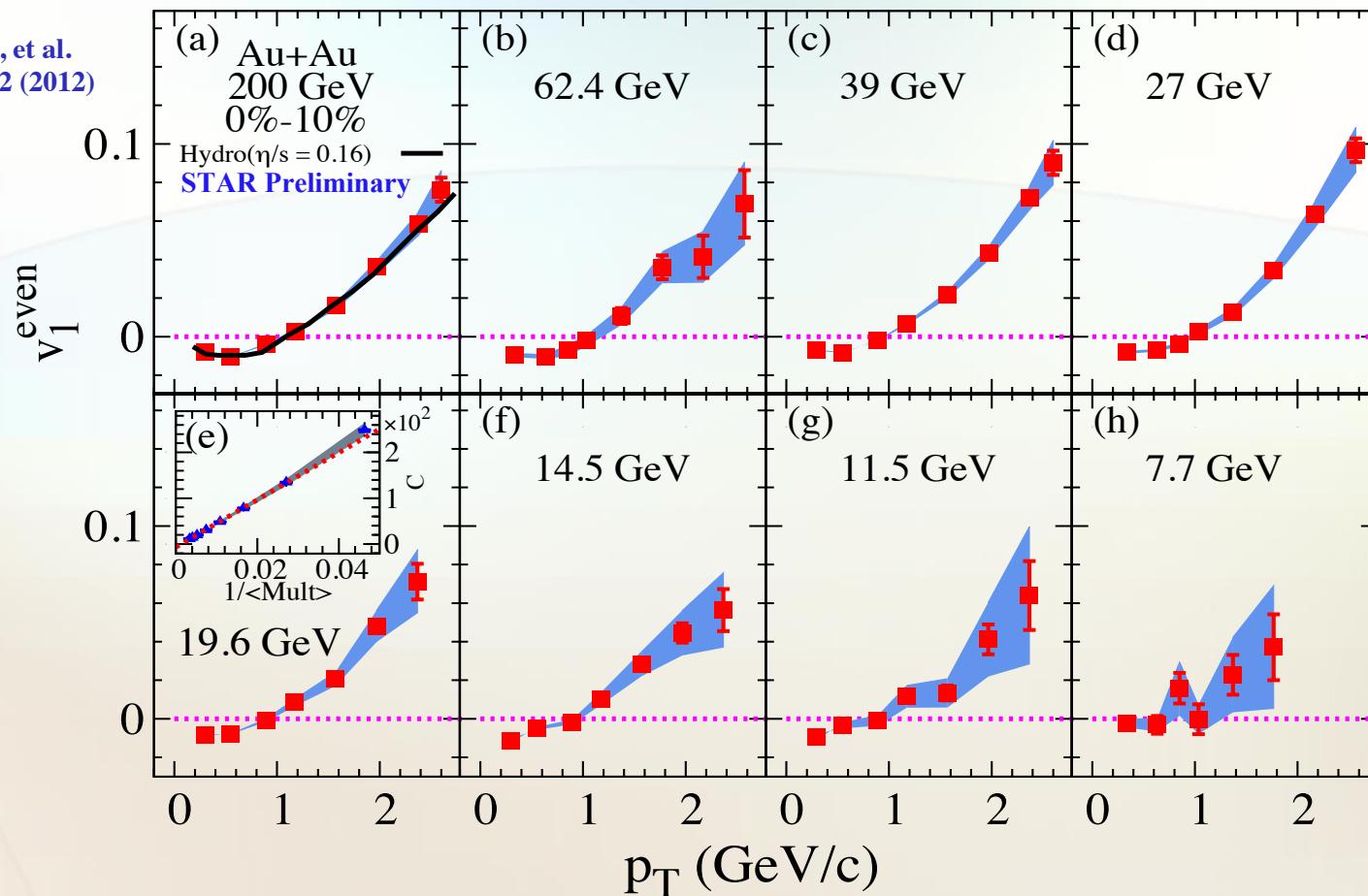
$|\eta| < 1$  and  $|\Delta\eta| > 0.7$

# Beam energy dependence of $v_1^{even}$

$$\mathbf{v}_{11}(p_T^a, p_T^t) = v_1^{even}(p_T^a)v_1^{even}(p_T^t) - C p_T^a p_T^t$$

