

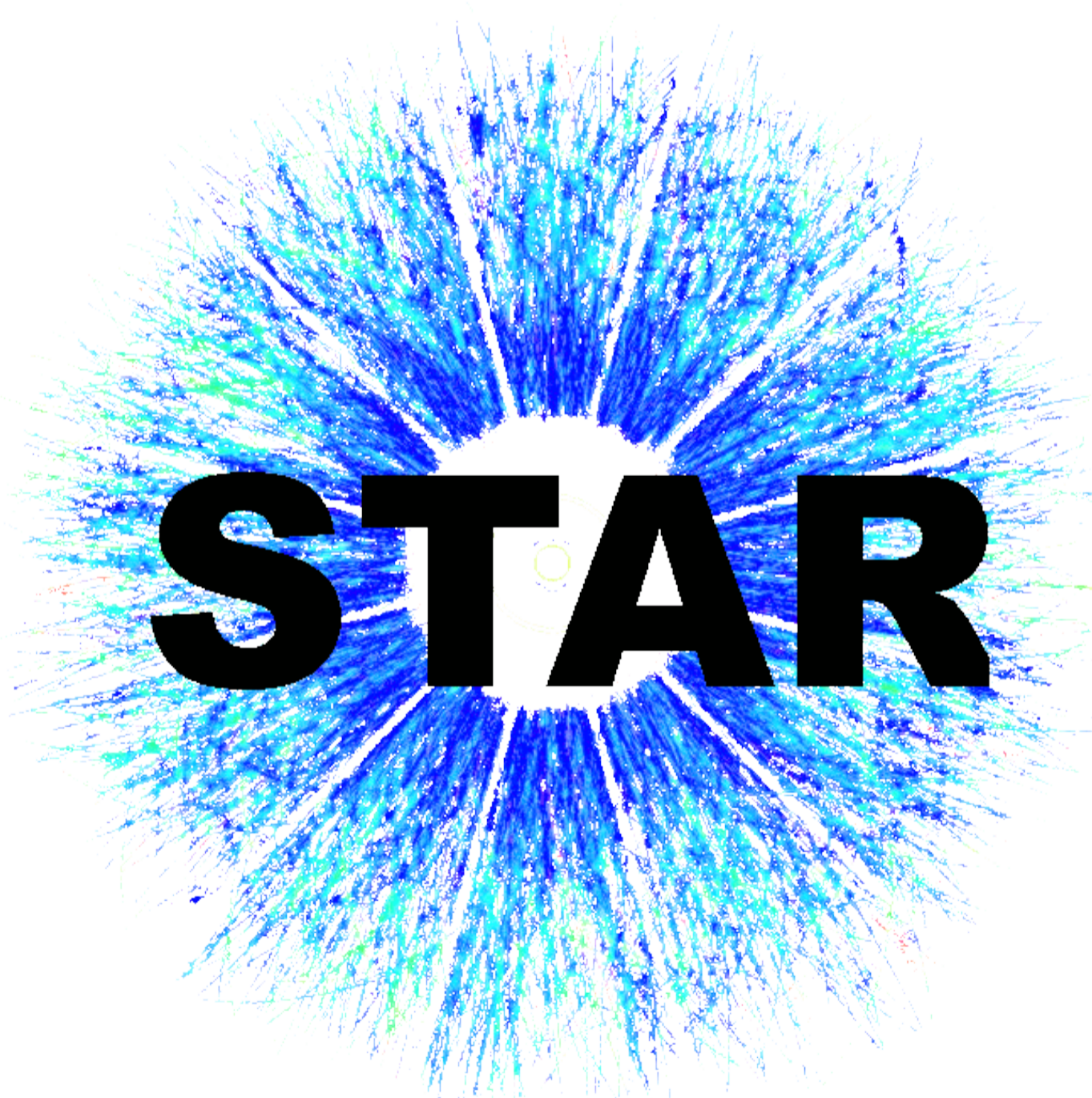
# Study of nonflow baseline for the CME signal via two-particle $(\Delta\eta, \Delta\phi)$ correlations in isobar collisions at STAR

