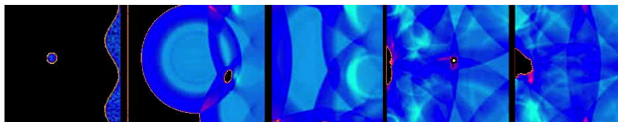


# $\Delta\eta$ - $\Delta\phi$ correlations and ridge in STAR

L.C. De Silva

for the STAR collaboration

University of Houston



28th Winter Workshop on Nuclear Dynamics  
Dorado del Mar, Puerto Rico



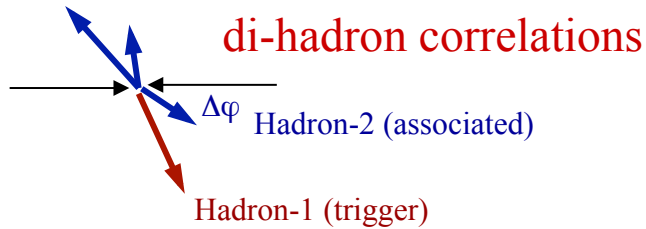
# Outline

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- Motivation
- Correlation measure
- $P_T$  dependence of  $\Delta\eta$ - $\Delta\phi$  correlations
- Model fit function
- Data interpretation
- Other ridge studies from STAR
- Summary and discussion



# Motivation – long range correlation in $\Delta\eta$



Centrality evolution using all charged particles – Untriggered analysis

proton-proton

Au-Au: 80-100%

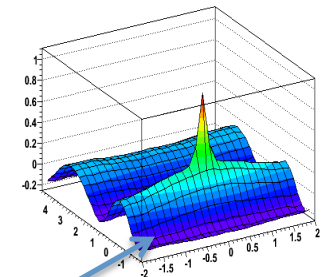
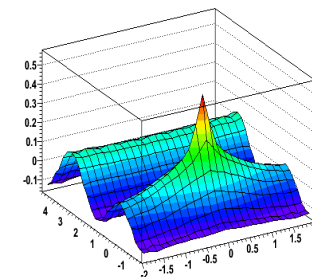
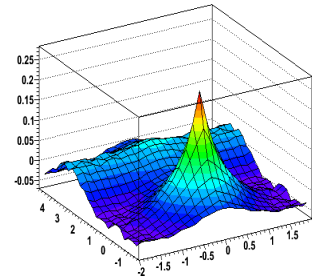
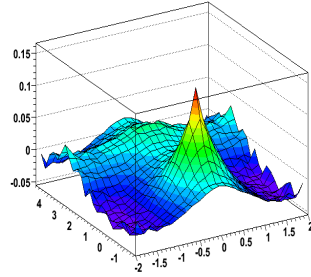
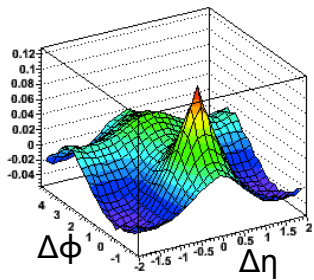
Au-Au: 70-80%

Au-Au: 50-60%

STAR preliminary

Au-Au: 00-10%

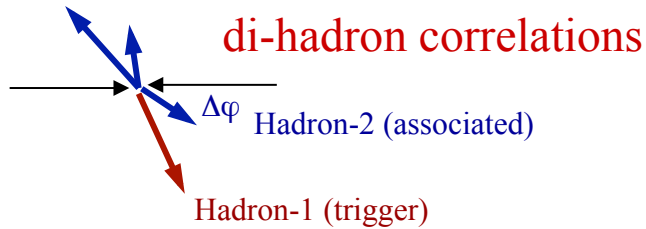
$$\frac{\Delta\rho}{\sqrt{\rho_{ref}}}$$



Long range correlation in  $\Delta\eta$  ("ridge")



# Motivation – long range correlation in $\Delta\eta$



Centrality evolution using all charged particles – Untriggered analysis

proton-proton

Au-Au: 80-100%

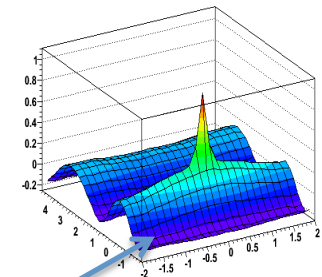
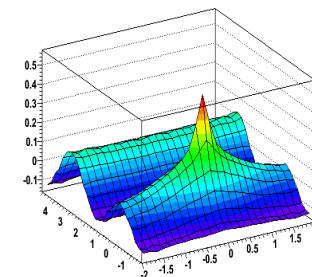
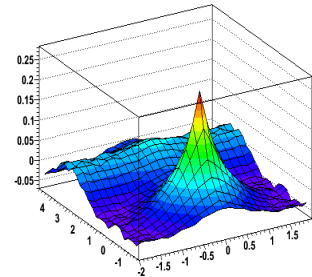
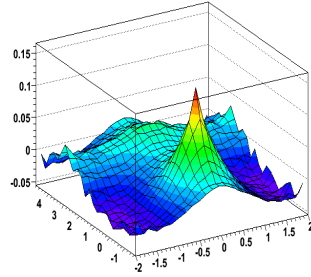
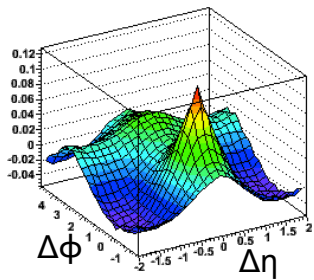
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STAR preliminary

— Au-Au: 00-10%

$$\frac{\Delta\rho}{\sqrt{\rho_{ref}}}$$

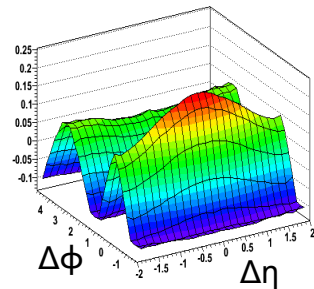


Long range correlation in  $\Delta\eta$  (“ridge”)

Momentum evolution – Untriggered analysis

$p_T > 0.15 \text{ GeV}/c$  Au-Au: 00-10%

$$\frac{\Delta\rho}{\sqrt{\rho_{ref}}}$$

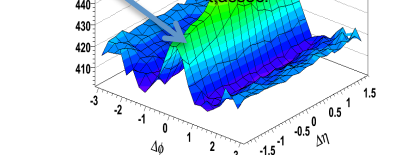


Phys. Rev. C 80, 064912 (2009)

Au-Au 0-10%:  $\sqrt{s_{NN}} = 200 \text{ GeV}$

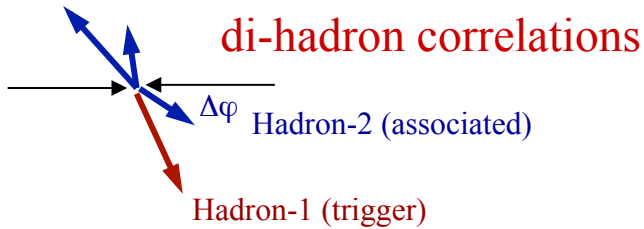
$3 < p_{T,trigger} < 4 \text{ GeV}$

$p_{T,assoc} > 2 \text{ GeV}$





# Motivation – long range correlation in $\Delta\eta$



Centrality evolution using all charged particles – Untriggered analysis

STAR preliminary

proton-proton

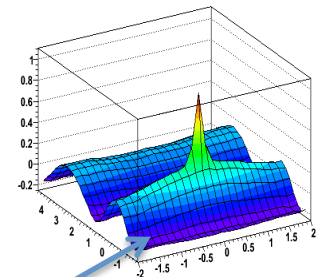
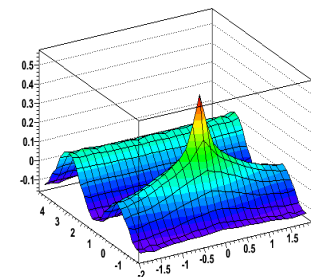
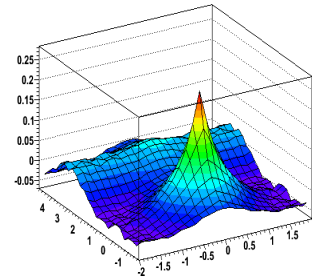
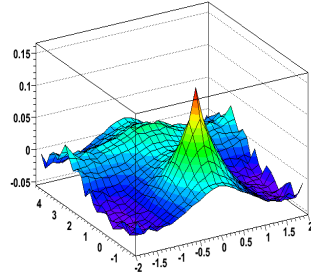
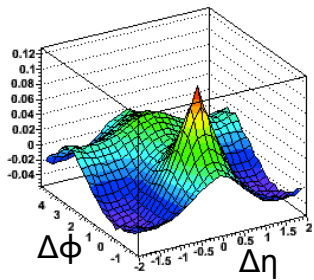
Au-Au: 80-100%

Au-Au: 70-80%

Au-Au: 50-60%

Au-Au: 00-10%

$$\frac{\Delta\rho}{\sqrt{\rho_{ref}}}$$



Long range correlation in  $\Delta\eta$  ("ridge")

Momentum evolution – Untriggered analysis

$p_T > 0.15 \text{ GeV}/c$  Au-Au: 00-10%

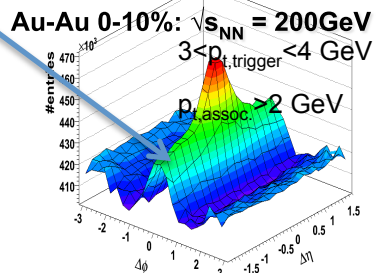
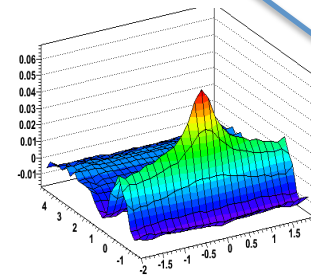
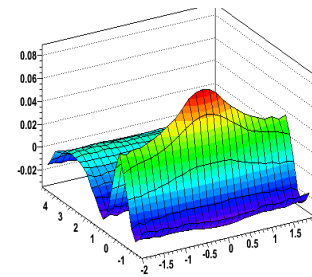
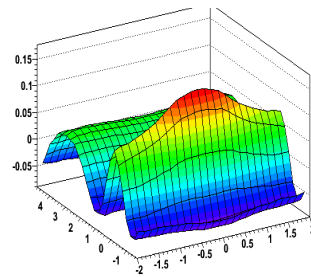
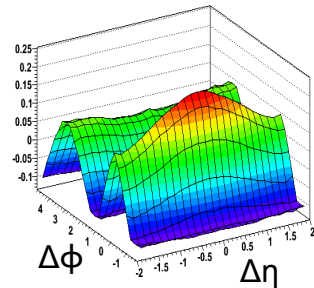
$p_T > 1.1 \text{ GeV}/c$

$p_T > 1.7 \text{ GeV}/c$

$p_T > 2.1 \text{ GeV}/c$

Phys. Rev. C 80, 064912 (2009)

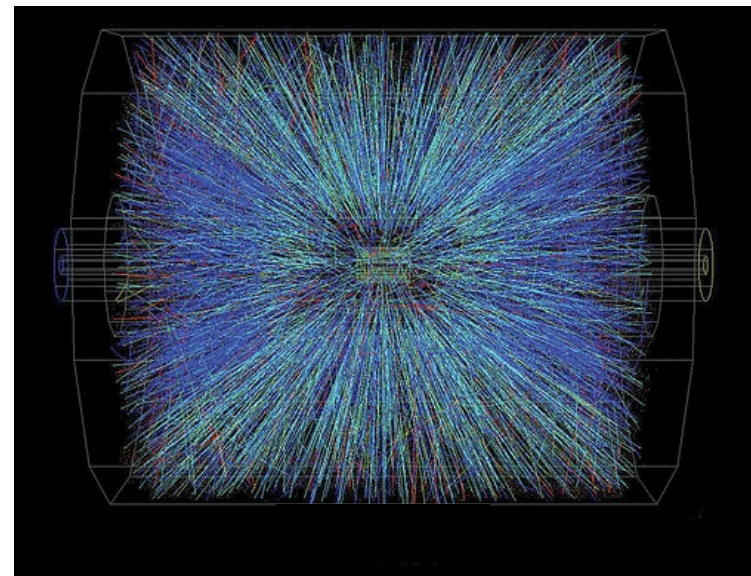
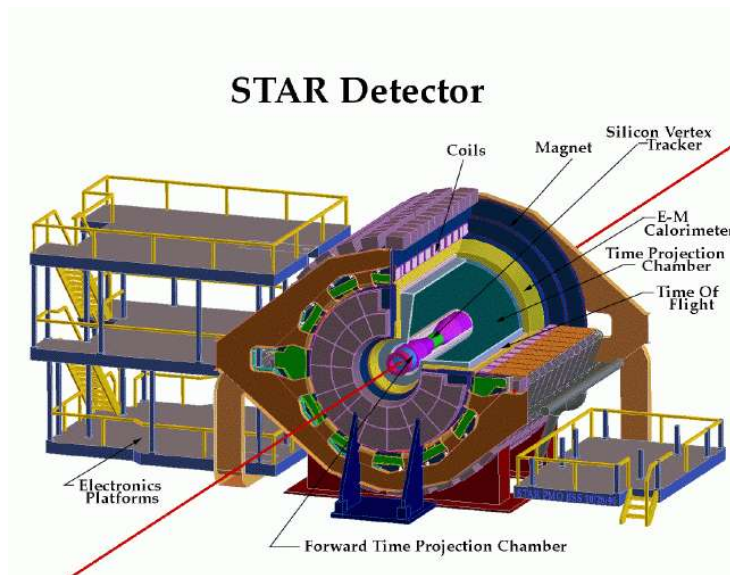
$$\frac{\Delta\rho}{\sqrt{\rho_{ref}}}$$