The extracted  $v_1^{even}(p_T)$  at all BES energies

Hydro  
E.Retinskaya , et al.  
PRL 108, 252302 (2012)



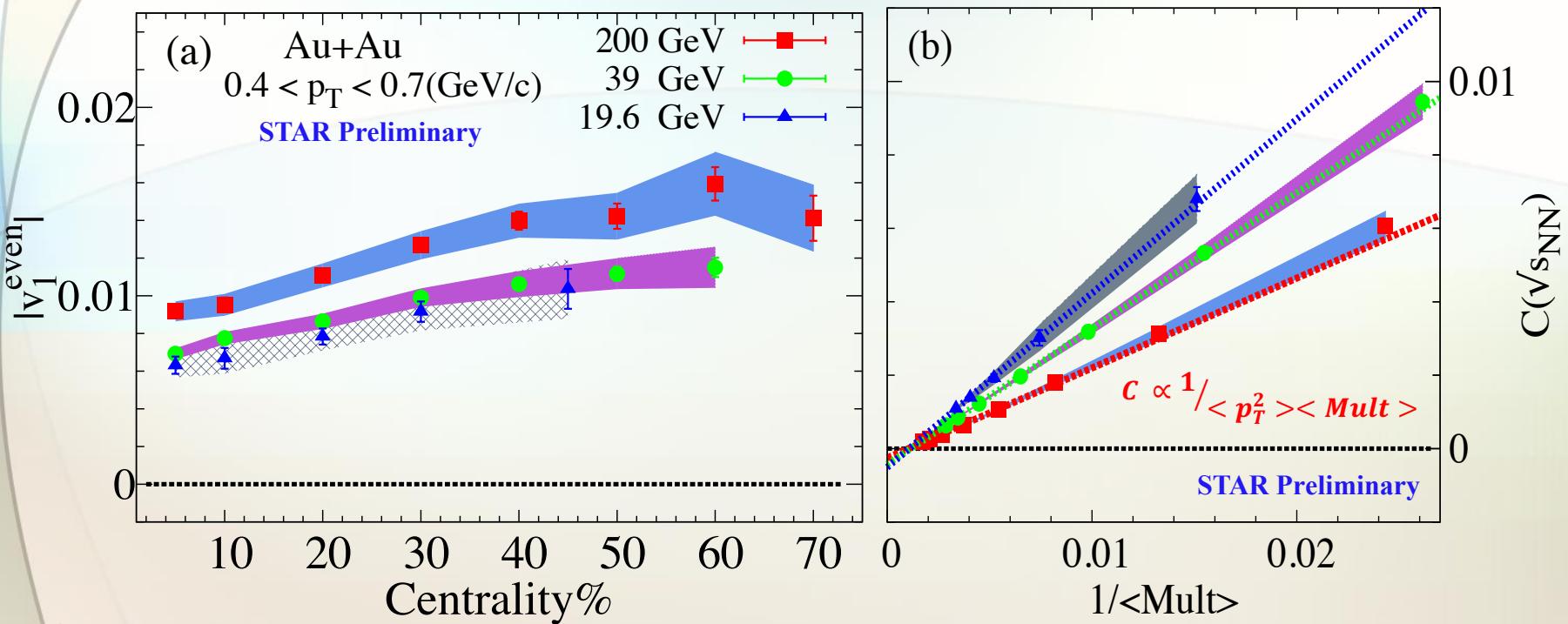
- Similar characteristic behavior of  $v_1^{even}(p_T)$  at all energies
- $v_1^{even}(p_T)$  agrees with hydrodynamic calculations at 200 GeV

$$|\eta| < 1 \text{ and } |\Delta\eta| > 0.7$$

# Beam energy dependence of $v_1^{even}$

$$v_{11}(p_T^a, p_T^t) = v_1^{even}(p_T^a)v_1^{even}(p_T^t) - c p_T^a p_T^t$$

The extracted  $v_1^{even}(Cent)$  and the momentum conservation parameter at different beam energies



