

# Measurements of Kaon Femtoscopy in Au+Au Collisions at $\sqrt{s_{NN}} = 3.0 - 4.5$ GeV by the STAR Experiment

Bijun Fan (*for the STAR collaboration*)

Central China Normal University



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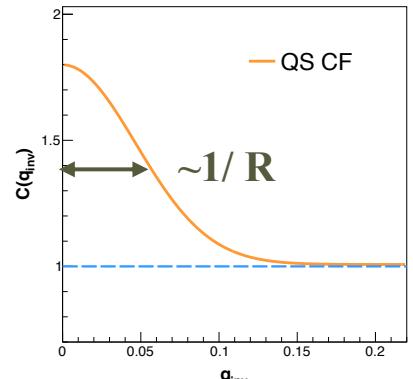
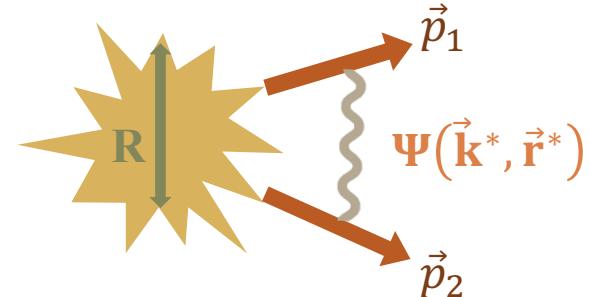
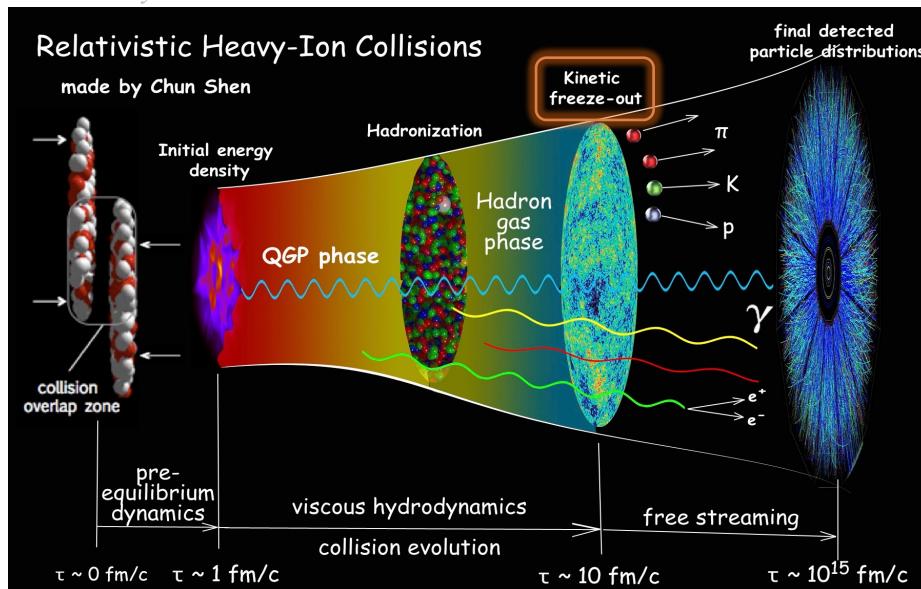
# Outline

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- ❖ **Introduction**
- ❖ **STAR Experimental Setup**
- ❖ **Analysis Details**
- ❖ **Results and Discussions**
  - 1) Correlation functions**
  - 2) Extracted parameters and  $m_T$ - scaling**
- ❖ **Summary**

# Introduction - femtoscopy

<https://u.osu.edu/vishnu/2014/08/06/sketch-of-relativistic-heavy-ion-collisions/>



$$C(q_{\text{inv}}) = \int S(\vec{r}^*) |\Psi(q_{\text{inv}}, \vec{r}^*)|^2 d^3 \vec{r}^* = \mathcal{N} \frac{N_{\text{same}}(q_{\text{inv}})}{N_{\text{mixed}}(q_{\text{inv}})}$$

Assumed Determined Measured

❖ Decode space and time evolution of source at kinetic freeze-out.

❖ Why study kaons?

- 1) less contribution from resonances decay
- 2) smaller rescattering cross-section

❖ Two-particle correlations are sensitive to:

- 1) Quantum Statistics (QS);
- 2) Final State Interactions (FSI)

❖ If we assume that we know the **emission function**, the **measured correlation function** can be used to determine **parameters of final state interactions**.

$\vec{r}^*$ : relative distance of the emitters in the Pair Rest Frame (PRF: in which frame the total momentum of the pair is zero)

$S(\vec{r}^*)$ : emission function

$q_{\text{inv}}$ : relative invariant momentum in PRF

$$q_{\text{inv}} = \sqrt{|\mathbf{q}|^2 - q_0^2}, \text{ where } \mathbf{q} = \mathbf{p}_1 - \mathbf{p}_2, q_0 = E_1 - E_2$$

For identical particles,  $q_{\text{inv}} = 2k^*$

$\Psi(q_{\text{inv}}, \vec{r}^*)$ : two-particle wave function

$\mathcal{N} \frac{N_{\text{same}}(q_{\text{inv}})}{N_{\text{mixed}}(q_{\text{inv}})}$ : measured correlation function

# Introduction - Parametrization

- ❖ CF including only Quantum Statistical(QS) effect:

$$CF(q_{inv}) = 1 + \lambda e^{-[R_G^2 q_{inv}^2]}$$

- ❖ For  $K^+ - K^+$  and  $\pi^+ - \pi^+$ , Bowler-Sinyukov<sup>[1]</sup> method to include FSI(Coulomb effect):

Coulomb effect QS effect

$$CF(q_{inv}) = N[(1 - \lambda) + K_{coul}(q_{inv}, R_G)\lambda(e^{-[R_G^2 q_{inv}^2]} + 1)]$$

**R<sub>G</sub>**: source radii parameter;  
**λ**: correlation strength;  
**N**: normalization factor;

- ❖ For  $K_S^0 - \bar{K}_S^0$ , Lednický-Lyuboshitz (L-L)<sup>[2]</sup> approach to include FSI(Strong interaction):

