



**Warsaw University
of Technology**



Two-particle correlation at the BES program at STAR

Introduction

- HIC and HBT method
- Correlation femtoscopy
- RHIC / STAR / BES;

Results

- Identical pions
- Other systems
- SI studies

Summary

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Supported in part by



**U.S. DEPARTMENT OF
ENERGY**

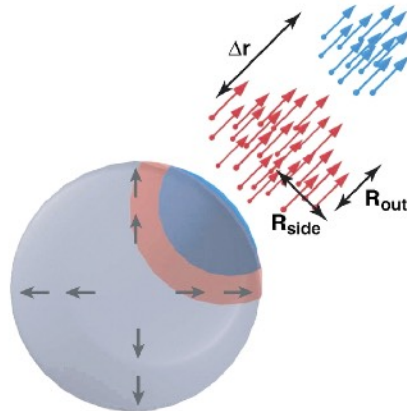
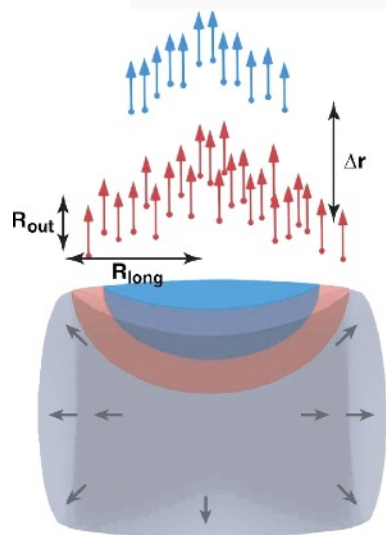
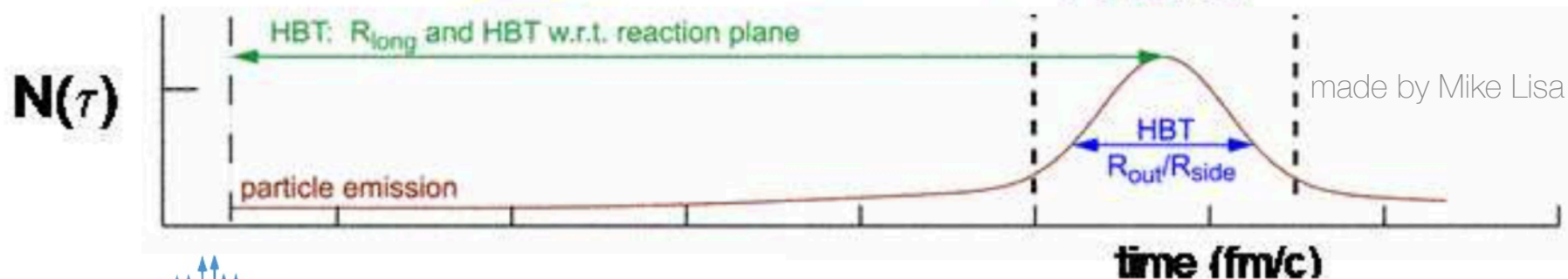
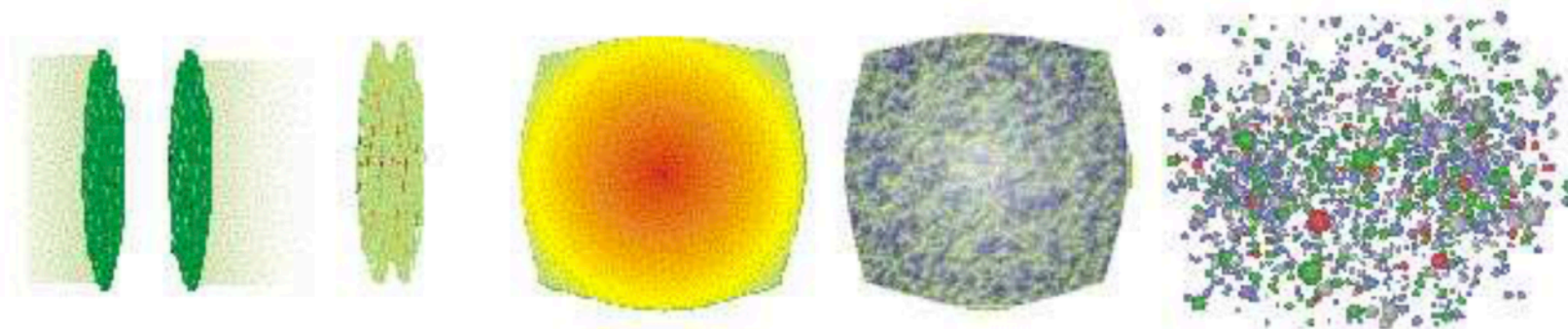


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Introduction

Heavy-Ion collision and **HBT** method



long - beam axis
out - pair transverse \mathbf{p}
side - perpendicular to out and long

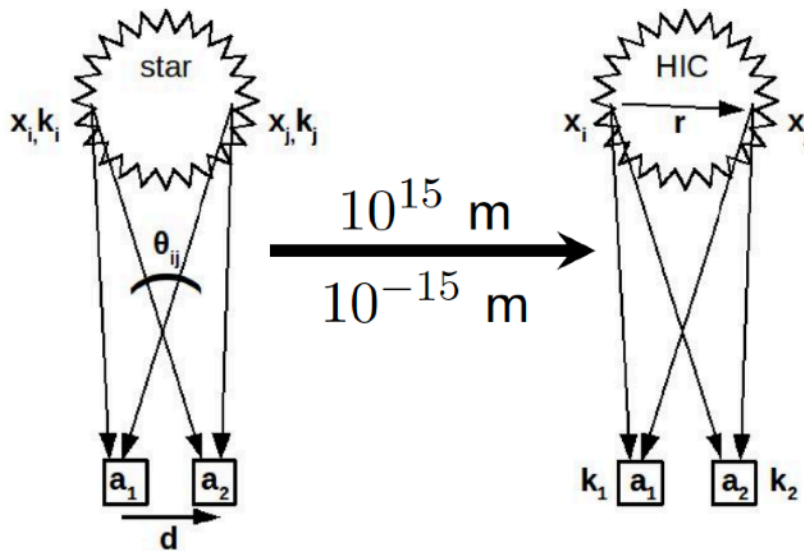
Homogeneity region

Correlation **femtosc**copy



Size: $\sim 10^{-15}$ m (**fm**)
Time: $\sim 10^{-23}$ s

**Impossible
to measure directly!**



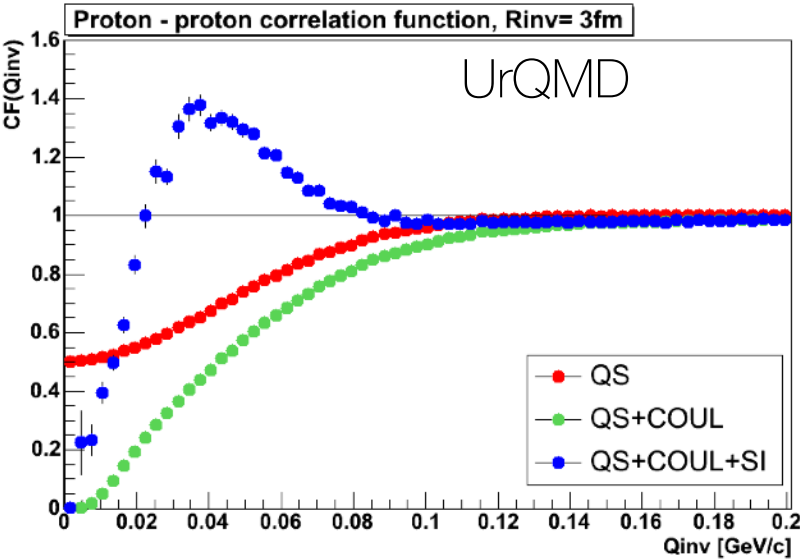
Femtosc (HIC) inspired by Hanbury Brown and Twiss interferometry method (Astronomy)

but!

- different scales,
- different measured quantities
- different determined quantities

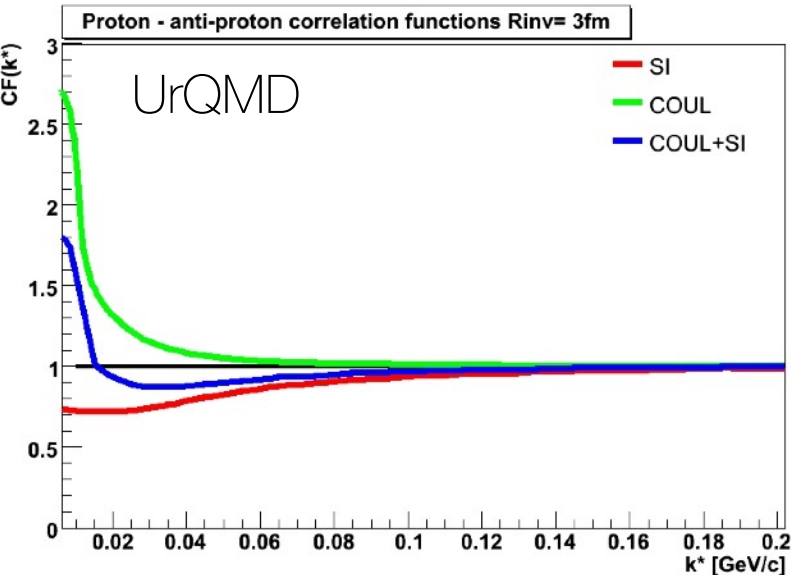
Hanbury Brown, R.; Twiss,
Nature 178, 1046–1048 (1956)

Two-particle correlations



Identical pairs:

- Quantum Statistics- **QS**
- Final State Interactions- **FSI**: Coulomb, Strong



Non-identical pairs:

- Final State Interactions- **FSI**: Coulomb, Strong

x_1, x_2 - space-time sizes (and dynamics)

(**can not** be measured directly) \rightarrow

Close velocity correlations
(**HBT + FSI**)

p_1, p_2 - momenta and momentum difference

(**can** be measured directly)

Single- and two-particle distributions:

