



**Warsaw University  
of Technology**



# Geometry and Dynamics in Heavy-ion Collisions Seen by the Femtoscopy Method in the STAR experiment

## Introduction

- HIC and HBT method
- Correlation femtoscopy
- RHIC / STAR / BES;

## Results

- Geometry
- Dynamics
- Interactions

## Summary

Hanna Zbroszczyk for the STAR Collaboration

e-mail: [hanna.zbroszczyk@pw.edu.pl](mailto:hanna.zbroszczyk@pw.edu.pl)

Supported in part by



U.S. DEPARTMENT OF

**ENERGY**

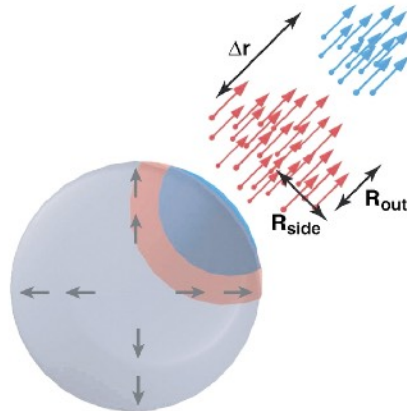
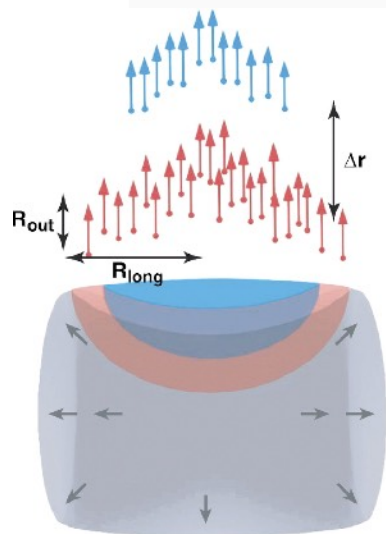
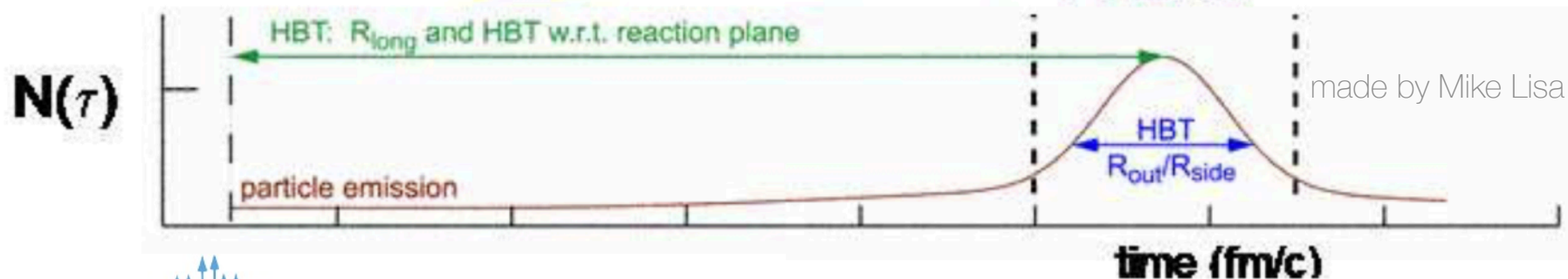
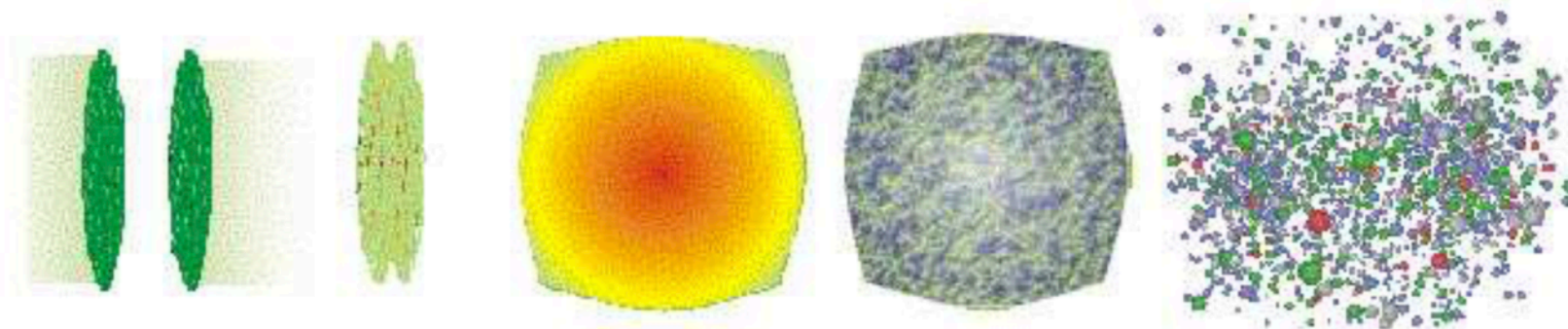


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# Introduction

# Heavy-Ion collision and **HBT** method



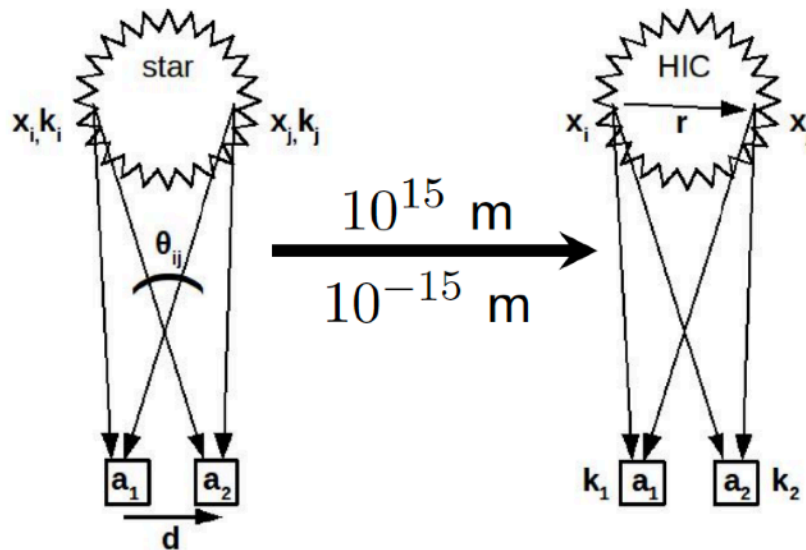
*long* - beam axis  
*out* - pair transverse  $\mathbf{p}$   
*side* - perpendicular to out and long

# Correlation **femtosc**copy



Size:  $\sim 10^{-15}$  m (**fm**)  
Time:  $\sim 10^{-23}$  s

**Impossible  
to measure directly!**



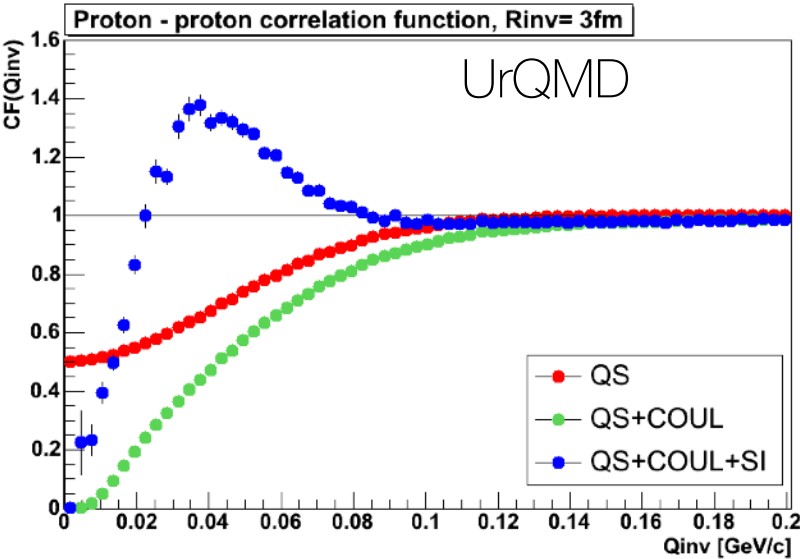
Femtosc (HIC) inspired by Hanbury Brown and Twiss interferometry method (Astronomy)

**but!**

- different scales,
- different measured quantities
- different determined quantities

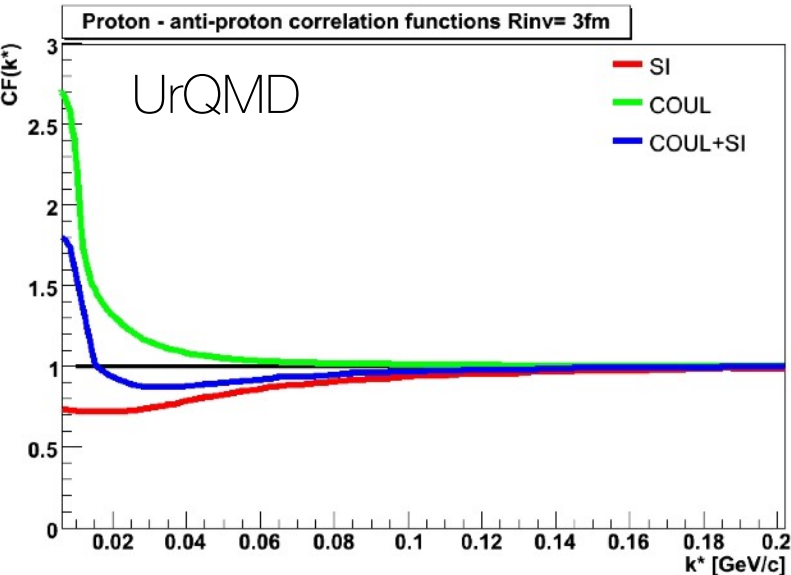
Hanbury Brown, R.; Twiss,  
Nature 178, 1046–1048 (1956)

