

LONG-RANGE PSEUDORAPIDITY CORRELATIONS AT HIGH P_T IN
 $\sqrt{S_{NN}} = 200$ GEV AU+AU COLLISIONS WITH STAR

A Dissertation

by

MARTIN JOHN MICHAEL CODRINGTON

Submitted to the Office of Graduate Studies of
Texas A&M University
in partial fulfillment of the requirements for the degree of

DOCTOR OF PHILOSOPHY

August 2012

Major Subject: Chemistry

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Approved by:

Co-Chairs of Committee,	Saskia Mioduszewski Joseph Natowitz
Committee Members,	Sherry Yenello Ralf Rapp Carl Gagliardi Charles Folden
Head of Department,	David Russell

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ABSTRACT

Long-Range Pseudorapidity Correlations at High p_T in $\sqrt{S_{NN}} = 200$ GeV Au+Au
Collisions with STAR. (August 2012)

Martin John Michael Codrington, B.S., Morgan State University

Co-Chairs of Advisory Committee: Dr. Saskia Mioduszewski
Dr. Joseph Natowitz

The Quark Gluon Plasma (QGP) is a form of matter in which quarks and gluons are deconfined, and was suggested to be formed in high-energy heavy-ion collisions. Since the discovery of high- p_T hadron suppression in central Au+Au collisions at the Relativistic Heavy Ion Collider (RHIC), and the related discovery of the quenching of the away-side jet in these collisions, the role of jets as key probes of the QGP was re-affirmed. The Solenoidal Tracker At RHIC (STAR) detector system, which is suited for jet studies because of its large solid-angle coverage, has produced a number of interesting jet measurements in recent years, including γ -jet measurements, attempts at full heavy-ion jet reconstruction, and two-dimensional correlations. A long-range correlation in pseudorapidity (the ‘‘Ridge’’) was studied (with statistical significance) out to $p_T^{trig.} < \sim 7$ GeV/ c and was assumed to have an integrated yield independent of $p_T^{trig.}$. Further studies out to higher p_T were limited by the minimum biased statistics taken in Run 4 (2004) with STAR. This work presents results of a ridge analysis with (non-reconstructed) π^0 s and direct- γ -rich triggers out to ~ 13.5 GeV/ c in $p_T^{trig.}$ using triggered data from Run 7 (2007) and Run 10 (2010) Au+Au collisions detected with STAR. Preliminary results seem to indicate that the ridge yield decreases with $p_T^{trig.}$, and that the ridge yield for direct- γ -rich triggers is consistent with zero.

To Rosalind Wilson (In Memoriam)

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CHAPTER I

INTRODUCTION I: RELATIVISTIC HEAVY-ION COLLISIONS

I.1. Overview

This dissertation presents results of a correlation analysis, investigating a long-range structure observed in pseudorapidity, with high p_T π^0 , and a sample of direct- γ -rich, triggers; using data taken in Runs 7 and 10 of the Relativistic Heavy Ion Collider (RHIC) using the Solenoidal Tracker At RHIC (STAR) detector system. The work is divided into seven chapters with one supplemental appendix. The first chapter is an overview of relativistic heavy ion collisions, with particular emphasis placed on those experimental and theoretical concepts that directly relate to this analysis, such as the Quark Gluon Plasma (QGP), collision geometry and centrality, elliptic flow, and jets and jet quenching. The second chapter discussed some theoretical calculations that seek to explain the existence of the ridge. The third chapter introduces RHIC and STAR in detail, emphasizing the trigger and detector systems used in this analysis. Chapter IV discusses the calibration of the STAR Barrel Shower-Maximum Detector (BSMD) in detail, and outlines its role in distinguishing between direct photons and π^0 s. Chapter V is the analysis chapter, in which details of analysis methods and cuts are discussed. Chapter VI is the results chapter and presents the most interesting results from this analysis. The final chapter, Chapter VII summarizes these results, draws conclusions, and suggests possible future analysis objective for π^0 and γ - triggered long-range pseudorapidity correlations. Following the last chapter is one appendix that list analysis details not appropriate for the main text.

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I.2. The Quark-Gluon Plasma

Quantum Chromodynamics (QCD)[28][29][30] is the underlying theory of the strong interaction, and the most successful theory in describing the behavior of nuclear matter at high densities and temperatures. One of the first QCD-based predictions of a new phase of nuclear matter was a 1975 prediction[31] that stated that in the center of neutron stars, because of the reduction of the coupling constant at small distances, there should exist a new type of matter composed entirely of deconfined quarks and gluons. Although this prediction was focused on the high-density, low-temperature regime, the authors suggested that a similar phase of matter may have existed in the high-temperature environment of the early universe. It was not until 1980 however, that a detailed exploration of this idea was provided in a review paper by Shuryak[32], who coined the phrase Quark-Gluon Plasma (QGP) to describe this state of deconfined quarks and gluons. The transition from hadronic nuclear matter, to this new partonic nuclear matter, was predicted to occur at a critical energy density, ϵ_C , of $\sim 1 \text{ GeV}/\text{fm}^3$, at a critical temperature, T_C , of $\sim 170 \text{ MeV}$; this is a region where the coupling constant is still large, making it difficult to do perturbative QCD calculations. The development of lattice QCD[33][34] allowed calculations (albeit for an idealized matter) to be made. Figure I.1 shows such a calculation of ϵ/T^4 versus T/T_C ; the rapid rise in the number of degrees of freedom at T_C indicates a phase transition[3]. The system then equilibrates to a ϵ/T^4 value less than the Stefan-Boltzmann limit for a non-interacting ideal gas, indicating that the new state present after the transition is interacting.

Although lattice QCD predicts (and experimental observations seem to show) a new state of matter being formed in relativistic heavy ion collisions, there is no definitive answer as to what the order of this transition from hadronic matter is[35].

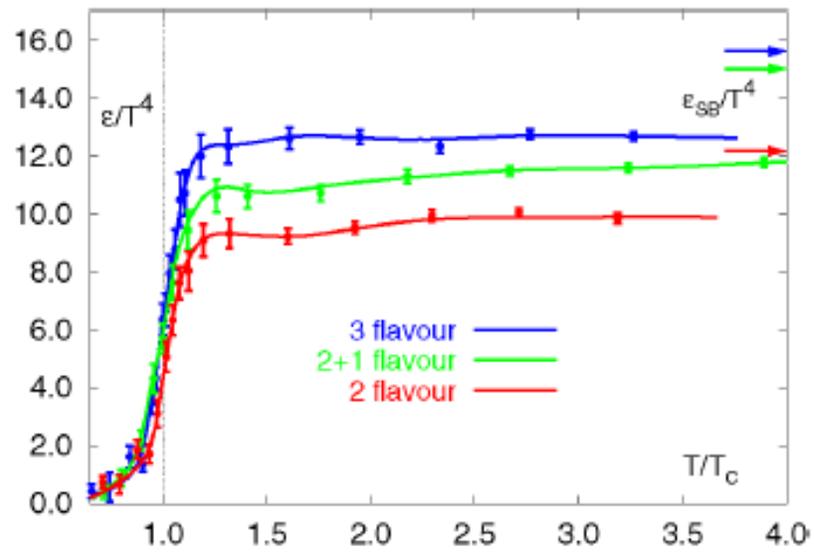


Fig. I.1.: Lattice QCD calculations[3] of energy density divided by T^4 as a function of T/T_c . The degrees of freedom rise sharply at T_c . Arrows indicate the Stefan-Boltzmann limit (ideal gas values for ϵ/T^4).

In lattice calculations where pure gauge theory (gluons only) is used, the transition is predicted to be first order; adding an up and down quark to this framework, changes the transition to second order; and adding a strange quark to the up and down, creates a smooth crossover. These calculations indicate that, in the real QGP, the order is unlikely to be first or second order; this makes the task of experimentally observing the QGP more difficult, because there will not be any obvious changes in behavior of the matter that will serve to indicate a transition. Experimental signatures of QGP formation will likely come from observed final-state effects in produced hadrons, or from prompt probes (such as the direct photon) that are created early in the collision dynamics.

I.3. Relativistic Heavy-Ion Collisions

Relativistic heavy-ion collisions, as the name suggests, are collisions between heavy ions in the relativistic regime (typically at speeds of $\sim 99.995\%$ the speed of light). It is with such collisions energies that the QGP is expected to form. This section begins with a brief overview of the stages in these collisions and puts in perspective the theoretical and experimental considerations for each stage. Next, the geometry of the collision, specifically the impact parameter and its experimental signatures, is described. Lastly, the bulk behavior of the medium is described by discussing flow, specifically elliptic flow.

I.3.1. The Stages of a Collision

Figure I.2[4] is a model illustration of the five stages of relativistic heavy-ion collisions. The theoretical stages can be described as follows.

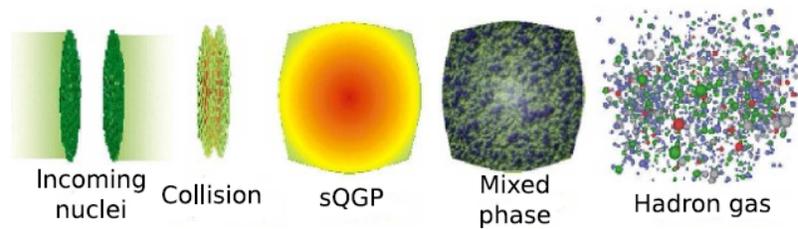


Fig. I.2.: Illustration of the five main stages in relativistic heavy ion collisions[4]. See text for a full description of these stages.

Stage I – Incoming Nuclei: The first stage shows the incoming nuclei which are Lorentz contracted (in the direction parallel to the beam axis) because of their relativistic speeds. Experimentally, this phase corresponds to the acceleration of bunches of heavy ions to 99.995% the speed of light, in the presence of a magnetic field. The acceleration of heavy ions is discussed in detail in the next chapter, in the context of the Relativistic Heavy Ion Collider (RHIC).

Stage II – Collision Occurs: In the second stage, collisions occur among the constituent quarks and gluons; hard-scatterings (see next section) occur during this stage. This is the stage with the highest temperature and energy density. However, it is not directly observable experimentally; except by detecting prompt non-interacting probes (such as the direct photon) that may be produced in the hard scatterings that occur in this stage.

Stage III – QGP Formation: In the figure the QGP is labeled sQGP; for strongly-interacting quark gluon plasma. This is the stage of theoretical interest in these types of collisions, but it also is not observable experimentally. Only Stage V is directly observable.

Stage IV – Mixed Phase: This stage is the mixed phase of hadron and partons, neither chemical nor kinetic freeze-out have occurred. New hadrons are being produced, existing hadrons may undergo transmutation, and collisions occur between hadrons and partons.

Stage V – Hadron Gas Formation: The final stage is the hadron gas stage; all partons are now bound in hadrons and chemical and kinetic freeze-out have occurred. These hadronic products now enter the detector volume and those with trajectories that overlap the detector acceptance will be detected (with some known efficiency) and their momentum, position, and identification can be used (in combination with similar information from all detected particles) to make inferences about the nature of the matter created in Stage III.

The chemical and kinetic freeze-out discussed in the description of Fig. I.2, are more clearly illustrated in Fig. I.3, an illustration of the space-time evolution of a collision. In the figure, the color gradient from red to blue indicates a cooling of the system as it expands.

I.3.2. Centrality and Impact Parameter

In Stage II of fig. I.2, the collision between the contracted nuclei is illustrated. Experimentally, it is useful to have a general idea of the collision geometry; i.e. to know if the incoming nuclei were exactly aligned and experienced a full head-on collision (central collision) where all of the nucleons in both ions participated in the collision, or (at the other extreme) if only a small fraction of the ionic surface areas align and therefore only few nucleons participate in the collision (peripheral collision). As hinted at in the description of the problem, one possible way to estimate this

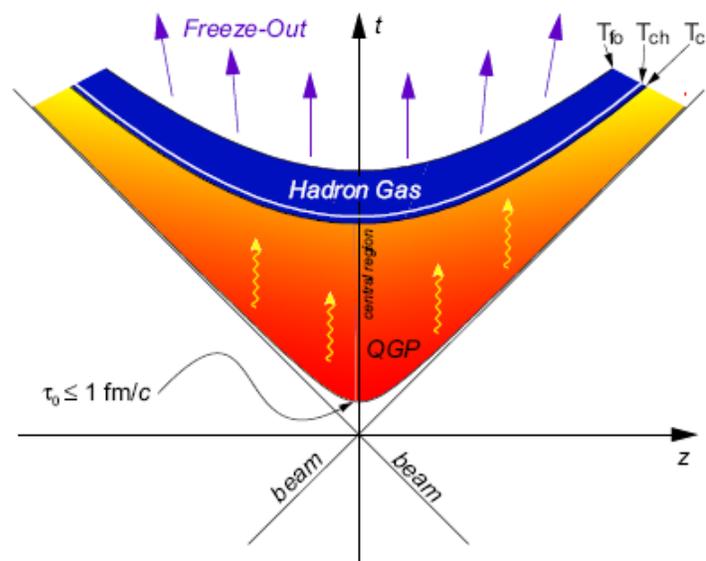


Fig. I.3.: The space-time evolution of relativistic heavy ion collisions[5]. T_c is the critical transition, T_{ch} is the chemical freeze-out point, and T_{fo} indicates kinetic freeze-out.

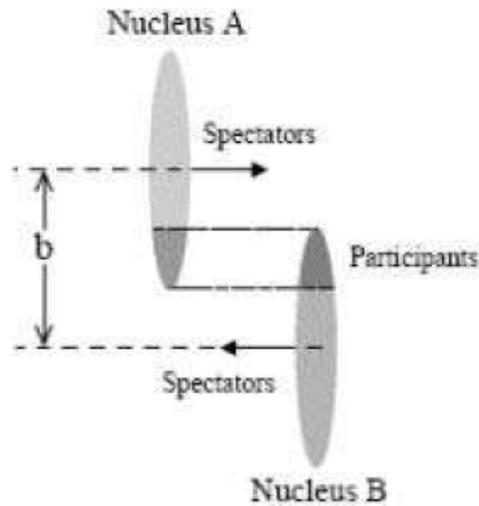


Fig. I.4.: Figure illustrating the impact parameter of two colliding nuclei. Nucleons that participate in the collision are called participants, those that do not are called spectators.

collision geometry (what is commonly referred to as the centrality of the collision) is to quantify the number of non-interacting nucleons after every collision. Indeed this is done in many experiments (including STAR as described in the next chapter) to obtain a rough online estimate of centrality for triggering purposes. However, a more accurate offline estimate is needed for analysis purposes. Before discussing the experimental estimate of centrality, a more formal definition of the problem is needed.

Figure I.4 is an illustration of two Lorentz-contracted nuclei, nucleus A and nucleus B, just before collision. The distance from the center of nucleus A to that of nucleus B is called the *impact parameter*, b . The greater the overlap (i.e. the more central the collision is) the smaller the distance from center-to-center and hence the smaller the impact parameter. The nucleons participating in the collision are called the participants, those that do not are called the spectators.

Although b exists and corresponds to centrality, it is not directly observable experimentally, this is because (as mentioned) Stage II is not accessible experimentally. Each experiment determines centrality differently, in STAR, charged particle reference multiplicity at mid-rapidity ($|\Delta\eta| < 0.5$) is used along with Monte-Carlo simulation based on the Glauber Model[36] to divide the set of events into multiple subsets of different centrality classes. For example the data presented in this work are all in the subset of the 0 - 10% most central events.

I.3.2.1. Elliptic Flow

In non-central collisions (collisions where there is only a partial overlap of the two nuclei) the overlap region is asymmetric in the plane perpendicular to beam direction (the transverse plane); this is illustrated in fig. I.5. This spatial anisotropy creates directional pressure gradients that creates a experimentally observable momentum-space anisotropy. A cartoon of this anisotropy relative to the reaction plane is shown in fig. I.6; this anisotropy can be well described mathematically using a Fourier expansion:

$$\frac{d^3N}{p_T dp_T dy d\phi} = \frac{d^2N}{p_T dp_T dy} \left[1 + 2 \sum_{\alpha} v_{\alpha} \cos(\alpha[\phi - \Psi_{RP}]) \right] \quad (1.1)$$

where p_T , y , and ϕ are the transverse momentum, the rapidity, and the azimuthal angle and v_{α} are the harmonic coefficients. One harmonic co-efficient in particular, v_2 , dominates the sum; it is referred to as *elliptic flow*.

Elliptic flow measured with the relativistic heavy ion collider (RHIC) is on average $\sim 70\%$ higher than flow measured at SPS energies. Indeed, the hydrodynamic models fit the data if and only if the initial equation of state condition reflects a transition to a QGP (rather than pure hadronic degrees of freedom)[8].

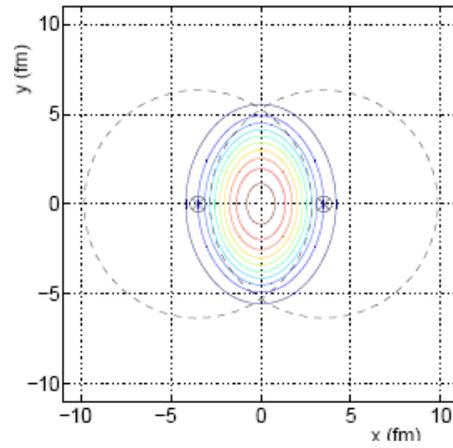


Fig. I.5.: Diagram of a non-central collision (beam-axis perspective) with the hydrodynamic density contours in the elliptical overlap region.[6].

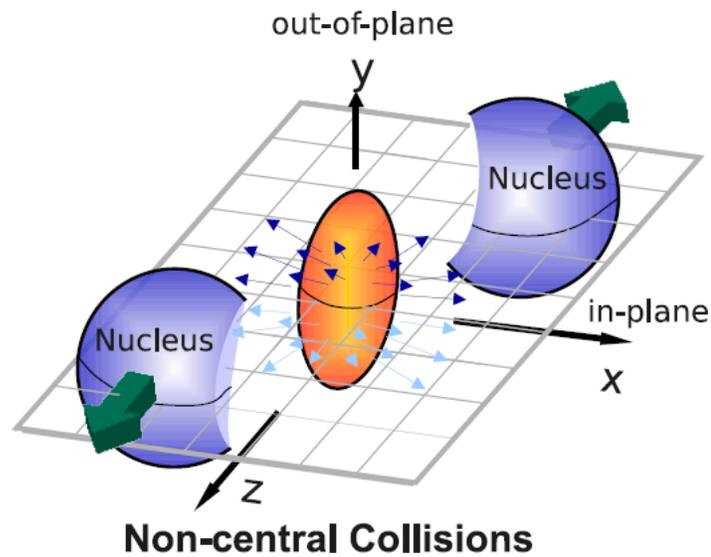


Fig. I.6.: Illustration of the non-central overlap region; spatial anisotropy is being transferred to a momentum-space anisotropy (indicated by the arrows showing particle emission under the influence of a pressure gradient)[7].

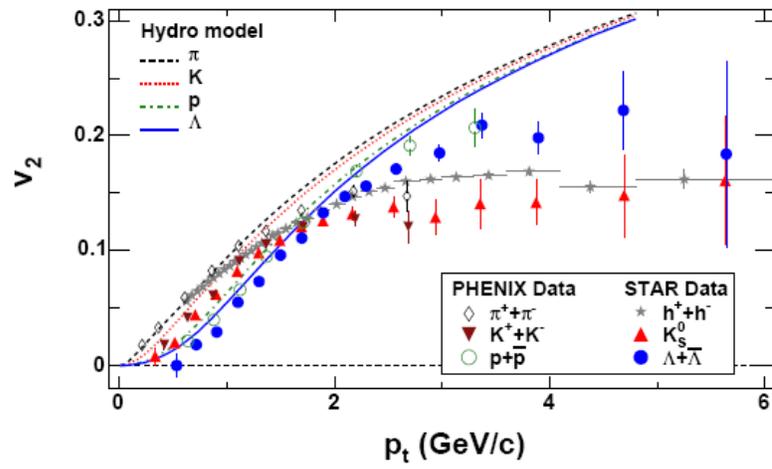


Fig. I.7.: v_2 (elliptic flow) as a function of p_T for identified pions, kaons, protons and lambdas in minimum-biased Au+Au collisions measured with the STAR and PHENIX detectors at RHIC[8]. The hydrodynamic model fits (which assume QGP formation) are overlaid.

I.4. Jets and Jet Quenching

Hard scatterings ('hard' refers to processes with large momentum transfer) are rare processes that are of great interest experimentally, because they occur early in the collision (Stage II, as discussed in Sec. I.3.1) and experience the full collision dynamics, serving as probes of the medium formed. Hard-scattered partons lead to the formation of di-jets and γ -jets, which can be used as probes experimentally.. This section starts with a discussion of jet formation (including γ -Jets and the Ridge) and two-particle correlations, then discusses the phenomenon of Jet quenching.

When two partons undergo a hard scattering, conservation of momentum causes the partons to be separated by $\sim 180^\circ$ in azimuth. This angular separation is essentially maintained in hadrons produced during fragmentation of these partons (which are emitted in narrow cones centered around the trajectory of the parent parton). This creates two back-to-back streams of hadrons called *Jets*. This process of Jet formation is illustrated, for a $p + p$ collision, in fig. I.8. The process of hadronization is well described by fragmentation functions, which represent the probability that a parton fragments into a specified hadron.

In proton-proton collisions, this di-Jet structure is easy to identify, because the partons fragment without traversing a medium. An example of an actual STAR $p + p$ event is shown in Fig. I.9, visually (and analytically) each charged-particle track in the TPC can be resolved and their origin traced back to the interaction point. The relative ease of Jet reconstruction in $p + p$ (and d+Au) means that Jets have been well-studied in these collision systems. Their modification in heavy ion collisions can therefore be quantified, relative to the 'pure' $p + p$ Jet.

In heavy ion collisions, Jets are not produced in a vacuum, but rather are part of a larger set of produced particles that constitute the dense medium associated

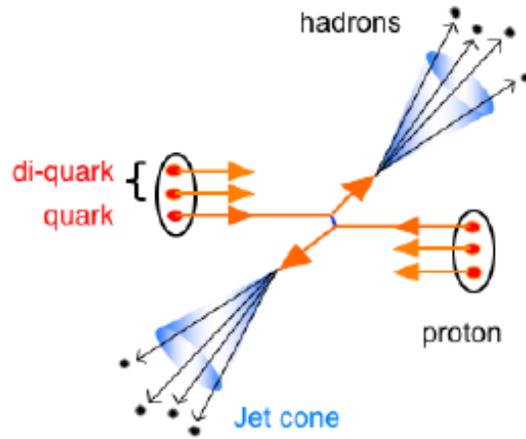


Fig. I.8.: An illustration of a $p + p$ hard-scattering event that produces a di-Jet

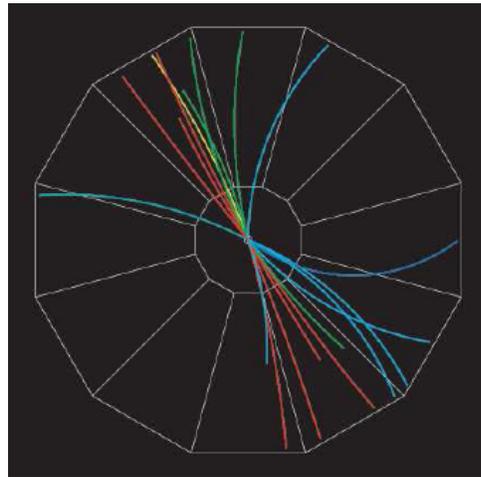


Fig. I.9.: An actual STAR $p + p$ event, clearly showing the di-Jet structure.

with these collisions. Jet reconstruction is therefore difficult in these collisions, and is replaced by a particle correlation analysis. In a correlation analysis, a high p_T particle (the *trigger*) is associated with all other (charged) particles (in some p_T range) in that event by constructing an angular correlation function $1/(N_{trig}.dN/d\Delta\phi)$. Here, N_{trig} denotes the number of trigger particles selected, so that the correlation function represents a statistical measure of jet-particle yields.. The particles correlated at small angular separation (close to zero) from the selected trigger are said to comprise the *near-side* Jet; particles correlated $\sim 180^\circ$ from the near-side Jet, are said to comprise the *away-side* Jet. Examples of $p + p$ and d+Au two-particle correlations are shown in fig. I.10 (a).

The first Jet correlation studies published by STAR were charged-particle correlation analyses, where charged triggers were combined with charged associated particles. These correlations attempt to probe di-Jets. However, also of interest are those hard-scatterings that produce a direct photon angularly correlated with a single Jet; since these photons do not interact via the strong force, they are expected to be unmodified by the QGP medium created at RHIC. Measurements of these special γ -jet events, were therefore expected to provide an internal standard by which to compare the modification of the hadronic away-size jet. STAR has published results from γ -Jets[37] produced in heavy ion collisions.

Correlations described thus far, have all looked at one-dimensional angular separation; STAR has also explored[10] correlations of particles in η as well as ϕ . For correlations in d+Au (fig. I.11) this added dimension produces no interesting additional information about jet production, it shows the near-side as a relatively narrow cone, and the away-side more broad. In Au+Au collisions however (fig. I.12), a new structure is observed; in addition to the near-side Jet peak, there is a broad near-side $\Delta\eta$ structure. This structure was called the *Ridge* because of its resemblance to a

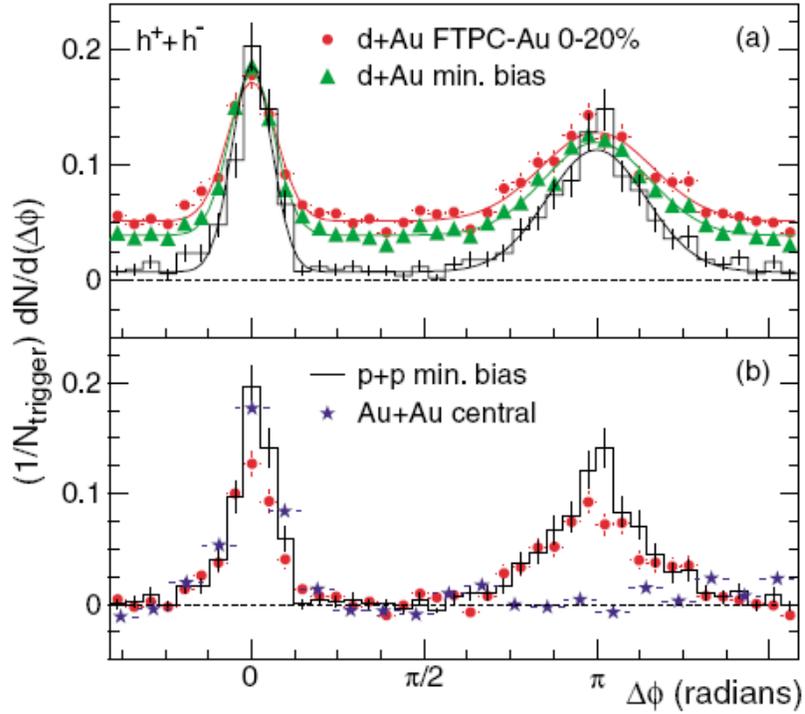


Fig. I.10.: $p+p$, d+Au, and Au+Au di-hadron correlations at $200 \text{ GeV}/c$. With $4.0 < p_T^{\text{trig.}} < 6.0 \text{ GeV}/c$ and $2.0 < p_T^{\text{assoc.}} < 4.0 \text{ GeV}/c$ [9] (a) Correlations for $p+p$, minimum-biased d+Au and central d+Au collisions with no background subtraction and (b) Correlations for $p+p$, d+Au and central Au+Au after background subtraction. Notice the quenching of the away-side Jet in the Au+Au data.

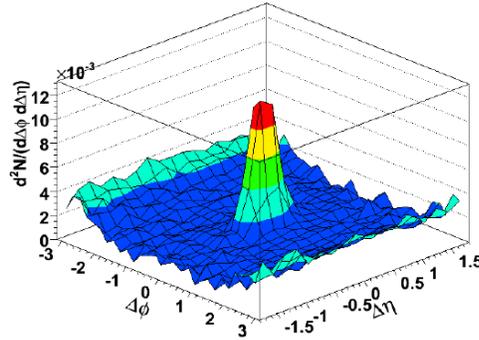


Fig. I.11.: d+Au long-range rapidity correlation. With $4.0 < p_T^{trig.} < 6.0 \text{ GeV}/c$ and $2.0 < p_T^{assoc.} < 4.0 \text{ GeV}/c$ [10].

mountain ridge. Early results from these long-range rapidity correlations have indicated that while the Jet yield increases as a function of $p_T^{trig.}$ the ridge yield remains constant[10].

As alluded to before, jets are expected to be modified in Au+Au collisions relative to $p+p$ or d+Au collisions, because of another interesting RHIC result: high p_T hadron suppression. If Au+Au were just a scaled-up version of $p + p$ collisions, i.e. if there were no phenomena unique to heavy ion collisions, the ratio of the hadron yields in heavy-ion compared to $p + p$ should reach unity (after scaling by N_{bin} , the number of binary collisions) at high p_T ; this ratio has been defined[11] as R_{AA} the *Nuclear Modification Factor*:

$$R_{AA} = \frac{d^2 N_{AA}/dP_T d\eta}{T_{AA} d^2 \sigma^{pp}/dP_T d\eta} \quad (1.2)$$

In Fig. I.13 R_{AA} as a function of p_T is shown for d+Au, peripheral Au+Au and central Au+Au collisions. At high p_T the R_{AA} for d+Au and peripheral Au+Au is unity (within the errors), suggesting (as previously discussed) that in cases where

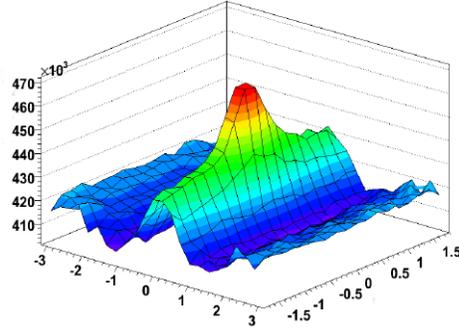


Fig. I.12.: Au+Au long-range rapidity correlation. With $4.0 < p_T^{trig.} < 6.0 \text{ GeV}/c$ and $2.0 < p_T^{assoc.} < 4.0 \text{ GeV}/c$ [10]. Notice the pronounced structure in $\Delta\eta$; this is referred to as the Ridge.

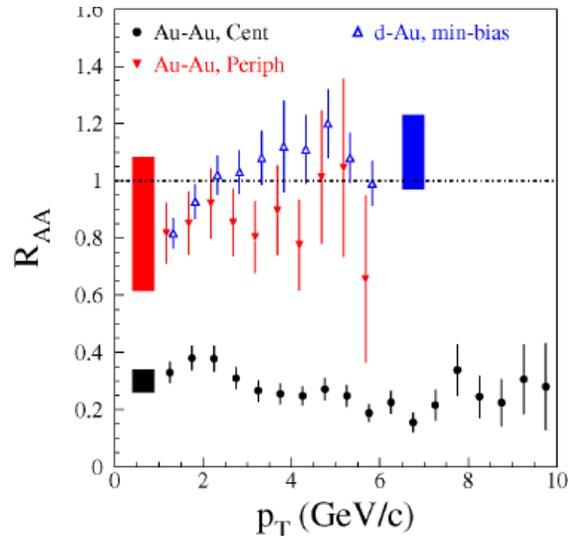


Fig. I.13.: R_{AA} as a function of p_T for d+Au, peripheral Au+Au and central Au+Au collisions[11].

one does not expect the QGP to form, there is little modification in hadronic yield compared to $p + p$ collisions[11]. However, in the central Au+Au data, there is a clear *suppression* of the hadronic yield[11]. This suppression is the explanation for another interesting RHIC result: the disappearance of the away-side Jet. In fig. I.10 (b) $p + p$, d+Au, and Au+Au two-particle correlations are plot; the $p + p$ and d+Au correlations are very similar on the near and the away-side, however, the Au+Au away-side is consistent with zero and we say that that Jet has been *quenched*. A detailed, quantitative understanding on jet quenching will allow for a better understanding of the nature of this new phase of matter created at RHIC. A powerful tool for doing so is the one-dimensional and two-dimensional two-particle correlation.

CHAPTER II

INTRODUCTION II: THEORETICAL MODELS OF RIDGE FORMATION

II.1. Overview of the Theoretical Models

The ridge phenomenon is a relatively recent experimental observation[10], our early understanding of its features was shaped by a measurement of the ridge yield in Au+Au collisions in a limited trigger p_T range. Based on this measurement, the ridge was assumed to be a $\Delta\eta$ feature of heavy-ion collisions with a yield essentially independent of trigger p_T . Most early theoretical calculations attempting to explain the existence of the ridge were largely based on these assumptions. However, recent CMS measurements[26][27] (and the results presented in this work), suggest these assumptions are not correct; as the ridge has been observed in $p + p$ collisions, and appears to decrease with increasing trigger p_T at very high p_T . Given the incomplete state of our experimental knowledge of the ridge, it is understandable that many early theoretical models will fall short in convincingly explaining the origin of these preliminary experimental observations. In this chapter, some of the most popular, early theoretical calculations are discussed (as well as a more recent one[20]); they can be categorized into three main categories, 1) those based on medium-induced gluon radiation[12][13][14]; 2) interaction of the jet with the medium[15][16]; or 3) transverse radial flow[17][18][38]. There is also a discussion of the concept of triangularity and triangular flow[19], which is an emerging theoretical concept that awaits further development by its proponents. There are numerous problems with the core assumptions or the methodology of all the theories presented in this chapter. For example, the calculations based on gluon radiation are unable to fully account for the extent of the pseudorapidity broadening; the calculations based on the jet-medium interaction

match the data, but do so as a result of numerous fits to the data; and the transverse radial flow calculation are unable to reproduce the experimentally observed features of the ridge, and are based on problematic assumptions that restrict their ability to explain general features of the data.

II.2. Medium-Induced Gluon Radiation

II.2.1. Gluon Radiation due to Collective Flow

The collective flow theory assumes that the ridge formation is due to radiated gluons that are broadened in pseudorapidity, and that this broadening does not only depend on the energy density of the medium, but also on the collective flow. The warrant for this assertion is the fact that high- p_T partons are not produced in an isotropic rest frame, i.e., a rest frame in which there is isotropic momentum transfer from the medium in the transverse (with respect to the direction of propagation) plane, but in an environment where they interact with a medium that shows strong transverse collective flow[12]. This difference is illustrated in Fig. II.1.

The contour plot in Fig. II.1 (lower part) show two significant medium-induced deviations. The first deviation is the observed broadening of the jet structure; this broadening is due to the Brownian motion (induced by the medium) of the partonic jet fragments. The second deviation is a significant rotational asymmetry (in the $\eta - \phi$ plane) in the jet shape; this asymmetry is a characteristic effect of collective flow. This second deviation is hard to verify experimentally, because the asymmetry is broken (in random directions in the $\eta - \phi$ plane) because of multiplicity fluctuations.

The difference in rapidity between the jet and the part of the medium that the jet passes through, determines the magnitude of the (collective flow induced) jet asymmetries. Plotting the asymmetries as a function of rapidity, R , should therefore

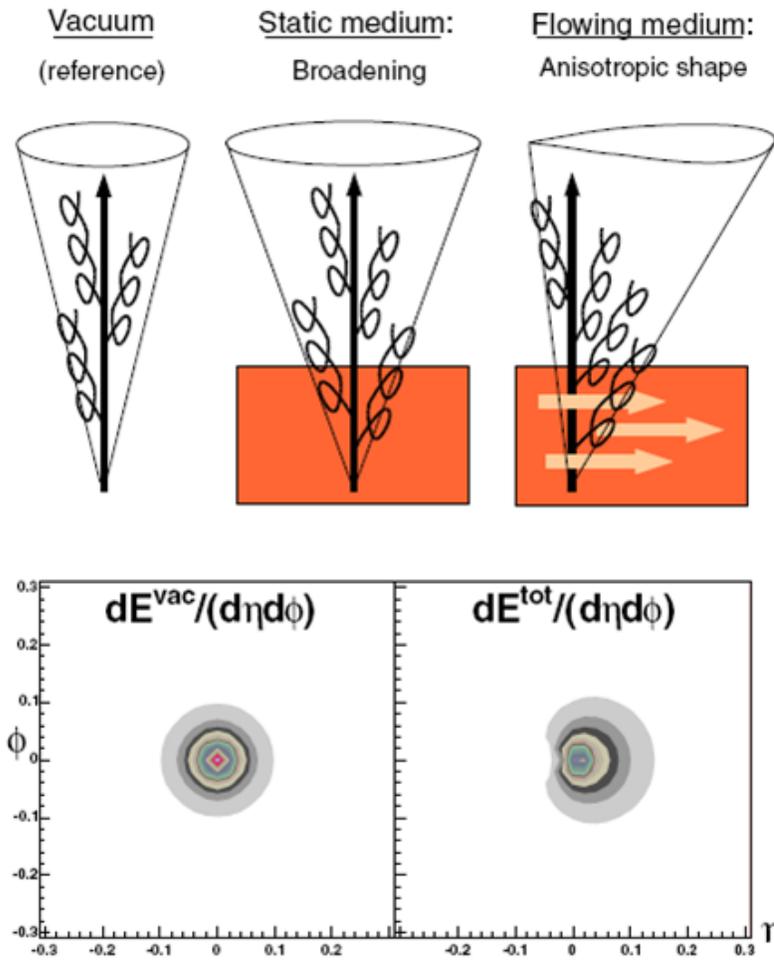


Fig. II.1.: Distortion of jet energy distributions. The upper part show a sketch of this distortion, and the lower part shows the calculated distortion in the $\eta - \phi$ plane for a $100 \text{ GeV}/c$ jet[12].

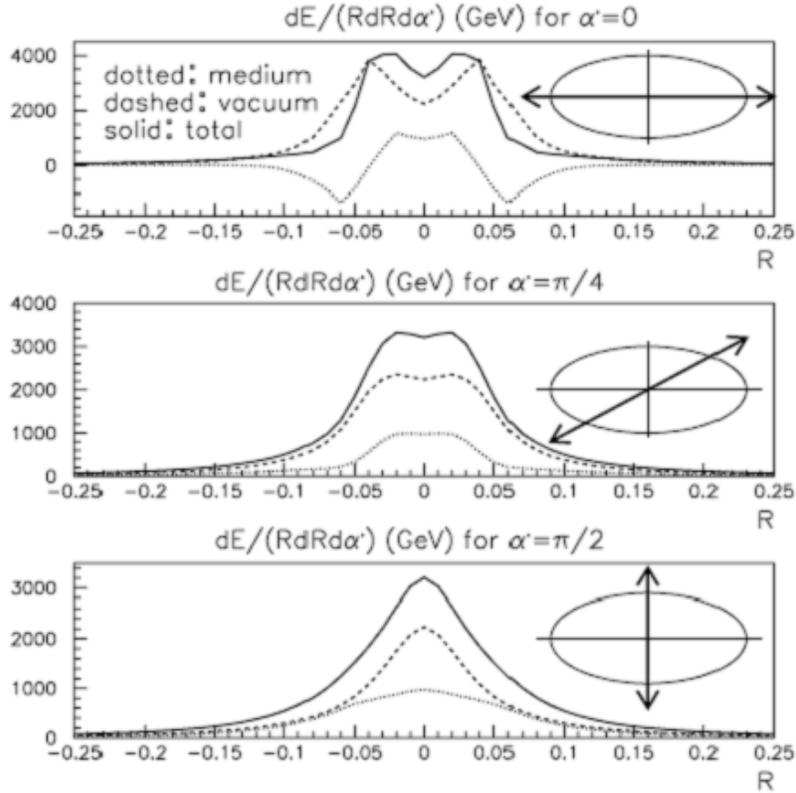


Fig. II.2.: Jet asymmetries as a function of rapidity for jets symmetric in pseudorapidity[12]. Vacuum and medium contributions (and their sum) are denoted by the different curves (as indicated in the figure).

provide a better understanding of the experimentally observed pseudorapidity broadening. Figure II.2 shows such a plot, of jet asymmetry vs. rapidity for jets centered at mid-rapidity, and that are symmetric across negative and positive pseudorapidity. The double-humped structure observed in the plotted distributions is of qualitative interest, because it supports that the author's[12] claims that the asymmetry of the jet energy distribution can be quantitatively inferred from measuring its rapidity width. However, large uncertainties in the calculations prohibit a more quantitative assessment of this jet width.