$$P_1(p) = E \frac{dN}{d^3p} = \int d^4x S(x, p)$$

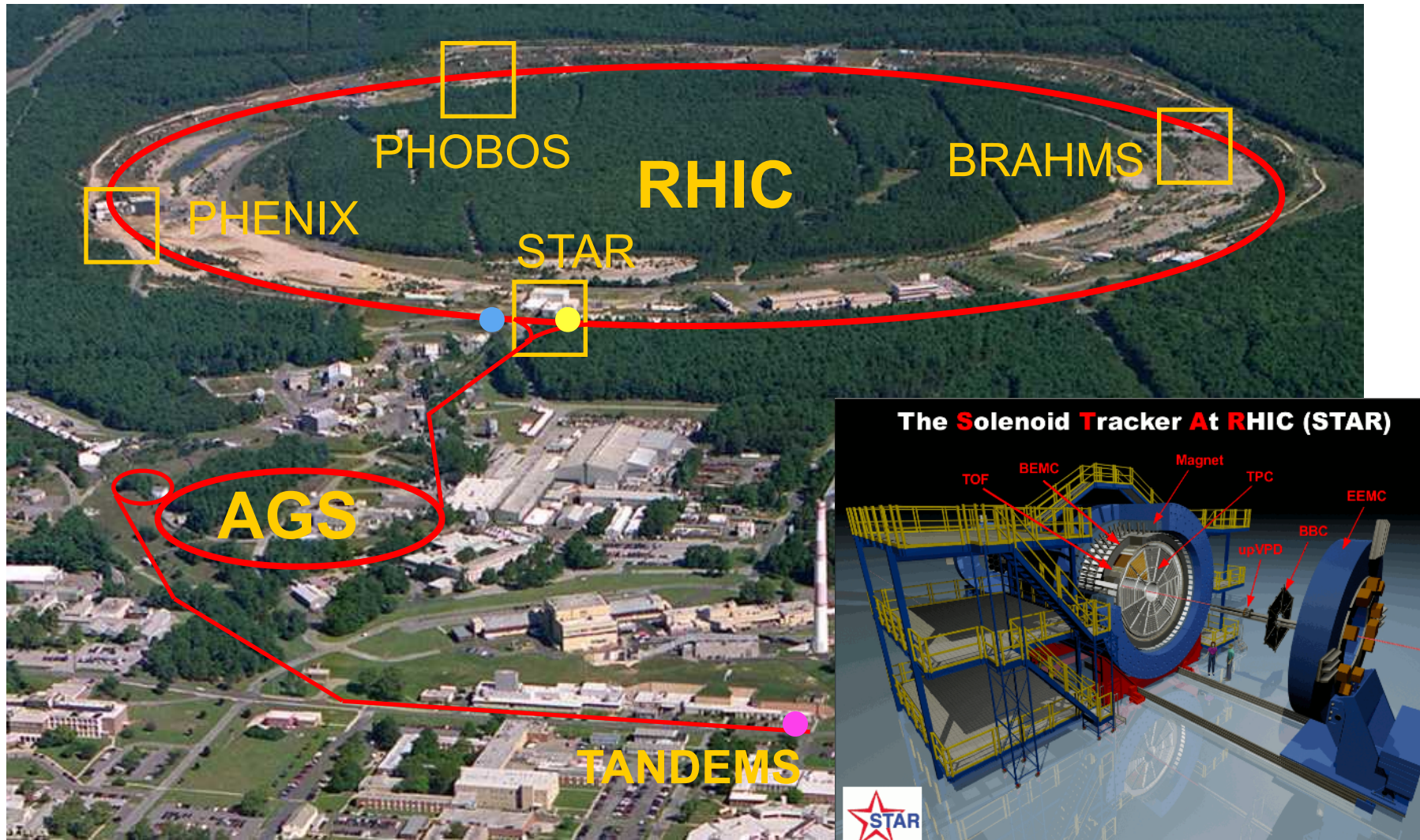
$$P_2(p_1, p_2) = E_1 E_2 \frac{dN}{d^3p_1 d^3p_2}$$

$$P_2(p_1, p_2) = \int d^4x_1 S(x_1, p_1) d^4x_2 S(x_2, p_2) \Phi(x_2, p_2 | x_1, p_1)$$

The correlation function:

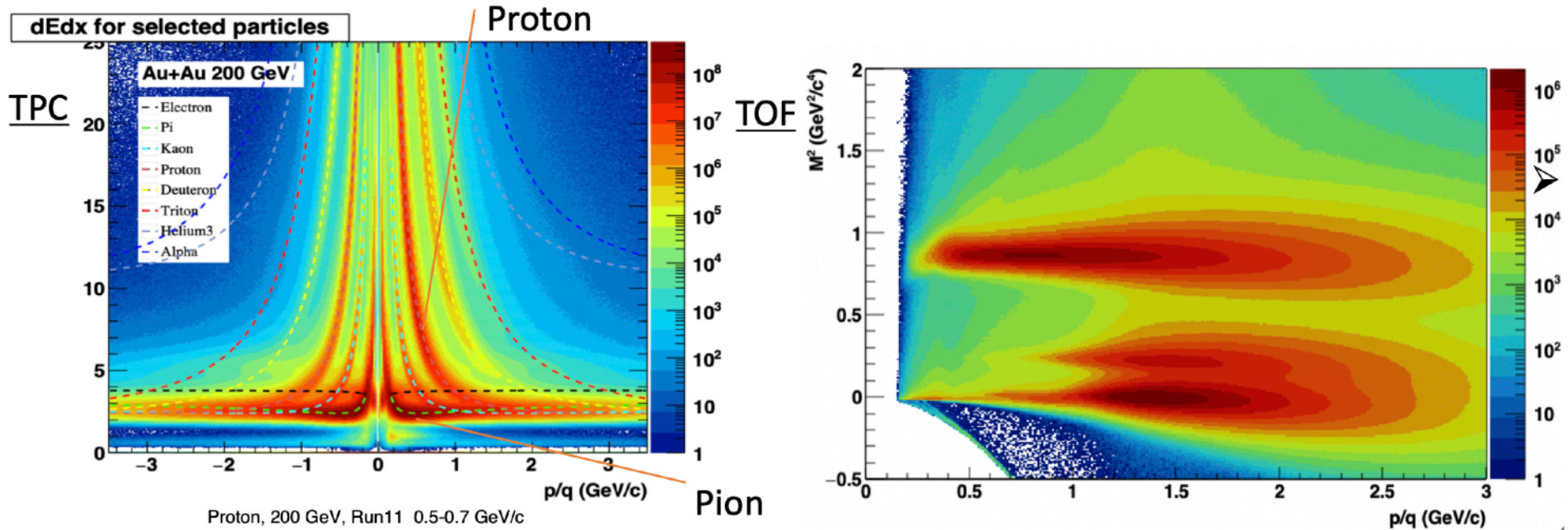
$$C(p_1, p_2) = \frac{P_2(p_1, p_2)}{P_1(p_1)P_1(p_2)}$$

Relativistic Heavy Ion Collider (**RHIC**) Brookhaven National Laboratory (**BNL**), Upton

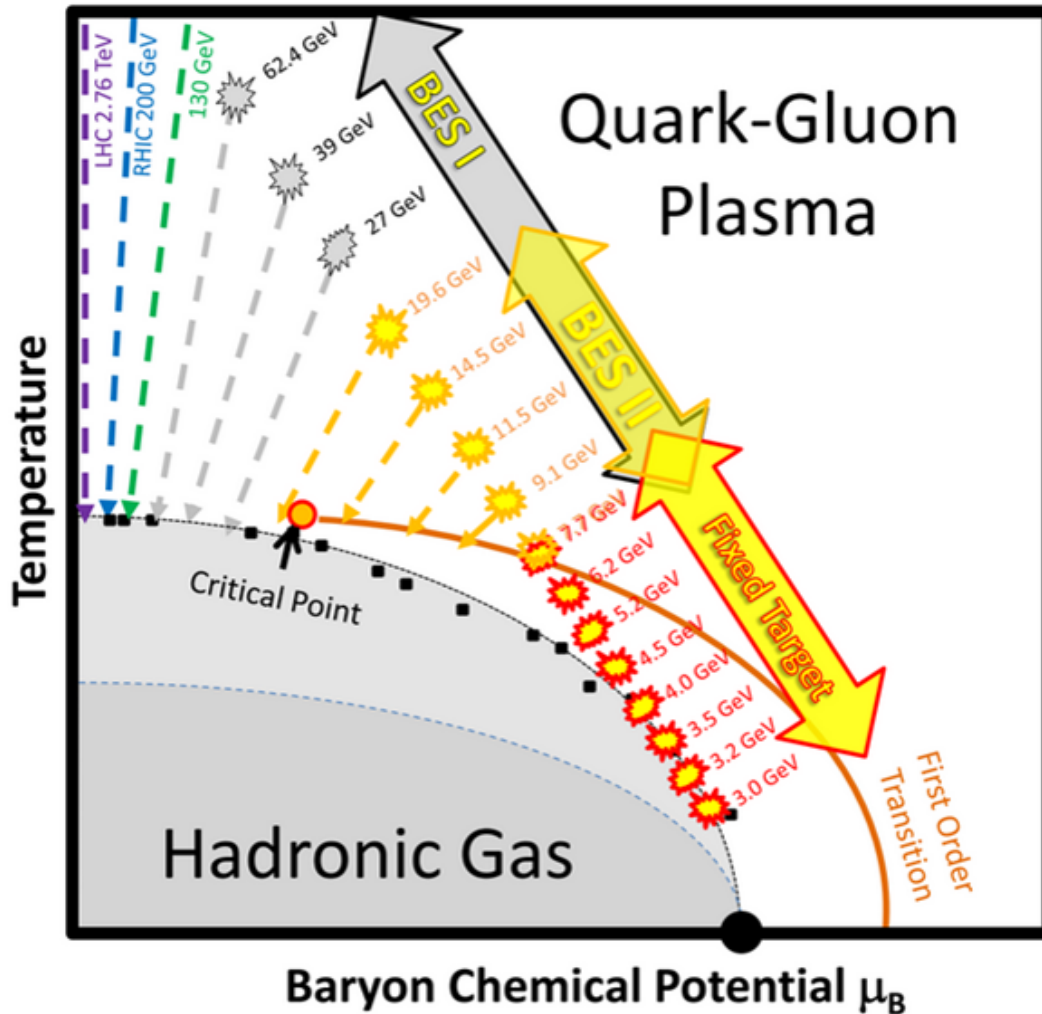


Particle Identification

Particle identification based on dE/dx and time-of-flight



Beam Energy Scan Program



RHIC Top Energy

p+p, p+Al, p+Au, d+Au,
 $^3\text{He}+\text{Au}$, Cu+Cu, Cu+Au,
Ru+Ru, Zr+Zr, Au+Au, U+U
QCD at high energy
density/temperature
Properties of QGP, EoS

Beam Energy Scan

Au+Au at $\sqrt{s_{NN}} = 7.7\text{-}62$ GeV

- QCD phase transition
- Search for critical point
- Turn-off of QGP signatures
- Chiral symmetry restoration