– a poster for Quark Matter 2022

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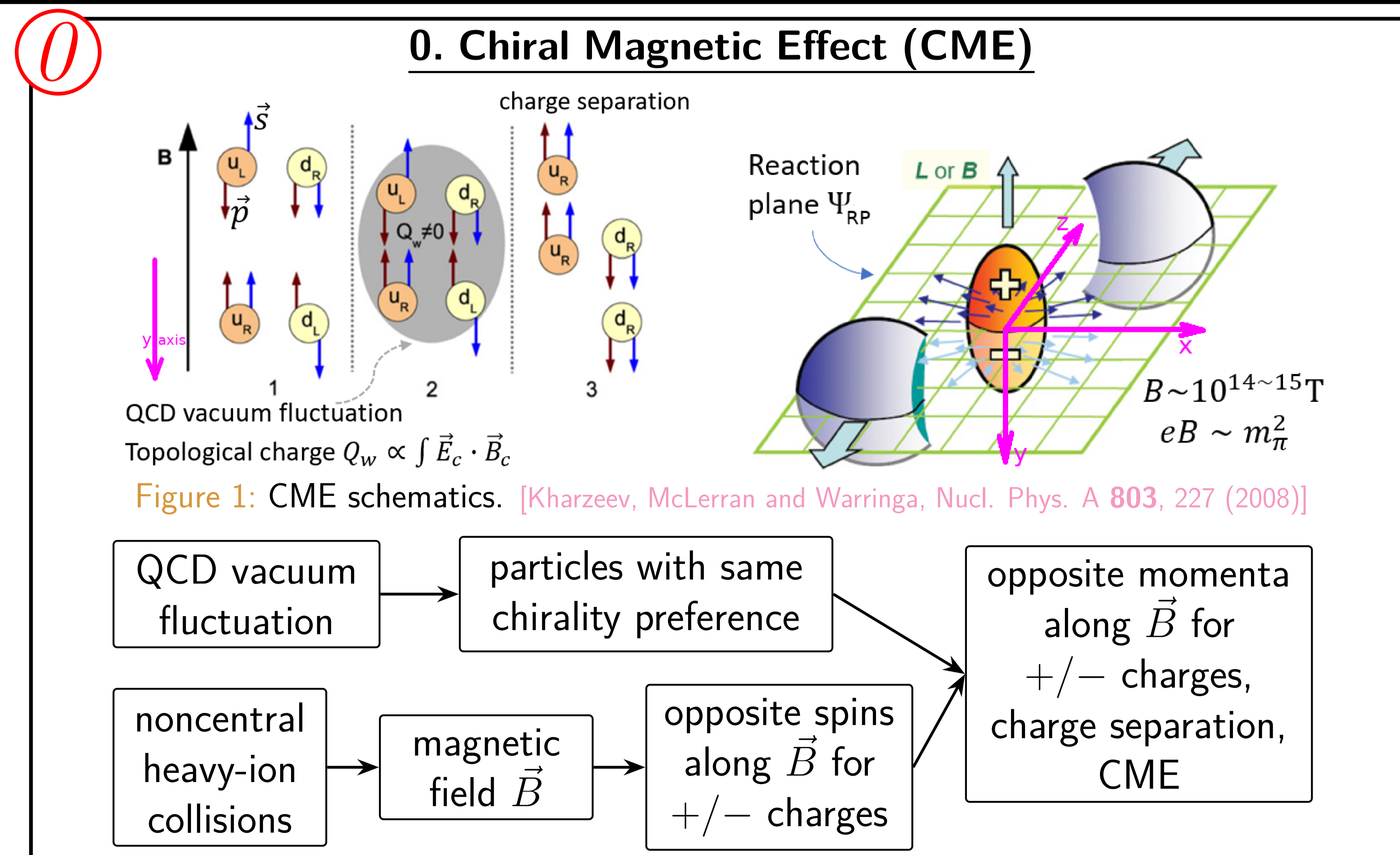
## Abstract

We study nonflow contributions in isobar data and arrive at a new background estimate for CME.

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## 1. $\Delta\gamma$ Observable

- ▶ The CME-sensitive observable  $\Delta\gamma$  is widely used,  $\Delta\gamma \equiv C_3/v_2^*$ , where  $C_{3,os} = \langle \cos(\phi_\alpha^\pm + \phi_\beta^\mp - 2\phi_c) \rangle$ ,  $C_{3,ss} = \langle \cos(\phi_\alpha^\pm + \phi_\beta^\pm - 2\phi_c) \rangle$ ,  $C_3 = C_{3,os} - C_{3,ss}$ . The subscript OS stands for opposite-sign pair and SS for same-sign pair.
- ▶ The asterisk (\*) on  $v_2$  indicates it is the measured  $v_2$  containing nonflow.
- ▶  $\Delta\gamma$  contains CME and a major background proportional to  $v_2$  (true  $v_2$  flow).

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## 2. Isobar Results

- ▶ Isobar expectation:  $\Delta\gamma/v_2$  in Ru+Ru is larger than in Zr+Zr.

