

1 Higher-Order Cumulants of Net-Proton Multiplicity
2 Distributions in ${}^{96}_{40}\text{Zr}+{}^{96}_{40}\text{Zr}$ and ${}^{96}_{44}\text{Ru}+{}^{96}_{44}\text{Ru}$ Collisions at
3 $\sqrt{s_{\text{NN}}} = 200 \text{ GeV}$ *

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7 The Relativistic Heavy Ion Collider (RHIC) at Brookhaven is a fa-
8 cility to create and study the strongly interacting Quark-Gluon Plasma
9 (QGP). Higher-order cumulants of the conserved quantities and their ra-
10 tios are powerful tools to study the properties of QGP and explore the QCD
11 phase structure, such as critical point and/or the first-order phase transi-
12 tion boundary. In these proceedings, we present the net-proton cumulants
13 and their ratios up to sixth-order as a function of multiplicity using high
14 statistics data of ${}^{96}_{40}\text{Zr}+{}^{96}_{40}\text{Zr}$ and ${}^{96}_{44}\text{Ru}+{}^{96}_{44}\text{Ru}$ collisions at $\sqrt{s_{\text{NN}}} = 200 \text{ GeV}$.
15 The STAR experiment collected two billion events for each colliding sys-
16 tem. We compared the multiplicity dependence to the published net-proton
17 cumulants in Au+Au collisions at $\sqrt{s_{\text{NN}}} = 200 \text{ GeV}$. In addition, we com-
18 pared the results to Lattice QCD, the Hadron Resonance Gas model, and
19 hadronic transport model calculations. The physics implications are dis-
20 cussed.

21 **1. Introduction**

22 Lattice QCD calculations show that the phase transition between the
23 QGP state and the hadronic state is an analytic crossover at vanishing
24 baryonic chemical potential (μ_B) [1] and at the temperature of 156.5 ± 1.5
25 MeV [2]. QCD based model calculations, see Ref. [3] for example, predict
26 a critical point followed by a first-order phase transition at high μ_B . STAR
27 detector at RHIC searches for the possible signature of the critical point and
28 the first-order phase transition in the QCD phase diagram on temperature
29 and μ_B plane QCD phase diagram by scanning the collision energy [4, 5].

30 Fluctuations of conserved quantities such as, net-baryon number, is used
31 for the critical point search. Moment analyses of these event-by-event fluctu-

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32 ating quantities are performed by studying their cumulants. The definitions
 33 of cumulants are in Sec. 2. Experimentally, the net-proton number is used
 34 as a proxy for the net-baryon number [6, 7].

35 It is expected that the fourth-order cumulant has a non-monotonic en-
 36 ergy dependence in the vicinity of the critical point [8, 9, 10, 11]. Fourth-
 37 order cumulant (C_4/C_2) analysis of net-proton in Au+Au collisions at STAR
 38 shows a non-monotonic energy dependence at $\sqrt{s_{\text{NN}}} = 7.7 - 62.4$ GeV with a
 39 significance of 3.1σ [5, 12]. Recent analyses of Au+Au collisions at $\sqrt{s_{\text{NN}}} =$
 40 2.4 and 3 GeV, at HADES [13] and STAR [14] respectively, show a sup-
 41 pression of net-proton C_4/C_2 . The hadronic transport model, UrQMD [15],
 42 reproduces the data at $\sqrt{s_{\text{NN}}} = 3$ GeV. Comparing to the transport model
 43 and the higher energy results, the suppression of C_4/C_2 indicates that it is
 44 hadronic interaction dominant in this high baryon density region ($\mu_B \geq 750$
 45 MeV). These results imply that if the critical point is created in heavy-ion
 46 collisions, it could only exist above the collision energy of 3 GeV [14].

47 Moving on to the low baryon density region, Lattice QCD calculations
 48 of crossover between QGP and hadronic phases predict the fifth and the
 49 sixth-order cumulants (C_5/C_1 and C_6/C_2) of the net-baryon number to be
 50 negative at the collision energy of $\sqrt{s_{\text{NN}}} = 200$ GeV [16]. The C_6/C_2 of
 51 net-proton number at the same collision energy of Au+Au collisions was
 52 also measured at STAR [17, 18]. The result shows a systematic trend where
 53 the value decreases to be negative as the collision centrality moves from pe-
 54 ripheral to central collisions. Then at the most central collisions, it becomes
 55 consistent with the Lattice QCD results in Ref. [16]. On the other hand,
 56 in two other collision energies, $\sqrt{s_{\text{NN}}} = 27$ and 54.4 GeV, the results are
 57 consistent with zero.

