



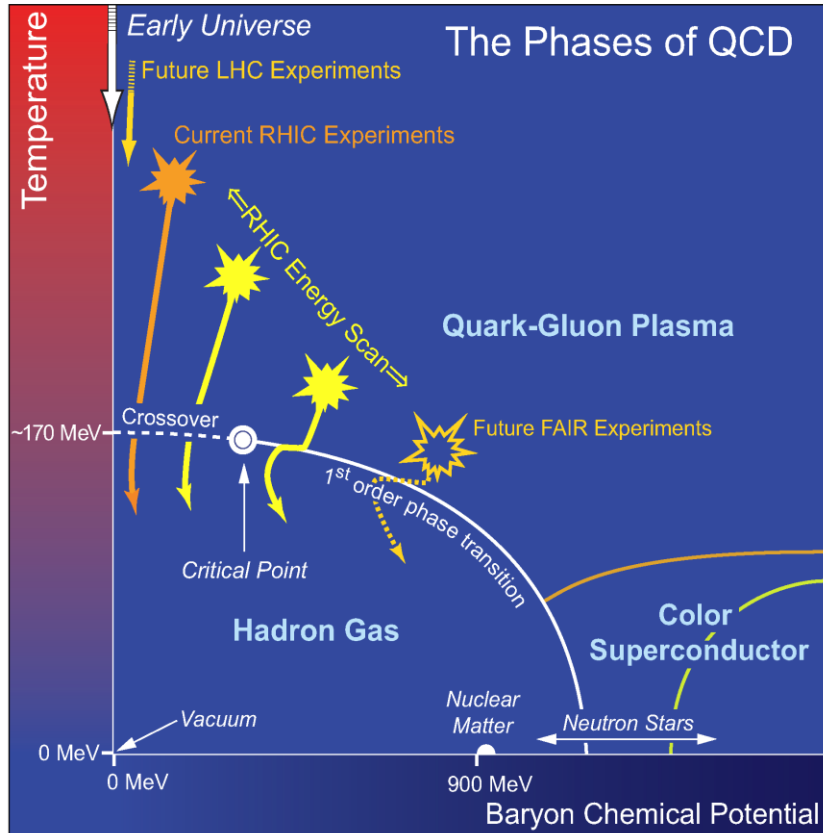
Search for the QCD Critical Point with Higher Moments of Net-proton Distributions



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Lattice QCD:

- Crossover at $\mu_B = 0$, 1st order phase transition at large μ_B .
- QCD Critical Point: The end point of first order phase transition boundary.

Y. Aoki et al., Nature 443, 675 (2006)

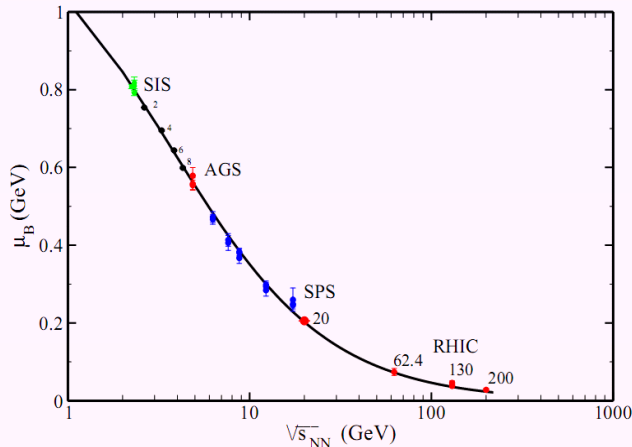
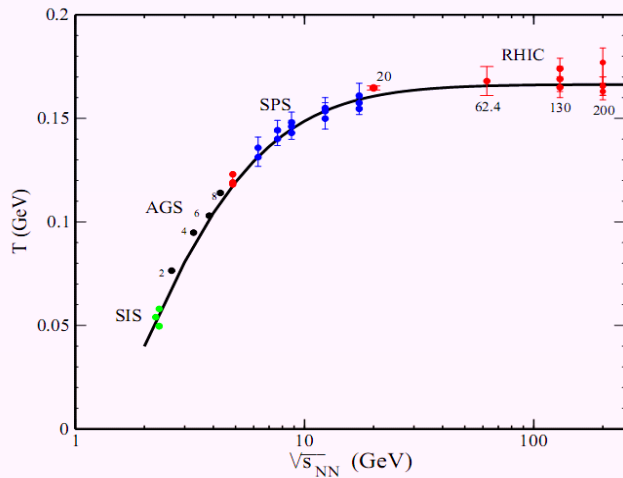
S. Gupta, et al. Science 332, 1525 (2011).

Motivations :

- Map the QCD Phase Boundary.
- Search for the QCD Critical Point.

➤ Particle ratio fitted by thermal model to extract Chemical freeze-out temperature (T) and baryon chemical potential (μ_B).

J. Cleymans et al, Phys. Rev. C73 (2006) 034905



➤ **RHIC Beam Energy Scan (BES) Program.**

Au+Au Collisions

Year	$\sqrt{s_{NN}}$ (GeV)
2010	7.7, 11.5, 39
2011	19.6, 27 (Analysis is ongoing)

➤ **STAR Detector : Large Uniform Acceptance.**

STAR is the ideal detector for the QCD critical point search.

