

# Geometry and dynamics of particle production seen by femtoscopic probes in the STAR experiment

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**Warsaw University  
of Technology**



**Faculty  
of Physics**

WARSAW UNIVERSITY OF TECHNOLOGY

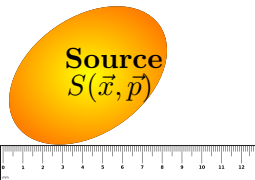


**NATIONAL SCIENCE CENTRE  
POLAND**



Strangeness in Quark Matter 2019  
Bari, Italy, 09-15.06.2019

Supported by the Polish National Science Centre grant no. 2017/27/B/ST2/01947



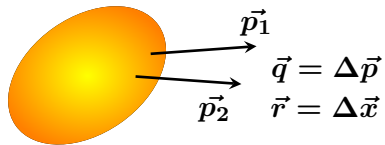
Impossible to examine the particle  
emitting source directly

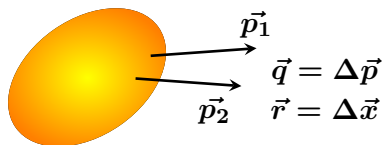
$$\text{size} \sim 10^{-15} \text{ m}$$

$$\text{life time} \sim 10^{-23} \text{ s}$$

**Femtoscscopy** measures space-time characteristics  
of the source through momentum correlations

# Femtoscropy





$$C(\vec{p}_1, \vec{p}_2) = \frac{P_{12}(\vec{p}_1, \vec{p}_2)}{P_1(\vec{p}_1)P_1'(\vec{p}_2)}$$

experiment

$$C(\vec{q}) = \frac{A(\vec{q})}{B(\vec{q})}$$

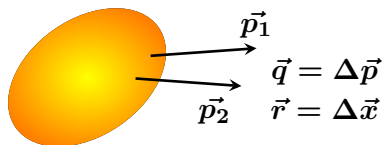
$A(\vec{q})$  - correlated  
 $B(\vec{q})$  - uncorrelated

theory (models)

$$C(\vec{q}) = \int d^3r S(\vec{q}, \vec{r}) |\Psi(\vec{q}, \vec{r})|^2$$

$S(\vec{q}, \vec{r})$  - source function  
 $\Psi(\vec{q}, \vec{r})$  - pair wave function

# Femtoscscopy



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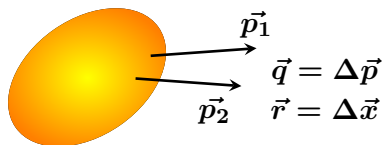
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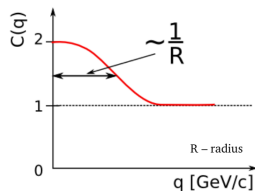
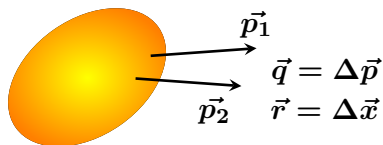
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# Femtoscscopy



calculate size ( $R$ ) of the source

$$C(\vec{p}_1, \vec{p}_2) = \frac{P_{12}(\vec{p}_1, \vec{p}_2)}{P_1(\vec{p}_1)P_1'(\vec{p}_2)}$$

experiment

theory (models)

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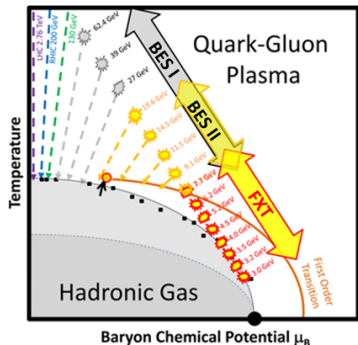
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# Introduction

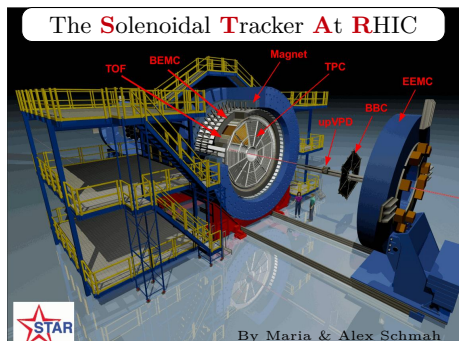
- **Kaon femtoscopy (geometry):**  
provides complementary information to pions
  - ▶ less affected by resonance decays
  - ▶ contain strange quark
  - ▶ heavier than pions
- **Non-identical particle femtoscopy (geometry + dynamics):**
  - ▶ examination of asymmetry in emission process between two kinds of particles ( $\pi K$ )
  - ▶ measuring Final State Interactions ( $p\Omega$ )