# Two-particle correlations



Identical pairs:

- Quantum Statistics- **QS**
- Final State Interactions- **FSI**: Coulomb, Strong



Non-identical pairs:

- Final State Interactions- **FSI**: Coulomb, Strong

$x_1, x_2$  - space-time sizes (and dynamics)

(**can not** be measured directly)  $\rightarrow$

**Close velocity correlations**  
(**HBT + FSI**)

$p_1, p_2$  - momenta and momentum difference

(**can** be measured directly)

Single- and two-particle distributions:

$$P_1(p) = E \frac{dN}{d^3p} = \int d^4x S(x, p)$$

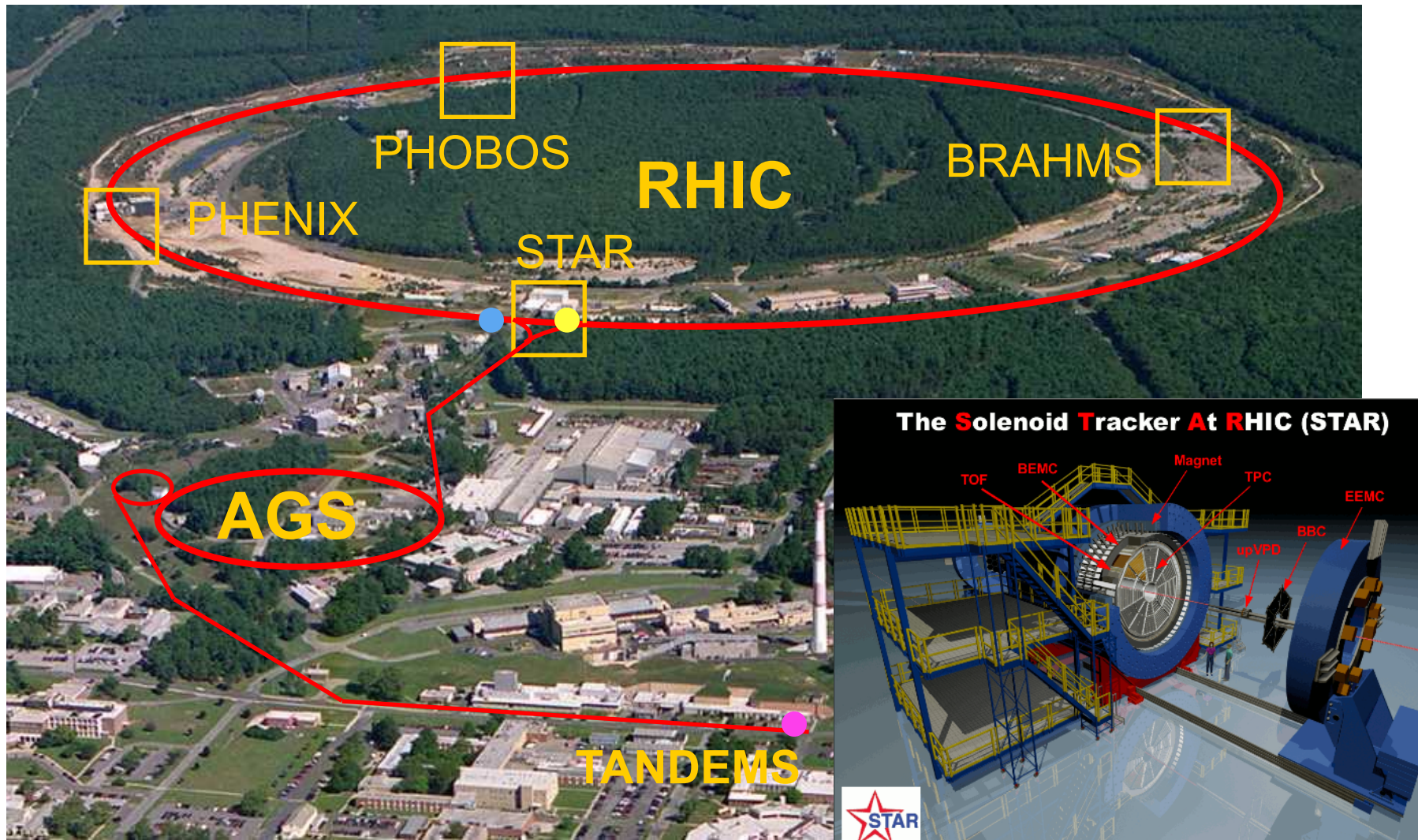
$$P_2(p_1, p_2) = E_1 E_2 \frac{dN}{d^3p_1 d^3p_2}$$

$$P_2(p_1, p_2) = \int d^4x_1 S(x_1, p_1) d^4x_2 S(x_2, p_2) \Phi(x_2, p_2 | x_1, p_1)$$

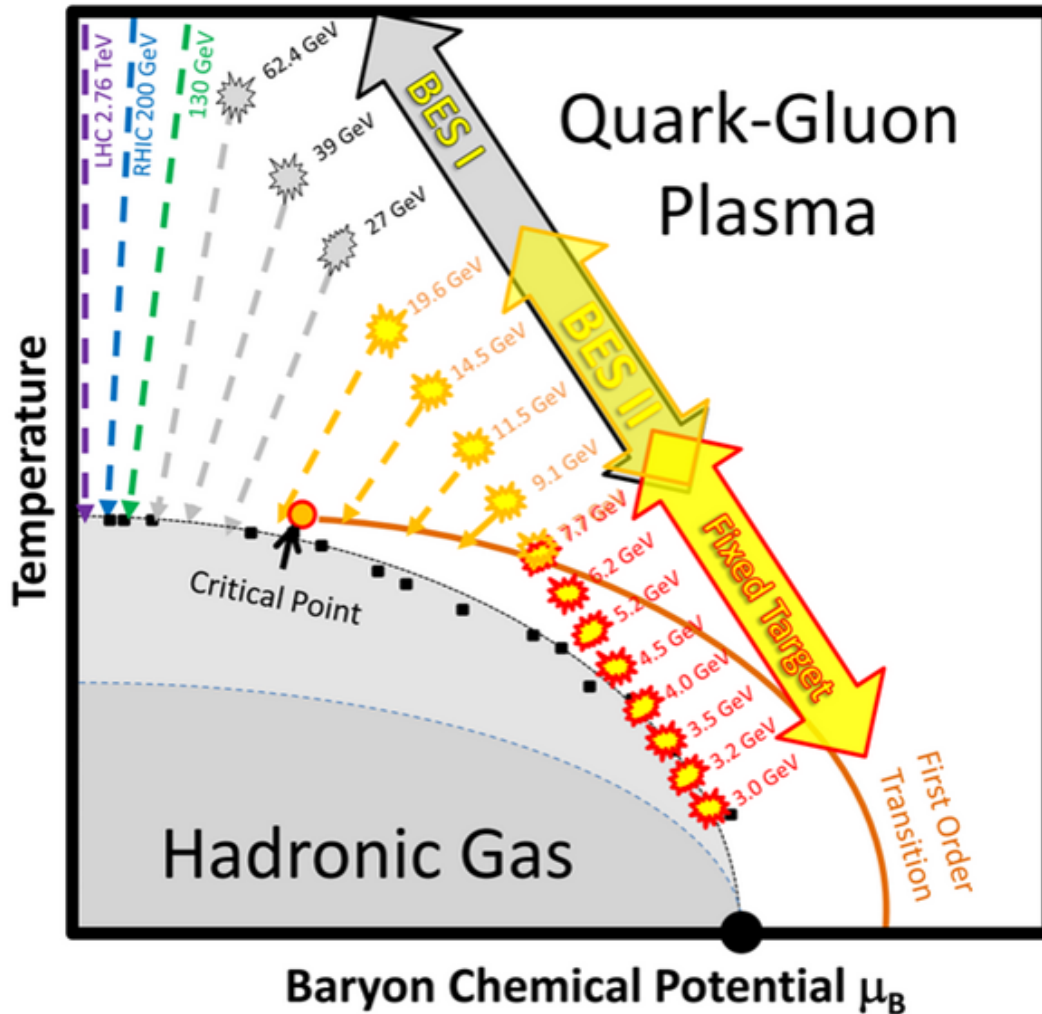
The correlation function:

$$C(p_1, p_2) = \frac{P_2(p_1, p_2)}{P_1(p_1)P_1(p_2)}$$

# Relativistic Heavy Ion Collider (**RHIC**) Brookhaven National Laboratory (**BNL**), Upton



# Beam Energy Scan Program



## RHIC Top Energy

p+p, p+Al, p+Au, d+Au,  
 $^3\text{He}+\text{Au}$ , Cu+Cu, Cu+Au,  
Ru+Ru, Zr+Zr, Au+Au, U+U  
QCD at high energy  
density/temperature  
Properties of QGP, EoS

## Beam Energy Scan

Au+Au at  $\sqrt{s_{NN}} = 7.7-62$  GeV

- QCD phase transition
- Search for critical point
- Turn-off of QGP signatures
- Chiral symmetry restoration