• We increase the momentum of both particles

# Data and cuts

- Au+Au 200GeV – 0-10%, 11M events
- p+p 200GeV – Minimum bias, 264M events
- Event cuts: Primary vertex cut (+/- 25cm) and z-vertex sub binning
- Track cuts:
  - Charged particle tracks in TPC were used
  - $p_T \geq x$  GeV/c; lower limit  $x$  is varied for both particles for the  $p_T$  evolution ( 0.15, 0.3, 0.5 GeV/c, .....)
  - $-1 \leq \eta \leq 1$



Tracks produced in a central event<sup>6</sup>

# Correlation Measure

❖ We construct the Pearson's correlation coefficient

- $\rho$  = Two particle density

- Sibling Pairs

$$\rho_{sib}(p_t, \eta, \phi) = \frac{\overline{n_a n_b}}{Area}$$

- Mixed Pairs

$$\rho_{ref}(p_t, \eta, \phi) = \frac{\overline{n_a n_b}}{Area}$$

Mix events in a multiplicity window of  $\pm 50$

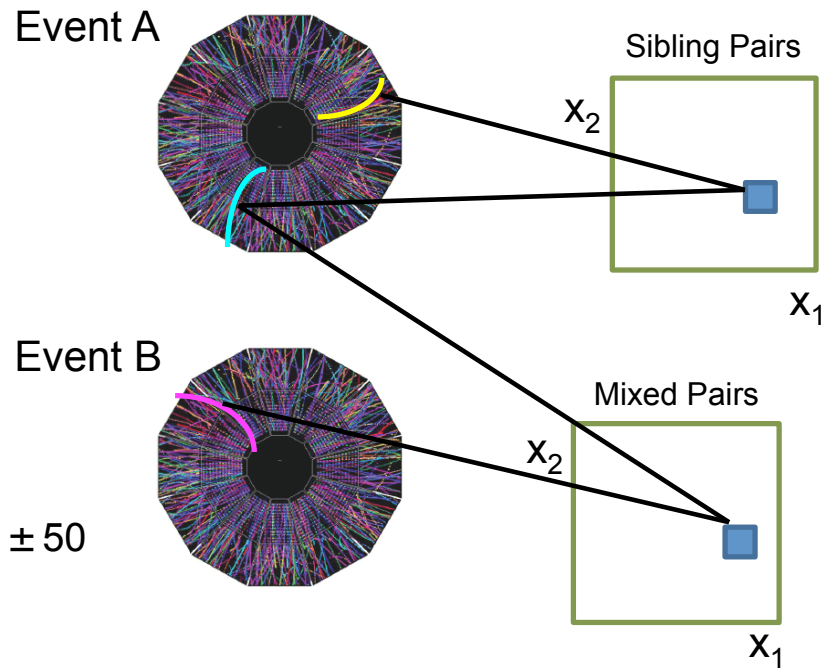
- Final Measure:

$$\frac{\rho_{sib} - \rho_{ref}}{\sqrt{\rho_{ref}}} = \frac{\Delta\rho}{\sqrt{\rho_{ref}}} \rightarrow \sqrt{\rho_{ref}} \frac{\Delta\rho}{\rho_{ref}}$$