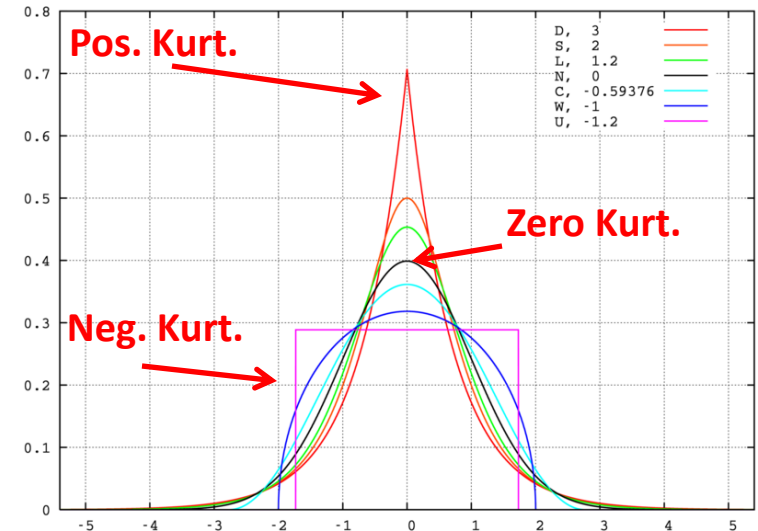
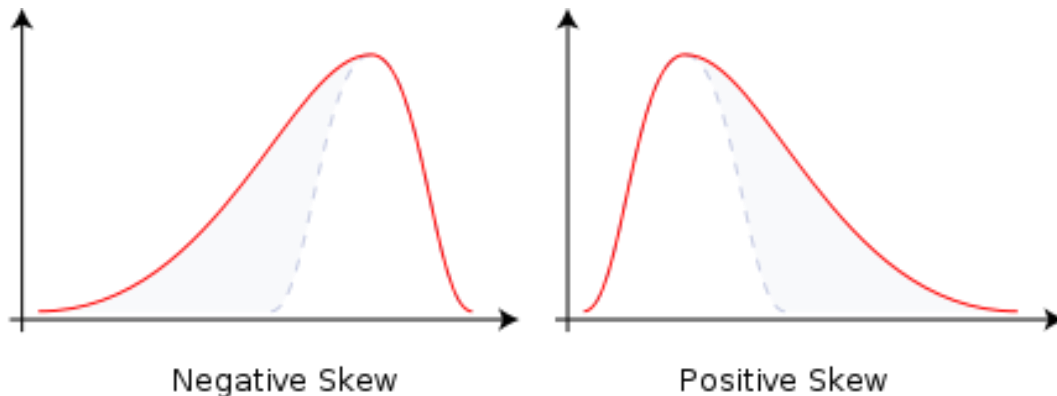
Definition : **N: Event by Event Multiplicity Distribution**

Mean: $M = \langle N \rangle$

St. Deviation: $\sigma = \sqrt{\langle (N - \langle N \rangle)^2 \rangle}$

Skewness: $s = \frac{\langle (N - \langle N \rangle)^3 \rangle}{\sigma^3}$

Kurtosis: $\kappa = \frac{\langle (N - \langle N \rangle)^4 \rangle}{\sigma^4} - 3$



➤ For Gaussian distribution, the skewness and kurtosis are equal to zero. **Ideal probe of the non-Gaussian fluctuations near the QCD Critical Point.**

X. Luo, arXiv: 1106.2926.

➤ **Link to Thermodynamic Susceptibilities in Lattice QCD and Hadron Resonance Gas (HRG) Model:**

$$\chi_B^{(n)} = \left. \frac{\partial^n (P/T^4)}{\partial (\mu_B/T)^n} \right|_T$$

M.Cheng et al, Phys. Rev. D 79, 074505 (2009)

F. Karsch and K. Redlich, Phys. Lett. B 695, 136 (2011)

$$\chi_B^2 = \frac{1}{VT^3} \langle \delta N_B^2 \rangle$$

$$\chi_B^3 = \frac{1}{VT^3} \langle \delta N_B^3 \rangle$$

$$\chi_B^4 = \frac{1}{VT^3} (\langle \delta N_B^4 \rangle - 3 \langle \delta N_B^2 \rangle^2)$$

$$\begin{aligned} \chi_B^4 / \chi_B^2 &= (\kappa \sigma^2)_B \\ \chi_B^3 / \chi_B^2 &= (S \sigma)_B \end{aligned}$$

Volume Cancel Out

Net-proton numbers fluctuations can reflect baryon and charge number fluctuations.

Y. Hatta et al, PRL 91, 102003 (2003)

➤ **Sensitive to Correlation Length (ξ) : Sigma Model Calculations.**

Due to finite size, finite time effects.
in heavy ion collisions. $\xi \sim 2-3$ fm.