Nucl. Phys. A 967, 808 (2017)



# The STAR experiment



## Time Projection Chamber

PID:  $dE/dx$

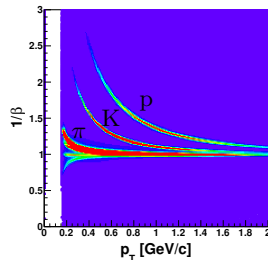
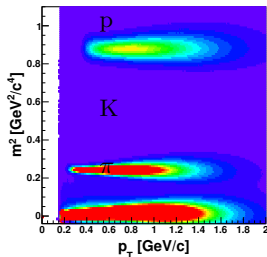
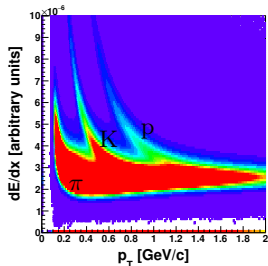
Tracking

$$0 < \phi < 2\pi, |\eta| < 1$$

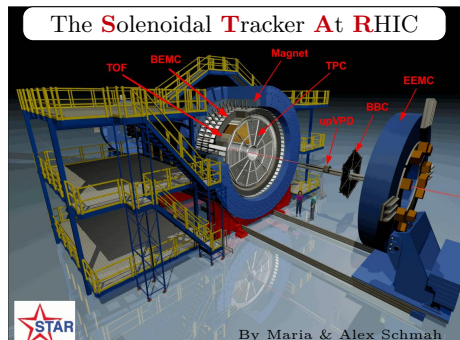
## Time-Of-Flight

Time resolution  $< 80$  ps

PID:  $m^2$  &  $1/\beta$



# The STAR experiment



## Time Projection Chamber

PID:  $dE/dx$

Tracking

$$0 < \phi < 2\pi, |\eta| < 1$$

## Time-Of-Flight

Time resolution  $< 80$  ps

PID:  $m^2$  &  $1/\beta$

$\sqrt{s_{NN}}$ [GeV]	7.7	11.5	39		
			(0-10%)	(10-30%)	(30-70%)
#events [mln]	0.24	1.3	11.7	25.7	45.4

## Longitudinally Co-Moving System (LCMS)

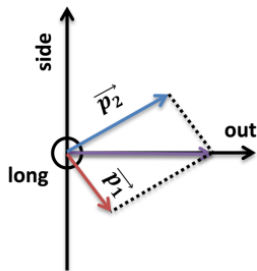
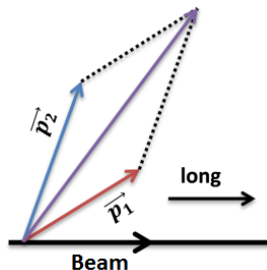
G. Bertsch, et al. S. Pratt.  
Phys. Rev. C37, 1896, (1988) Phys. Rev. D33, 1314 (1986)

**Long:** sensitive to the longitudinal dynamics and evolution time

**Out:** sensitive to the geometrical size, emission time and space-time correlation

**Side:** sensitive to the geometrical size

$$k_T = \frac{|p_{T,1} + p_{T,2}|}{2}$$



# Reference frame

## Pair Rest Frame (PRF)



$$k_T = \frac{|p_{T,1} + p_{T,2}|}{2}$$

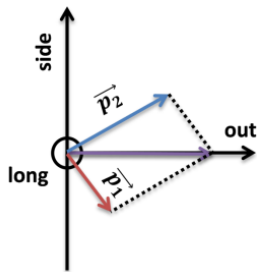
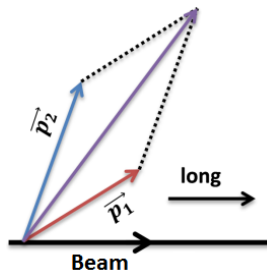
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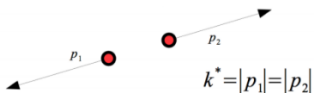
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# Reference frame

## Pair Rest Frame (PRF)



## Longitudinally Co-Moving System (LCMS)

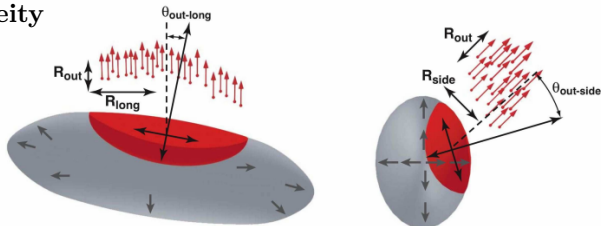
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**Side:** sensitive to the geometrical size