QS effect

Strong interaction through  $f_0(980)$  /  $a_0(980)$  resonances

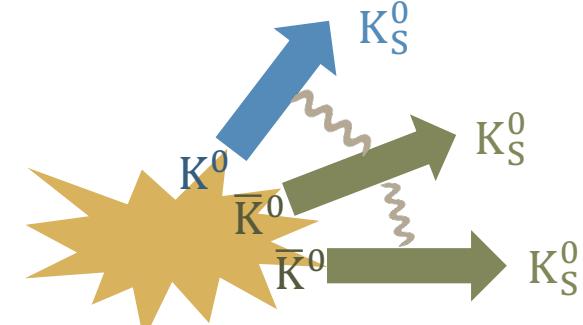
$$CF(q_{inv}) = 1 + \lambda(e^{-[R_G^2 q_{inv}^2]} + \frac{1 - \epsilon^2}{2} [\left| \frac{f(k^*)}{R_G} \right|^2 + \frac{4\text{Re}[f(k^*)]}{\sqrt{\pi}R_G} F_1(q_{inv}R_G) - \frac{2\text{Im}[f(k^*)]}{R_G} F_2(q_{inv}R_G)])$$

abundance asymmetry  $\epsilon$

$$\epsilon = \frac{K - \bar{K}}{K + \bar{K}}$$

Resonance parameters:

|                          | $m_{f_0}$ | $\gamma_{f_0 KK}$ | $\gamma_{f_0 \pi\pi}$ | $m_{a_0}$ | $\gamma_{a_0 KK}$ | $\gamma_{a_0 \pi\eta}$ |
|--------------------------|-----------|-------------------|-----------------------|-----------|-------------------|------------------------|
| Antonelli <sup>[3]</sup> | 0.973     | 2.763             | 0.5283                | 0.985     | 0.4038            | 0.3711                 |



- $K_S^0 - \bar{K}_S^0$  consist of  $K^0 - K^0$  ( $\bar{K}^0 - \bar{K}^0$ ) and  $K^0 - \bar{K}^0$  states
- Kaon abundance asymmetry can be extracted by  $K_S^0 - \bar{K}_S^0$  CF

$$F_1(z) = \int_0^z dx \frac{e^{x^2 - z^2}}{z}; F_2(z) = \frac{1 - e^{-z^2}}{z}.$$

$$\text{scattering amplitude: } f(k^*) = \frac{f_0(k^*) + f_1(k^*)}{2}$$

$$f_I(k^*) = \frac{\gamma_I}{m_I - s - i\gamma_I k^* - i\gamma'_I k'_I}, s = 4(m_K^2 + k^{*2})$$

$I = 0$  or  $1$  for the  $f_0$  or  $a_0$ ;

$m_I$ : mass of the resonance;

$\gamma_I$  and  $\gamma'_I$ : couplings of the resonances to their decay channels;

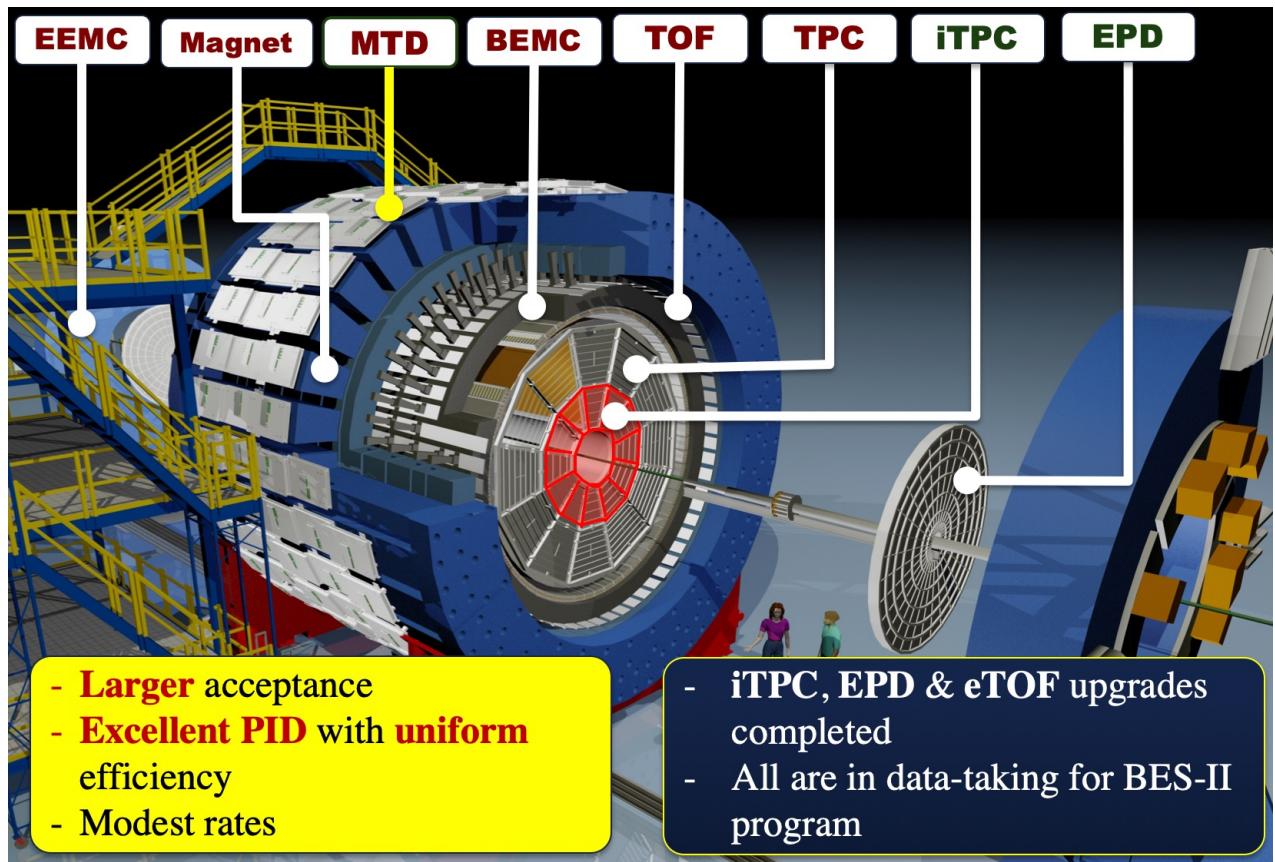
$k'_I$ : momentum in the second decay channel.