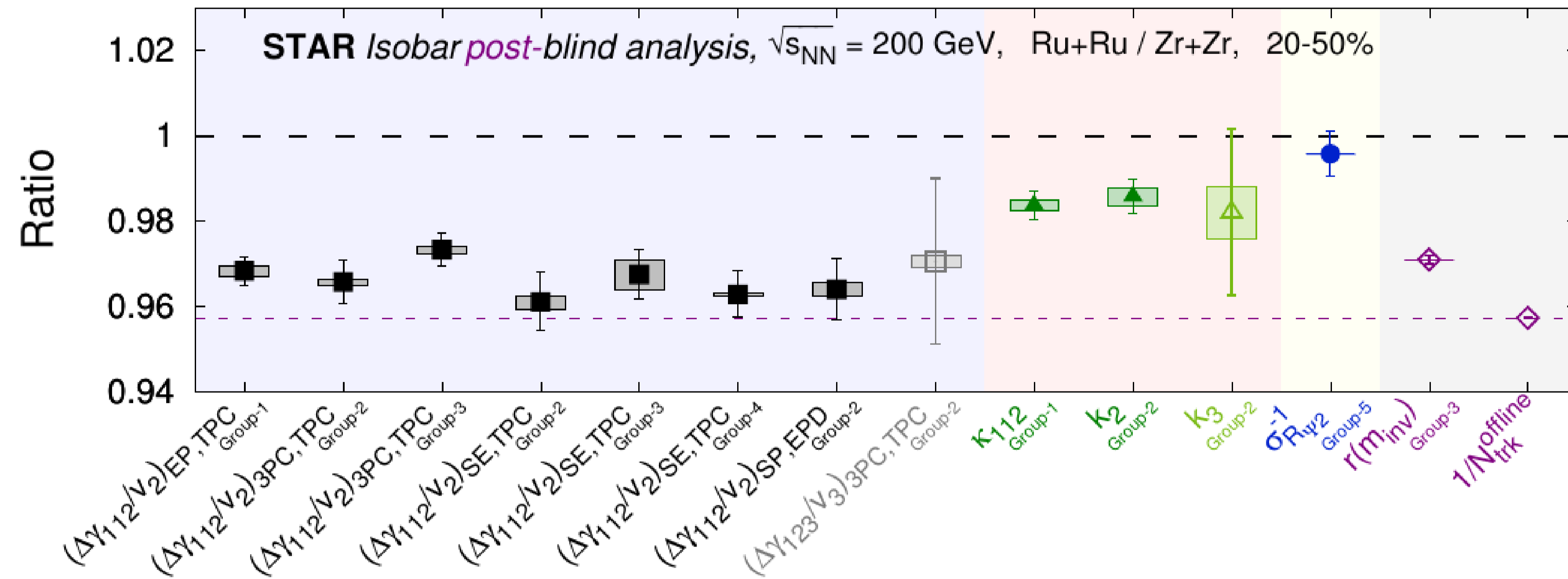


Figure 2: Post-blind results from STAR isobar analysis [STAR, Phys. Rev. C **105**, 014901 (2022)].

- ▶ The main reason that the isobar ratio of  $\Delta\gamma/v_2$  is less than unity is because of the multiplicity difference.
- ▶ The better quantity is  $N\Delta\gamma/v_2$ . Its naive background baseline is unity.
- ▶ Isobar data are above this naive baseline.

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## 3. Nonflow contribution to isobar baseline

- ▶ The naive baseline of unity would be correct if there was no nonflow. Nonflow correlations will cause the baseline to deviate from unity.
- ▶ We use the letter “ $\epsilon$ ” to denote the nonflow components.
- ▶ Nonflow in  $v_2^*$ :  $v_2^{*2} = v_2^2 + v_{2,nf}^2$ ,  $\epsilon_{nf} \equiv v_{2,nf}^2/v_2^2$ .
- ▶  $C_3$  is composed of flow-induced background (major), 3p nonflow correlations (minor), and possible CME (not written out) [Y. Feng, J. Zhao, H. Li, H. j. Xu and F. Wang, Phys. Rev. C **105**, 024913 (2022)]:

$$C_3 = \frac{C_{2p}N_{2p}}{N^2}v_{2,2p}v_2 + \frac{C_{3p}N_{3p}}{2N^3} = \frac{v_2^2\epsilon_2}{N} + \frac{\epsilon_3}{N^2}, \quad (1)$$