$$\langle (\delta N)^2 \rangle \approx \xi^2$$

$$\langle (\delta N)^3 \rangle \approx \xi^{4.5}$$

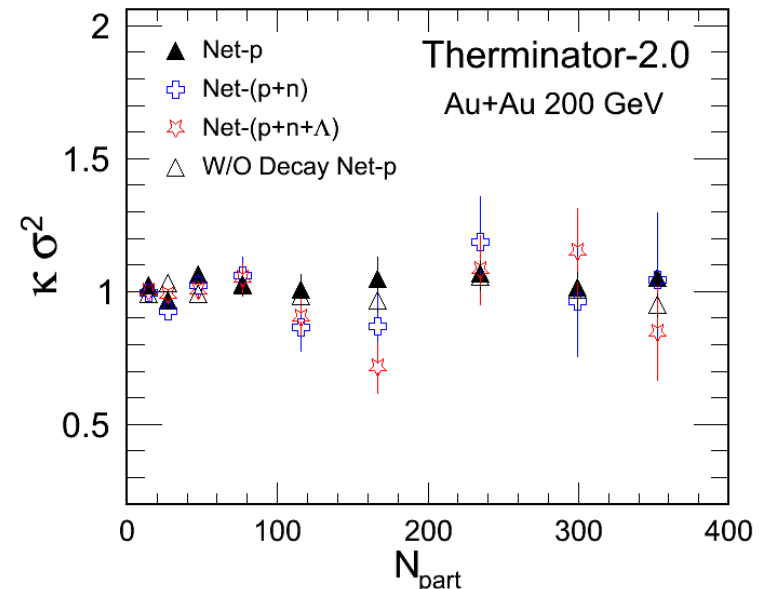
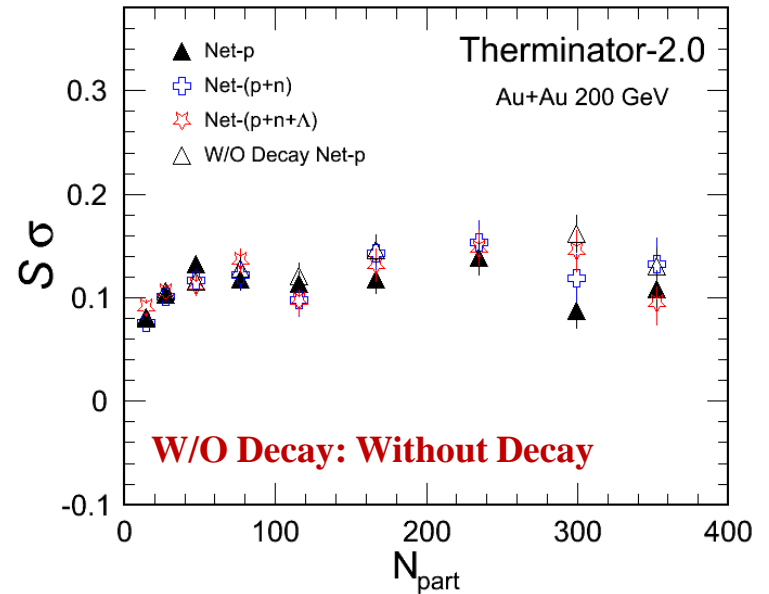
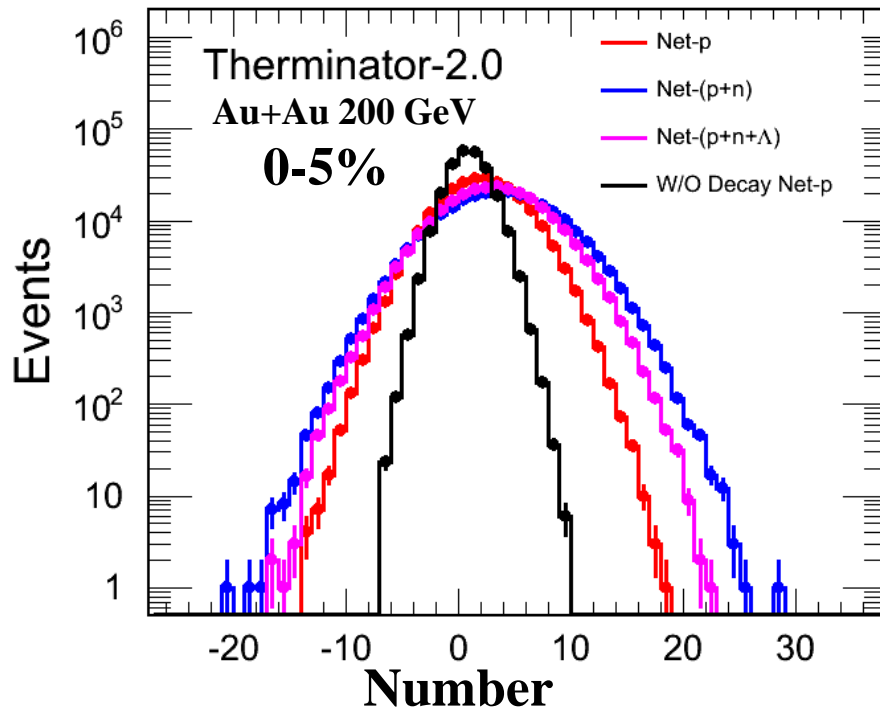
$$\langle (\delta N)^4 \rangle - 3 \langle (\delta N)^2 \rangle^2 \approx \xi^7$$