Fixed-Target Program

Au+Au at $\sqrt{s_{NN}} = 3.0\text{-}7.7$ GeV

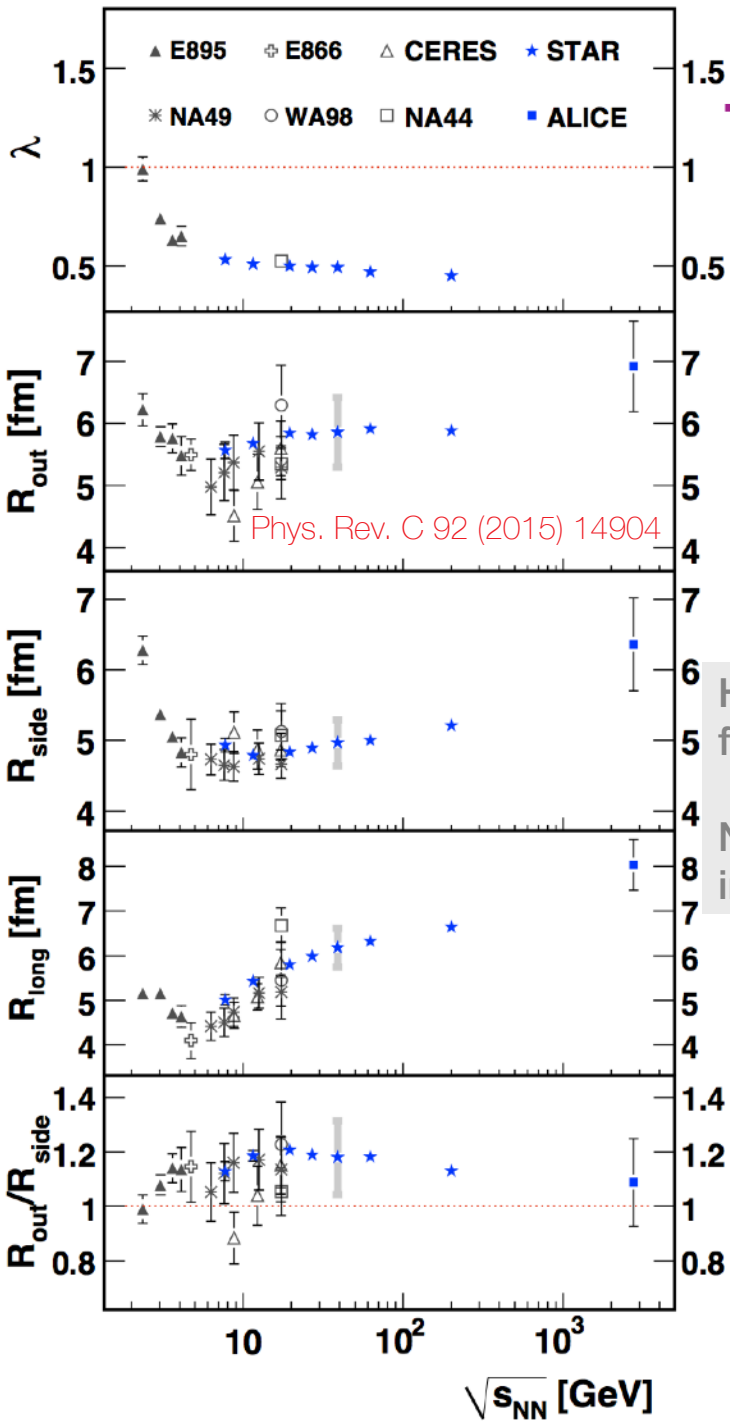
High baryon density regime

with $\mu_B = 420\text{-}720$ MeV



Results

Identical pion femtoscopy

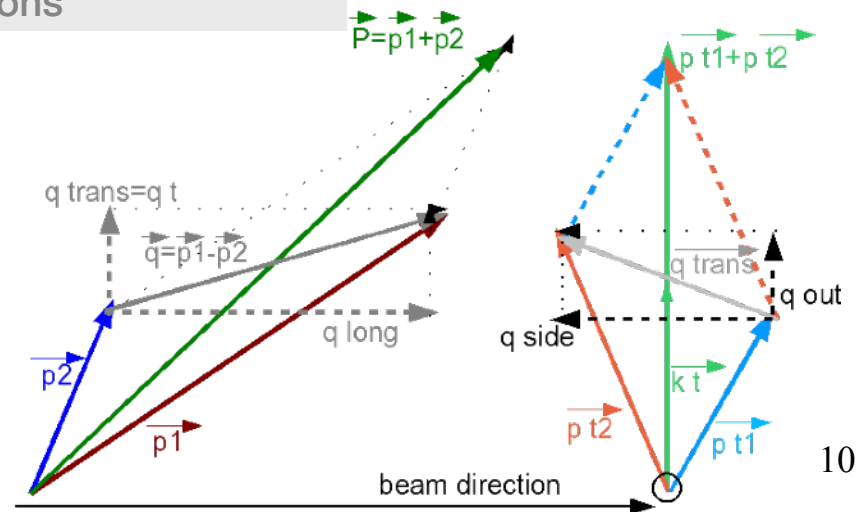


- R_{side} spatial source evolution in the transverse direction
- R_{out} related to spatial and time components
- R_{out}/R_{side} signature of phase transition
- $R_{out}^2 - R_{side}^2 = \Delta\tau^2 \beta_t^2$; $\Delta\tau$ – emission time
- R_{long} temperature of kinetic freeze-out and source lifetime

$$C(\vec{q}) = (1 - \lambda) + K_{Coul}(q_{inv})\lambda \times \exp(-q_o^2 R_o^2 - q_s^2 R_s^2 - q_l^2 R_l^2 - 2q_o q_s R_{os} - 2q_o q_l R_{ol})$$

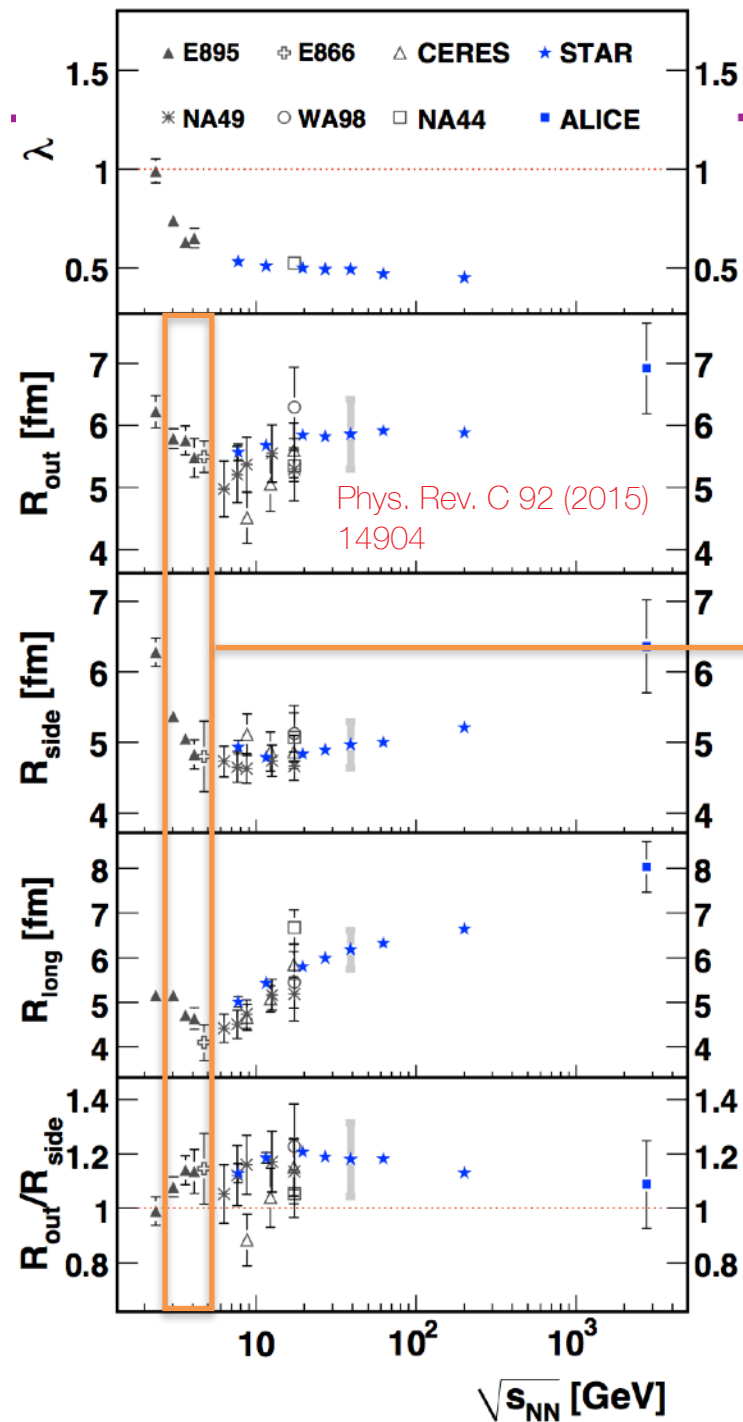
HBT source sizes determined for a wide range of collision energy;

Non-monotonic behavior seen in three directions

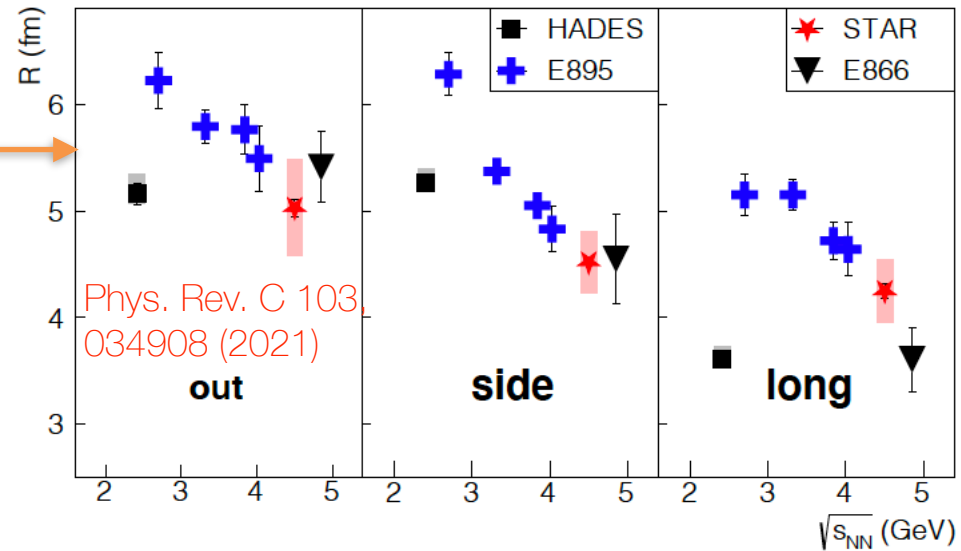


Identical pion femtoscopy

- R_{side} spatial source evolution in the transverse direction
- R_{out} related to spatial and time components
- R_{out}/R_{side} signature of phase transition
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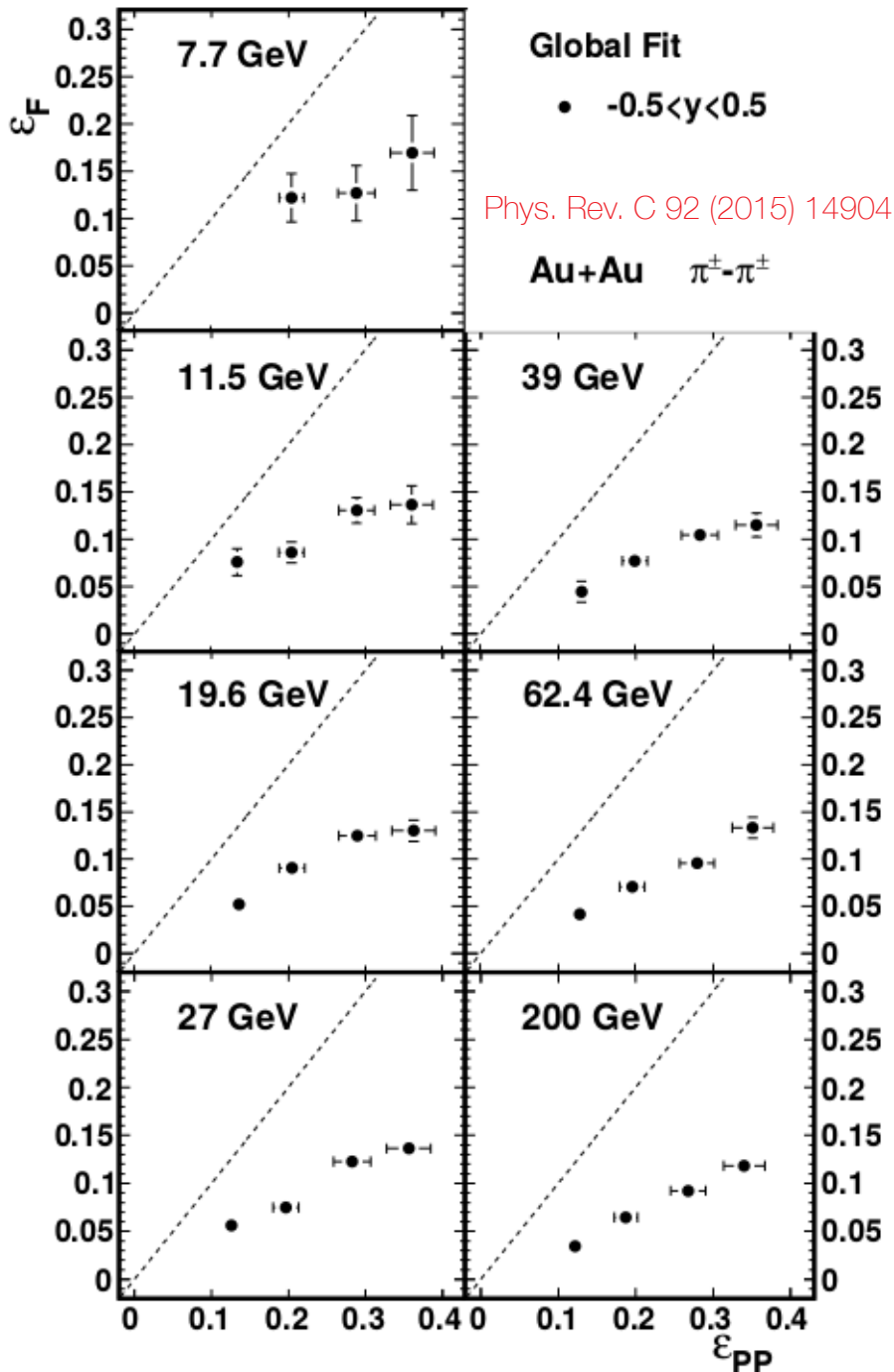