[1] Phys. Lett. B, 432(3-4), 248-257 (1998)

[2] J.Nucl.Phys. 35, 770 (1982)

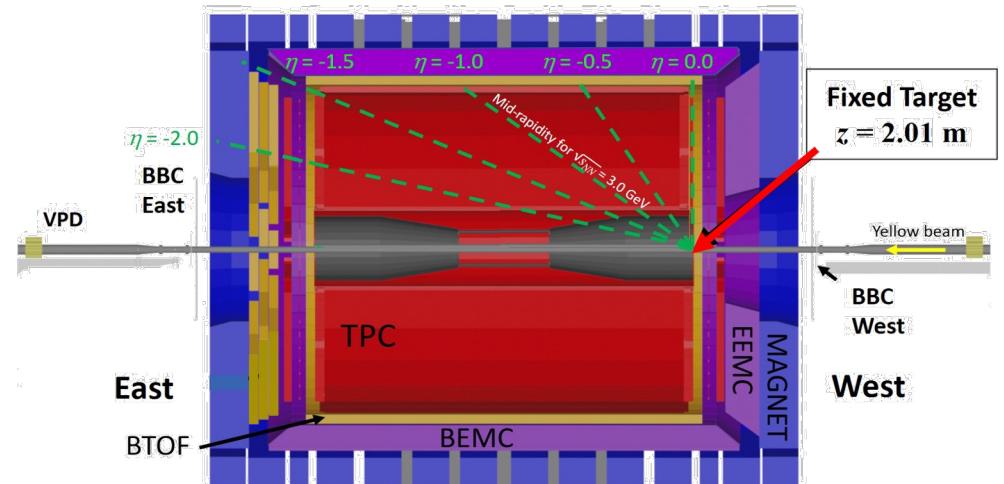
[3] eConfC020620, THAT06 (2002)

# STAR Experimental Setup



## Main sub-detectors for PID

- ❖ Time Projection Chamber (TPC): Ionization energy loss ( $dE/dx$ )
- ❖ Time of Flight (TOF):  $m^2$



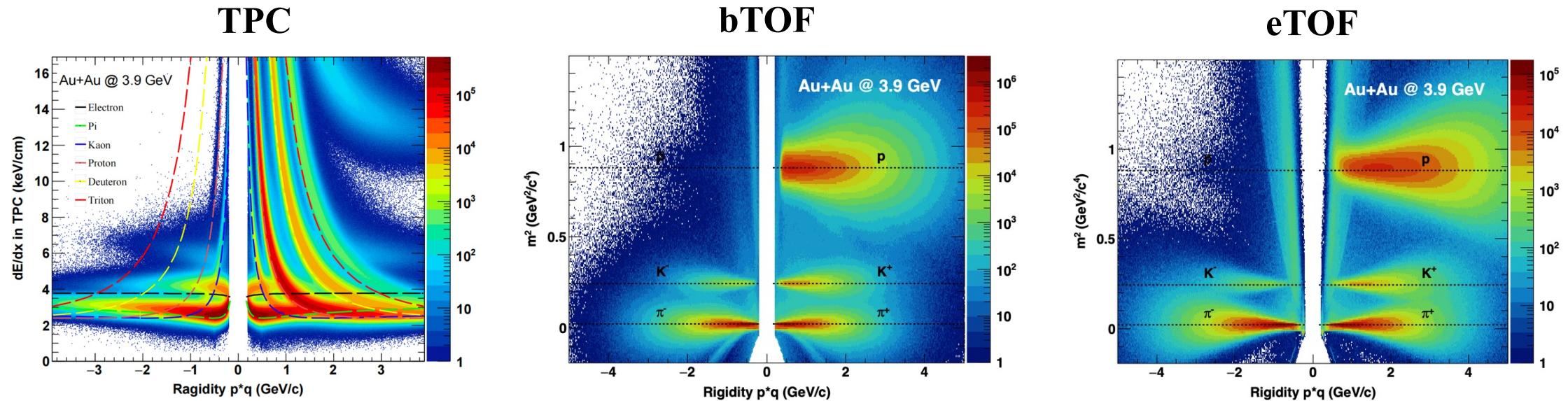
## BES-II Upgrades

- ❖ Inner-Time Projection Chamber (iTPC)
  - Extended eta acceptance and improved tracking and  $dE/dx$  resolution
- ❖ Endcap Time of Flight (eTOF)
  - Extended PID coverage
- ❖ Event Plane Detector (EPD)
  - Improved Event plane resolution

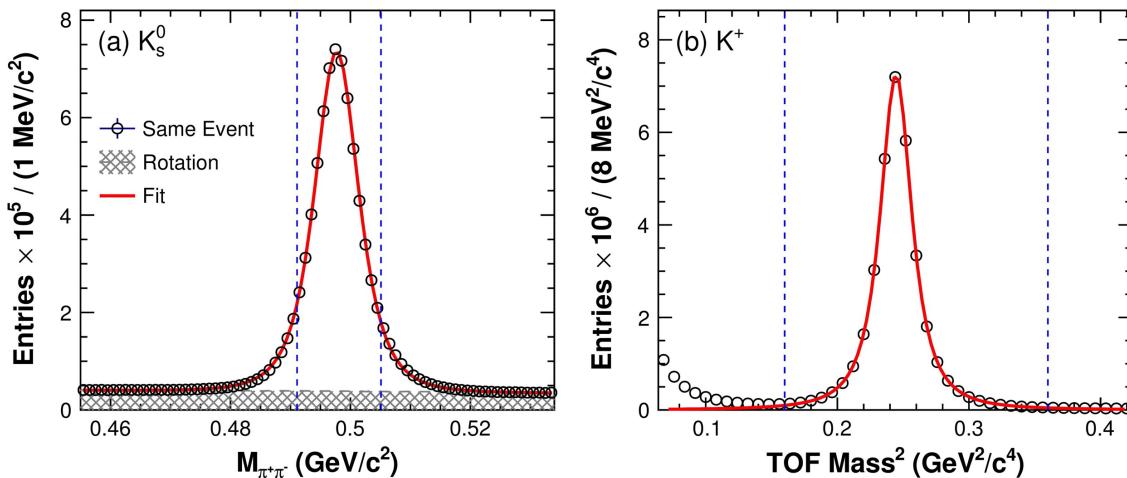
## Fixed-Target Experiment

- ❖ FXT extends energy reach down to 3 GeV ( $\mu_B = 750 \text{ MeV}$ )