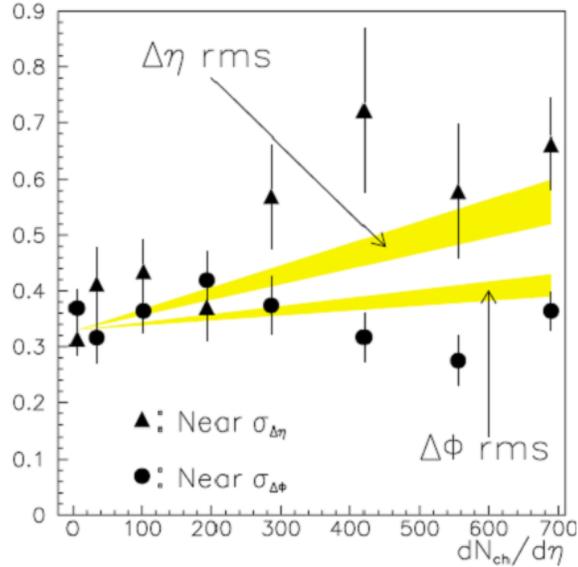


Fig. II.3.: Near-side $\Delta\eta$ and $\Delta\phi$ widths of unidentified charged hadrons with $4.0 < p_T^{trig.} < 6.0 \text{ GeV}/c$ and $2.0 < p_T^{assoc.} < 4.0 \text{ GeV}/c$ from [10] plotted with theoretical bands from [12].

The jet asymmetries that are described in Fig. II.2 are still present in the particle correlation distributions, as illustrated in Fig. II.3. This figure shows the STAR near-side $\Delta\eta$ and $\Delta\phi$ widths from [10], plot on top of the calculations from [12]; the STAR data show a significant broadening of the $\Delta\eta$ widths, the calculations also describe a broadening, but with a smaller magnitude than the data. This suggest that while this theory hints at the existence of a broadening in pseudorapidity, it is unable to fully describe the extent to which this is experimentally the case; i.e. it cannot account for the existence of the ridge.

II.2.2. Gluon Radiation due to Turbulent Color Fields

The longitudinal broadening by turbulent color fields theory, claims that the near-side jet broadening is due to a final state effect; the deflection of radiated gluons by a soft, transverse, turbulent color field; which is formed under the influence of the instabilities in the QCD plasma. A description of this theory can be found in [13], the authors (Majumder et al.) assume that the ridge is composed of hadrons that are produced in the fragmentation of radiated gluons (before or after these gluons are absorbed by the medium); therefore, they believe that the ridge shape will be determined by the final (after medium traversal) kinematic distribution of the radiated gluons. The authors also highlight the fact that no quantitative explanation of the ridge shape had thus far been provided by other theorists (namely Armesto[12] (see Sec. II.2.1), and Hwa[16] (see Sec. II.3.2)) who have proposed longitudinal expansion as the cause of the ridge. Furthermore, Majumder et al. argues that Romatschke's[14] (Sec. II.2.3) proposal that the ridge can be explained by the fact that the momentum of a transversely propagating heavy-quark is broadened by the elastic collisions in the expanding medium preferentially in the longitudinal direction; is likely not correct, as the ridge is composed mostly of light quarks.

The authors approach is based on work[39][40][41] that show that in an expanding medium, color fields are formed under the influence of the instabilities in the plasma, and can be described conceptually as follows: A transversely (with respect to the beam direction) scattered hard parton will radiate soft gluons which are then deflected by the turbulent color field. Since the instabilities in the plasma are not random, the deflection pattern is not isotropic with respect to the jet axis, but rather are deflected (preferentially) in the transverse direction. This expansion then results in a final particle distribution that features an elongated structure along the beam axis; the

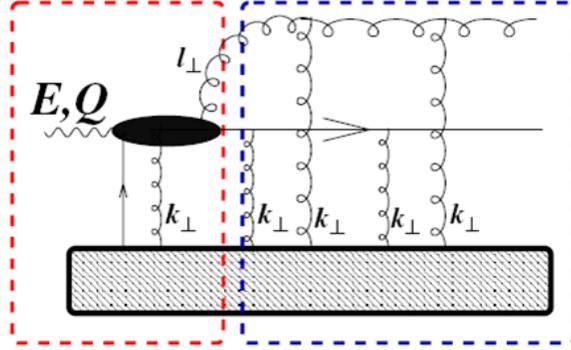


Fig. II.4.: Illustration of the Gluon Radiation due to Turbulent Color Fields theory; multiple soft rescatterings preceded by a hard scatterings[13].

ridge.

Figure II.4 is an illustration of the process of gluon radiation proposed by Majumder et al. The dark ellipse represents the distance over which the produced parton undergoes multiple scatterings in-medium, then emits a hard gluon, this includes the hard-hard and hard-soft double scattering processes. The in-medium soft scattering of the gluon and parent parton that follows are described as being independent of the processes described by the dark ellipse (the production and radiation). The rectangular boxes in the figure represent the factorization.

The authors calculate the gluon distribution (before broadening) by taking the ratio of the cross-section σ_{gg} for radiating a gluon with momentum $(p_{T_2}, \mathbf{l}_\perp)$ (left-hand rectangle in Fig. II.4) and the quark (with momentum p_{T_1} and rapidity y) production inclusive cross-section σ_q . The distribution is given by Eq. 2.1:

$$\frac{d^2\sigma_{gg}(p_{T_2}, \mathbf{l}_\perp)}{d\sigma_q} = C(p_{T_1}, p_{T_2}) \frac{\alpha_s}{2\pi} \frac{1}{l_\perp^4} \times \int_0^{\zeta_{max}(\mathbf{r})} d\zeta p(\mathbf{r} + \hat{n}\zeta) \frac{\zeta_0}{\zeta} \times [2 - 2\cos(\eta_L\zeta)]. \quad (2.1)$$

- \hat{n} – Jet axis.

- ζ – Distance traveled by the produced partons from the primary vertex along \hat{n} .
- ζ_{max} – Maximum allowed value for ζ ; the distance from \mathbf{r} to the surface.
- $\eta_L = l_{\perp}^2/(2p_{T_2}z_1)$ the inverse formation time of a gluon with momentum l_{\perp} transverse to \hat{n} .
- $C(p_{T_1}, p_{T_2})$ – A constant that accounts for the fact that the final parton momentum in the numerator and denominator of the equation are different.

The results of the calculation are shown in Fig. II.4, where the dotted and dashed lines show the output from Eq. 2.1; and the solid lines show the distribution at the moment that the gluon leaves the medium. The figure shows a broadening of the gluon distribution in the η but not in ϕ . However, two important points must be noted; first, these calculations assume an ideal, ultra-relativistic liquid to calculate the soft gluon density; and second, although the results show some broadening it (like the other theoretical description of the ridge based on gluon radiation) is not sufficient to account for the shape and extent of the the ridge as observed experimentally.

II.2.3. Longitudinal Momentum Broadening in an Anisotropic QGP

A large number of relativistic heavy ion theoretical calculations (including all the theoretical calculations discussed in this chapter) assume a thermalized and homogeneous QGP. Romatschke's theoretical calculation[14] is different, in that it seeks to explain the existence of the ridge by assuming a homogeneous but locally anisotropic system. The calculation, like the work by Moore and Teaney[42] on which it is based, focuses on a heavy-quark with momentum p , moving in a thermal medium with a

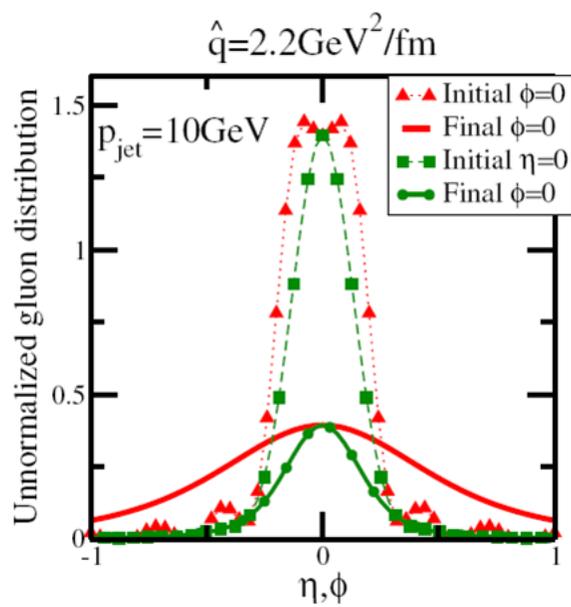


Fig. II.5.: Gluon distribution in η and ϕ for a total jet momentum of $10 \text{ GeV}/c$ [13].

Final item on legend is presumably an error and should read $\eta = 0$.

temperature T , and with a broadened momentum distribution described by Eqs. 2.3 from [42].

$$\begin{aligned}
\frac{d}{dt}\langle p \rangle &= -p\eta_D(p) \\
\frac{d}{dt}\langle (\Delta p_{\parallel})^2 \rangle &= \kappa_{\parallel}(p) \\
\frac{d}{dt}\langle (\Delta p_{\perp})^2 \rangle &= \kappa_{\perp}(p) \\
\frac{d}{dt}\langle (\Delta p_z)^2 \rangle &= \kappa_z(p)
\end{aligned} \tag{2.2}$$

The kinetic theory based functions η_D , κ_{\parallel} , κ_{\perp} , and κ_z describe the momentum loss as well as fluctuations (transverse and longitudinal). They are given as Eqs. 2.3.

$$\begin{aligned}
\frac{d}{dt}\langle p \rangle &= \frac{1}{2v} \int_{k,q} |\mathcal{M}|^2 q^0 \{f(k)[1 \pm f(k - q^0)] - f(k - q^0)[1 \pm f(k)]\} \\
\frac{d}{dt}\langle (\Delta p_{\parallel})^2 \rangle &= \int_{k,q} |\mathcal{M}|^2 q_{\parallel}^2 f(k)[1 \pm f(k - q^0)] \\
\frac{d}{dt}\langle (\Delta p_{\perp})^2 \rangle &= \int_{k,q} |\mathcal{M}|^2 q_{\perp}^2 f(k)[1 \pm f(k - q^0)] \\
\frac{d}{dt}\langle (\Delta p_z)^2 \rangle &= \int_{k,q} |\mathcal{M}|^2 q_z^2 f(k)[1 \pm f(k - q^0)]
\end{aligned} \tag{2.3}$$

- $v = p/p^0$
- $f(k)$ – Gluon (quark) distribution function.
- \mathcal{M} – Scattering matrix.
- $\int_k = \int d^3k/(2\pi)^3$

The coordinate system is shown in Fig. II.6, the heavy-quark moves in a direction that coincides with the anisotropic direction.

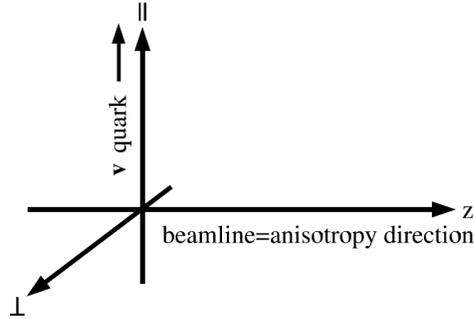


Fig. II.6.: An illustration of the coordinate system used in theoretical calculations of longitudinal broadening in an anisotropic QGP[14].

Particles move in all directions with equal probability in an isotropic system. In an anisotropic system however, this is not the case; there must be at least one preferred direction in the system, which in this theoretical calculation is conveniently chosen to be the z direction (along the beam axis). This is, of course, a problematic assumption as it first assumes that if the system is anisotropic, it has only one preferred direction, then assumes that that direction is the longitudinal one. The warrant for this assumption, is the spatial anisotropy that exists in collisions with a non-zero impact parameter. However, it must be noted that this anisotropy exists independently on the thermodynamic properties of the medium, and therefore it is doubtful whether this is a strong enough warrant for the assumption of a preferred direction in an anisotropic system.

The author concludes that for an anisotropic system k_z/k_\perp is always larger than 1 (to leading log accuracy). This means that a heavy-quark jet in an anisotropic QGP (that undergoes only collisional broadening) will preferentially experience longitudinal broadening. That ratio, k_z/k_\perp is interpreted by the author as approximating the ratio of the η and ϕ jet correlation width; $\langle\Delta\eta\rangle/\langle\Delta\phi\rangle$.

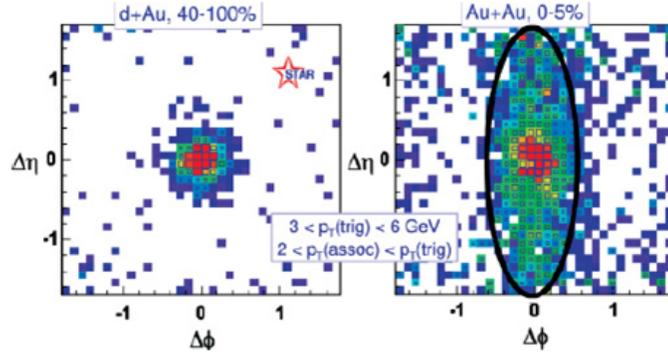


Fig. II.7.: d+Au 40 - 100% centrality (left) and Au+Au 0 - 5% centrality (right) $\Delta\eta$ and $\Delta\phi$ correlations, with theoretical calculations from [14] plot as the black ellipse on top of the Au+Au data.

The author's calculation with a k_z/k_\perp ratio of ~ 3 is plot (as the black ellipse) on top of STAR[43]. The ellipse quantitatively accounts for the $\Delta\eta$ broadening. It is not clear, however, the author's reasoning for choosing this particular value of the ratio (other than the fact that it well fits the data).

In general the theoretical calculation discussed in this section is interesting for the fact that it does not assume a thermalized system. However, the arguments in favor of longitudinal broadening, and the ability of the theory to reproduce the $\Delta\eta$ broadening (let alone the 3D shape of the ridge) are both very much in doubt. In addition the leading-order accuracy and the heavy-quark focus add further caveats to the conclusions of the calculations.

II.3. Interaction of the Jet with the Medium

II.3.1. The Momentum Kick Model and Ridge Structure

In the theoretical calculation by Wong [15], the momentum kick model is used to explain the ridge structure; the ridge particles are identified as medium particles that undergo collisions with the jet and experience a momentum kick along the jet direction. The theory is based on the following three assumptions about the ridge yield:

1. The yield is nearly independent of the flavor content of the associated particles.
2. The meson/hyperon nature of the associated particles.
3. The trigger particle p_T .

This last assumption has been questioned by recent CMS results[27] and by conclusion from this dissertation analysis (see Chapter VI).

The momentum kick model employed by Wong can be summarized conceptually as follows;

1. A near-side jet is produced near the surface of the medium and its constituent particles collide with medium partons as it makes its way to the detectors.
2. The momentum distribution of the collided medium partons is sampled at the moment of the jet-parton collision. Each collided parton undergoes at most one collision with the jet (because of the production near the surface requirement on the jet).
3. The collided parton experiences a momentum kick \mathbf{q} , from the jet-parton collision. The parton's initial momentum distribution $P_i(\mathbf{p}_i)$ is modified by the

momentum kick into its final momentum distribution $P_f(\mathbf{p}_f)$. These collided partons then hadronize (retaining the collided parton's final momentum distribution) and materialize as ridge particles.

The final momentum distribution of the collided partons is given by Eq. 2.4:

$$P_f(\mathbf{p}_f) = \int \frac{d\mathbf{p}_i}{E_i} \int d\mathbf{q} P_i(\mathbf{p}_i) E_f \sigma(\mathbf{p}_f - \mathbf{p}_i - \mathbf{q}). \quad (2.4)$$

The momentum kick distribution $P_q(\mathbf{q})$ can be normalized as described in Eq. 2.5;

$$\int d\mathbf{q} P_q(\mathbf{q}) = 1, \quad (2.5)$$

The numbers of collided partons before and after the jet-parton collision are conserved by the kinetic quantities E_i and E_f and are given by Eq. 2.6;

$$N_f = \int \frac{d\mathbf{p}_f}{E_f} P_f(\mathbf{p}_f) = \int \frac{d\mathbf{p}_i}{E_i} P_i(\mathbf{p}_i) = N_i. \quad (2.6)$$

The momentum kick $P_q(\mathbf{q})$, is not a quantity that can be obtained from first principles of QCD, and in the calculations described in Wong[15], the momentum kick is only generally explored; a single parameter \mathbf{q} is used to describe the momentum kick distribution, as shown in Eq. 2.7;

$$P_q(\mathbf{q}) = \sigma(\mathbf{q} - q\mathbf{e}_{jet}), \quad (2.7)$$

where $q = |\mathbf{q}| \geq 0$, and \mathbf{e}_{jet} is the unit vector along the jet direction. Thus, the distribution of partons undergoing a jet-parton collision is given (using Eq. 2.4) as Eq. 2.8:

$$P_f(\mathbf{p}_f) = \left[P_i(\mathbf{p}_i) \frac{E_f}{E_i} \right]_{\mathbf{p}_i = \mathbf{p}_f - q\mathbf{e}_{jet}} = \left[P_i(\mathbf{p}_i) \frac{\sqrt{m^2 + p_f^2}}{\sqrt{m^2 + p_i^2}} \right]_{\mathbf{p}_i = \mathbf{p}_f - q\mathbf{e}_{jet}} ; \quad (2.8)$$

The final pseudorapidity distribution of the particles is given as;

$$\frac{dN_f}{d\eta_f d\phi_f p_{tf} dp_{tf}} = \frac{dN_f}{dy_f d\phi_f p_{tf} dp_{tf}} \sqrt{1 - \frac{m^2}{m_{tf}^2 \cosh^2 y_f}}, \quad (2.9)$$

where m is the rest mass of the parton and $m_{tf} = \sqrt{m^2 + p_{tf}^2}$.

This calculation assumes parton-hadron duality, it identifies the momentum of the associated particles as the final momentum of the energetic partons after the jet-parton collisions.

Central to Wong's theoretical calculations, and one of its major criticisms, are the fits to the STAR data (from a private communication of G. Wang and H. Huang) that are used to reproduce its main features; specifically the following parameters were chosen from fits, $q = 0.8 GeV$, σ_y (the standard deviation of the Gaussian rapidity distribution) = 5.5, and $T = 0.47 GeV$. Fits to data are common in theoretical calculations, and do not necessarily make their conclusions less credible, however, the fits to data are problematic in this case; the ability of this calculation to describe the data varies greatly depending on the values chosen for the three parameters. For example, consider Fig. II.8, which show $\Delta\eta$ - $\Delta\phi$ calculated particle distributions with varying values for q (with the other two parameters constant) and varying values for σ_y (with the other parameters constant); changing the q value by a factor of 1/2

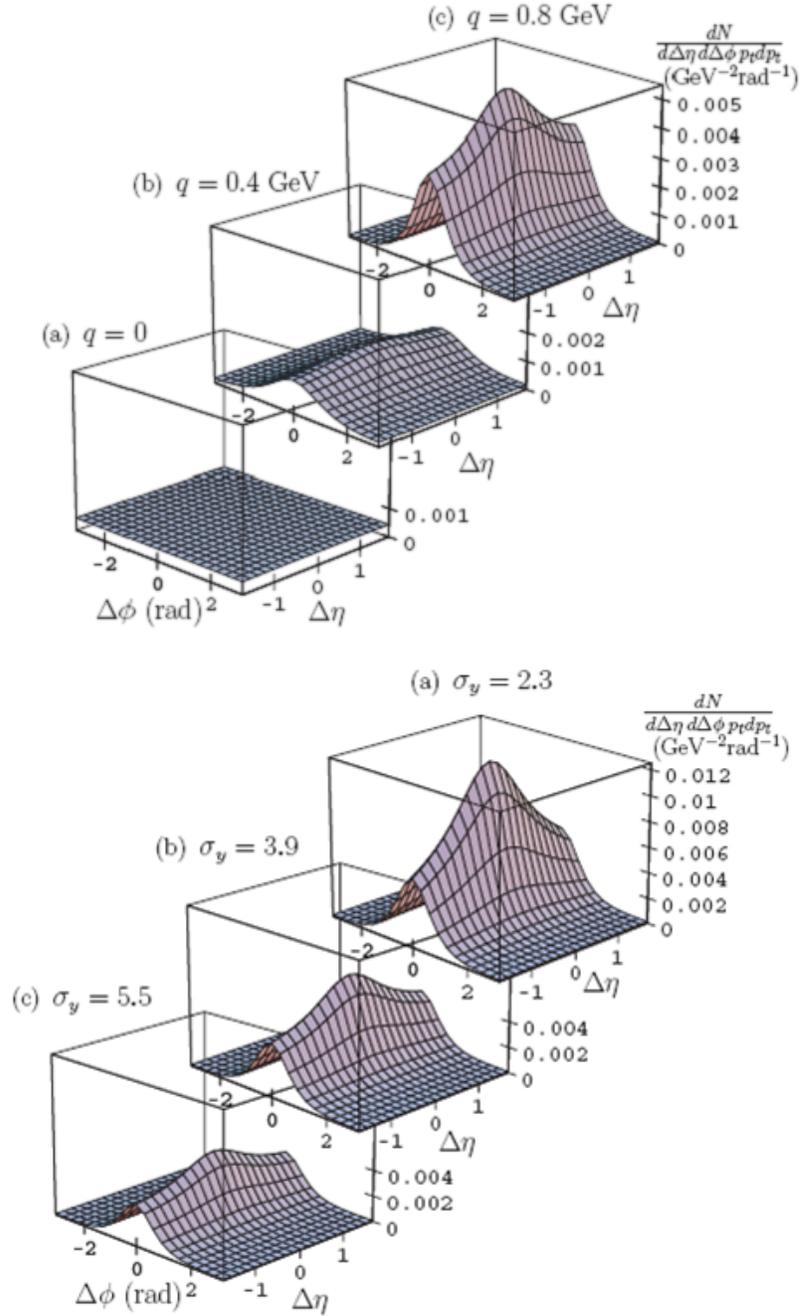


Fig. II.8.: Theoretical results of the momentum kick model, for the yield in $\Delta\eta - \Delta\phi$ of ridge particles. On top is the distribution varying the value of q while keeping the other two parameters constant, and on the bottom is the distribution varying the value of σ_y while keeping the other two parameters constant[15].

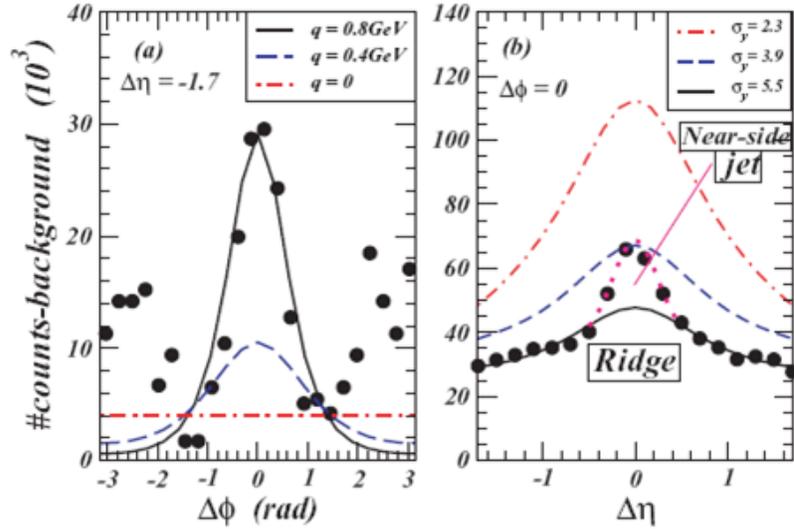


Fig. II.9.: $\Delta\eta$ and $\Delta\phi$ particle distributions fit with theoretical calculations using the momentum-kick model. The solid circles are STAR data, the solid curves are theoretical ridge particle yields for $p_T = 2\text{GeV}$, $q = 0.8\text{GeV}$, $\sigma_y = 5.5$, and $T = 0.47\text{GeV}$ (all fixed from fits to the data), which are normalized by matching to the data at $(\Delta\phi, \Delta\eta) = (0, -1.7)$. The dashed and dotted curves are the momentum theoretical calculation results obtained by varying q (left plot) and σ_y (right plot)[15].

compared to the fixed value essentially flattens (not just the ridge structure, but) the entire particle distribution, while changing σ_y by a factor of 1/2 skews the ridge shape into a steep slope that departs from the shape observed in experimental data. The $\Delta\phi$ and $\Delta\eta$ projections of the particle are shown in Fig. II.9. In addition to the fits to extract the parameters, the theoretical calculations are further matched to the data by normalizing them at $(\Delta\phi, \Delta\eta) = (0, -1.7)$ (as shown in the figure).

Another aspect of the model that cast doubts on the validity of its claims to describe the data, is its assumption that the initial rapidity distribution is Gaussian with a standard deviation of σ_y (which, as previously mentioned, is set by fits

to the STAR data). The real distribution, however, may be multi-centered or non-Gaussian; further theoretical justification of a Gaussian with a standard deviation of 5.5 is needed. The author further points out another issue with the momentum kick model as applied to low p_T partons: The calculation is based on the idealization of parton-hadron duality in which the momentum and energy losses caused by absorbing a sea quark (or anti-quark) and that of emitting a soft gluon are neglected[15]. However, these processes have a greater effect on low p_T parton and cannot be ignored; they must be accounted for before the momentum kick model can be accepted as a reasonable theoretical description of $\Delta\eta$ - $\Delta\phi$ particle distributions.

II.3.2. Medium Heating, Recombination, and Ridge Structure

The phenomenological calculations by Chiu and Hwa[16] introduces the parton recombination/Coalescence model[44][45] to the study of the 2D $\Delta\eta$ and $\Delta\phi$ jet structure (pedestal and peak structure), extending the work done by Fries et al.[46] from one dimension ($\Delta\phi$) to two. The paper claims that the ridge structure originates from the longitudinal expansion of thermal partons which are enhanced by the energy loss processes of hard partons as they traverse the medium. The calculated correlation depends only on the correlation among shower partons, and is affected (primarily in the intermediate- p_T range) by recombination between thermal and shower partons.

The main assumption of this calculation is that the shower partons in a jet, while they are dynamically independent, are kinematically constrained (please see [47] for a detailed exploration of the consequences of this assumption on the particle correlations). Another assumption made in [16] is that the shower partons have a Gaussian angular distribution (relative to the jet axis), which is the same in both $\Delta\eta$ and $\Delta\phi$. The two main parameters in this treatment are the width of the angular distribution in the jet cone, and the magnitude of the thermal enhancement: These

are both fixed by fits to the data.

The formalization of single and two-particle distributions in the recombination model framework is given by the following equations[44][45][48][47]:

$$\frac{dN_{\pi_1}}{p_1 dp_1} = \frac{1}{p_1^2} \int \frac{dq_1}{q_1} \frac{dq_2}{q_2} F_2(q_1, q_2) R_{\pi_1}(q_1, q_2, p_1), \quad (2.10)$$

$$\frac{dN_{\pi_1 \pi_2}}{p_1 p_2 dp_1 dp_2} = \frac{1}{p_1^2 p_2^2} \int \left(\prod_{j=1}^4 \frac{dq_j}{q_j} \right) F_4(q_1, q_2, q_3, q_4) \times R_{\pi_1}(q_1, q_3, p_1) R_{\pi_2}(q_2, q_4, p_2), \quad (2.11)$$

the recombination function for a pion is[49]

$$R_{\pi}(q_1, q_2, p) = \frac{q_1 q_2}{p^2} \delta \left(\frac{q_1}{p} + \frac{q_2}{p} - 1 \right). \quad (2.12)$$

F_2 and F_4 (the two- and four-parton distributions) can be written as

$$F_2(1, 2) = (\mathcal{T}\mathcal{T} + \mathcal{T}\mathcal{S} + \mathcal{S}\mathcal{S})_{12}, \quad (2.13)$$

$$F_4(1, 2, 3, 4) = (\mathcal{T}\mathcal{T} + \mathcal{T}\mathcal{S} + \mathcal{S}\mathcal{S})_{13} (\mathcal{T}\mathcal{T} + \mathcal{T}\mathcal{S} + \mathcal{S}\mathcal{S})_{24}. \quad (2.14)$$

The thermal parton distribution is given as

$$\mathcal{T}(q) = C q e^{-q/T}, \quad (2.15)$$

and the shower partons in a jet have the form

$$\mathcal{S}(q) = \xi \sum_i \int dk k f_i(k) \mathcal{S}_i^j(q/k), \quad (2.16)$$

where $f_i(k)$ is the distribution of hard parton i in a heavy-ion collision and ξ is the average fraction of hard partons that emerge from the thermal medium to hadronize.

For two shower partons (\mathcal{SS}), their joint distribution is

$$(\mathcal{SS})(q_1, q_2) = \xi \sum_i \int dk k f_i(k) \left\{ \mathcal{S}_i^j\left(\frac{q_1}{k}\right), \mathcal{S}_i^{j'}\left(\frac{q_2}{k - q_1}\right) \right\}, \quad (2.17)$$

where the quantity of the curly braces has the form;

$$\left\{ \mathcal{S}_i^j(x_1), \mathcal{S}_i^{j'}\left(\frac{x_2}{1 - x_1}\right) \right\} = \frac{1}{2} \left[\mathcal{S}_i^j(x_1) \mathcal{S}_i^{j'}\left(\frac{x_2}{1 - x_1}\right) + \mathcal{S}_i^{j'}\left(\frac{x_1}{1 - x_2}\right) \mathcal{S}_i^j(x_2) \right]. \quad (2.18)$$

These equations can then be used (as described in [16]) to extend this formulation to $\Delta\eta$, which results in the following distribution equation;

$$\begin{aligned} \frac{dN_{\pi^+\pi^-}^{TSTS}}{p_1 dp_1 d\eta_1 d\phi_1 p_2 dp_2 d\eta_2 d\phi_2} &= \frac{1}{(p_1 p_2)^3} \xi \sum_i \int dk k f_i(k) \int dq_1 \int dq_2 \theta(k - q_1 - q_2) \\ &\quad \times \sum_{j,j'} \mathcal{T}(p_1 - q_1, \eta_1) \left\{ \mathcal{S}_i^j\left(\frac{q_1}{k}\right), \mathcal{S}_i^{j'}\left(\frac{q_2}{k - q_1}\right) \right\} \\ &\quad \times \mathcal{T}(p_2 - q_2, \eta) \mathcal{G}\left(\psi, \frac{q_2}{k}\right) \Big|_{\psi=2\tan^{-1}g(\eta, \eta_1)}, \end{aligned} \quad (2.19)$$

The authors conclude that the ridge is related to ΔT in the local distribution, and that it is a consequence of the recombination of the thermal and shower partons;

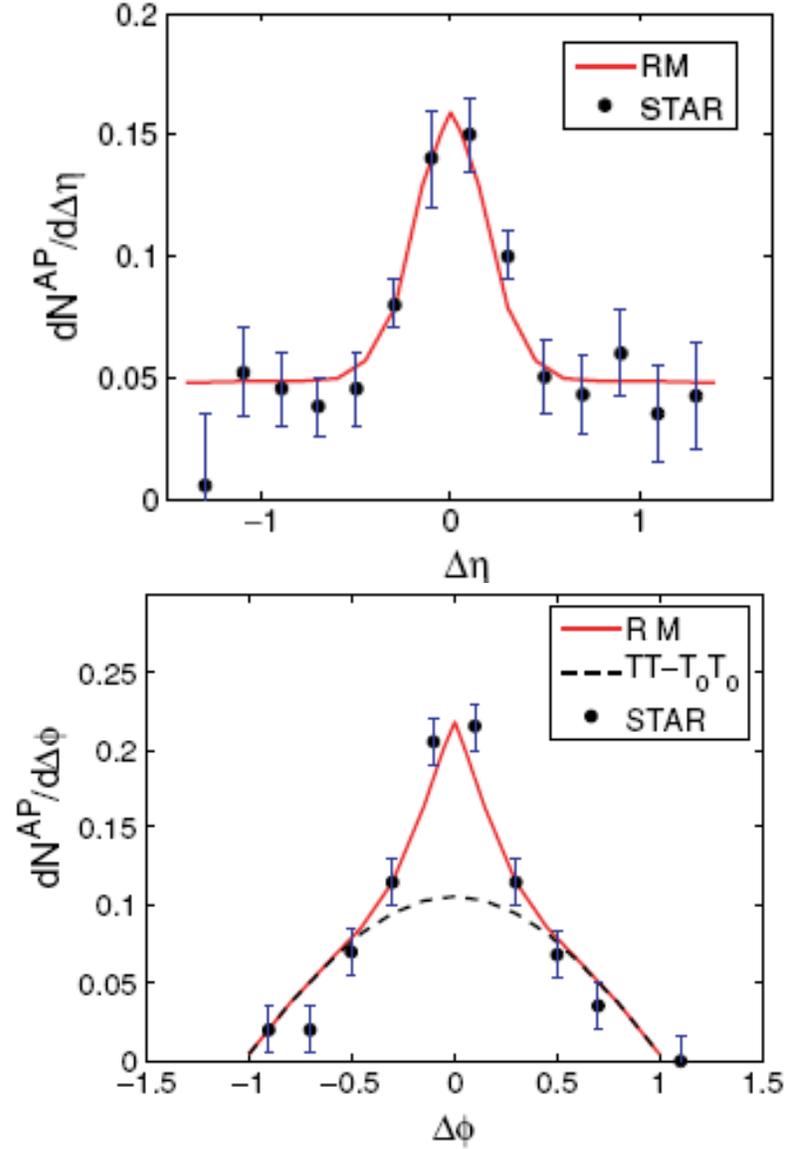


Fig. II.10.: STAR $\Delta\eta$ (left) and $\Delta\phi$ (right) data with normalized theoretical calculations from the recombination-based model of jet production[16]. With $4.0 < p_T^{trig.} < 6.0 \text{ GeV}/c$ and $2.0 < p_T^{assoc.} < 4.0 \text{ GeV}/c$. The solid lines are the calculations, and the dashed line in the right plot is the ridge-effect in $\Delta\phi$ that is forced to vanish by the ZYAM procedure (see Chapter V for details of this).

i.e. the ridge is not part of the jet, but is associated with jet production. Calculating only $\pi^+\pi^-$ production, the authors were able to reproduce the $\Delta\eta$ and $\Delta\phi$ particle distribution peaks (see Fig. II.10), however, like Wong's calculations in the previous section, the numerous fits to the data reduces the strength of the authors' claim to a theoretical understanding of the ridge. With regards to this data fitting, the authors make the following statement;

What we do here is to fix all the extra free parameters of the problem by the experimental features of the data. Since our aim is to reproduce the observed characteristics of the data which are presented with specific cuts, it is impossible to do so without incorporating those cuts. However, it does not imply that we are merely fitting the data... it is by no means trivial that the data can be fitted so well.[16].

A more recent quark coalescence study is the paper by L. Ravagli and R. Rapp[50], in which the authors present a reformation of quark coalescence models in heavy-ion collisions by calculating meson production via resonance formation in quark-antiquark scattering based on a transport equation. Their work explicitly includes energy conservation in the calculations and employs a well-defined thermal equilibrium limit.

II.4. Ridge Formation due to Transverse Radial Flow

In this section, transverse radial flow (and its proposed effects on particle correlations) is discussed, referencing three main works, papers by Voloshin[17], Shuryak[18] and Pruneau, Gavin and Voloshin[38].

In [17], Voloshin proposes that the interaction between partons produced in heavy-ion collisions, causes a buildup in the pressure of the system, leading to longitudinal and transverse expansion, with the transverse radial expansion resulting in

an increase in the particle final transverse momenta and characteristic rapidity and azimuthal two-particle correlation. These characteristic features in the correlation are explained by the reasoning that all particles produced in the same NN collision have the same initial transverse spatial position and get on average the same push which results in a correlation.

These calculations use a thermal model, in which particles are produced by freeze-out of the thermalized matter at a temperature T , which is approximated by a boosted Boltzman distribution. In the model, the following assumptions are made[17]:

1. Boost-invariant longitudinal expansion
2. Freeze-out at constant proper time
3. Uniform matter density
4. A power law transverse rapidity flow profile
5. During the expansion time (before freeze-out) the particles produced originally at the same spatial position, do not diffuse far from each other (compared to the system size)

The two-particle spectrum is given by the following expression[17];

$$\frac{dn_{pair}}{d\mathbf{p}_{t,1}d\mathbf{p}_{t,2}} \sim \int dp_t d\phi_b p_t^{2/n-1} J(\mathbf{p}_{t,1}; T, p_t \phi_b) J(\mathbf{p}_{t,2}; T, p_t \phi_b), \quad (2.20)$$

and the results of the calculation are shown in Fig. II.11 (as a function of $\langle p_t^2 \rangle = \langle p_t \rangle^2 (4n + 4) / (2 + n)^2$);

The calculations are compared to STAR data in Fig. II.12. The two-particle correlations were not explored in detail in this paper, and no estimates of ridge shape or yield were given.

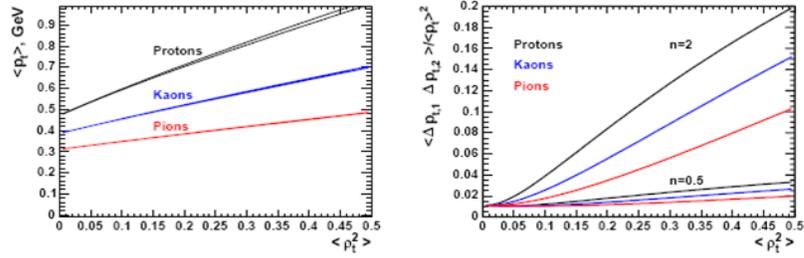


Fig. II.11.: Blast wave calculation of mean transverse momentum (left) and two-particle correlation (right) from [17].

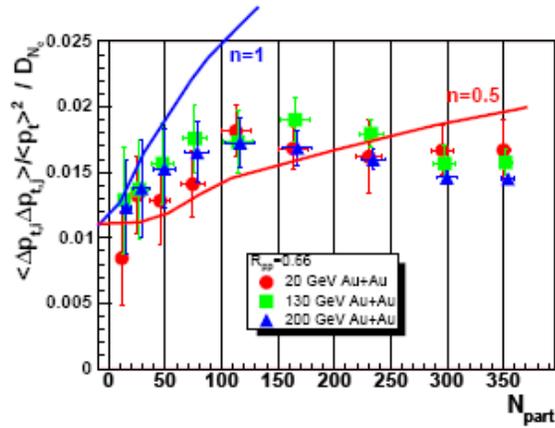


Fig. II.12.: Comparison of blast wave calculation with STAR data[17].