Normalized Ref Pairs: Total number of sibling to mixed pairs

$$\frac{dN_{ch}}{d\eta d\phi}$$

- Number of correlated pairs *per* final state particle

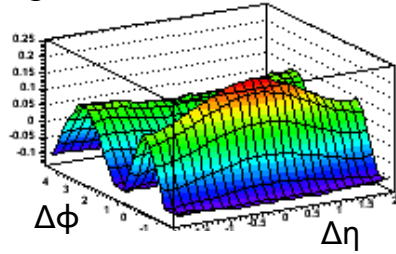


# Momentum evolution – AuAu200GeV

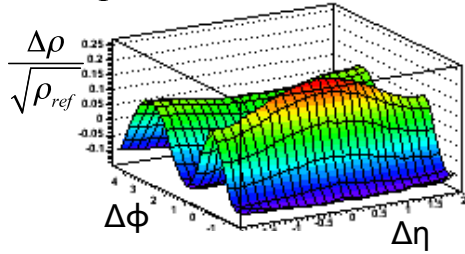
0 – 10%

STAR preliminary

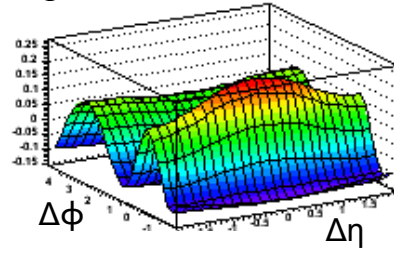
$p_T > 150 \text{ MeV}/c$



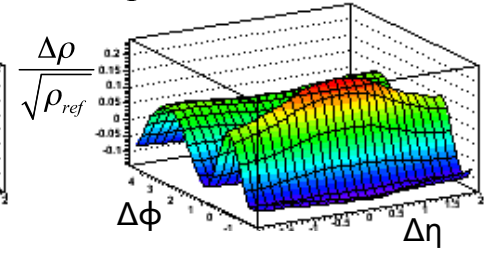
$p_T > 300 \text{ MeV}/c$



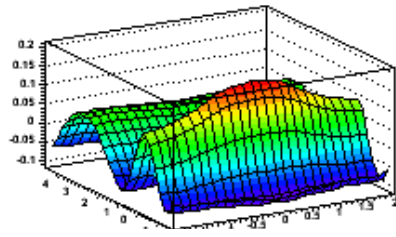
$p_T > 500 \text{ MeV}/c$



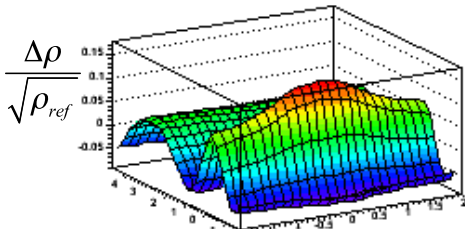
$p_T > 700 \text{ MeV}/c$



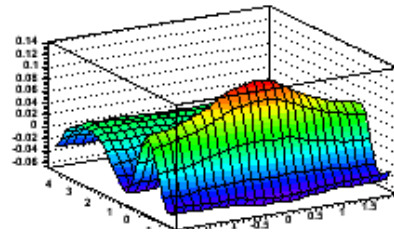
$p_T > 900 \text{ MeV}/c$



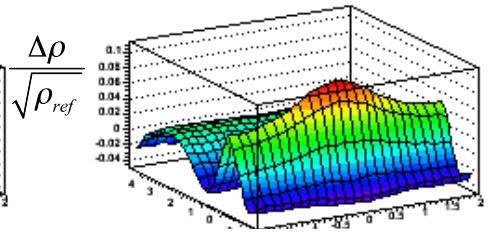
$p_T > 1100 \text{ MeV}/c$



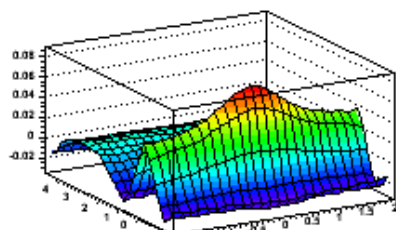
$p_T > 1300 \text{ MeV}/c$



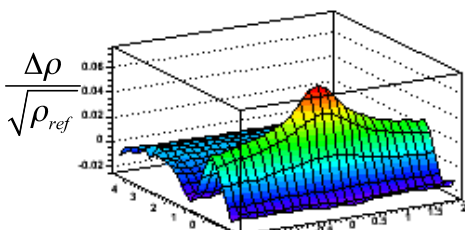
$p_T > 1500 \text{ MeV}/c$



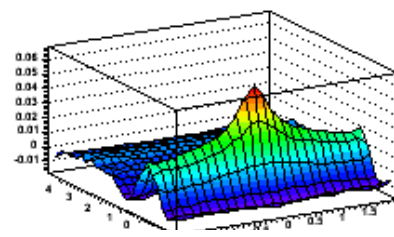
$p_T > 1700 \text{ MeV}/c$



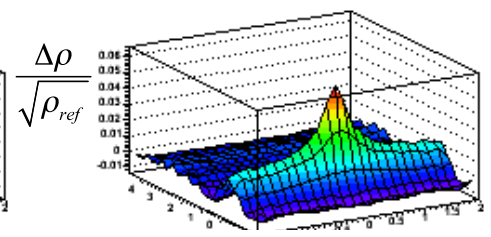
$p_T > 1900 \text{ MeV}/c$



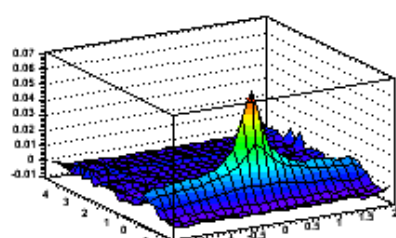
$p_T > 2100 \text{ MeV}/c$



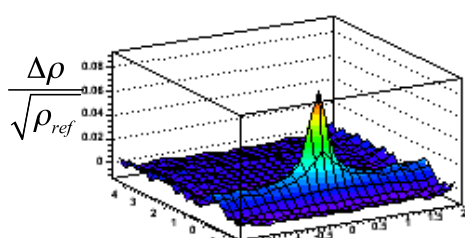
$p_T > 2300 \text{ MeV}/c$



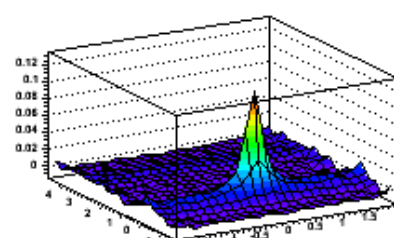
$p_T > 2500 \text{ MeV}/c$



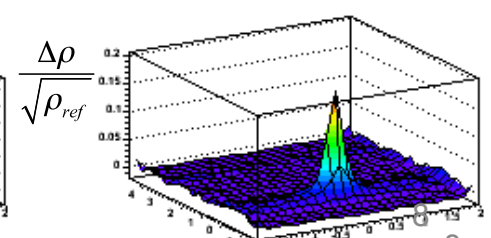
$p_T > 2700 \text{ MeV}/c$



$p_T > 2900 \text{ MeV}/c$



$p_T > 3100 \text{ MeV}/c$



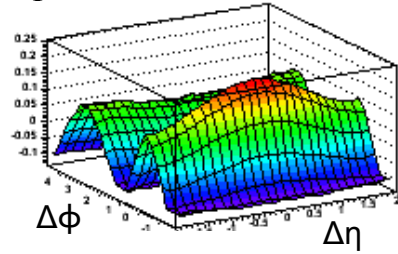


# Momentum evolution – AuAu200GeV

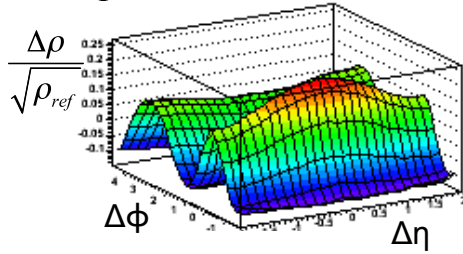
0 – 10%

STAR preliminary

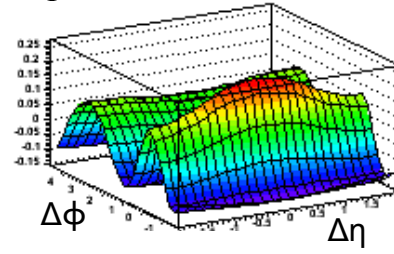
$p_T > 150 \text{ MeV}/c$



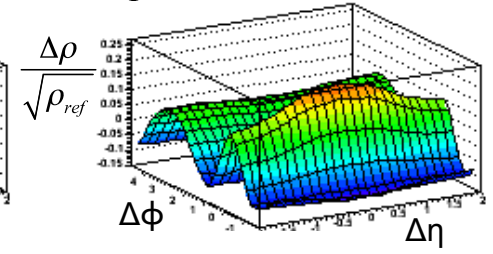
$p_T > 300 \text{ MeV}/c$



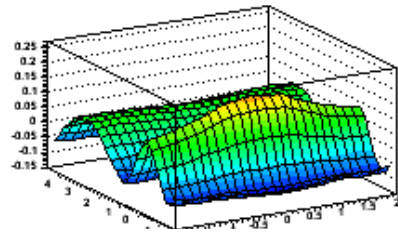
$p_T > 500 \text{ MeV}/c$



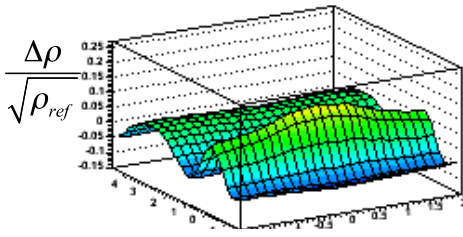
$p_T > 700 \text{ MeV}/c$



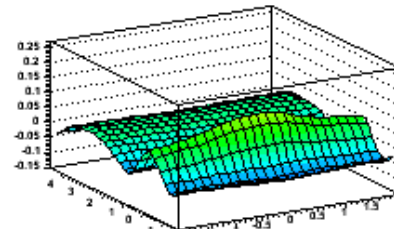
$p_T > 900 \text{ MeV}/c$



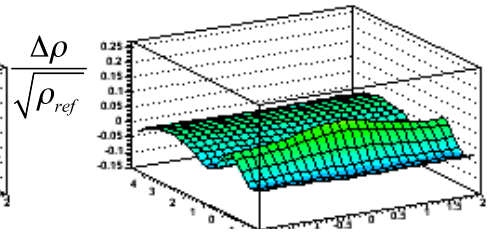
$p_T > 1100 \text{ MeV}/c$



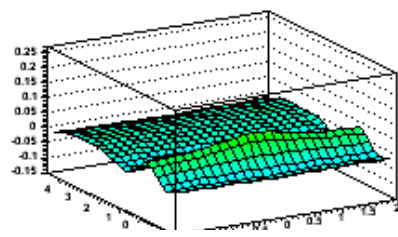
$p_T > 1300 \text{ MeV}/c$



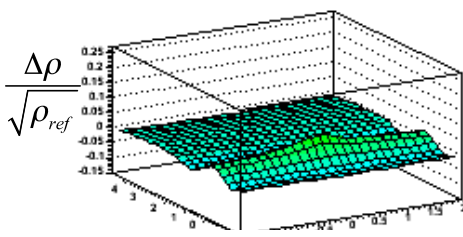
$p_T > 1500 \text{ MeV}/c$



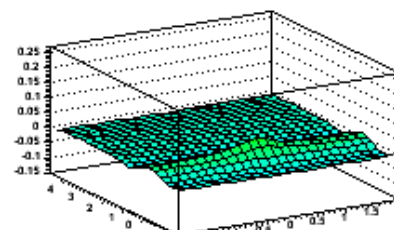
$p_T > 1700 \text{ MeV}/c$



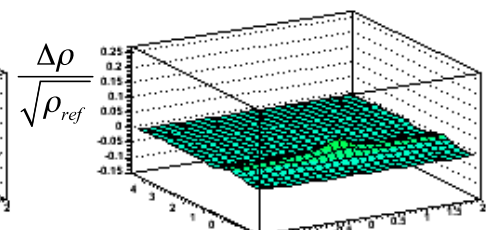
$p_T > 1900 \text{ MeV}/c$



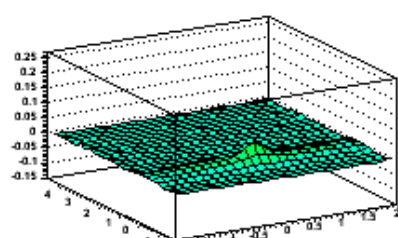
$p_T > 2100 \text{ MeV}/c$



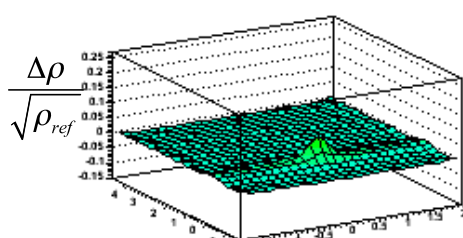
$p_T > 2300 \text{ MeV}/c$



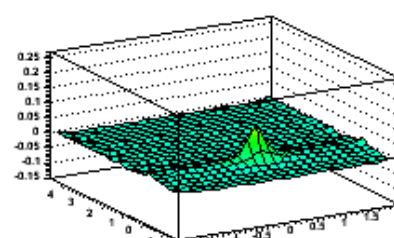
$p_T > 2500 \text{ MeV}/c$



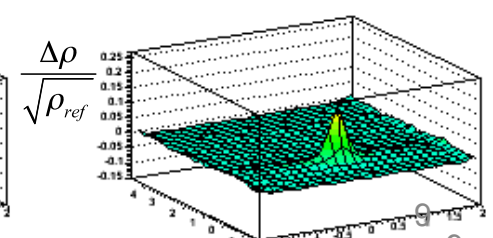
$p_T > 2700 \text{ MeV}/c$



$p_T > 2900 \text{ MeV}/c$



$p_T > 3100 \text{ MeV}/c$



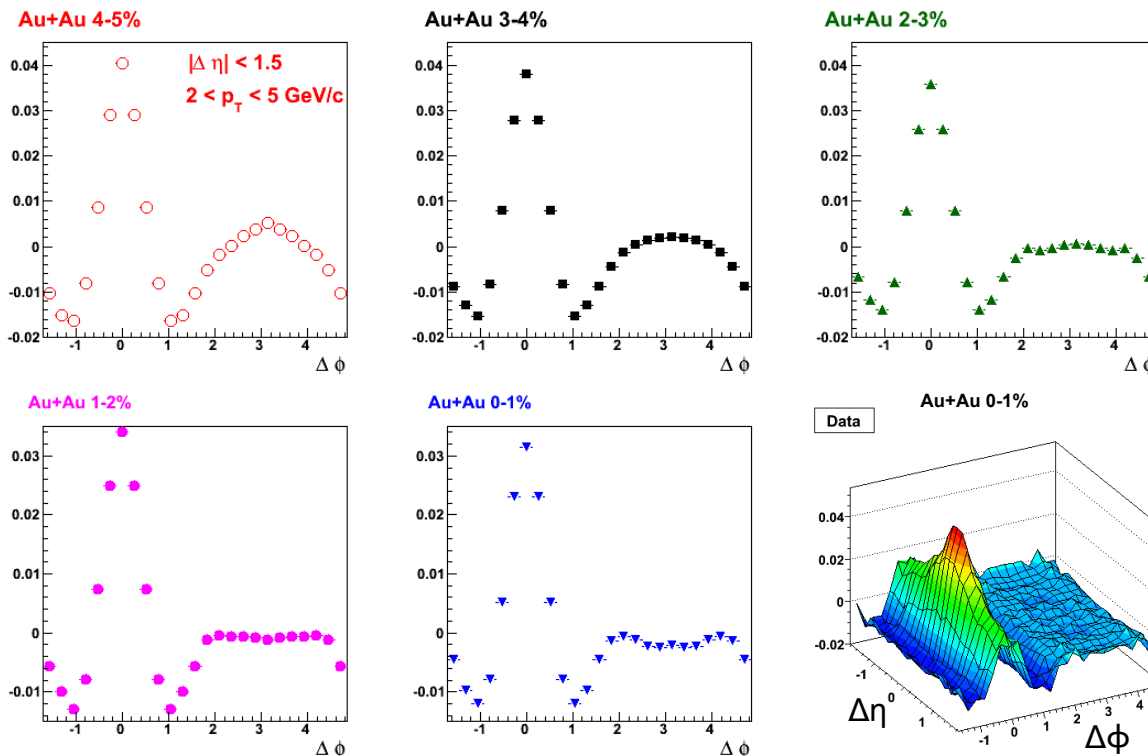
# Does the data support higher order harmonics?

Higher order Fourier coefficients seen in high  $p_T$  very central (0-1%) raw di-hadron correlation spectra at RHIC and LHC

$2 \leq p_T \leq 5 \text{ GeV/c}$

STAR preliminary

Theory prediction



Using a transport model theorists have predictions for higher order azimuthal anisotropies in very central events

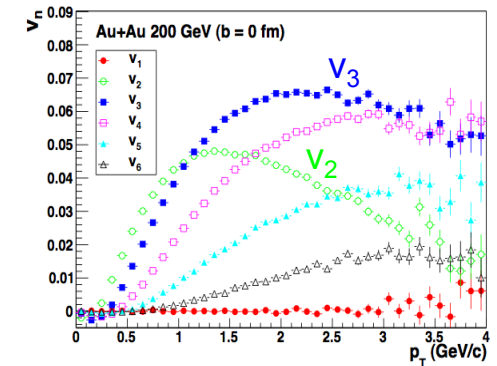


FIG. 2: (Color online) Azimuthal anisotropies of hadron spectra  $v_n(p_T)$  ( $n = 1 - 6$ ) in central ( $b = 0$ ) Au + Au collisions at  $\sqrt{s} = 200 \text{ GeV}$  from AMPT model calculation.

arXiv: 1011.5249v2

# Model Fit function

$$\begin{aligned}
 f_1 &\propto c_0 \\
 f_2 &\propto c_1 \cdot \cos(\Delta\phi) \\
 f_3 &\propto c_2 \cdot \cos(2\Delta\phi) \\
 f_4 &\propto c_3 \cdot \cos(3\Delta\phi) \\
 f_5 &\propto c_4 \cdot \cos(4\Delta\phi) \\
 f_6 &\propto c_5 \cdot \cos(5\Delta\phi) \\
 f_7 &\propto c_6 \cdot \exp(-0.5 \cdot ((\Delta\eta/c_7)^2 + (\Delta\phi/c_8)^2))
 \end{aligned}$$

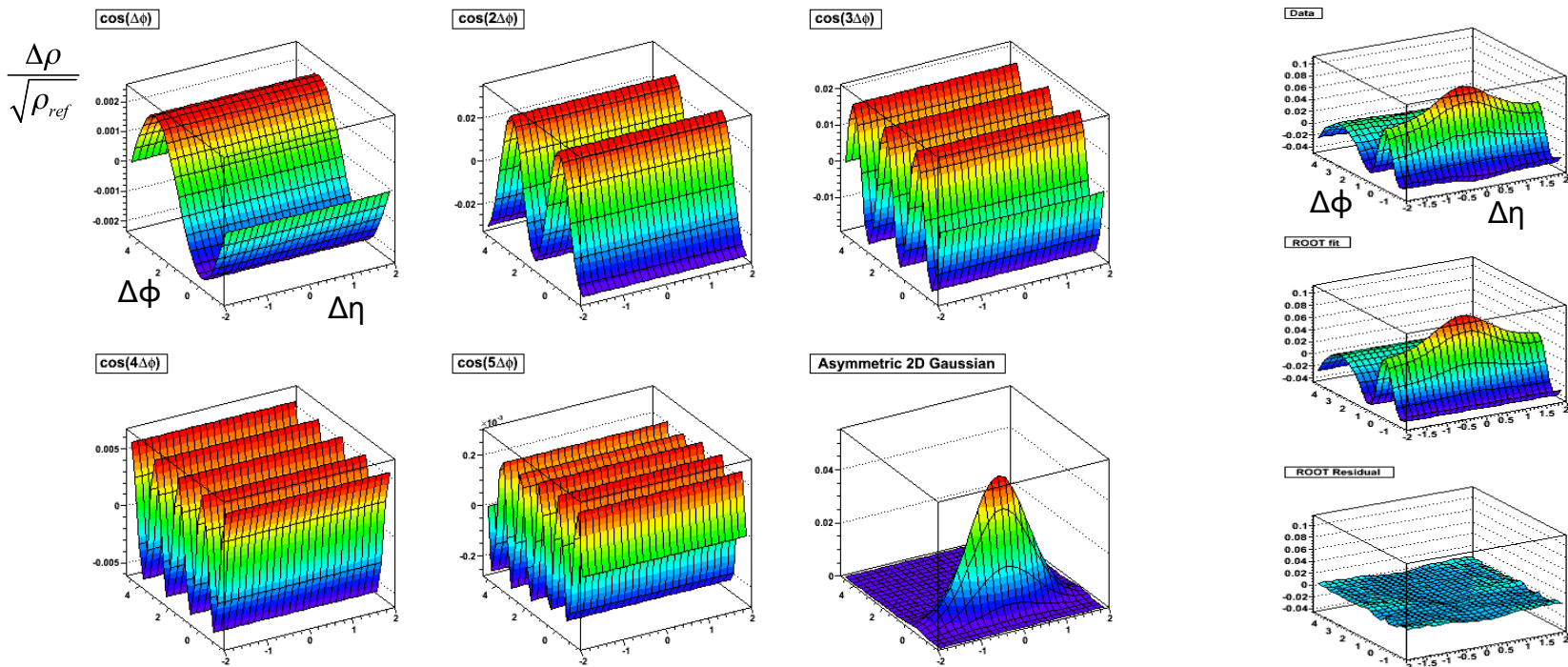
Offset  
 Away-side momentum conservation  
 2<sup>nd</sup> order Fourier term  
 3<sup>rd</sup> order Fourier term  
 4<sup>th</sup> order Fourier term  
 5<sup>th</sup> order Fourier term  
 Asymmetric 2d Gaussian