# Analysis details – PID, reconstruction



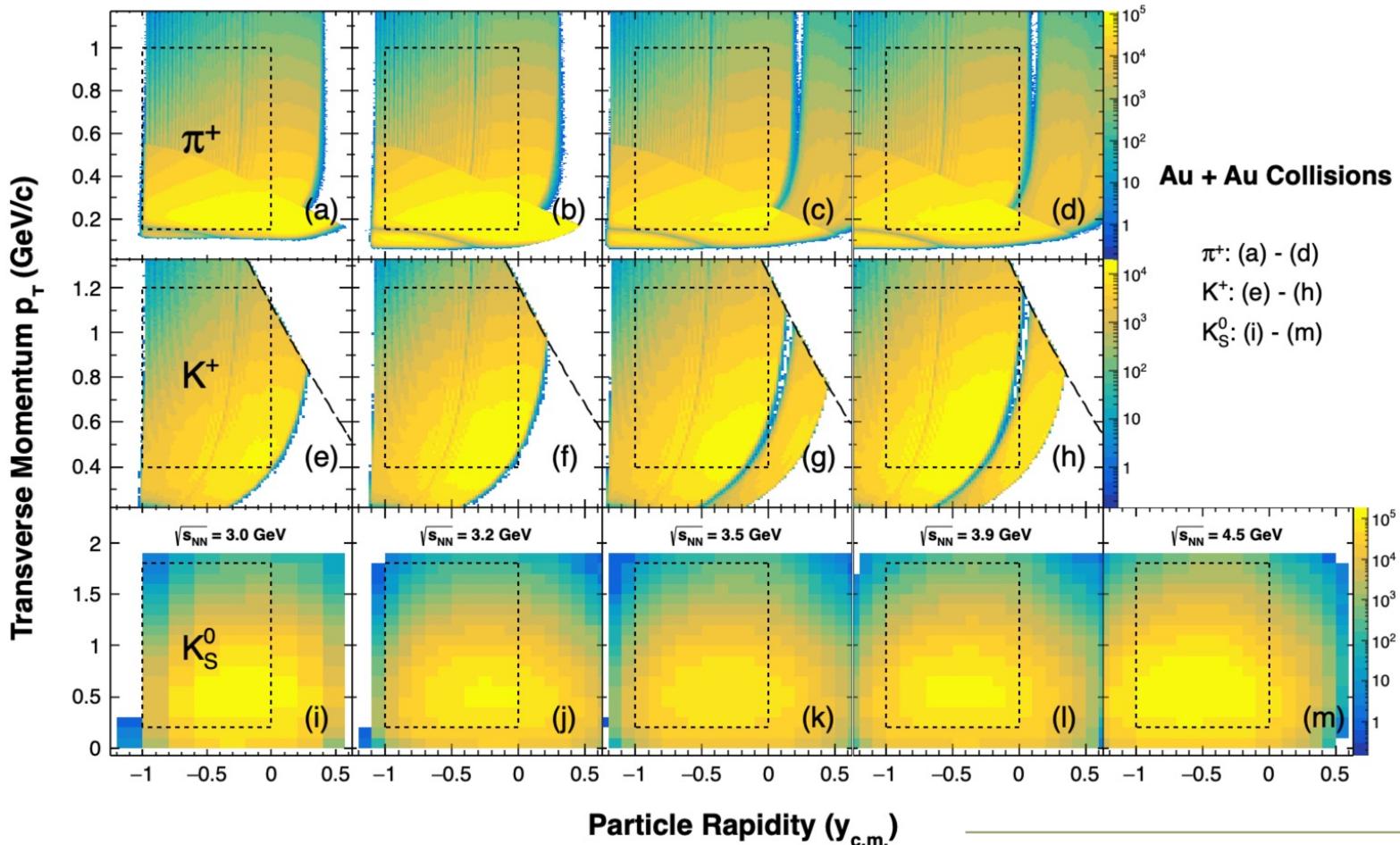
3.9 GeV Au + Au Collisions at RHIC



- ❖  $\pi^+$  and  $K^+$  particles identified by TPC and TOF
- ❖  $K_S^0$  hadrons reconstructed using invariant mass method:  

$$K_S^0 \rightarrow \pi^+\pi^-$$

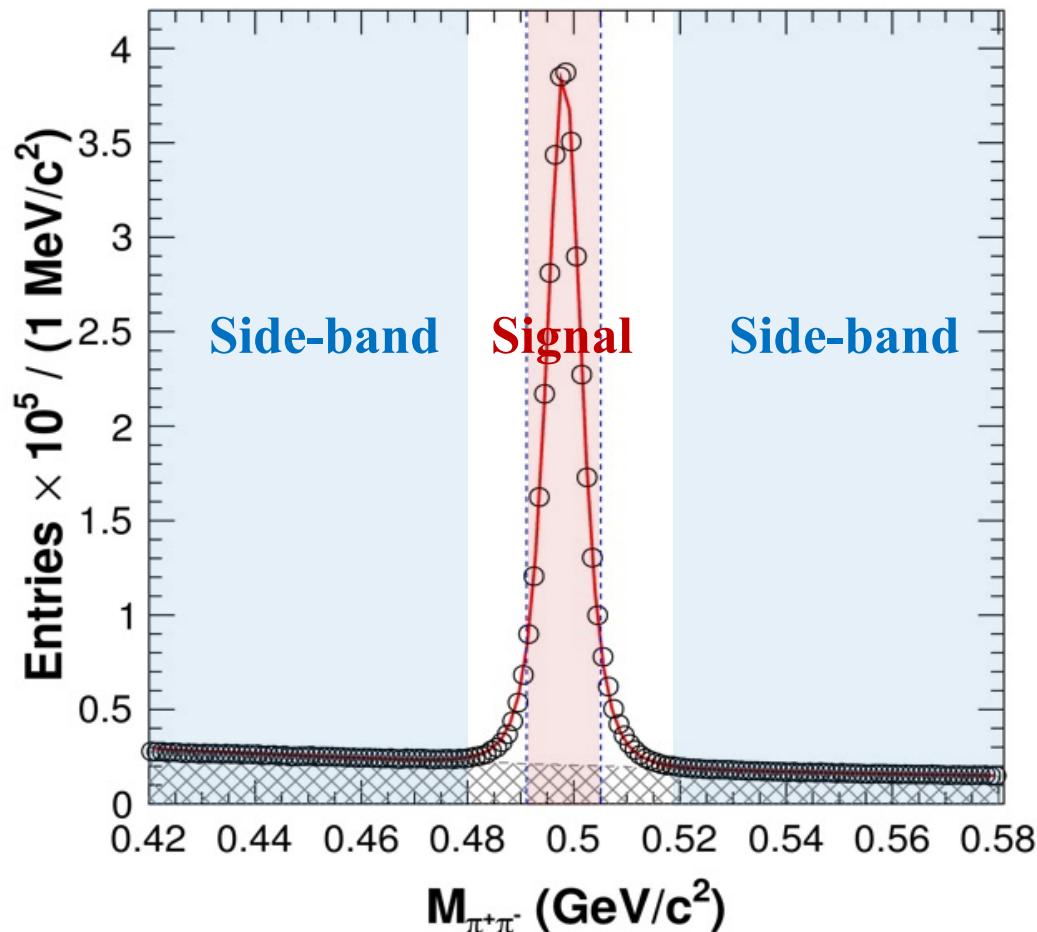
# Analysis details – acceptance



- ❖  $K_S^0$  reconstruction: KF Particle package
- ❖ Good coverage from beam-rapidity to mid-rapidity

| Particle | Analysis window                                  |
|----------|--|
| $\pi^+$  | $-1.0 < y < 0, 0.15 < p_T < 1.0 \text{ (GeV/c)}$ |
| $K^+$    | $-1.0 < y < 0, 0.4 < p_T < 1.2 \text{ (GeV/c)}$  |
| $K_S^0$  | $-1.0 < y < 0, 0.2 < p_T < 1.8 \text{ (GeV/c)}$  |