The calculation by Shuryak[18], also suggest that the ridge is formed as a result of jet quenching and transverse radial flow; specifically by QCD bremsstrahlung along the beam (longitudinally) boosted by transverse flow. Unlike the Voloshin calculation, Shuryak provides a comparison of the 2-particle correlation ($\Delta\phi$) from data with that from his calculation. However, the theory ultimately fails at matching the data.

The correlation function generated in Shuryak's calculation is given as

$$C(p_t, \phi) = \int P_{prod}(r)P_{quench}(r, \phi_1) \times F(p_t, v(r), \phi_1 - \phi)rdrd\phi_1. \quad (2.21)$$

The results of this function, $\Delta\phi$ distribution (for absorption lengths of 1, 0.5, 0.25 fm), are shown in Fig. II.13 and compared with the STAR data. This correlation function does not do a good job of matching the width of the data; the author concluded that more complicated models for quenching would produce better agreement with the data, but that this mechanism of ridge production “basically works”[18]. It is, however, difficult to justify this statement based on the strength of the calculations presented in [18].

A more detailed exploration of the transverse radial flow effect on two-particle correlations, is presented in [38]; these calculations use a transverse radial boost incorporated in PYTHIA events to show how this flow can affect two- and three-particle correlations.

The model (unlike previous models discussed in this chapter) uses vacuum $p + p$ events and thus neglect effects such as jet quenching, diffusion processes and string melting. The produced particles are boosted radially in the transverse plane at fixed velocity in a random ϕ direction. The jets are assumed to be maximally coupled to the transverse radial flow. The authors describe two scenarios to explain the conceptual

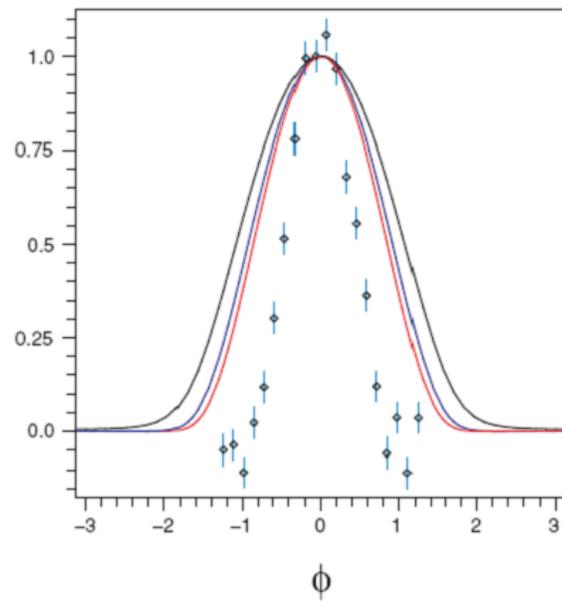


Fig. II.13.: Correlation function, calculated using Eq. 2.21 (solid curves)[18] plot with Au+Au 0 - 10% most central STAR data

basis for this theoretical interpretation[38]:

1. Two incoming partons are subject to transverse kicks before they collide to produce jets. The jet production in the rest frame of the parton pair is essentially the same as if the partons were not radially boosted, but the produced hadrons are boosted in the lab frame.
2. Two incoming partons interact as if in vacuum, but their collision products are subject to a transverse boost due to momentum kicks by the dense medium: Jet hadronization proceeds quickly within the medium and sufficient medium-flow builds up to radially push hadrons produced by parton fragmentation.

The authors conclude that the near side jet peak amplitude increases with increasing radial velocity due to the kinematical focusing produced by the radial boost on the trigger and associated particles. They further conclude that the away-side ridge is deflected and defocused away.

There are two major issues that must be highlighted: First, since the simulations use one boosted $p+p$ collision per simulated event, momentum conservation is globally violated; second, they assume that parton-parton collisions in a dense medium proceed exactly as those in vacuum. It should also be noted, that the authors base their conceptual understanding of ridge formation on the experimental results that initially predicted that the ridge yield is flat with trigger p_T , which (as mentioned earlier in this chapter) is likely not the case. In spite of these deficiencies in the model, the authors invite us to consider the “spirit of the model” [38] seriously as it explains many different phenomena simultaneously.

II.5. Triangular Flow in Heavy-Ion Collisions

The calculations by Alver and Roland[19] introduce the concept of triangularity and triangular flow. They suggest that the near- and away-side structures are due to event-by-event fluctuations which create triangular anisotropy in the azimuthal particle production. The authors cite, in partial support of this hypothesis, results of the NEXSPHERIO hydrodynamic model[51] that suggest that in two-particle correlations broad near- and away-side structures arise, if fluctuations in the initial conditions are introduced.

In this calculation the authors focus on the first three coefficients of a Fourier expansion of the azimuthal correlation; directed flow (v_1); elliptic flow (v_2); triangular flow (v_3). The authors start by redefining eccentricity and elliptic flow. Eccentricity is given as[19];

$$\epsilon_2 = \frac{\sqrt{\langle r^2 \cos(2\phi_{part}) \rangle^2 + \langle r^2 \sin(2\phi_{part}) \rangle^2}}{\langle r^2 \rangle}, \quad (2.22)$$

when the coordinate system is taken as the center of mass of the participating nucleons; r and ϕ_{part} are the polar coordinate positions of participating nucleons. This region defines an ellipse, whose minor axis is given as

$$\psi_2 = \frac{\text{atan2}(\langle r^2 \sin(2\phi_{part}) \rangle^2, \langle r^2 \cos(2\phi_{part}) \rangle^2) + \pi}{2}; \quad (2.23)$$

v_2 is then defined with respect to ψ_2 (as opposed to the reaction plane)

$$v_2 = \langle \cos(2(\phi - \psi_2)) \rangle. \quad (2.24)$$

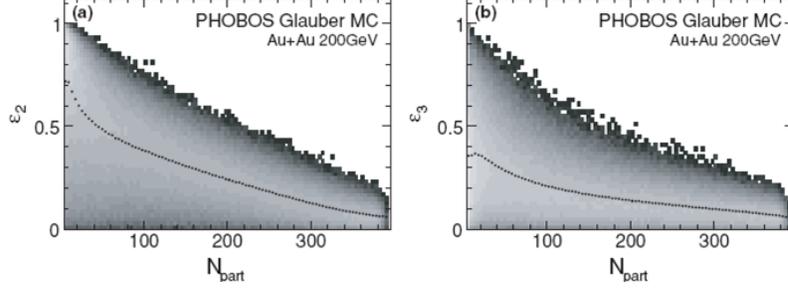


Fig. II.14.: Eccentricity, ϵ_2 (left) and triangularity, ϵ_3 (right) distributions; as a function of N_{part} in 200 GeV Au+Au collisions[19].

Similar equations can be defined for the third coefficient giving triangularity ϵ_3 and triangular flow v_3 [19]

$$\epsilon_3 \equiv \frac{\sqrt{\langle r^2 \cos(3\phi_{part}) \rangle^2 + \langle r^2 \sin(3\phi_{part}) \rangle^2}}{\langle r^2 \rangle}, \quad (2.25)$$

$$v_3 \equiv \langle \cos(3(\phi - \psi_3)) \rangle. \quad (2.26)$$

The minor axis of the participant triangularity, ψ_3 is given by[19]

$$\psi_3 = \frac{\text{atan2}(\langle r^2 \sin(3\phi_{part}) \rangle^2, \langle r^2 \cos(3\phi_{part}) \rangle^2) + \pi}{3}. \quad (2.27)$$

This axis is uncorrelated with both the reaction plane angle and ψ_2 , and therefore is calculated as zero with respect to these angles.

Calculated values of ϵ_2 and ϵ_3 are shown in Fig. II.14, these values are calculated with a PHOBOS Glauber Monte Carlo implementation.

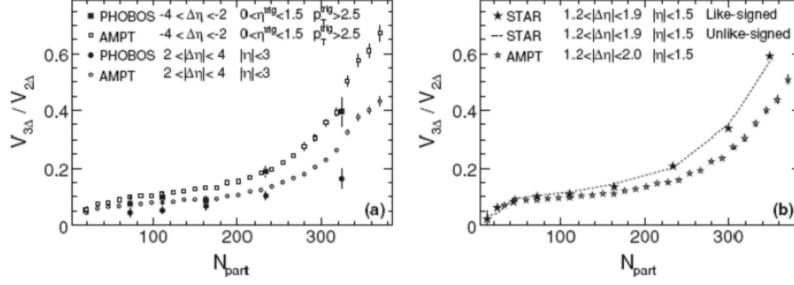


Fig. II.15.: The ratio of triangular flow (v_3) to elliptic flow (v_2) as a function of N_{part} in 200 GeV Au+Au collisions[19]. Filled points are data from PHOBOS (right) and STAR (left), open points show the theoretical calculations.

The authors then make use of an AMPT model to study v_2 and v_3 . The model consists of four components; initial conditions; parton cascade; string fragmentation; relativistic transport model[52]. The initial conditions for the model are obtained from Heavy Ion Jet Interaction Generator (HIJING). This AMPT model underestimates the v_2 magnitude, so for comparisons with the data, the ratio of the third to the second coefficient is calculated, for data this is given as[19]

$$\frac{V_{3\Delta}}{V_{2\Delta}} = \frac{\int C(\Delta\phi)\cos(3\Delta\phi)d\Delta\phi}{\int C(\Delta\phi)\cos(2\Delta\phi)d\Delta\phi}. \quad (2.28)$$

The ratio for STAR and PHOBOS data and for the calculation is shown in Fig. II.15. There is a qualitative agreement between the data and the calculation, the authors claim that since the v_3 component is related to triangular anisotropy, that it suggest that “triangular flow may play an important role in understanding the ridge and broad away-side structures in data”[19].

In this paper the authors introduce a new idea, and suggested that it may be useful in understanding the ridge. There is little that can be criticized in the discus-

sion, because no qualitative or quantitative assertions were made about the ridge as interpreted through this theory: There were no attempts to reproduce the ridge magnitude or shape, its yield, its variation with trigger p_T or its variation with centrality (to name a few quantitative features of the ridge). A more detailed treatment of this theoretical idea is needed so that it can be evaluated on the strength of its ability not just to match the data, but to explain the ridge and all its quantitative features.

II.6. A More Recent Calculation & Conclusion

There have been many recent theoretical studies that attempt to explain various features of the ridge, some by introducing new theoretical ideas, others by assuming the validity of an existing theory and extending that to the explanation of these features. I will close this chapter with an exploration of one such calculation; the work of Sorensen et. al[20] which focuses on the centrality dependence of the ridge amplitude and attempts to explain it by relating it to density inhomogeneities in the initial overlap region. The work used measured v_2 and single particle rapidity density dN/dy with a Monte-Carlo Glauber model for the initial density to calculate the ridge amplitude (A_1) as a function of centrality.

The model is based on the following three assumptions[20]:

1. The expansion of the fireball in heavy-ion collisions converts anisotropies from coordinate-space into momentum-space.
2. The conversion efficiency increases with density.
3. The relevant expansion plane is the participant plane.

To model the eccentricity fluctuations, the authors calculate the quantity $\epsilon_{n,part}^2$;

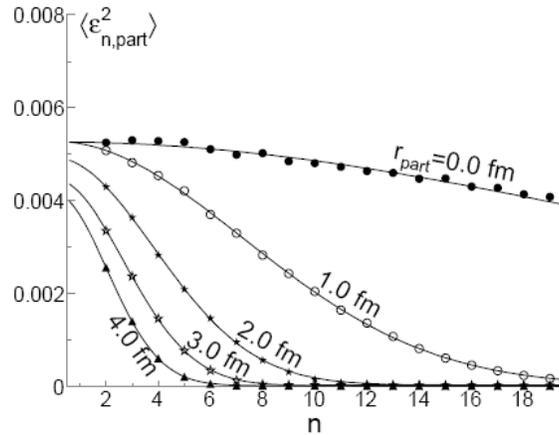


Fig. II.16.: $\epsilon_{n,part}^2$ vs. n^{th} harmonic[20], for different values of r_{part} (the radius of the disk that define the geometry of each participant).

$$\epsilon_{n,part}^2 = \frac{\langle r^2 \cos(n\phi) \rangle^2 + \langle r^2 \sin(n\phi) \rangle^2}{\langle r^2 \rangle}; \quad (2.29)$$

This is show in II.16 for different values of n (the n^{th} harmonic) for central Au+Au collisions. The different curves in the figure correspond to different values of r_{part} , which represents the radius of a disk that is used to represent the spatial distribution of the participants.

To calculate the Gaussian amplitude A_1 from the predicted correlation for the 2^{nd} harmonic, the authors use the following equation (similar calculations can be made for higher harmonics);

$$\frac{1}{2\pi} \int_{-\pi}^{+\pi} \frac{\Delta\rho}{\sqrt{\rho_{ref}}} \cos(2\Delta\phi) d\Delta\phi = 0.11A_1. \quad (2.30)$$

The estimate of the ridge amplitude A_1 based on $\epsilon_{n,part}^2$ vs. centrality parameter

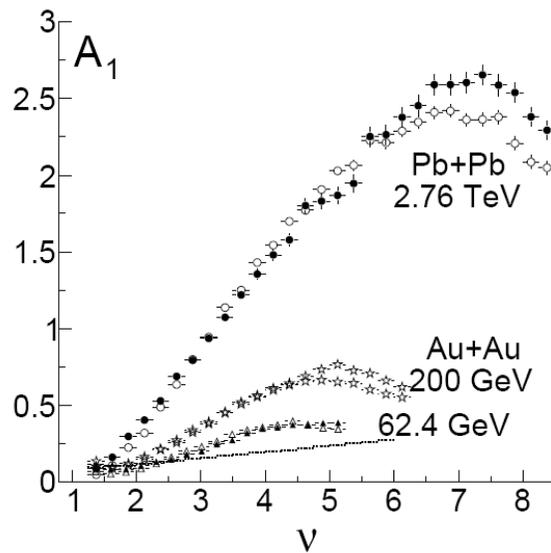


Fig. II.17.: Contribution of eccentricity fluctuations to the near-side Gaussian peak amplitude A_1 [20].

$\nu = 2N_{bin}/N_{part}$ (N_{bin} and N_{part} are the number of binary collisions and the number of participants) is shown for these collision systems for the 2^{nd} and 3^{rd} harmonics.

The authors' estimate of A_1 agrees with what has been observed at 200 and 62.4 GeV (see Fig. II.17). A_1 increases from a small initial value, at a rate greater than the rate expected from scaled $p + p$ collisions. The maximum is reached at $\nu \sim 5$ after which it decreases.

The authors' claim that the rise and fall of the ridge amplitude with centrality is as a result of initial geometry fluctuations and that they “know of no other plausible scenarios to explain the rise and fall of the ridge other than this explanation”[20]. However, this argument is a weak argument because it is based on two major logical fallacies. The first, and more obvious, fallacy is that it is a form of *argumentum ad ignorantiam*; the assertion of a premise justified by the fact that no other explanation

is known. The second fallacy is the *post hoc ergo propter hoc* fallacy, or as it is more commonly phrased in a scientific context; *correlation does not equal causation*, the authors could be identifying another effect of some other (currently unknown) cause. This criticism of their argument is not to assert that it is wrong, but that it is not justified, and that their claims are not properly supported by sound reasoning. What is absent from this paper, is a discussion on exactly how these initial state fluctuations result in the ridge formation. In fairness, the authors never claimed to be supplying an explanation for the existence of the ridge, but for the variation of its amplitude with centrality.

Throughout this chapter we have explored many theoretical calculations that all sought to explain the existence of the ridge by various mechanisms. These mechanisms were broadly group into three parent categories; broadening due to gluon radiation, interactions of the jet with the medium and transverse radial flow. None of the calculations stand out as being the likely explanation for the ridge formation. Although we have focused on the more popular calculations, it is clear that more theoretical work is needed in this area; and more experimental measurements are needed to further describe the properties of the ridge. We have also explored a recent theoretical study that attempts to explain features of the ridge rather than explore its formation, which is an emerging trend as previous theories are not yet discounted by experimental observations.

CHAPTER III

EXPERIMENTAL FACILITIES AND DETECTORS

This chapter describes the Relativistic Heavy-Ion Collider (RHIC) and the Solenoidal Tracker at RHIC (STAR) detector system, with particular emphasis placed on the detectors and trigger algorithms used in this study. The chapter starts with an overview of RHIC, followed by an outline of the STAR detector system (including the star magnet design and function). The next sections explore, in more detail, the Time Projection Chamber (TPC) and the Barrel Electro-Magnetic Calorimeter (BEMC). This exploration is followed by a brief discussion of the Zero-Degree Calorimeters (ZDCs) and the Beam-Beam Counters (BBCs); two detectors used in the STAR triggering system (which is discussed in the last three sections of this chapter).

III.1. The Relativistic Heavy-Ion Collider

In 1991, the Alternating Gradient Synchrotron (AGS) Survey and Alignment Group was given the task of aligning the components for the Relativistic Heavy-Ion Collider (RHIC). The site of the canceled ISAbelle Accelerator was chosen for the new collider. The RHIC rings are large (2.4 miles in diameter), and the entire RHIC facility is a complex of accelerators and beam transfer equipment linking them[53]. It is capable of colliding heavy ions (described in detail in this work) and protons.

Heavy ions originate from the Tandem Van de Graaff (TVG) ion source. They are accelerated (using static electricity) through a foil on the positive terminal of the TVG, which strips them of some of their electrons. The now positively charged ions are accelerated to the negative terminal of the TVG and then to the exit where they lose further electrons (to give an Au^{32+} ion) as they pass into the 0.8 km Tandem to Booster Line (TTB), also called the Heavy Ion Transfer Line (HITL) with an energy

per nucleon of 1 MeV/u. The TTB is a vacuum line with steering magnets that injects the ions into the Booster Synchrotron. At this stage, the ions are travelling at 5% the speed of light. Protons, conversely, originate from the linear accelerator (Linac), where they are injected into the Booster Synchrotron (stacked in betatron phase space with an energy per nucleon of 200 MeV/u).

The Booster Synchrotron further accelerates the gold ions to 37% the speed of light, with an energy per nucleon of 95 MeV/u and removes additional electrons yielding Au^{77+} ions. The ions are then transferred to the AGS, which accelerates them to 99.7% of the speed of light, with an energy of 10.8 GeV/u (28.1 GeV for protons). As the ions leave the AGS and are transferred to the AGS-to-RHIC Line, the K-shell electrons are stripped off producing an Au^{79+} ion. The ions are then injected into the AGS-to-RHIC (ATR) transfer line and are directed (by a switch magnet) either left to the clockwise RHIC ring or right to travel counter-clockwise in the second RHIC ring.

The RHIC rings are hexagonally shaped, with a circumference of 3833.8 meters. The bunches of ions are steered by the 1,740 superconducting magnets. There are six places where the beams cross (these are called the RHIC intersection points), two of which correspond to the active experimental collaborations; the Pioneering High Energy Nuclear Interaction Experiment (PHENIX) and the Solenoidal Tracker At RHIC (STAR). The STAR detector system is described in detail in the following section.

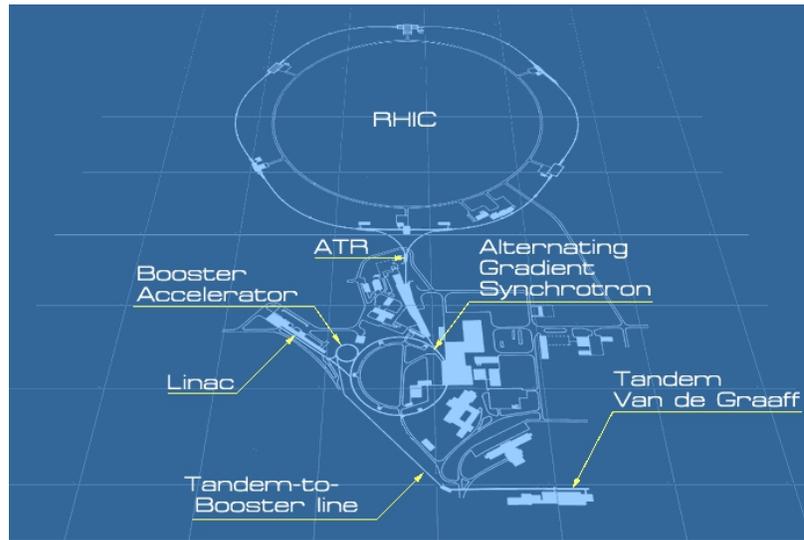


Fig. III.1.: Schematic of the RHIC complex (not drawn to scale).

III.2. The Solenoidal Tracker at RHIC (STAR) Detector

III.2.1. Structure and Sub-Systems

The STAR detector[21] was designed to be able to operate in both the low-multiplicity $p+p$ collision environment, and in the heavy-ion collision environment where particle multiplicities are of the order of thousands per event. It is in these heavy-ion collisions that the QGP (see Sec. I.2)[31] is predicted to be formed. The study of the QGP, and its interactions with and effect on particles produced in these collisions, is one of the main goals of STAR. However, STAR is also suited for studying physics in $p+p$, polarized $p+p$, and $d+Au$ collisions; including the spin structure function of the proton, the contributions from the preferential orientation of gluon spins to the overall spin of the proton, and the initial parton distribution function of the incident nucleus (in $d+Au$). This dissertation will focus on the components of the STAR detector system that make it suitable for studying the QGP in heavy-ion collisions.

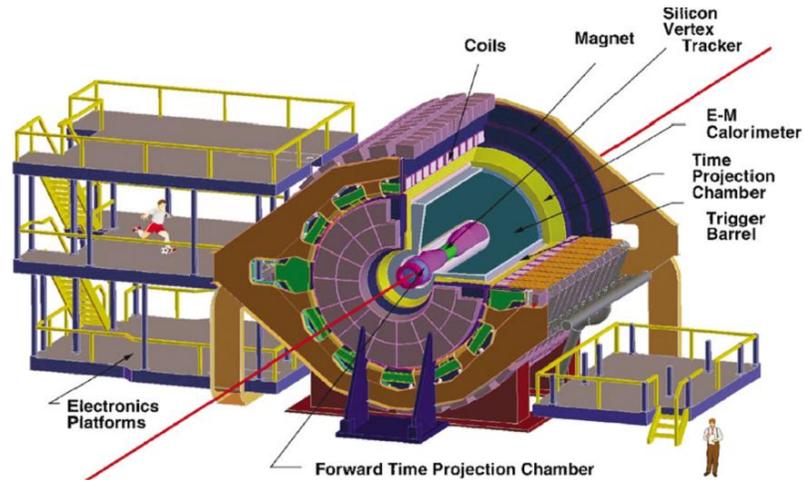


Fig. III.2.: Illustration of the STAR detector system, showing the main component detector[21].

An illustration of the STAR detector system is shown in figure III.2.

One of the main tasks for this detector system is to provide particle tracking for all produced charged particles. STAR uses a 0.5 T room-temperature solenoidal magnet, with a uniform magnetic field (the magnet design considerations and structure are outlined in the following section). In the run 7 data presented in this work, tracking near the interaction region was provided by the Silicon Vertex Tracker (SVT); a detector consisting of 216 silicon drift detectors arranged in three cylindrical layers at distances of approximately 7, 11 and 15 cm from the beam axis[54]. This detector was removed after run 7 because it was unable to effectively assist in a more accurate collision vertex determination near the interaction region, in addition, less material near the interaction point would result in lower background.

More important for particle tracking and identification is the STAR TPC[1]. This 4 m long detector is located at a radial distance of 50 - 200 cm from the beam axis. The TPC covers a pseudorapidity range of $|\eta| \leq 1.8$, and the complete azimuthal

range of $|\phi| = 2\pi$. The TPC helps to identify particles by their ionization energy loss; its energy loss resolution (dE/dx) is approximately 7% and its momentum resolution ($\delta p/p$) is 0.02 for a majority of the tracks. This momentum resolution increases as the particle momentum decreases. In the forward region, there is also a radial drift TPC, the Forward TPC (FTPC), with an η coverage of $2.5 < |\eta| < 4$ and full azimuthal coverage. The FTPC is not used in this analysis and will therefore not be discussed further. However, additional information about the STAR FTPC can be found in [55].

For the measurement of electromagnetic particles, STAR uses the BEMC. This calorimeter is a sampling calorimeter with alternating stacks of lead and plastic scintillator, and has an η coverage of $|\eta| < 1.0$ and full azimuthal coverage. Apart from measuring the transverse energy of particles such as photons and electrons, the BEMC is also used to trigger on high-energy electromagnetic particles in the STAR trigger system. A forward calorimeter, the Endcap Electro-Magnetic Calorimeter (EEMC), is also part of the STAR detector setup; that detector is not discussed in this work, but is well-documented in [56].

In a heavy-ion RHIC run, beam-crossings at the interaction point occur approximately every 107 ns. However, only a small sample of these collisions are of interest for a physics analysis. In addition, the slowest detectors (i.e. the TPC) have readout times on the order of a few hundred Hz. The STAR data acquisition system (DAQ), must therefore only be completed on those events that are likely to be of interest in a physics analysis. This targeted readout of the detector system is achieved using the STAR trigger system[23]. The STAR trigger system is a 10 MHz system that uses the fast detectors to select events of interest before the slower detectors are read-out. The Level 0 trigger is the fastest trigger while Level 1 and Level 2 are slower but allow for additional selection criteria. The Level 3 trigger[57] makes use of tracking and

includes an online display by which a sample of the events can be visually inspected. The fast detectors that are used in the trigger system are the BEMC, the BBC, the ZDC, the Central Trigger Barrel (CTB) (Run 7) and the Time of Flight (TOF) (Run 10).

III.2.2. The STAR Detector Magnet

There were several factors that influenced the STAR magnet[58] design. Two of these factors were the TPC structure (and the requirements for the tracking of charged particles) and the BEMC position outside the TPC.

The STAR TPC, described in the next section, is a large cylindrical tracking detector, that spans the pseudo-rapidity range of $|\eta| < 1.8$ and the full azimuthal range of $0 < \phi < 2\pi$. The TPC is divided into two halves (each 210 cm in length along the z axis) by a central membrane at $z = 0$. The nearly-uniform electric field in each half (East and West) is aligned in an opposite direction to the other half. Charged particles are tracked by the TPC, as they create clusters of ionization, which drift (under the influence of the electric field) to cathode plates at the end of the cylinder.

One of the main measurements taken with the STAR detector is the momentum measurement of charged tracks. The electron, in particular, is problematic; requirements on the magnetic field to ensure a well understood electron drifts are the limiting consideration, in the determination of the magnetic field homogeneity. The field homogeneity requirement was determined by combining the tracking accuracy requirement for these electrons ($\sim 200 \mu m$), with estimates of the position reconstruction accuracy due to uncertainties in the magnetic field.

The STAR BEMC, described in Sec.III.4(68), sits outside the TPC area, this fact poses an additional constraint on the magnet design: There must be sufficient space inside the magnet coils for the BEMC detector components, and space between

the coils for the BEMC electronics. A final design constraint is the need for the measurement of particles at large pseudo-rapidity ($|\eta| > 2.0$).

The STAR magnet is approximately cylindrical in geometry and consists of 30 flux return bars (backlegs), four end rings, and two poletips. The three types of magnetic coils used are: Main, Space Trim, and Poletip Trim. The Main and Space Trim coils are built from two layer pancakes wound in a bifilar fashion (13 turns per coil), while the Poletip Trim coils contain six layers wound in a trifilar fashion (118 turns per coil). There are five separate power supplies that power the STAR magnet; a main power supply (828 V, 5300 A), two booster power supplies (50 V, 600 A), and two poletip trim power supplies (140 V, 1600 A). These supplies (with the exception of the booster supplies) are in two parts; transformer and rectifier control sections, and they all supply a negative voltage, with the exception of the main supply, which supplies both positive and negative.

In the case of overheating of any of the power supplies, the currents are run down over an interval of 2 minutes, if this fails to lower the temperature, the power supplies are immediately shutdown. This overheating procedure ensures that the magnet system is protected, and that the stress on the system is minimized. The temperature of the magnet coils is maintained at a mean of 29°C, by a closed-loop water cooling system (supply temp. = 24°C, return temp. = 29°C, pressure = 200 PSI, flow rate 1200 GPM), which dissipates approximately 3.5 MW of power. This closed-loop system is in turn cooled by an open-loop system with a cooling tower.

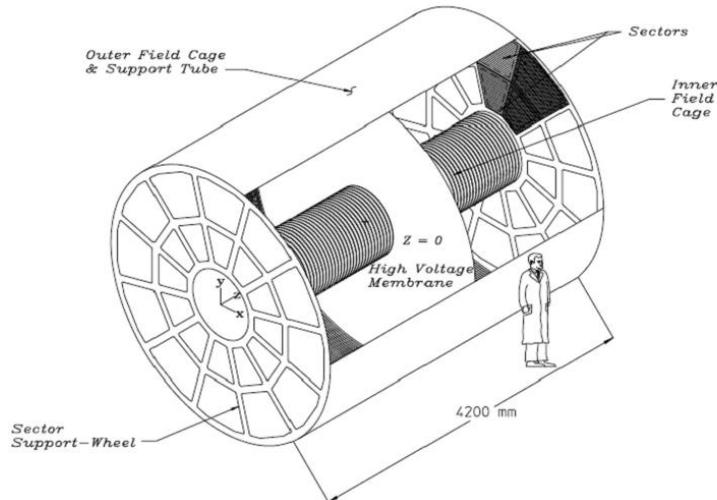


Fig. III.3.: Sketch of the STAR TPC[1].

III.3. The STAR Time Projection Chamber (TPC)

III.3.1. The TPC Structure

The STAR TPC[1] operates in a high multiplicity environment, with typical heavy-ion multiplicities of 1000 particles per unit pseudorapidity, with an average p_T of approximately 500 MeV/c. Additionally, a significant number of secondary particles are produced from the decay of short-lived hadrons, and primary particle interactions with detector material. In this environment the TPC must serve as the primary tracking detector and effectively record tracks of all produced particles, measure their momenta (from 100 MeV/c to 30 GeV/c) and identify the particles (from 100 MeV/c to ~ 1 GeV/c) by measuring their ionization energy loss (dE/dx). The TPC has a relatively large acceptance ± 1.8 units of pseudorapidity, and full azimuthal coverage.

The TPC is 4.2 m in length, with a diameter of 4.0 m. The TPC is essentially a large cylindrical gas-filled detector with a uniform electric field of ~ 135 V/cm. As primary ionization particles pass through the gas in the detector, their paths are

reconstructed via the secondary electrons they release that drift in the electric field (defined by the thin conductive Control Membrane (CM) at the center of the TPC) to the readout endcaps at the end of the chamber.

The TPC readout system is based on Multiwire Proportional Chambers (MWPC) with readout pads. The drifting electrons are amplified on avalanche by a factor of 100 - 3000, at the 20 μm anode wires. Several adjacent pads share the induced charge from the avalanche, so the original track position can be reconstructed to a fraction of a pad width. In total, there are 136, 608 pads in the TPC readout system.

The TPC CM is operated at 28 KV with the end caps at ground. The CM cathode is made of 70 μm thick carbon-loaded Kapton film with 230 Ω per square surface resistance.

The TPC is designed with an inner field cage (IFC) and an outer field cage (OFC). The material in the inner radius was limited because this is where multiple coulomb scattering is most important for accurate tracking and accurate momentum reconstruction. Aluminum was therefore used in the IFC limiting it to 0.5% radiation length (X_0). Copper was used for the OFC (because of the need for electrical connectivity) giving it a thickness of 1.3% X_0 .

The TPC readout planes are MWPC chambers with pad readout that are mounted on aluminum support wheels. The readout modules are arranged as on a clock with 12 sectors around the circle. There are only 3 mm spaces between the sectors which translates to a small dead area between the chambers. The chamber consist of a pad plane on one side, the ground wire plane on the other, and a gating grid. A comparison of the inner and outer subsector geometries is given in table III.1.

Real TPC tracks may not cross all 45 pad rows. The number of rows crossed depends on the radius of curvature of the track, the track pseudorapidity, fiducial cuts near sector boundaries, and other details about the particle's trajectory. The overall

Table III.1.: Comparison of the inner and outer TPC subsector geometries[1].

	Inner subsector	Outer subsector
Pad size	2.85 mm x 11.5 mm	6.20 mm x 19.5 mm
Isolation gap between pads	0.5 mm	0.5 mm
Pad rows	13 (#1 - #13)	32 (#14 - #45)
Number of pads	1750	3942
Anode wire to pad plane spacing	2 mm	4 mm
Anode voltage	1170 V	1390 V
Anode gas gain	3770	1230

tracking efficiency is about 80 - 90%. The track of a primary particle passing through the TPC is reconstructed by finding ionization clusters along the track. These clusters are found separately in x, y and z space.

III.3.2. The TPC Gas System

The STAR TPC gas system[2] has two main functions; the first is to provide one of two gas mixtures (P10- Ar 90% + CH₄ 10%, or He 50% C₂H₆, the former is the favored mixture in STAR) to the TPC, and the second is to cool the outer field cage resistor strings which are located at the top of the drift volume. The system (which is normally a closed circuit gas system) can be operated as an open system for purging. The gas circulated at a rate of 36,000 L/h which allows for one volume change of the 50,000 L TPC every 1.4 h. Additional gas system parameters are given in the table III.2.

The purity and composition of the gas mixture is monitored with O₂, H₂O and

Table III.2.: TPC gas system parameters[2].

TPC Volume	50,000 L
Gas Mixture 1	(10 \pm 0.1%) CH ₄ in Ar
Gas Mixture 2	(50 \pm 0.1%) C ₂ H ₆ in He
Compressor Pressure	90 - 120 mbar
Supply Pressure	2.2 - 2.4 mbar
Return Pressure	0.5 - 1.6 mbar
Internal TPC Pressure	2.0 \pm 0.03 mbar
Recirculation Flow	36,000 L/h
Purge Flow	12,000 L/h
Make-up Gas Flow	3.0 - 33 L/h
Oxygen Content	< 25 ppm
Water Content	< 20 ppm

CH₄ (or C₂H₆) monitors which are distributed in such a way that each section of the gas system can be selected separately for monitoring. If the percentage of O₂ in the mixture exceeds 0.1% the flow of flammable gas is immediately shut off and replaced by an inert gas. For CH₄, if the percentage in the mixture exceeds 11%, its flow is immediately shut off. The mixture is decontaminated with a dryer and purifier that withdraw about 40 - 45 L/min of the upstream flow. The purifier is filled with a catalyzer that catalyzes the incomplete oxidation, at 210 - 220 °C, of the hydrocarbon (CH₄ or C₂H₆) by O₂ forming their respective alcohols. This alcohol can then be removed by the dryer. The catalyzer is in continuous use in order to maintain the acceptable 19 - 22 ppm O₂ level. Without the catalyzer the equilibrium O₂ level is 60 ppm.

In addition to monitoring and regulating gas composition, it is very important to monitor and regulate the TPC pressure. The TPC pressure must track the atmospheric pressure as accurately as possible. Because of the location of the detector in the Long Island, NY, area, it is common to have frequent storms, which are often preceded by rapid changes in atmospheric pressure. In the gas system, there are two sources of pressure; the first is a compressor located at the TPC exit, and the second is the flow of fresh gas through the mixing manifold. Maintaining a constant pressure downstream and regulating the amount of gas shunted from the compressor output to intake help to achieve normal pressure regulation.

In the event of rapid fluctuations of the atmospheric pressure additional measures are needed. For example, when the internal TPC pressure is greater than 2.0 mbar above the atmospheric pressure, the gas control system will close the solenoid valves in the gas supply lines and open a vent valve, allowing the TPC to vent directly to the atmosphere. If the pressure difference exceeds 3.0 mbar, the TPC is vented to the atmosphere through a bubbler. Equally undesirable is TPC under pressure; if the

pressure falls too low, the flow of flammable gas is shut off by the compressor and inert gas is allowed to flow into the system. This system can account for a maximum rate of increase of atmospheric pressure of up to 6 mbar/min.

The TPC gas system is controlled by a DAQ subsystem which is composed of three separate devices:

1. A barometer to measure atmospheric pressure
2. A commutator for temperature measurement
3. A custom I/O board

All data are kept in a Microsoft Access database, which allows for easy access and analysis.

III.3.3. The TPC Laser System

Any large gas detector needs to have a system for testing, calibrating, and monitoring its function during a physics run. Typically these gas detectors use an ultraviolet (UV) laser system to generate beams that mimic straight particle tracks. UV-laser beams are used, because they produce ionization in gaseous detectors via a two-photon ionization process of the ppb level organic compounds usually present in the detector volume. A Nd-YAG (Neodymium-doped Yttrium Aluminum Garnet) frequency-quadrupled laser ($\lambda = 266$ nm) produces equivalent ionization to a mip in common detector volume gas mixtures, without the need for additives. This allows it to be easily integrated into the detector system, as it does not need a modified setup to be run.

In general, laser systems help to reduce the uncertainties on track measurement in a gas detector. For the STAR TPC specifically, there are 5 main sources[59] of

track coordinate measurement uncertainty that require an independent method of calibrating and monitoring this detector:

1. Variation in drift velocity caused by gas mixture, temperature, pressure and electric field variation.
2. TPC misalignment in the magnet and existence of the global $E \times B$ effect.
3. Radial inhomogenities of magnetic and electric field.
4. Space charge buildup due to high multiplicity in Au + Au collisions.
5. TPC endcap wheel displacement and inclination.

TPC track distortion varies along the length of the detector. In order to accurately monitor all of these distortions, the desired number of laser beams per TPC half is 100 - 400. This issue (as well as the sources of track coordinate measurement uncertainties listed above) lead to the following 6 specifications[59]:

1. Number of laser tracks $\sim 100 - 400$ in each half of the TPC.
2. Laser beams should fill the TPC volume uniformly.
3. Electron density along the laser beam in any point must be higher than ionization from relativistic particles.
4. The accuracy of the position and stability during operation of each laser beam at any point must be smaller than $\sim 200\mu$ in azimuthal and radial directions and smaller than $\sim 700\mu$ in axial direction.
5. Synchronization of the time of the laser beams appearance in the TPC volume to the RHIC clock within ~ 5 ns error to provide $\sim 0.01\%$ accuracy in drift velocity measurements.

6. Laser system must provide alignment, steering and stable position of laser beams with the accuracy specified above.

Because of these requirements (in particular the requirement on the number of desired laser tracks), the STAR laser system had to employ a novel design, as older-generation system designs would have been inadequate. The STAR design produces a large number of narrow laser beams by splitting a wide laser beam (of diameter $\sim 20 - 30\text{mm}$) with many small-diameter mirrors. These small mirrors are made from glass rods cut at 45° , polished and covered by dielectric coating with 100% reflectivity. The mirrors are grouped in bundles with seven mirrors per bundle, with each mirror in the bundle rotated in a different direction.

The diameter of each mirror was chosen to be 1 mm, because mirrors smaller than 1mm in diameter are more difficult to produce and align and also create significant divergence. And mirrors with longer diameters require wider beams and increased laser power.

The total number of laser beams is determined by the wide laser beam area and the number of bundles occupying it. In the STAR TPC, bundles are installed along the z-axis 30 cm apart.

The STAR TPC laser can be operated remotely using the global TPC operations slow control infrastructure. A graphical user interface (GUI) is accessible on a PC in the STAR control room. The laser beam image can also be visually monitored. This is done using a miniature CMOS CCD Camera (lens and fluorescence screen are ~ 20 mm in diameter). This camera is designed to be operated in a high magnetic field environment (up to 1.0 T). STAR detectors are synchronized with the RHIC clock (10 MHz) and the laser trigger system can accept the external RHIC clock signal; which allows for easy integration in the system during a physics run.