M. A. Stephanov, Phys. Rev. Lett. 102, 032301 (2009)

C. Athanasiou, M. Stephanov, K. Rajagopal, Phys. Rev. D 82, 074008 (2010)

Resonance Decay and Neutron Effect

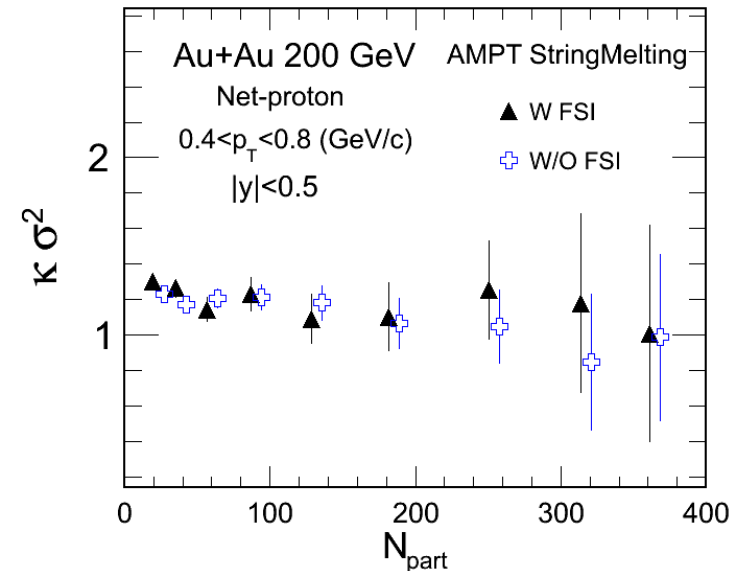
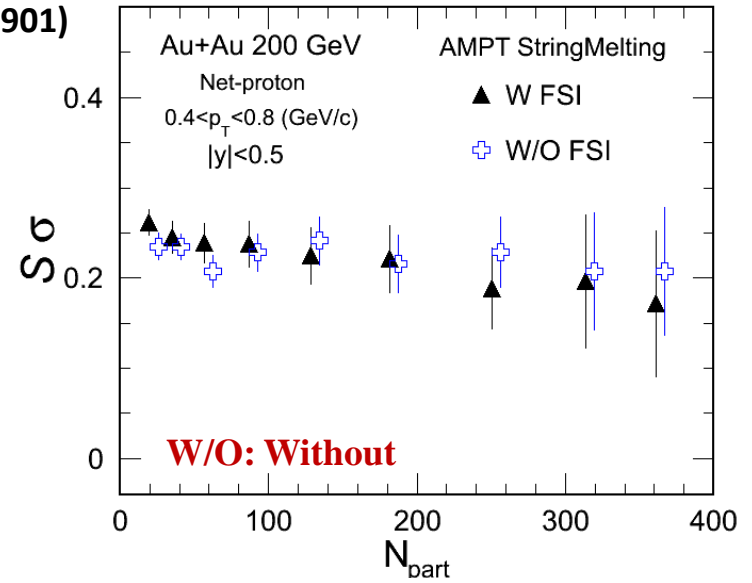
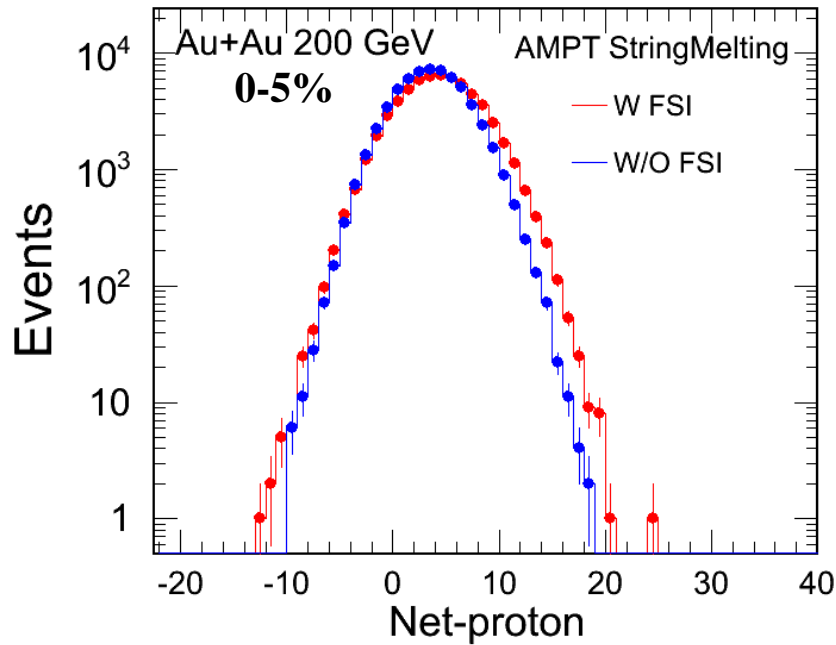
Model: Therminator-2.0 (arXiv:1102.0273)



- Effect of **resonance decay on $S\sigma$ and $\kappa\sigma^2$** is small. (based on the right two plots).
- Effect of inclusion of neutrons is small:
Indicates: **Net-proton fluctuation can reflect the net-baryon fluctuation.**
- **Error estimation:** X. Luo, arXiv:1109.0593