## Fixed-Target Program

Au+Au at  $\sqrt{s_{NN}} = 3.0-7.7$  GeV

High baryon density regime

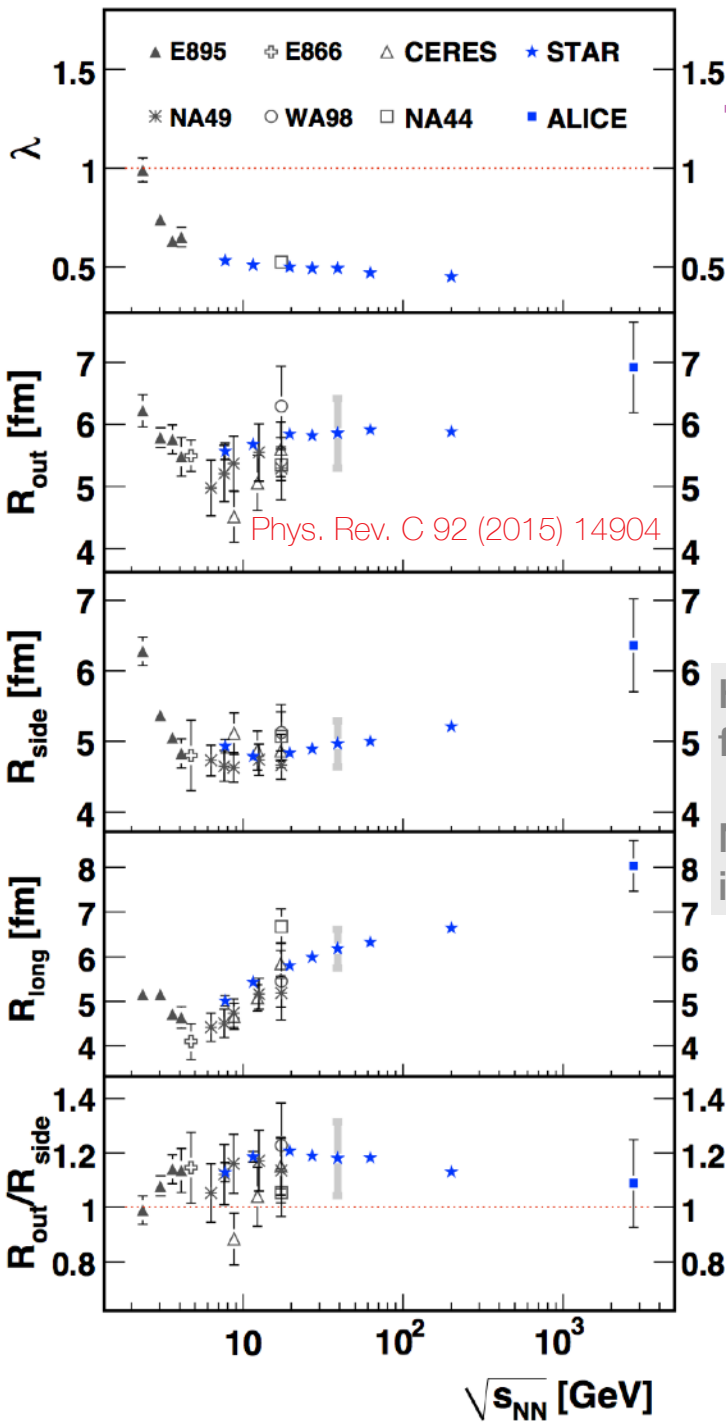
with  $\mu_B = 420-720$  MeV



# Results



# Source **geometry** seen by pions

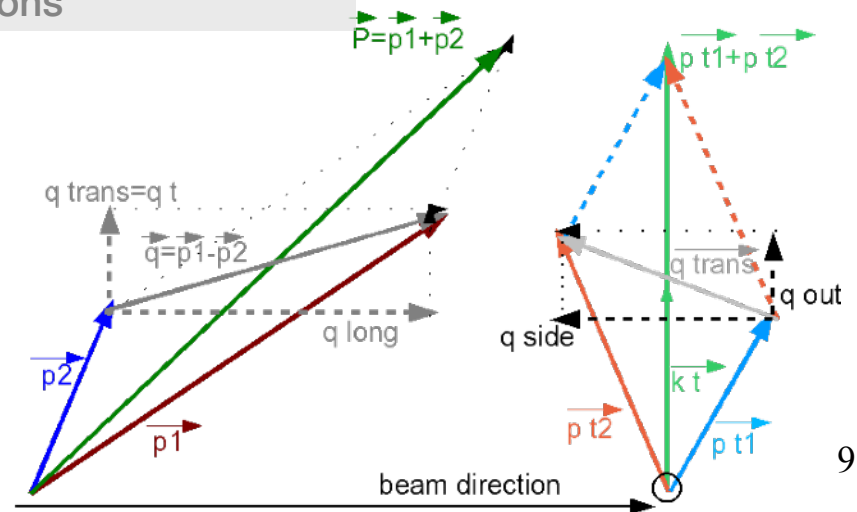


- $R_{side}$  spatial source evolution in the transverse direction
- $R_{out}$  related to spatial and time components
- $R_{out}/R_{side}$  signature of phase transition
- $R_{out}^2 - R_{side}^2 = \Delta\tau^2 \beta_t^2$ ;  $\Delta\tau$  – emission time
- $R_{long}$  temperature of kinetic freeze-out and source lifetime

$$C(\vec{q}) = (1 - \lambda) + K_{Coul}(q_{inv})\lambda \times \exp(-q_o^2 R_o^2 - q_s^2 R_s^2 - q_l^2 R_l^2 - 2q_o q_s R_{os} - 2q_o q_l R_{ol})$$

HBT source sizes determined for wide range of collision energy;

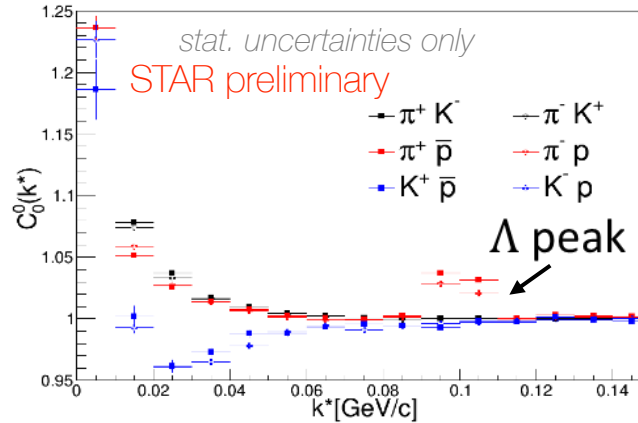
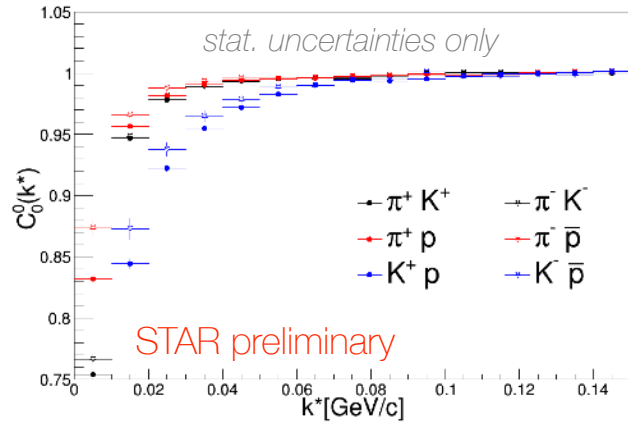
Non-monotonic behavior seen in three directions



# Source **dynamics**: system dependence

Like-sign 0-10% @ Au+Au 39 GeV

Unlike-sign 0-10% @ Au+Au 39 GeV



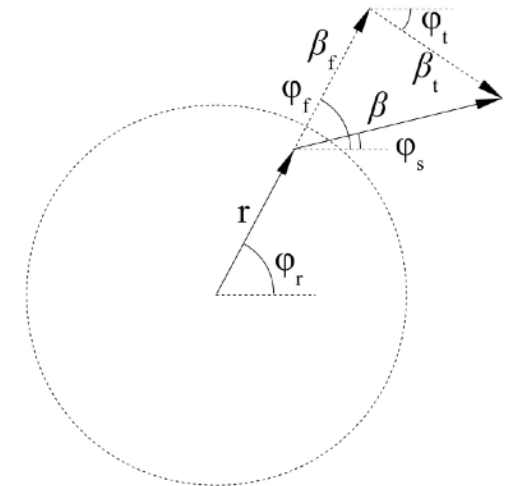
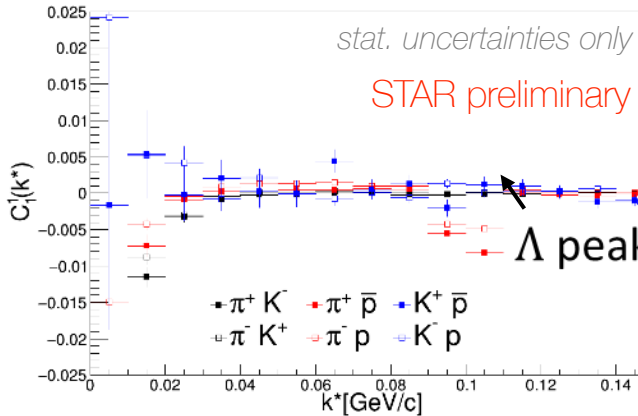
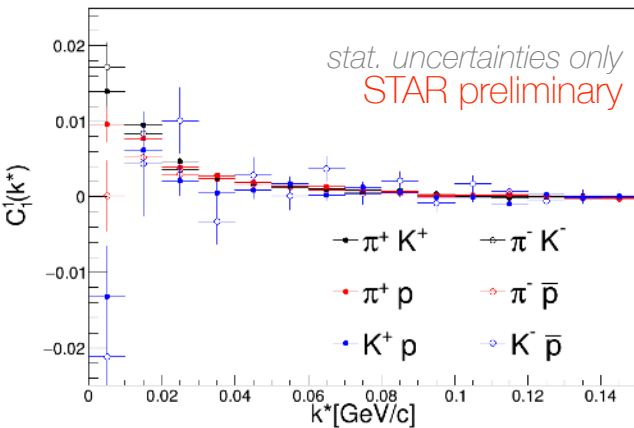
Heavier particles directed towards edge of the source.