58 STAR at RHIC collected 2 billion and 1.9 billion events for ${}^{96}_{40}\text{Zr}+{}^{96}_{40}\text{Zr}$ and
 59 ${}^{96}_{44}\text{Ru}+{}^{96}_{44}\text{Ru}$ collisions, respectively at $\sqrt{s_{\text{NN}}} = 200$ GeV in 2018. Studying
 60 the net-proton cumulants and their ratios provide much improved statistics
 61 over Au+Au collision results. Additionally, in these proceedings, we in-
 62 spect the collision system dependence by comparing the results from p+p ,
 63 the isobars (${}^{96}_{40}\text{Zr}+{}^{96}_{40}\text{Zr}$ and ${}^{96}_{44}\text{Ru}+{}^{96}_{44}\text{Ru}$), and Au+Au at the same collision
 64 energy of $\sqrt{s_{\text{NN}}} = 200$ GeV.

65 As mentioned later in the outlook of Sec. 5, analysis on cumulant ratios
 66 of mixed quantum numbers may enable us to measure the magnetic field
 67 created in the heavy-ion collisions [19]. Aside from the high statistics, the
 68 isobar collisions make them suitable data sets for this future analysis due to
 69 the charge number difference. Thus, checking the collision system depen-
 70 dence of the net-proton cumulants and ratios is needed before we move on
 71 to the next endeavor.

2. Experimental Observables

Cumulants from the first to the sixth-order can be written as:

$$\begin{aligned}
C_1 &= \langle N \rangle, \\
C_2 &= \langle (\delta N)^2 \rangle, \\
C_3 &= \langle (\delta N)^3 \rangle, \\
C_4 &= \langle (\delta N)^4 \rangle - 3\langle (\delta N)^2 \rangle^2, \\
C_5 &= \langle (\delta N)^5 \rangle - 10\langle (\delta N)^2 \rangle \langle (\delta N)^3 \rangle, \\
C_6 &= \langle (\delta N)^6 \rangle + 30\langle (\delta N)^2 \rangle^3 - 15\langle (\delta N)^2 \rangle \langle (\delta N)^4 \rangle - 10\langle (\delta N)^3 \rangle^2,
\end{aligned} \tag{1}$$

where N represents the event-by-event conserved quantity distribution and $\delta N = N - \langle N \rangle$. The symbol $\langle N \rangle$ represents the average value of N over the events. The higher the cumulant order, the more the cumulant is sensitive to the correlation length [20]. Taking the ratio of the cumulants cancels out the volume dependence and the ratios can be directly compared to theoretical calculations.