❖ Asymmetric 2d Gaussian assumed to be modified jet fragmentation

$p_T > 1.5 \text{ GeV}/c : 0-10\%$

$$f = f_1 + f_2 + f_3 + f_4 + f_5 + f_6 + f_7$$

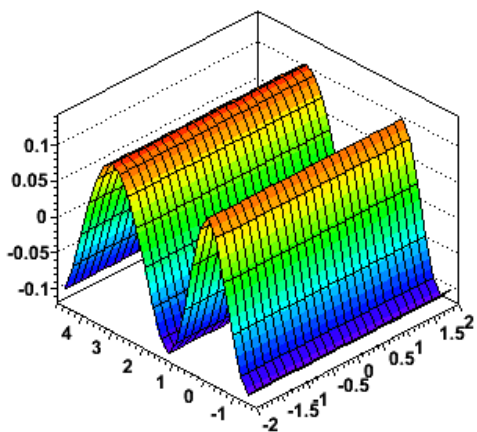
STAR preliminary



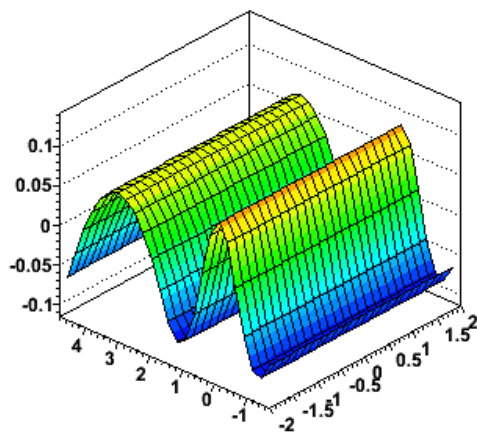
# Model fit - harmonics

- $\langle p_T \rangle$  evolution of resulting harmonics structure :  $v_2 + v_3 + v_4 + v_5$

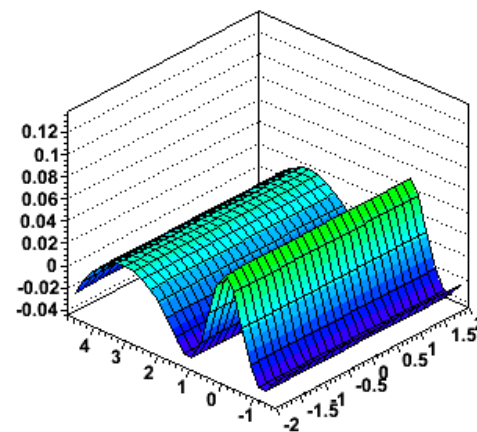
$p_T > 300$  MeV/c



$p_T > 900$  MeV/c

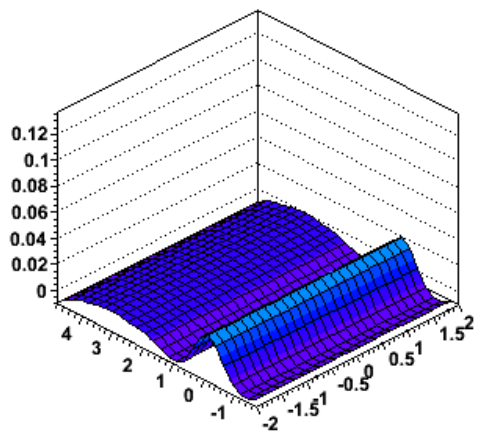


$p_T > 1500$  MeV/c

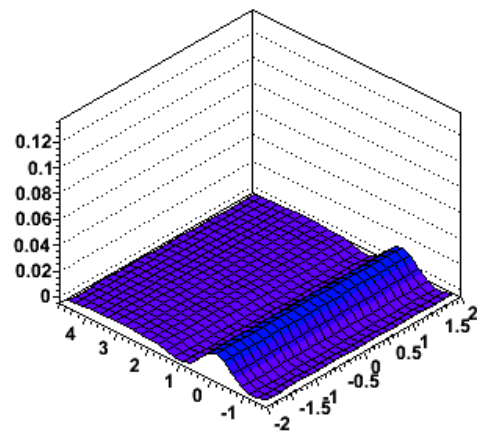


STAR preliminary

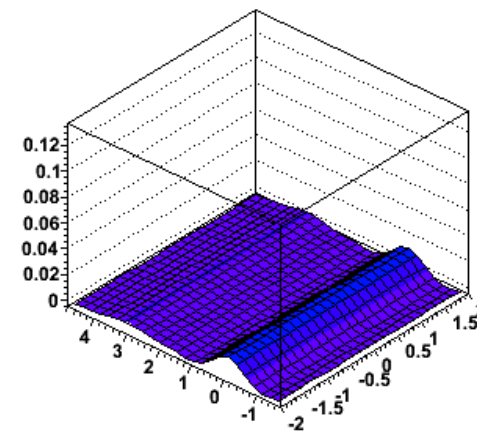
$p_T > 2100$  MeV/c



$p_T > 2500$  MeV/c



$p_T > 3100$  MeV/c

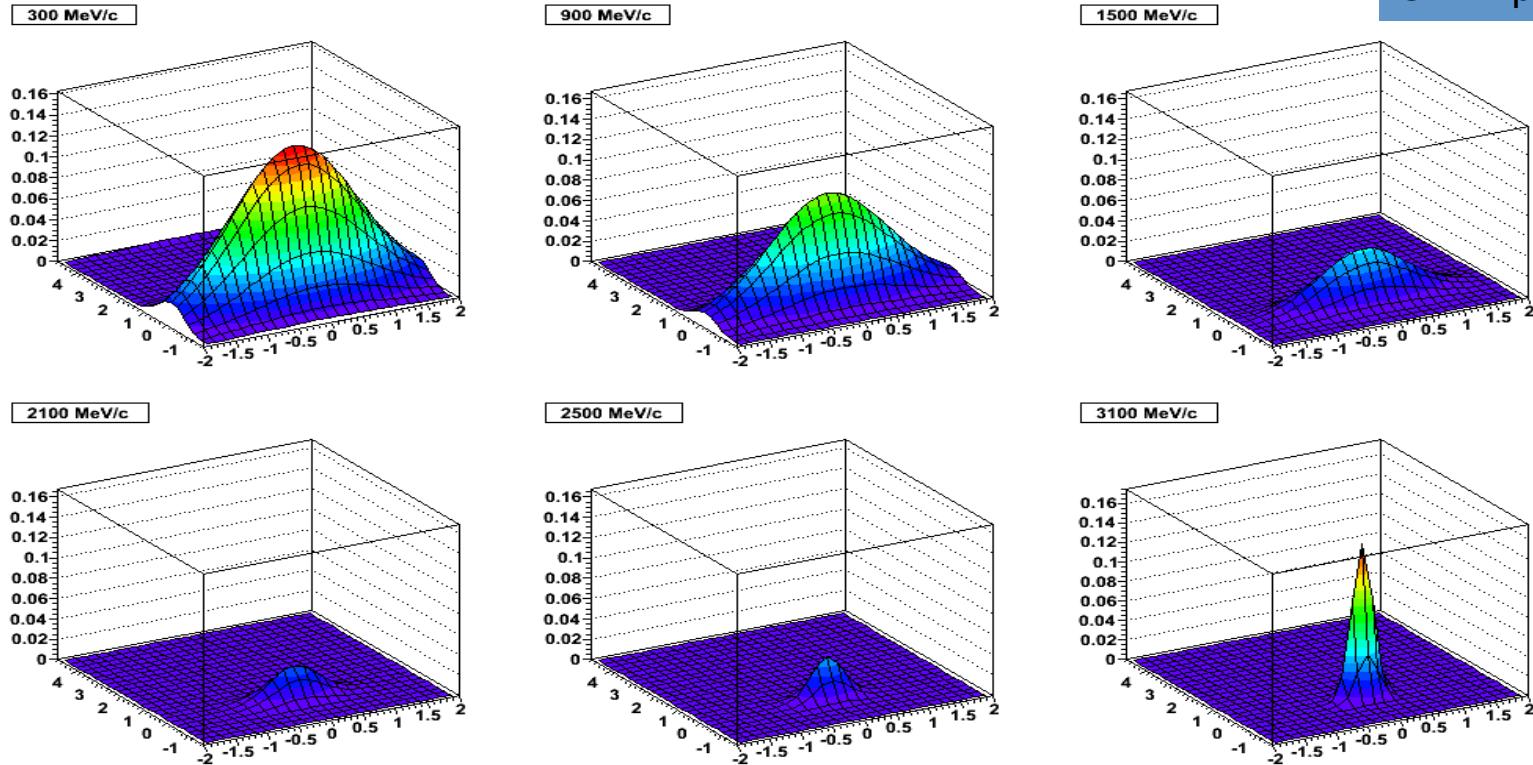


- Harmonics do not model  $\Delta\eta$  dependence

# Model fit - asymmetric 2d Gaussian

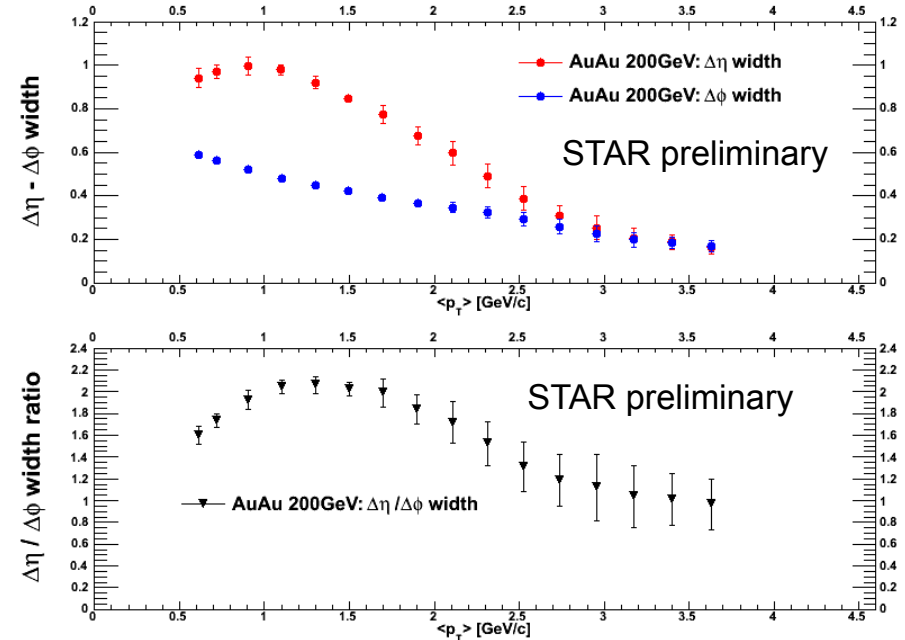
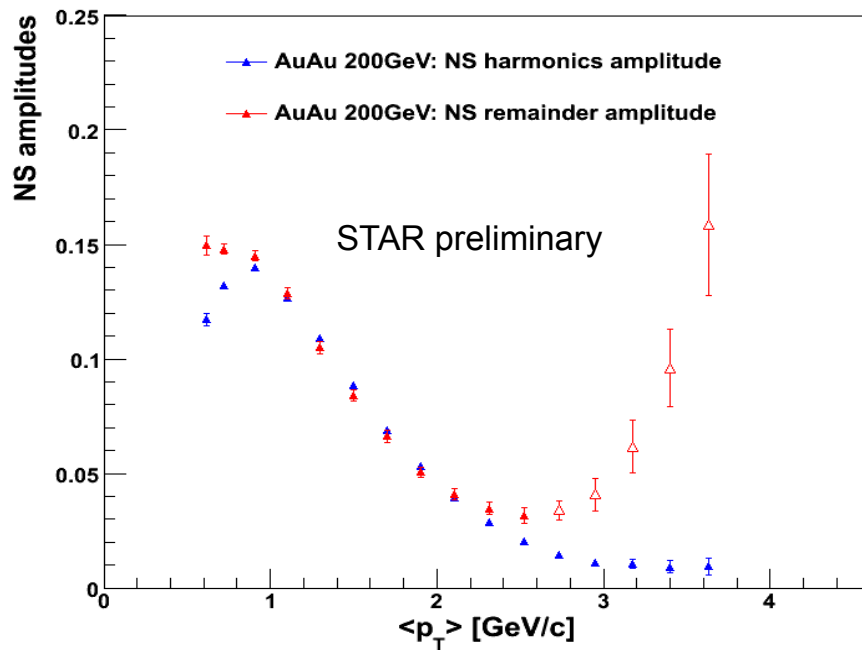
- Shows the asymmetric 2d Gaussian (“remainder”) component  $p_T$  cut evolution after higher harmonics subtraction