During a RHIC run, the laser trigger is implemented to interleave laser events in a physics run. The drift velocity from the physics run, and from the laser system are then calculated and compared. Laser drift velocity is determined using the Z position difference of the mirror position for the set of laser tracks closest to and furthest from the pad plane. This drift velocity is affected by several factors; barometric pressure, cathode voltage, temperature, clock frequency, methane concentration, and unknown additives in TPC gas. However the methane concentration is the most influential parameter.

III.4. The STAR Barrel Electro-Magnetic Calorimeter (BEMC)

III.4.1. The BEMC Structure

The STAR TPC is less effective for identifying charged particles with momenta above $\sim 2 \text{ GeV}/c$. The STAR physics program requires that the detector system is able to distinguish between electrons and hadrons at high transverse momenta. In addition, momentum measurements using a magnetic field only work for charged particles. For photon and neutral meson (such as π^0 s and η s, both of which primarily decay into two photons) measurements, both of which are an important part of the STAR physics program, a new type of detector is needed.

In STAR, this role is filled by an electromagnetic calorimeter. Calorimeters measure the energy of electromagnetic particles via a destructive process (this is why they are usually located behind tracking detectors). They can be used for Particle Identification (PID) to trigger on interesting events (because of their relatively fast readout times). Calorimeters are usually made up of two types of material, an active material responsible for generation of a signal (e.g. ionization, light), and a passive material, which is responsible for creating the shower. In STAR's BEMC, the active

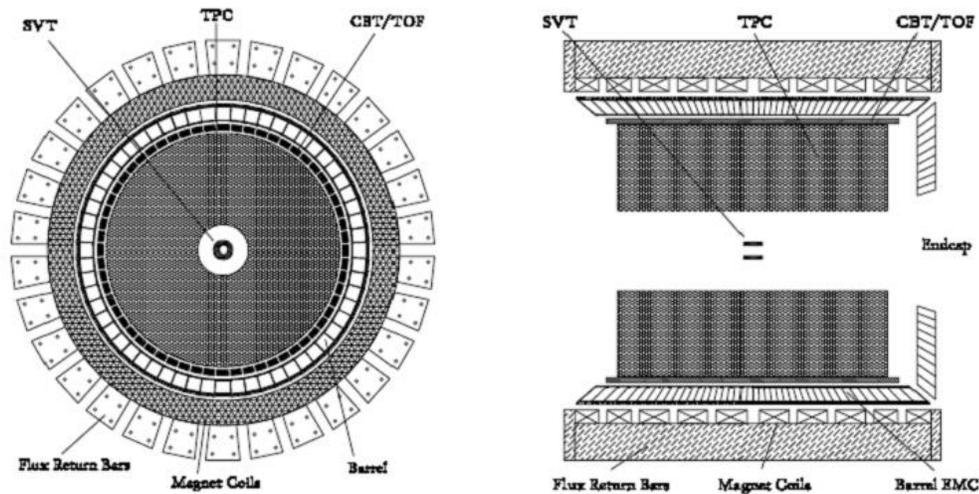


Fig. III.4.: Cross sectional views of the STAR detector system, showing the relative position of the BEMC[22].

material is a plastic scintillator, and the passive material is lead.

In an electromagnetic shower, the original particle interacts with the passive layers creating many lower energy particles. These lower energy particles deposit energy (via ionization in the active layers); the amount of ionization is proportional to the amount of energy deposited in the calorimeter.

The STAR BEMC[22] is a sampling calorimeter; it does not directly measure the full energy of the incident particle, but rather it can be used to calculate this energy based on the shower energy that it supplies. It is located inside the aluminum coil of the STAR solenoid and has coverage in η of $|\eta| \leq 1.0$, and full coverage in ϕ . The BEMC largely matches the TPC tracking coverage. This layout is shown in figure III.4.

The BEMC is comprised of 120 calorimeter modules, of dimension 6° in ϕ (~ 0.1 rad) and 1.0 unit in η . They are mounted 60 in ϕ , by 2 in η . Each module is segmented

into 40 towers, 2 in ϕ and 20 in η ; to give a total of 4800 towers. Each tower has dimensions of 0.05 in ϕ and 0.05 in η , and is projective, i.e. pointing back to the center of the interaction diamond. Each calorimeter module consists of a lead-scintillator stack and a shower maximum detector (see next section) situated approximately $5.0 X_0$ from the front of the stack. There are 20 layers of 5 mm thick lead, 19 layers of 5 mm thick scintillator and 2 layers of 6 mm thick scintillator. The thicker scintillator layers are used in the preshower portion of the detector. The BEMC is under a fixed internal pressure of 15 psi.

III.4.2. The Barrel Shower-Maximum Detector (BSMD)

The width of the towers in the BEMC is larger than the width of an electromagnetic shower. Therefore, in order to provide a precise spacial description of the shower width, and to discriminate between one (direct- γ candidates) and two closely spaced electromagnetic showers (π^0 decay-photon candidates), a detector with a much finer segmentation is needed. This functionality is provided by the STAR Barrel Shower-Maximum Detector (BSMD)[22].

The BSMD is a wire proportional counter, strip readout detector that makes use of gas amplification; it has two independent planes of proportional wires, and two independent cathode planes with strips in both η and ϕ . These two planes allow for a two-dimensional spacial description of an electromagnetic shower. The BSMD is located at variable depths within the BEMC modules varying from $4.6 - 7.1 X_0$ as η varies from 0 to 1. The position of the BSMD within a tower can be found in Fig. III.5, a schematic illustration of the detector can be found in Fig. III.6 and a cross-section view can be found in Fig. III.7.

The *BSMD- η* strips are perpendicular to the anode wires, and provide an image of the shower spatial distribution in the η direction. These strips span 30 wires and

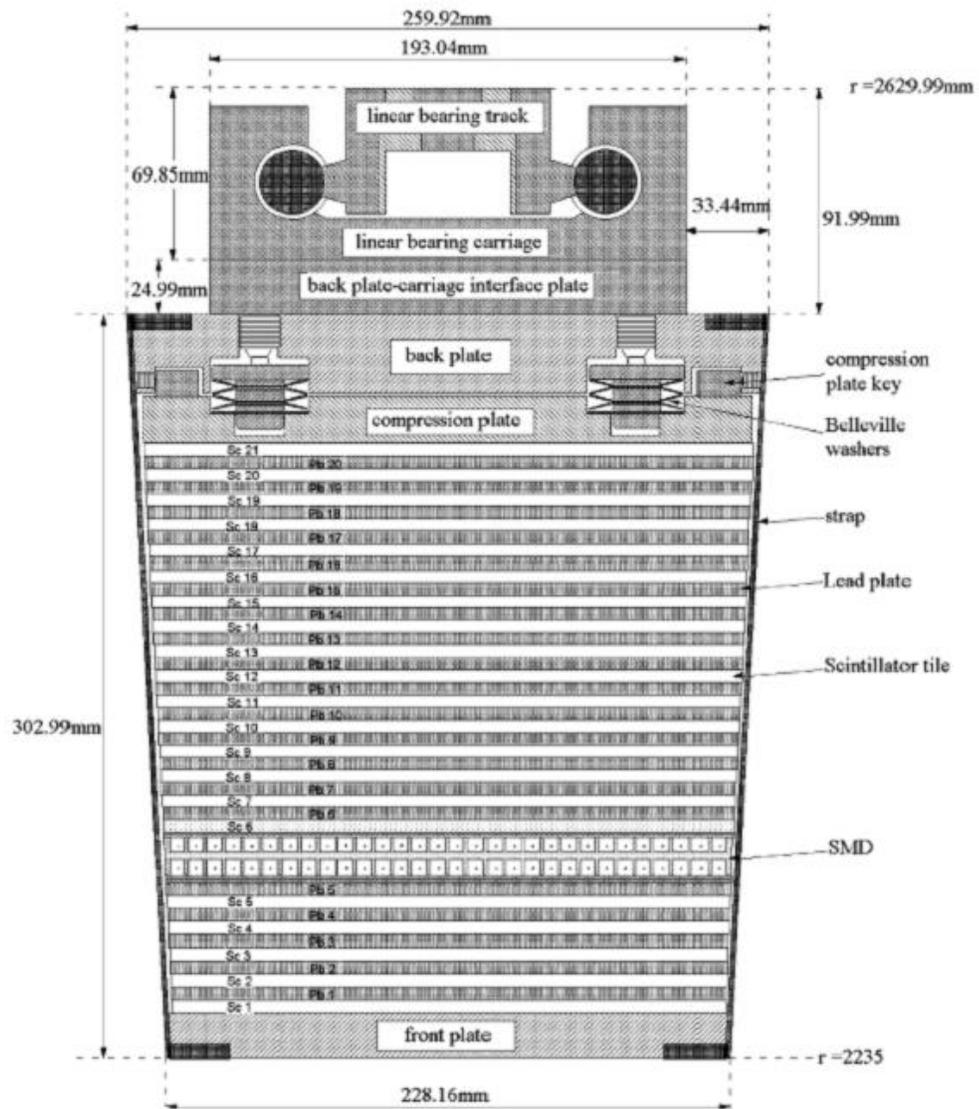


Fig. III.5.: Schematic of a BEMC module (side view) showing the electronic and mechanical structure[22].

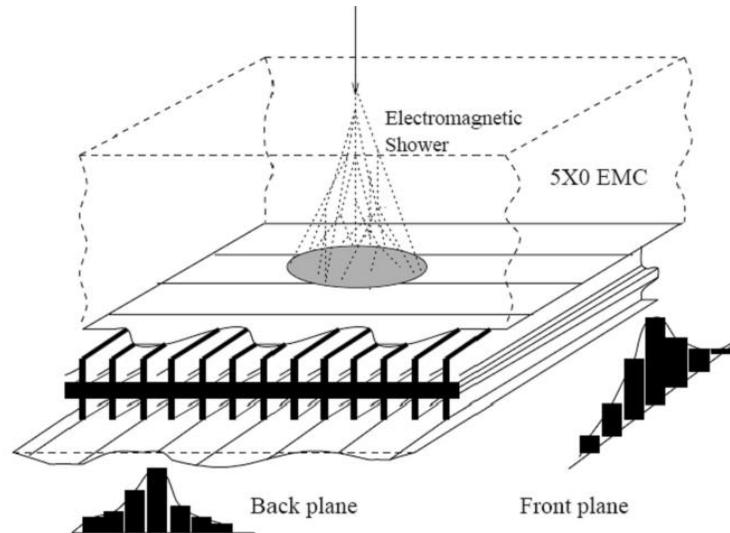


Fig. III.6.: Schematic illustration of the STAR BSMD detector showing the two (η and ϕ detector planes[22].

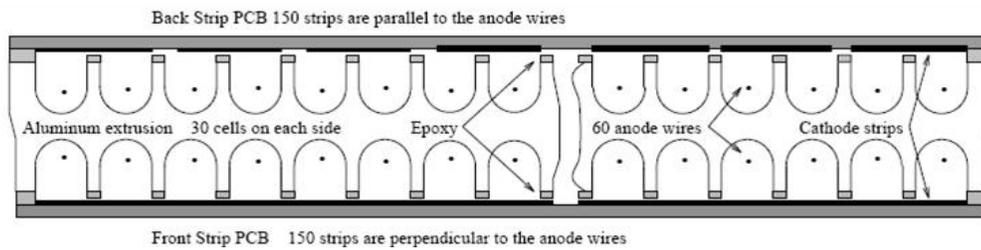


Fig. III.7.: Cross-section of the STAR BSMD detector showing the $50 \mu m$ gold-plated tungsten anode wires and cathode strips that sense the induced charge from the amplification near the wires[22].

have size of 0.1 rad in ϕ (one module width) and 0.0064 in η . The ϕ strips are parallel to the anode wires and have size of 1.33 cm in width and 0.1 η units in length. In total there are 36,000 strips in the full BSMD detector, and 120 wire channels in the BEMC. Each of the 1200 distinct areas, approximately 0.1 by 0.1 in $\eta - \phi$, has 15 ϕ strips and 15 η strips.

More information about the BSMD can be found in [22]; additionally, BSMD calibration and π^0/γ discrimination is discussed in detail in Chapter VI (page 77).

III.5. The STAR Trigger System

RHIC beam crossings occur approximately every 107 ns. Not all of these crossings, however, result in collisions; so it is firstly important for STAR to quickly detect when collisions occur, and secondly for STAR to make a decision on whether or not the collisions are useful for achieving the STAR analysis goals for that running period. Additionally, being able to "label" certain collisions as more useful for one analysis goal versus another (or for multiple goals) will allow more selectivity in the production process. All of these objectives are achieved by the STAR trigger system[23]; a pipelined system in which digitized signals are analyzed at every RHIC beam crossing to determine whether to begin the amplification-digitization-acquisition (ADA) cycle for the slower detectors. This section describes the STAR trigger detectors that are most important in heavy ion collisions and the general logic of the Level 0, Level 1, and Level 2 triggers. An outline of the data flow through the STAR trigger is illustrated in figure III.8 (page 74). A full discussion of all the STAR trigger detectors and trigger logic can be found in [23] and [57].

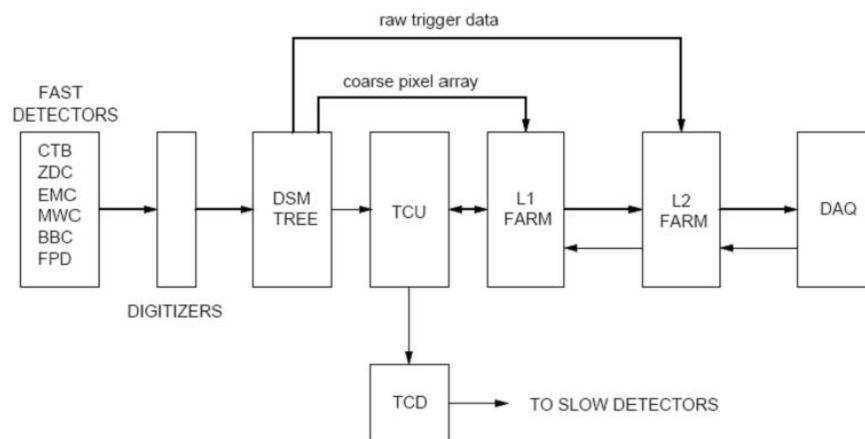


Fig. III.8.: Data flow through the STAR trigger.[23]. Definitions: Central Trigger Barrel (CTB), Zero Degree Calorimeter (ZDC), ElectroMagnetic Calorimeter (EMC), Multi-Wire Counter (MWC), Beam-Beam Counter (BBC), Forward π^0 Detector (FPD), Data Storage and Manipulation (DSM), Trigger Control Unit (TCU), Trigger Clock Distribution (TCD), DAQ (Data AcQuisition).

III.5.1. The RHIC Zero Degree Calorimeters (ZDCs)

In a 200 GeV/c Au+Au collision at RHIC, evaporation neutrons diverge by less than 2 milli-radians from the beam axis; in this 'zero degree' region, collision products and secondary products deposit negligible energy compared with that of the beam fragmentation neutrons. The accurate detection of these neutrons can be used to calculate event multiplicity, which can be related to event geometry and used as a basis of a fast trigger decision (see following section) for the STAR DAQ system.

The RHIC ZDCs[24] (identical design for all original RHIC experiments) were designed to detect these neutrons and measure their energy; they are longitudinally segmented hadron calorimeters (see Fig. III.9). Since the spatial distribution of neutrons emitted in the fragmentation region carries very limited information about the collision, the ZDCs are not built with transverse segmentation. The ZDCs are composed of modules which consist of a tungsten absorber with undoped fiber optical ribbons in the sampling layer.

III.5.2. The Level 0 (L0), Level 1 (L1) and the Level 2 (L2) Triggers

All detectors channels in the STAR Level 0 trigger system, are digitized for each RHIC crossing and these data are transferred first to the Data Storage and Manipulation (DSM) board and from there into the Trigger Control Unit (TCU) where the status of each detector is used to construct a 18 bit address to a lookup table (LUT), which each address corresponds to a trigger word that is itself an address to an Action Word LUT that tells the detector system what action is to be taken and what detectors are to be involved. Level 0 is designed to issue a decision within $1.5 \mu s$

If the L0 algorithm decides to accept the event, the slower detectors begin to start amplifying and digitizing the signal, the trigger detectors information is aggregated

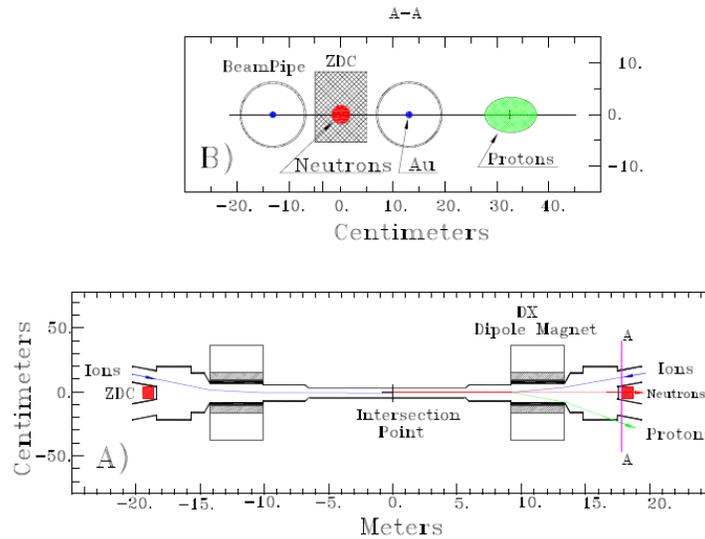


Fig. III.9.: Schematic of the collision region (drawn to scale), highlighting the ZDC position and showing the deflection of protons and charged fragments[24].

(by VME processors) and examined in a coarse pixel array (CPA) at Level 1. The cells of this CPA are of dimensions $\delta\eta \sim 0.5$ and $\delta\phi \sim \pi/2$, which help to identify gross spatial symmetries in particle distributions that are indicative of beam-gas events.

If not aborted, the data acquisition cycle continues and the trigger information is passed to the L2 farm where both the coarse and fine pixel arrays are analyzed to determine whether the event fits certain higher-level analysis-oriented standards. If an event is accepted at L2, the trigger systems hands control of the event to the central Data Acquisition (DAQ) system. The L2 decision time is 5 ms.

CHAPTER IV

DETECTOR CALIBRATION AND DIRECT/DECAY PHOTON
DISCRIMINATION

As discussed in the previous chapter, the Barrel ElectroMagnetic Calorimeter (BEMC) (see Sec. III.4) is a sampling calorimeter, with alternating layers of a plastic scintillating material and lead. This calorimeter spans the entire azimuthal angle (ϕ) range and extends from -1 to +1 in pseudorapidity (η). The BEMC is divided into 4800 sections, called towers, which project towards the point of interaction. At a depth of ~ 5.6 radiation lengths in each tower, sits the Barrel Shower Maximum Detector (BSMD)(III.4.2, page 70); two perpendicular planes (η and ϕ) of 36,000 (18,000 in each plane) proportional strips that vary in thickness across η .

The STAR BSMD measures the energy of an electromagnetic shower, typically extending over a few strips (in both planes) in the detector, initiated when an electromagnetic particle hits a section of the detector. If these 36,000 strips do not give a uniformed digital response to an electromagnetic shower of constant energy, then the detector cannot be relied upon to provide any accurate (or precise) quantitative descriptions of that shower. It is therefore necessary to force as uniform a response as possible, by scaling the raw digitized signals from each strip by a set of 36,000 constants mapped to each strip ID in the detector. This section discusses the first complete calibration of the STAR BSMD, using 3.1 million minimum biased Au+Au events from Run 7, and also discusses the role that this detector plays in discriminating between direct and two close photons from a symmetric decay.

IV.1. BSMD Calibration

The first step in the calibration is to obtain the raw digitized signal in each strip, for each event in which the BSMD is read-out. This digitized signal must be obtained before the STAR ADC-to-energy conversion algorithm is run because this algorithm anticipates a difference in detector response and attempts to correct for it by applying a set of calibration constants determined solely by Monte-Carlo simulation. The only mathematical manipulation done on these raw ADC values is a pedestal subtraction in which the pedestal mean, recorded for that strip during that period of the run, as well as 5 times the pedestal RMS value, are subtracted from the raw ADC to give a pedestal-subtracted ADC value.

Running over 3.1 million events, and aggregating the pedestal-subtracted ADC values for each of the 18,000 *BSMD- η* and 18,000 *BSMD- ϕ* detector channels, should ideally give a response biased only by the natural pseudorapidity dependence of electromagnetic particle distributions. These ADC values are stored in two two-dimensional histogram of pedestal-subtracted ADC versus strip ID, which can be projected to give the one-dimensional ADC distribution of each strip as illustrated in Fig. IV.1.

IV.1.1. BSMD Strip Gains Before Calibration

The 2D histograms for all 120 modules in η and ϕ are shown in Fig. IV.2 and IV.3. The empty plots correspond to modules that were turned off for the entire running period. These histograms are projected for each strip to yield 150 1D histograms of strip ADC values. These histograms must be fit with a function where one parameter (related to the slope of the distribution) can be extracted and interpreted as the gain for that strip. A simple exponential of the form $e^{(C_0+C_1x)}$ does not give a very good

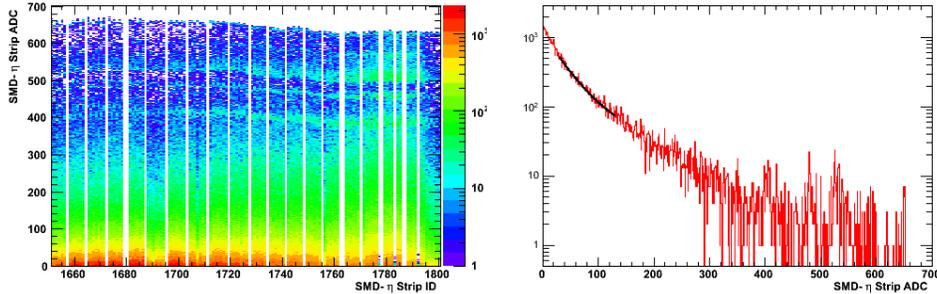


Fig. IV.1.: ADC distributions *BSMD-η* Module 12, 2D (left) and 1D projection of strip #8 in Module 12, strip ID η -1658 (right).

fit (based on initial trials) and consequently does not describe the detector strip gain. A higher order exponential was therefore needed, but by including additional term in the fit function, the goal of having one value to interpret as the gain became more difficult to achieve. The solution is therefore to first fit the ADC distributions with a function of the form of Eq. 4.1.

$$e^{(C_0+C_1x+C_2x^2)} \quad (4.1)$$

A sample of these fits are shown in Fig. IV.4 and Fig. IV.5.

The next step is to assume that the ratio of the 3rd to the 2nd parameter of these fits ($\alpha = C_2/C_1$) should be constant, and to fill this value in a profile histogram with 300 pseudorapidity bins in the case of *BSMD-η* and 20 in the case of *BSMD-φ* (from -1 to +1, corresponding to the detector construction as outlined in the previous chapter) a ROOT histogram class (TProfile) that averages the y-value for all entries in a particular x-bin, (optionally) weighted by the error on each individual x-value in a particular bin. In this case the profile averages α , weighted by the error on the fit, and with an RMS defined as the spread in values for that pseudorapidity bin. This

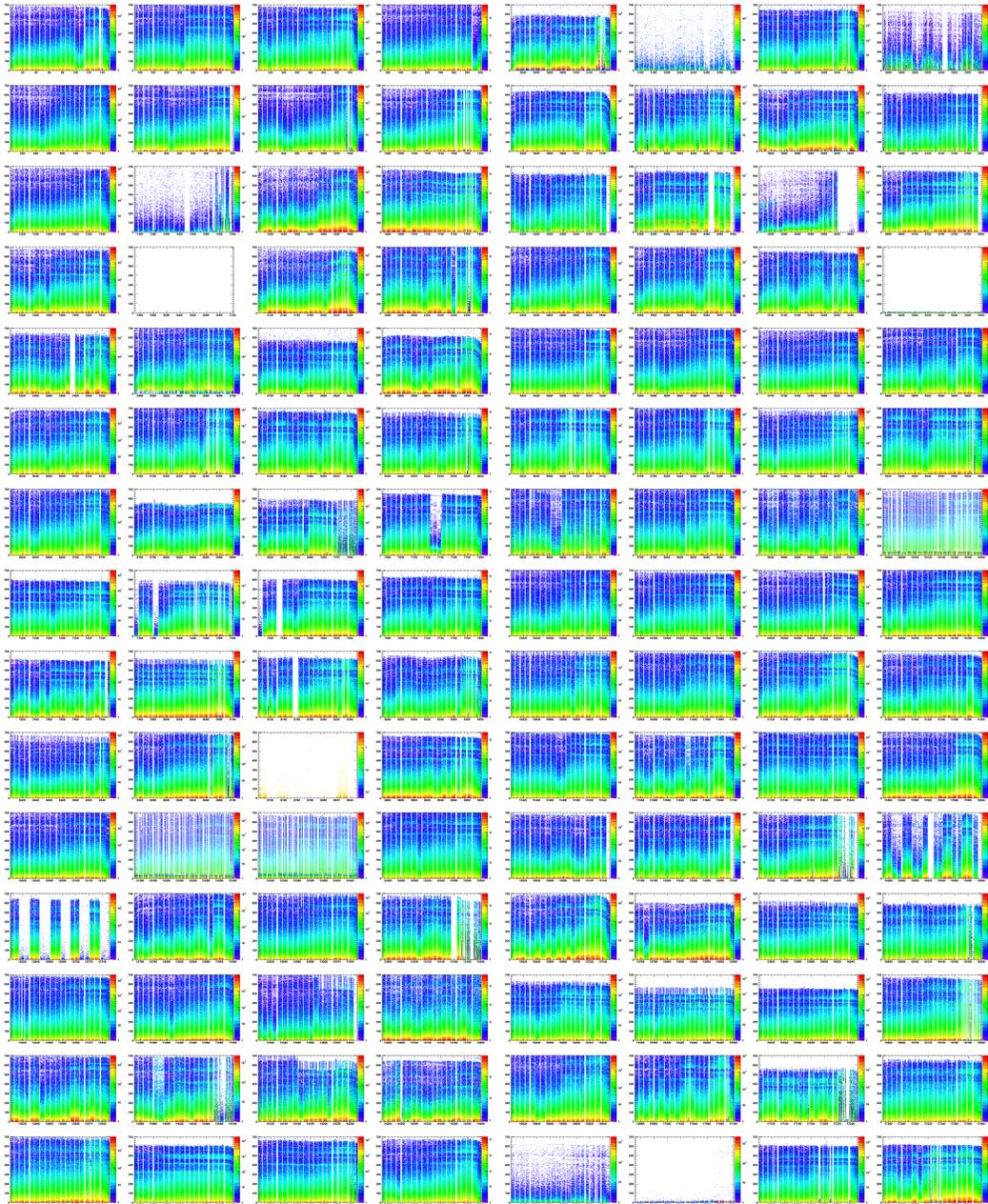


Fig. IV.2.: ADC distributions for all 120 $BSMD-\eta$ Modules (150 strips per module).

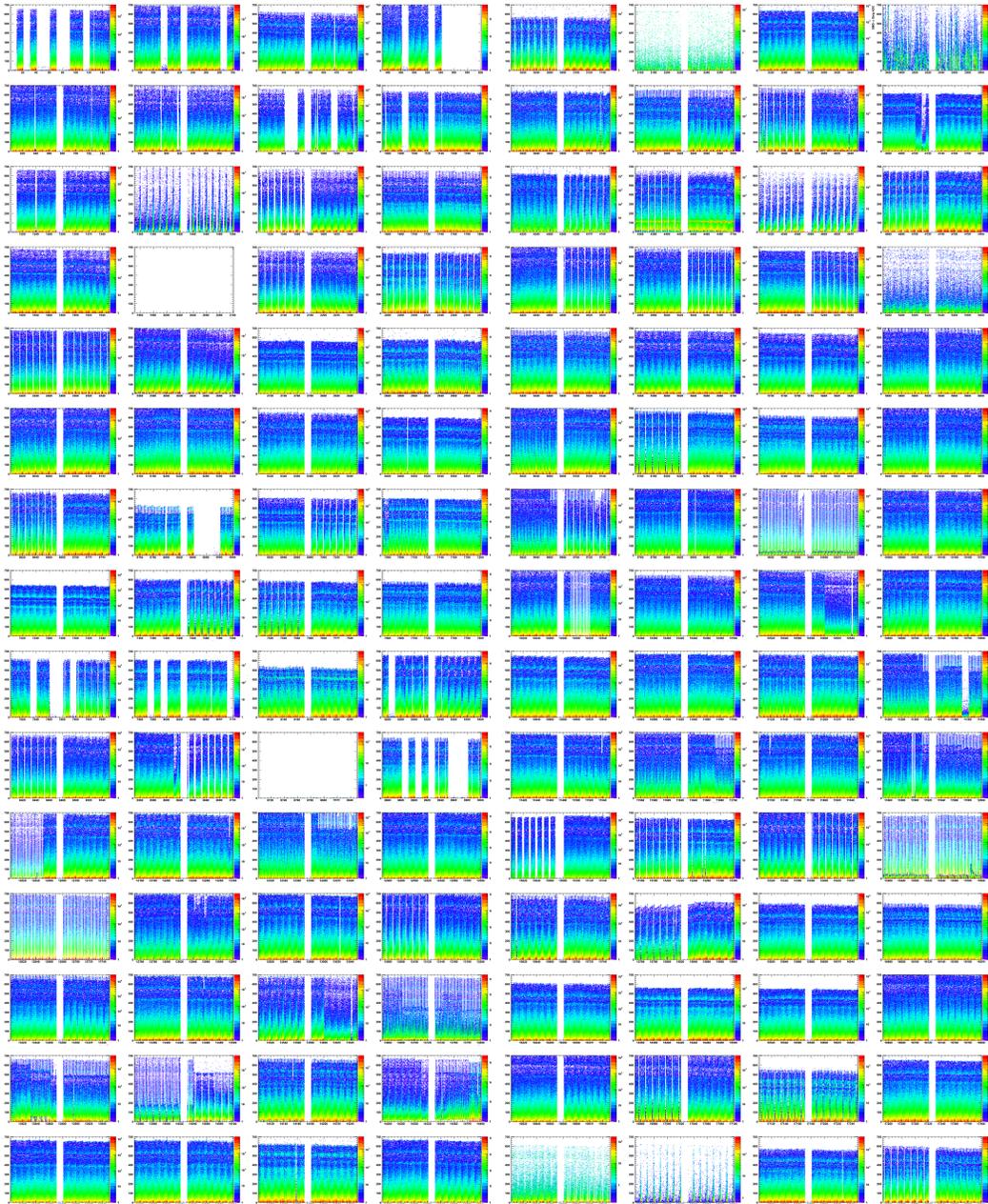


Fig. IV.3.: ADC distributions for all 120 *BSMD- ϕ* Modules (150 strips per module).

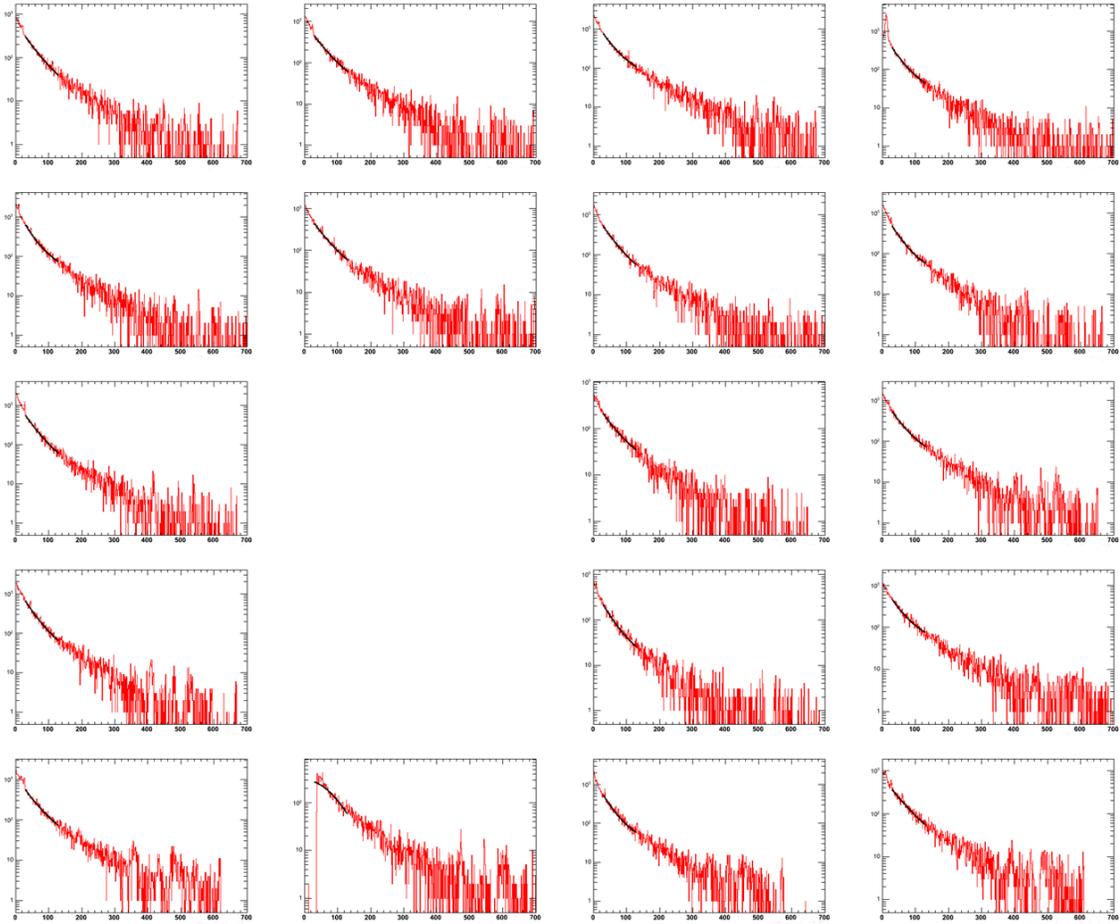


Fig. IV.4.: ADC distributions and fits with equation 4.1 (black line) for the 8th strip in each of the first 20 *BSMD-η* modules. Empty spaces correspond to dead strips.

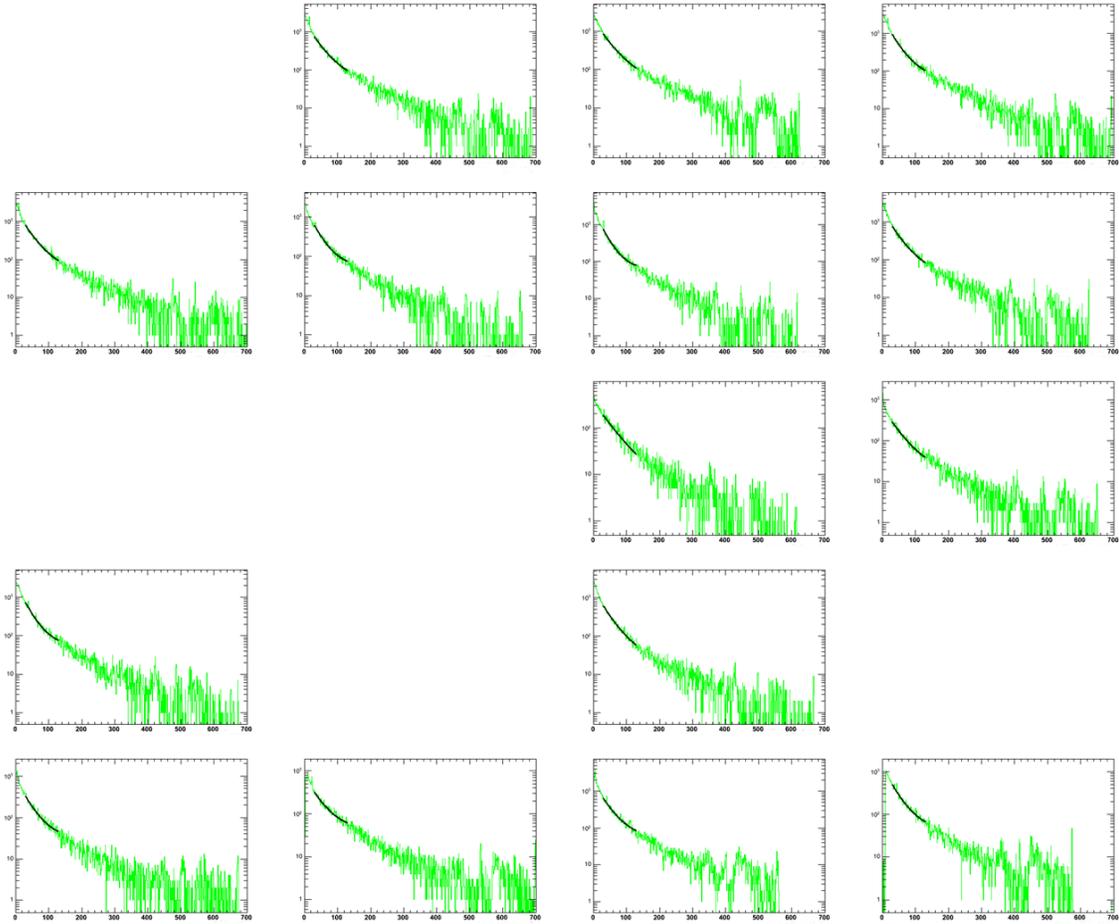


Fig. IV.5.: ADC distributions and fits with equation 4.1 (black line) for the 8th strip in each of the first 20 $BSMD-\phi$ modules. Empty spaces correspond to dead strips.

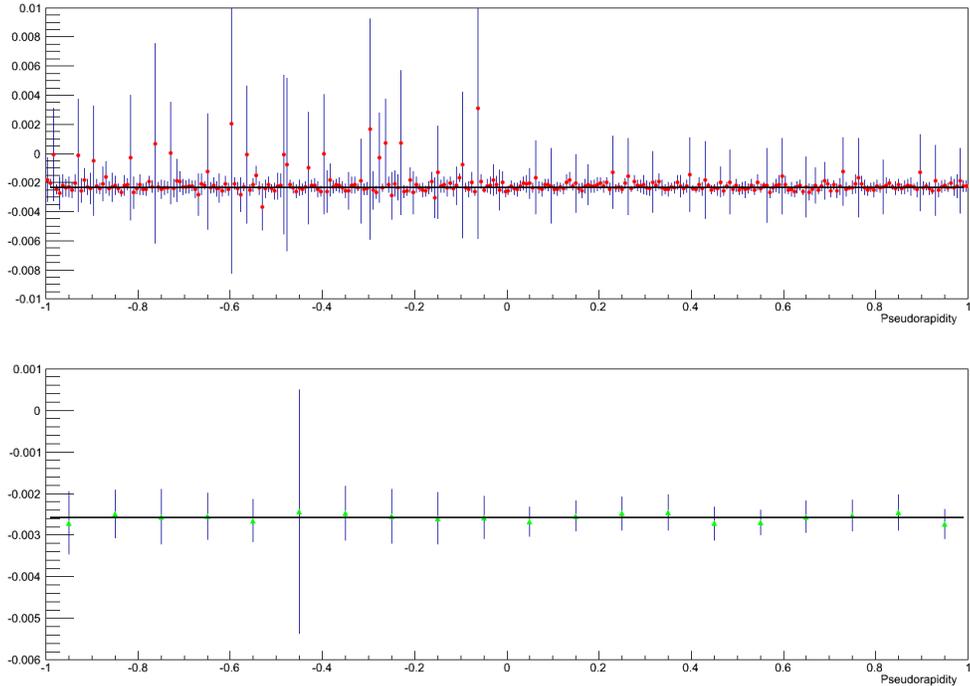


Fig. IV.6.: α profile histogram for $BSMD-\eta$ (top) and $BSMD-\phi$ (bottom) - linear fit to extract α shown as black line.

profile histogram is then fit with a line to find the average value of this ratio to yield the values α_η and α_ϕ . These profiles are shown in Fig. IV.6.