## Region of homogeneity



$$k_T = \frac{|p_{T,1} + p_{T,2}|}{2}$$

Ann. Rev. Nucl. Part. Sci 55, 357 (2005)  
Phys. Lett. B356, 525 (1995)

# Kaons — fitting procedure

$$S(\vec{r}) \sim \exp\left(-\frac{r_o^2}{4R_o^2} - \frac{r_s^2}{4R_s^2} - \frac{r_l^2}{4R_l^2}\right)$$
$$|\Psi(\vec{q}, \vec{r})|^2 = 1 + \cos(\vec{q}\vec{r})$$

**Bowler-Sinyukov formula:**

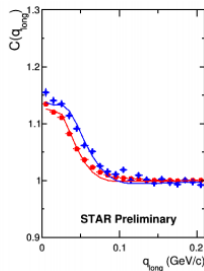
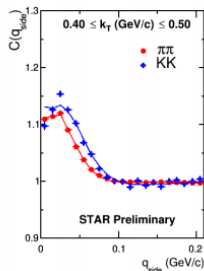
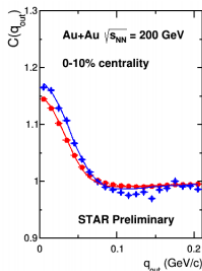
$$C(q_o, q_s, q_l) = 1 - \lambda + \lambda K(q_{inv})(1 + \exp[-R_o^2 q_o^2 - R_s^2 q_s^2 - R_l^2 q_l^2])$$

$\lambda$  - the correlation strength

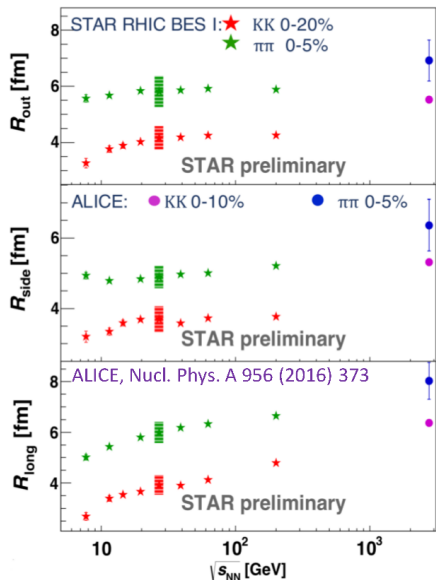
$K(q_{inv})$  - Coulomb factor

M. Bowler  
Phys. Lett. B270, 69 (1991)

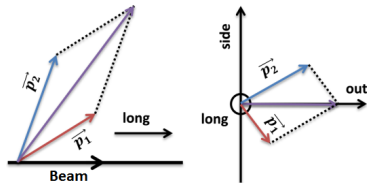
Y. Sinyukov, et al.  
Phys. Lett. B432, 248 (1997)



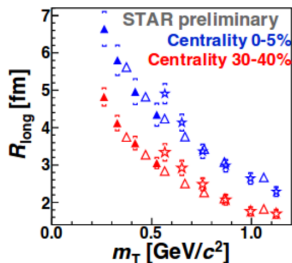
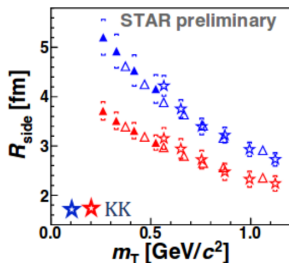
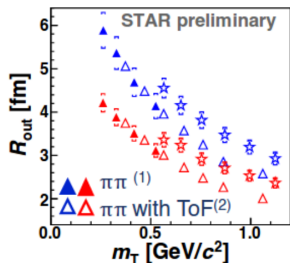
# Radii from BES-I



- $R_{side}$  spatial source evolution in the transverse direction
- $R_{out}$  related to spatial and time components
- $R_{long}$  temperature of kinetic freezeout and source lifetime



# Results from 200 GeV



- $R_{side}$  trend for kaons is similar to that of pions
- $R_{out}$  and  $R_{long}$  of pion and kaon source radii follow different  $m_T$  dependences
- $R_{long}(K) > R_{long}(\pi)$ 
  - ▶ contribution from long-lived resonances at the kinetic freeze-out?<sup>(3)</sup>