➤ For different energies

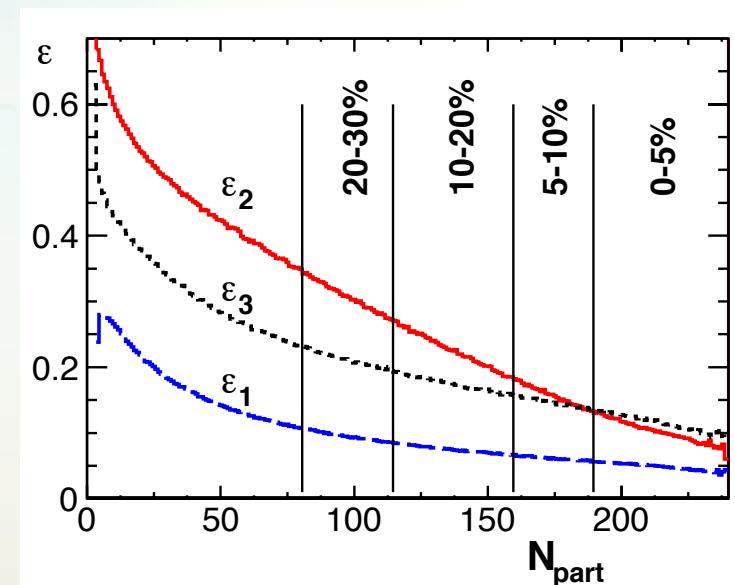
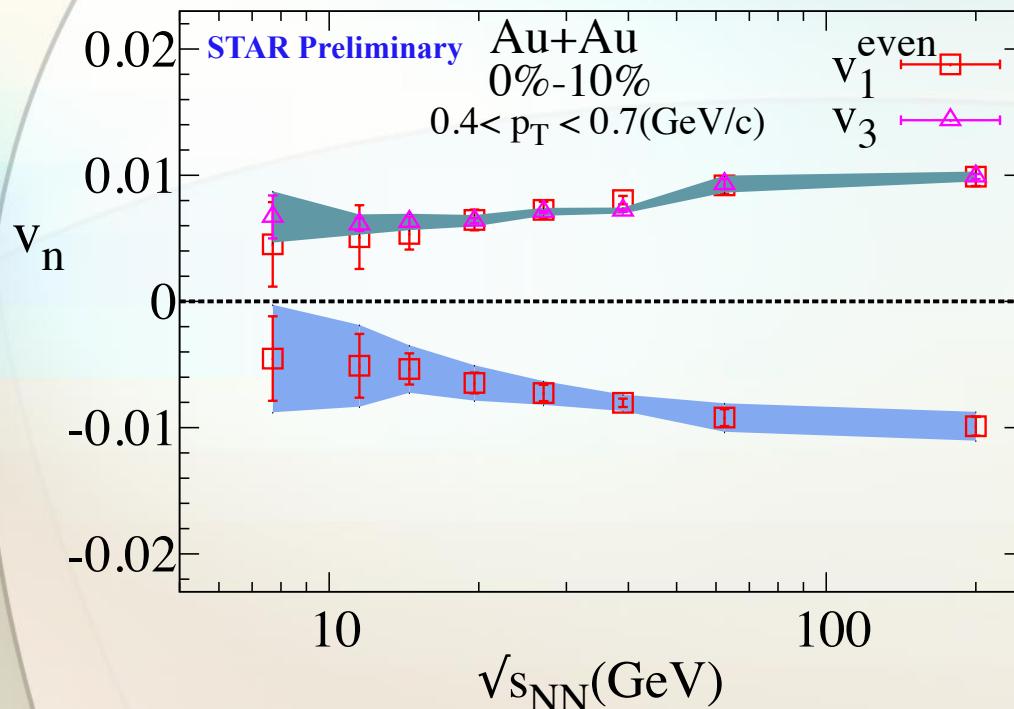
- ✓  $v_1^{even}$  increases as collisions become more peripheral
- ✓  $v_1^{even}$  shows a weak centrality dependence
- ✓ Momentum conservation parameter  $C$  scales as  $\langle \text{Mult} \rangle^{-1}$