- ▶ The CME-sensitive observable  $\Delta\gamma$  is  $\Delta\gamma = C_3/v_2^*$ , and then

$$\frac{N\Delta\gamma}{v_2^*} = \frac{NC_3}{v_2^{*2}} = \frac{\epsilon_2}{1 + \epsilon_{nf}} + \frac{\epsilon_3}{Nv_2^2(1 + \epsilon_{nf})} = \frac{\epsilon_2}{1 + \epsilon_{nf}} \left( 1 + \frac{\epsilon_3/\epsilon_2}{Nv_2^2} \right) \quad (2)$$

- 2-particle (2p) nonflow (e.g., resonance, ...)  $C_{2p} \equiv \langle \cos(\phi_\alpha + \phi_\beta - 2\phi_{2p}) \rangle$ .
- 3-particle (3p) nonflow (e.g., jets, ...)  $C_{3p} \equiv \langle \cos(\phi_\alpha + \phi_\beta - 2\phi_c) \rangle$ .
- $N \approx N_+ \approx N_-$  is POI multiplicity;  $N_{2p,3p}$  is 2p (3p) nonflow pair (triplet) multiplicity. (POI stands for particle of interest.)
- $\epsilon_2 \equiv C_{2p}N_{2p}v_{2,2p}/(Nv_2)$  is the 2p correlation w.r.t. the 2p cluster azimuth and coupled with 2p cluster elliptic flow.
- $\epsilon_3 \equiv C_{3p}N_{3p}/(2N)$  is the 3p correlation within the correlated triplet.

- ▶ Isobar ratio: (where notation  $\Delta X = X^{Ru} - X^{Zr}$ )

$$\begin{aligned} \frac{(N\Delta\gamma/v_2^*)^{Ru}}{(N\Delta\gamma/v_2^*)^{Zr}} &\equiv \frac{(NC_3/v_2^{*2})^{Ru}}{(NC_3/v_2^{*2})^{Zr}} \approx \frac{\epsilon_2^{Ru}}{\epsilon_2^{Zr}} \cdot \frac{(1 + \epsilon_{nf})^{Zr}}{(1 + \epsilon_{nf})^{Ru}} \cdot \frac{[1 + \epsilon_3/\epsilon_2/(Nv_2^2)]^{Ru}}{[1 + \epsilon_3/\epsilon_2/(Nv_2^2)]^{Zr}} \\ &\approx 1 + \frac{\Delta\epsilon_2}{\epsilon_2} - \frac{\Delta\epsilon_{nf}}{1 + \epsilon_{nf}} + \frac{\epsilon_3/\epsilon_2/(Nv_2^2)}{1 + \epsilon_3/\epsilon_2/(Nv_2^2)} \left( \frac{\Delta\epsilon_3}{\epsilon_3} - \frac{\Delta\epsilon_2}{\epsilon_2} - \frac{\Delta N}{N} - \frac{\Delta v_2^2}{v_2^2} \right) \end{aligned} \quad (3)$$

- ▶ Need  $\epsilon_{nf}$ ,  $\epsilon_2$ ,  $\epsilon_3$  for a new background estimate.