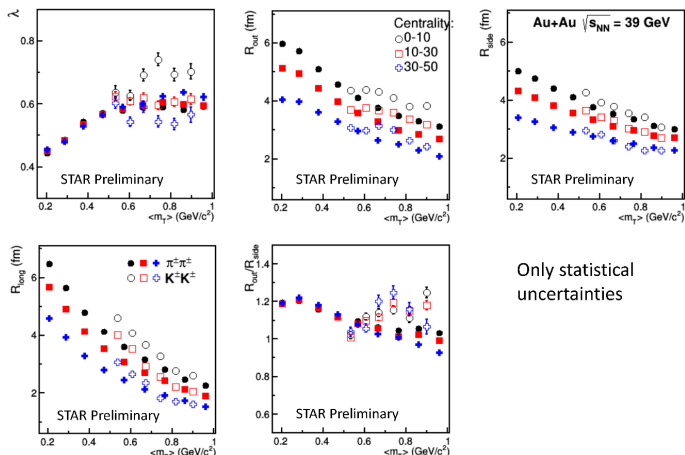
(1) STAR, Phys. Rev. C 92, 014904 (2015)

(2) STAR Preliminary

(3) Y. Sinyukov, et al. Nucl. Phys. A 946, 227 (2016)



# Results from 39 GeV



Only statistical uncertainties

- $R_{long}$  &  $R_{out}$  are larger for kaons at the same  $m_T \rightarrow$  breaking of the  $m_T$ -scaling
- $R_{side}$  radii for pions and kaons are closer than in other directions

# Pion-kaon femtoscopy — Spherical harmonics (SH)

SH representation of 3D correlation function as a set of 1D plots

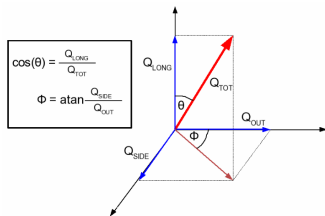
$$C(\mathbf{q}) = \sum_{l,m} C_l^m(q) Y_l^m(\theta, \phi) \quad C_l^m(q) = \int_{\Omega} C(q, \theta, \phi) Y_l^m(\theta, \phi) d\Omega$$

$\Omega$  - full solid angle

$Y_l^m(\theta, \phi)$  - spherical harmonic function

$q = |\mathbf{q}|$  - pair relative momentum

$\theta$  and  $\phi$  - polar and azimuthal angle



P. Danielewicz and S. Pratt.  
Phys. Lett B618, 60 (2005)  
Phys. Rev. C75, 034907 (2007)

Z. Chajecki and M. Lisa  
Phys. Rev. C78, 064903 (2008)

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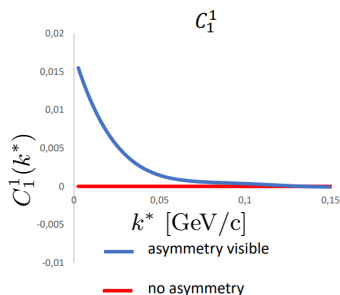
$Y_l^m(\theta, \phi)$  - spherical harmonic function

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$\theta$  and  $\phi$  - polar and azimuthal angle

$C_0^0 \rightarrow$  sensitive to the size of the emitting source  
(shapes same as correlation function)

$C_1^1 \rightarrow$  sensitive to the spacetime emission asymmetry



P. Danielewicz and S. Pratt.  
Phys. Lett B618, 60 (2005)  
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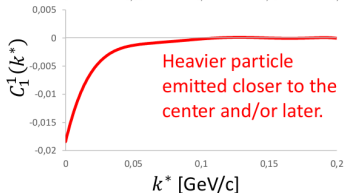
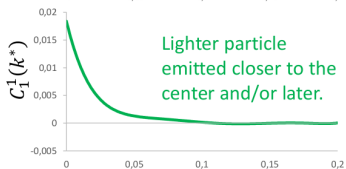
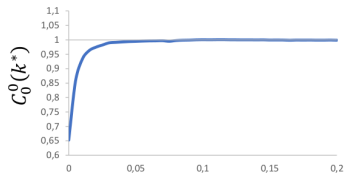
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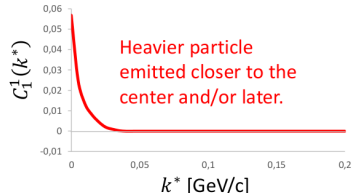
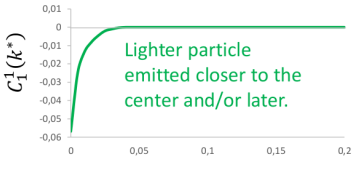
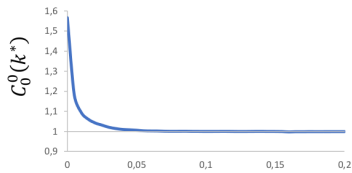
A. Kisiel  
Phys. Rev. C81, 064906 (2010)