Phys. Rev. C 92 (2015)
14904



New data from $\sqrt{s_{NN}} = 4.5$ GeV follow trend observed for low collision energies

Identical pion femtoscopy



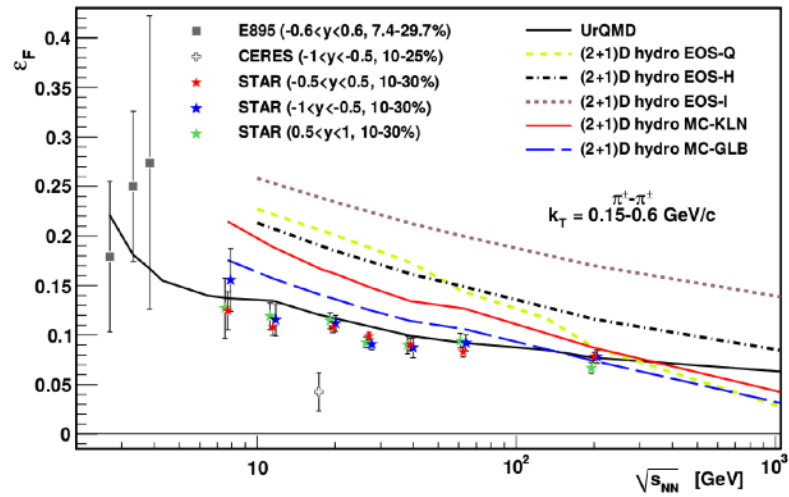
$$\varepsilon_{PP} = \frac{\sqrt{(\sigma_y^2 - \sigma_x^2)^2 + 4\sigma_{xy}^2}}{\sigma_x^2 + \sigma_y^2}$$

$$\varepsilon_F = \frac{\sigma_y^2 - \sigma_x^2}{\sigma_y^2 + \sigma_x^2} \approx 2 \frac{R_{s,2}^2}{R_{s,0}^2}$$

$$\sigma_x^2 = \{x^2\} - \{x\}^2 \text{ and } \sigma_y^2 = \{y^2\} - \{y\}^2$$

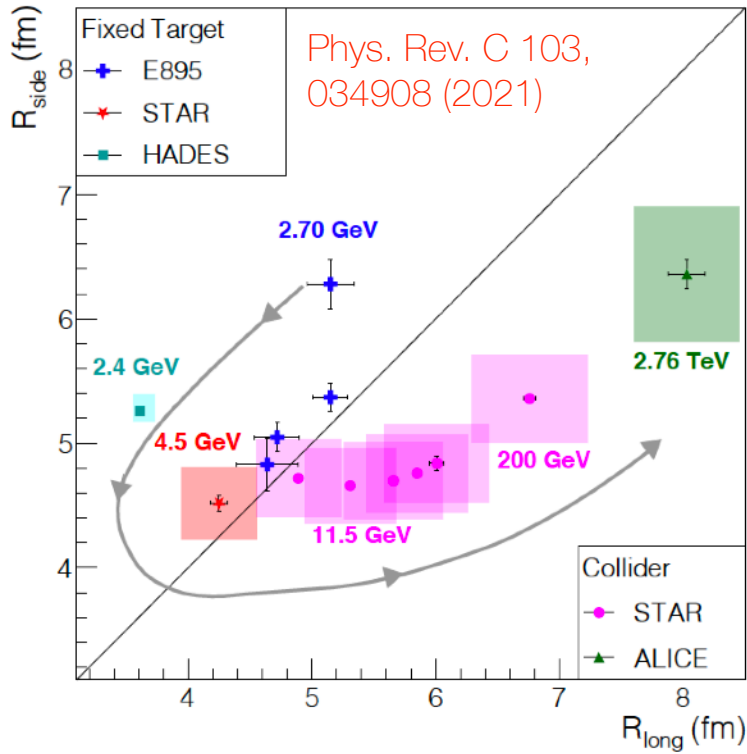
$$R_{\mu}^2(\Phi) = R_{\mu,0}^2 + 2 \sum_{n=2,4,6\dots} R_{\mu,n}^2 \cos(n\Phi) \quad (\mu = o, s, l, ol)$$

$$R_{\mu}^2(\Phi) = R_{\mu,0}^2 + 2 \sum_{n=2,4,6\dots} R_{\mu,n}^2 \sin(n\Phi) \quad (\mu = os)$$



System evolves faster in the reaction plane

How to measure a phase transition?



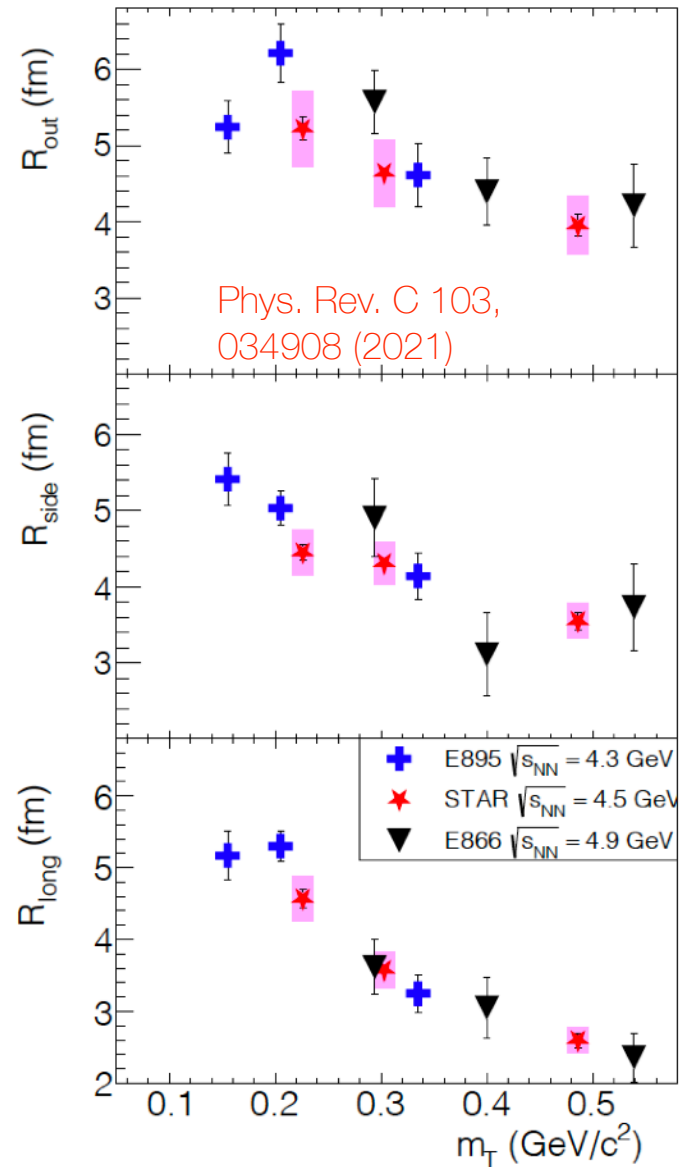
Clear evolution in the freeze-out shape indicated

Lower energies: system more oblate ($R_{side} > R_{long}$)

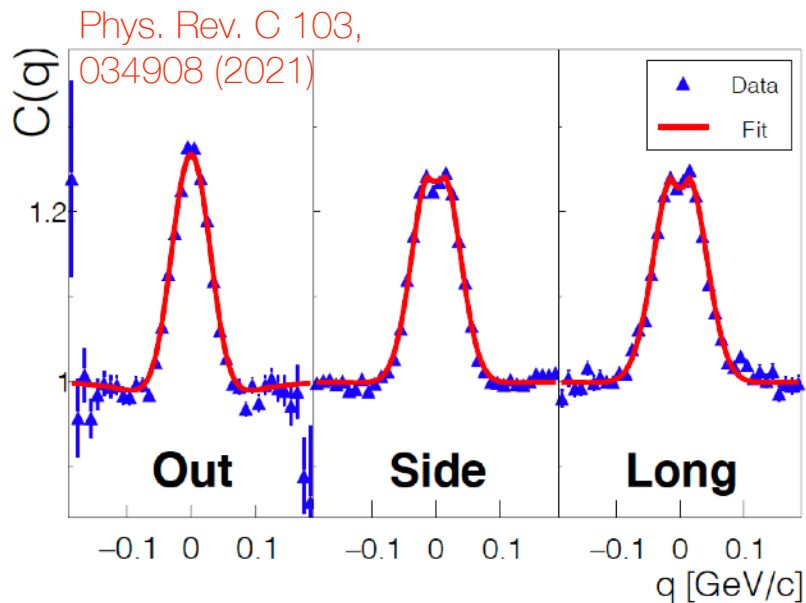
Higher energies: system more prolate ($R_{side} < R_{long}$)

$\sqrt{s_{NN}} = 4.5$ GeV: round system ($R_{side} \simeq R_{long}$)

Transition region between dynamics dominated by stopping and boost-invariant dynamics.



How to measure a phase transition?