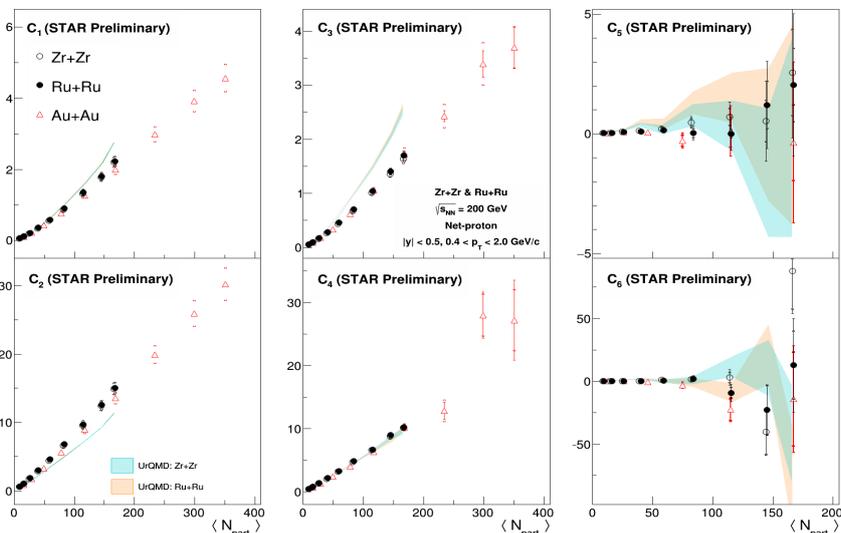
3. Analysis Setup

The (anti-)proton acceptance for the analysis is $0.4 < p_T < 2.0$ GeV/ c in transverse momentum and $|y| < 0.5$ in rapidity. The events are categorized into nine different collision centralities: 0-5%, 5-10%, 10-20%, 20-30%, ..., 70-80%. The collision centralities are determined by the number of charged particle multiplicity. In this analysis, the charged particle multiplicity is defined as the number of detected charged particles excluding the (anti-)proton tracks in the pseudorapidity region of $|\eta| < 1$.

The efficiencies of the detector acceptance and tracking are corrected track-by-track [21, 22]. The Centrality Bin Width Correction (CBWC) is applied when merging the multiplicity bins into centrality bins [23]. The statistical uncertainties are calculated based on the Delta theorem [24].

4. Results

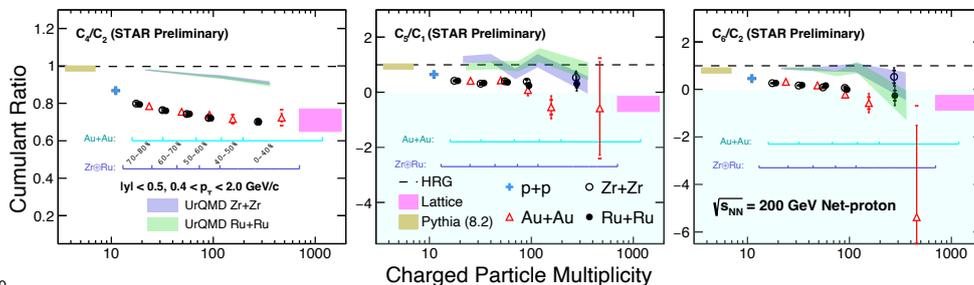
The net-proton cumulants up to sixth-order are plotted in Fig. 1. Results in Au+Au collisions [12] are also plotted for comparison. The detectors efficiencies for all data points are corrected. The results are plotted to the average number of participating nucleons ($\langle N_{\text{part}} \rangle$). Results in ${}^{96}_{40}\text{Zr}+{}^{96}_{40}\text{Zr}$ and ${}^{96}_{44}\text{Ru}+{}^{96}_{44}\text{Ru}$ are consistent. In addition, both results from isobars and Au+Au at $\sqrt{s_{\text{NN}}} = 200$ GeV GeV follow the same $\langle N_{\text{part}} \rangle$ trend. As shown in Fig. 1, the data are compared with the UrQMD calculations, where the same acceptance as used in STAR analysis was adopted. The



103 Fig. 1: Cumulants of net-proton in $^{96}_{40}\text{Zr}+^{96}_{40}\text{Zr}$ and $^{96}_{44}\text{Ru}+^{96}_{44}\text{Ru}$ collisions
 104 from the first to the sixth-order are plotted to the average number of par-
 105 ticipating nucleons. Results from Au+Au collisions are presented for comp-
 106 arison. The x-axis ranges for C_5 and C_6 are decreased. Detector efficiencies
 107 are corrected. The bars and brackets for each marker represent the statisti-
 108 cal and systematic uncertainties, respectively. UrQMD calculations are
 109 shown in bands.

101 UrQMD generally shows a similar trend as in the data, however overpre-
 102 dicts C_1 and C_3 while it underpredicts C_2 .