Heavier particles freeze-out earlier

Phys. Rev. C81:064906 2010

Determined by **Coulomb** Interactions

Determined by full **FSI: Coulomb** and **Strong** interactions (kaon-proton)



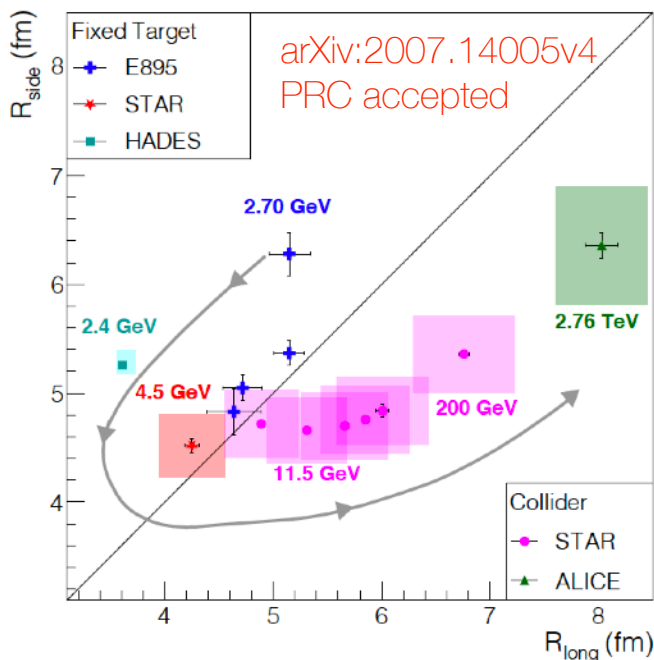
$$\langle x_{out} \rangle = \frac{\langle r \beta_f \rangle}{\langle \sqrt{\beta_t^2 + \beta_f^2} \rangle} = \frac{r_0 \beta_0 \beta}{\beta_0^2 + T/m_t}$$

Nucl. Phys. A 982 (2019), 359-362

$\beta_f$  - the same for both particles

$\beta_t \sim 1/m_T$  - smaller for heavier particles

# How to measure a phase transition?



Clear evolution in the freeze-out shape indicated

Lower energies: system more oblate

$$(R_{side} > R_{long})$$

Higher energies: system more prolate

$$(R_{side} < R_{long})$$

$$\sqrt{s_{NN}} = 4.5 \text{ GeV: round system } (R_{side} \simeq R_{long})$$

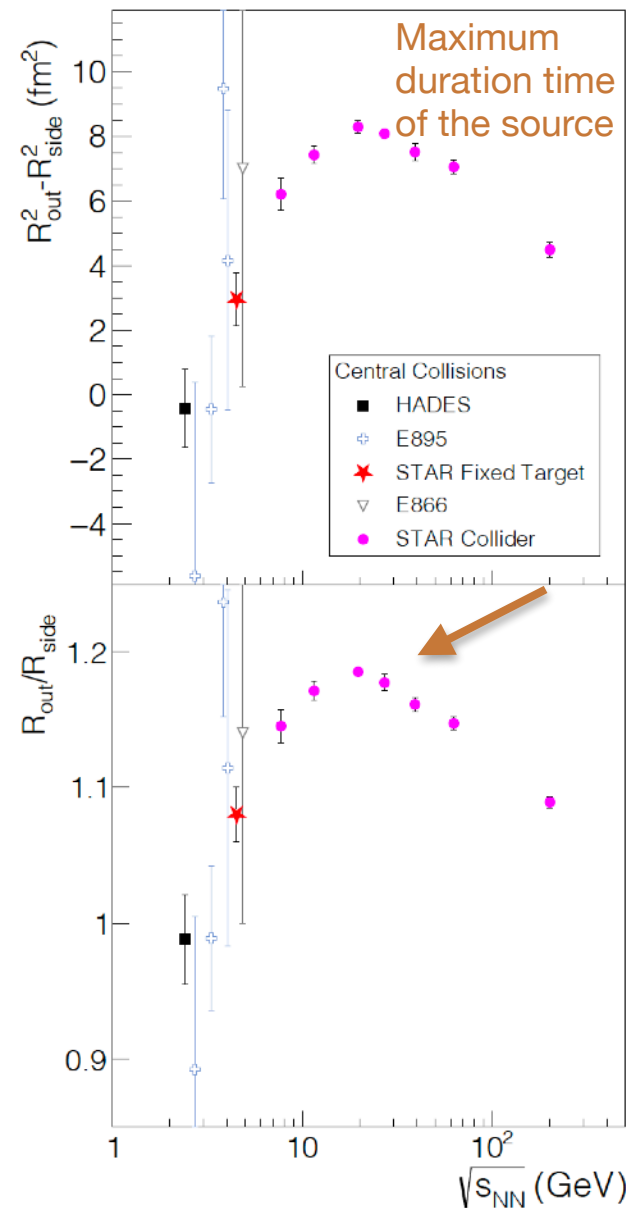
Transition region between dynamics dominated by stopping and boost-invariant dynamics.

$$R_{out}^2 - R_{side}^2 = \beta_t^2 \Delta\tau^2$$

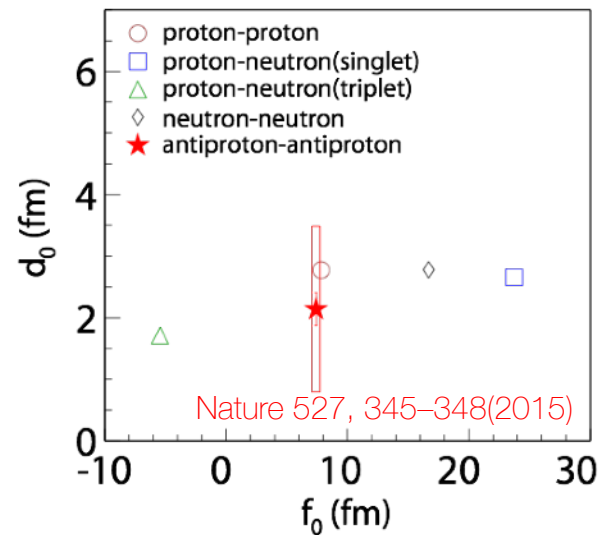
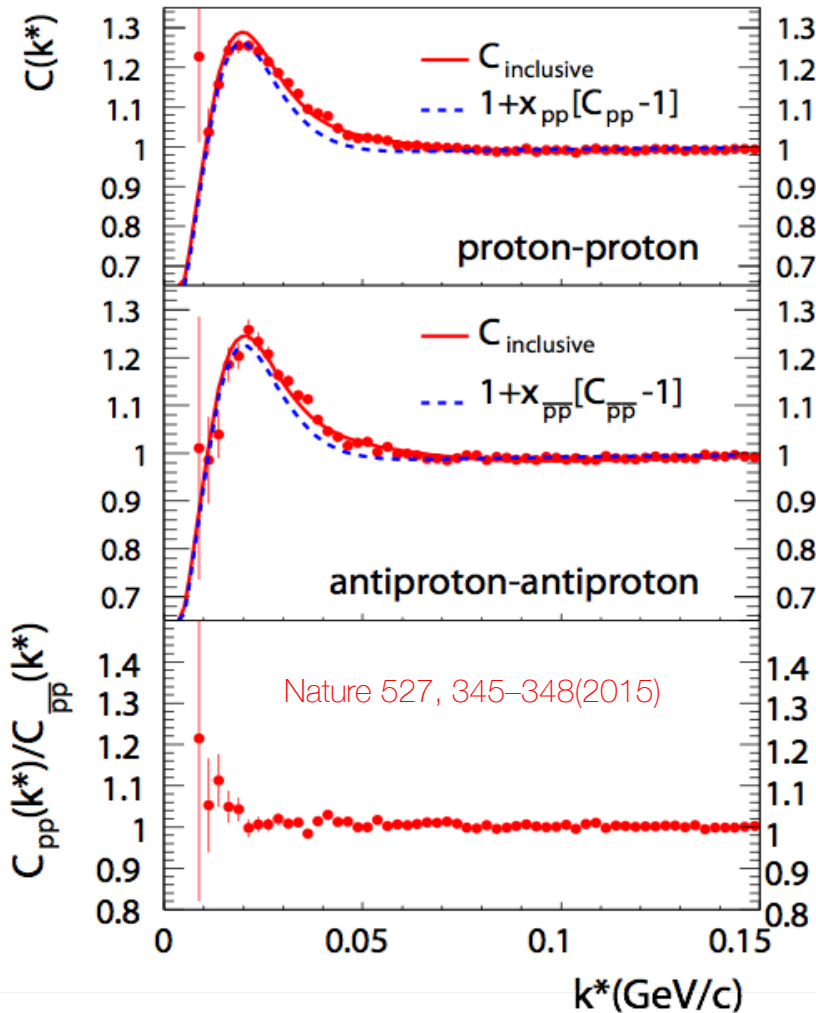
Visible peak in  $\frac{R_{out}}{R_{side}}(\sqrt{s_{NN}})$  near the  $\sqrt{s_{NN}} \simeq 20 \text{ GeV}$

QCD calculations predict a peak near to the QGP transition threshold - signature of first-order phase transition?