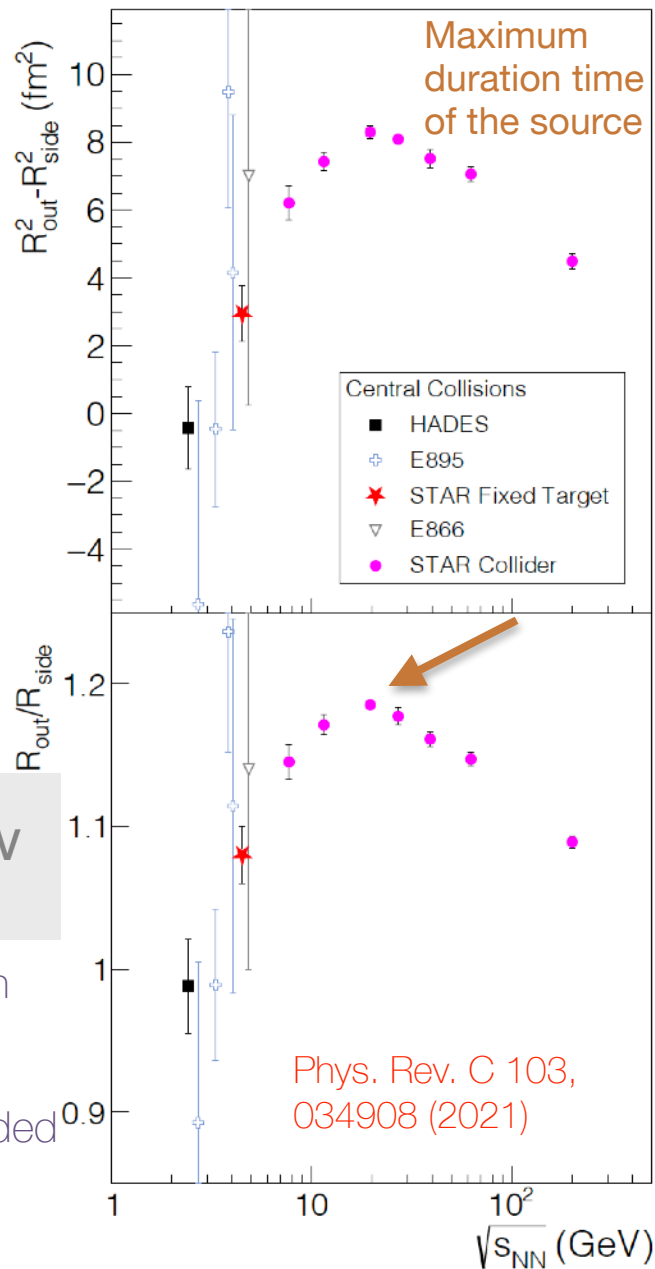


$$R_{out}^2 - R_{side}^2 = \beta_t^2 \Delta\tau^2$$

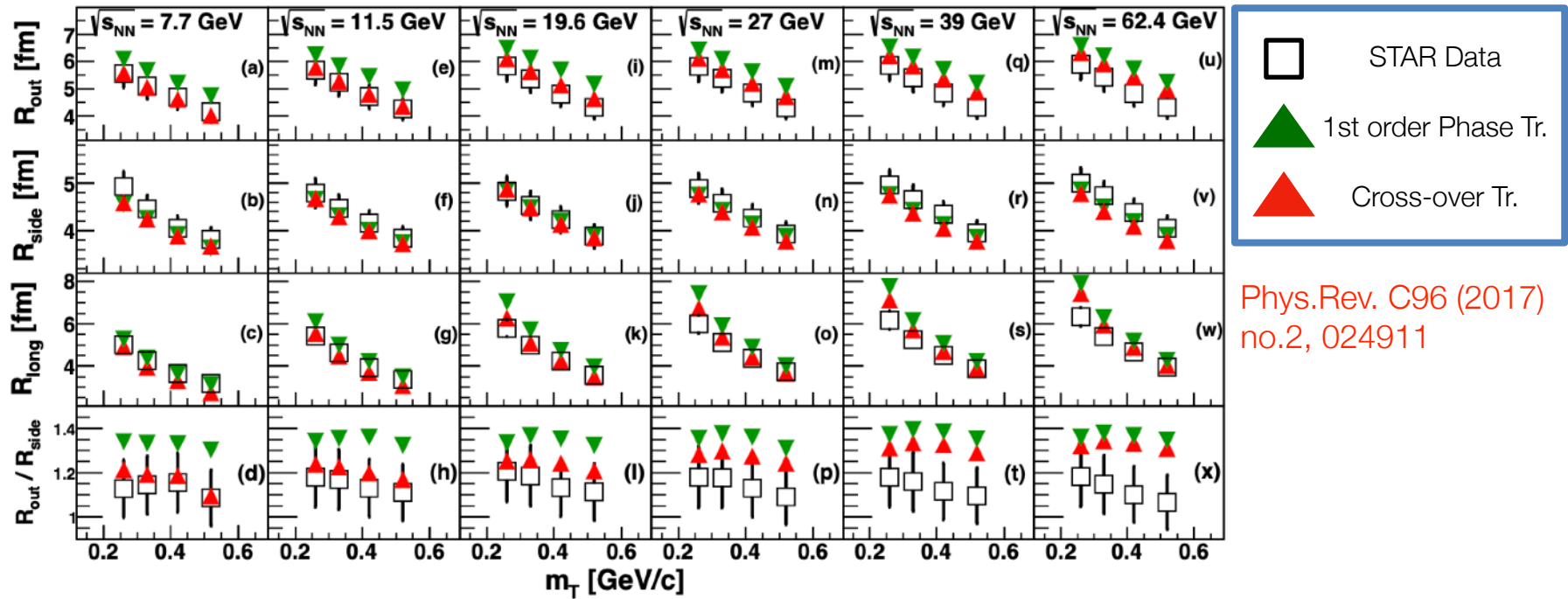
Visible peak in $\frac{R_{out}}{R_{side}}(\sqrt{s_{NN}})$ near the $\sqrt{s_{NN}} \simeq 20$ GeV

QCD calculations predict a peak near to the QGP transition threshold - signature of first-order phase transition?

Theoretical attention from hydro and transport models needed



How to measure a phase transition?



Pre-thermal phase



Hydrodynamical phase



Hydronic cascades

UrQMD

vHLEE

UrQMD

vHLEE (3+1)-D viscous hydrodynamics
 Iu. Karpenko, P. Huovinen, H. Petersen, M. Bleicher
 Phys.Rev. C 91, 064901 (2015), arXiv:1502.01978,1509.3751

HadronGas + Bag Model \rightarrow 1st order PT

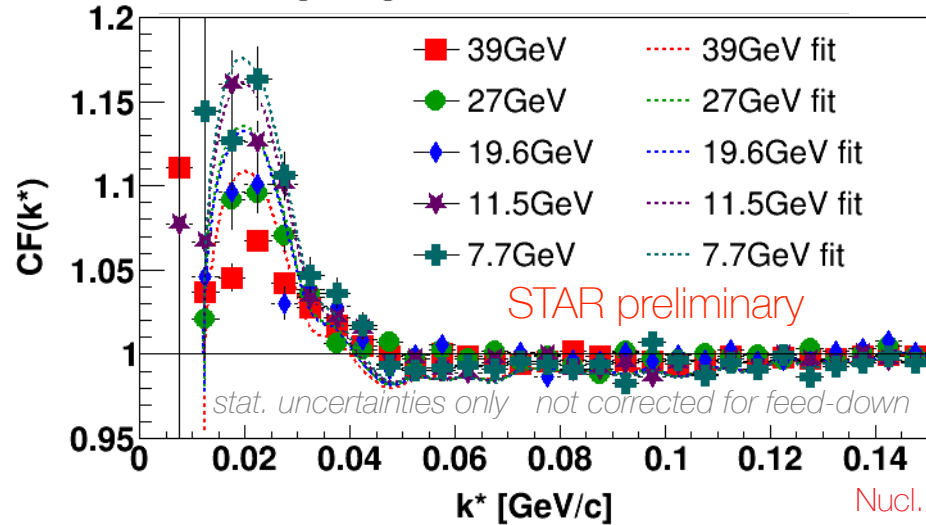
P.F. Kolb, et al, PR C 62, 054909 (2000)

Chiral EoS \rightarrow crossover PT (XPT)
 J. Steinheimer, et al, J. Phys. G 38, 035001 (2011)

vHLEE+UrQMD model verifies sensitivity of HBT measurements to the first-order phase transition

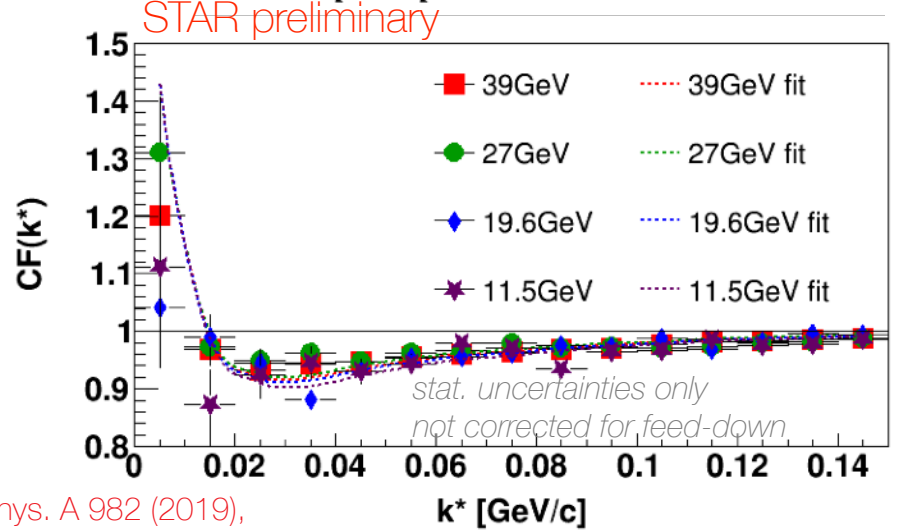
Other systems: energy dependence

$p - p$: Au+Au 0-10%

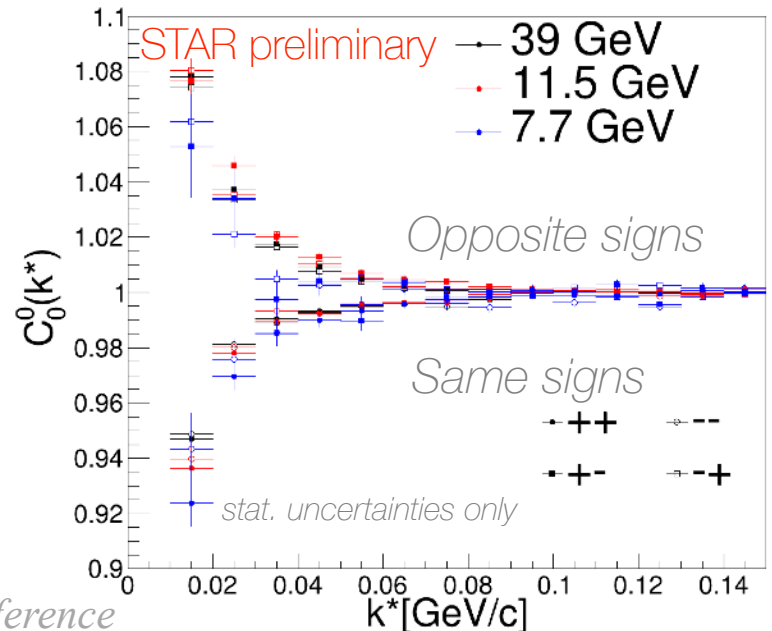


Nucl. Phys. A 982 (2019),
359-362

$p - \bar{p}$: Au+Au 0-10%



$\pi - K$: Au+Au 0-10 %



energy	$R_{inv} p - p$ [fm]	$R_{inv} p - \bar{p}$ [fm]
7.7 GeV	$3.59 \pm 0.16 \pm 0.19$	
11.5 GeV	$3.66 \pm 0.08 \pm 0.05$	$3.30 \pm 0.42 \pm 0.28$
19.6 GeV	$3.82 \pm 0.15 \pm 0.06$	$3.32 \pm 0.25 \pm 0.13$
27 GeV	$3.80 \pm 0.12 \pm 0.08$	$3.49 \pm 0.25 \pm 0.16$
39 GeV	$4.00 \pm 0.15 \pm 0.02$	$3.39 \pm 0.12 \pm 0.14$

Clear energy dependence seen

k^* - momentum of the first particle in the Pair Rest Frame reference

Non-identical particle correlations - introduction

$$C(\mathbf{q}) = \sum_{l,m} C_l^m(\mathbf{q}) Y_l^m(\theta, \phi)$$

$$C_l^m(\mathbf{q}) = \int_{\Omega} C(\mathbf{q}, \theta, \phi) Y_l^m(\theta, \phi) d\Omega$$