After α is extracted from the linear fit, the strips are fit again, with a function that uses this constant, where the 2^{nd} parameter, P_1 is taken as the strip gain (Fig. IV.7).

$$e^{(P_0+P_1(x+\alpha x^2))} \quad (4.2)$$

The shape of the $BSMD-\eta$ gains (Fig. IV.7) corresponds to the shape expected (from simulation) due to the natural acceptance distribution of electromagnetic particles across the calorimeter (and the higher than average voltage in the the modules in which the 4 bins separated from the bulk of the other bins in the plot correspond

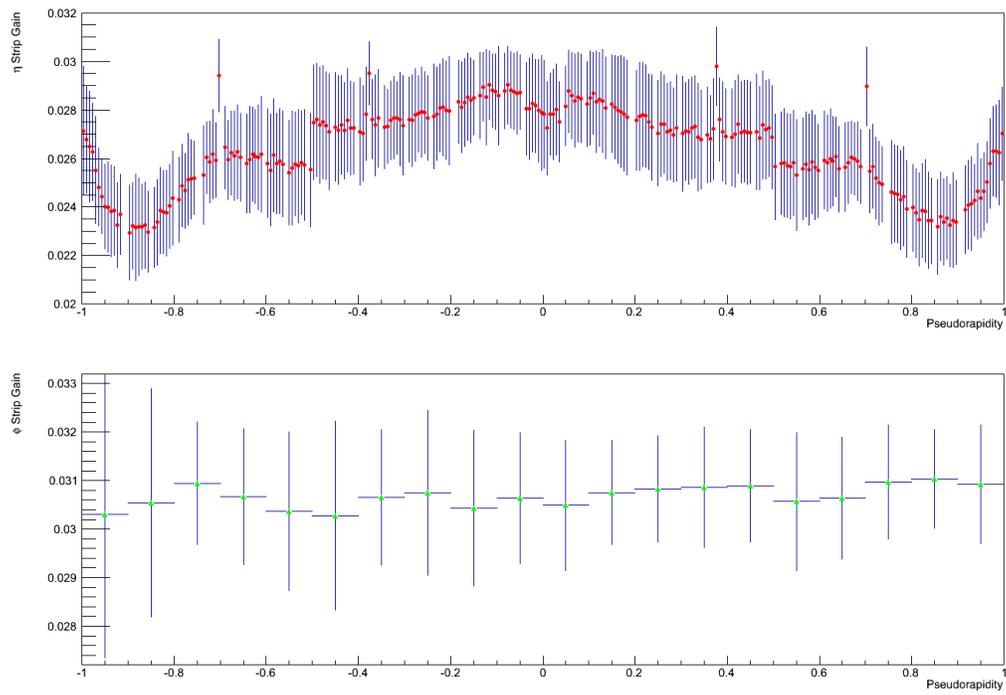


Fig. IV.7.: P_1 (strip gain) profile histogram before calibration for $BSMD$ - η (top) and $BSMD$ - ϕ (bottom).

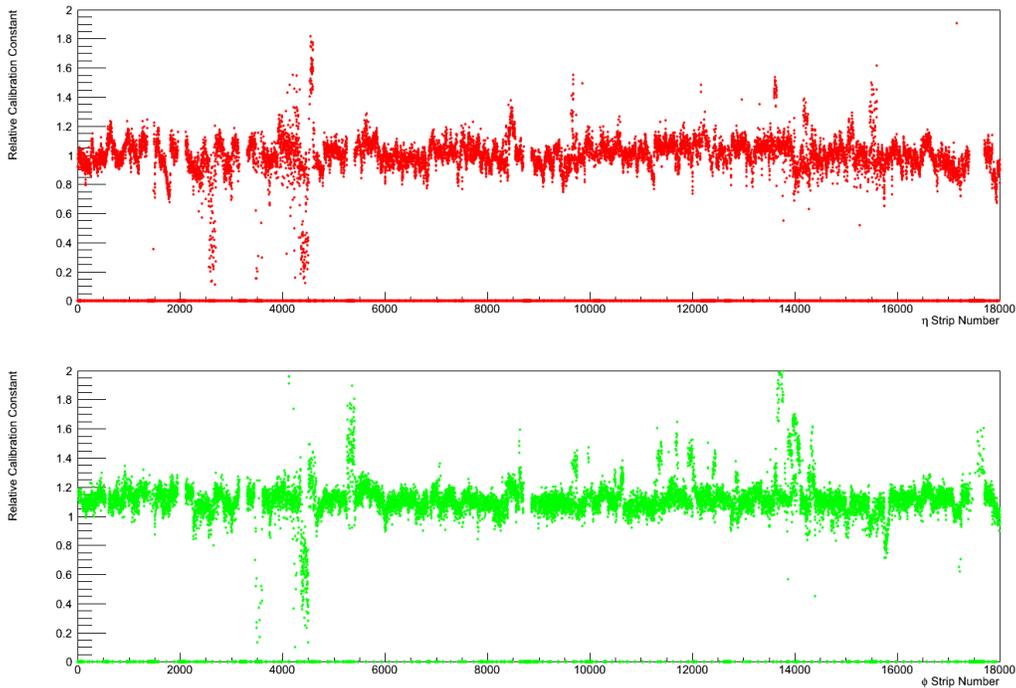


Fig. IV.8.: Calibration constants for $BSMD-\eta$ (top) and $BSMD-\phi$ (bottom)

to). This shape is used as the ideal gain distribution in $BSMD-\eta$; in the $BSMD-\phi$ however, a pseudorapidity dependence is not expected, and therefore the ideal gain value is taken as a constant (0.03) across all 20 pseudorapidity bins. The relative calibration constants for all 36,000 strips are calculated by dividing the extracted gain by the ideal gain; these calibration constants are shown as a function of strip number in Fig. IV.8. The constants are then applied to the strips and their effect on the strip gain tested.

IV.1.2. BSMD Strip Gains After Calibration

After applying the calibration constants to the ADC values of each strip, the new calibration can be tested by fitting the new ADC values with the same functional

form as equation 4.2. The new extracted gains can then be compared to determine if they are closer to the ideal gain than they were pre-calibration (the strips that did not get closer, or that got worse are assigned a calibration constant of 0 in the generation of the final constants). In total, 86% of the *BSMD- η* , and 78% of the *BSMD- ϕ* strips were successfully calibrated. Profile histograms for the gains (after calibration) are shown in Fig. IV.9. Figure IV.10 illustrates the improvement in the detector after calibration, by isolating the RMS values of the gains before and after calibration, showing a clear reduction in the magnitude in the latter case. The reduced spread on the gain RMS is important for direct/decay photon discrimination, which is described in the following section.

IV.2. Direct/Decay Photon Discrimination

Above 5.5 *GeV/c* the opening angle between the two photons resulting from the symmetric decay of a π^0 is less than 0.05 radians, and therefore these photons likely hit the detector within the same BEMC tower (dimensions 0.05 x 0.05 rad); and will be impossible to distinguish (using this detector alone), from a single photon. This ability to distinguish between direct and two close decay photons is essential to this analysis, so the BSMD is used to provide additional spatial information about the electromagnetic shower.

Electromagnetic showers are identified in the detector with the help of a clustering algorithm. The clustering algorithm used in this analysis was designed by A.M. Hamed and is documented in his dissertation [60]. The algorithm starts at a *BSMD- η* strip and compares the energy of that strip with the energy of the 7 preceding strips, and the energy of the 7 strips that follow; if the energy of each of these 14 strips is less than the energy of the first strip (the cluster seed), then the algorithm

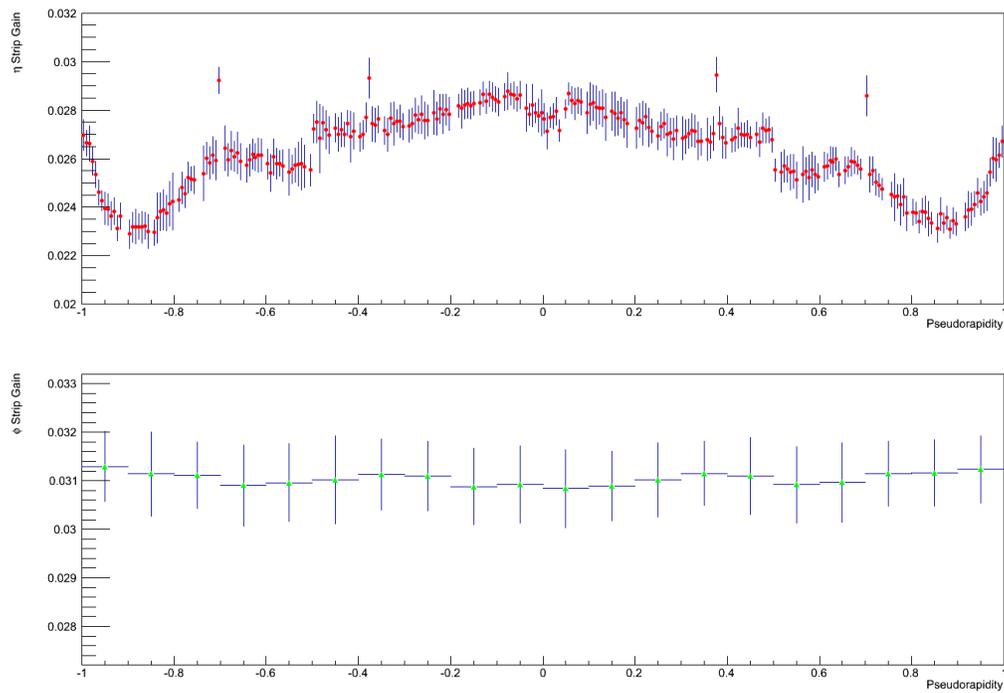


Fig. IV.9.: P_1 (strip gain) profile histogram after calibration for $BSMD-\eta$ (top) and $BSMD-\phi$ (bottom). Notice the reduction in the RMS as compared to figure IV.7. See figure IV.10 for a plot of these RMS values.

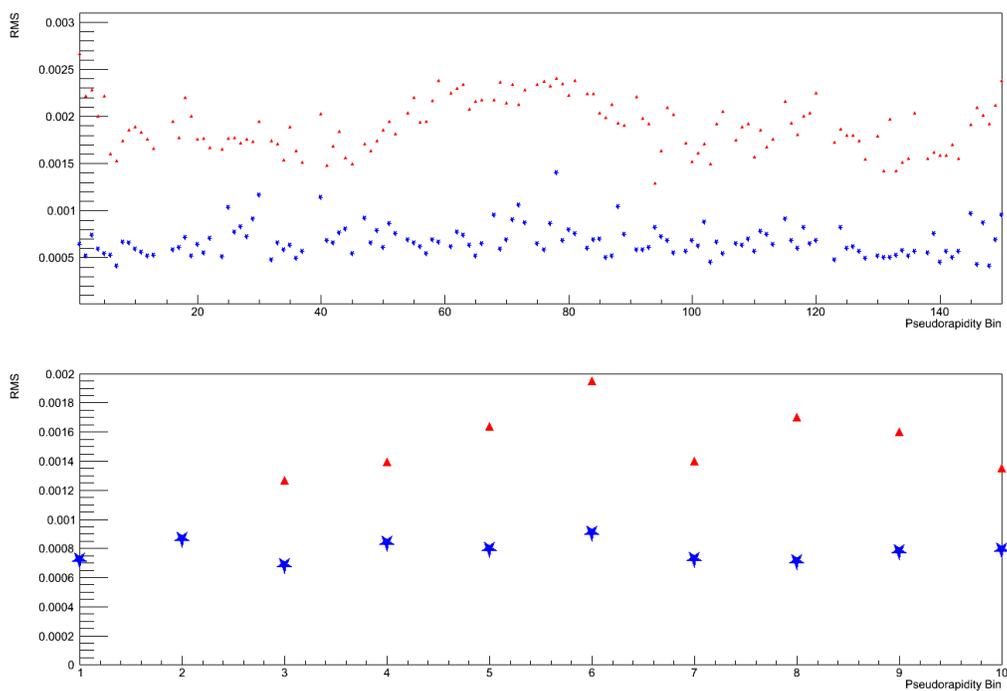


Fig. IV.10.: Gain RMS before (triangles) and after (stars) calibration for $BSMD-\eta$ (top) and $BSMD-\phi$ (bottom).

identifies that collection of 15 strips as a *BSMD- η* cluster. The algorithm then looks in the same region in *BSMD- ϕ* and tries to identify a similarly defined ϕ cluster, if a cluster is found, the algorithm then identifies the BEMC tower in which the cluster lies and uses the energy of this tower as the cluster energy. The distribution of the percentage of the cluster energy in each of the 15 strips, when plot versus the position of that strip relative to the cluster seed (which has a position of 0) is called the Transverse Shower Profile (TSP) of that electromagnetic shower. In principle, the TSP should be qualitatively different for a single photons, than for two photons that hit the detector in the same tower. Figure IV.11 shows this difference by looking at the TSP for Monte-Carlo generated electrons (the BSMD produces a similar response for electrons as photons) and π^0 s simulated (one electron or π^0 per event) in the STAR detector using the geometry of the detector for Run 7.

The difference between the two TSPs can be exploited with a quantitative cut that separates a sample of data into two sets, a γ -rich and a π^0 -rich set. This is done by inputting the strip energies into equation 4.3[37], where e_i and r_i are the energy of the strip and the distance of the strip from the cluster seed (respectively); the value 1.5 was chosen (from a MC simulation analysis) because it provided the best separation between electrons and π^0 s.

$$\frac{E_{cluster}}{\sum_i e_i r_i^{1.5}}. \quad (4.3)$$

A diagram of this quantity is shown in Fig. IV.12, plotted are the embedded π^0 s and γ s distributions; acceptable cuts generate a 65 - 70% pure γ -rich sample and a 95% pure π^0 -rich sample.

The TSP for electrons in data (from all three collision systems Au+Au, d+Au and $p + p$), is not as narrow as expected from simulation, this was thought to be due to the uncalibrated BSMD; a final test of a calibration of that detector therefore, is

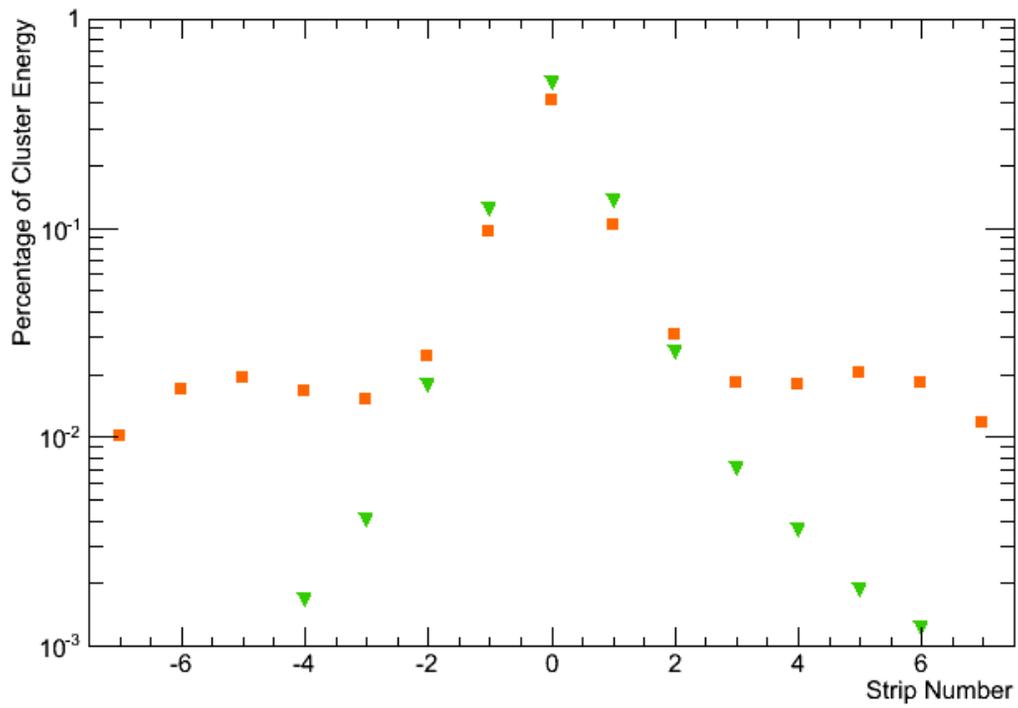


Fig. IV.11.: *BSMD*- η Monte-Carlo simulated Transverse Shower Profile (TSP) for electrons (triangles) and π^0 s (squares) with $6.0 \leq p_T \leq 8.0 \text{ GeV}/c$.

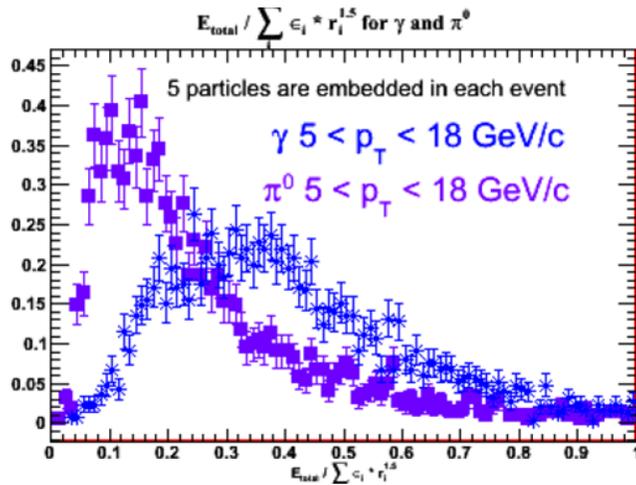


Fig. IV.12.: Transverse shower profile quantity for embedded π^0 s and γ s. In central Au+Au, cuts on this quantity yield a 65 - 70% pure γ -rich sample and a 95% pure π^0 -rich sample.

to compare the electron TSP before and after calibration. This comparison is shown in Fig. IV.13; the detector calibration reduces the width of the TSP, but not to the level of the MC simulation. This suggests that there are other effects on the width of the TSP than are included in simulation.

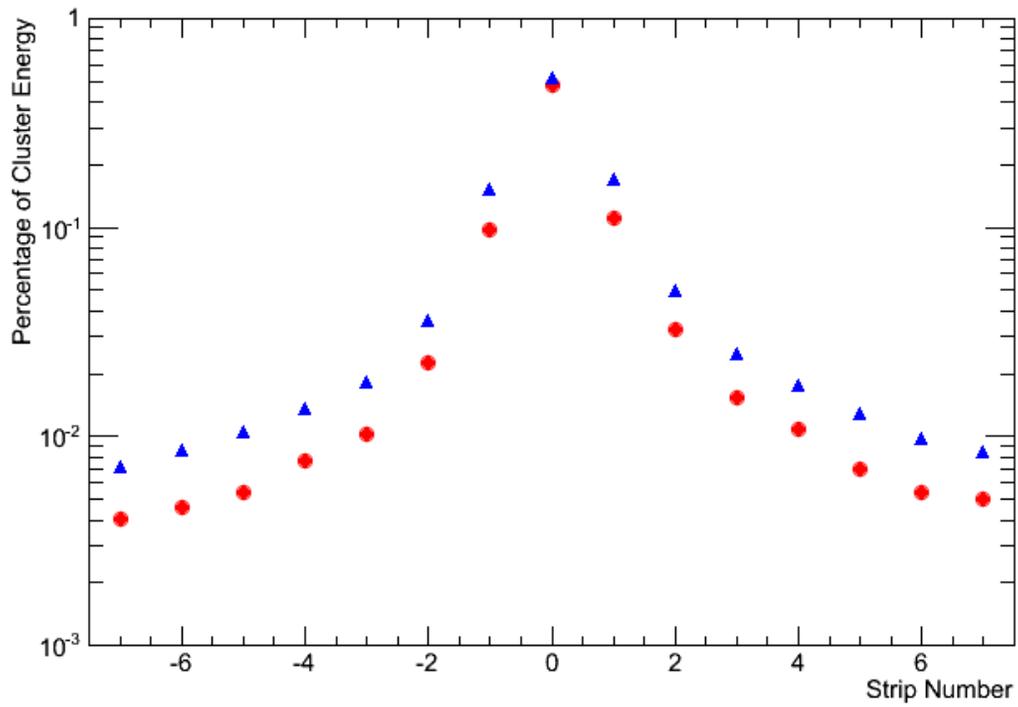


Fig. IV.13.: *BSMD*- η electron Transverse Shower Profile (TSP) from the Au+Au 2007 L2Upsilon trigger set before calibration (triangles) and after calibration (circles) with $6.0 \leq p_T \leq 8.0 \text{ GeV}/c$.

CHAPTER V

DATA ANALYSIS: AZIMUTHAL 2-PARTICLE CORRELATIONS

In this chapter, the details of the two-particle correlation analysis are discussed. The chapter starts with an overview of the two-particle correlation algorithm, next, Sec. V.2 deals with specific analysis cuts applied to both the photon triggers and the associated tracks, as well as an outline of the method of pair acceptance correction (a procedure that corrects for the finite detector acceptance), and ends with a brief discussion of single-particle efficiency correction. In Sec. V.3, the v_2 background subtraction and the ridge-yield determination methods are explained in detail. Finally, the method of statistical and systematic error determination are outlined.

V.1. Two-Particle Correlation Technique

V.1.1. Overview of Two-Particle Correlations

Two-particle correlations reveal the angular relationship between particles in a sample of events; they display the frequency of pairs as a function of angular pair separation distance. These correlations are used as an indirect method to study di-jets, as they measure jet-particle production on a statistical basis (averaged over many events), and do not require event-by-event jet identification.

The algorithm is the same for all data sets. The event is first classified into one of 22 vertex bins of equal width (from -55 cm to 55 cm), because of the need for pair acceptance correction (see Sec. V.2.2). Only events meeting the selection criteria in Sec. V.2.1 are selected. Next, the highest p_T trigger (that passed these criteria) for that event is selected as the trigger particle, then the $\Delta\eta$ and $\Delta\phi$ values for this trigger and each associated particle which pass the cut for associated particles are

calculated as follows:

$$\Delta\eta = \eta^{assoc.} - \eta^{trig.} \quad (5.1)$$

$$\Delta\phi = \phi^{assoc.} - \phi^{trig.} \quad (5.2)$$

The $\Delta\eta$ and $\Delta\phi$ values distributions are filled in a histogram (as described in Sec. V.2.1), and the final distribution is corrected by the single associated particle efficiency, and by the number of triggers (so no correction by the trigger efficiency is needed).

V.2. Analysis Details and Corrections

V.2.1. Data Selection, Analysis Cuts and Histogram Binning

Data discussed in this work are from Au+Au collisions at $\sqrt{S_{NN}} = 200 \text{ GeV}$, detected with the STAR detector, from RHIC's Run 7 (2006 - 2007) and Run 10 (2009 - 2010). These data satisfy either a High Tower (HT) trigger or both the High Tower and the L2Gamma trigger. In Run 7, the BHT2 trigger is the HT trigger used; this requires a ZDC coincidence, and a high energy tower in the BEMC ($E_T > 5.5 \text{ GeV}/c$, 5.75 in some cases). The L2Gamma set in this run satisfies the BHT2 but imposes a higher E_T cut on the cluster (of 1 or 2 towers) of $8.0 \text{ GeV}/c$.

All events accepted for this analysis have a well-defined vertex, within 55 cm of the center of the TPC (along the z-axis) and are in the events with the 10% most central impact parameter values. Centrality, in this case, is measured by Reference Multiplicity, and in Run 7, the 10% most central events are defined as those with a reference multiplicity greater than or equal to 399, and in Run 10, the cut is 375. The lower reference multiplicity cut in Run 10, can be explained by the dead sector in the TPC during this run (see figure V.2, bottom left and right plots, on page 99).

In addition to the event-level cuts, there are also cuts on the photon candidates accepted as triggers, and on the charged tracks accepted as associated particles. For the triggers, the following cuts are made;

1. *BSMD Threshold Cut*: The photon candidate must deposit at least $0.25 \text{ GeV}/c$ in the *BSMD- η* and the *BSMD- ϕ* cluster seed (see Chapter III).
2. *Charge-Rejection Cut*: No track with p_T higher than $1.375 \text{ GeV}/c$ for (BHT2) and $2.0 \text{ GeV}/c$ for (L2Gamma) is allowed to point to the tower that triggered the event. This cut is put into place to eliminate electrons, positrons, and high- p_T hadrons from the trigger sample, as they deposit energy in the calorimeter and leave charged tracks in the TPC.
3. *Trigger p_T Cut*: The trigger p_T is restricted to $5.5 - 8.0 \text{ GeV}/c$ for BHT2 data, and $8.0 - 16.0 \text{ GeV}/c$ for L2Gamma data.
4. *Tower η Cut*: The $|\eta|$ of the tower of the trigger particle must be less than 0.9.
5. *Triggers Per Event Cut*: Only one trigger is selected per event. This is the trigger with the highest p_T (among the triggers that passed all trigger cuts).
6. *Hot Towers Cut*: All towers with hit frequency greater than 5σ (2σ in run 10) above the mean are masked. (See Appendix A for list of masked towers)

For the associated tracks, the following cuts are made;

1. *Track Flag Cut*: Only good tracks from the TPC (STAR Track Flag = 301) and, in run 7, the SVT (STAR Track Flag = 601) are accepted.
2. *Fit Points Cut*: The number of track fit points exceeds 20.

3. *DCA Cut:* The track Distance of Closest Approach (DCA) to the primary vertex is less than 3.0.
4. *Fit Point Ratio Cut:* The ratio of the track fit points to the possible points is greater than 0.52.
5. *Track p_T Cut:* The track p_T is greater than or equal to 2.0 GeV/c and is less than the trigger p_T .
6. *Track η Cut:* The $|\eta|$ is less than or equal to 1.0.

The triggers and tracks that pass these cuts are used to calculate the $\Delta\eta$ and $\Delta\phi$ values which are filled in a 2D histogram (ROOT Class TH2D), with $\Delta\eta$ filled in the y-axis bins and $\Delta\phi$ filled in the x-axis bins (see Fig. V.1 and Fig. V.2). There are 96 $\Delta\eta$ bins spanning from -2.00 on the left-edge of bin 1 (bin numbering begins at 1 in ROOT) to +2.00 on the right-edge of bin 96; giving a $\Delta\eta$ bin width of 0.04167. For $\Delta\phi$, there are 48 bins spanning from -3.14159 on the left-edge of bin 1 to +3.14159 on the right-edge; giving a bin width of 0.1309. The z-axis in all 2D histograms is $1/N_{trig}(d^2N/d\Delta\phi d\Delta\eta)$ and $1/N_{trig}(dN/dx)$ for 1D histograms (where x is either η or ϕ).

V.2.2. Pair Acceptance Correction

As discussed in Chapter II, the STAR BEMC (Sec. III.4) and TPC (Sec. III.3) have pseudo-rapidity coverage from $|\eta| \leq 1.0$. However, their pair acceptance in $\Delta\phi$ and $\Delta\eta$ (the ratio of detected to produced particles) varies over this range. The largest acceptance (~ 1.0) is found at the center of the detector at $\eta = 0$, and the acceptance decreases as you move outward from the center to its lowest value at the edges of the

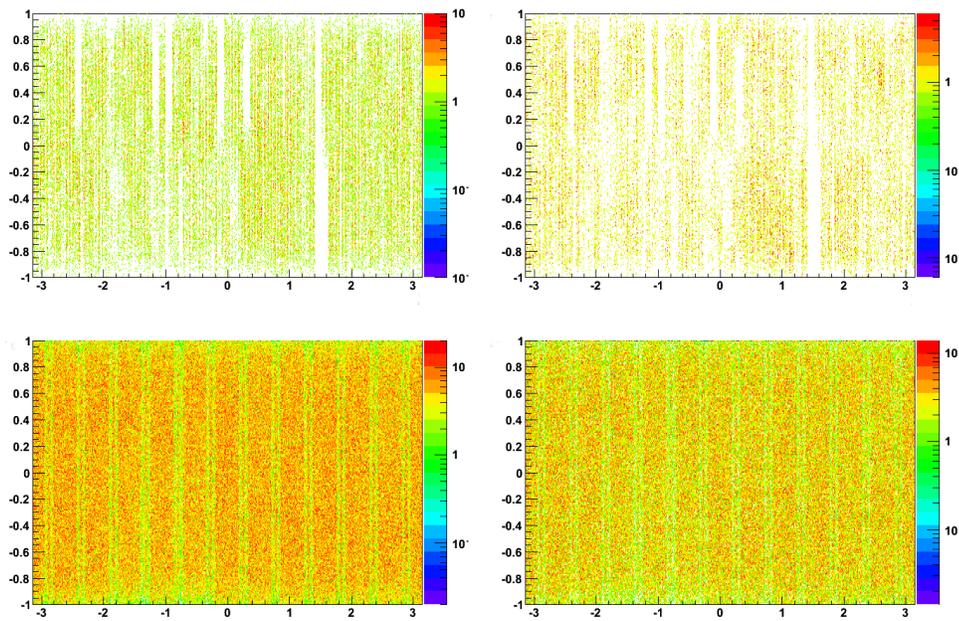


Fig. V.1.: Run 7 $\eta - \phi$ distributions for mixing. For γ -rich trigger(top left), π^0 -rich trigger(top right), associated tracks for γ -rich triggers (bottom left), associated tracks for π^0 -rich triggers (bottom right) for the 5.5 - 7.0 GeV/c bin.

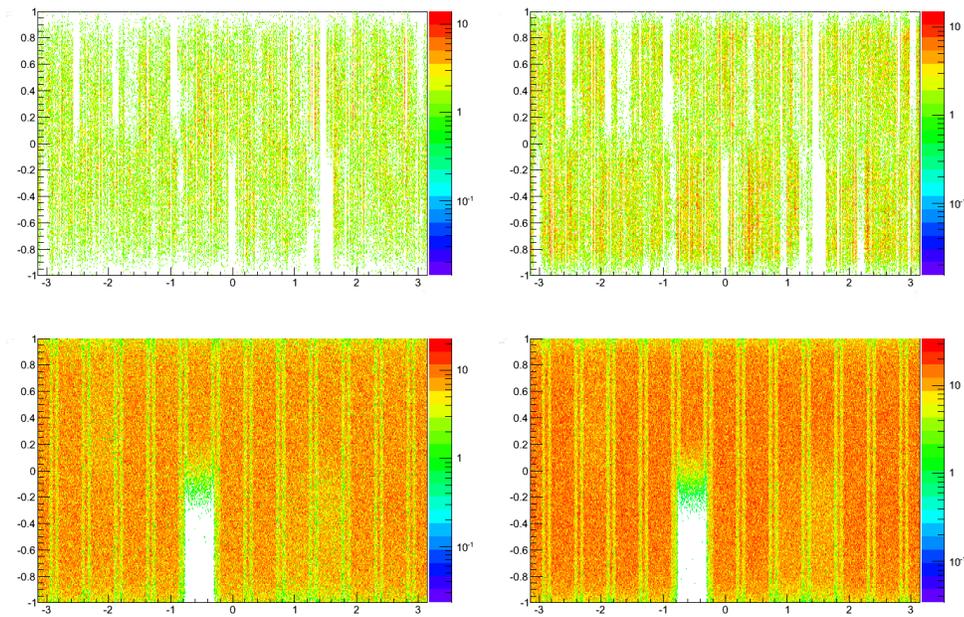


Fig. V.2.: Run 10 $\eta - \phi$ distributions for mixing. For γ -rich trigger(top left), π^0 -rich trigger(top right), associated tracks for γ -rich triggers (bottom left), associated tracks for π^0 -rich triggers (bottom right) for the 5.5 - 7.0 GeV/c bin.

Table V.1.: The five p_T bins, their corresponding p_T ranges and triggers.

p_T Bin	p_T Range (GeV/c)	Trigger (2007)	Trigger (2010)
1	5.5 - 7.0	BHT2	BHT
2	7.0 - 8.0	BHT2	BHT
3	8.0 - 10.0	L2Gamma	L2Gamma
4	10.0 - 12.0	L2Gamma	L2Gamma
5	12.0 - 16.0	L2Gamma	L2Gamma

detector at $|\eta| = 1.0$. These detectors have a near uniform acceptance in ϕ with the exception of the 0 acceptance in the boundaries between the ϕ sectors in the TPCs.

Because of the unique acceptance of the STAR TPC and BEMC, any data analysis dependent on an accurate measure of relative particle multiplicities, in different sectors of the $\eta - \phi$ space (such as a correlation analysis), will be biased towards particles produced near the center of the detector volume (where the acceptance approaches unity). Such an analysis will therefore need to be corrected to account for this varying acceptance. This correction is called pair acceptance correction, because it uses a distribution of uncorrelated pairs of particles to correct for the acceptance shape.

Mixed pairs are generated by randomly sampling separate histograms of trigger and associated particle $\eta - \phi$ distributions, filled in 22 vertex bins of 5 cm width (from -55 to 55 cm) and in the 5 p_T bins described in table V.1. Both the trigger and associated distribution histograms are filled simultaneously with the real pairs, so they are subject to the same trigger and associated cuts outlined in Sec. V.2.1.

A trigger is then randomly selected, from the $\eta - \phi$ distributions, in the p_T bin

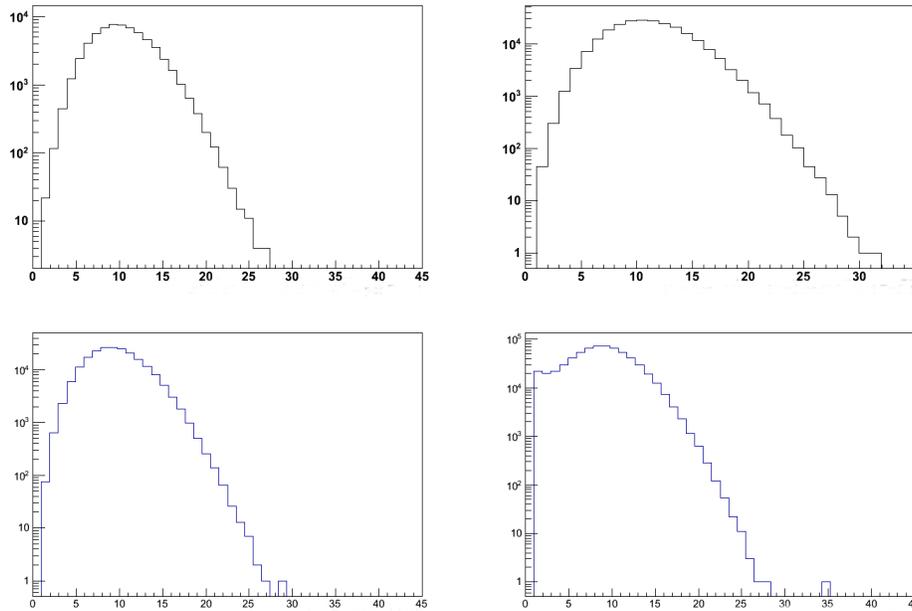


Fig. V.3.: The number of associated charged-particles per event for trigger sets "L2gamma 2007" (top left), "HighTower 2007" (top right), "L2gamma 2010" (bottom left), and "HighTower 2010" (bottom right).

in which the mixed pair would be generated. Then the $\Delta\eta$ and $\Delta\phi$ are calculated, by mixing this trigger with randomly chosen associated particles from the corresponding associated p_T bin. The number of associated particles mixed with the trigger is sampled from a histogram (Fig. V.3) filled with the number of associated particles for each real trigger. The average number of associated particles is ~ 10 .

A total of 100 million triggers are mixed with the randomly selected number of associated particles in each of the 5 p_T bins for each trigger sample. The mixed pair distribution (see Fig. V.4 and V.5) is then normalized to give a maximum acceptance of 1.0, and used to correct the raw correlation; by dividing the raw correlation by the acceptance histogram. Uncorrected and corrected correlations for the first p_T bin (5.5

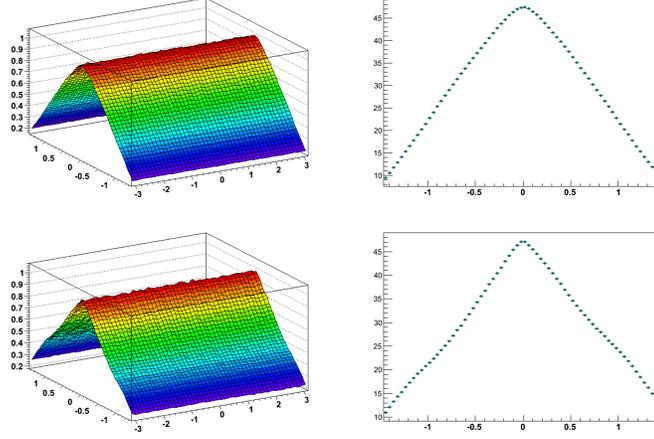


Fig. V.4.: Run 7 mixed-pair(acceptance) distributions for γ -rich triggered 2D(top left), its $\Delta\eta$ projection(top right), π^0 triggered 2D(bottom left), and its $\Delta\eta$ projection(bottom right) for the 5.5 - 7.0 GeV/c bin.

- 7.0 GeV/c), for both γ and π^0 triggers are shown in figures V.6 and V.7 (Run 7), and in Fig. V.8 and V.9 (Run 10). Figures for all the p_T bins are found in Chapter V.

V.2.3. Single Particle Efficiency Correction

The yield of correlated trigger and associated hadron pairs in a given region of the $\Delta\phi$ - $\Delta\eta$ phase-space, is dependent on the distribution of charged hadrons in that region. This distribution reflects the real particle distribution, modified by the reconstruction efficiency of the detector (specifically the TPC (section III.3)). Since all final correlation distributions in this analysis are scaled (divided) by the number of reconstructed triggers, only the efficiency of the associated hadrons affects the correlation yield in a given region of the phase-space.

The efficiency correction used in this analysis, is a parameterization, taken from

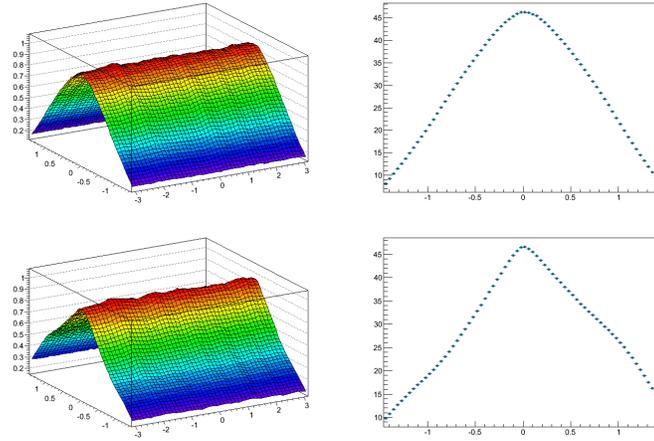


Fig. V.5.: Run 10 mixed-pair(acceptance) distributions for γ -rich triggered 2D(top left), its $\Delta\eta$ projection(top right), π^0 triggered 2D(bottom left), and its $\Delta\eta$ projection(bottom right) for the 5.5 - 7.0 GeV/c bin.