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## 4. Nonflow Estimates

### a) Nonflow to $v_2^*$ -measurement of $\epsilon_{nf}$

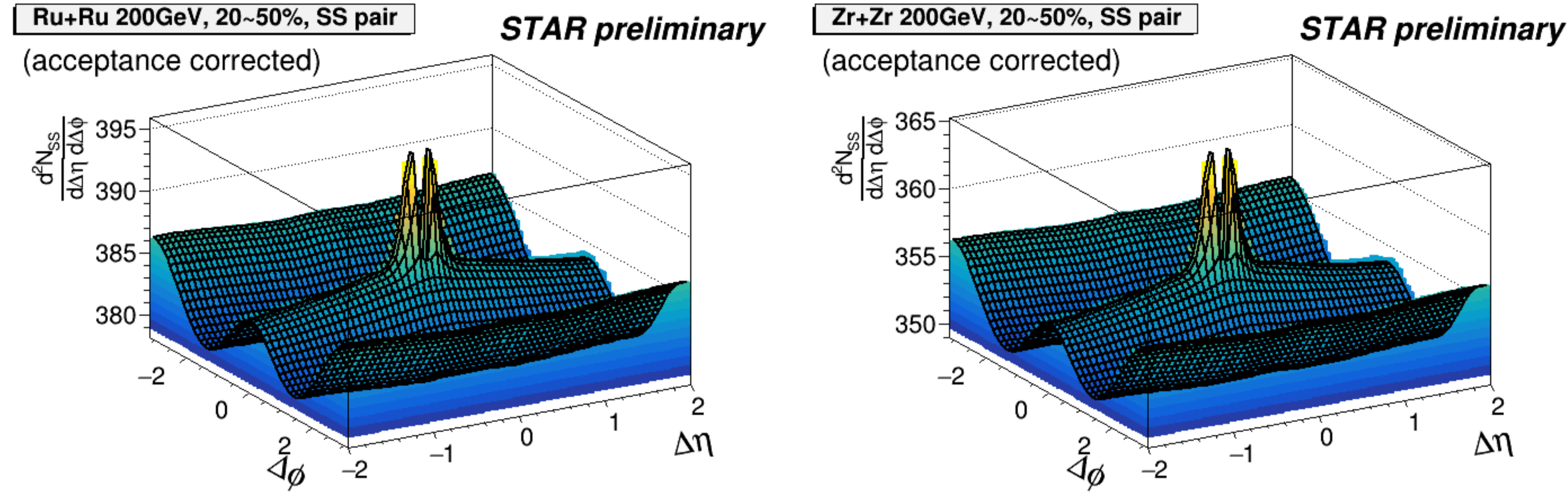


Figure 3: The two-particle  $(\Delta\eta, \Delta\phi)$  distributions of SS pairs (left: Ru+Ru; right: Zr+Zr). The POI are from  $0.2 < p_T < 2.0$  GeV/c,  $|\eta| < 1$ . The centrality range is 20 – 50%, which is defined by the POI multiplicity. The acceptance is corrected by mixed-event technique.

#### ► Fit function $f(\Delta\eta, \Delta\phi)$

$$A_1 G_{NS,W}(\Delta\eta) G_{NS,W}(\Delta\phi) + A_2 G_{NS,N}(\Delta\eta) G_{NS,N}(\Delta\phi) + A_3 G_{NS,D}(\Delta\eta) G_{NS,D}(\Delta\phi) \\ + \frac{B}{2 - |\Delta\eta|} \text{erf}\left(\frac{2 - |\Delta\eta|}{\sqrt{2}\sigma_{\Delta\eta,AS}}\right) G_{AS}(\Delta\phi \pm \pi) + D G_{RG}(\Delta\eta) \\ + C [1 + 2V_1 \cos(\Delta\phi) + 2V_2 \cos(2\Delta\phi) + 2V_3 \cos(3\Delta\phi)],$$

$G_s(x)$  Gaussian function,  $V_n = v_n^2$  assumed  $\eta$ -independent.

NS–nearside, AS–awayside, RG–ridge;  $W$ –wide,  $N$ –narrow,  $D$ –dip.

STAR preliminary		Ru+Ru	Zr+Zr
SS	fit parameter $C$	$381.651 \pm 0.011$	$351.988 \pm 0.009$
	fit parameter $V_2 = v_2^2$	$0.002972 \pm 0.000003$	$0.002867 \pm 0.000003$
	$\langle \cos(2\Delta\phi) \rangle_{SS} ( \Delta\eta  > 0.05)$	$0.0035968 \pm 0.0000010$	$0.0034930 \pm 0.0000010$
inclusive	$\langle \cos(2\Delta\phi) \rangle = v_2^{*2} ( \Delta\eta  > 0.05)$	$0.0037161 \pm 0.0000007$	$0.0036088 \pm 0.0000007$
	nonflow $U = \langle \cos(2\Delta\phi) \rangle - V_2$	$0.000745 \pm 0.000003$	$0.000742 \pm 0.000003$
	$\epsilon_{nf} = U/V_2$	$(25.06 \pm 0.10)\%$	$(25.88 \pm 0.09)\%$

- If the nearside wide Gaussian ( $A_1$  term) is counted into “true” flow,  $(v_2^2)^{Ru} = 0.003489$ ,  $(v_2^2)^{Zr} = 0.003381$ ,  $\epsilon_{nf}^{Ru} = 6.50\%$ ,  $\epsilon_{nf}^{Zr} = 6.73\%$ . Half of this difference from the default is counted as systematic uncertainty.  $\Delta\epsilon_{nf} = (-0.82 \pm 0.13 \mp 0.30)\%$ ,  $-\Delta\epsilon_{nf}/(1 + \epsilon_{nf}) = (0.65 \pm 0.11 \pm 0.22)\%$ .  $\Delta v_2^2/v_2^2 = \Delta V_2/V_2 = (3.7 \pm 0.1 \mp 0.3)\%$ .