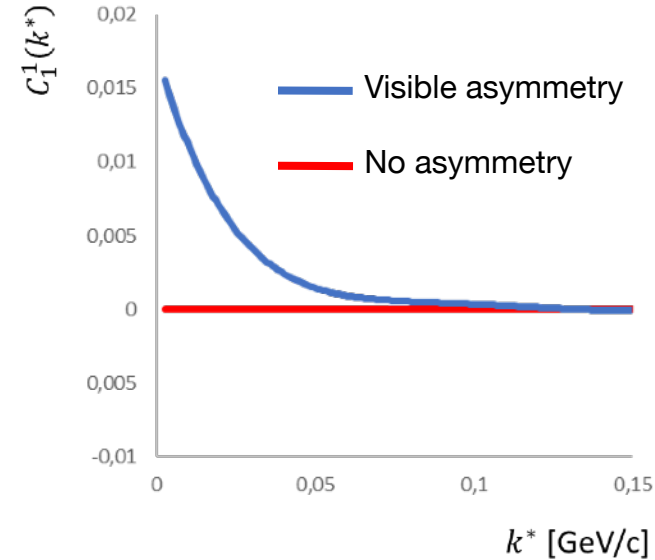
Ω – full solid angle

$Y_l^m(\theta, \phi)$ – spherical harmonic function

$\mathbf{q} = |\mathbf{q}|, \theta, \phi$ – spherical coordinates

$C_0^1 \rightarrow$ source **size**

$C_1^1 \rightarrow$ space-time **asymmetry**

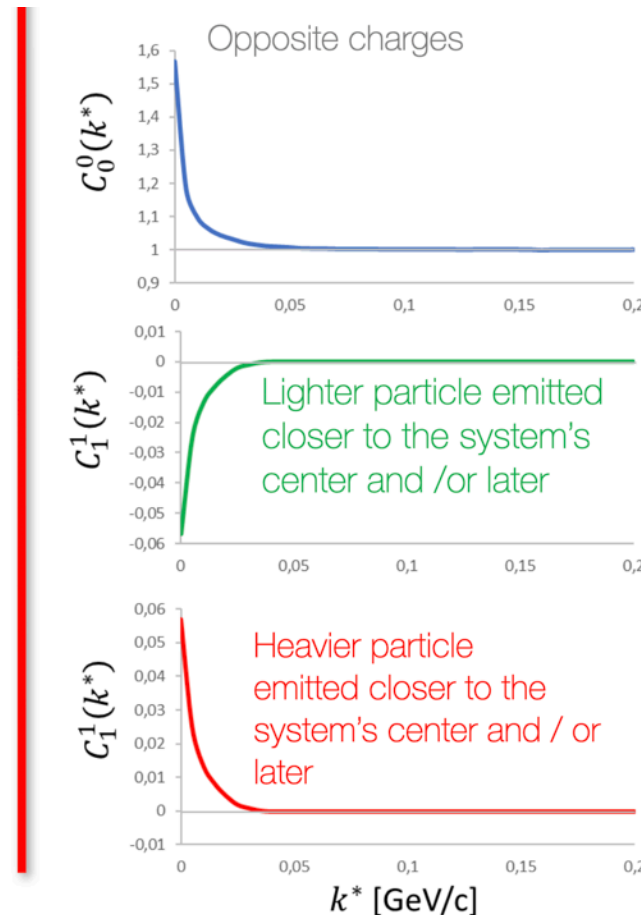
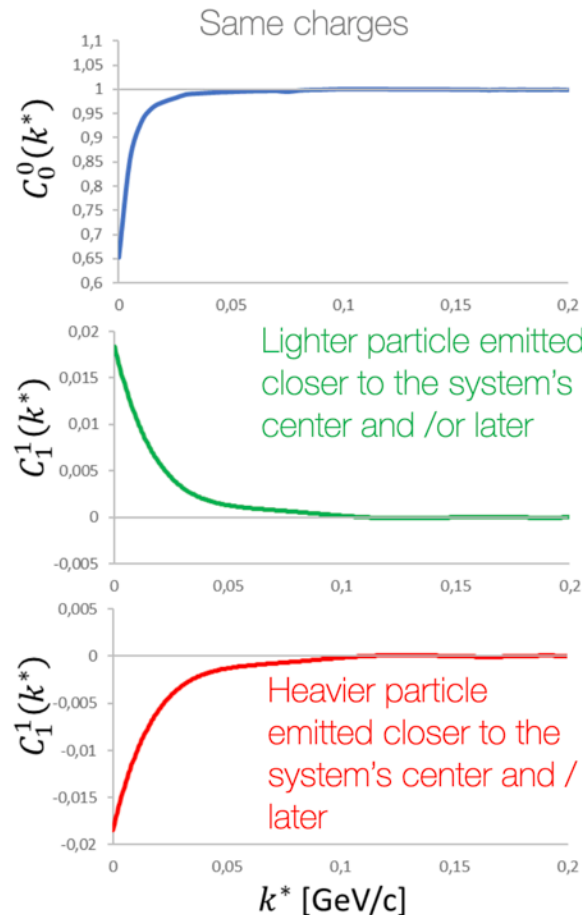


P. Danielewicz and S.Pratt.
Phys. Lett. B618: 60 2005

P. Danielewicz and S.Pratt.
Phys. Rev. C75:034907 2007

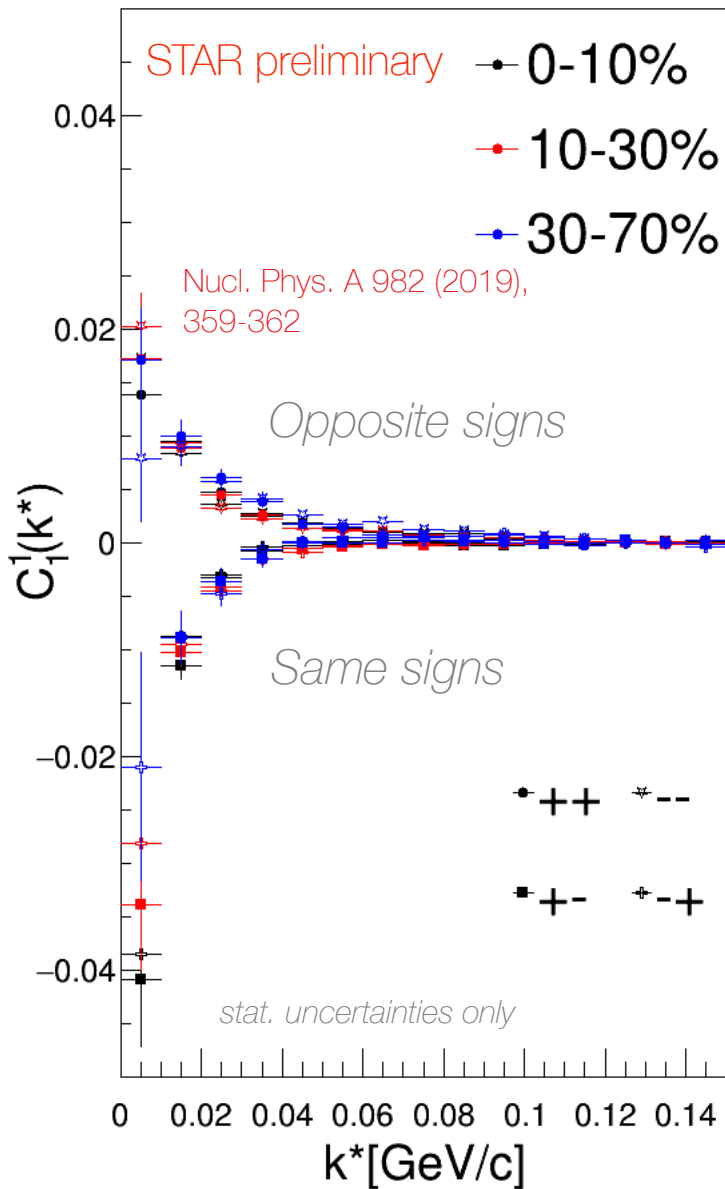
A. Kisiel
Phys. Rev. C81:064906 2010

A. Kisiel and D. A. Brown
Phys. Rev. C80:064911 2009



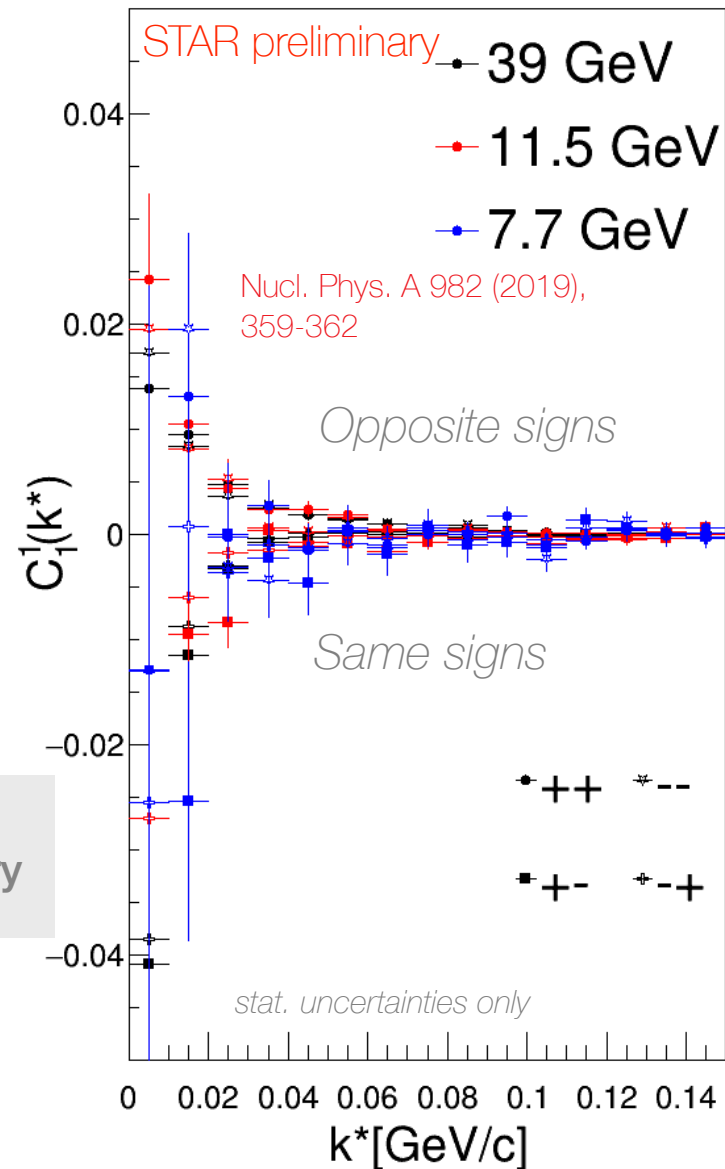
Source dynamics: **centrality** and **energy** dependencies

$\pi - K$ @ Au+Au 39 GeV



Asymmetry does not disappear in lower energies

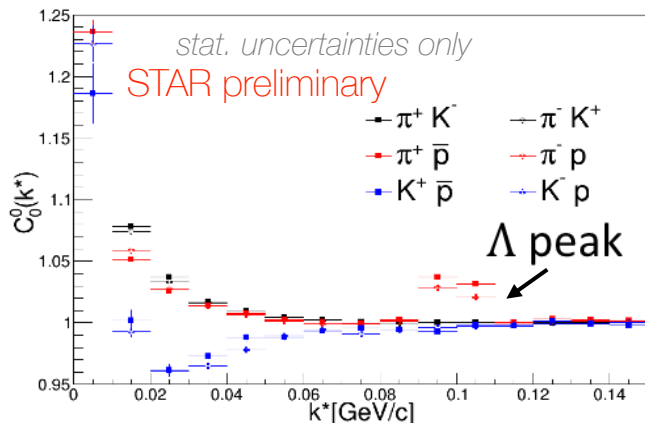
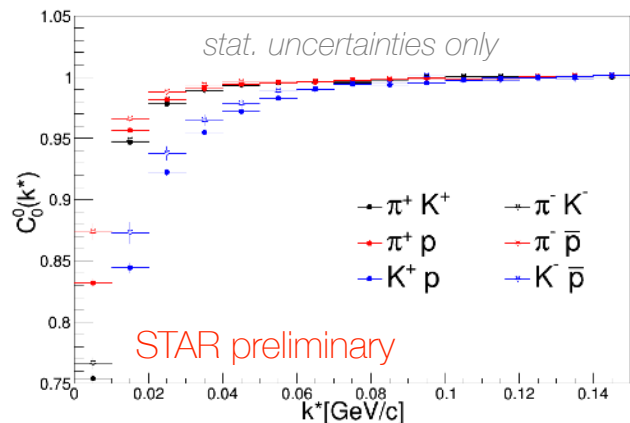
$\pi - K$: Au+Au 0-10%



Source dynamics: **system** dependence

Like-sign 0-10% @ Au+Au 39 GeV

Unlike-sign 0-10% @ Au+Au 39 GeV



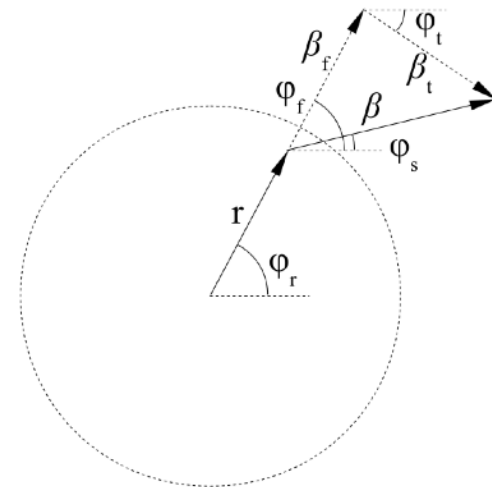
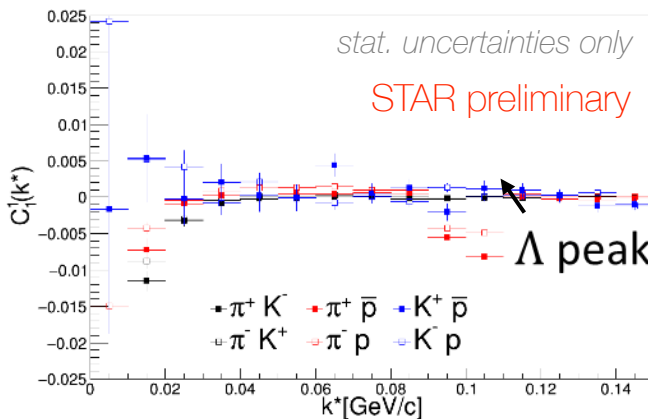
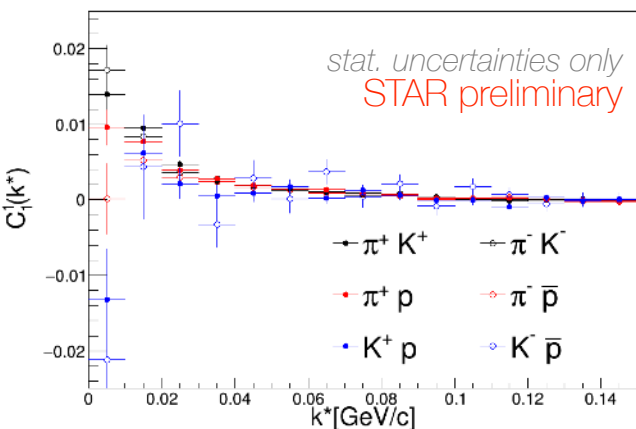
Heavier particles directed towards edge of the source.