STAR preliminary



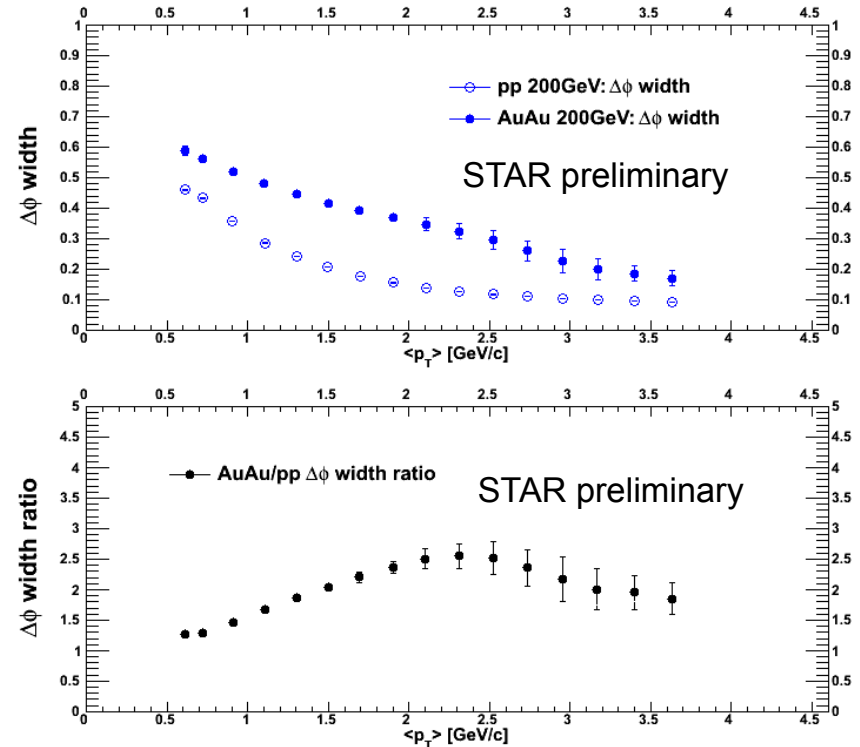
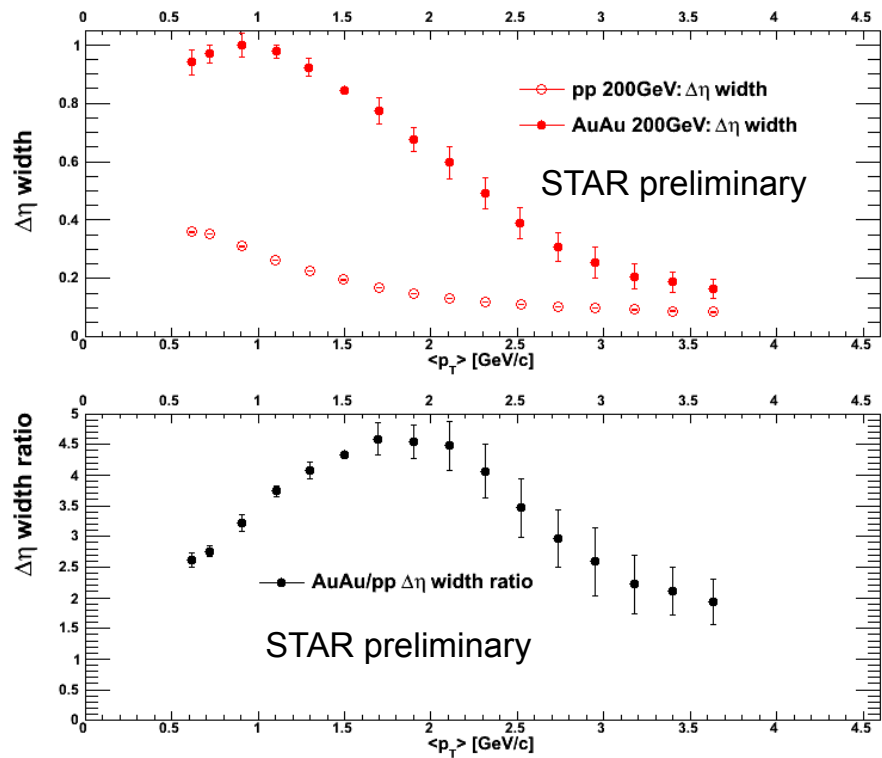
- Near side (NS) peak strength around (0,0) increases at higher  $p_T$  cuts
  - An effect due to definition of correlation measure (also visible in raw correlation)
  - The effect is constrained in a narrow  $\Delta\eta$ - $\Delta\phi$  region around (0,0) (“jet region”)
  - In this region the raw same event and mixed event pair count fall off exponentially
  - The relative fall off for same event pairs is smaller compared to mixed pairs as a function of  $p_T$  cut

# Free parameter comparison



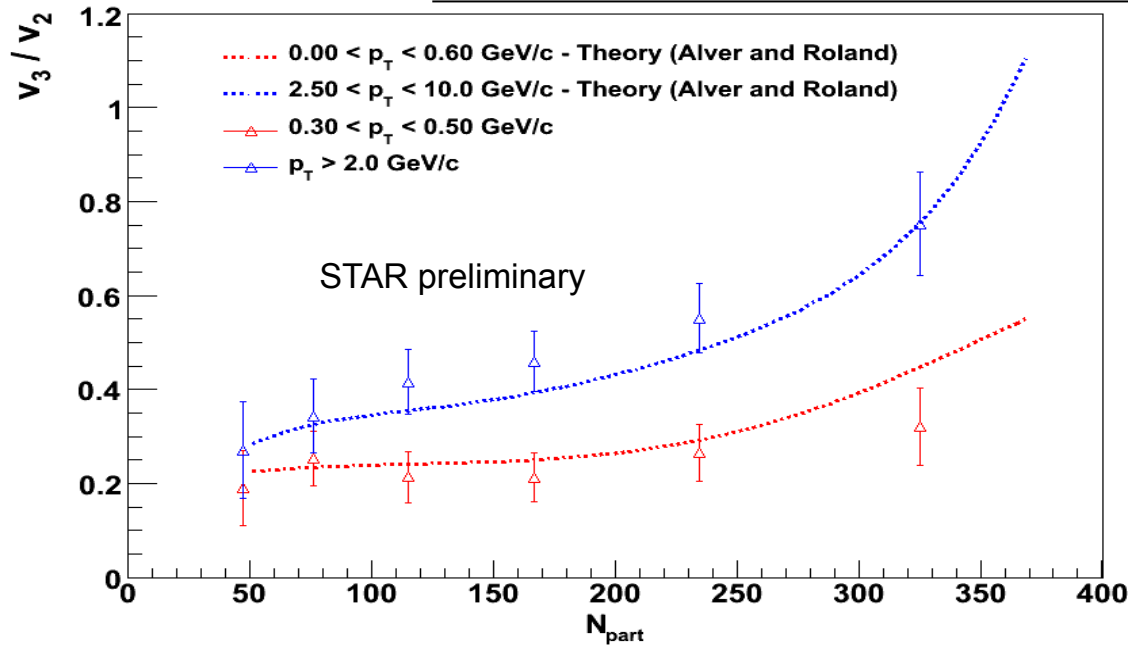
- NS harmonics and remainder amplitudes are compared
- Asymmetry of remainder is quantified
- NS harmonics strength reaches a minimum value at higher  $p_T$
- NS harmonics amplitude in the  $\langle p_T \rangle$  region from 1-2 GeV/c is comparable to remainder amplitude
- Above  $\langle p_T \rangle \sim 2.5$  GeV/c the remainder models possible unmodified jet correlation
  - The widths become symmetric above  $\sim 2.5$  GeV/c
  - Correlation function strength increases in jet region
- Below  $\langle p_T \rangle \sim 2.5$  GeV/c remainder could be due to possible modified jet phenomena
  - $\Delta\eta$  width peaks around 0.9 GeV/c.  $\Delta\eta/\Delta\phi$  widths ratio is  $\sim 2:1$  around 0.9 GeV/c
  - See next slide for comparison to widths in 200 GeV p+p collisions

# Asymmetric 2d Gaussian – p+p comparison

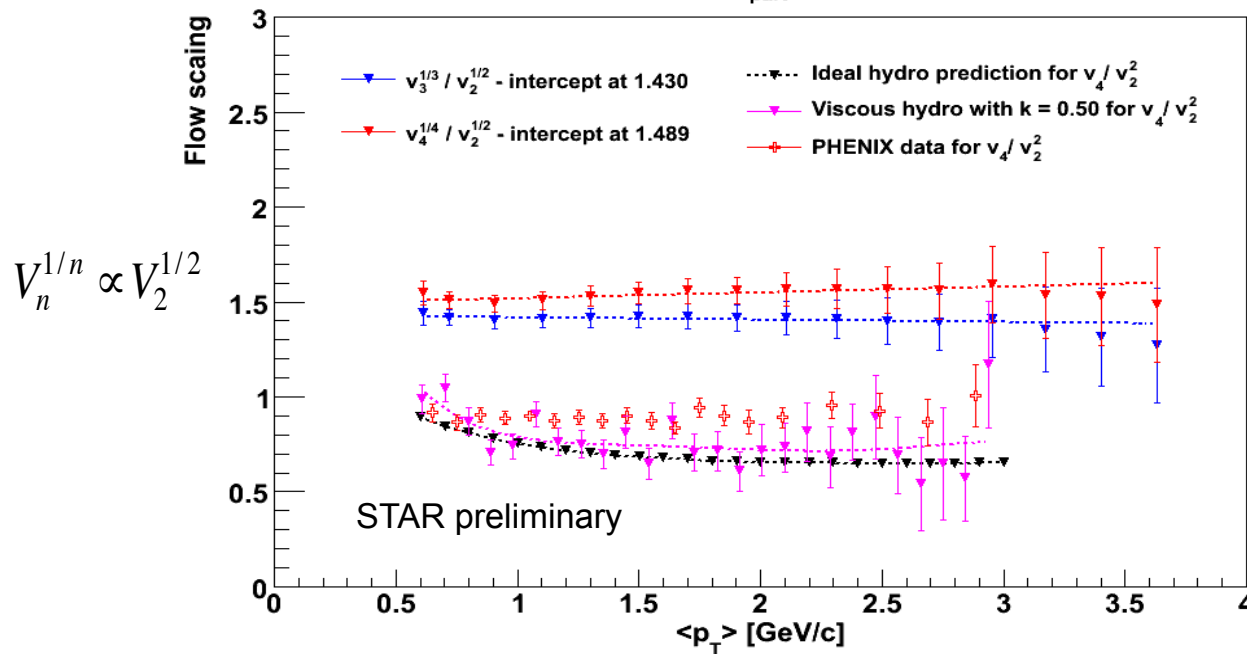


- At the highest momenta ( $\langle p_T \rangle > 2\text{GeV}/c$ ) the Au+Au widths are increased by about a factor of 2 relative to the p+p widths
- Asymmetry in p+p widths disappears at  $\langle p_T \rangle \sim 1.5\text{ GeV}/c$
- Maximum  $\Delta\eta$  width modification is larger (by a factor 2) than that of  $\Delta\phi$

# Flow comparisons



- Alver and Roland :  
*Phys. Rev. C 81, 054905 (2010)*



- Hydro scaling relation plot at 0 – 10% :  
*Phys. Rev. C 81, 014901(2010)*

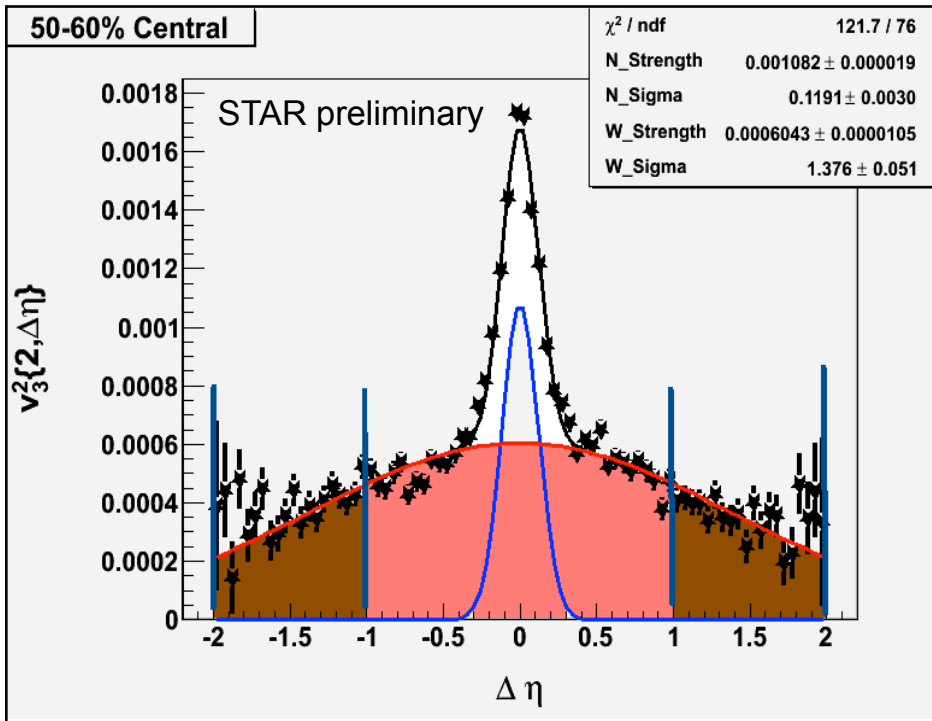
All scaled flow ratios are flat as a function of  $p_T$  at higher  $p_T$  as predicted by hydrodynamics