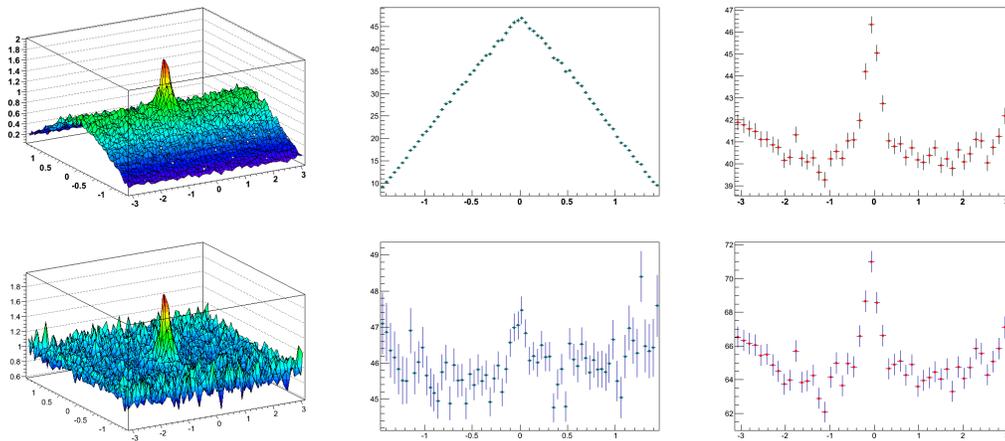


Fig. V.6.: γ -rich triggered Run 7 uncorrected correlations. 2D(top left), its $\Delta\eta$ projection(top middle), its $\Delta\phi$ projection(top right) and the acceptance-corrected correlations for γ -rich triggered 2D(bottom left), its $\Delta\eta$ projection(bottom middle), its $\Delta\phi$ projection(bottom right) for the 5.5 - 7.0 GeV/c bin.

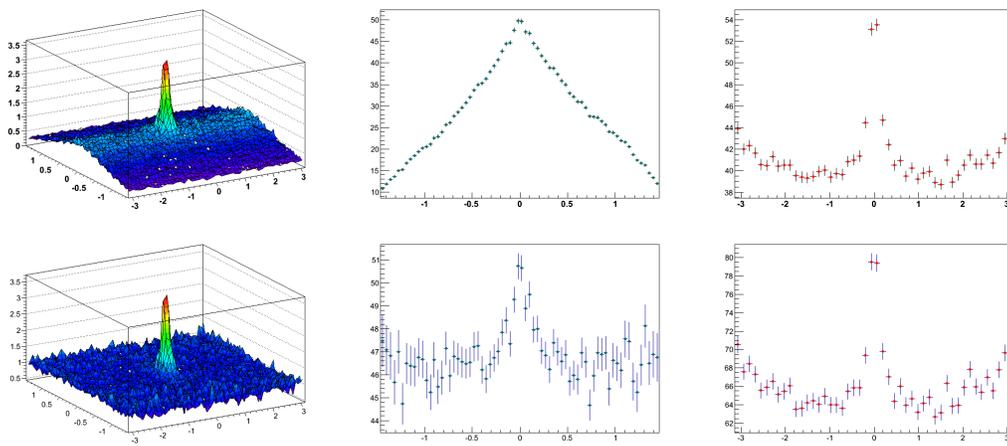


Fig. V.7.: π^0 -triggered Run 7 uncorrected correlations. 2D(top left), its $\Delta\eta$ projection(top middle), its $\Delta\phi$ projection(top right) and the acceptance-corrected correlations for π^0 triggered 2D(bottom left), its $\Delta\eta$ projection(bottom middle), its $\Delta\phi$ projection(bottom right) for the 5.5 - 7.0 GeV/c bin.

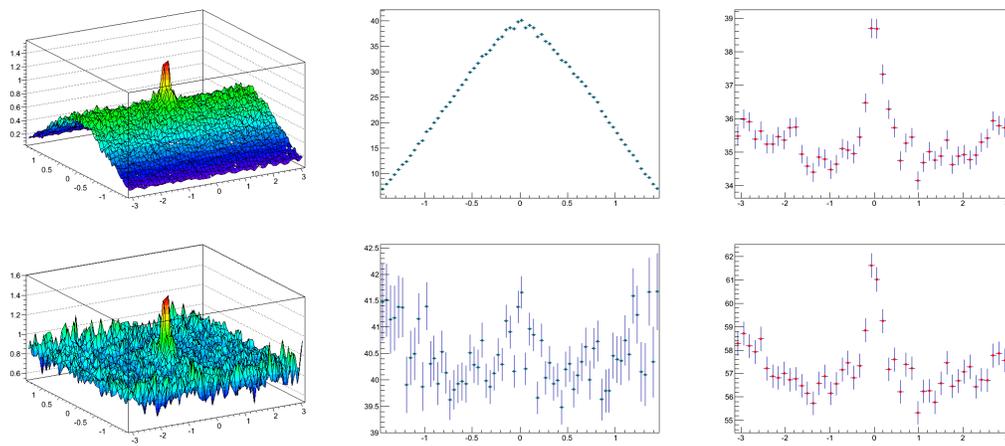


Fig. V.8.: γ -rich triggered Run 10 uncorrected correlations. 2D(top left), its $\Delta\eta$ projection(top middle), its $\Delta\phi$ projection(top right) and the acceptance-corrected correlations for γ -rich triggered 2D(bottom left), its $\Delta\eta$ projection(bottom middle), its $\Delta\phi$ projection(bottom right) for the 5.5 - 7.0 GeV/c bin.

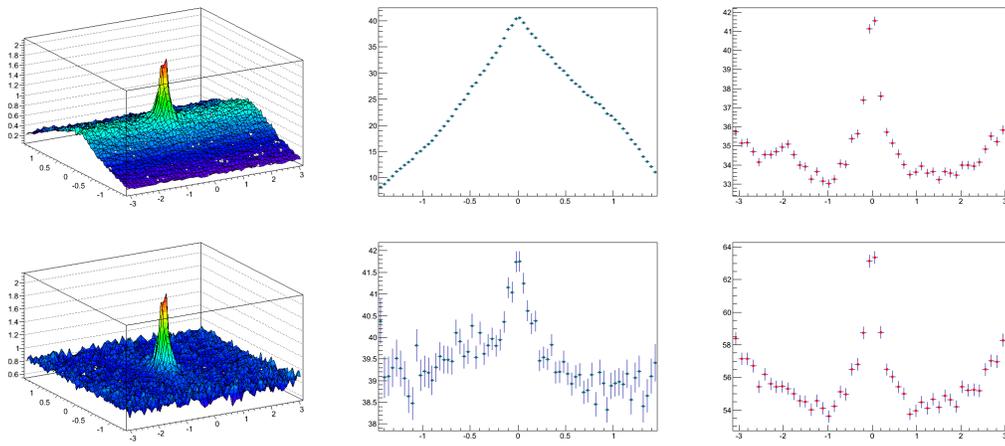


Fig. V.9.: π^0 -triggered Run 10 uncorrected correlations. 2D(top left), its $\Delta\eta$ projection(top middle), its $\Delta\phi$ projection(top right) and the acceptance-corrected correlations for π^0 triggered 2D(bottom left), its $\Delta\eta$ projection(bottom middle), its $\Delta\phi$ projection(bottom right) for the 5.5 - 7.0 GeV/c bin.

a study which made use of data and simulation to determine the charged-hadron efficiency. This efficiency was calculated under the assumption that the detector response to unidentified charged-hadrons is the same as the detector response to charged pions. This is a reasonable assumption because charged pions are the most abundantly produced charged-hadrons in relativistic ion collisions. Furthermore, the response of the protons (also abundantly produced in these collisions) is similar to that of the pions.

The first step in this efficiency analysis, is to simulate the interaction of pure single-tracks, with the specific geometry and detector material of the STAR TPC. This simulation is done using GEANT [61] [62], a software package that contains libraries of the cross sections for the interactions of different types of particles in various materials, in a specific 3D detector shape (which is encoded by the user). Input particle distributions are Monte-Carlo sampled, and each type of particle (charged pions in this instance) is simulated as it passes through the STAR detector system. All interactions of the particle (and its daughters) with the detector volume, and any change in its energy or trajectory is recorded. The particle's energy loss in the TPC, can then be determined.

In the next step, the single particle Monte-Carlo sampled signals are added to the distribution of particles in a real event in a process called embedding. For this analysis, particles are embedded into Run 7 data files. The STAR track reconstruction algorithm is then run over this embedded event, and the reconstructed hits and tracks are associated with the simulated hits and tracks. One of the parameters used to measure the hit reconstruction efficiency is the distance between the reconstructed and simulated hit. For tracks, one of the parameters used to study the efficiency is the number of reconstructed hits for that track.

The results of this study show that the reconstruction efficiency of single particles

depends on the collision system, center-of-mass energy, p_T , and centrality. For this analysis, a single centrality bin, in a single collision system, for a single center-of-mass energy is used, and since the efficiency is essentially flat for $p_T > 2 \text{ GeV}/c$ (the lowest p_T accepted in this analysis); a single efficiency factor is used for each run year: 0.85 in Run 7 with Run 10 assumed to have the same efficiency. The correlation yield is then uniformly scaled (divided) by this efficiency.

V.3. Ridge Yield Extraction

V.3.1. v_2 Subtraction

In addition to the correction for the finite detector acceptance, the raw correlations must also be background corrected to remove non jet-like correlations. If this background only consisted of uncorrelated pairs, a simple background constant could be subtracted from the correlation histograms. However, all particles are correlated to the reaction plane, which creates a $\cos(2\Delta\phi)$ modulation of the background. This background, $B(\Delta\phi, p_T)$, is described[8] by Eq. 5.3; where $\langle v_2^{trigger} v_2^{associated} \rangle$ is v_2 per pair, ϕ is the azimuthal angle, and C is a constant determined from normalization to the $\Delta\phi$ projection of the correlation, see Sec. V.3.2 for details.

$$B(\Delta\phi, p_T) = C(1 + 2\langle v_2^{trigger} v_2^{associated} \rangle \cos 2\Delta\phi) \quad (5.3)$$

This modulation is a function of the azimuthal distribution, of the p_T of the trigger and the associated particles, and of the centrality. In STAR, there is a common parameterization of this modulation [63] that is used in this analysis. In this parameterization, $\langle v_2^{trigger} v_2^{associated} \rangle$ is approximated as $\langle v_2^{trigger} \rangle \langle v_2^{associated} \rangle$, and the modulation is calculated per centrality bin (see Table V.2, and Fig. V.10).

Ideally, it is most accurate to perform this subtraction on a pair-wise basis.

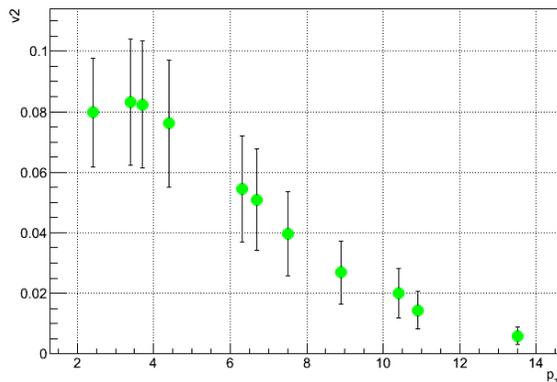


Fig. V.10.: v_2 values for the associated charged-hadrons (first 3 bins) and for trigger particle (assuming a π^0). Errors are systematic.

However, because of the large systematic errors on $\langle v_2^{trigger} \rangle$ and $\langle v_2^{associated} \rangle$, this is not practical. The constant C is fixed using an assumption of zero yield at minimum (ZYAM) [64]. Two methods of fixing the constant are outlined in the following section on ridge yield extraction.

V.3.2. Yield Extraction

V.3.2.1. Yield Extraction Method 1

Method 1 depends on the assumption that the near-side jet yield is contained in $|\Delta\eta| \leq 0.7$ (because of histogram binning, the value used in this analysis is 0.7083). Any non-zero yield (after acceptance and background subtraction) in the $\Delta\phi$ near-side region ($|\Delta\phi| \leq 0.7854$) is then assumed to be the ridge yield.

The first step in this method therefore, is to project the range $0.7083 \leq |\Delta\eta| \leq 1.4167$ onto the full $\Delta\phi$ to create a 1D $\Delta\phi$ correlation histogram (Fig. V.11). The 'minimum' range used for ZYAM assumption is $0.9163 \leq |\Delta\phi| \leq 1.309$ (bins 15 - 17

Table V.2.: $\langle v_2^{trigger} \rangle$ and $\langle v_2^{associated} \rangle$ values for all 5 p_T bins.

p_T Bin	Mean p_T (GeV/c)	$\langle v_2^{trigger} \rangle$	$\langle v_2^{associated} \rangle$
1	6.2	0.0546	0.0802
2	7.4	0.0397	0.0803
3	8.8	0.0270	0.0804
4	10.8	0.0144	0.0806
5	13.4	0.0060	0.0809

and 32 - 34) and their v_2 modulation is scaled by the constant necessary to reduce the yield in this region to zero when the v_2 modulation is subtracted.

$$B_{\Delta\phi}^{m1}[-0.7854, 0.7854] \equiv b_{\Delta\phi}^{m1} \int_{-0.7854}^{0.7854} d\Delta\phi (1 + 2\langle v_2^{trigger} \rangle \langle v_2^{associated} \rangle \cos 2\Delta\phi) \Big|_{0.7083 \leq |\Delta\eta| \leq 1.4167} \quad (5.4)$$

After the v_2 modulation subtraction, the resulting background-corrected histogram is integrated in the range $|\Delta\phi| \leq 0.7854$, and this value is then scaled over the entire $\Delta\eta$ range ($|\Delta\eta| \leq 1.7$) to give the scaled integrated ridge yield.

$$Y_{ridge}^{m1} = \frac{3.5000}{1.4167} \left[\int_{-0.7854}^{0.7854} d\Delta\phi \frac{dN}{d\Delta\phi} \Big|_{0.7083 \leq |\Delta\eta| \leq 1.4167} - B_{\Delta\phi}^{m1}[-0.7854, 0.7854] \right] \quad (5.5)$$

V.3.2.2. Yield Extraction Method 2

Method 2 is the method used in the first published STAR ridge paper[10]. The first step in this method is to project $|\Delta\phi| \leq 0.7854$ onto $\Delta\eta$ to give a 1D histogram (Fig. V.12). This histogram is then integrated over $0.9583 \leq |\Delta\eta| \leq 1.4167$, to extract the

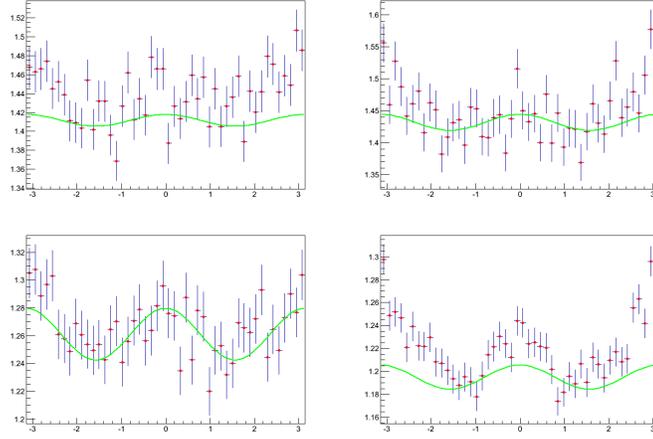


Fig. V.11.: Yield Extraction Method 1: $\Delta\phi$ projection ($0.7083 \leq |\Delta\eta| \leq 1.4167$) of corrected correlations (p_T bin 1) showing the v_2 modulation (Eq. 5.3) that is subtracted, for triggers: γ -rich 2007(top left), π^0 2007(top right), γ -rich 2010(bottom left), and π^0 2010(bottom right).

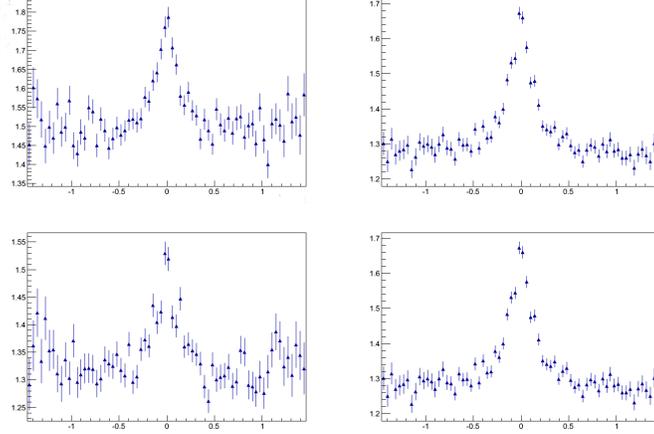


Fig. V.12.: Yield Extraction Method 2: $\Delta\eta$ projection ($|\Delta\phi| \leq 0.7854$) of corrected correlations (p_T bin 1) used to calculate $b_{\Delta\eta}^{m2}$, for triggers; γ -rich 2007(top left), π^0 2007(top right), γ -rich 2010(bottom left), and π^0 2010(bottom right)

flat background. This integral value is then scaled to represent the interval over $|\Delta\eta| \leq 1.4167$ by the value of $b_{\Delta\eta}^{m2}$, which is defined as

$$b_{\Delta\eta}^{m2} = \frac{2.8334}{0.9168} \left[\int_{-1.4167}^{-0.9583} d\Delta\eta \frac{dN}{d\Delta\eta} \Big|_{|\Delta\phi| \leq 0.7854} + \int_{0.9583}^{1.4167} d\Delta\eta \frac{dN}{d\Delta\eta} \Big|_{|\Delta\phi| \leq 0.7854} \right]. \quad (5.6)$$

The next step is to scale the v_2 modulation function described in method 1 to a $\Delta\phi$ 1D histogram that was created by projecting the $\Delta\eta$ range $|\Delta\eta| \leq 1.4167$ (Fig. V.13). ZYAM is assumed in the same range as previously described, the v_2 function is scaled, and then integrated over the range $|\Delta\phi| \leq 0.7854$. This integrated value is $B_{\Delta\phi}^{m2}$.

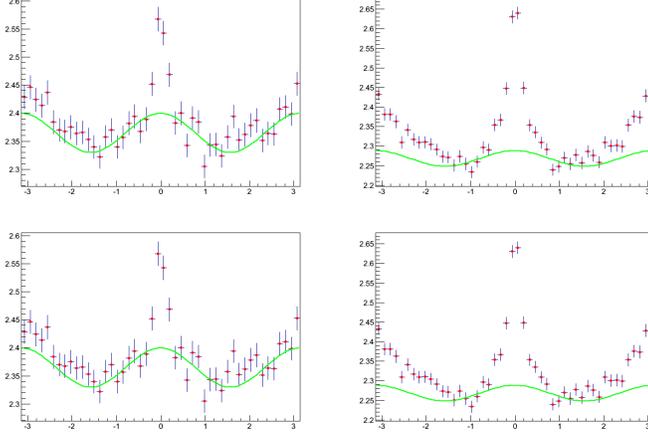


Fig. V.13.: Yield Extraction Method 2: $\Delta\phi$ projection ($|\Delta\eta| \leq 1.4167$) of corrected correlations (p_T bin 1) showing the v_2 modulation (Eq. 5.3), for triggers; γ -rich 2007(top left), π^0 2007(top right), γ -rich 2010(bottom left), and π^0 2010(bottom right).

$$B_{\Delta\phi}^{m2}[-0.7854, 0.7854] \equiv b_{\Delta\phi}^{m2} \int_{-0.7854}^{0.7854} d\Delta\phi (1 + 2\langle v_2^{trigger} \rangle \langle v_2^{associated} \rangle \cos 2\Delta\phi) \Big|_{|\Delta\eta| \leq 1.4167} \quad (5.7)$$

The ridge yield is then taken as $b_{\Delta\eta}^{m2} - B_{\Delta\phi}^{m2}$, and is scaled to the full $\Delta\eta$ range ($|\Delta\eta| \leq 1.7500$).

$$Y_{ridge}^{m2} = b_{\Delta\eta}^{m2} - B_{\Delta\phi}^{m2}[-0.7854, 0.7854] \quad (5.8)$$

V.4. Error Determination

V.4.1. Statistical Error

All correlation histograms are filled after the ROOT TH1::Sumw2 function is called. This function creates a structure to store the sum of the squares of the weights. The error per histogram bin is then computed as the square root of the sum of the squares of the weight for each bin. This bin error can then be accessed from the histogram object by calling the "GetBinError" function (if Sumw2 were not set, this function would return the square root of the contents of that bin).

Sections V.4.1.1 and V.4.1.2 describe the calculation of the statistical error using the bin numbers of the $\Delta\eta$ and $\Delta\phi$ projection histograms; it may be useful, therefore, to rewrite Eqs. 5.5, 5.6 and 5.8 as 5.9, 5.10 and 5.11(respectively), to show the calculation of the yield as a summation of bins. $\Delta\phi b$ ($\Delta\eta b$) followed by a number refers to that bin number in the $\Delta\phi$ ($\Delta\eta$) histogram:

$$Y_{ridge}^{m1} = \frac{3.5000}{1.4167} \times \left[\sum_{i=19}^{30} \Delta\phi ProjectionContent_{bin\ i} \Big|_{15 \leq \Delta\eta b \leq 32 \ \& \ 65 \leq \Delta\eta b \leq 82} - B_{\Delta\phi}^{m1}[\Delta\phi b19, \Delta\phi b30] \right] \quad (5.9)$$

$$b_{\Delta\eta}^{m2} = \frac{2.8334}{0.9168} \times \left[\sum_{i=15}^{25} \Delta\phi ProjectionContent_{bin\ i} \Big|_{19 \leq \Delta\phi b \leq 30} + \sum_{j=72}^{82} \Delta\phi ProjectionContent_{bin\ j} \Big|_{19 \leq \Delta\phi b \leq 30} \right] \quad (5.10)$$

$$Y_{ridge}^{m2} = b_{\Delta\eta}^{m2} - B_{\Delta\phi}^{m2}[\Delta\phi b19, \Delta\phi b30] \quad (5.11)$$

V.4.1.1. Method 1

The two sources of statistical error in the ridge yield determination for method 1 are the errors on the 6 bins used to set the ZYAM point for subtracting the v_2 function, and from the errors on the 12 bins over which the ridge yield is integrated. The functional form used to calculate the total error is;

$$\sigma_{Total}^{m1} = \sqrt{(\sigma_{Yield}^{m1})^2 + (\sigma_{B_{\Delta\phi}}^{m1})^2} \quad (5.12)$$

The values σ_{Yield}^{m1} and $\sigma_{B_{\Delta\phi}}^{m1}$ were determined from the bin errors on the $\Delta\phi$ correlation (see figure V.11, page 111). σ_{Yield}^{m1} was calculated as follows:

$$\sigma_{Yield}^{m1} = \frac{3.5000}{1.4167} \left[d\Delta\phi \sqrt{\sum_{i=19}^{30} \sigma_{bin\ i}^2} \right] \quad (5.13)$$

The first step in calculating $\sigma_{B_{\Delta\phi}}^{m1}$ is to add the errors on the 6 bins in quadrature, then divide by the number of bins, to obtain $\sigma_{b_{\Delta\phi}}^{m1}$:

$$\sigma_{b_{\Delta\phi}}^{m1} = \frac{1}{6} \sqrt{\sum_{i=15}^{17} \sigma_{bin\ i}^2 + \sum_{j=32}^{34} \sigma_{bin\ j}^2} \quad (5.14)$$

The mean value, m , of the absolute value of $\Delta\phi$ of the 6 bins is then calculated, and the v_2 function is evaluated at m to give the value $v_2^{m1}(m)$:

$$v_2^{m1}(m) = (1 + 2\langle v_2^{trigger} \rangle \langle v_2^{associated} \rangle \cos 2m) \Big|_{0.7083 \leq |\Delta\eta| \leq 1.4167} \quad (5.15)$$

Finally, $\sigma_{B_{\Delta\phi}}^{m1}$ is calculated, by multiplying the integral of the v_2 function (over the near-side $\Delta\phi$ range) by the ratio of $\sigma_{b_{\Delta\phi}}^{m1}$ to $v_2^{m1}(m)$:

$$\sigma_{B_{\Delta\phi}}^{m1} = \frac{\sigma_{b_{\Delta\phi}}^{m1}}{v_2^{m1}(m)} \left[\int_{-0.7854}^{0.7854} d\Delta\phi (1 + 2\langle v_2^{trigger} \rangle \langle v_2^{associated} \rangle \cos 2\Delta\phi) \Big|_{0.7083 \leq |\Delta\eta| \leq 1.4167} \right] \quad (5.16)$$

V.4.1.2. Method 2

In method 2, the two contributing errors to the total statistical error are the errors on $b_{\Delta\eta}^{m2}$ and on $B_{\Delta\phi}^{m2}$. There is no other source of statistical error, because the yield is given as the difference between these two background values. The functional form is;

$$\sigma_{Total}^{m1} = \sqrt{(\sigma_{b_{\Delta\eta}}^{m1})^2 + (\sigma_{B_{\Delta\phi}}^{m1})^2} \quad (5.17)$$

The values $\sigma_{b_{\Delta\eta}}^{m2}$ and $\sigma_{B_{\Delta\phi}}^{m2}$ are determined from the errors in the specified bins in the $\Delta\eta$ and $\Delta\phi$ correlations respectively. $B_{\Delta\phi}^{m2}$ is calculated as follows;

$$\sigma_{B_{\Delta\phi}}^{m1} = \frac{\sigma_{b_{\Delta\phi}}^{m1}}{v_2^{m2}(m)} \left[\int_{-0.7854}^{0.7854} d\Delta\phi (1 + 2\langle v_2^{trigger} \rangle \langle v_2^{associated} \rangle \cos 2\Delta\phi) \Big|_{|\Delta\eta| \leq 1.4167} \right] \quad (5.18)$$

$\sigma_{b_{\Delta\phi}}^{m2}$ is calculated in the same way as it is in method 1 (equation 5.14), and $v_2^{m2}(m)$ is calculated as follows;

$$v_2^{m2}(m) = (1 + 2\langle v_2^{trigger} \rangle \langle v_2^{associated} \rangle \cos 2m) \Big|_{|\Delta\eta| \leq 1.4167} \quad (5.19)$$

$\sigma_{b_{\Delta\eta}}^{m2}$ is calculated according to the following equation;

$$\sigma_{b_{\Delta\eta}}^{m2} = \frac{d\Delta\phi(2.8334)}{0.9168} \left[\sum_{i=15}^{25} \sigma_{bin\ i}^2 \Big|_{19 \leq \Delta\phi b \leq 30} + \sum_{j=72}^{82} \sigma_{bin\ j}^2 \Big|_{19 \leq \Delta\phi b \leq 30} \right] \quad (5.20)$$

V.4.2. Systematic Error

The dominant contribution to the systematic error on the calculated yield (in most p_T bins), comes from the error on the v_2 calculation. The parameterization used [63] outputs a high, a low and an average v_2 estimate for each combination of trigger and associated particle p_T and for each centrality bin (in 5% increments, in this case the 0-5% and the 5-10% values are averaged to give a v_2 value for the 0-10% bin; which all the data in this dissertation occupy) of which the average is used as the v_2 value, and the difference between either of the two extreme estimates and the average is taken as the systematic error on the yield.

However, an additional error analysis was conducted to verify that there were no additional sources of error that contributed beyond statistical uncertainties. If the percent systematic error associated with varying the number of bins (from 1 to 3) used to set the ZYAM point was greater than or equal to 3 standard deviations of the independent portion of the statistical error associated with switching from one number of bins to the next, then this systematic error was added in quadrature to the systematic error from the v_2 estimation to give a total systematic error for that bin. A significant systematic error from this analysis was observed in very few of the trigger and p_T bins. Please see the following chapter for a discussion of the full results of this analysis.

CHAPTER VI

RESULTS AND DISCUSSION

In this chapter the full results from the analysis methods described in the previous chapter will be presented and discussed. The first section is concerned with a charged-particle triggered analysis that was done on data from Runs 7 and 10; this analysis serves as a consistency check against the data from Run 4 that were presented in the original ridge analysis[10]. The following section is concerned with the γ -triggered results from Runs 7 and 10 that are the central focus of this dissertation; and the final section details the results of a χ^2 analysis of the γ -triggered ridge yields, that tests the previous conclusion[10] that the ridge yield is independent of trigger p_T .

VI.1. Consistency Check: Ridge Yields in Charged-particle Triggered Correlations

One reason why a consistency check is needed, is that the STAR detector system has continually evolved since the first Run ended in 2000. Upgrades to detector components, triggering algorithms, data acquisition hardware, and the periodic decommissioning and removal of detectors means that, in each running year, the STAR geometry and components have significantly changed. In the case of the two data sets used in this dissertation (Au+Au collisions Runs 7 and 10) and the one to which they are compared (Au+Au collisions Run 4), there have been several changes in particular. Between Runs 4 and Runs 7, the remaining 1/2 of the Barrel Electromagnetic Calorimeter (BEMC) and the Barrel Shower-Maximum Detector (BSMD) were added to the detector system, and after Run 7 the Silicon Vertex Tracker (SVT) was removed and an upgrade was made to the STAR DAQ system that increased the number of collisions the DAQ was able to process in a given period of time, the Central Trigger Barrel (CTB) was replaced by the Time of Flight (TOF) detector

after Run 4; in addition, there was an entire module in the Time Projection Chamber (TPC) that was not operational in Run 10. Similar analyses using data sets from multiple years should yield consistent results (after correction for single-particle efficiencies, acceptance, and multiplicity); differences usually point to unsolved problems unique to that running year. For example, in 2004 most charged-charged analyses used a vertex cut of ± 30 cm, however in 2007, charged particles from events with vertices greater than ± 15 cm were found to have skewed pseudorapidity distributions and were therefore excluded from this analysis. The reason for this difference has not been completely identified, but for consistency purposes, the same cut is made in the Run 10 data presented here.

The second reason why a consistency check is needed is that the main analysis presented in this dissertation (γ -triggered 2D correlation analysis) is new, and it would be hard to interpret any difference in the ridge yield compared to a charged-particle triggered analysis, without first verifying that the method used in this analysis can convincingly reproduce the results obtained by the primary investigators in their previous work[10]. Furthermore, although low-level code (code that accesses the raw event and converts the raw digital detector signals to physical quantities) is commonly used and maintained collaboration-wide, higher level analysis code is typically written, used, and maintained within specific institutions or individual research groups within those institutions. New results using a new analysis code are therefore compared to older results, to add confidence to conclusions made from new results.

VI.1.1. Charged-Particle Triggered Correlation Histograms

The uncorrected correlations are shown in Fig. VI.1 and VI.2; the analysis cuts on the fit points, DCA, and pseudorapidity are similar to those described in Sec. V.2.1. The trigger charged-particle was required to be within the p_T ranges of 3.0 - 4.0,

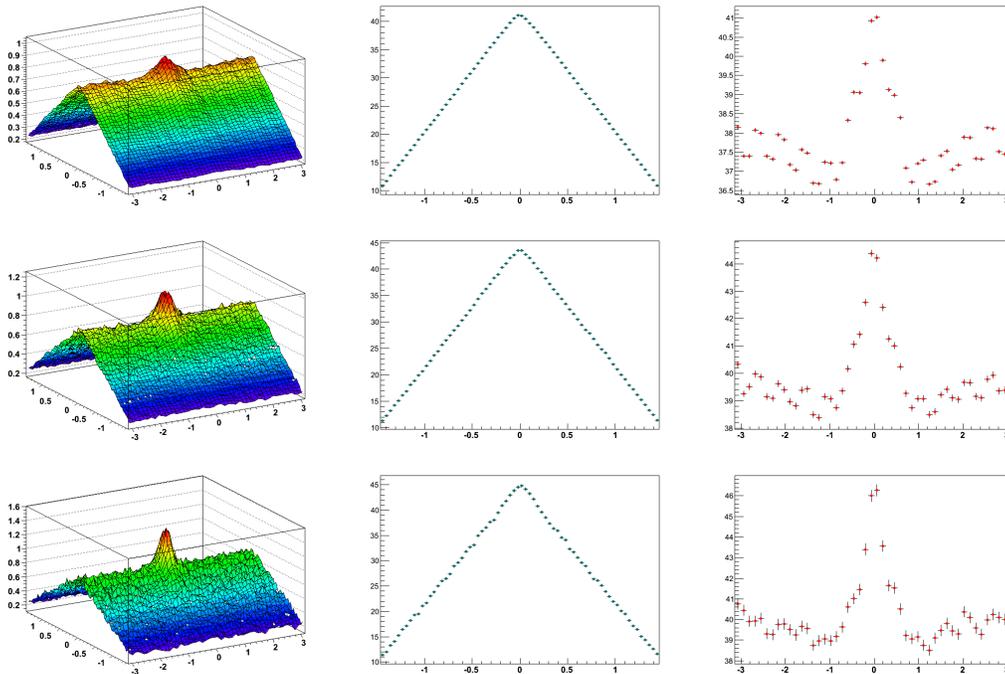


Fig. VI.1.: Uncorrected charged-particle correlations (Run 7). Columns from top to bottom show plots for the 3 p_T bins, 3.0 – 4.0, 4.0 – 5.0, and 5.0 – 6.0 GeV/c , and rows from left to right show the 2D correlations, the $\Delta\eta$ and the $\Delta\phi$ projections.

4.0 - 5.0, and 5.0 - 6.0 GeV/c for the three trigger p_T bins, associated particles with $2.0 < p_T^{assoc.} < p_T^{trig.}$ were factored into the correlation. This associated particle p_T range differs from the published Run 4 results; those results show data with accepted associated particles similar to the method of this analysis, but also with associated particle p_T between 2.0 and 4.0 GeV/c independent of the trigger p_T . Another difference between those results and these, is that this analysis accepts only one trigger particle per event.

The acceptance distributions are found in Figs. VI.3 and VI.4, and the corrected correlations are shown in Figs. VI.6 and VI.5; Fig. VI.7 shows one p_T bin for Run 4, Run 7 and Run 10. These figures visually confirm that the ridge is observed in all

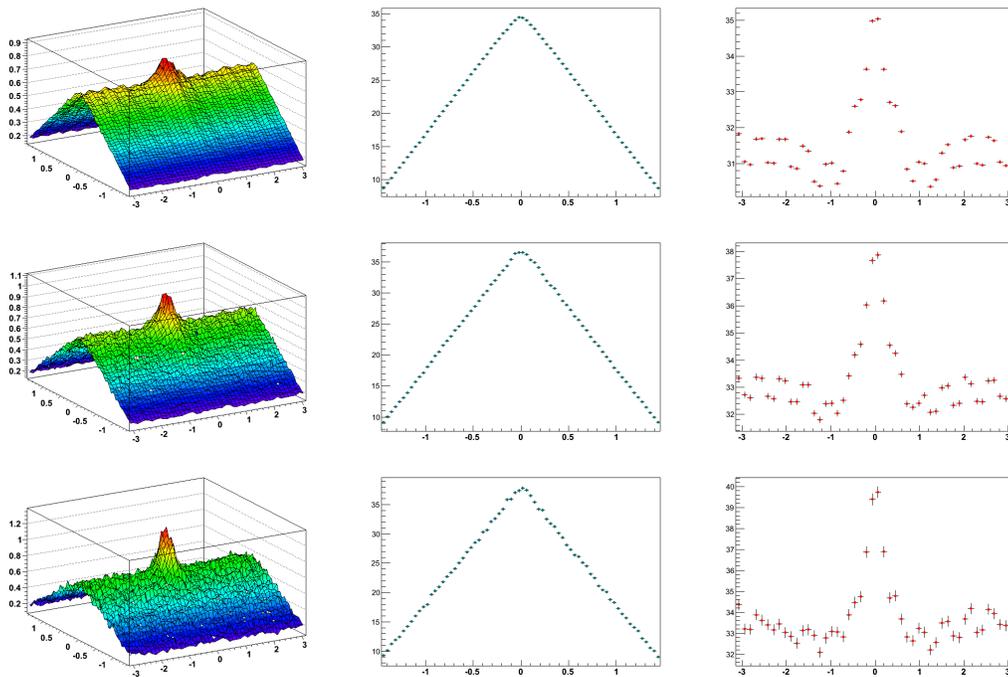


Fig. VI.2.: Uncorrected charged-particle correlations (Run 10). Columns from top to bottom show plots for the 3 p_T bins, 3.0 – 4.0, 4.0 – 5.0, and 5.0 – 6.0 GeV/c , and rows from left to right show the 2D correlations, the $\Delta\eta$ and the $\Delta\phi$ projections.

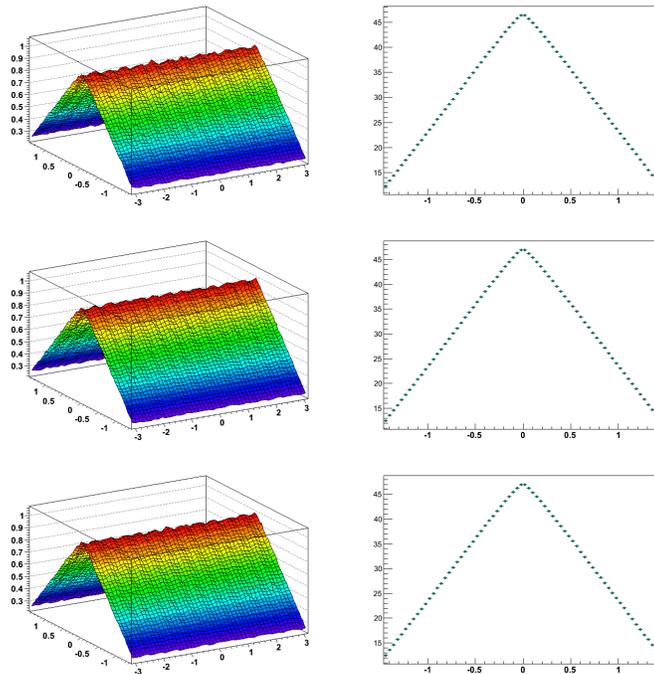


Fig. VI.3.: Charged-particle acceptance (Run 7). Columns from top to bottom show plots for the 3 p_T bins, 3.0 - 4.0, 4.0 - 5.0, and 5.0 - 6.0 GeV/c , and rows from left to right show the 2D correlations, and the $\Delta\eta$ projection.

three runs. The next section compares the yields and discusses the systematic error determination.

VI.1.2. Charged-Particle Triggered Yields and Systematic Error Analysis

Figures VI.8 (Run 7) and VI.9 (Run 10) show the $\Delta\phi$ projection of the ridge region (before v_2 subtraction) and the v_2 modulation after it has been normalized to the 3 bins (as described in the previous chapter). Figures VI.10 (Run 7) and VI.11 (Run 10) show two sets of histograms; the first is a $\Delta\eta$ projection of the entire $\Delta\phi$ range and the second is the $\Delta\phi$ projection of the full $\Delta\eta$ range (as well as the ZYAM-normalized v_2 functions).