Heavier particles freeze-out earlier

Phys. Rev. C81:064906 2010

Determined by **Coulomb** Interactions

Determined by full **FSI: Coulomb** and **Strong** interactions (kaon-proton)



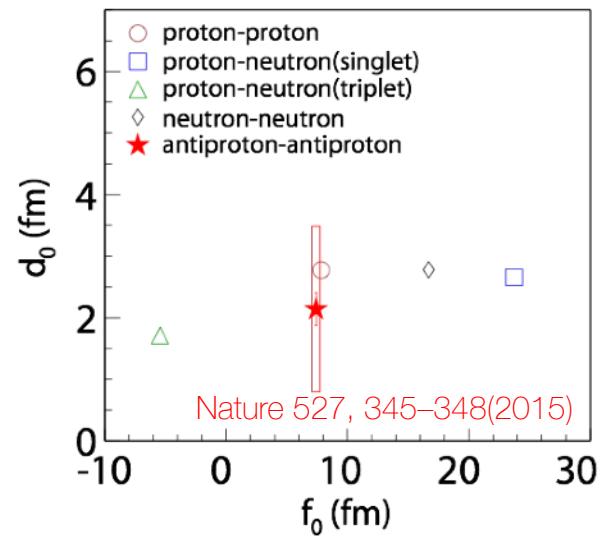
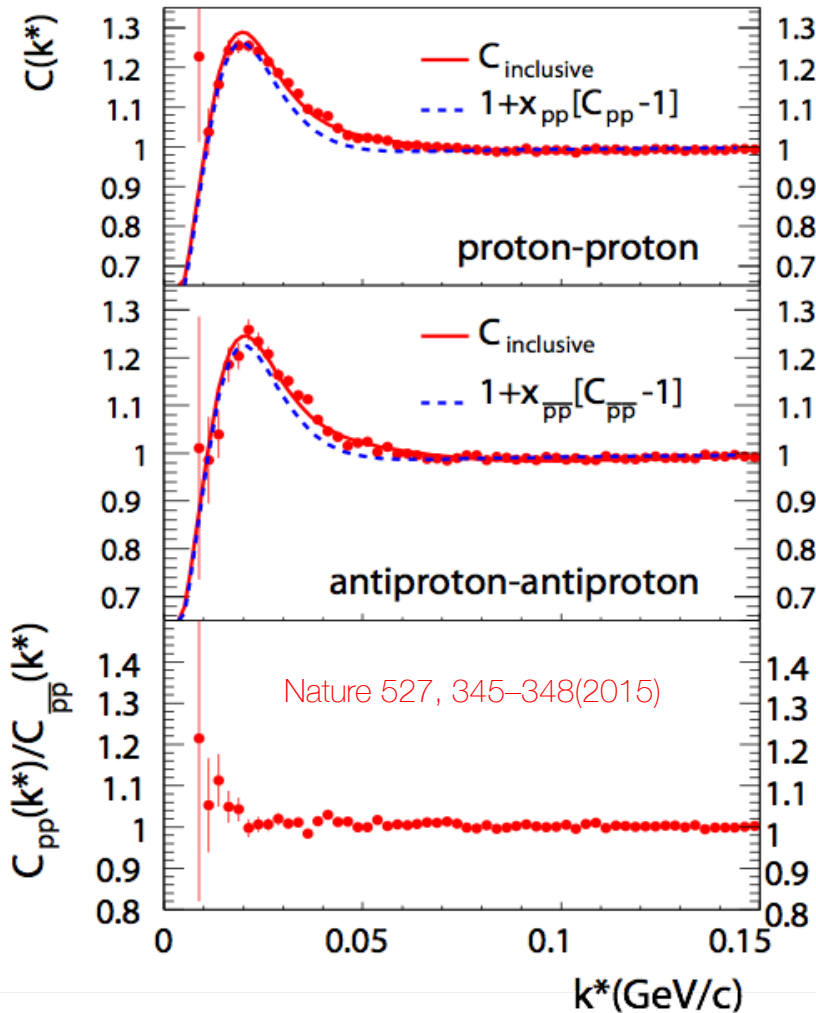
$$\langle x_{out} \rangle = \frac{\langle r \beta_f \rangle}{\langle \sqrt{\beta_t^2 + \beta_f^2} \rangle} = \frac{r_0 \beta_0 \beta}{\beta_0^2 + T/m_t}$$

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β_f - the same for both particles

$\beta_t \sim 1/m_T$ - smaller for heavier particles

Strong interactions between anti-nucleons



f_0 and d_0 - parameters of strong interaction

Scattering length f_0

Effective range d_0

Elastic cross section σ_e

$$\lim_{k \rightarrow 0} \sigma_e = 4\pi f_0^2$$

- f_0 and d_0 for the antiproton-antiproton interaction consistent with parameters for the proton-proton interaction.
- Descriptions of the interaction among antimatter (based on the simplest systems of anti-nucleons) determined.
- A quantitative verification of matter-antimatter symmetry in context of the forces responsible for the binding of (anti)nuclei.

p-p CF,

$R=2.75 \pm 0.01$ fm; $\chi^2/\text{NDF} = 1.66$;

antiproton-antiproton CF,

$R=2.80 \pm 0.02$ fm, $f_0=7.41 \pm 0.19$ fm,

$d_0=2.14 \pm 0.27$ fm; $\chi^2/\text{NDF}=1.61$

Strange Baryon Correlations (including p-Ω)

Binding energy **E_{bin}** [MeV]

Scattering length **a₀** [fm]

Effective range **r_{eff}** [fm]

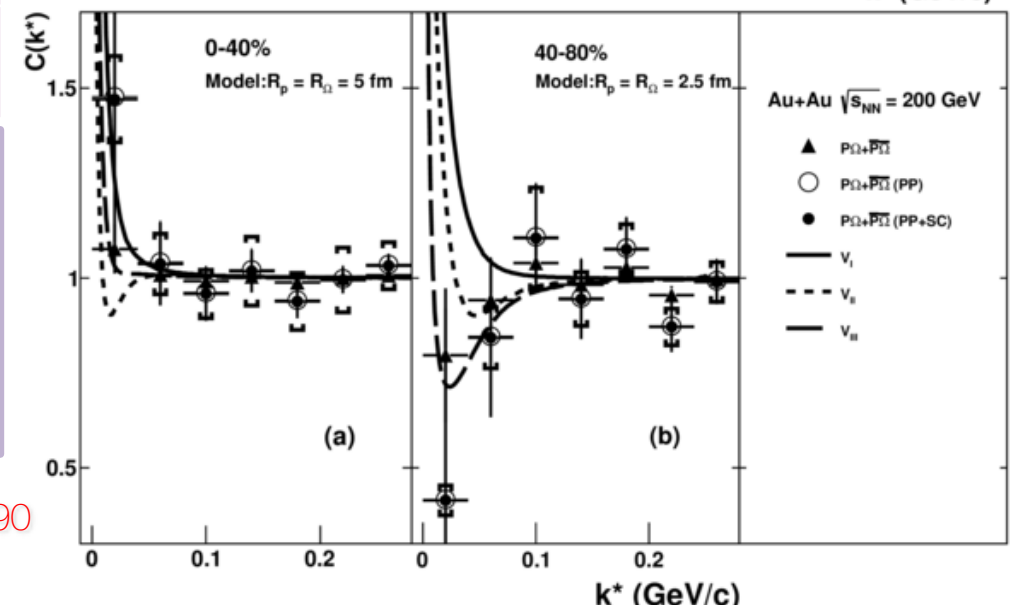
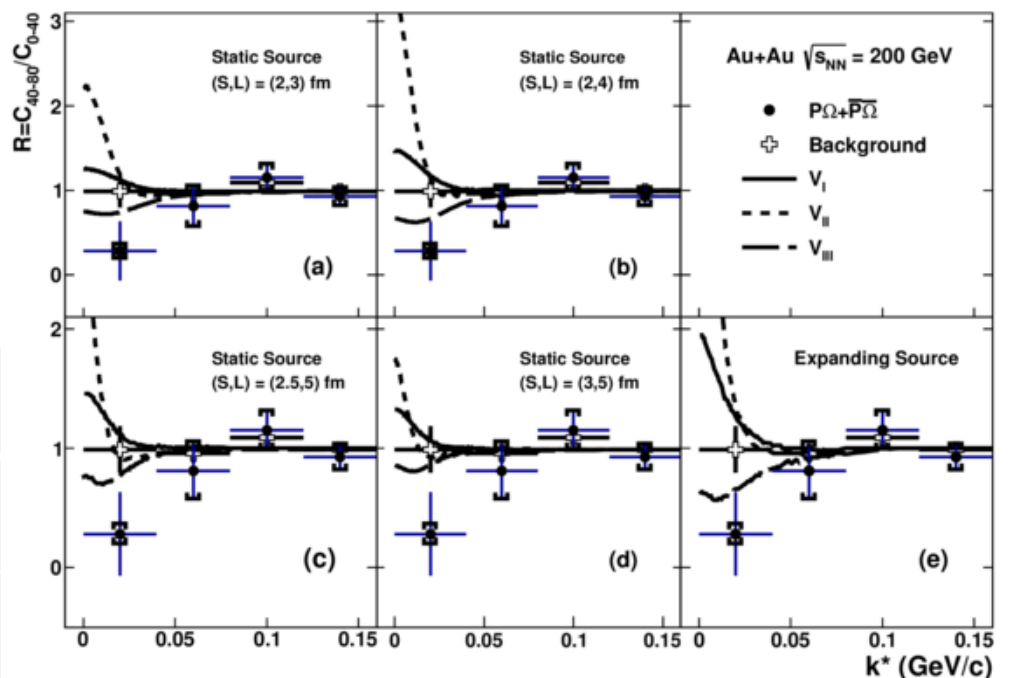
for 3 scenarios:

K. Morita et al. Phys. Rev. C 94, 031901 (2016)

	V ₁	V ₂	V ₃
E_{bin} [MeV]	-	6.3	26.9
a₀ [MeV]	-1.12	5.79	1.29
r_{eff} [MeV]	-1.16	0.96	0.65

A comparison of the measured correlation functions from Au+Au collisions with theoretical predictions