# Which particle...?

## Like-sign particle combinations



## Unlike-sign particle combinations



# Pion-kaon femtoscopy — asymmetry

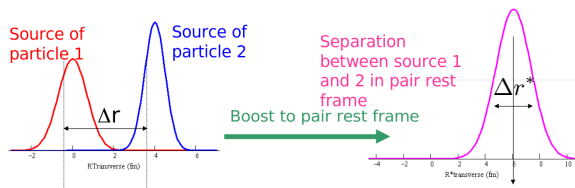
$$C(\vec{q}) = \int |\Psi(\vec{q}, \vec{r})|^2 S(\vec{r}) d^3r$$

known
unknown

R. Lednicky, et al.  
Phys. Lett. B373, 30 (1996)

$$S(\vec{r}) = \exp\left(-\frac{(r_{out} - \mu_{out})^2}{\sigma_{out}^2} - \frac{r_{side}^2}{\sigma_{side}^2} - \frac{r_{long}^2}{\sigma_{long}^2}\right)$$

$\mu_{out}$  — asymmetry in the *outward* direction  
 assumption:  $\sigma_{side} = \sigma_{out}$ ,  $\sigma_{long} = 1.3\sigma_{out}$



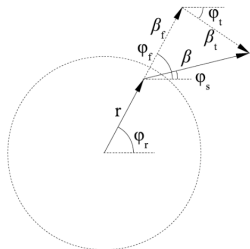
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$$\beta_{particle} = \beta_f + \beta_t$$

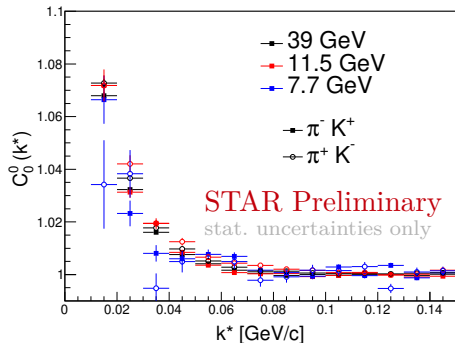
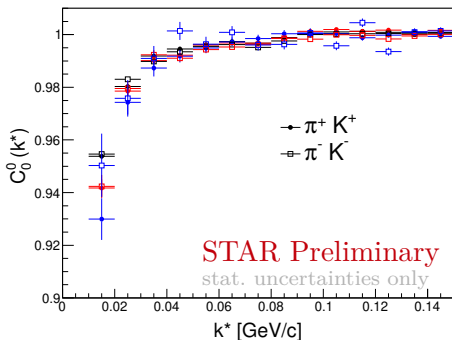
$\beta_f$  — collective (flow) velocity

$\beta_t$  — thermal (random) velocity

A. Kisiel  
Phys. Rev. C81, 064906 (2010)

Emission asymmetry arises in a system where both thermal and collective velocities exist and are comparable in magnitude

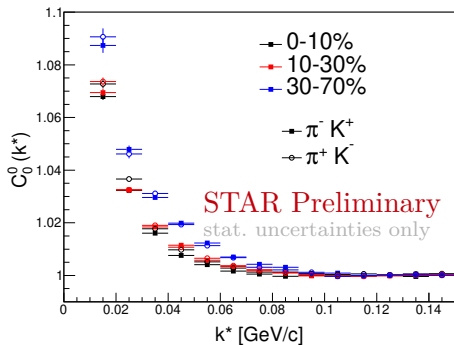
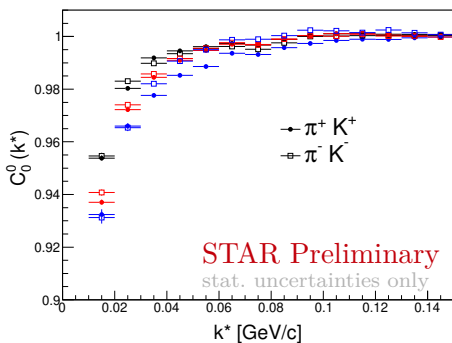
# Energy dependence



- Visible energy dependence

- Higher statistics for lowest energy needed (BES-II)