$$|\eta| < 1 \text{ and } |\Delta\eta| > 0.7$$

# Beam energy dependence of $v_1^{even}$

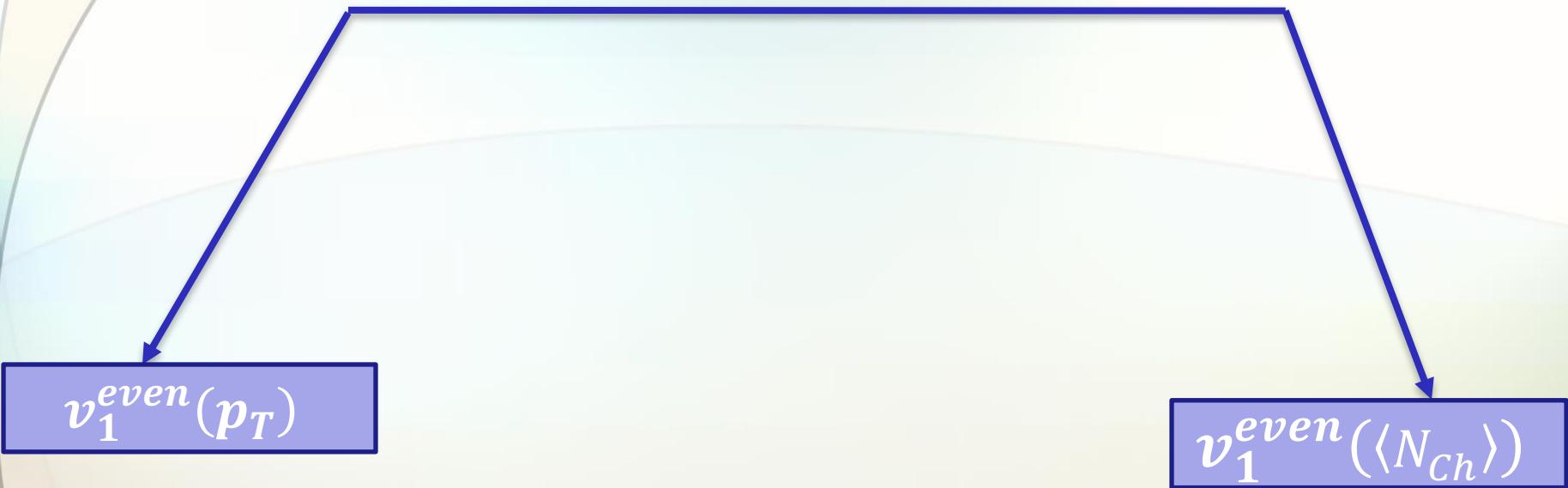
$$v_{11}(p_T^a, p_T^t) = v_1^{even}(p_T^a)v_1^{even}(p_T^t) - C p_T^a p_T^t$$

The extracted  $v_1^{even}$  vs  $\sqrt{s_{NN}}$  at 0%-10% centrality



- $|v_1^{even}|$  shows similar values to  $v_3$  at  $0.4 < p_T < 0.7 (\text{GeV}/c)$
- $\epsilon_3 > \epsilon_1$
- ✓  $v_3$  has larger viscous effect than  $v_1^{even}$

## Rapidity-even dipolar flow



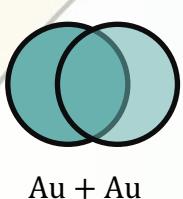
# Acoustic ansatz

PRC 84, 034908 (2011)  
P. Staig and E. Shuryak.