### b) Estimate of $\Delta\epsilon_2/\epsilon_2$

- $\epsilon_2$  can be obtained from ZDC measurement (no nonflow, assuming negligible CME) [STAR, Phys. Rev. C 105, 014901 (2022)]  $\epsilon_2 = \frac{N\Delta\gamma\{ZDC\}}{v_2\{ZDC\}} \approx 0.57 \pm 0.04 \pm 0.02$  (tracking efficiency  $\sim 80\%$ ) and  $\Delta\epsilon_2/\epsilon_2 \approx (2.3 \pm 9.2)\%$ . The  $\Delta\epsilon_2$  precision is too poor.
- AMPT simulation w.r.t. reaction plane gives  $\Delta\epsilon_2/\epsilon_2 \approx (3.5 \pm 1.4)\%$ .
- However, the pair multiplicity difference  $r \equiv (N_{OS} - N_{SS})/N_{OS}$  is relatively precisely measured [STAR, Phys. Rev. C 105, 014901 (2022)]. Assuming  $C_{2p}^{Ru} = C_{2p}^{Zr}$ , then  $\epsilon_2 \propto Nr$ , and  $\Delta\epsilon_2/\epsilon_2 = \Delta r/r + \Delta N/N = (-2.95 \pm 0.08)\% + 4.4\% = (1.45 \pm 0.08)\%$ .

### c) Estimate of $\Delta\epsilon_3/\epsilon_3$

- We use HIJING simulation to obtain  $\epsilon_3 \approx (1.84 \pm 0.04)\%$ , and  $\Delta\epsilon_3/\epsilon_3 = (0.5 \pm 2.7)\%$  ( $\sim 8.6 \times 10^8$  events for each isobar).
- We assume 50% systematic uncertainty for  $\epsilon_3$  ( $\pm 0.92\%$ ), and assume  $\Delta\epsilon_3/\epsilon_3$  is presently dominated by statistics.
- HIJING without jet quenching gives  $\epsilon_3 = (2.24 \pm 0.05)\%$ , differing from the default by 22%, suggesting 50% systematics a safe guesstimate.