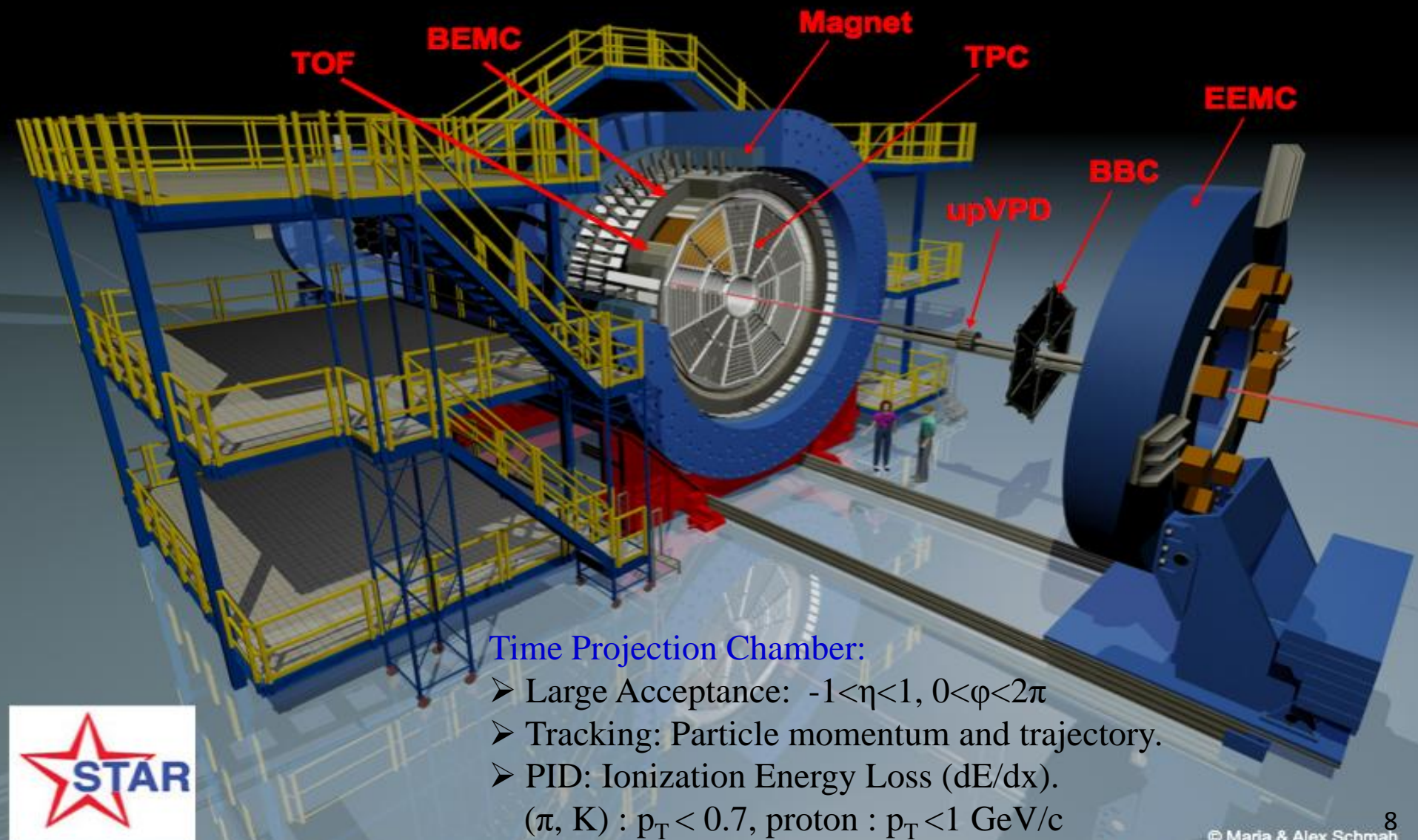
Final State Interaction (FSI) Effect

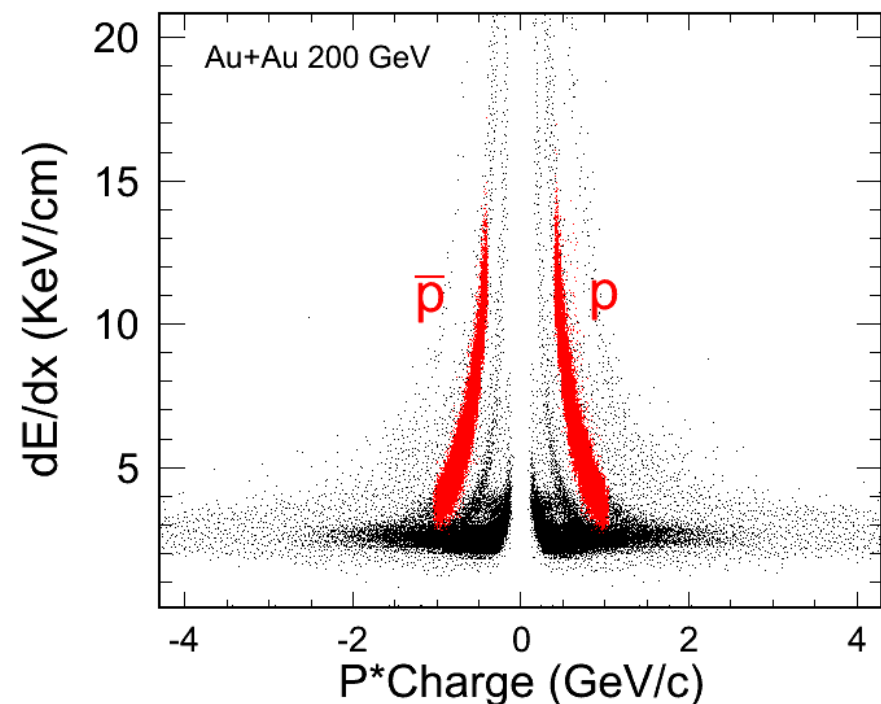
Model: AMPT StringMelting (Phys. Rev. C 72, 064901)



- Effects of Final State Interaction (FSI) on $S\sigma$ and $\kappa\sigma^2$ are small.
(based on the results in the right two plots).

The Solenoid Tracker At RHIC (STAR)





➤ Track Quality Cuts:

$N_{fits} > 20$,
 $N_{fits}/N_{FitPoss} > 0.52$.
 $gDca < 1$ cm.