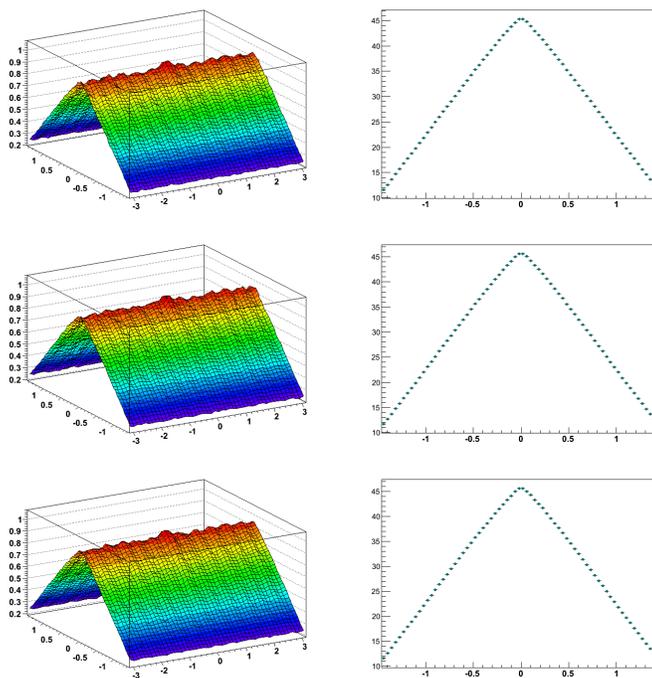


Fig. VI.4.: Charged-particle acceptance (Run 10). Figures are arranged in the same manner as described above.

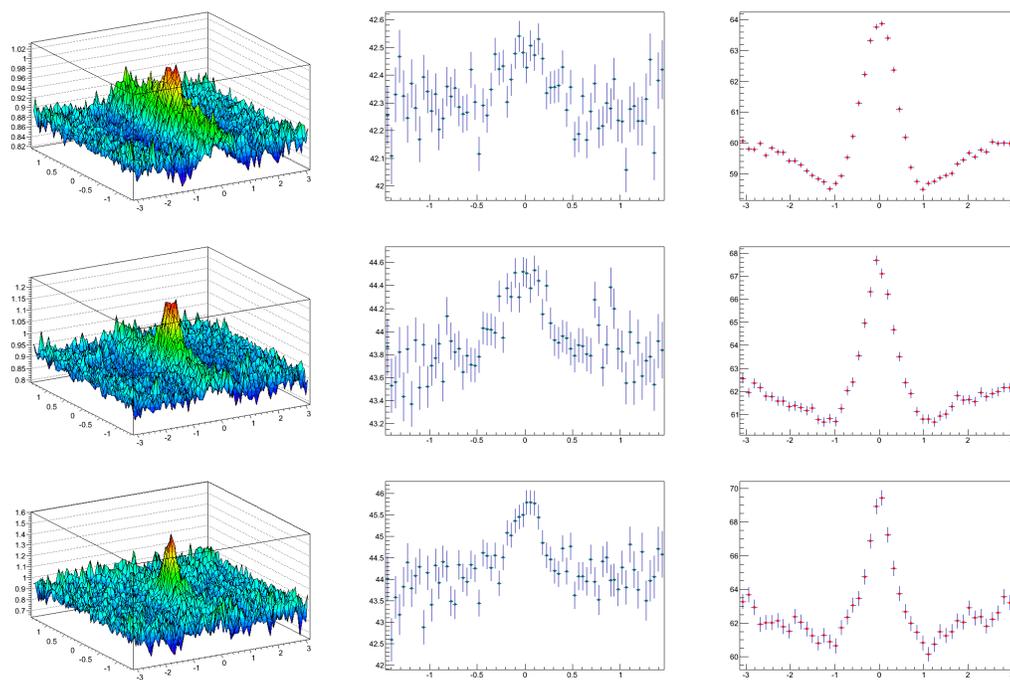


Fig. VI.5.: Corrected charged-particle correlations (Run 7). Figures are arranged in the same manner as described above.

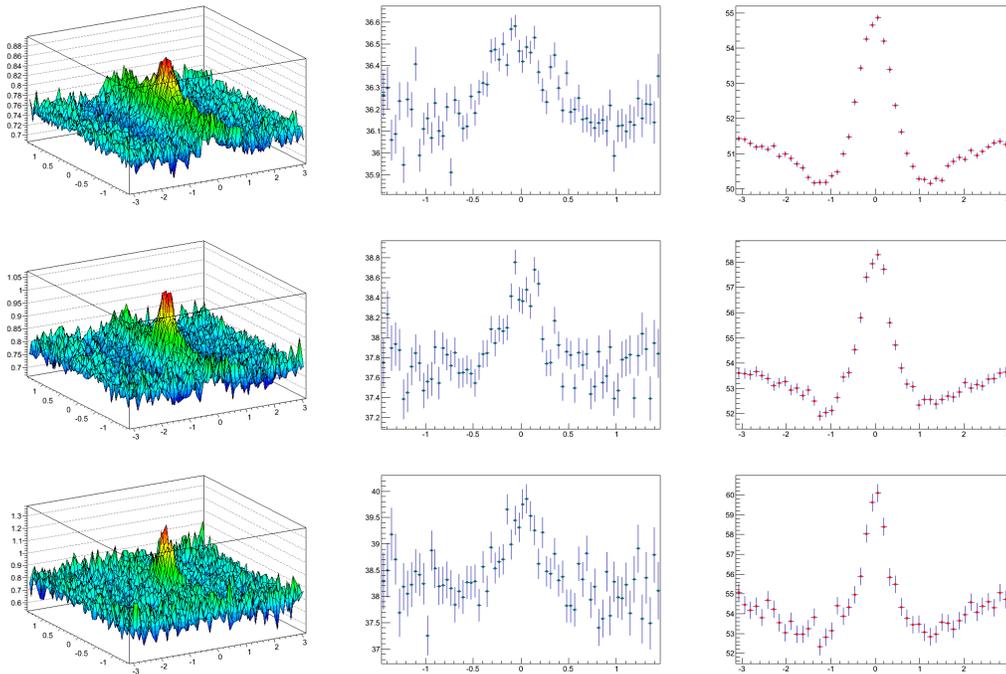


Fig. VI.6.: Corrected charged-particle correlations (Run 10). Figures are arranged in the same manner as described above.

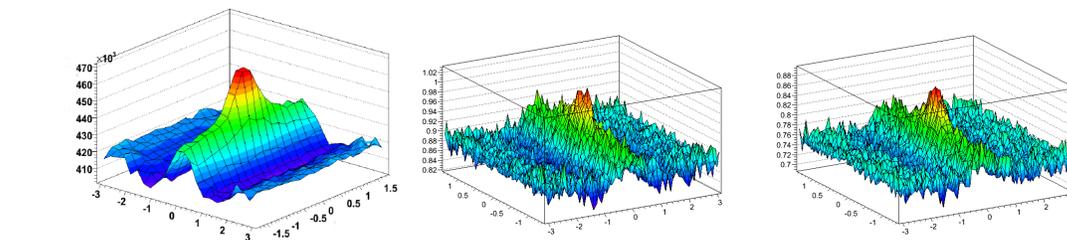


Fig. VI.7.: Corrected correlations with $3.0 < p_T^{trig} < 4.0$ and $2.0 < p_T^{trig} \cdot p_T^{trig}$, for Au+Au collisions in Run 4 (left)[10], Run 7 (middle), and Run 10 (top). Apart from the finer binning in the two plots from this analysis (and the fact that the published results calculate the absolute value of $\Delta\eta$ and $\Delta\phi$ then reflected that quadrant onto the other three), all three results show the characteristic ridge shape and are similar.

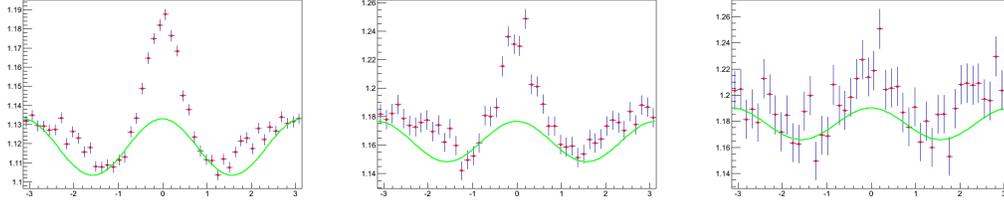


Fig. VI.8.: Charged-particle yield extraction method 1, Run 7. $\Delta\phi$ projection (of $|\Delta\eta| \leq 1.4167$) showing the v_2 modulation (equation 5.3)– for all 3 p_T bins.

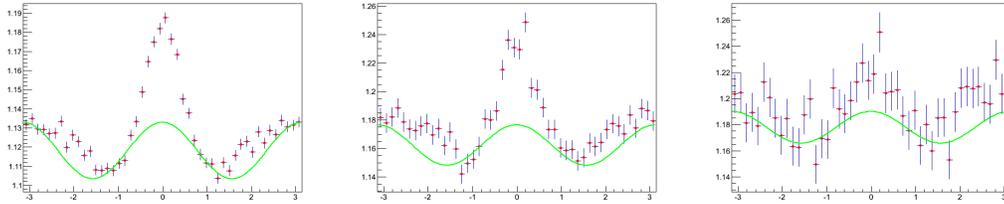


Fig. VI.9.: Charged-particle yield extraction method 1, Run 10. $\Delta\phi$ projection (of $|\Delta\eta| \leq 1.4167$) showing the v_2 modulation (equation 5.3)– for all 3 p_T bins.

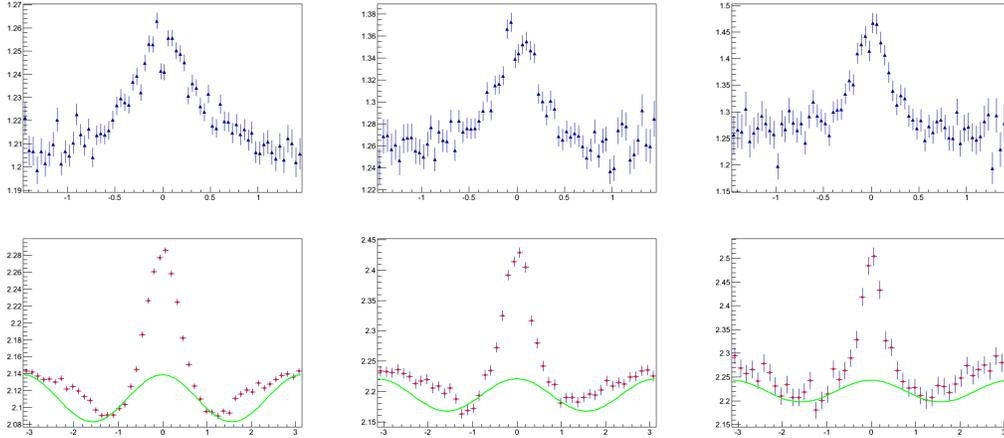


Fig. VI.10.: Charged-particle yield extraction method 2, Run 7. $\Delta\eta$ projection (of $|\Delta\phi| \leq 0.7854$) used to calculate $b_{\Delta\eta}^{m2}$ (top row), and $\Delta\phi$ projection (of $|\Delta\eta| \leq 1.4167$) showing the v_2 modulation (equation 5.3)(bottom row)– for all 3 p_T bins.

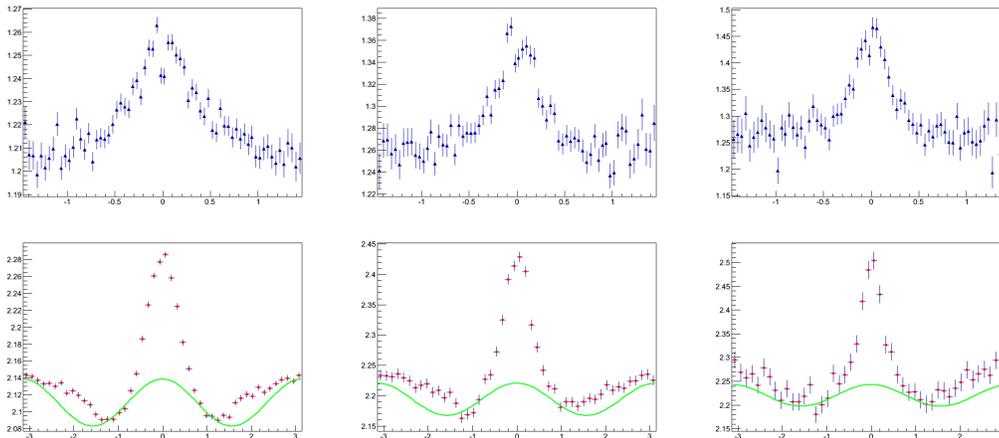


Fig. VI.11.: Charged-particle yield extraction method 2, Run 10. $\Delta\eta$ projection (of $|\Delta\phi| \leq 0.7854$) used to calculate $b_{\Delta\eta}^{m2}$ (top row), and $\Delta\phi$ projection (of $|\Delta\eta| \leq 1.4167$) showing the v_2 modulation (equation 5.3)(bottom row)– for all 3 p_T bins.

Figure VI.12 shows the ridge yields for the three p_T bins from both methods in both runs. The four yields in each p_T bin all agree within the statistical errors, with the exception of one yield in the first bin; and they all agree within the scope of the systematic errors. Figure VI.13 shows the published Run 4 yields; again the yields agree statistically with the exception of the first bin (a difference in the same bin was also observed by another collaborator who attempted to reproduce these results).

The data used for the calculation of the systematic error for Run 7 and Run 10 are found in Tables. VI.1 and VI.2. Rows 1 – 3 show the ridge yields calculated using 3, 2 and 1 histogram bins to set ZYAM for v_2 subtraction (described in Sec. V.4.2) these are referred to in the table as Y^{3bins} , Y^{2bins} , and Y^{1bin} ; the next 3 rows (rows 4 – 6) show the total statistical error associated with the yield values (σ_Y^3 , σ_Y^2 , and σ_Y^1); rows 7 – 9 show the percent systematic error between yields calculated with ZYAM determined by 3 bins and 1 bin ($S_Z^{3,1}$), 3 bins and 2 bins ($S_Z^{3,2}$), and the systematic error due to v_2 uncertainties ($S_Z^{v_2}$); finally, the last 2 rows (10 and 11) show the independent

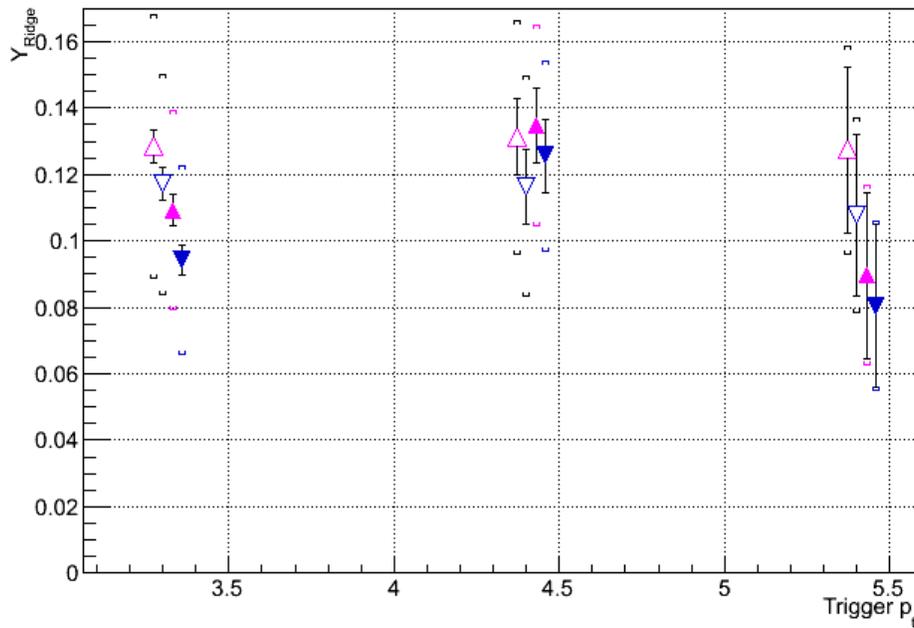


Fig. VI.12.: Charged-particle triggered ridge yields for Run 7 method 1 magenta open (up) triangle, Run 7 method 2 navy-blue open (down) triangle, Run 10 method 1 magenta full (up) triangle, Run 10 method 2 navy-blue full (down) triangle. Error bars are statistical, braces are systematics.

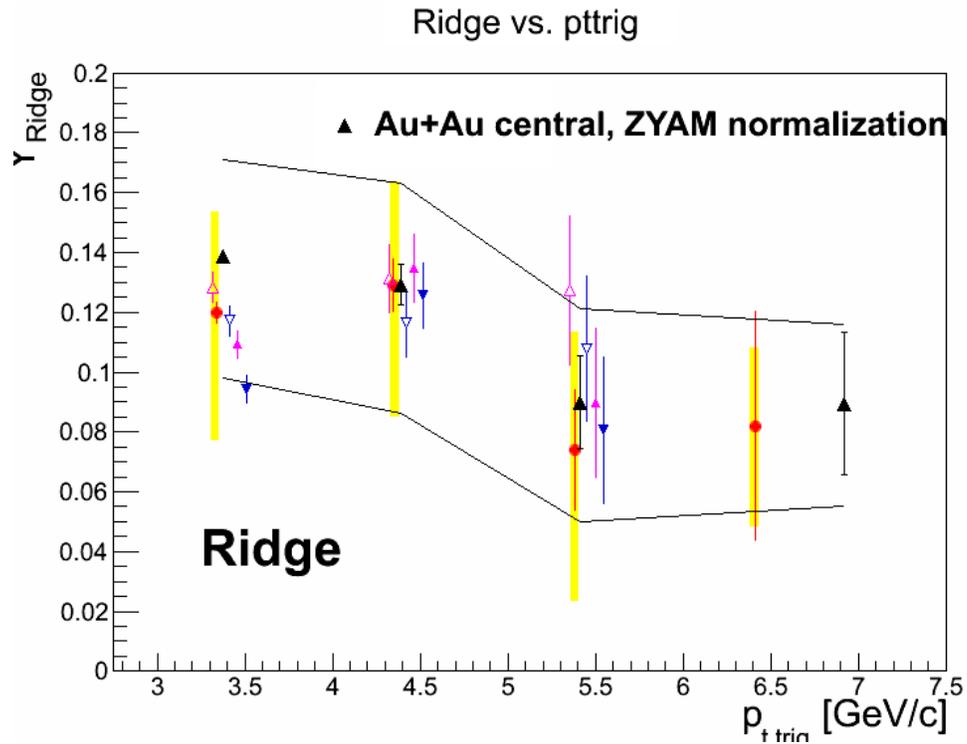


Fig. VI.13.: Ridge yields, charged-particle correlations. Run 4 published data[10] (black triangles) plot with the data from this dissertation (see Fig. VI.12) and with data from Run 4 (red circles) from another STAR collaborator (Christine Nattrass, Private Communication). The yellow bars are systematic errors for the Nattrass data, the black lines for the published data (the systematics for the data in this dissertation are omitted for clarity).

Table VI.1.: Run 7 charged-particle ridge yield systematic error calculations.

	$M1$ 3–4 <i>GeV</i>	$M1$ 4–5 <i>GeV</i>	$M1$ 5–6 <i>GeV</i>	$M2$ 3–4 <i>GeV</i>	$M2$ 4–5 <i>GeV</i>	$M2$ 5–6 <i>GeV</i>
Y^{3bins}	0.13	0.13	0.13	0.12	0.12	0.11
Y^{2bins}	0.14	0.14	0.11792	0.13	0.12	0.12
Y^{1bin}	0.15	0.15	0.098	0.14	0.13	0.12
σ_Y^3	0.0050	0.011	0.025	0.0049	0.011	0.024
σ_Y^2	0.0056	0.013	0.028	0.0051	0.012	0.026
σ_Y^1	0.0072	0.017	0.036	0.0058	0.013	0.029
$\%S_Z^{3,1}$	14.5	11.6	23.3	16.0	11.4	12.3
$\%S_Z^{3,2}$	8.4	5.3	7.4	9.4	3.0	14.7
$\%S_Z^{v_2}$	27.3	26.8	24.4	28.2	28.4	27.1
$\%\sigma_Z^{3,1}$	4.06	9.2	20.6	2.7	6.3	14.7
$\%\sigma_Z^{3,2}$	2.0	4.6	10.3	1.3	3.1	7.3

part of the statistical error between Y^{3bins} and Y^{1bin} ($\sigma_Z^{3,1}$), and between Y^{3bins} and Y^{2bins} ($\sigma_Z^{3,2}$). The systematic error algorithm returns the systematic error from varying the ZYAM bins added in quadrature to the v_2 systematics if the ZYAM bin error is greater than 3σ , otherwise, the algorithm returns only the v_2 systematic error. The only p_T bin in which the ZYAM bin error was included in the final systematic error is the 3.0 – 4.0 *GeV/c* bin from method 1 in Run 7. As previously mentioned, this was the only bin that differed significantly (statistically) from the previously published results.

Table VI.2.: Run 10 charged-particle ridge yield systematic error calculations.

	$M1$ 3–4GeV	$M1$ 4–5GeV	$M1$ 5–6GeV	$M2$ 3–4GeV	$M2$ 4–5GeV	$M2$ 5–6GeV
Y^{3bins}	0.11	0.13	0.090	0.094	0.13	0.0804
Y^{2bins}	0.11	0.13	0.084	0.097	0.13	0.071
Y^{1bin}	0.11	0.14	0.064	0.099	0.14	0.061
$\% \sigma_Y^3$	0.0047	0.011	0.025	0.0046	0.011	0.025
$\% \sigma_Y^2$	0.0053	0.012	0.028	0.0048	0.012	0.026
$\% \sigma_Y^1$	0.0068	0.016	0.036	0.0054	0.013	0.029
$S_Z^{3,1}$	3.2	1.6	29.1	5.6	10.7	24.0
$S_Z^{3,2}$	0.7	0.1	6.6	3.4	3.7	12.2
S_Z^{v2}	27.5	22.4	30.2	30.0	22.7	31.7
$\% \sigma_Z^{3,1}$	4.5	8.8	29.3	3.1	5.7	19.8
$\% \sigma_Z^{3,2}$	2.2	4.4	14.6	1.6	2.8	9.9

Table VI.3.: Ridge yields (Run 7, method 1) with their associated statistical and systematic errors.

$P_T bin$	$\langle P_T \rangle$	No. of Trig.	Yield	Stat. Err.	% Sys. Err.
3.0 – 4.0	3.3	3,195,087	0.13	0.0050	30.9
4.0 – 5.0	4.4	613,366	0.13	0.011	26.8
5.0 – 6.0	5.4	128,948	0.13	0.025	24.4

Table VI.4.: Ridge yields (Run 7, method 2) with their associated statistical and systematic errors.

$P_T bin$	$\langle P_T \rangle$	No. of Trig.	Yield	Stat. Err.	% Sys. Err.
3.0 – 4.0	3.3	3,195,087	0.12	0.0049	28.2
4.0 – 5.0	4.4	613,366	0.12	0.011	28.4
5.0 – 6.0	5.4	128,948	0.11	0.024	27.1

Table VI.5.: Ridge yields (Run 10, method 1) with their associated statistical and systematic errors.

$P_T bin$	$\langle P_T \rangle$	No. of Trig.	Yield	Stat. Err.	% Sys. Err.
3.0 – 4.0	3.3	3,255,214	0.11	0.0047	27.5
4.0 – 5.0	4.4	575,726	0.13	0.011	22.4
5.0 – 6.0	5.4	117,601	0.090	0.025	30.2

Table VI.6.: Ridge yields (Run 10, method 2) with their associated statistical and systematic errors.

$P_T bin$	$\langle P_T \rangle$	No. of Trig.	Yield	Stat. Err.	% Sys. Err.
3.0 – 4.0	3.3	3,255,214	0.094	0.0046	30.0
4.0 – 5.0	4.4	575,726	0.13	0.011	22.7
5.0 – 6.0	5.4	117,601	0.080	0.025	31.7

VI.2. Ridge Yields in γ/π^0 -Triggered Correlations

This section presents the yield correlation plots for the π^0 -rich triggers, and the integrated yield for both the γ -rich and the π^0 -rich triggers. A detailed analysis of these yields follows in Sec. VI.3. The systematic error calculations for both methods and triggers in both runs can be found in Appendix B.

VI.2.1. γ/π^0 -Triggered Yields

The γ/π^0 -triggered correlation plots for the ridge yield methods 1 and 2 are shown, for Run 7 in Fig. VI.14, and for Run 10 in Fig. VI.15.

The π^0 -triggered ridge yields from methods 1 and 2, from Runs 7 and 10 are shown in Fig. VI.16.

Although the focus of this this is the π^0 -triggered correlations and ridge yields, the γ -triggered correlations and yields are presented for completeness. However there are three main issues with this sample that prohibit us from using them to draw conclusions about the nature of the γ -triggered ridge:

1. The same v_2 values for the π^0 - rich triggers are used for the γ -rich triggers. This leads to an over subtraction of the background in this sample.
2. The statistics in this set are lower than in the π^0 -triggered set; resulting in large statistical uncertainties.
3. A more meaningful measurement would be of background subtracted direct γ -triggered correlations. This measurement will be calculated after the solution for the statistic woes (see Chapter VII) is implemented.

The γ -triggered yields are show in Fig. VI.17. Although they appear consistent with zero, this conclusion cannot be made, as a result of the three issues previously

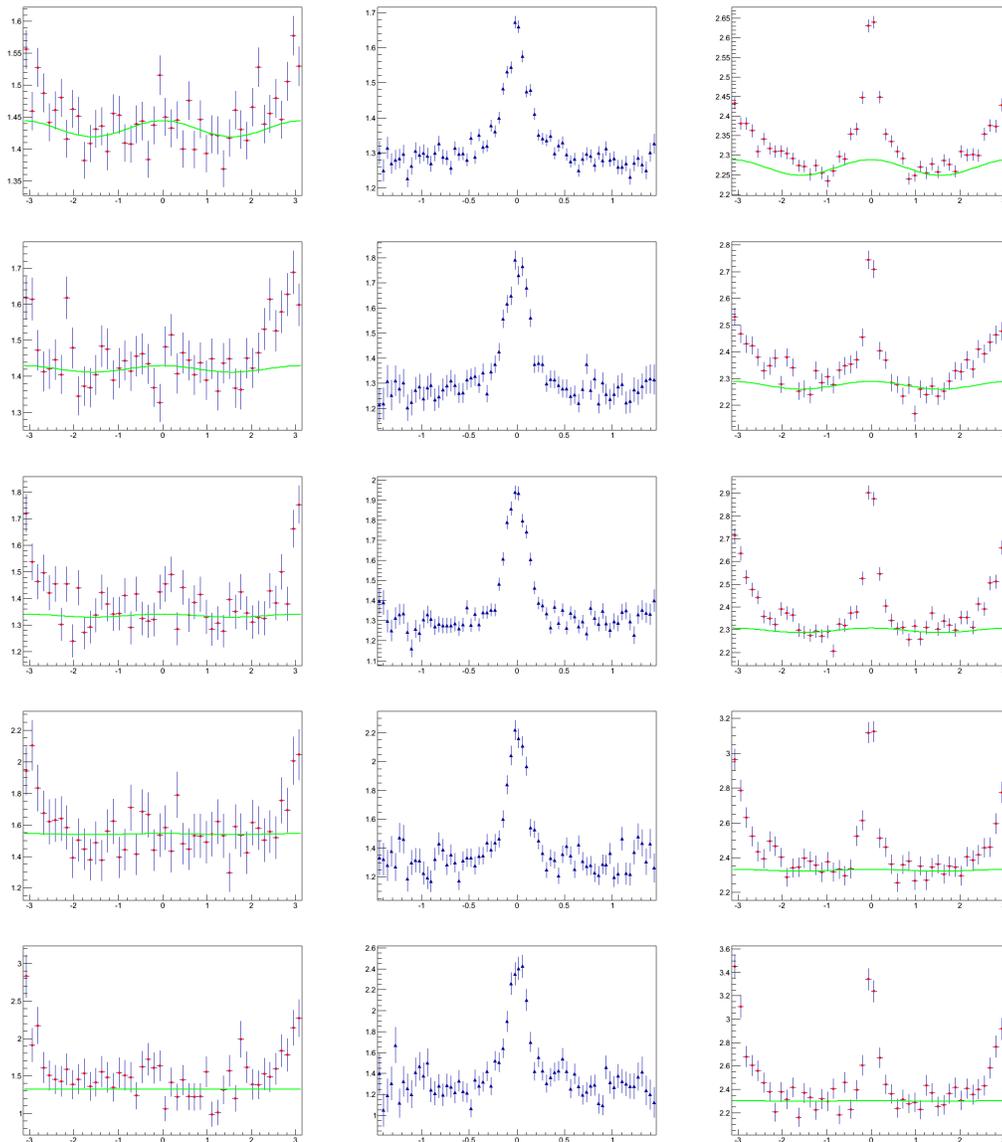


Fig. VI.14.: γ -triggered (π^0 -rich sample) yield extraction plots Run 7. Method 1: $\Delta\phi$ projection (of $|\Delta\eta| \leq 1.4167$) showing the v_2 modulation (left column). Method 2: $\Delta\eta$ projection (of $|\Delta\phi| \leq 0.7854$) used to calculate $b_{\Delta\eta}^m$ (middle column), and $\Delta\phi$ projection (of $|\Delta\eta| \leq 1.4167$) showing the v_2 modulation (right column). Rows are the 5 p_T bins from lowest to highest.

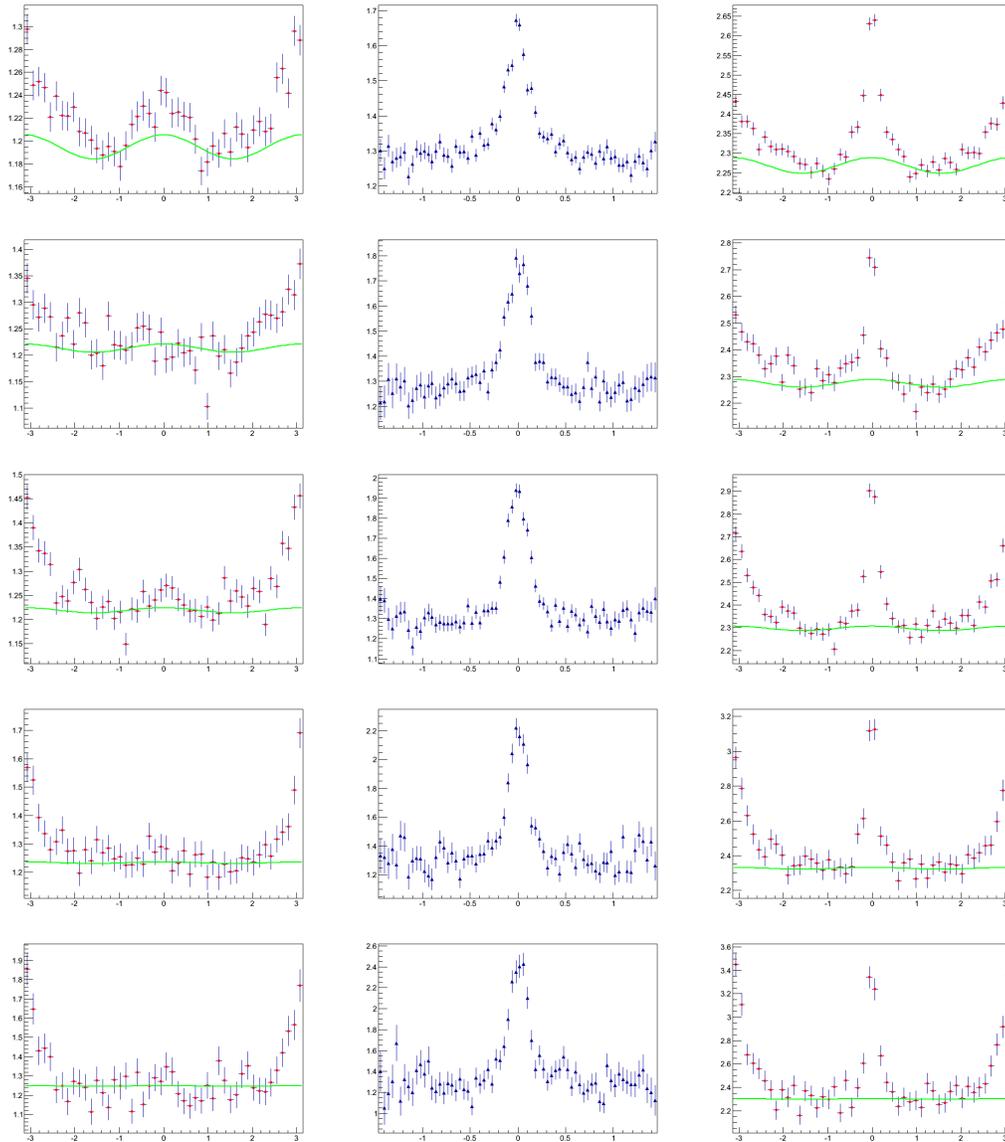


Fig. VI.15.: γ -triggered (π^0 -rich sample) yield extraction plots Run 10. Method 1: $\Delta\phi$ projection (of $|\Delta\eta| \leq 1.4167$) showing the v_2 modulation (left column). Method 2: $\Delta\eta$ projection (of $|\Delta\phi| \leq 0.7854$) used to calculate $b_{\Delta\eta}^{m2}$ (middle column), and $\Delta\phi$ projection (of $|\Delta\eta| \leq 1.4167$) showing the v_2 modulation (right column). Rows are the 5 p_T bins from lowest to highest.

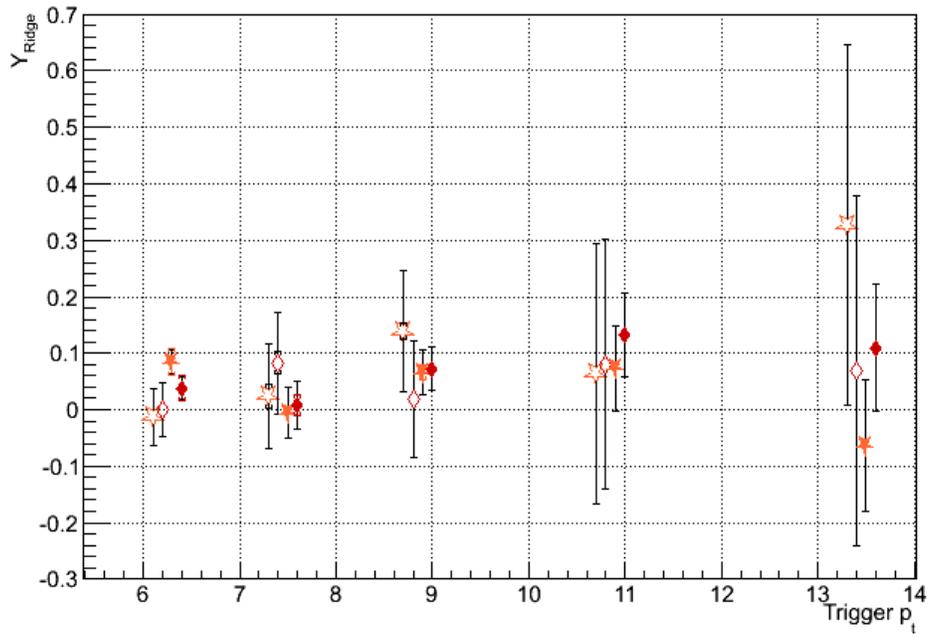


Fig. VI.16.: γ -triggered (π^0 -rich sample) triggered ridge yields for Run 7 method 1 dark-orange open stars, Run 7 method 2 dark-red open diamonds, Run 10 method 1 dark-orange full stars, Run 10 method 2 dark-red full diamonds. Error bars are statistical, braces are systematics.

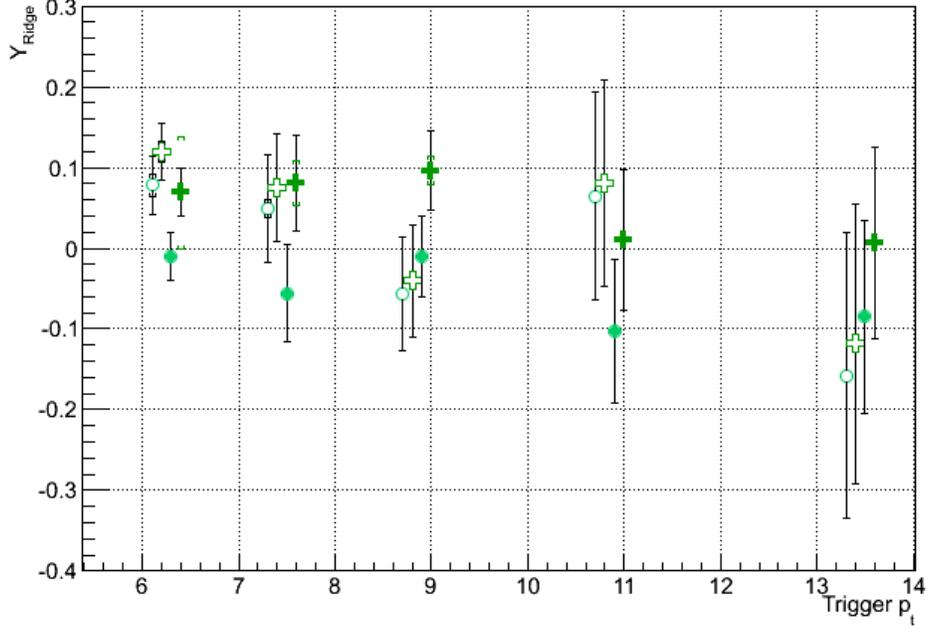


Fig. VI.17.: γ -triggered (direct- γ -rich sample) triggered ridge yields for Run 7 method 1 sea-green open circles, Run 7 method 2 dark-green open cross, Run 10 method 1 sea-green full circles, Run 10 method 2 dark-green full cross. Error bars are statistical, braces are systematics.

discussed.

VI.3. χ^2 Analysis of Ridge Yields

The conclusion from the initial ridge results[10] is that the ridge yield is constant (and non-zero) for all trigger p_T values. Certainly at low p_T (in the charged-particle triggered correlations) this appears to be a fair assumption, however in light of the new results presented in this work, it is not clear that that conclusion remains valid for the π^0 -triggered correlations at higher p_T . But, because of the relatively large statistical and systematic uncertainties in these new results; it is difficult to make

Table VI.7.: Expected yield values (E_i) from fit to charged-particle triggered yield values.

Run	Method	Expected Value	%Error of Fit
7	1	0.13	3.5
7	2	0.12	3.8
10	1	0.11	3.8
10	2	0.10	4.2

a definitive statement about trends in the ridge yields at higher p_T . A quantitative measure of how the data trends is therefore needed. This quantitative measure can be defined as a variation of a χ^2 sum, in which a weighted (by the variance on this error) sum-of-the-squares of the “error” (the difference between the observed yield value and the expected yield value) is calculated.

The first step in this analysis is to fit, with a constant value, the ridge yields in the charged-particle triggered correlation. This best estimate of a constant yield will be used as the expected value in the χ^2 calculation at higher p_T . To allow for independent assessment of the different yield determination methods, and of the impact on the increased statistics of Run 10; a separate expected yield value is extracted for each method in each running year. These values and the percent error of the fit are tabulated in Table VI.7.

The expected values from Tab. VI.7 are used as the value E_i in the χ^2 “goodness-of-fit” equation,

$$\chi_f^2 = \sum_i \frac{(O_i - E_i)^2}{\sigma_i^2}, \quad (6.1)$$

Table VI.8.: χ_f^2 values for charged-particle triggered ridge yields in Run 7 & Run 10.

Run	Method	$(\chi_f^2)^4$	$(\chi_f^2)^5$	$(\chi_f^2)^6$
7	1	6.8×10^{-3}	2.7×10^{-2}	1.9×10^{-2}
7	2	7.2×10^{-3}	4.0×10^{-3}	4.6×10^{-2}
10	1	4.3×10^{-1}	2.2	1.7
10	2	7.9×10^{-1}	3.5	2.485

$$\chi_0^2 = \sum_i \frac{O_i^2}{\sigma_i^2}, \quad (6.2)$$

where O_i is the observed value (the yield for that p_T bin), and σ_i is the error on O_i (which is assumed to be normally distributed). The second χ^2 equation (Eq. 6.2) is used to test how consistent with zero the yield values are.