# Analysis details – Purity correction



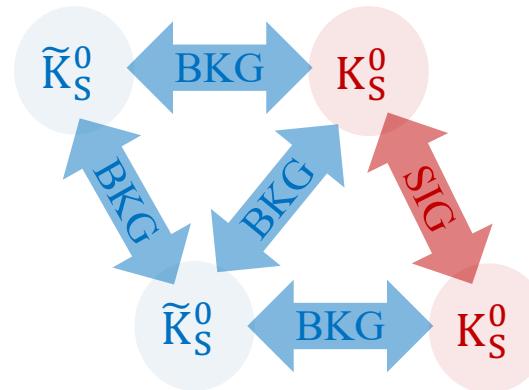
$$C(q_{\text{inv}}) - 1 =$$

measured

$$\omega_{\text{Pair Purity}}[C_{\text{pure}}(q_{\text{inv}}) - 1] +$$

we want this

Combinatorial background



$K_S^0$ : Signal

$\bar{K}_S^0$ : Background

Signal pair:  $K_S^0 - K_S^0$

Background pair:  $K_S^0 - \bar{K}_S^0, \bar{K}_S^0 - \bar{K}_S^0$

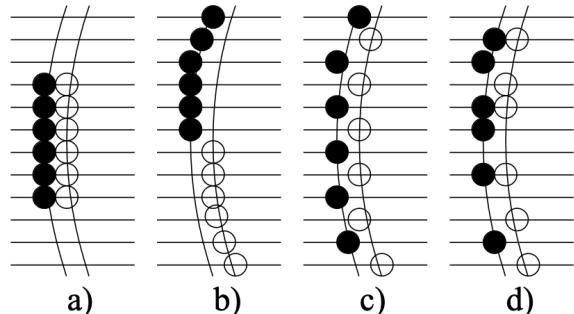
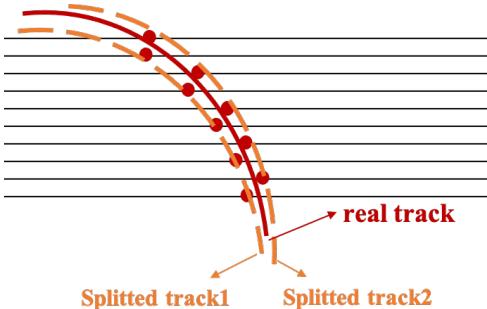


$$(1 - \omega_{\text{Pair Purity}})[C_{\text{BKG}}(q_{\text{inv}}) - 1]$$

background

# Analysis details – Pair track correction

## Track-splitting effect



$$\text{Splitting Level (SL)} \equiv \frac{\sum_i S_i}{\text{Nhits}_1 + \text{Nhits}_2}$$

$S_i = +1$ : one hit  
 $S_i = -1$ : two hits<sup>[1]</sup>  
 $S_i = 0$ : no hit

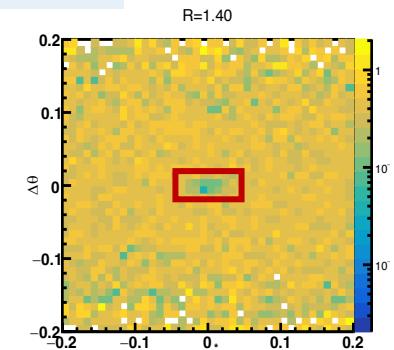
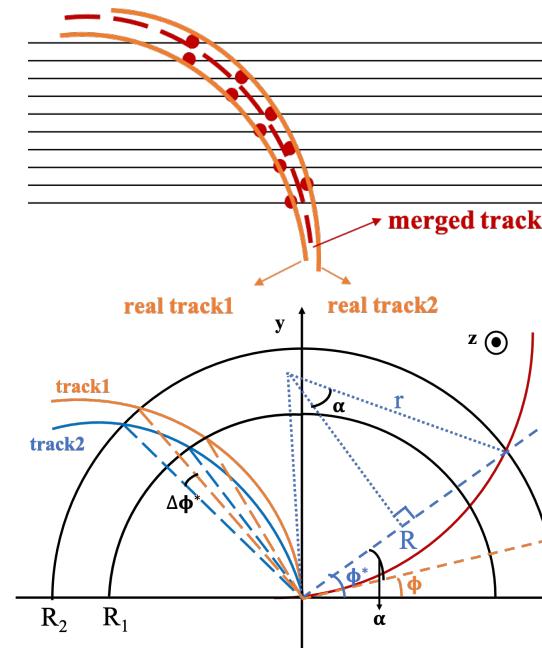
- ❖ Results in an increase of pairs, amplifying signal of CF
- ❖ Remove:  $-0.5 < \text{SL} < 0.6$  used both for Kaon and pion

i - the pad-row number

Nhits<sub>1</sub> & Nhits<sub>2</sub> - the total number of hits associated to each track in the pair