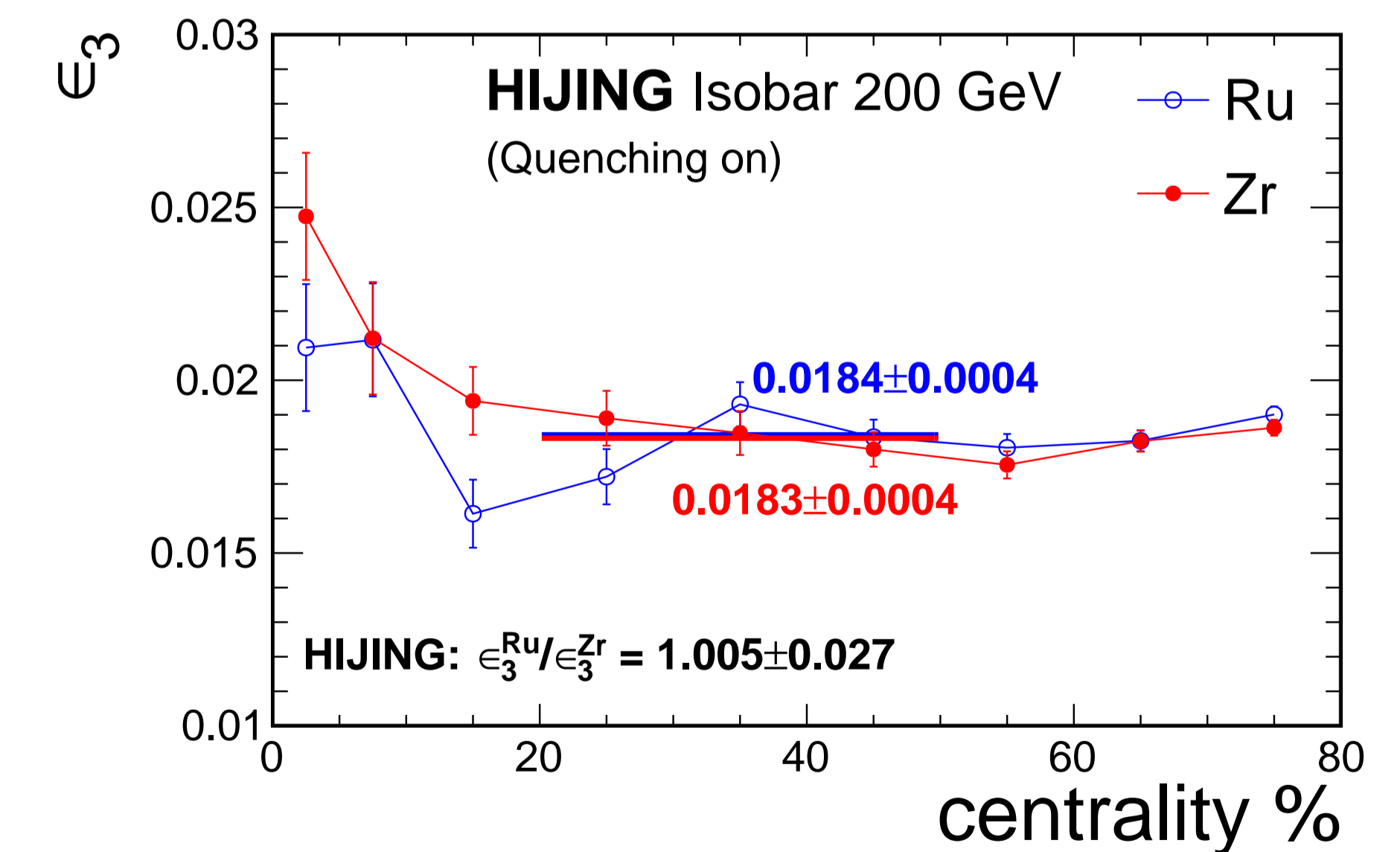


Figure 4: HIJING simulation estimates  $\epsilon_3$ .

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## 5. Estimated Background Level For Isobar $N\Delta\gamma/v_2$ Ratio

\* Except this column, all numbers on this poster refer to those for full-event.

Quantity		Method	Systematic uncertainty	Full-event value	Sub-event value*
Multiplicity $\Delta N/N$	Measured		Negligible	4.4%	4.4%
Flow $\Delta v_2^2/v_2^2$	Measured	Nonflow subtracted as per below	From nonflow syst.	$\Delta v_2^2/v_2^2 = (3.7 \pm 0.1 \pm 0.3)\%$	$\Delta v_2^2/v_2^2 = (3.7 \pm 0.1 \pm 0.3)\%$
$v_2$ nonflow	Measured	$(\Delta\eta, \Delta\phi)$ correlations, experimentally measured	Nonflow $\sim 25\%$ (full event), dominated by NS wide Gaus; consider $\pm 1/2$ WG as syst. uncertainty	$-\Delta\epsilon_{\text{nf}} = (0.82 \pm 0.13 \pm 0.30)\%$ $\frac{-\Delta\epsilon_{\text{nf}}}{1+\epsilon_{\text{nf}}} = (0.65 \pm 0.11 \pm 0.22)\%$	$-\Delta\epsilon_{\text{nf}} = (0.59 \pm 0.15 \pm 0.27)\%$ $\frac{-\Delta\epsilon_{\text{nf}}}{1+\epsilon_{\text{nf}}} = (0.48 \pm 0.12 \pm 0.22)\%$
$v_2$ -induced bkgd: $\epsilon_2 = N\Delta\gamma/v_2$	Measured	Measured by ZDC (assume negligible CME)	Small	$\epsilon_2 = (0.57 \pm 0.04 \pm 0.02)\%$	$\epsilon_2 = (0.79 \pm 0.05 \pm 0.01)\%$
$v_2$ -induced bkgd difference: $\frac{\Delta\epsilon_2}{\epsilon_2} \sim \frac{\Delta(N_{2p}/N)}{(N_{2p}/N)} = \frac{\Delta(rN)}{rN}$	Measured	$r = (N_{\text{OS}} - N_{\text{SS}})/N_{\text{OS}}$ experimentally measured	Negligible	$\frac{\Delta\epsilon_2}{\epsilon_2} = (1.45 \pm 0.08)\%$	$\frac{\Delta\epsilon_2}{\epsilon_2} = (1.45 \pm 0.08)\%$
3p contribution to $C_3$ : $\epsilon_3 = C_{3p}N_{3p}/(2N)$	Model estimate	HIJING simulations quenching-on	Quenching-on and off difference $\sim 20\%$ . Take $\pm 50\%$ as syst. uncertainty	$\epsilon_3 = (1.84 \pm 0.04 \pm 0.92)\%$	$\epsilon_3 = (1.91 \pm 0.09 \pm 0.95)\%$
3p contribution difference: $\Delta\epsilon_3/\epsilon_3$	Model estimate	HIJING simulation quenching-on	Assumed negligible relative to the large stat. uncertainty	$\frac{\Delta\epsilon_3}{\epsilon_3} = (0.5 \pm 2.7)\%$ $\frac{\epsilon_3/\epsilon_2}{Nv_2^2} = 0.104 \pm 0.008 \pm 0.053$	$\frac{\Delta\epsilon_3}{\epsilon_3} = (-1.8 \pm 6.3)\%$ $\frac{\epsilon_3/\epsilon_2}{Nv_2^2} = 0.079 \pm 0.006 \pm 0.040$
background estimate				$1.013 \pm 0.003 \pm 0.005$	$1.011 \pm 0.005 \pm 0.005$