➤ PID Cut: dE/dx

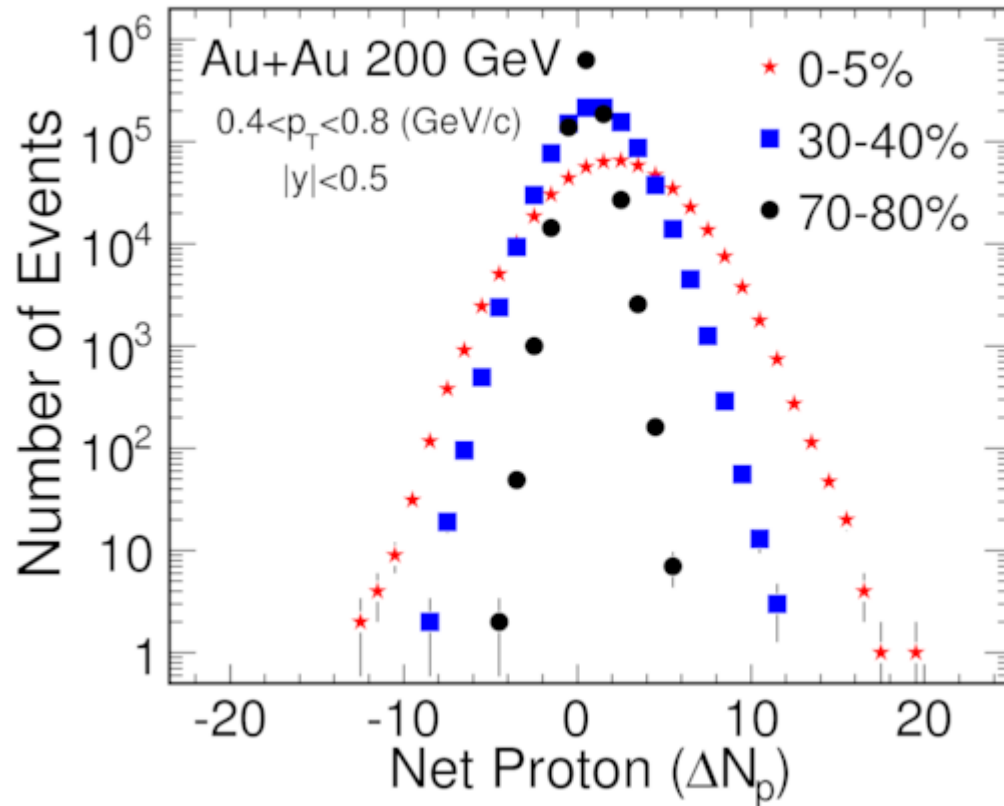
$$|Z_p| < 2$$

$$Z = \frac{\log\left[\left(\frac{dE}{dx}\right)_{\text{measure}} / \left(\frac{dE}{dx}\right)_{\text{expected}}\right]}{\sigma_E}$$

Advantages for using $0.4 < p_T < 0.8$ (GeV/c) and $|y_p| < 0.5$:

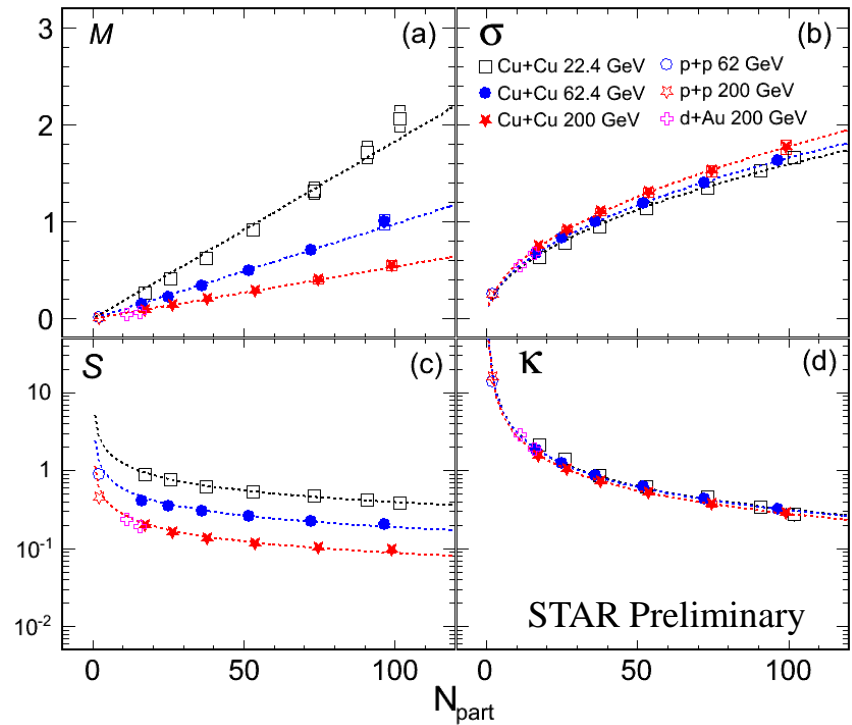
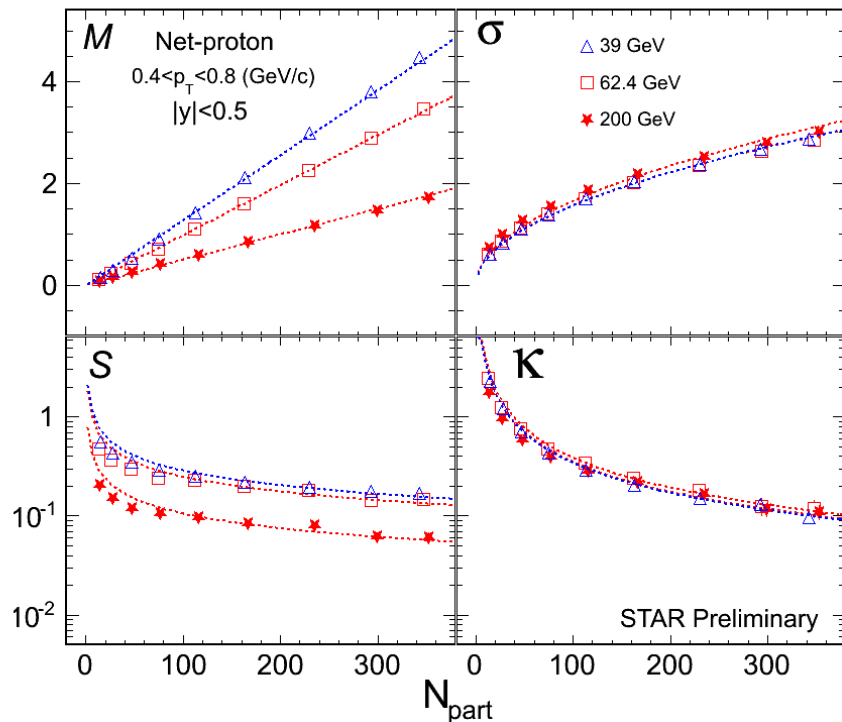
- Clean proton and antiproton identification with TPC dE/dx.
- Similar detection efficiency for proton and anti-proton.
- Larger long wavelength critical fluctuations developed in low p_T .