[1] arXiv:nul-ex/0411036

## Track-merging effect

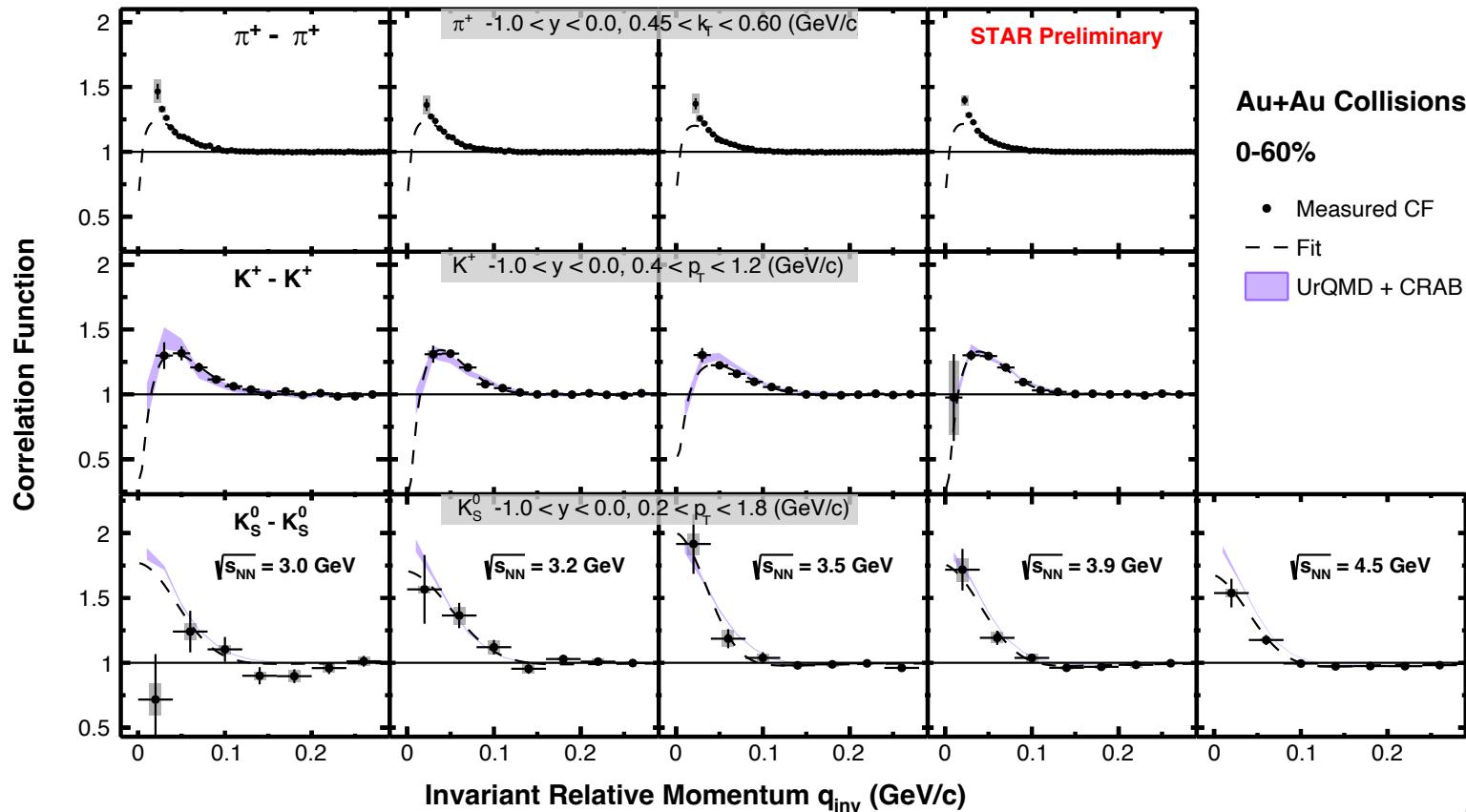


**R** - The radius of TPC we choose;  
**r** - The radius of the rotation of particle;  
**B** - Magnetic field intensity;  
**q** - The charge of particle;  
**p<sub>T</sub>** - The transverse momentum of particle;

$$\Delta\phi^* = \Phi_1^* - \Phi_2^* = \Delta\phi + \sin^{-1}\left(\frac{0.15q_1BR}{p_{T1}}\right) - \sin^{-1}\left(\frac{0.15q_2BR}{p_{T2}}\right)$$

- ❖ Results in a reduction of pairs, reducing signal of CF
- ❖ Remove: for Kaon,  $|\Delta\theta| > 0.02 \quad \text{||} \quad |\Delta\phi^*(R = 1.4m)| > 0.05$   
for pion,  $|\Delta\eta| > 0.04 \quad \text{||} \quad |\Delta\phi^*(R = 1.4m)| > 0.06$

# Results - Correlation functions



- ❖ CF of  $\pi^+$ ,  $K^+$ , and  $K_S^0$  with same rapidity range are shown
- ❖ Calculations of UrQMD+CRAB consistent with experimental data
- ❖ Four different scattering amplitude parameters<sup>[1,2,3,4]</sup> for  $K_S^0$  compared, and consistent with each other

Au+Au Collisions

0-60%

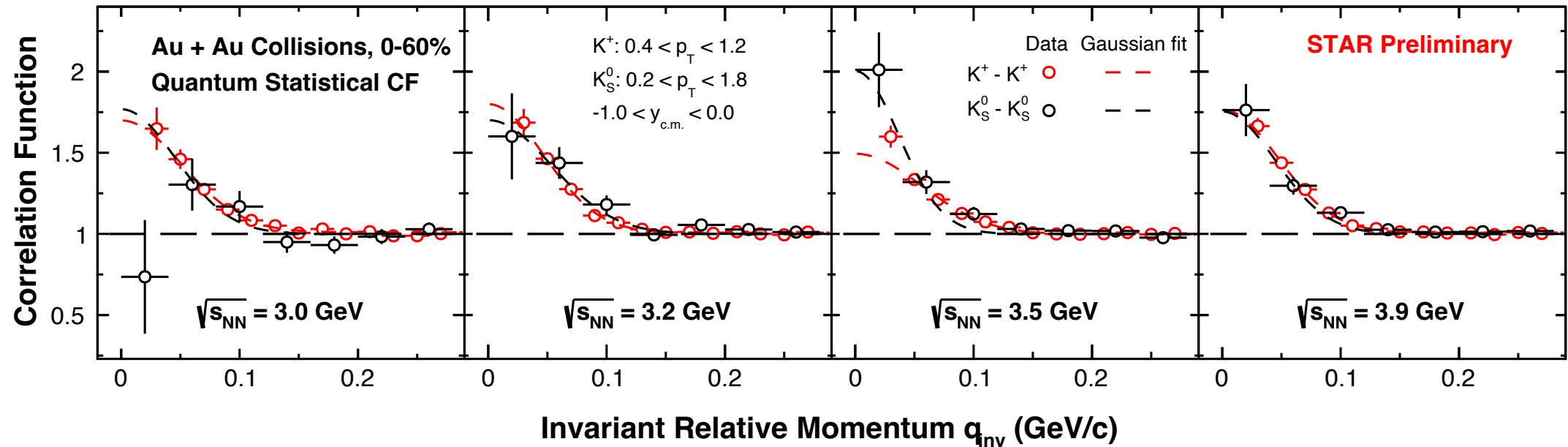
- Measured CF
- Fit
- UrQMD + CRAB

- ❖ UrQMD (provide phase space)<sup>[5,6]</sup>  
Version: 3.4  
Cascade mode
- ❖ CRAB (generate correlation: QS, FSI)  
Version: 3.0b

<https://web.pa.msu.edu/people/pratts/freecodes/crab/home.html>

- [1] eConfC020620, THAT06 (2002)
- [2] Phys. Rev. D 63, 094007 (2001)
- [3] Phys. Rev. D 68, 014006 (2003)
- [4] Nucl. Phys. B 121, 514–530 (1977)
- [5] S.A.Bass et al., Prog.Part.Nucl.Phys. 41 (1998) 225
- [6] M.Bleicher et al., J.Phys. G25 (1999) 1859