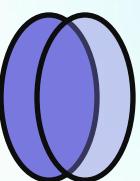
arXiv:1305.3341  
Roy A. Lacey, et al.

PRC 88, 044915 (2013)  
E. Shuryak and I. Zahed

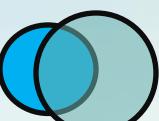
arXiv:1601.06001  
Roy A. Lacey, et al.



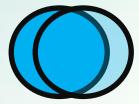
Au + Au



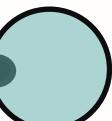
U + U



Cu + Au



d + Au



p + Au

- $v_n$  measurements for different systems are sensitive to system shape ( $\varepsilon_n$ ), dimensionless size ( $RT$ ) and transport coefficients  $\left(\frac{\eta}{s}, \frac{\zeta}{s}, \dots\right)$ .

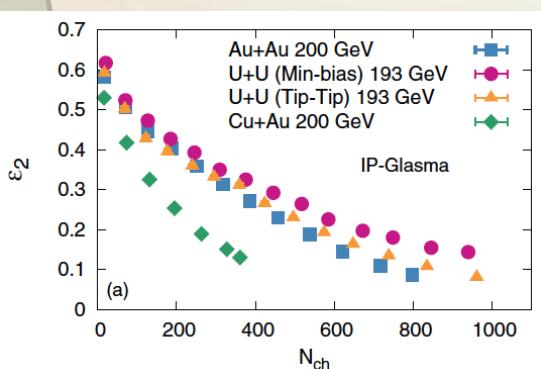
$$v_n/\varepsilon_n \propto e^{-A\left(\frac{\eta}{s}\frac{n^2}{RT}\right)}$$

$$S \sim (RT)^3 \sim \langle N_{ch} \rangle \text{ then } RT \sim \langle N_{ch} \rangle^{1/3}$$

$$\ln\left(\frac{v_n}{\varepsilon_n}\right) \propto -A \left(\frac{\eta}{s}\right) \langle N_{ch} \rangle^{-1/3}$$

## Even Harmonic $v_2$

$\varepsilon_2$  scaling is needed



B.Schenke , et al.  
PRC 89, 064908 (2014)

PRC 88, 044915 (2013)  
E. Shuryak and I. Zahed

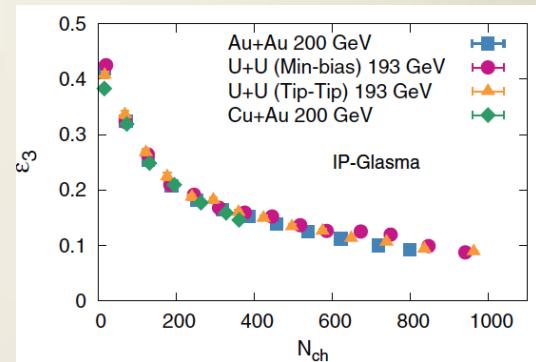
At the same  $\frac{\eta}{s}$  and  $\langle N_{ch} \rangle^{-1/3}$   
 $v_n \xrightarrow{\text{driven by}} \varepsilon_n + \dots$