► The numerical value of Eq. 3 (for full-event method as example) can thus be estimated as follows:

$$\begin{aligned} \frac{(N\Delta\gamma/v_2^*)^{\text{Ru}}}{(N\Delta\gamma/v_2^*)^{\text{Zr}}} &\approx 1 + (1.45 \pm 0.08)\% + (0.65 \pm 0.11 \pm 0.22)\% + (0.094 \pm 0.007 \pm 0.048)[(0.5 \pm 2.7)\% - (1.45 \pm 0.08)\% - 4.4\% - (3.7 \pm 0.1 \pm 0.3)\%] \\ &= 1 + (1.45 \pm 0.08)\% + (0.65 \pm 0.11 \pm 0.22)\% - (0.85 \pm 0.26 \pm 0.44)\% = 1.013 \pm 0.003 \pm 0.005 \end{aligned} \quad (4)$$

## 6. Summary and Outlook

- ▶  $v_2$  nonflow and 2p nonflow are measured. 3p nonflow is estimated by HIJING. Large degree of cancellation between 2p and 3p nonflow.
- ▶ New preliminary isobar background estimate  $\frac{(N\Delta\gamma/v_2^*)_{Ru}}{(N\Delta\gamma/v_2^*)_{Zr}} \approx (1.013 \pm 0.003 \pm 0.005)$  for full-event,  $(1.011 \pm 0.005 \pm 0.005)$  for sub-event.
- ▶  $\epsilon_3$  estimate in a data-driven way in future?

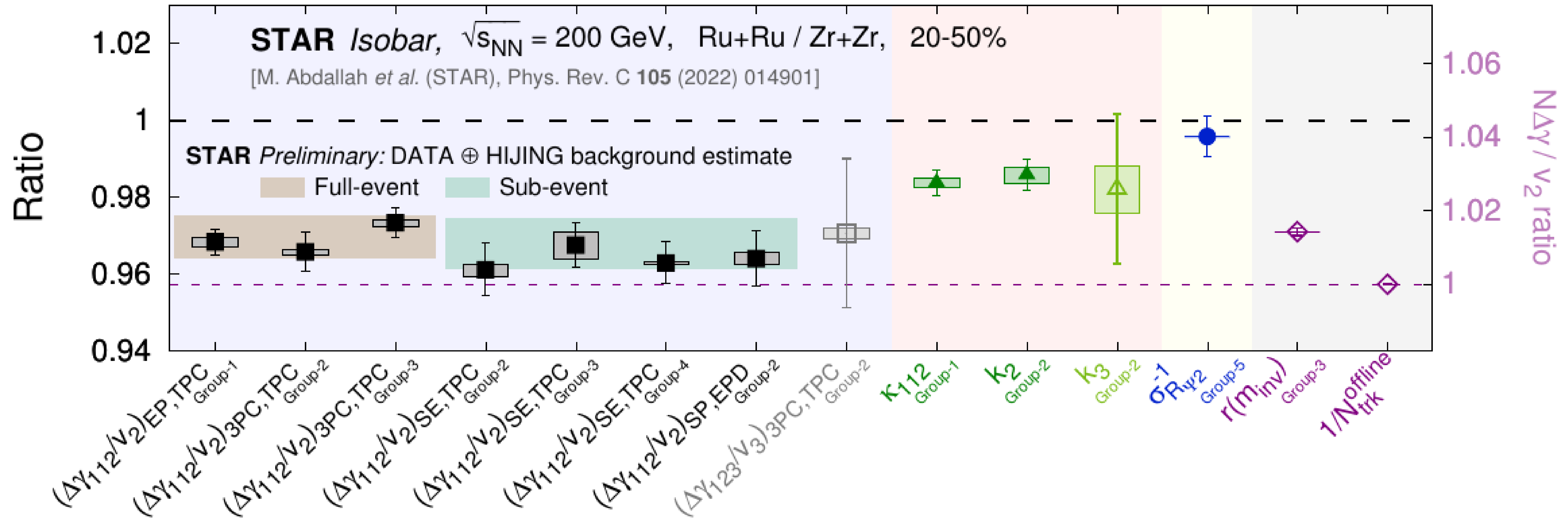


Figure 5: Background estimate in brown on the isobar Ru/Zr ratio of  $\Delta\gamma/v_2$  from STAR isobar analysis [STAR, Phys. Rev. C 105, 014901 (2022)].

The STAR Collaboration,

<https://drupal.star.bnl.gov/STAR/presentations>