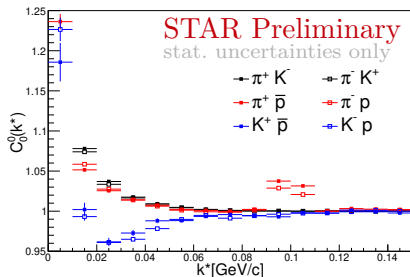
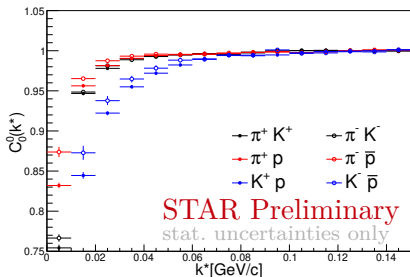
# Centrality dependence, $\sqrt{s_{NN}} = 39$ GeV



- Visible centrality dependence

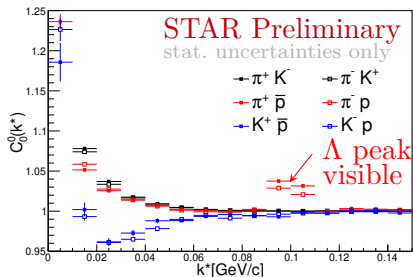
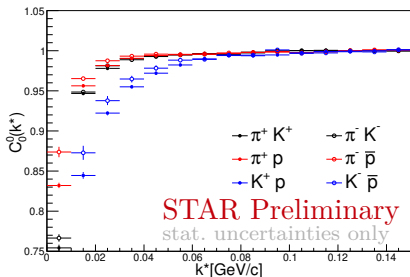


# System dependence, $\sqrt{s_{NN}} = 39$ GeV, 0-10%



- Like sign pairs are dominated by Coulomb
- Kp  $\rightarrow$  strongest correlation

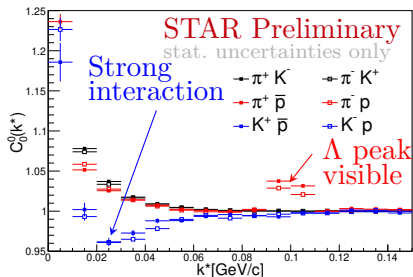
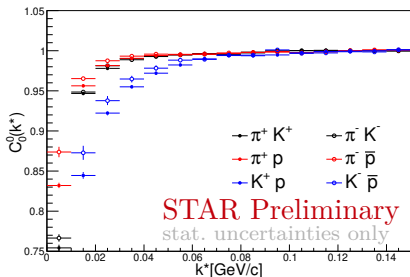
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- Unlike sign more complicated
- $\Lambda$  peak visible in pion-proton

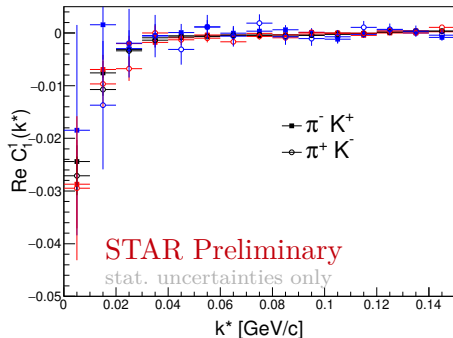
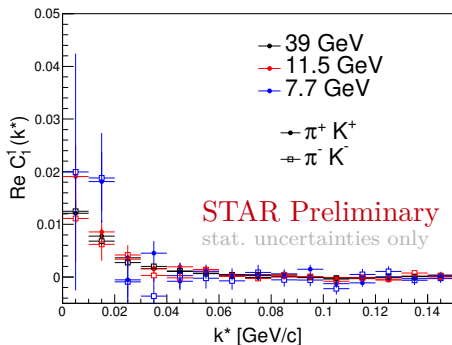
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- Like sign pairs are dominated by Coulomb
- Kp  $\rightarrow$  strongest correlation

- Unlike sign more complicated
- $\Lambda$  peak visible in pion-proton
- Strong interaction not negligible in Kp

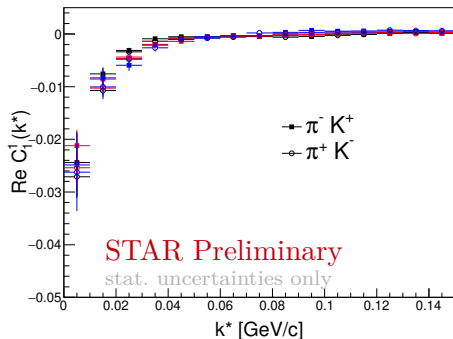
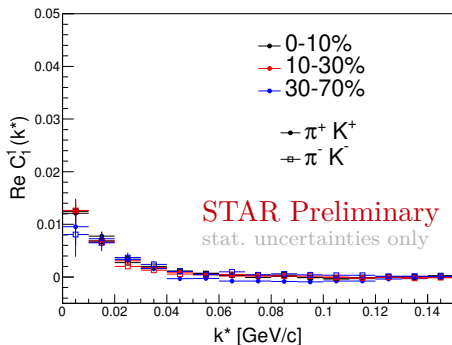
# Source dynamics — energy dependence