Theoretical attention from hydro and transport models needed



# Strong interactions between anti-nucleons



$f_0$  and  $d_0$  - parameters of strong interaction

Scattering length  $f_0$

Effective range  $d_0$

Elastic cross section  $\sigma_e$

$$\lim_{k \rightarrow 0} \sigma_e = 4\pi f_0^2$$

- $f_0$  and  $d_0$  for the antiproton-antiproton interaction consistent with parameters for the proton-proton interaction.
- Descriptions of the interaction among antimatter (based on the simplest systems of anti-nucleons) determined.
- A quantitative verification of matter-antimatter symmetry in context of the forces responsible for the binding of (anti)nuclei.

**p-p** CF,

$R=2.75 \pm 0.01 \text{ fm}$ ;  $\chi^2/\text{NDF} = 1.66$ ;

**antiproton-antiproton** CF,

$R=2.80 \pm 0.02 \text{ fm}$ ,  $f_0=7.41 \pm 0.19 \text{ fm}$ ,

$d_0=2.14 \pm 0.27 \text{ fm}$ ;  $\chi^2/\text{NDF}=1.61$

# Strange Baryon Correlations (including p-Ω)

Binding energy **E<sub>bin</sub>** [MeV]

Scattering length **a<sub>0</sub>** [fm]

Effective range **r<sub>eff</sub>** [fm]

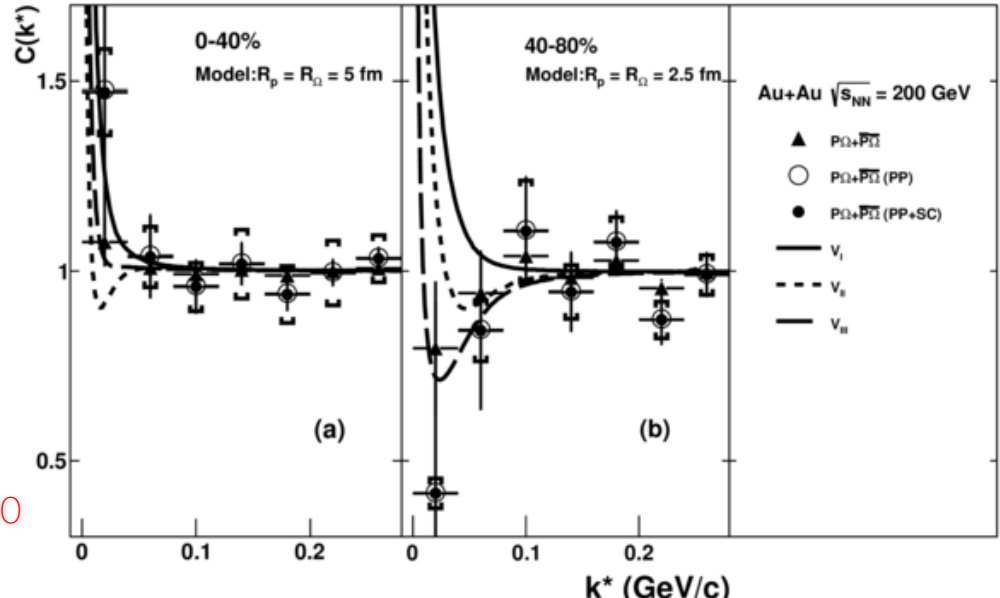
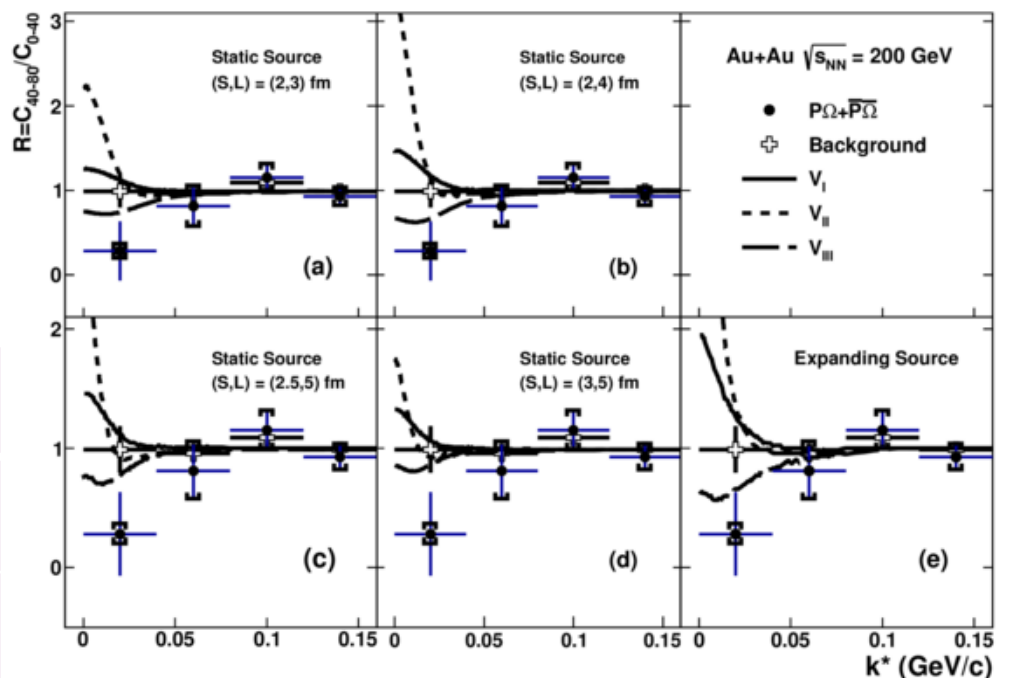
for 3 scenarios:

K. Morita et al. Phys. Rev. C 94, 031901 (2016)

	V <sub>1</sub>	V <sub>2</sub>	V <sub>3</sub>
<b>E<sub>bin</sub></b> <b>[MeV]</b>	-	6.3	26.9
<b>a<sub>0</sub></b> <b>[MeV]</b>	-1.12	5.79	1.29
<b>r<sub>eff</sub></b> <b>[MeV]</b>	-1.16	0.96	0.65

A comparison of the measured correlation functions from Au+Au collisions with theoretical predictions

**Scattering length is positive and favor pΩ bound state hypothesis**





# Summary

Correlation **femtoscscopy** probes the system:

- **geometry:**

- Pure geometrical information: source parametrized in 3D space (out-side-long);
- Source's lifetime, particle emission duration, temperature of kinetic freeze-out, etc..;

- **dynamics:**

- emission sequence (particle of which type is emitted earlier or later);
- collectivity seen through homogeneity region,

- **Interactions:**

- First attempt to determine strong forces responsible for binding anti-nuclei;
- A quantitative verification of matter-antimatter symmetry (forces responsible for the binding of anti-nuclei);
- Strong interaction between strange ( $\Lambda$ ,  $\Omega$ ) particles is investigated;