# Results - Correlation functions

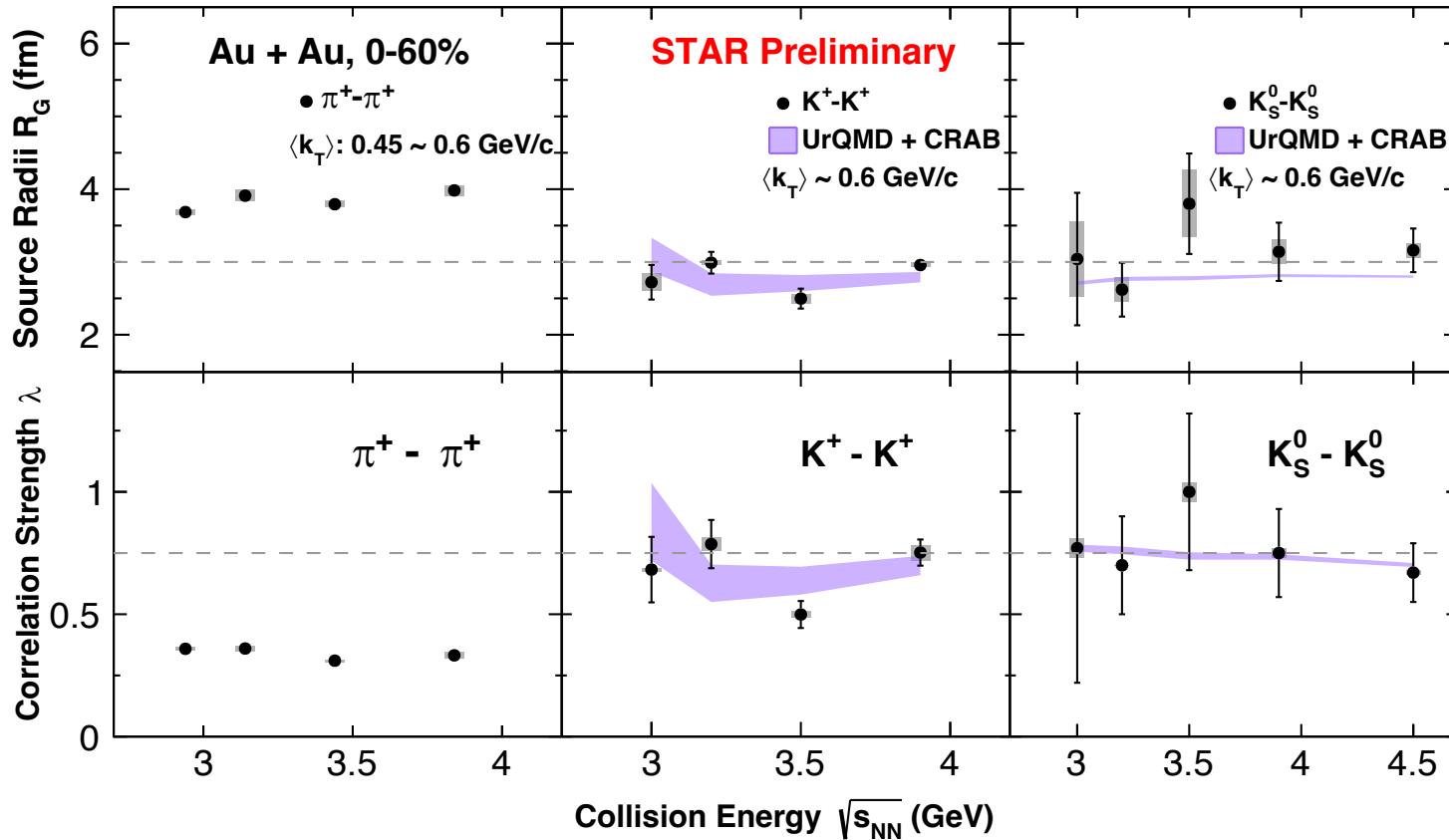


- ❖ CF of  $K^+ - K^+$  after subtracting Coulomb effect consistent with  $K_S^0 - K_S^0$  without strong interaction

Extraction of QS correlation function:

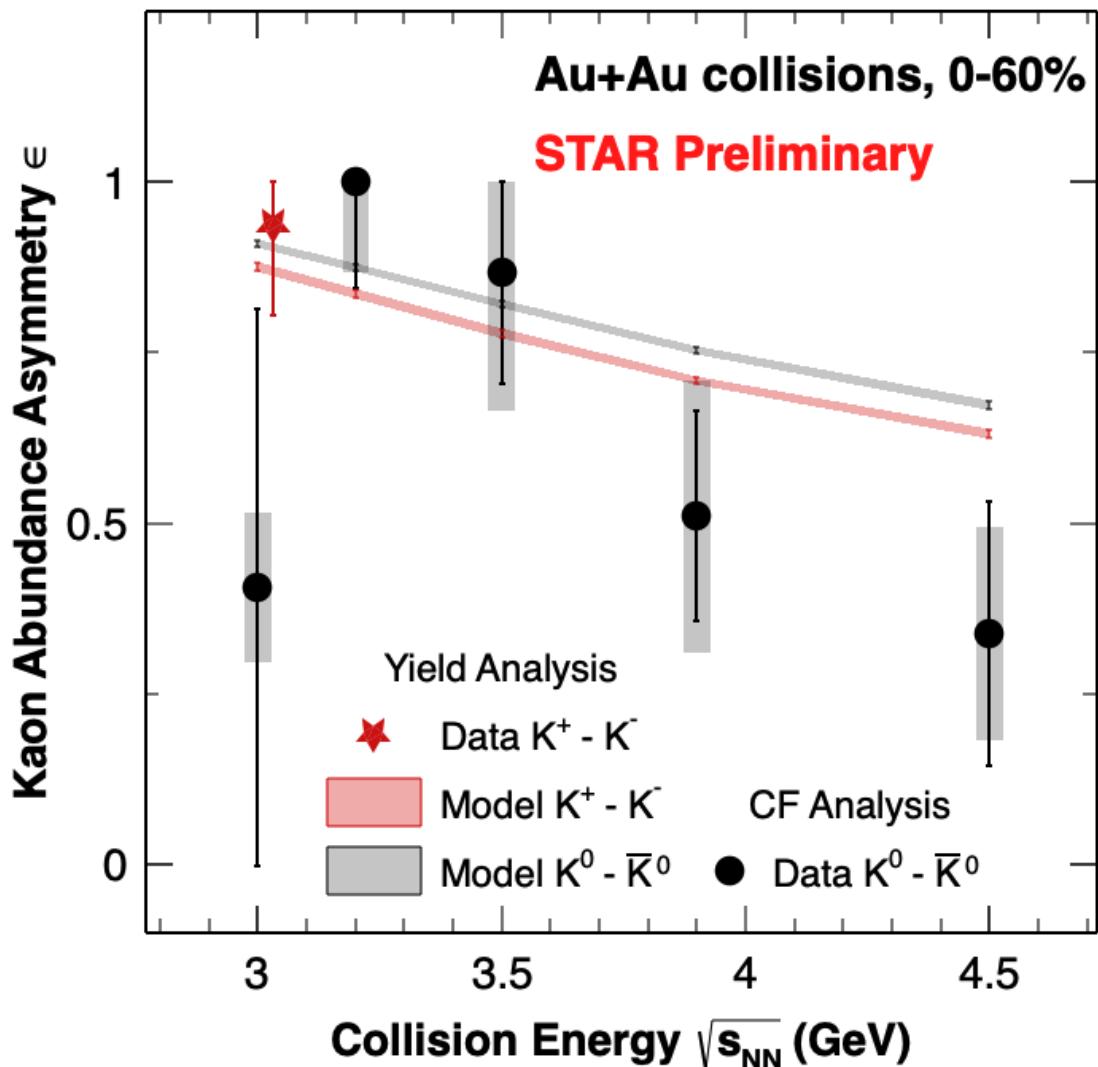
1. Fit the measured correlation function
2. Extract the parameters and get the FSI function
3. Subtract FSI from data points to get the Quantum statistics part contribution