111 Figure 2 compares the higher-order cumulant ratios C_4/C_2 , C_5/C_1 , and
 112 C_6/C_2 at $\sqrt{s_{NN}} = 200$ GeV for different collision systems, p+p, the isobars,
 113 and Au+Au [12, 17], as a function of charged particle multiplicity. For bet-
 114 ter statistics, the collision centralities from 0% to 40% are merged into one
 115 central collision bin. For p+p collisions, only the cumulant ratio in aver-
 116 age charged particle multiplicity bin is shown. Not only the $^{96}_{40}\text{Zr}+^{96}_{40}\text{Zr}$ and
 117 the $^{96}_{44}\text{Ru}+^{96}_{44}\text{Ru}$ results are consistent, but all results from different collision
 118 systems agree among themselves. All cumulant ratios in Fig. 2 decrease as
 119 the multiplicity increases and deviate further from the Hadron Resonance
 120 Gas (HRG) model calculations in the Grand Canonical Ensemble picture.
 121 Although the UrQMD calculations describe the overall multiplicity depen-
 122 dent trend, they overpredict the presented higher-order ratios. At the top
 123 0-40% central Au+Au collisions, the results become consistent with the
 124 Lattice QCD prediction for the formation of thermalized QCD matter and
 125 smooth crossover transition. PYTHIA 8.2 (Pythia) calculations in Fig. 2
 126 represent the cumulant ratios averaged over charged particle multiplicity of



130

131 Fig. 2: Cumulant ratios C_4/C_2 , C_5/C_1 , and C_6/C_2 of ${}^{96}_{40}\text{Zr}+{}^{96}_{40}\text{Zr}$ and
 132 ${}^{96}_{44}\text{Ru}+{}^{96}_{44}\text{Ru}$ collisions as a function of charged particle multiplicity. Results
 133 from Au+Au and p+p collisions are presented for comparison. Cumulant
 134 ratios for p+p presented only in averaged charged particle multiplicity. The
 135 detector efficiencies for the charged particle multiplicity are not corrected
 136 but corrected for the cumulant ratios. The bars and brackets for each marker
 137 represent the statistical and systematic uncertainties, respectively. UrQMD
 138 calculations are shown in bands. HRG calculations are shown in dashed
 139 lines. Magenta bands represent Lattice QCD prediction for the formation
 140 of thermalized QCD matter. Pythia calculations shown in gold bands are
 142 for average charged particle multiplicity in p+p collisions.

127 the p+p collisions. All the higher-order cumulant ratios from Pythia are
 128 consistently positive which is inconsistent with the Lattice QCD results in
 129 the case of the fifth and the sixth-order.

143

5. Summary and Outlook

144 We have presented net-proton cumulants and their ratios up to sixth-
 145 order in isobar collisions at $\sqrt{s_{\text{NN}}} = 200$ GeV. The results fit into the mul-
 146 tiplicity dependence of cumulant ratios in p+p and Au+Au collisions. Al-
 147 though the hadronic transport model, UrQMD, over- and underpredicts the
 148 results, it shows a similar trend as in the data. All C_4/C_2 , C_5/C_1 , and
 149 C_6/C_2 show decreasing trends as multiplicity increases and deviate further
 150 from the HRG model calculation. In the most central collision centrality of
 151 Au+Au collisions, the higher-order cumulant ratios become consistent with
 152 the Lattice QCD calculations. The consistency between the data and the
 153 theory calculations implies that the transition between the thermalized QGP
 154 to the hadronic matter is a smooth crossover in central Au+Au collisions
 155 at top RHIC energy. This is a direct comparison between data and the first
 156 principle QCD calculations.

157 Other than the fluctuation measurements, one of the most important
 158 studies in the field of heavy-ion collisions is Chiral Magnetic Effect (CME).
 159 Measuring the magnetic field created in the heavy-ion collisions would greatly

160 help to study the CME. Recent Lattice QCD results show a possibility to
 161 experimentally assess the magnetic field created in the heavy-ion collisions
 162 by studying the cumulant ratios of mixed quantum numbers [19]. Due to
 163 the charge number difference between ${}^{96}_{40}\text{Zr}+{}^{96}_{40}\text{Zr}$ and ${}^{96}_{44}\text{Ru}+{}^{96}_{44}\text{Ru}$, we ex-
 164 pect about a 15% difference in the magnetic field squared [25]. Therefore,
 165 the high statistics of ${}^{96}_{40}\text{Zr}+{}^{96}_{40}\text{Zr}$ and ${}^{96}_{44}\text{Ru}+{}^{96}_{44}\text{Ru}$ collision data collected by
 166 STAR offer an opportunity to measure the magnetic field strength, or at
 167 least, the difference between the isobars.

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