Scattering length is positive and favor pΩ bound state hypothesis





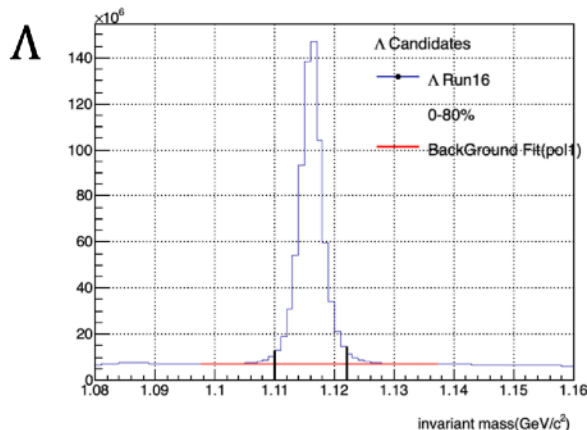
Reconstruction of Λ and Ξ

	Decay channel	Mass (from PDG 2018)
Λ (uds) $\bar{\Lambda}$	$\Lambda \rightarrow \pi^- + p$ $\bar{\Lambda} \rightarrow \pi^+ + \bar{p}$ (63.9%)	1.115683 (GeV/c^2)
Ξ (dss) $\bar{\Xi}$	$\Xi \rightarrow \Lambda + \pi^+$ $\bar{\Xi} \rightarrow \bar{\Lambda} + \pi^-$ (99.87%)	1.32171 (GeV/c^2)

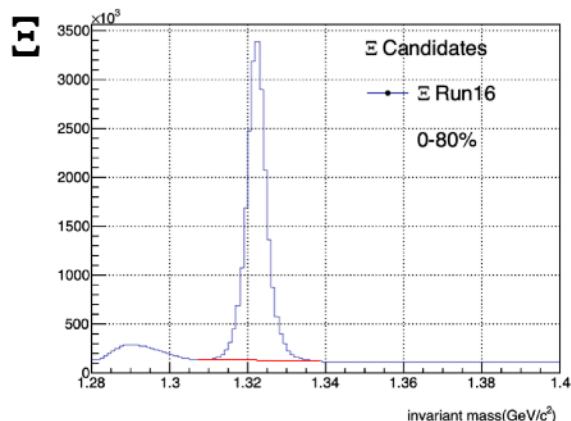
- KFParticle package was used.
KFParticle is based on Kalman filter.
- Very good Purity for Λ (~88%) and Ξ (~90%).

Daughter particle selection for Λ and Ξ

Invariant mass



2021/05/19



SQM 2021 Moe Isshiki

For pion

- $|n_{\sigma,\pi}| < 3$
- $-0.15 < \text{Mass}^2 < 0.15 (\text{GeV}/c^2)^2$

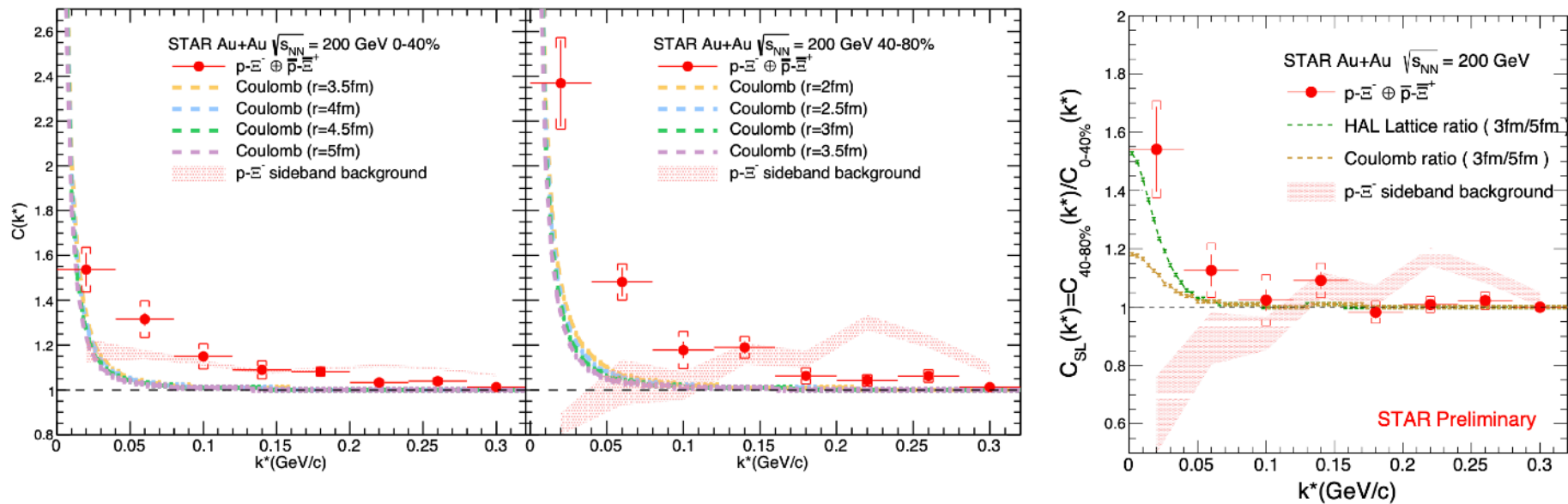
For proton

- $|n_{\sigma,p}| < 3$
- $0.5 < \text{Mass}^2 < 1.5 (\text{GeV}/c^2)^2$

For Λ and Ξ

- $p_T \geq 0.4 \text{ GeV}/c$
- $|y| < 1.0$

Studies of strong interactions



Strong and Coulomb

Final State Interactions.

$C(k^*)$ ratio of small to large systems,

$$C_{SL}(k^*) = \frac{C(k^*)_{40-80\%}}{C(k^*)_{0-40\%}}$$

$C_{SL}(k^*)$ is more sensitive to strong interaction with largely canceled Coulomb interaction[1].

- Below $k^* = 0.1$ GeV/c, the signal is enhanced beyond the Coulomb interaction and background.
- Similar to lattice QCD calculation [2] which suggests an attractive strong interaction between p and Ξ^- .

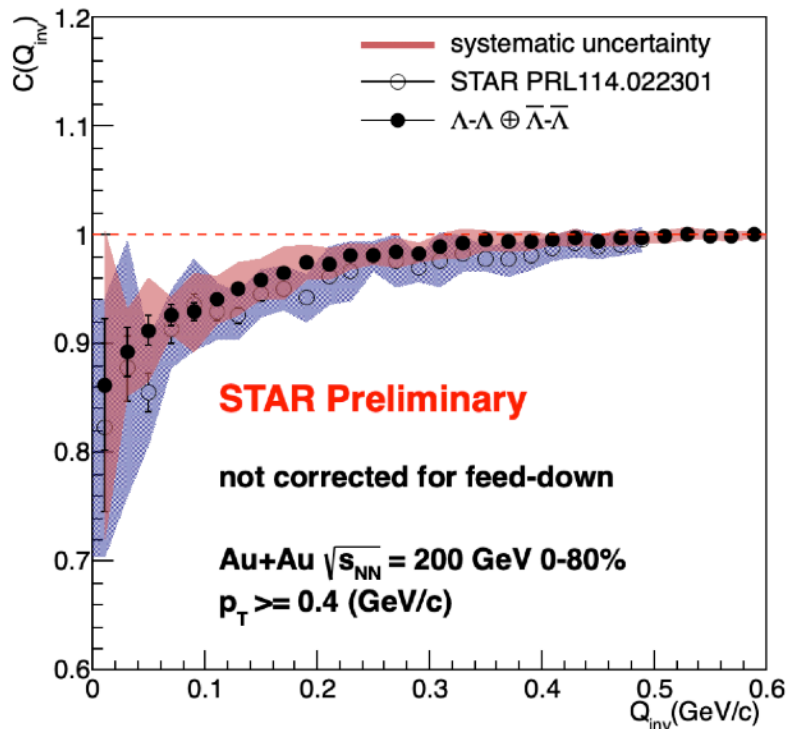
[1] K. Morita et al, Phys. Rev. C94(2016) 031901

[2] T.Hatsuda Nuclear Physics A 967 (2017) 856–859

Search for bound states?

Hyperon-Hyperon (Y-Y) and Hyperon-Nucleon (Y-N) interactions: important to study exotic hadronic states (e.g. H-dibaryon) and to understand the EoS of neutron stars.

Do bound state of Y-N and Y-Y ($S=-2$) exist ?



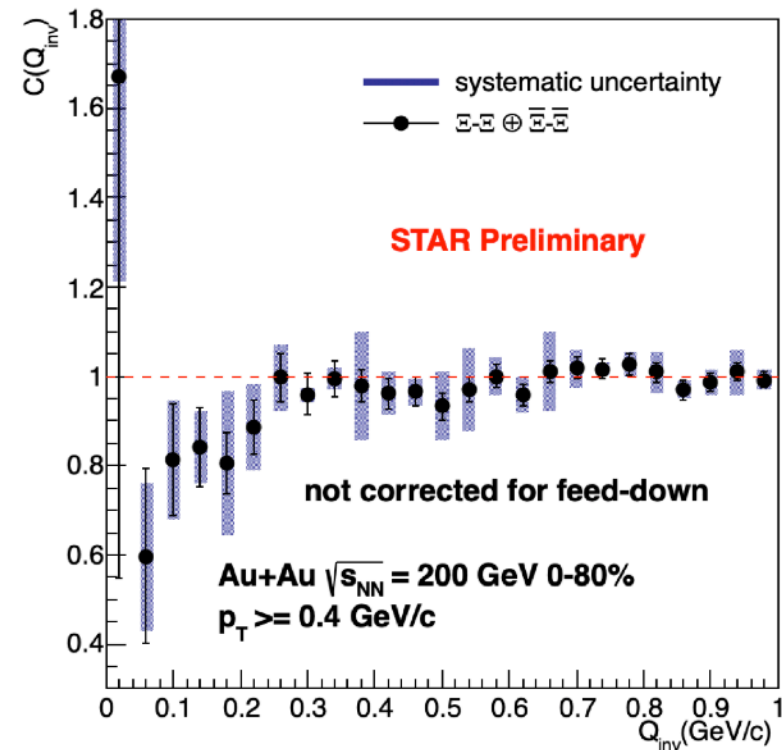
New high statistics data ~ 4 times larger than before

Not corrected for feed-down.

Anti-correlation seen

Possible to determine possible bound state

Search for bound states?



First measurement of $\Xi-\Xi$ correlation in Au+Au collisions.

Lattice QCD/chiral EFT calculations indicate an attractive interaction, but not strong enough to form a bound state [1,2].

The result shows anti-correlation at $2k^* < 0.25$ GeV/c.

Combination of quantum statistics, strong interaction, and Coulomb interaction.

[1] J. Haidenbauer et al., Eur. Phys. J. A 51: 17 (2015)

[2] T,Doi et al., EPJ Web Conf. 175 (2018) 05009

Feed-down and Coulomb effects need to be evaluated for further discussion.

More events will be taken in 2023 and 2025



Summary

Summary

- Femtoscopic source parameters determined for a wide range of collisions energy;
- Non-monotonic behavior of $R(\sqrt{s_{NN}})$ seen in three directions;
- New data for $\sqrt{s_{NN}} = 4.5$ GeV follow trend observed for low collision energies;
- Data for $\sqrt{s_{NN}} = 7.7$ GeV and higher collision energies indicated that the system evolves faster in the reaction plane;
- System created for $\sqrt{s_{NN}} = 4.5$ GeV is round-shaped ($R_{side} \simeq R_{long}$);
- Visible peaks in around $\sqrt{s_{NN}} \simeq 20$ GeV at R_{out}/R_{side} and $R_{out}^2 - R_{side}^2$ consistent with prediction of QGP transition threshold;
- vHLEE + UrQMD verifies sensitivity of HBT measurements to changes in EOS;
- A clear energy dependence of source sizes for particles combinations other than pions;
- A clear signal of emission asymmetry between nonidentical particle combinations;
- Heavier particles directed towards the edge of the source or freeze-out earlier.

Studies of strong interactions possible

Thank you for Your attention



Backup slides