Before the γ/π^0 -charged yield values are analyzed, the two χ^2 equations are applied to the charged-particle triggered yield. These results are shown in Tables VI.8 and VI.9. As predicted by the small $\sim 3.8\%$ fit error, these data should show a strong agreement with the expected value, and a weak agreement with 0. To get a more detailed mathematical description of how these data tend, 3 χ^2 values are calculated, one up to 4 $GeV/c((\chi_{f/0}^2)^4)$, using the first p_T bin, the next up to 5 $GeV/c((\chi_{f/0}^2)^5)$, using the first and second p_T bins and the last up to 6 $GeV/c((\chi_{f/0}^2)^7)$, using all the p_T bins.

For the γ -triggered correlations, 5 χ^2 values are calculated to show how the the yields trend with increasing trigger p_T (the super-script p_T is the right edge of that p_T bin); $(\chi^2)^7$, $(\chi^2)^8$, $(\chi^2)^{10}$, $(\chi^2)^{12}$ and $(\chi^2)^{16}$. These values can be found in Tables VI.10 and VI.11, and Tables VI.12 & VI.13; they are also plot in Figs. VI.18 and VI.19.

The results of this χ^2 analysis can be summarized in the following two points

Table VI.9.: χ_0^2 values for charged-particle triggered ridge yields in Run 7 & Run 10.

Run	Method	$(\chi_0^2)^4$	$(\chi_0^2)^5$	$(\chi_0^2)^6$
7	1	663	397	273
7	2	579	343	235
10	1	548	345	235
10	2	425	277	188

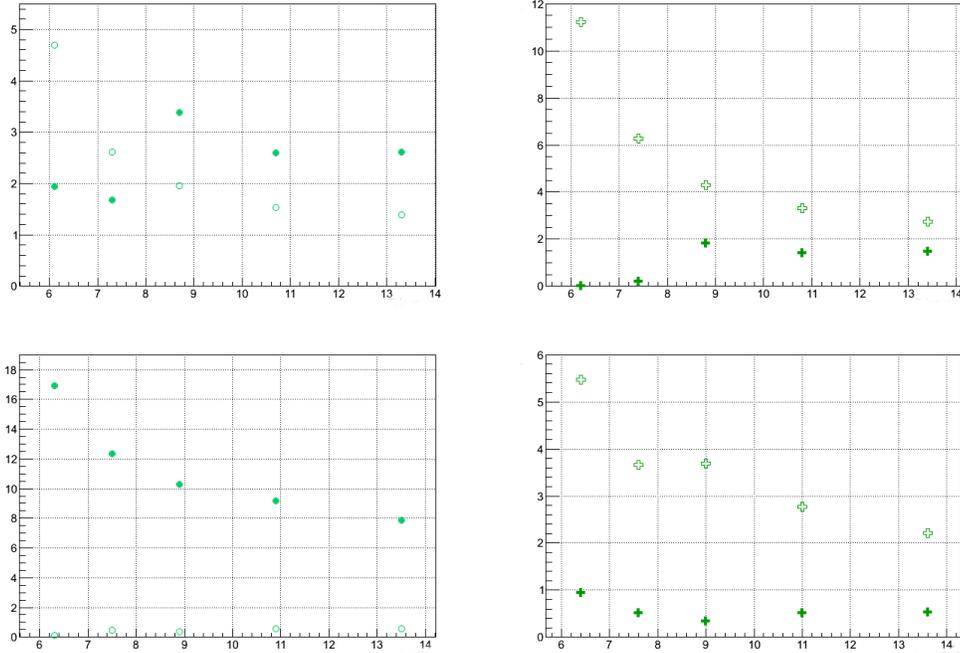


Fig. VI.18.: χ^2 values vs. p_T^{trig} for γ -triggered ridge yields in Run 7 & Run 10 - γ -rich sample. Method 1 Run 7 (top left), Method 2 Run 7 (top right), Method 1 Run 10 (bottom left) and Method 2 Run 10 (bottom right). Closed markers are χ_f^2 and open markers χ_0^2 . Please see Tables VI.10 and VI.11, and Tables VI.12 & VI.13 for data values.

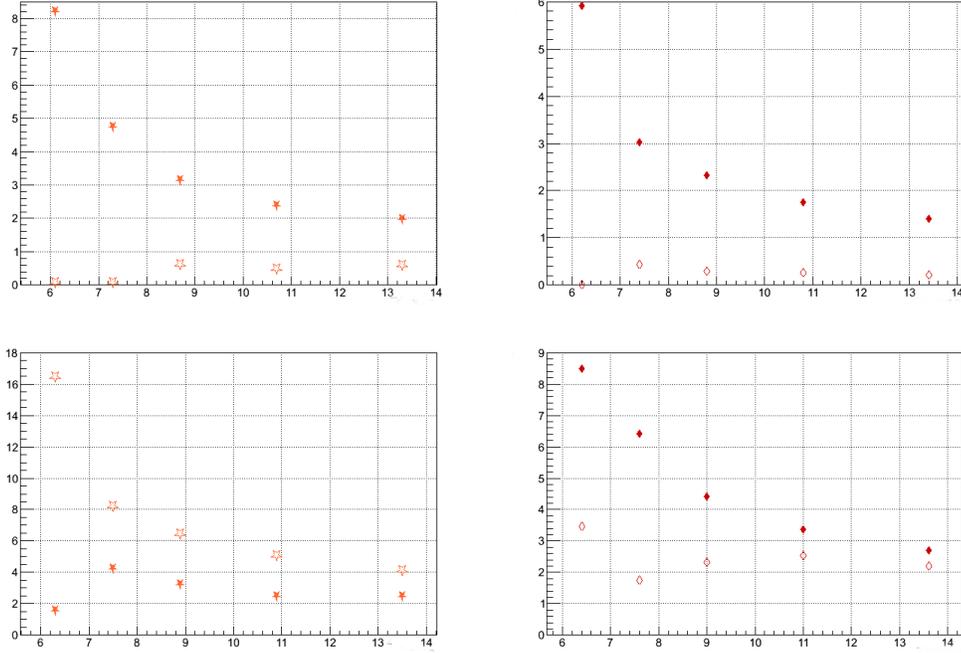


Fig. VI.19.: χ^2 values vs. p_T^{trig} for γ -triggered ridge yields in Run 7 & Run 10 - π^0 -rich sample. Method 1 Run 7(top left), Method 2 Run 7 (top right, Method 1 Run 10 (bottom left) and Method 2 Run 10 (bottom right). Closed markers are χ_f^2 and open markers χ_0^2 . Please see Tables VI.10 and VI.11, and Tables VI.12 & VI.13 for data values.

Table VI.10.: χ_f^2 values for γ -triggered ridge yields in Run 7.

Trigger Set	$(\chi_f^2)^7$	$(\chi_f^2)^8$	$(\chi_f^2)^{10}$	$(\chi_f^2)^{12}$	$(\chi_f^2)^{16}$
$\gamma - rich$ M1	1.94	3.35	10.16	10.40	13.02
$\gamma - rich$ M2	7.47×10^{-3}	4.07×10^{-1}	5.49	5.57	7.43
$\pi^0 - rich$ M1	8.21	9.50	9.51	9.59	9.97
$\pi^0 - rich$ M2	5.91	6.05	6.96	6.99	7.01

Table VI.11.: χ_0^2 values for γ -triggered ridge yields in Run 7.

Trigger Set	$(\chi_0^2)^7$	$(\chi_0^2)^8$	$(\chi_0^2)^{10}$	$(\chi_0^2)^{12}$	$(\chi_0^2)^{16}$
$\gamma - rich$ M1	4.67	5.23	5.86	6.12	6.91
$\gamma - rich$ M2	11.24	12.52	12.85	13.25	13.72
$\pi^0 - rich$ M1	7.32×10^{-2}	1.38×10^{-1}	1.83	1.91	2.95
$\pi^0 - rich$ M2	1.91×10^{-6}	8.55×10^{-1}	8.84×10^{-1}	1.02	1.06

Table VI.12.: χ_f^2 values for γ -triggered ridge yields in Run 10.

Trigger Set	$(\chi_f^2)^7$	$(\chi_f^2)^8$	$(\chi_f^2)^{10}$	$(\chi_f^2)^{12}$	$(\chi_f^2)^{16}$
$\gamma - rich$ M1	16.90	24.69	30.81	36.68	39.42
$\gamma - rich$ M2	9.39×10^{-1}	1.02	1.03	2.04	2.64
$\pi^0 - rich$ M1	1.60	8.48	9.79	10.06	12.36
$\pi^0 - rich$ M2	8.50	12.84	13.28	13.48	13.49

(strongly indicates a χ^2 value less than 2):

1. π^0 -rich sample (Run 7): The yields strongly tend to zero for trigger p_T less than 8 GeV/c and weakly tend to zero for trigger p_T greater than 8 GeV/c using Method 1, and strongly tend to zero for all trigger p_T s with Method 2.
2. π^0 -rich sample (Run 10): The yields strongly tend to the fit for the first bin (trigger p_T less than 7 GeV/c), but only weakly tend to the fit for all other p_T bins with Method 1, and weakly tend to zero for all p_T bins with Method 2.

Table VI.13.: χ_0^2 values for γ -triggered ridge yields in Run 10.

Trigger Set	$(\chi_0^2)^7$	$(\chi_0^2)^8$	$(\chi_0^2)^{10}$	$(\chi_0^2)^{12}$	$(\chi_0^2)^{16}$
$\gamma - rich$ M1	1.26×10^{-1}	9.82×10^{-1}	1.03	2.36	2.87
$\gamma - rich$ M2	5.48	7.31	11.08	11.09	11.10
$\pi^0 - rich$ M1	16.45	16.46	19.29	20.22	20.53
$\pi^0 - rich$ M2	3.45	3.48	6.97	10.09	11.03

CHAPTER VII

CONCLUSION AND OUTLOOK

VII.1. Summary and Conclusions

This work explored γ/π^0 triggered long-range rapidity correlations in $\sqrt{S_{NN}} = 200$ GeV Au + Au collisions with the STAR detector system. The neutral particle triggered events were separated into two groups: direct- γ -rich photons and π^0 -rich photons. The separation of photons into these two groups was accomplished by making a cut on the transverse shower profile (TSP) of the photon candidate in the STAR's Barrel Shower-Maximum Detector (BSMD) (which was calibrated in an attempt to improve this photon discrimination) in the Barrel Electromagnetic Calorimeter (BEMC).

The first question that this work attempted to address was the question of the dependence of the ridge yield on trigger p_T , i.e. how far the ridge extend in trigger p_T . The assumption in the first published study[10] was that the ridge was independent of trigger p_T . These data show a statistically significant ridge signal in two of the p_T bins for the π^0 -rich trigger sample. Figure VII.1 (the χ^2 results presented in the previous chapter) seems to indicate that the ridge yield actually decreases from the first p_T bin to some minimum value in the other bins (the first bin strongly tends towards the expected yield values from the fit, while the other bins tend away from this value). However, this analysis can only suggest that the assumption of constant ridge yield may not be true, but because of the lack of statistics, a conclusive statement that it is false cannot be made. The other question that this analysis aimed to confront was the question of whether or not the ridge is observed in direct- γ -triggered jet-like events, however, the lack of statistics prohibits an answer to this question.

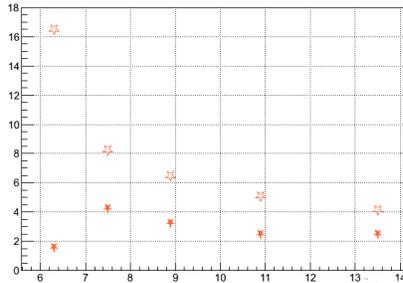


Fig. VII.1.: χ^2 values for Run 10 - π^0 -rich sample. Closed markers are χ_{fit}^2 and open markers χ_{zero}^2 .

VII.1.1. Solution for Overcoming the Effect of Statistics

In order to understand phenomena observed at low to mid p_T , it is often desirable to extend the analysis to higher p_T . The relatively few charged particles at higher p_T make this impractical with a charged-particle triggered analysis. Because of a HT trigger, a γ/π^0 -triggered analysis is theoretically possible to explore ridge yields (if the ridge persists) out to higher p_T . However, as the results in this work have shown, the statistics for γ candidates obtained during any single Run period, is likely to be inadequate for statistically significant data out to very high p_T . Combining data from multiple Au+Au runs is therefore a possible strategy for this type of analysis.

The feasibility of a combination of multiple data sets must be assessed on an analysis-by-analysis basis. In this analysis, the comparison of the ridge yields in the charged-particle consistency check suggest that even though there have been many changes to the detector system, the triggers and the electronics, that the data from Run 7 and Run 10 can be combined (Run 11 must be analyzed separately to determine whether it too should be added). The factor of ~ 2.6 increase in luminosity (Fig. VII.2) for all 3 runs over using Run 10 alone, and the estimated factor of ~ 6 increase

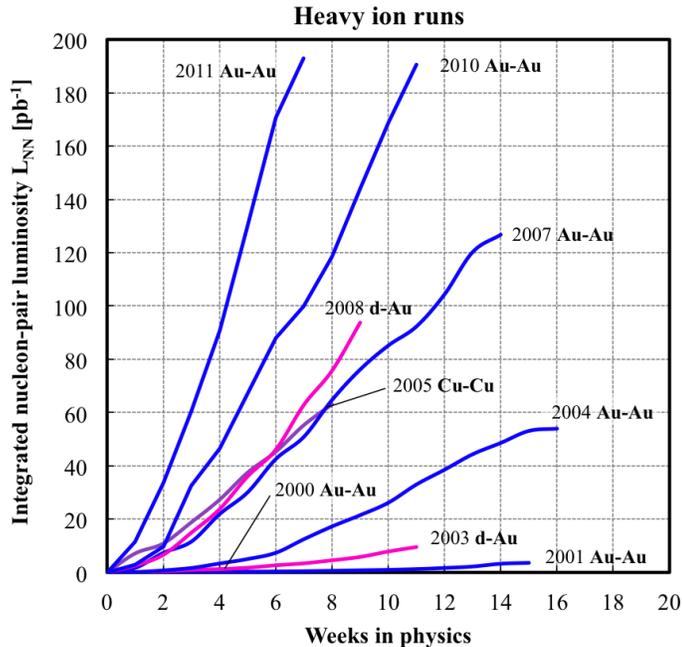


Fig. VII.2.: Integrated nucleon-pair luminosity in RHIC heavy ion runs through Run 11[25]. Combining the Runs 7, 10, and 11 data will provide a factor of ~ 2.6 increase in luminosity over using Run 10 alone, and a factor of ~ 6 increase in the statistics of Run 10.

in the statistics for events that satisfy the L2Gamma trigger, should yield statistically significant data out to ~ 13.5 in trigger p_T .

The acceptance correction employed in this analysis serves as a justification for the claim that these datasets can be combined. The mixed-events sample corrects for the effect of the finite detector acceptance in the correlations. This is seen in the fact that the acceptance for the direct- γ -rich + charged particles and the π^0 -rich + charged particles samples for each p_T bin have different shapes that describe features in the $\Delta\eta$ - $\Delta\phi$ space unique to these different trigger sets. In addition, the acceptance changes between runs for the charged particle triggered correlations.

The following method can be used for combining data from each of the 3 most recent Au+Au runs;

1. For each run (and in each trigger p_T bin), construct a raw correlation.
2. Create an acceptance distribution and correct for the acceptance (also in each of these bins).
3. Add the corrected histograms together and calculate the ridge yield.
4. Determine statistical and ZYAM systematic errors from the combined histogram.
5. Determine additional systematic errors (as described below)

For the error analysis in the combined data correlations, the statistical error method does not need to be modified; these errors can be calculated from the combined histograms as long as the errors were correctly propagated. Three components to the systematic error should be considered. The first component is the systematic from v_2 subtraction, which is independent of the statistics of the correlation to which it is applied (it is of course not independent of the data that was used in the parameterization) so it can be added as systematic on the combined corrected histogram. The second component to the systematic error is the choice of minimum in the ZYAM procedure. This error can also be easily calculated in a combined correlation; run dependent systematic effects were not dominant. With combined statistics, the systematic error can be studied in more detail.

VII.2. Future Outlook

STAR (by combining data from Runs 7, 10 and 11) should be able to make a statistically significant measurement of a direct- γ -rich versus a π^0 -rich ridge yield in the

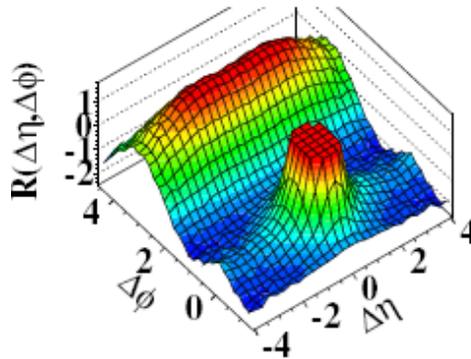


Fig. VII.3.: CMS $p + p$ ($\sqrt{S_{NN}} = 7 \text{ TeV}$) long-range rapidity correlation with track multiplicity > 110 and $1.0 < p_T < 3.0 \text{ GeV}/c$. The near-side jet peak is truncated to better show the ridge structure[26].

very near future. If the ridge is not present in the direct- γ -rich case (which these results seem to indicate) that fact would lead one to believe, that the ridge arises from some interaction of the near-side associated particles with the medium. However, in the long term, the LHC is anticipated to be the source of the many new ridge results. Already two interesting recent results from the CMS experiment at the LHC have raised a few questions about the nature of the ridge phenomenon. The first result[26] is an untriggered correlation analysis in high-multiplicity $p + p$ collisions with $1.0 < p_T < 3.0 \text{ GeV}/c$ that shows a weak associated yield (Figs. VII.3 and VII.4) in the highest multiplicity bins. The only background subtraction done was a random background subtraction generated by mixing all particles from one event with all particles from another event in the same multiplicity range (and vice-versa). It is expected that future publications will address this observation in more detail.

The second interesting result is the long-range correlations reported in [27] in Pb + Pb collisions at $\sqrt{S_{NN}} = 2.76 \text{ TeV}$ (Figs. VII.5 and VII.6). Their results show a

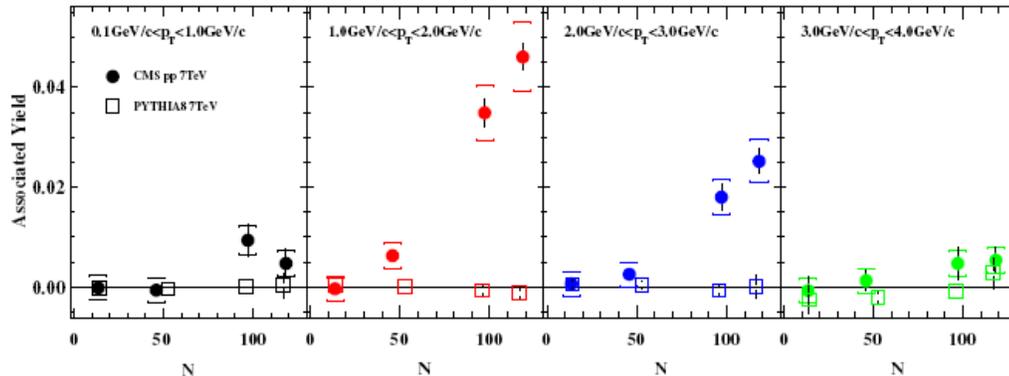


Fig. VII.4.: CMS $p + p$ ($\sqrt{S_{NN}} = 7 \text{ TeV}$) near-side associated yields integrated over $2.0 < \Delta\eta < 4.8$ [26].

ridge signal over twice the pseudorapidity range (up to ± 4) that STAR can measure and consequently shows that the ridge structure persists at higher $\sqrt{S_{NN}}$. More importantly, the results also show (as the data in this dissertation seem to indicate) that the yield decreases with increasing trigger p_T .

Because of the higher luminosity of LHC runs, there is the potential for the LHC to produce some interesting results for γ -triggered correlations in the future. These results presented in this dissertation represent the first step in the direction of using photon triggered correlations in two-dimensions, to understand more about the effect of the jet on the medium.

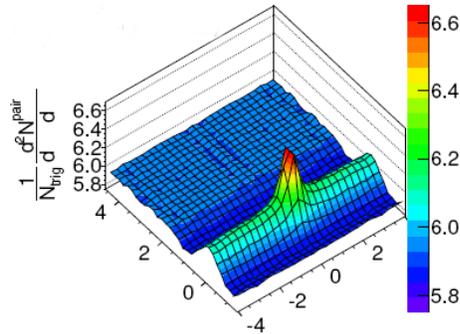


Fig. VII.5.: CMS Pb + Pb ($\sqrt{S_{NN}} = 2.76 \text{ TeV}$) long-range rapidity correlation (0 - 5% most central events). With $4.0 < p_T^{trig.} < 6.0$ and $2.0 < p_T^{assoc.} < 4.0$ [27].

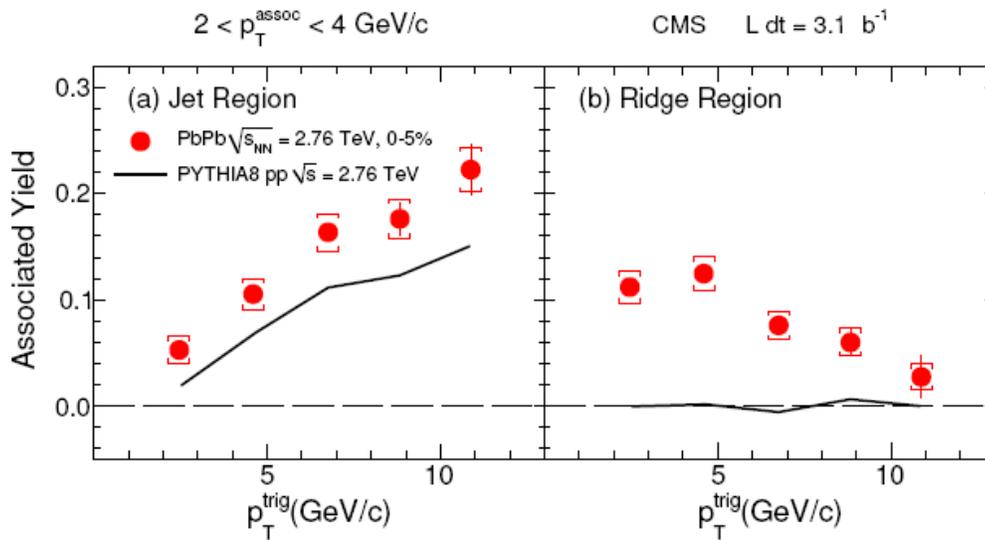


Fig. VII.6.: CMS Pb + Pb ($\sqrt{S_{NN}} = 2.76 \text{ TeV}$) jet and ridge yields vs. $p_T^{trig.}$. These data show a clear reduction in ridge yield with increasing p_T [27].

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APPENDIX A

MASKED TOWERS, γ -TRIGGERED RIDGE YIELDS, AND SYSTEMATIC
ERROR ANALYSIS TABLES

Run 7 Masked Tower IDs(L2Gamma & High Tower): 30, 55, 59, 95, 114, 169, 292, 308, 316, 334, 439, 509, 576, 580, 591, 600, 631, 636, 654, 714, 740, 775, 779, 784, 830, 882, 899, 915, 1020, 1025, 1130, 1132, 1153, 1172, 1197, 1257, 1278, 1294, 1300, 1320, 1340, 1350, 1480, 1537, 1665, 1666, 1709, 1786, 1791, 1800, 1871, 1909, 1935, 1938, 1945, 2043, 2058, 2171, 2313, 2383, 2398, 2559, 2642, 2774, 2878, 2880, 3093, 3240, 3271, 3273, 3277, 3280, 3359, 3518, 3559, 3577, 3597, 3673, 3674, 3711, 3720, 3750, 3751, 3840, 3916, 4005, 4006, 4007, 4133, 4260, 4262, 4400, 4422, 4453, 4498, 4539

Run 10 Masked Tower IDs(L2Gammam): 23, 29, 30, 96, 308, 555, 576, 591, 796, 882, 897, 903, 963, 986, 1176, 1197, 1278, 1284, 1294, 1337, 1350, 1378, 1382, 1537, 1705, 1709, 1781, 1787, 1909, 1921, 1935, 1966, 1986, 2043, 2047, 2050, 2068, 2129, 2141, 2171, 2181, 2190, 2192, 2248, 2290, 2445, 2497, 2749, 2981, 3013, 3028, 3061, 3083, 3163, 3186, 3215, 3271, 3273, 3327, 3375, 3481, 3686, 3691, 3692, 3821, 3838, 3861, 3948, 4006, 4013, 4226, 4288, 4423, 4482, 4498, 4563

Run 10 Masked Tower IDs(High Tower): 23, 30, 96, 308, 555, 561, 562, 576, 637, 681, 749, 796, 801, 882, 897, 953, 954, 986, 1044, 1046, 1078, 1130, 1132, 1176, 1197, 1278, 1284, 1294, 1306, 1337, 1350, 1375, 1378, 1382, 1397, 1537, 1705, 1709, 1781, 1787, 1909, 1935, 1984, 2043, 2050, 2068, 2097, 2106, 2129, 2141, 2162, 2171, 2190, 2192, 2290, 2445, 2589, 2749, 3013, 3028, 3061, 3271, 3273, 3375, 3690, 3692, 3718, 3821, 3838, 3861, 3948, 4013, 4288, 4498, 4563, 4765

Table A.1.: γ -triggered (direct- γ -rich sample) ridge yields (Run 7, method 1) with their associated statistical and systematic errors.

$P_T bin$	$\langle P_T \rangle$	No. of Trig.	Yield	Stat. Err.	% Sys. Err.
5.5 – 7.0	6.2	35,729	-0.013	0.050	215.3
7.0 – 8.0	7.4	10,051	0.024	0.093	92.8
8.0 – 10.0	8.8	7,521	0.14	0.11	10.6
10.0 – 12.0	10.8	2,090	0.064	0.23	15.2
12.0 – 16.0	13.4	865	0.33	0.32	1.1

Table A.2.: γ -triggered (direct- γ -rich sample) ridge yields (Run 7, M2) with their associated statistical and systematic errors.

$P_T bin$	$\langle P_T \rangle$	No. of Trig.	Yield	Stat. Err.	% Sys. Err.
5.5 – 7.0	6.2	35,729	-6.64e-05	0.048	40773.5
7.0 – 8.0	7.4	10,051	0.083	0.090	24.8
8.0 – 10.0	8.8	7,521	0.018	0.10	79.8
10.0 – 12.0	10.8	2,090	0.080	0.22	11.08
12.0 – 16.0	13.4	865	0.069	0.31	5.28

Table A.3.: γ -triggered (π^0 -rich sample) ridge yields (Run 7, method 1) with their associated statistical and systematic errors.

$P_T bin$	$\langle P_T \rangle$	No. of Trig.	Yield	Stat. Err.	% Sys. Err.
5.5 – 7.0	6.2	71,480	0.078	0.036	18.2
7.0 – 8.0	7.4	20,460	0.049	0.067	21.6
8.0 – 10.0	8.8	17,092	-0.057	0.071	11.5
10.0 – 12.0	10.8	5,361	0.065	0.13	5.0
12.0 – 16.0	13.4	2,756	-0.16	0.18	0.8

Table A.4.: γ -triggered (π^0 -rich sample) ridge yields (Run 7, M2) with their associated statistical and systematic errors.

$P_T bin$	$\langle P_T \rangle$	No. of Trig.	Yield	Stat. Err.	% Sys. Err.
5.5 – 7.0	6.2	71,480	0.12	0.036	11.1
7.0 – 8.0	7.4	20,460	0.075	0.066	13.4
8.0 – 10.0	8.8	17,092	-0.040	0.069	15.3
10.0 – 12.0	10.8	5,361	0.080	0.13	3.8
12.0 – 16.0	13.4	2,756	-0.12	0.17	0.9

Table A.5.: γ -triggered (direct- γ -rich sample) ridge yields (Run 7, method 1) with their associated statistical and systematic errors.

$P_T bin$	$\langle P_T \rangle$	No. of Trig.	Yield	Stat. Err.	% Sys. Err.
5.5 – 7.0	6.2	204,724	0.086	0.021	28.2
7.0 – 8.0	7.4	46,960	-0.0048	0.045	4011.3
8.0 – 10.0	8.8	49,688	0.067	0.040	20.14
10.0 – 12.0	10.8	14,179	0.073	0.076	10.58
12.0 – 16.0	13.4	6,006	-0.064	0.12	5.5

Table A.6.: γ -triggered (direct- γ -rich sample) ridge yields (Run 7, M2) with their associated statistical and systematic errors.

$P_T bin$	$\langle P_T \rangle$	No. of Trig.	Yield	Stat. Err.	% Sys. Err.
5.5 – 7.0	6.2	204,724	0.038	0.021	59.8
7.0 – 8.0	7.4	46,960	0.0077	0.043	226.6
8.0 – 10.0	8.8	49,688	0.073	0.039	17.5
10.0 – 12.0	10.8	14,179	0.13	0.074	5.6
12.0 – 16.0	13.4	6,006	0.11	0.11	3.0

Table A.7.: γ -triggered (π^0 -rich sample) ridge yields (Run 7, method 1) with their associated statistical and systematic errors.

$P_T bin$	$\langle P_T \rangle$	No. of Trig.	Yield	Stat. Err.	% Sys. Err.
5.5 – 7.0	6.2	152,844	-0.011	0.030	404.0
7.0 – 8.0	7.4	39,714	-0.056	0.060	54.7
8.0 – 10.0	8.8	36,649	-0.011	0.050	177.4
10.0 – 12.0	10.8	11,944	-0.10	0.089	9.4
12.0 – 16.0	13.4	6,622	-0.085	0.12	3.9

Table A.8.: γ -triggered (π^0 -rich sample) ridge yields (Run 7, M2) with their associated statistical and systematic errors.

$P_T bin$	$\langle P_T \rangle$	No. of Trig.	Yield	Stat. Err.	% Sys. Err.
5.5 – 7.0	6.2	152,844	0.069	0.030	100.2
7.0 – 8.0	7.4	39,714	0.081	0.060	34.8
8.0 – 10.0	8.8	36,649	0.096	0.049	18.2
10.0 – 12.0	10.8	11,944	0.010	0.088	88.8
12.0 – 16.0	13.4	6,622	0.0066	0.12	46.3

Table A.9.: γ -rich M1 Run 7

	M1 5.5–7.0GeV	M1 7.0–8.0GeV	M1 8.0–10.0GeV	M1 10.0–12.0GeV	M1 12.0–16.0GeV
Y^{3bins}	0.078	0.049	-0.057	0.065	-0.16
Y^{2bins}	0.067	0.14	-0.030	0.082	-0.13
Y^{1bin}	0.053	0.19	-0.17	0.17	-0.65
σ_Y^3	0.036	0.067	0.071	0.13	0.18
σ_Y^2	0.041	0.075	0.080	0.15	0.20
σ_Y^1	0.053	0.097	0.10	0.19	0.27
$\%S_Z^{3,1}$	32.8	292.0	203.6	161.5	313.5
$\%S_Z^{3,2}$	14.6	186.6	47.3	25.8	19.7
$\%S_Z^{v2}$	18.2	21.6	11.5	5.0	0.750
$\%\sigma_Z^{3,1}$	48.9	141.1	135.7	205.4	124.8
$\%\sigma_Z^{3,2}$	24.3	70.4	65.9	103.1	59.1

Table A.10.: γ -rich M2 Run 7

	$M2$ 5.5–7.0GeV	$M2$ 7.0–8.0GeV	$M2$ 8.0–10.0GeV	$M2$ 10.0–12.0GeV	$M2$ 12.0–16.0GeV
Y^{3bins}	0.12	0.074	-0.040	0.080	-0.12
Y^{2bins}	0.12	0.11	-0.053	0.13	-0.063
Y^{1bin}	0.092	0.15	-0.12	0.17	-0.24
σ_Y^3	0.036	0.067	0.070	0.13	0.17
σ_Y^2	0.037	0.070	0.073	0.13	0.18
σ_Y^1	0.042	0.078	0.083	0.15	0.21
$\%S_Z^{3,1}$	23.2	99.364	201.7	109.3	98.8
$\%S_Z^{3,2}$	3.4	48.9	32.2	65.6	47.2
$\%S_Z^{v2}$	11.1	13.4	15.3	3.8	0.95
$\%\sigma_Z^{3,1}$	19.0	55.6	114.4	99.3	97.3
$\%\sigma_Z^{3,2}$	9.4	27.8	56.2	49.5	47.0

Table A.11.: π^0 -rich M1 Run 7

	$M1$ 5.5–7.0GeV	$M1$ 7.0–8.0GeV	$M1$ 8.0–10.0GeV	$M1$ 10.0–12.0GeV	$M1$ 12.0–16.0GeV
Y^{3bins}	-0.013	0.024	0.14	0.064	0.33
Y^{2bins}	-0.037	0.034	0.17	0.17	0.19
Y^{1bin}	-1.61×10^{-5}	0.064	0.12	0.44	-0.56
σ_Y^3	0.050	0.093	0.11	0.23	0.32
σ_Y^2	0.056	0.10	0.12	0.26	0.36
σ_Y^1	0.072	0.13	0.15	0.33	0.49
$\%S_Z^{3,1}$	99.9	171.0	13.0	591.5	270.8
$\%S_Z^{3,2}$	179.1	42.9	19.2	162.6	43.2
$\%S_Z^{v_2}$	215.3	92.8	10.6	15.2	1.2
$\%\sigma_Z^{3,1}$	391.1	411.5	81.1	363.1	112.7
$\%\sigma_Z^{3,2}$	197.0	205.0	40.091	191.3	52.3

Table A.12.: π^0 -rich M2 Run 7

	$M2$ 5.5–7.0GeV	$M2$ 7.0–8.0GeV	$M2$ 8.0–10.0GeV	$M2$ 10.0–12.0GeV	$M2$ 12.0–16.0GeV
Y^{3bins}	-6.64×10^{-5}	0.08	0.018	0.080	0.069
Y^{2bins}	0.015	0.075	0.023	0.13	-0.033
Y^{1bin}	0.059	0.037	-0.0056	0.36	-0.38
σ_Y^3	0.048	0.090	0.10	0.22	0.31
σ_Y^2	0.051	0.095	0.11	0.23	0.33
σ_Y^1	0.057	0.11	0.12	0.26	0.38
$\%S_Z^{3,1}$	88837.0	55.1	131.8	347.2	652.4
$\%S_Z^{3,2}$	22737.3	9.9	28.0	63.5	148.4
$\%S_Z^{v_2}$	40773.5	24.8	79.8	11.1	5.3
$\%\sigma_Z^{3,1}$	47482.2	71.4	386.6	173.1	317.5
$\%\sigma_Z^{3,2}$	23854.3	35.5	191.9	90.7	152.4

Table A.13.: γ -rich M1 Run 10

	$M1$ 5.5–7.0GeV	$M1$ 7.0–8.0GeV	$M1$ 8.0–10.0GeV	$M1$ 10.0–12.0GeV	$M1$ 12.0–16.0GeV
Y^{3bins}	-0.011	-0.056	-0.011	-0.10	-0.085
Y^{2bins}	0.015	-0.055	-0.065	-0.13	-0.054
Y^{1bin}	0.081	-0.073	-0.049	-0.028	-0.28
σ_Y^3	0.030	0.060	0.050	0.089	0.12
σ_Y^2	0.034	0.068	0.056	0.10	0.16
σ_Y^1	0.043	0.088	0.072	0.13	0.18
$\%S_Z^{3,1}$	867.3	31.2	365.4	72.7	234.4
$\%S_Z^{3,2}$	239.8	1.3	513.6	29.3	36.5
$\%S_Z^{v2}$	404.0	54.7	177.4	9.4	3.9
$\%\sigma_Z^{3,1}$	294.2	115.2	499.9	90.3	155.4
$\%\sigma_Z^{3,2}$	148.5	57.4	254.6	46.3	74.6

Table A.14.: γ -rich M2 Run 10

	$M2$ 5.5–7.0GeV	$M2$ 7.0–8.0GeV	$M2$ 8.0–10.0GeV	$M2$ 10.0–12.0GeV	$M2$ 12.0–16.0GeV
Y^{3bins}	0.070	0.081	0.096	0.010	0.0067
Y^{2bins}	0.085	0.095	0.076	-0.022	0.048
Y^{1bin}	0.13	0.092	0.073	0.049	-0.039
σ_Y^3	0.030	0.060	0.049	0.088	0.12
σ_Y^2	0.031	0.062	0.052	0.092	0.12
σ_Y^1	0.035	0.070	0.0581	0.10	0.14
$\%S_Z^{3,1}$	81.8	13.6	23.7	384.0	690.0
$\%S_Z^{3,2}$	21.7	17.0	20.2	314.9	621.6
$\%S_Z^{v2}$	57.7	34.8	18.2	88.8	46.3
$\%\sigma_Z^{3,1}$	26.5	46.3	32.2	537.9	1146.3
$\%\sigma_Z^{3,2}$	13.4	23.1	16.3	274.8	556.0

Table A.15.: π^0 -rich M1 Run 10

	M1 5.5–7.0GeV	M1 7.0–8.0GeV	M1 8.0–10.0GeV	M1 10.0–12.0GeV	M1 12.0–16.0GeV
Y^{3bins}	0.086	-0.0048	0.067	0.073	-0.064
Y^{2bins}	0.097	0.053	0.088	0.079	-0.041
Y^{1bin}	0.13	0.19	0.0513	0.13	-0.075
σ_Y^3	0.021	0.045	0.040	0.076	0.12
σ_Y^2	0.024	0.050	0.045	0.086	0.13
σ_Y^1	0.030	0.064	0.058	0.11	0.17
$\%S_Z^{3,1}$	50.0	3992.4	23.1	70.7	17.1
$\%S_Z^{3,2}$	13.8	1199.7	31.6	8.2	36.2
$\%S_Z^{v2}$	28.2	388.6	20.1	10.6	5.6
$\%\sigma_Z^{3,1}$	25.7	942.0	62.6	108.5	193.1
$\%\sigma_Z^{3,2}$	12.9	478.8	31.0	54.2	96.3

Table A.16.: π^0 -rich M2 Run 10

	$M2$ 5.5–7.0GeV	$M2$ 7.0–8.0GeV	$M2$ 8.0–10.0GeV	$M2$ 10.0–12.0GeV	$M2$ 12.0–16.0GeV
Y^{3bins}	0.038	0.0077	0.073	0.13	0.11
Y^{2bins}	0.051	0.030	0.086	0.12	0.14
Y^{1bin}	0.076	0.067	0.051	0.13	0.12
σ_Y^3	0.021	0.043	0.039	0.074	0.11
σ_Y^2	0.022	0.046	0.041	0.078	0.12
σ_Y^1	0.024	0.052	0.046	0.089	0.13
$\%S_Z^{3,1}$	99.5	769.3	29.6	2.4	11.1
$\%S_Z^{3,2}$	32.8	286.2	18.0	6.6	28.0
$\%S_Z^{v2}$	59.8	226.6	17.5	5.6	3.0
$\%\sigma_Z^{3,1}$	35.0	359.2	34.8	36.5	66.8
$\%\sigma_Z^{3,2}$	17.5	181.2	17.2	18.3	33.3