## Expectations

- Odd harmonics are system independent
- Even harmonics are system dependent

## Odd Harmonic $v_3$

$$\varepsilon_3 \propto \frac{1}{\sqrt{N}}$$



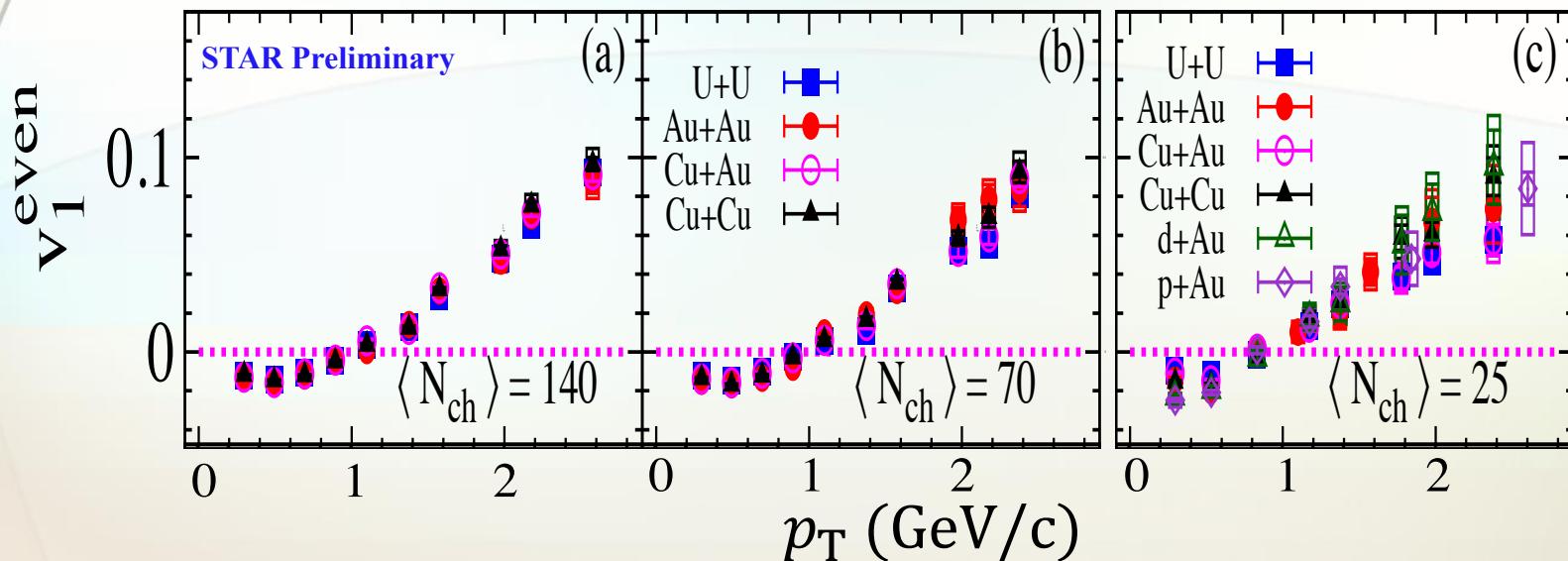
B.Schenke , et al.  
PRC 89, 064908 (2014)

# $v_1^{even}$ for different systems

$$\ln\left(\frac{v_n}{\varepsilon_n}\right) \propto -A (\eta/s) \langle N_{ch} \rangle^{-1/3}$$