M. Stephannov, K. Rajagopa, E. Shuryak, Phys. Rev. D 60, 114028 (1999)



STAR: Phys. Rev. Lett. 105 (2010) 022302

- The event-by-event net-proton distributions are more symmetrical in central collision than peripheral.



Central Limit Theorem (CLT)

$$M_i = M_x \times C \times N_{part}, \sigma_i^2 = \sigma_x^2 \times C \times N_{part}$$

$$S_i = \frac{S_x}{\sqrt{C \times N_{part}}}, K_i = \frac{K_x}{(C \times N_{part})}$$

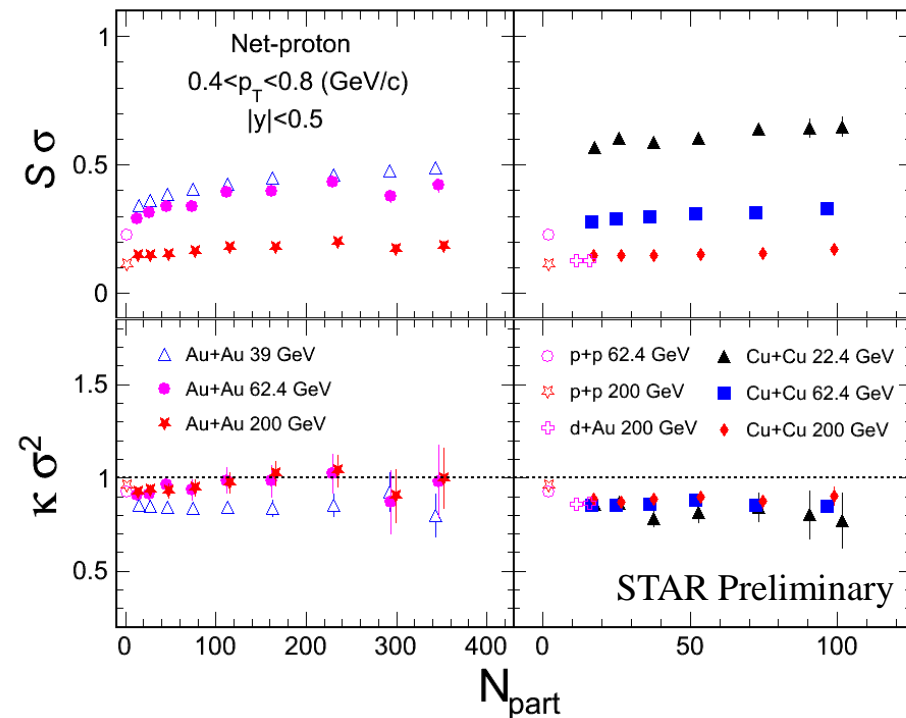
The 62.4 and 200 GeV data are published in PRL 105 (2010) 022302

X. Luo, arXiv:1106.2926

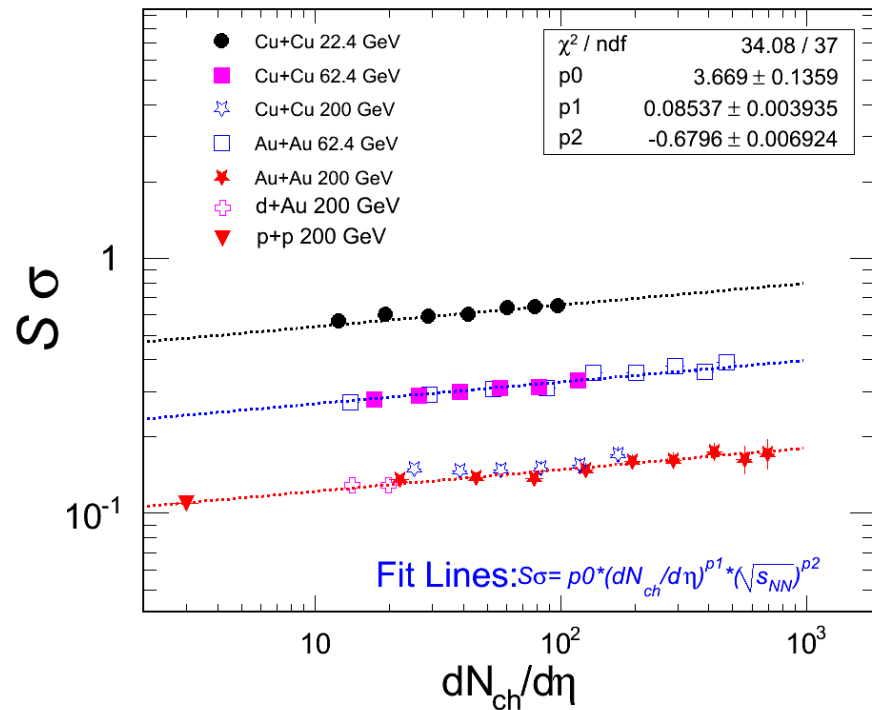
Consistent with CLT Expectations (lines).