# Results - extracted parameters

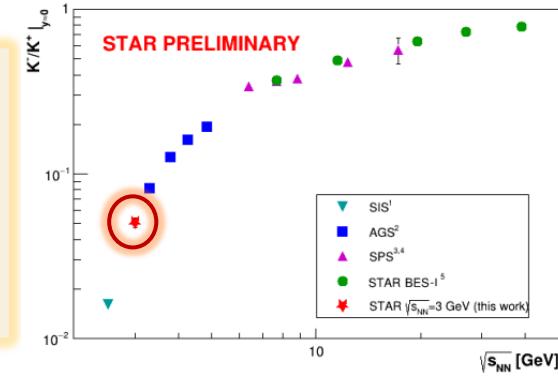


- ❖ No clear energy dependence for  $R_G$  and  $\lambda$ , model consistent with data
- ❖  $\lambda$  of kaons larger than pions', implying less impact from resonances decay
- ❖ Within uncertainties,  $R_G$  and  $\lambda$  of charged kaon correlation data consistent with that from neutral kaon

# Results – Kaon abundance asymmetry

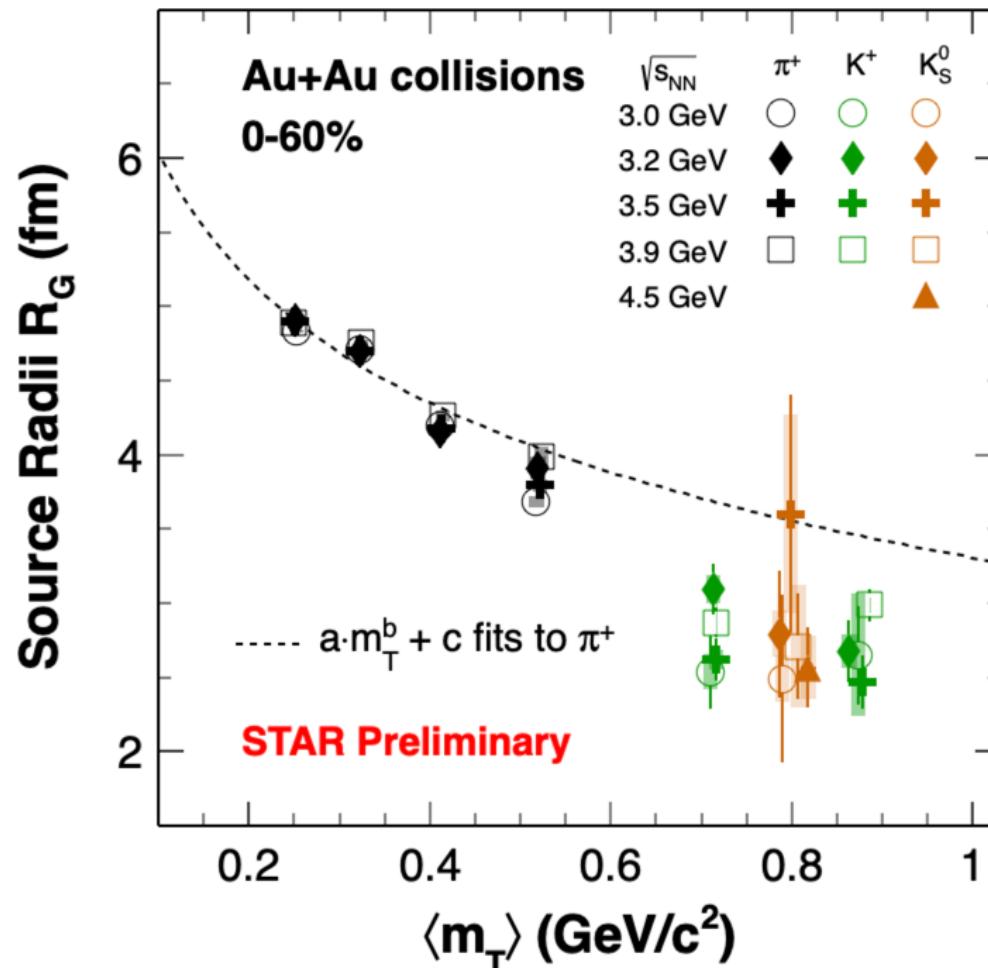


- ❖ Yield Analysis:  $\epsilon = \frac{K - \bar{K}}{K + \bar{K}}$
- Yield of  $K^- / K^+$  at 3 GeV: STAR Preliminary
- ❖ CF Analysis: L-L fitting from  $K_S^0 - \bar{K}_S^0$  CF



- ❖  $K_S^0$  is a mixture of s,  $\bar{s}$  quarks, thus can extract  $\epsilon$  by correlation function
- ❖ First measurement of neutral kaon  $\epsilon$  in heavy ion collisions
- ❖  $\epsilon$  of kaon decreases with energy, model reproduce trend of data
  - 1) Associate production dominates at high baryon density
  - 2) Pair production more important at higher energies

# Results - $m_T$ - scaling



- ❖  $R_G$  of kaons smaller than that of pions
- ❖  $R_G$  of kaons do not follow  $m_T$  - scaling of pions', implying no equilibrium amongst pions and kaons at high baryon density

# Summary

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- ❖ First measurement of kaon and pion femtoscopy at high baryon density
- ❖ Within uncertainties, extracted parameters of charged kaon correlation data are consistent with that from neutral kaon
- ❖  $\lambda$  of kaons larger than pions', implying less impact from resonances decay
- ❖ For  $\sqrt{s_{NN}} = 3.0 - 4.5$  GeV:
  - 1) No clear energy dependence of  $R_G$  and  $\lambda$  while  $\epsilon$  of kaon decreases with energy
  - 2)  $R_G$  of kaons do not follow  $m_T$ - scaling of pion's, implying no equilibrium amongst pions and kaons

Thanks for your attention!