Thank you for Your attention

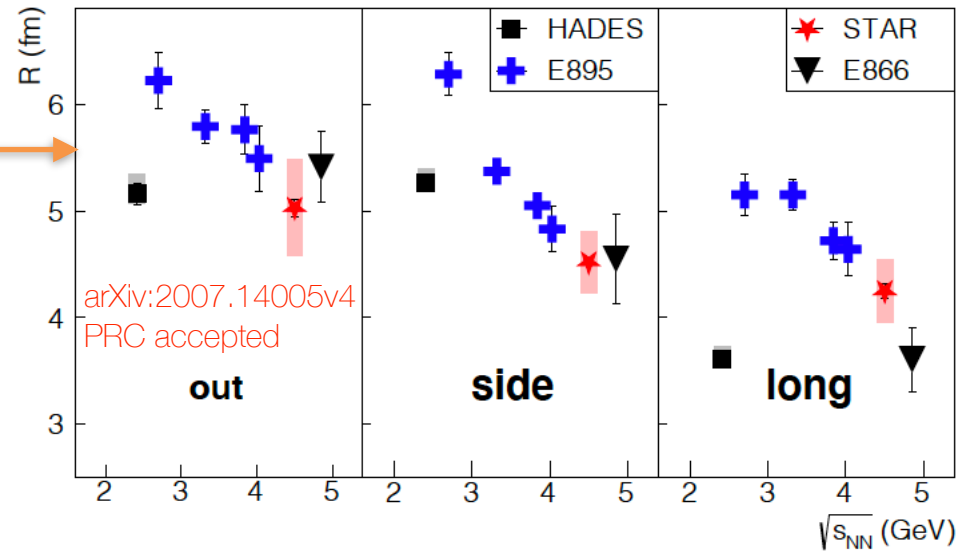
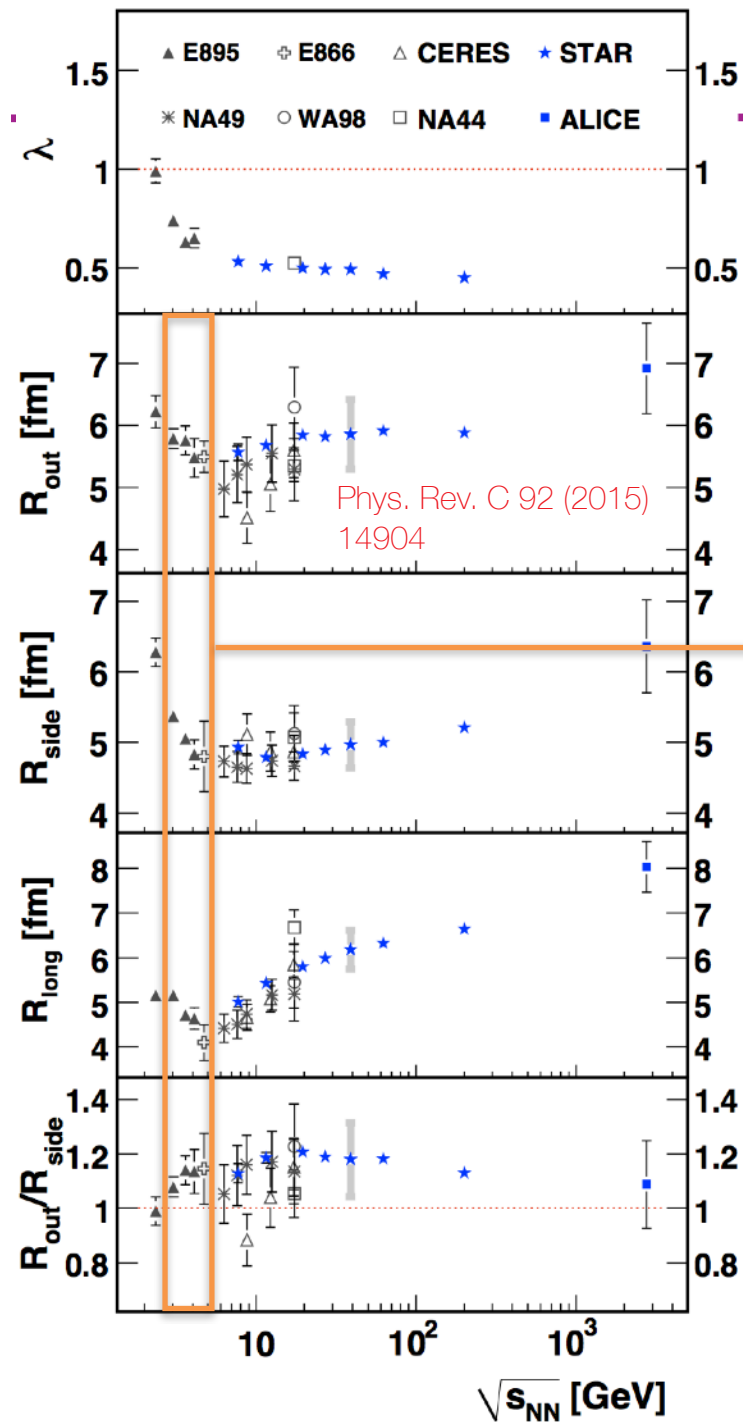


Backup slides



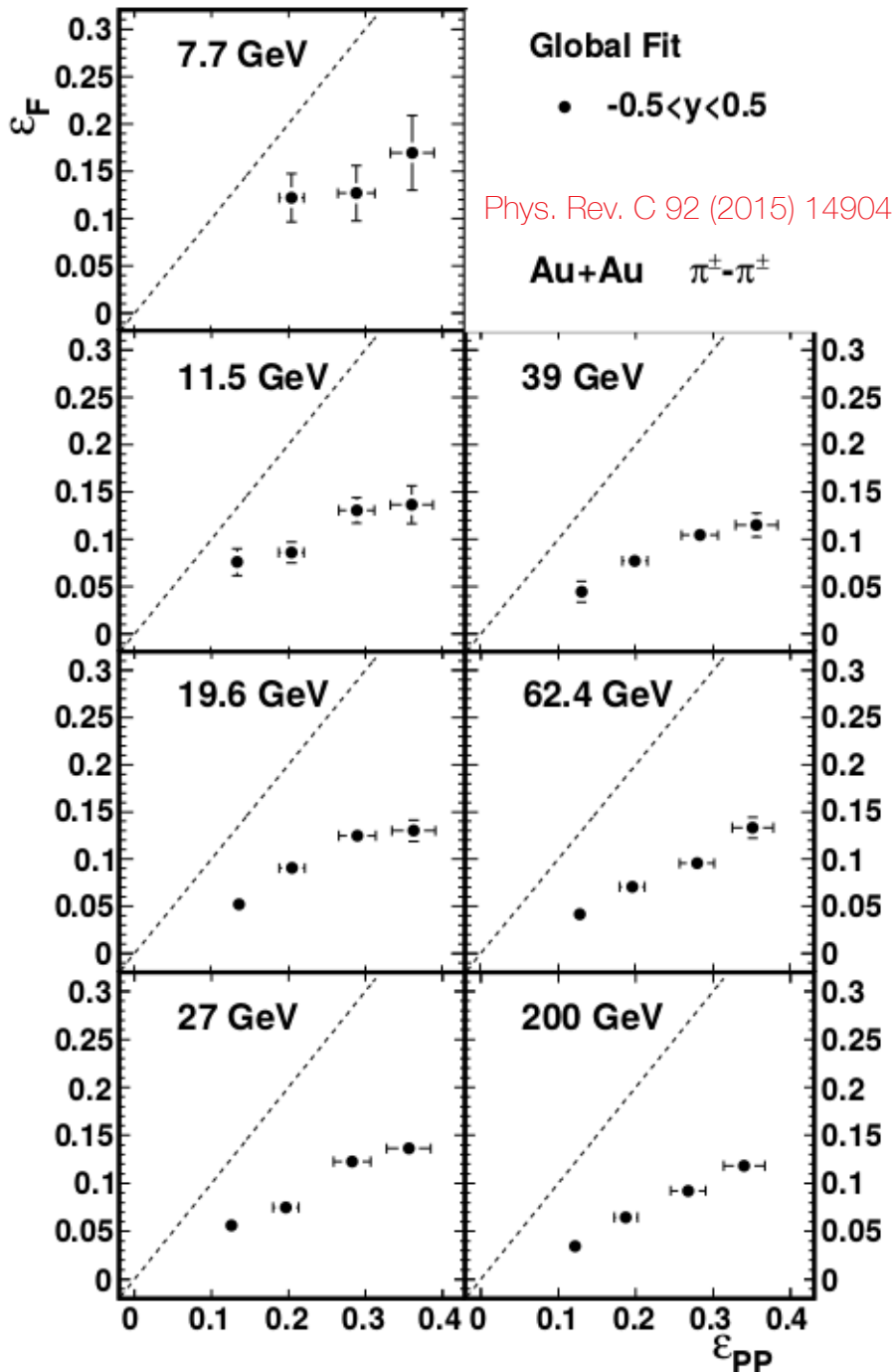
# Identical pion femtoscopy

- $R_{\text{side}}$  spatial source evolution in the transverse direction
- $R_{\text{out}}$  related to spatial and time components
- $R_{\text{out}}/R_{\text{side}}$  signature of phase transition
- $R_{\text{out}}^2 - R_{\text{side}}^2 = \Delta\tau^2 \beta_t^2$ ;  $\Delta\tau$  – emission time
- $R_{\text{long}}$  temperature of kinetic freeze-out and source lifetime



New data from  $\sqrt{s_{NN}} = 4.5$  GeV follow trend observed for low collision energies

# Identical pion femtoscopy



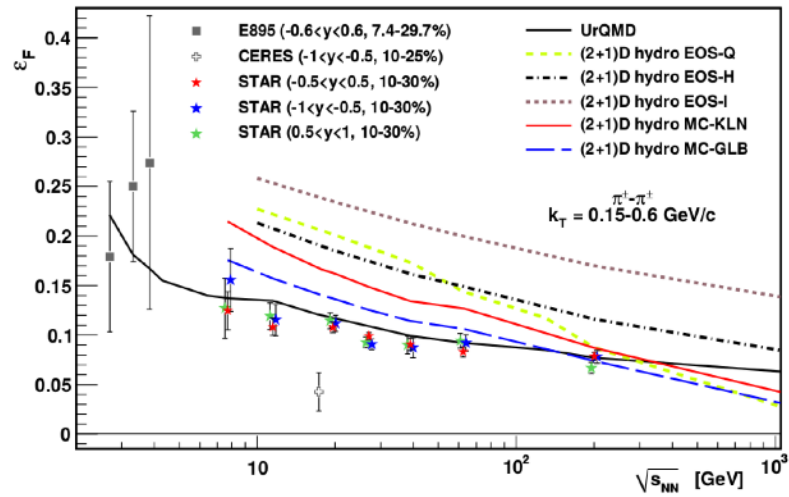
$$\varepsilon_{PP} = \frac{\sqrt{(\sigma_y^2 - \sigma_x^2)^2 + 4\sigma_{xy}^2}}{\sigma_x^2 + \sigma_y^2}$$

$$\varepsilon_F = \frac{\sigma_y^2 - \sigma_x^2}{\sigma_y^2 + \sigma_x^2} \approx 2 \frac{R_{s,2}^2}{R_{s,0}^2}$$