- Clear signal of emission asymmetry

- Visible energy dependence

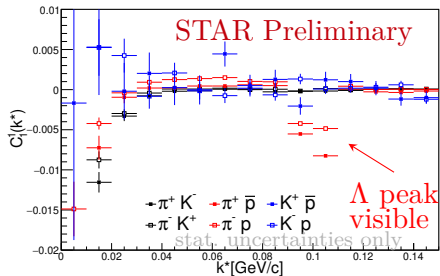
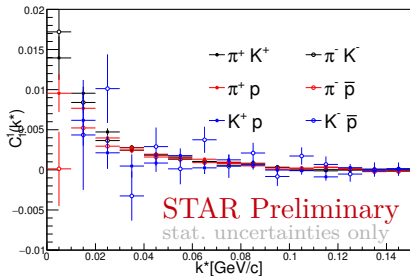
# Source dynamics — centrality dependence



- Clear signal of emission asymmetry

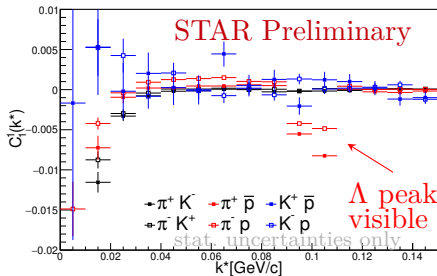
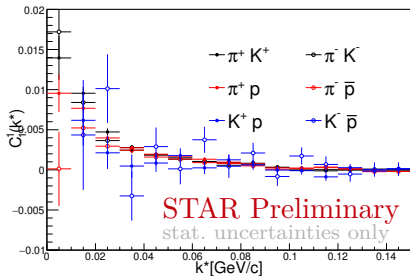
- Visible centrality dependence

# Source dynamics — system dependence



- Visible signal of emission asymmetry

# Source dynamics — system dependence



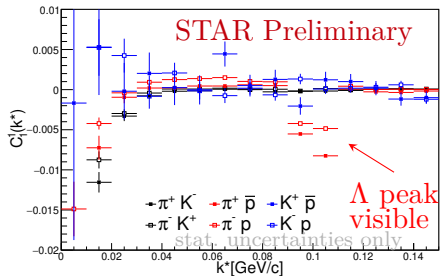
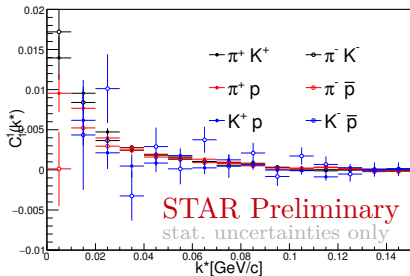
- Visible signal of emission asymmetry

- Expected ordering of particles — confirmed

Lighter particle is emitted closer to the center and/or later.

R. Lednicky, et al., Phys. Lett. B272, 20 (1996)  
STAR, Phys. Rev. Lett. 91, 262302 (2003)  
A. Kisiel, Phys. Rev. C81, 064906 (2010)

# Source dynamics — system dependence



- Visible signal of emission asymmetry

- Expected ordering of particles — confirmed

We are sensitive to collective effects



# $p\Omega$ dibaryon

## The ways to study

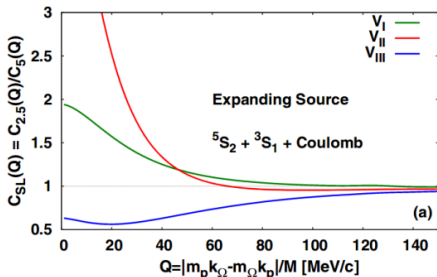
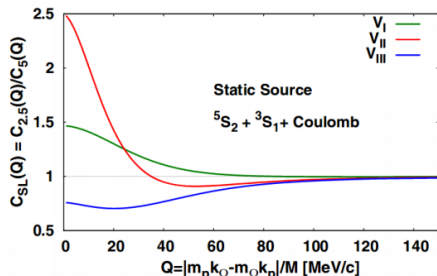
- Invariant mass method  
(Large combinatorial background)
- Two-particle correlation functions  
(Final State Interactions, exotic particles)

The ratio of correlation function between small and large collision systems can be used to extract strong interactions between proton and  $\Omega$