# Other ridge studies from STAR

# $\Delta\eta$ dependence of triangular flow ( $v_3$ )

❖ Focus on mid central,  $0.15 < p_T < 2$  GeV/c, 2 – particle cumulant



Main Idea:

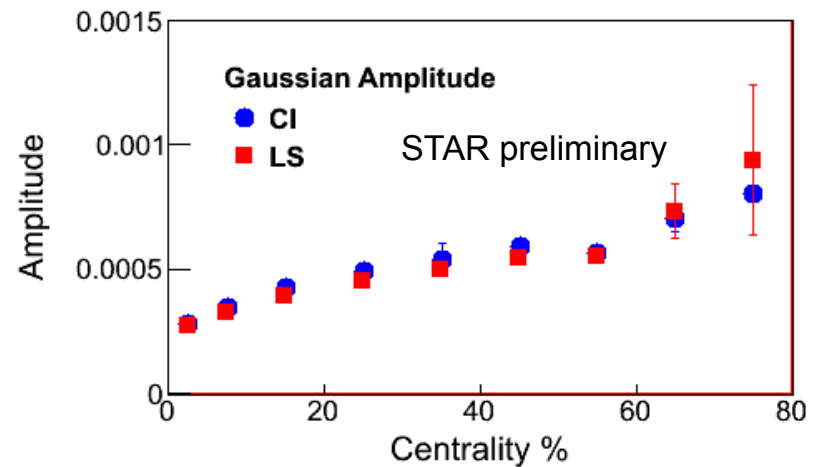
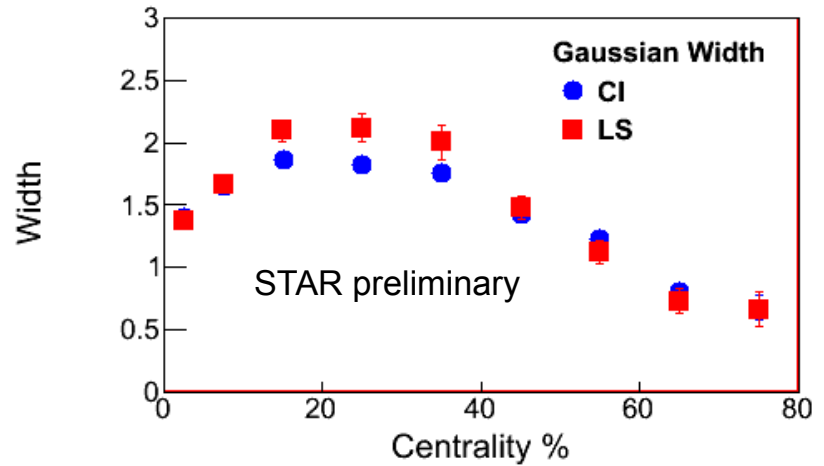
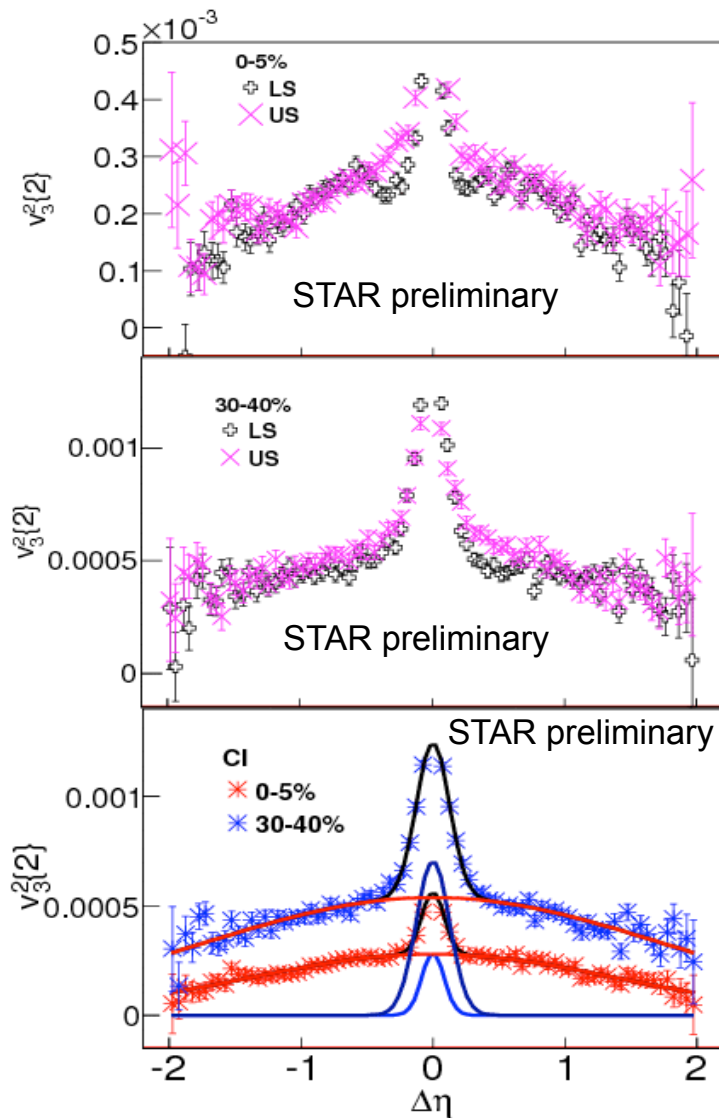
$v_3^2\{2, \Delta\eta\}$  as a function of  $\Delta\eta$   
data can be fitted with sum of two  
Gaussians:

1. A narrow Gaussian: Short range non flow (HBT/ $e^+e^-$ )
2. A wide Gaussian: Flow + Flow fluctuations + Long range non flow

Triangular flow harmonic shows  $\Delta\eta$  dependence

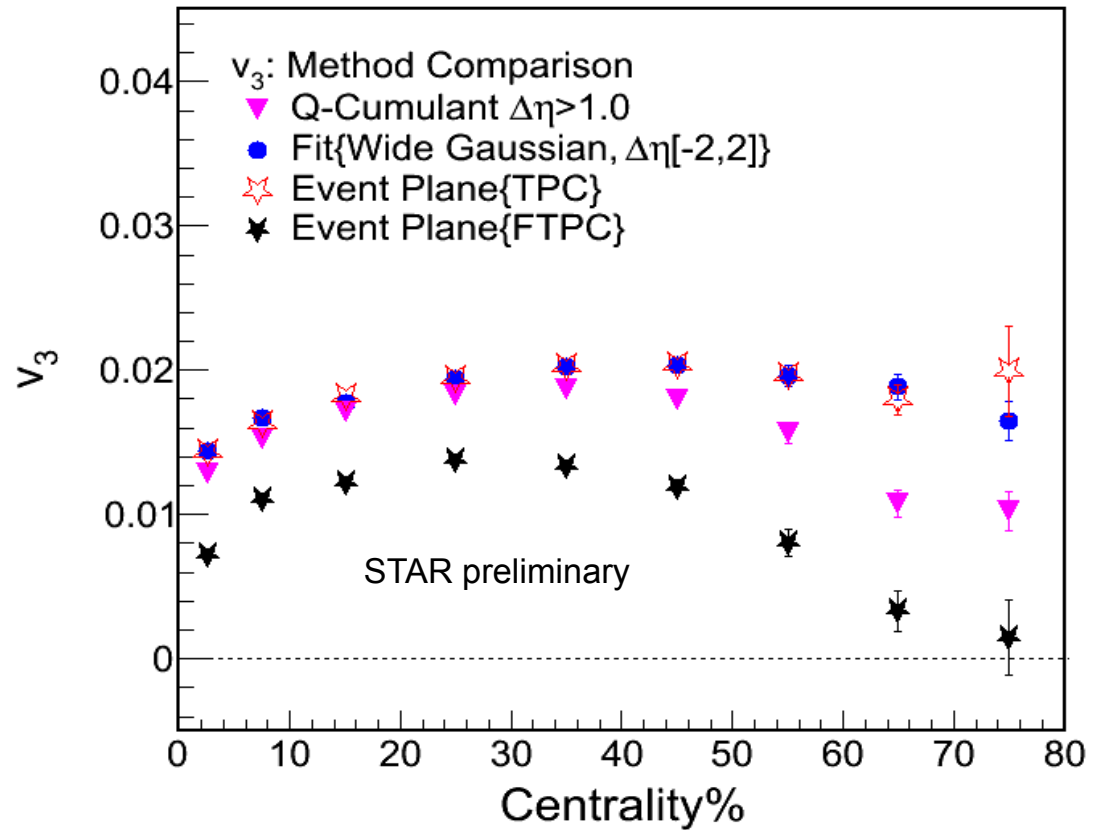
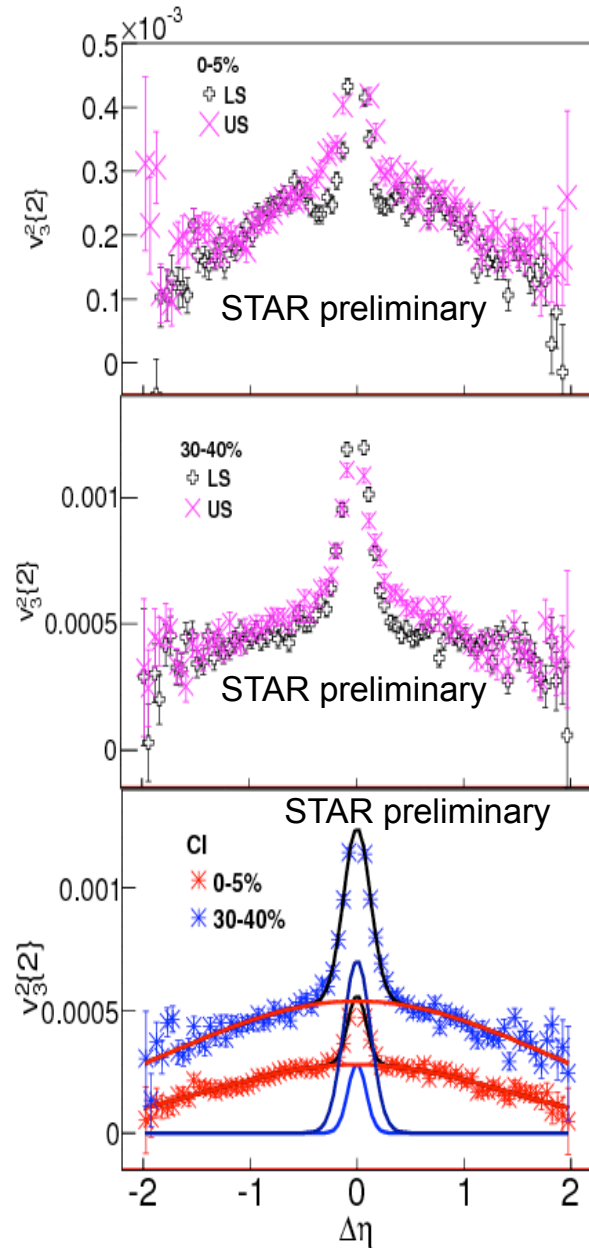
# Triangular flow ( $v_3$ ): Flow, flow fluctuations and non-flow

Charge dependence studies estimate possible non-flow contribution



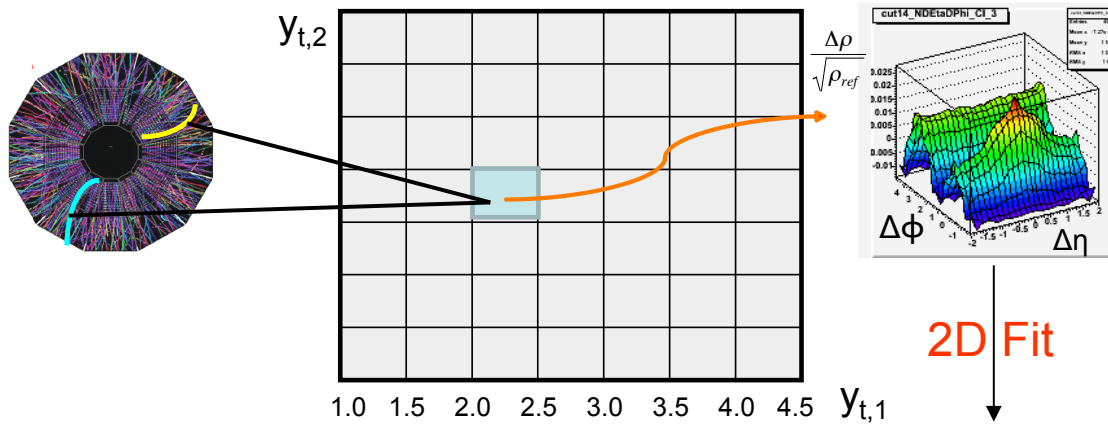
Width and amplitude of the wide Gaussian