$$\sigma_x^2 = \{x^2\} - \{x\}^2 \text{ and } \sigma_y^2 = \{y^2\} - \{y\}^2$$

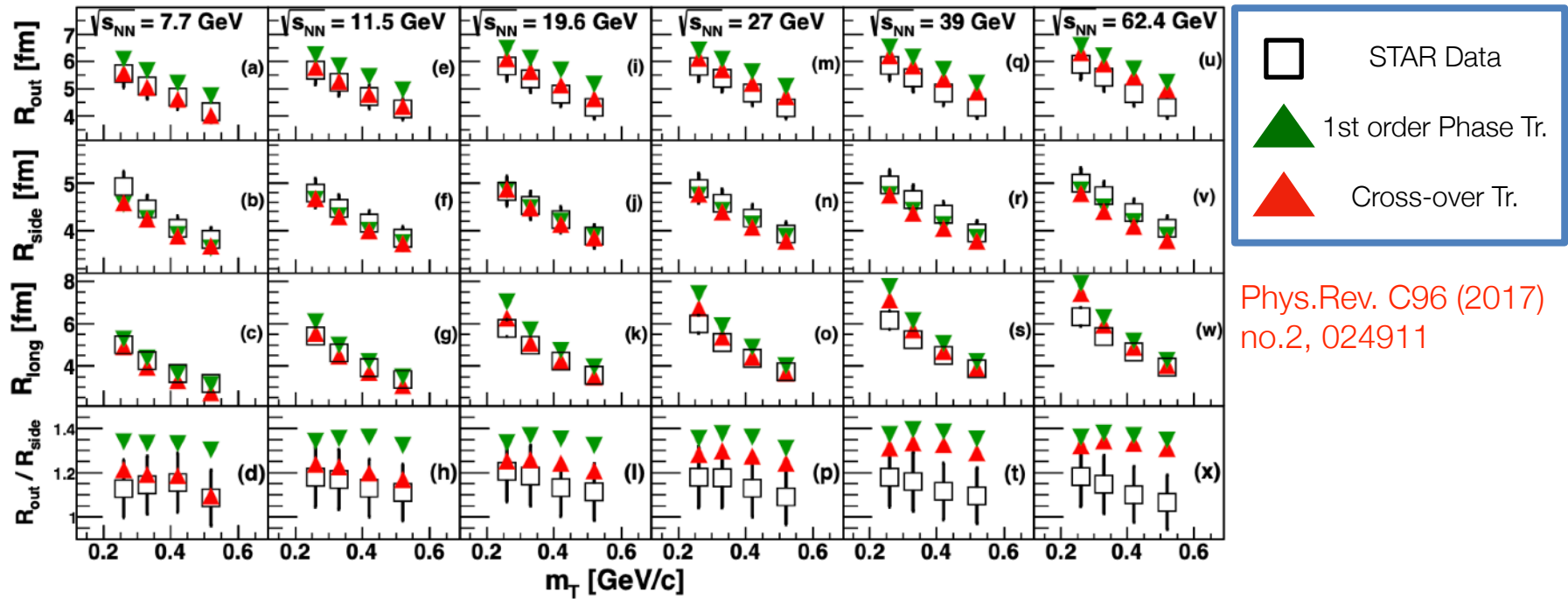
$$R_{\mu}^2(\Phi) = R_{\mu,0}^2 + 2 \sum_{n=2,4,6\dots} R_{\mu,n}^2 \cos(n\Phi) \quad (\mu = o, s, l, ol)$$

$$R_{\mu}^2(\Phi) = R_{\mu,0}^2 + 2 \sum_{n=2,4,6\dots} R_{\mu,n}^2 \sin(n\Phi) \quad (\mu = os)$$



System evolves faster in the reaction plane

# How to measure a phase transition?



Pre-thermal phase



Hydrodynamical phase



Hydronic cascades

UrQMD

vHLEE

UrQMD

vHLEE (3+1)-D viscous hydrodynamics  
 Iu. Karpenko, P. Huovinen, H. Petersen, M. Bleicher  
 Phys.Rev. C 91, 064901 (2015), arXiv:1502.01978,1509.3751

HadronGas + Bag Model  $\rightarrow$  1<sup>st</sup> order PT

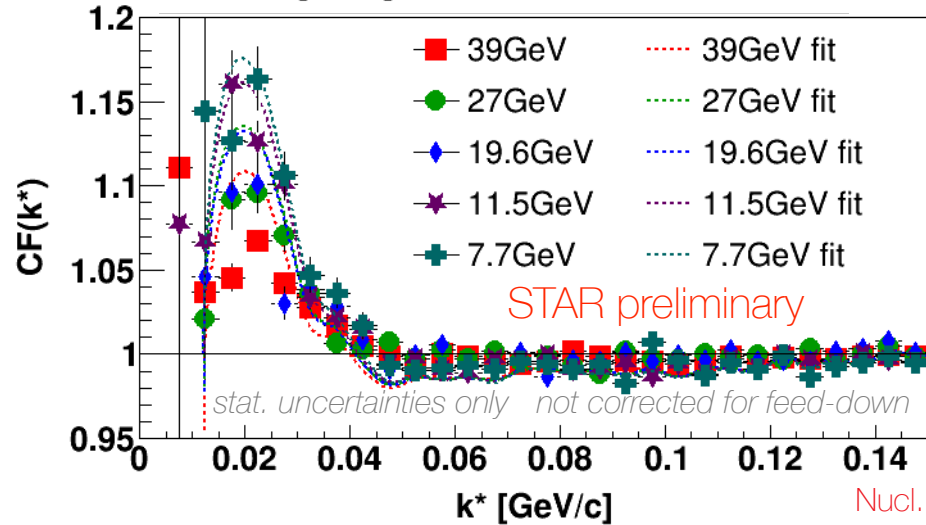
P.F. Kolb, et al, PR C 62, 054909 (2000)

Chiral EoS  $\rightarrow$  crossover PT (XPT)  
 J. Steinheimer, et al, J. Phys. G 38, 035001 (2011)

vHLEE+UrQMD model verify sensitivity of HBT measurements to the first-order phase transition

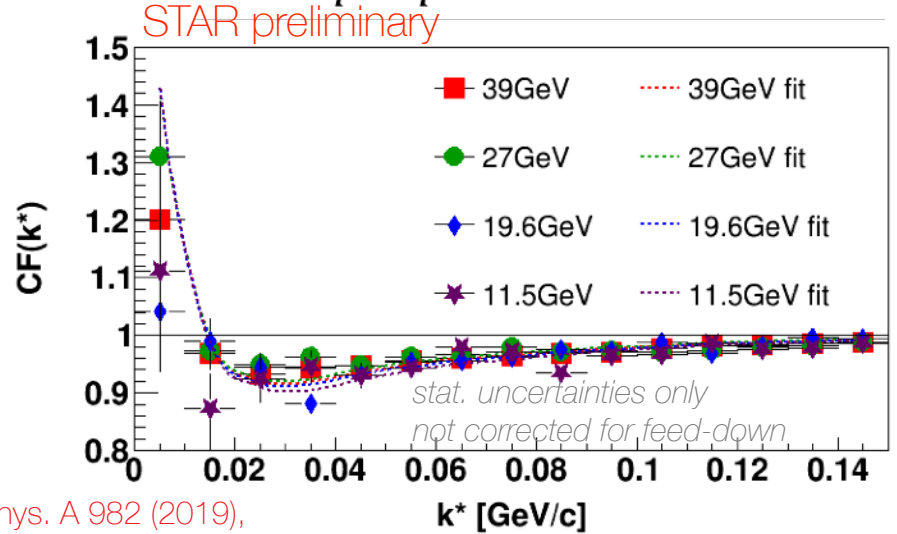
# Other systems: energy dependence

$p - p$  : Au+Au 0-10%

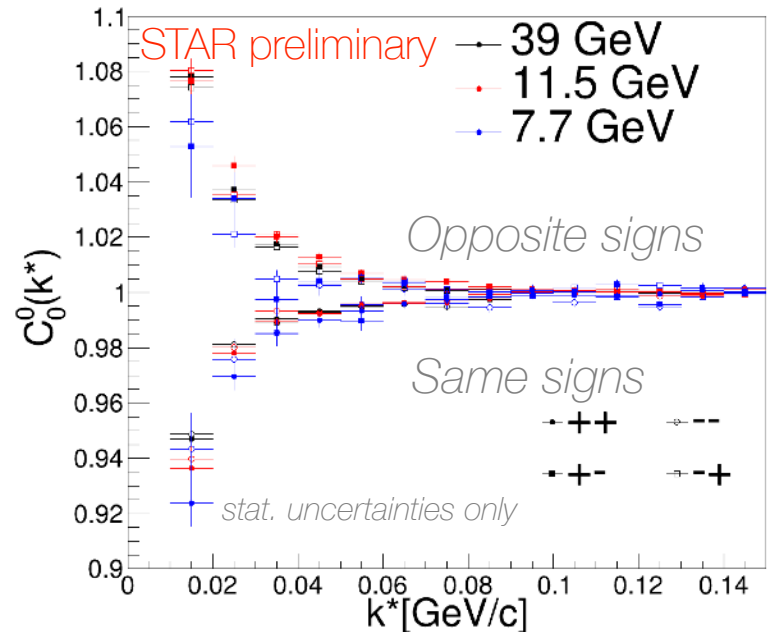


Nucl. Phys. A 982 (2019),  
359-362

$p - \bar{p}$  : Au+Au 0-10%



$\pi - K$  : Au+Au 0-10 %



energy	$R_{inv} p - p$ [fm]	$R_{inv} p - \bar{p}$ [fm]
7.7 GeV	$3.59 \pm 0.16 \pm 0.19$	
11.5 GeV	$3.66 \pm 0.08 \pm 0.05$	$3.30 \pm 0.42 \pm 0.28$
19.6 GeV	$3.82 \pm 0.15 \pm 0.06$	$3.32 \pm 0.25 \pm 0.13$
27 GeV	$3.80 \pm 0.12 \pm 0.08$	$3.49 \pm 0.25 \pm 0.16$
39 GeV	$4.00 \pm 0.15 \pm 0.02$	$3.39 \pm 0.12 \pm 0.14$