$|\eta| < 1$  and  $|\Delta\eta| > 0.7$

$v_1^{even}$  vs  $p_T$  at different  $\langle N_{ch} \rangle$  for all systems



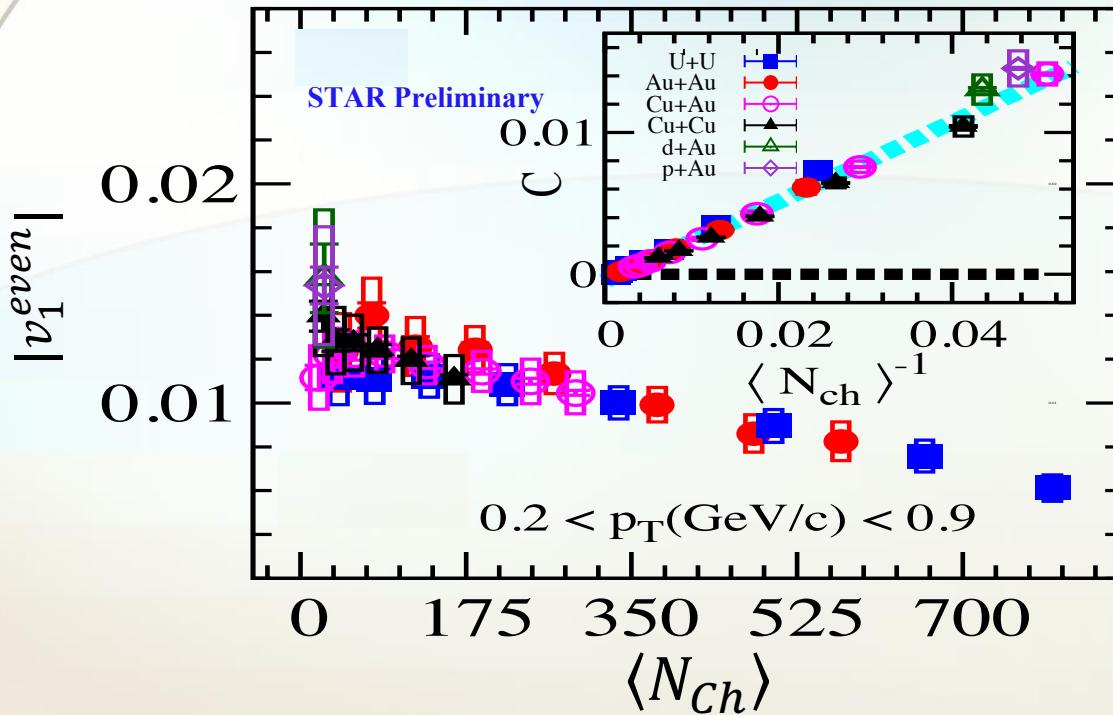
- The efficiency corrections for  $N_{Ch}$  have applied for Au+Au and U+U collisions.
- Within the experimental uncertainties  $v_1^{even}$  shows similar trends and magnitudes for all systems.
  - $v_1^{even}$  is system independent.

# $v_n$ for different systems

$$\ln\left(\frac{v_n}{\epsilon_n}\right) \propto -A (\eta/s) \langle N_{ch} \rangle^{-1/3}$$

$v_1^{even}$  vs  $\langle N_{ch} \rangle$  for all systems

$|\eta| < 1$  and  $|\Delta\eta| > 0.7$



- Momentum conservation parameter  $C$  scales as  $\langle N_{Ch} \rangle^{-1}$  for all systems