Indicates many identical, independent particle emission sources.

Centrality Dependence (II): Moment Products



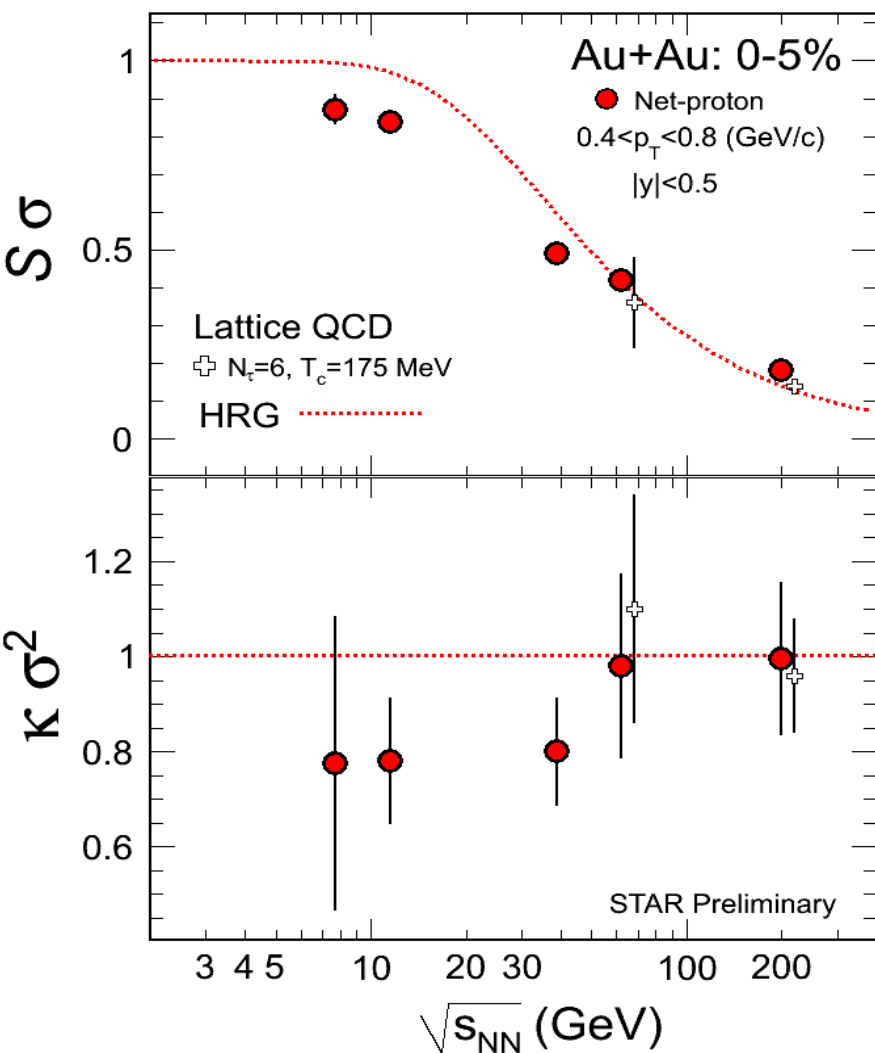
The 62.4 and 200 GeV data are published
in PRL 105 (2010) 022302



X. Luo, arXiv:1106.2926

- $S\sigma$: Slightly increase with centrality and strong energy dependence.
Scale with the $dN/d\eta$ for fixed energy.
- $K\sigma^2$: Weak centrality and energy dependence.

STAR Energy Dependence of Moment Products



➤ Consistent with HRG and Lattice QCD results at high energy.

R. Gavai and S. Gupta, Phys. Lett. B 696, 459 (2011)
 F. Karsch and K. Redlich, Phys. Lett. B 695, 136 (2011)

➤ Deviations from HRG model from 39 GeV.

Possible Reasons of the deviations:

1. Link to the chiral phase transition and/or critical point.

B. Friman et al., Eur. Phys. J. C71, 1694 (2011)
 M. A. Stephanov, arXiv:1104.1627

2. Non-applicable of Grand Canonical Ensemble (GCE).

Analysis of 19.6 and 27 GeV data with high statistics are ongoing....

62.4 and 200 GeV data are published in PRL 105 (2010) 022302

- Higher moments are directly related to thermodynamic susceptibilities in Lattice QCD and HRG model. **It opens a new domain of probing bulk properties of nuclear matter.**
- Higher moments of net-proton distributions in heavy ion collisions are applied to **search for the QCD critical point.** Preliminary results from STAR BES data are obtained.
- Deviations from HRG model for $S\sigma$ and $\kappa\sigma^2$ are observed. The possible reasons are discussed.

Outlook: The results for 19.6 and 27 GeV high statistics data will come soon.