Clear energy dependence seen

# Non-identical particle correlations - introduction

$$C(\mathbf{q}) = \sum_{l,m} C_l^m(\mathbf{q}) Y_l^m(\theta, \phi)$$

$$C_l^m(\mathbf{q}) = \int_{\Omega} C(\mathbf{q}, \theta, \phi) Y_l^m(\theta, \phi) d\Omega$$

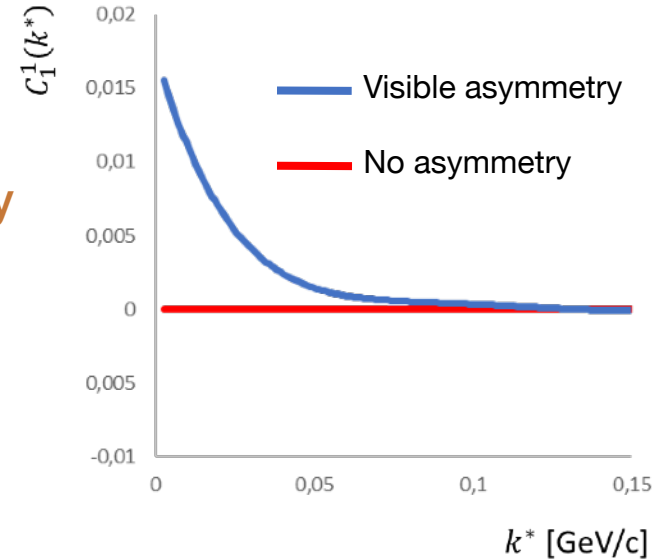
$\Omega$  – full solid angle

$Y_l^m(\theta, \phi)$  – spherical harmonic function

$\mathbf{q} = |\mathbf{q}|, \theta, \phi$  – spherical coordinates

**C00** → source size

**C11** → space-time asymmetry

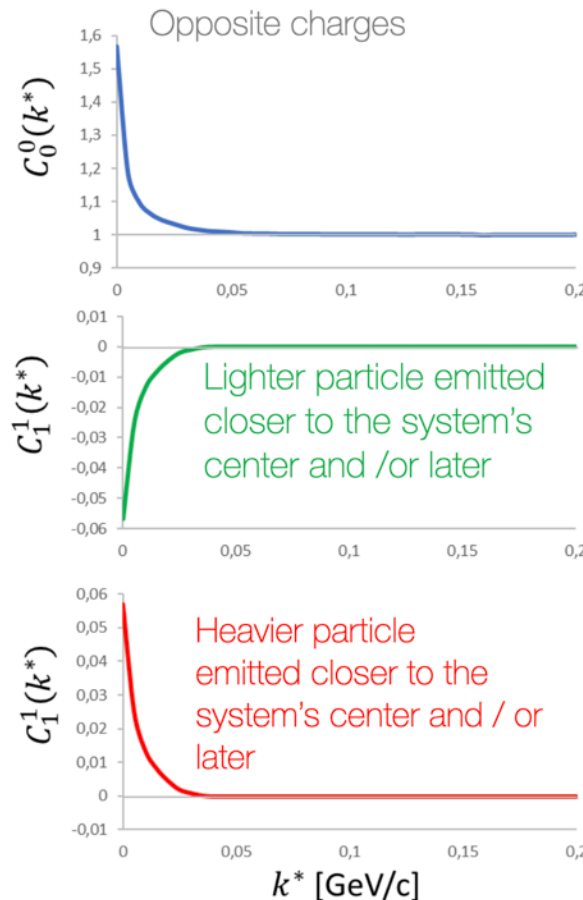
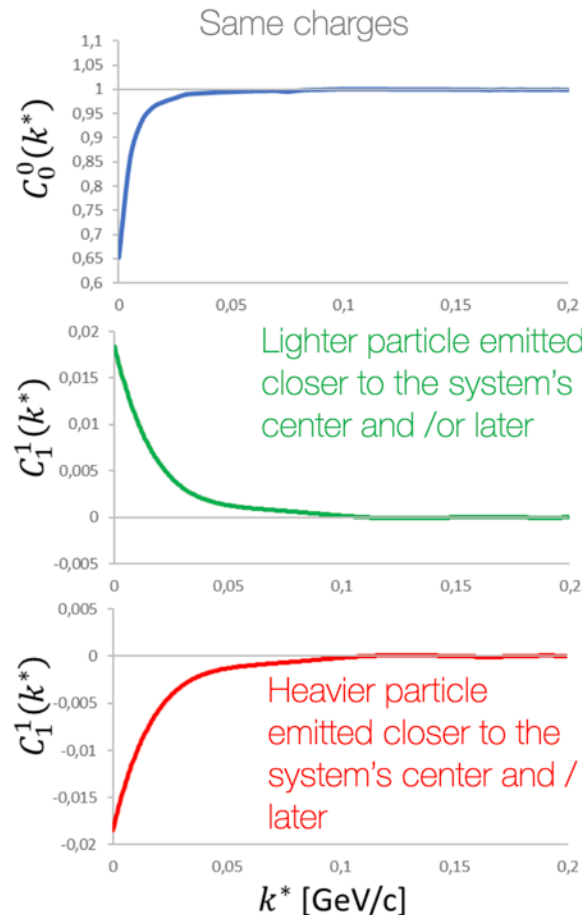


P. Danielewicz and S.Pratt.  
Phys. Lett. B618: 60 2005

P. Danielewicz and S.Pratt.  
Phys. Rev. C75:034907 2007

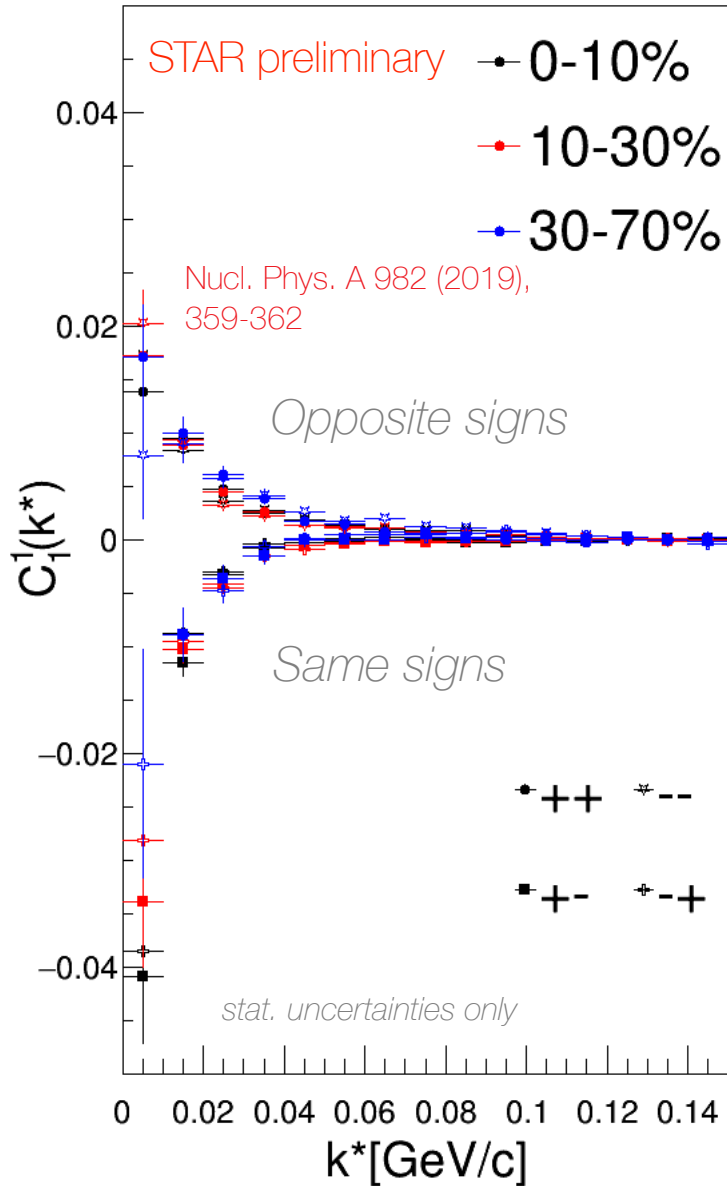
A. Kisiel  
Phys. Rev. C81:064906 2010

A. Kisiel and D. A. Brown  
Phys. Rev. C80:064911 2009



# Source dynamics: **centrality** and **energy** dependencies

$\pi - K$  @ Au+Au 39 GeV



Asymmetry does not disappear in lower energies

Clear signal of emission asymmetry

$\pi - K$  : Au+Au 0-10%