# Triangular flow ( $v_3$ ): Flow, Fluctuations and Non Flow



Gaussian fit parameters are used to calculate  $v_3^2$  and compared to various other methods

# Additional study of 2d correlations



Intend to form a measure which is  $\propto \log(p_t)$

$$y_t = \ln\left(\frac{m_t + p_t}{m_\pi}\right), \quad \text{where } m_t = \sqrt{p_t^2 + m_\pi^2}$$

2D Fit

$$f = f_1 + f_2 + f_3 + f_4 + f_5 + f_6$$

$$f_1 \propto c_0$$

$$f_2 \propto c_1 \cdot \cos(\Delta\phi)$$

$$f_3 \propto c_2 \cdot \cos(2\Delta\phi)$$

$$f_4 \propto c_3 \cdot \exp(-0.5 \cdot ((\Delta\eta/c_4)^2 + (\Delta\phi/c_5)^2))$$

$$f_5 \propto c_6 \cdot \exp(-1.0 \cdot V \cdot ((\Delta\eta/c_7)^2 + (\Delta\phi/c_8)^2))$$

$$f_6 \propto c_9 \cdot \exp(-0.5 \cdot (\Delta\eta/c_{10})^2)$$

Offset

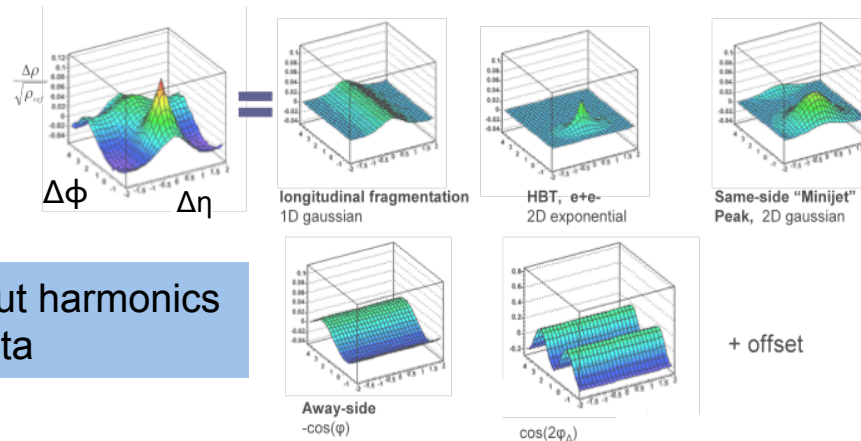
Away-side momentum conservation

2<sup>nd</sup> order Fourier term

Modified jet fragmentation

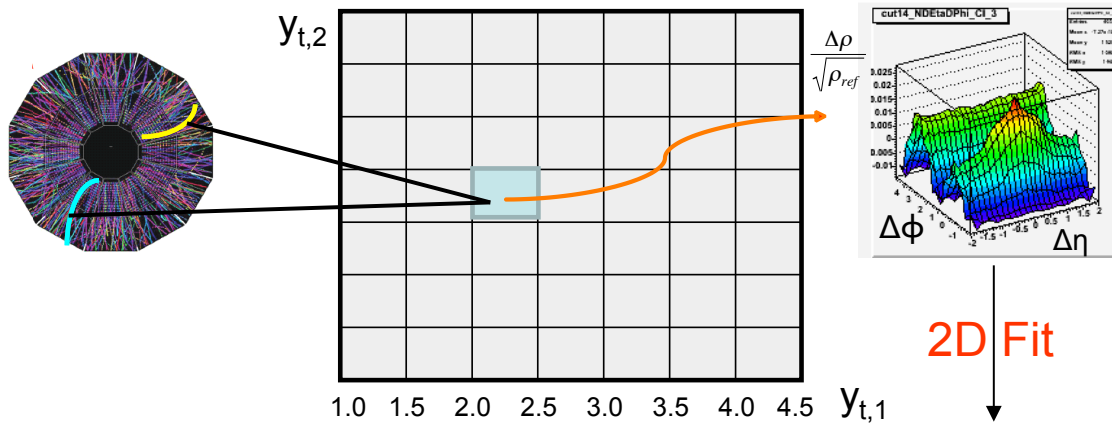
HBT/e<sup>+</sup>e<sup>-</sup>

Longitudinal fragmentation



Alternate fit model without harmonics  
can also describe the data

# Additional study of 2d correlations



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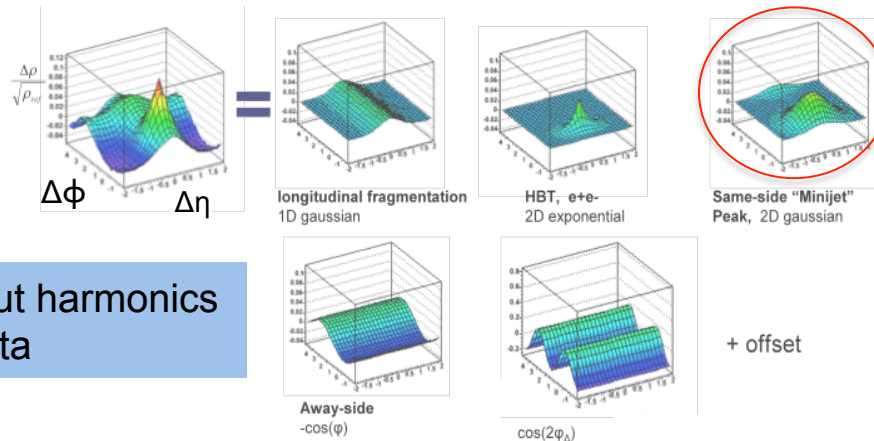
Away-side momentum conservation

2<sup>nd</sup> order Fourier term

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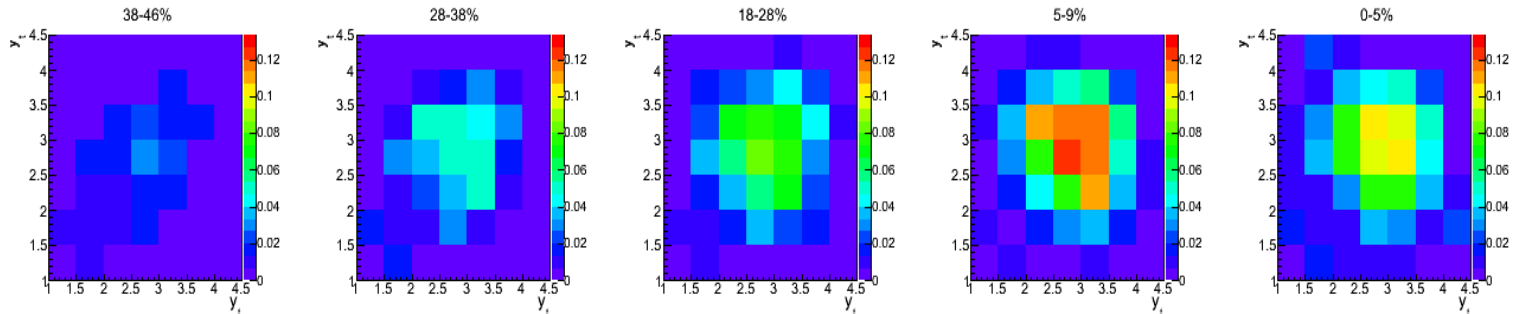
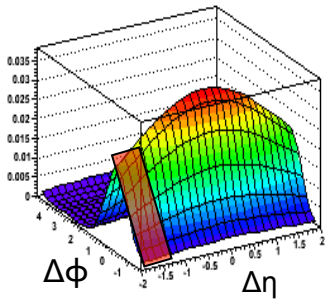
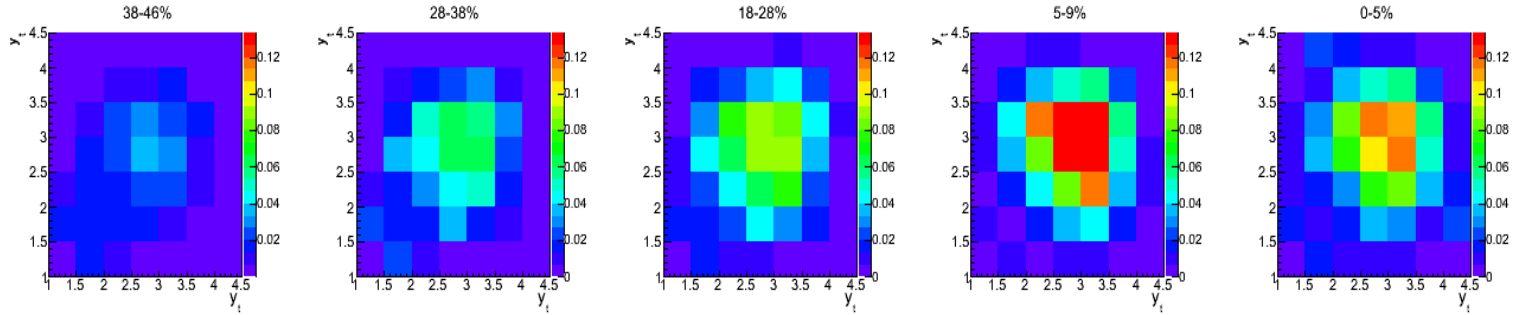
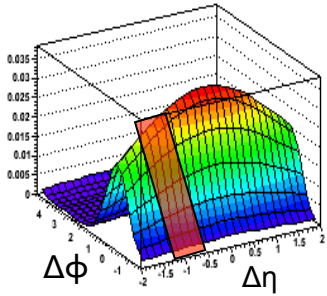
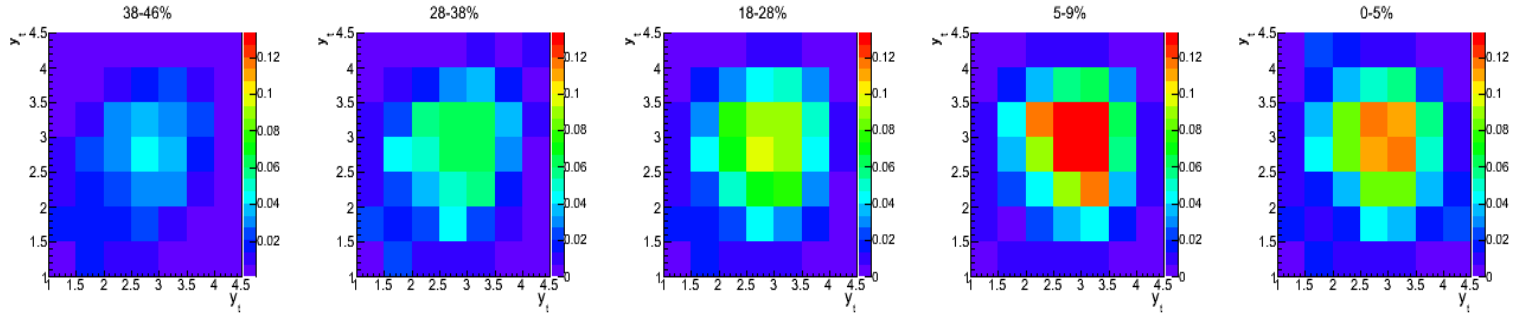
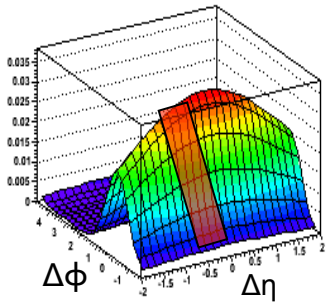
Longitudinal fragmentation