K. Morita et al. Phys. Rev. C 94, 031901 (2016)

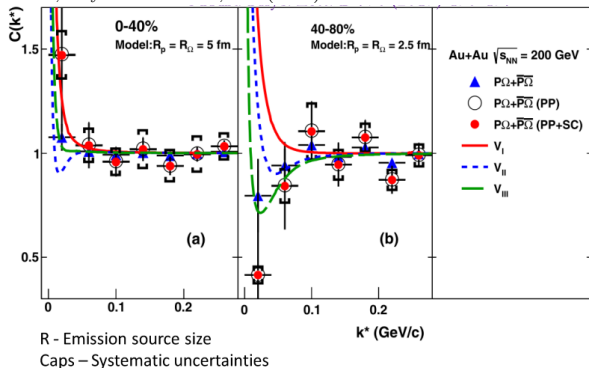
TABLE I. Binding energy ( $E_B$ ), scattering length ( $a_0$ ), and effective range ( $r_{\text{eff}}$ ) with and without the Coulomb attraction in the  $p\Omega$  system. Physical masses of the proton and  $\Omega$  are used.

Spin-2 $p\Omega$ potentials		$V_I$	$V_{II}$	$V_{III}$
Without Coulomb	$E_B$ (MeV)		0.05	24.8
	$a_0$ (fm)	-1.0	23.1	1.60
	$r_{\text{eff}}$ (fm)	1.15	0.95	0.65
With Coulomb	$E_B$ (MeV)		6.3	26.9
	$a_0$ (fm)	-1.12	5.79	1.29
	$r_{\text{eff}}$ (fm)	1.16	0.96	0.65



# $p\Omega$ correlation functions

STAR, Phys. Lett. B 790, 490 (2019)



K. Morita et al. Phys. Rev. C 94, 031901 (2016)

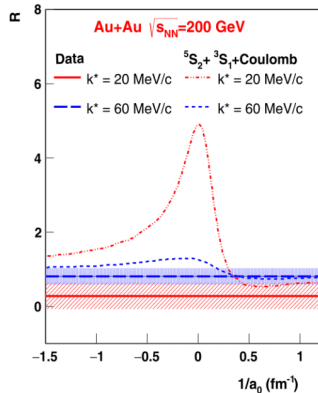
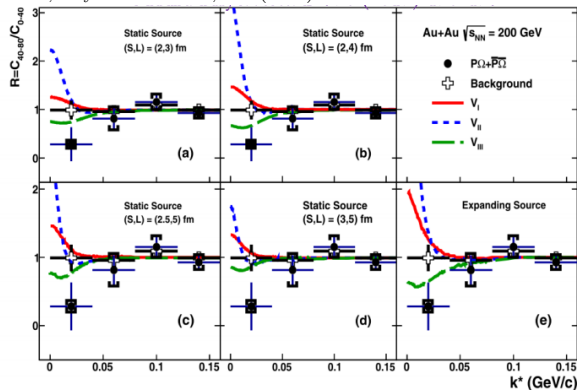
Binding energy ( $E_b$ ), scattering length ( $a_0$ ) and effective range ( $r_{\text{eff}}$ ) for the Spin-2 proton- $\Omega$  potentials [24].

Spin-2 $p\Omega$ potentials	$V_I$	$V_{II}$	$V_{III}$
$E_b$ (MeV)	–	6.3	26.9
$a_0$ (fm)	–1.12	5.79	1.29
$r_{\text{eff}}$ (fm)	1.16	0.96	0.65

Comparison of the measured  $p\Omega$  correlation functions from 0-40% and 40-80% central Au+Au collisions with the predictions for  $p\Omega$  interaction potentials  $V_I$ ,  $V_{II}$  and  $V_{III}$

# $p\Omega$ correlation functions

STAR, Phys. Lett. B 790, 490 (2019)



- Data favor a positive scattering length for the  $p\Omega$  interaction
- Positive scattering length and measured ratio less than unity for  $k^* < 40$  MeV/c (within  $1\sigma$ ) favors  $p\Omega$  interaction potential  $V_{III}$  with  $E_b \sim 27$  MeV for proton and  $\Omega$

## Geometry:

- Femtoscopy is sensitive to the homogeneity length
- Visible centrality, system and energy dependence of source size at BES energies
- Pion and kaon radii seem to follow different  $m_T$  dependence

## Dynamics:

- Clear signal of emission asymmetry for pion-kaon systems
  - ▶ which implies collectivity effects
- Lighter particles are emitted closer to the center and/or later

## Hadron physics:

- Obtained data indicate that the scattering length is positive and favor  $p\Omega$  bound state hypothesis

Thank you for your attention