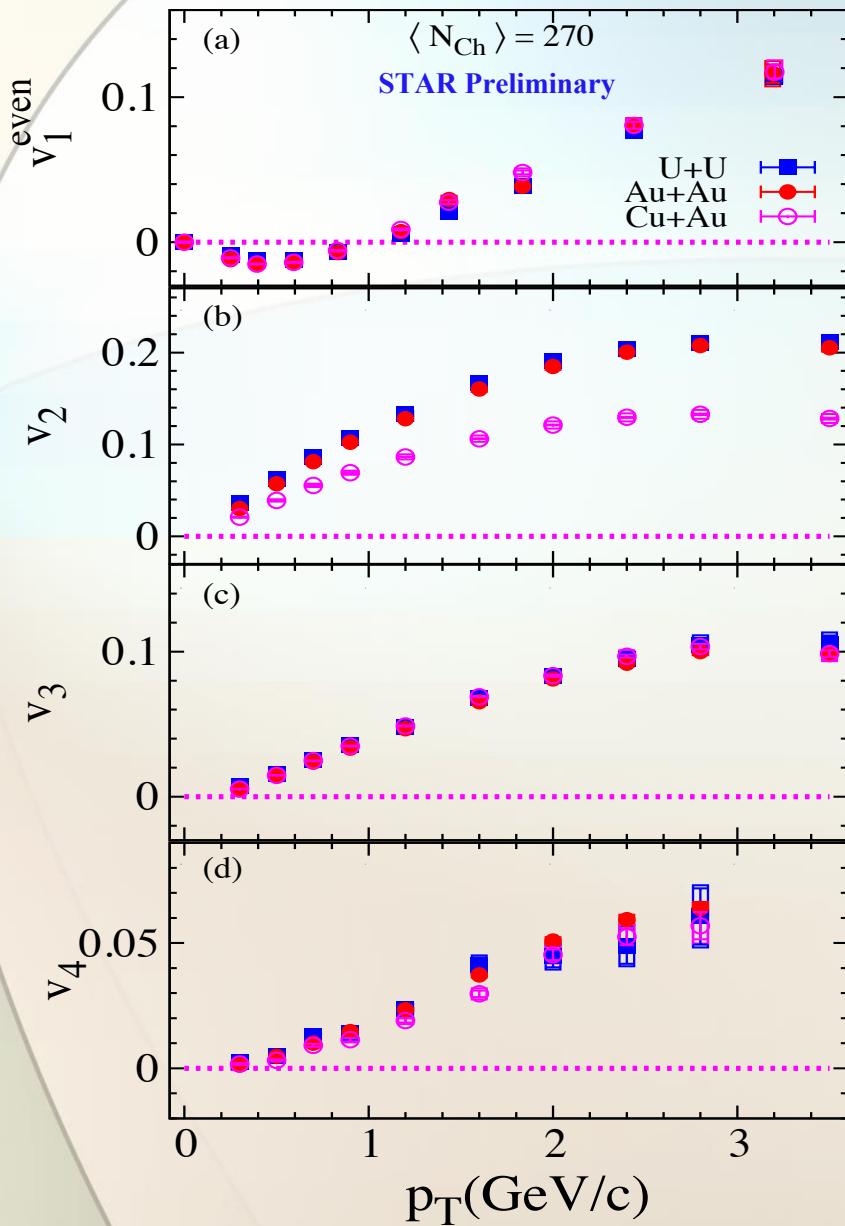
- The efficiency corrections for  $N_{Ch}$  have applied for Au+Au and U+U collisions.
- Within the experimental uncertainties  $v_1^{even}$  shows similar trends and magnitudes for all systems.
  - $v_1^{even}$  is system independent.

# $v_n$ for large systems ( $A + B$ )

$$\ln\left(\frac{v_n}{\varepsilon_n}\right) \propto -A (\eta/s)\langle N_{Ch} \rangle^{-1/3}$$

$v_n$  vs  $p_T$  at  $\langle N_{Ch} \rangle = 270$

$|\eta| < 1$  and  $|\Delta\eta| > 0.7$



- Odd harmonics are system independent.
- Even harmonics are system dependent with less dependence for higher harmonics.

# Conclusion

Comprehensive set of STAR measurements presented for  $v_1^{even}(p_T, \text{Cent}\%, \sqrt{s_{NN}})$  for several collision systems.

- For  $Au + Au$  beam energy scan
  - ✓  $v_1^{even}$  shows a weak dependence on centrality and beam energy
  - ✓ Within the experimental uncertainties  $|v_1^{even}|(\sqrt{s_{NN}})$  shows a similar magnitude to  $v_3$  suggesting that  $v_3$  has larger viscous effect than  $v_1^{even}$
- For different systems at similar multiplicity ( $200\text{ GeV}$ )
  - ✓ Within the experimental uncertainties  $v_1^{even}$  shows similar trends and magnitudes for all systems
  - ✓  $v_1^{even}$  is system independent.

Within the experimental uncertainties, the similar trends and magnitudes of the measured  $v_1^{even}$  for different colliding systems at  $\sqrt{s_{NN}} \sim 200\text{ GeV}$  suggest a comparable viscous coefficient  $(A \frac{\eta}{s})$

**THANK YOU**