Alternate fit model without harmonics  
can also describe the data

# NS 2d Gaussian Volume by $\Delta\eta$ Region

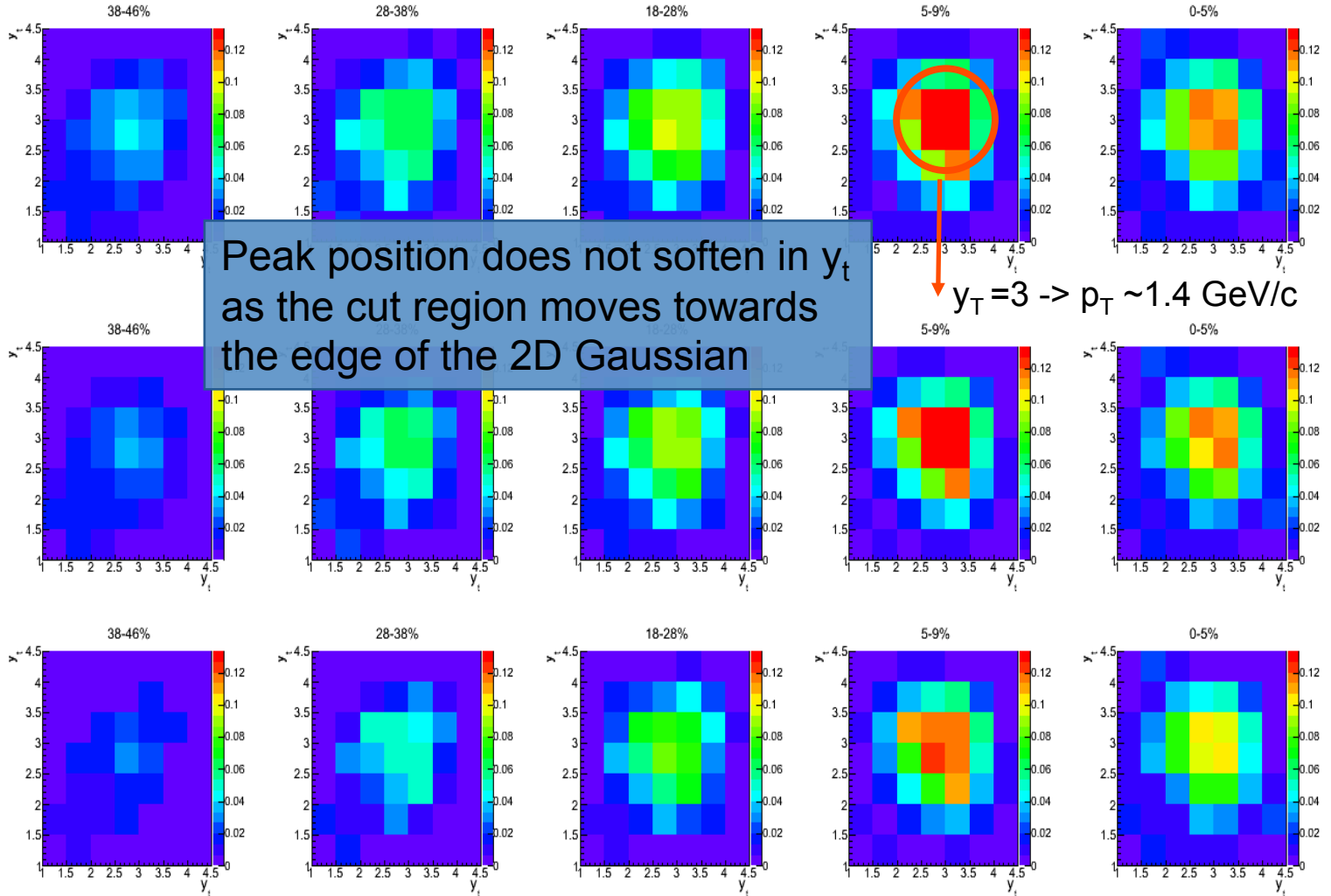
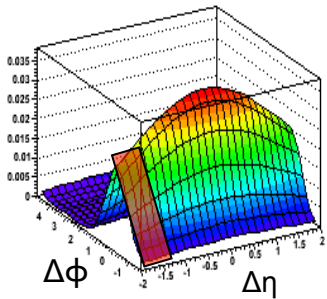
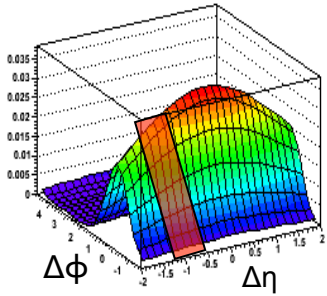
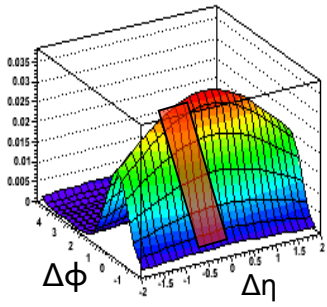
NS 2d Gaussian  $\langle p_T \rangle \sim 1.4 \text{ GeV}/c$



\*STAR Preliminary

# NS 2d Gaussian Volume by $\Delta\eta$ Region

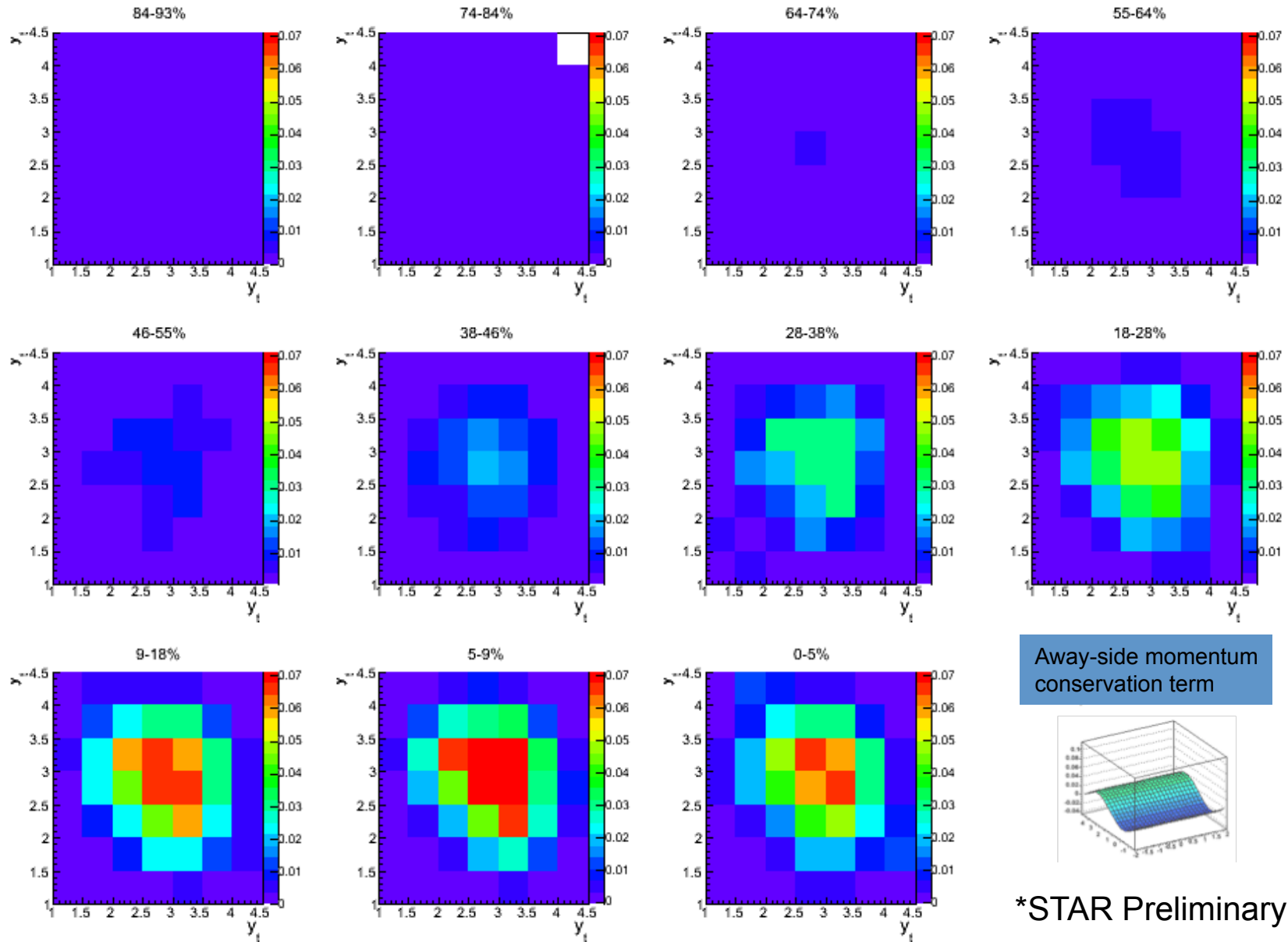
NS 2d Gaussian  $\langle p_T \rangle \sim 1.4 \text{ GeV}/c$



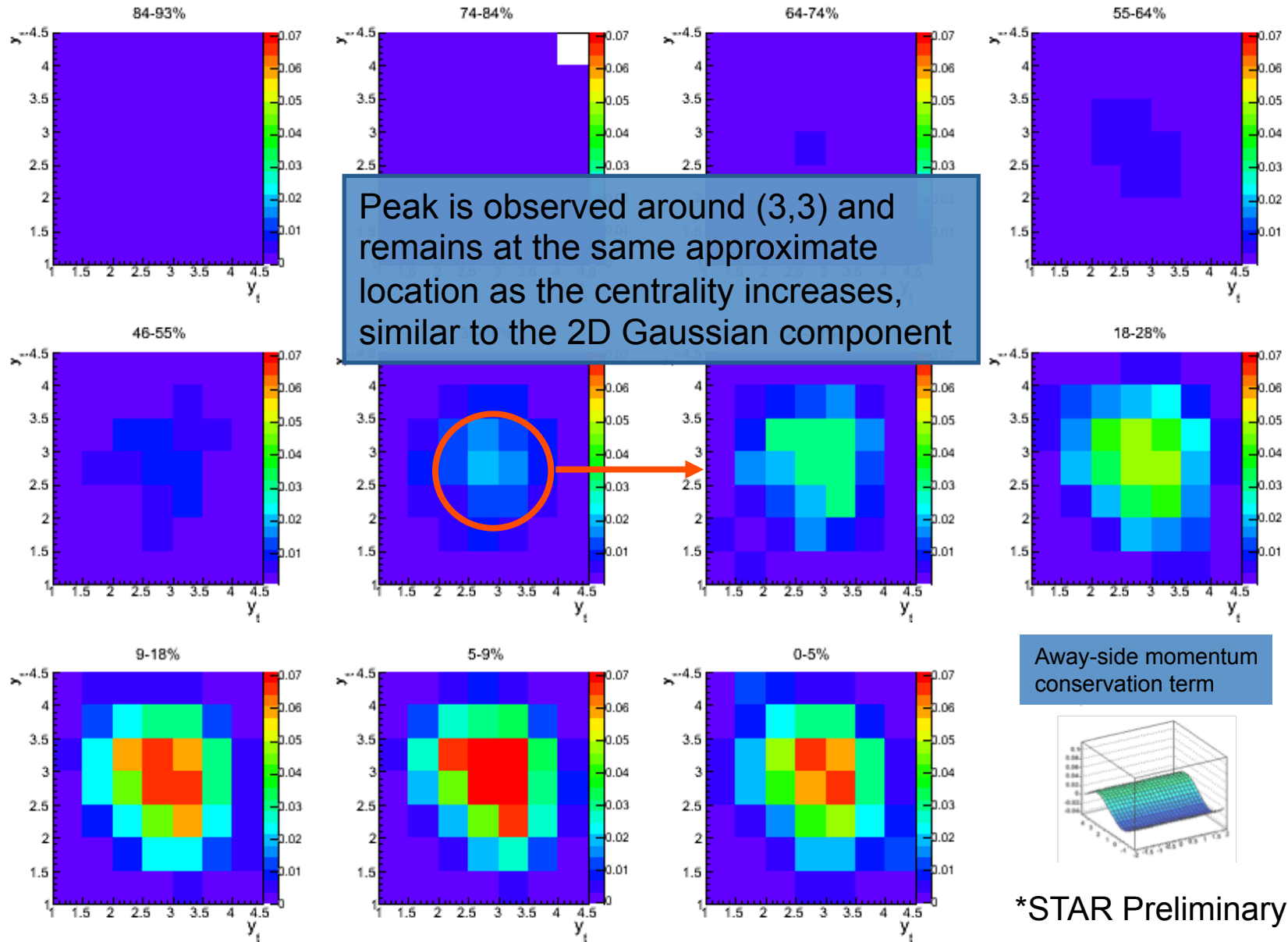
\*STAR Preliminary



# Away-side momentum Distribution



# Away-side momentum Distribution



# Summary and discussion

- Near side  $\Delta\eta$ - $\Delta\phi$  correlations show a smooth evolution as a function of  $\langle p_T \rangle$ . One interpretation of the "Ridge structure" is a sum of "initial state density fluctuations" in addition to a "modified jet-like structure"
- Possible initial state density fluctuation contributions are extracted using higher harmonics model components which agree reasonably well with predicted hydro scaling relations
- Higher harmonics correlation strength ( $\text{yield} \cdot v_n$ ) reduces at higher  $\langle p_T \rangle$
- The remaining structure after higher harmonics subtraction is quantified using p+p data at the same collision energy
- Within the assumptions of the model presented, a "modified jet" structure is observed as a function of  $\langle p_T \rangle$
  
- Additional studies reveal possible  $\Delta\eta$  dependency in triangular flow
- An alternate model without higher harmonics and representing possible modified jet formation can describe the data and indicates a  $\langle p_T \rangle$  at large  $\Delta\eta$  that is higher than the  $\langle p_T \rangle$  of the inclusive spectra