

Probing the parton shower with multi-differential jet substructure measurements in pp collisions at STAR

Youqi Song (youqi.song@yale.edu)

for the STAR Collaboration

BOOST 2023, Berkeley, CA

8/2/2023

Supported in part by



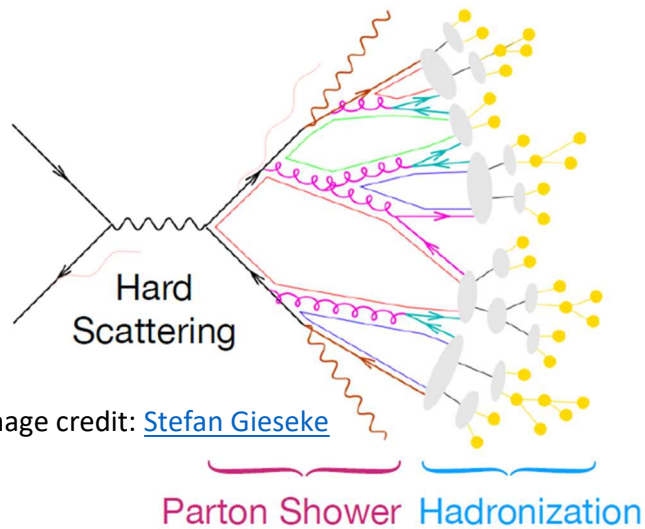
U.S. DEPARTMENT OF
ENERGY

Office of
Science

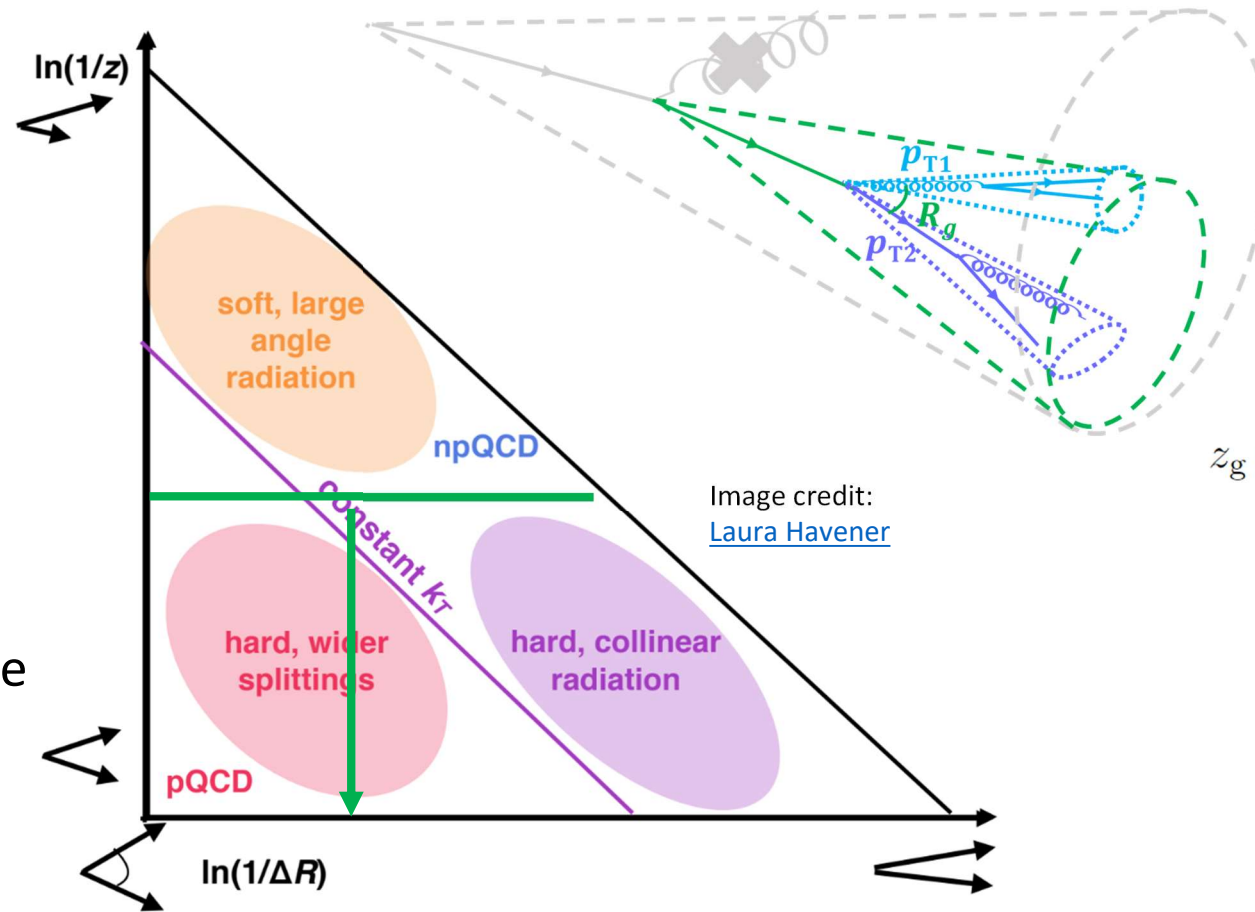


Jets and SoftDrop grooming

Jet is a multi-scale object



To enhance perturbative contributions, SoftDrop grooming is often used to remove soft wide-angle radiation



Larkoski, et al. JHEP 05 (2014) 146.
Dasgupta et al. JHEP 09 (2012) 29.

$$z_g = \frac{\min(p_{T,1}, p_{T,2})}{p_{T,1} + p_{T,2}} > z_{\text{cut}} (R_g / R_{\text{jet}})^\beta$$

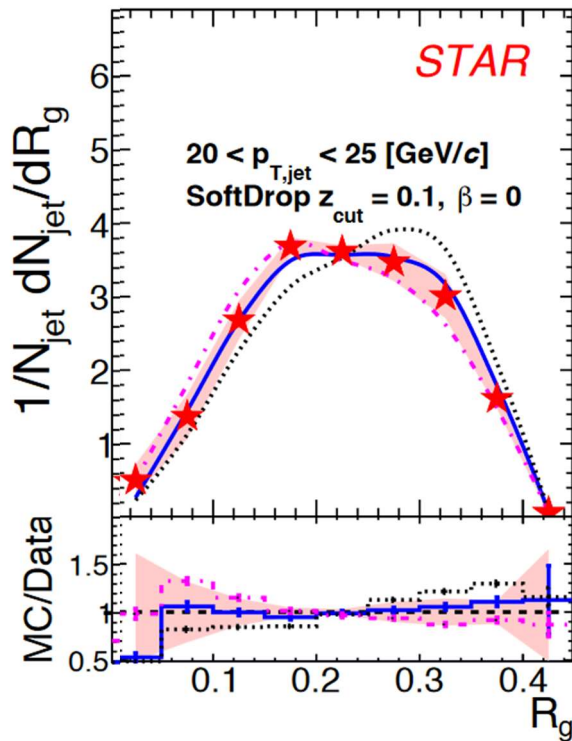
Image credit:
[Laura Havener](#)

The Lund Plane

Jets and SoftDrop grooming

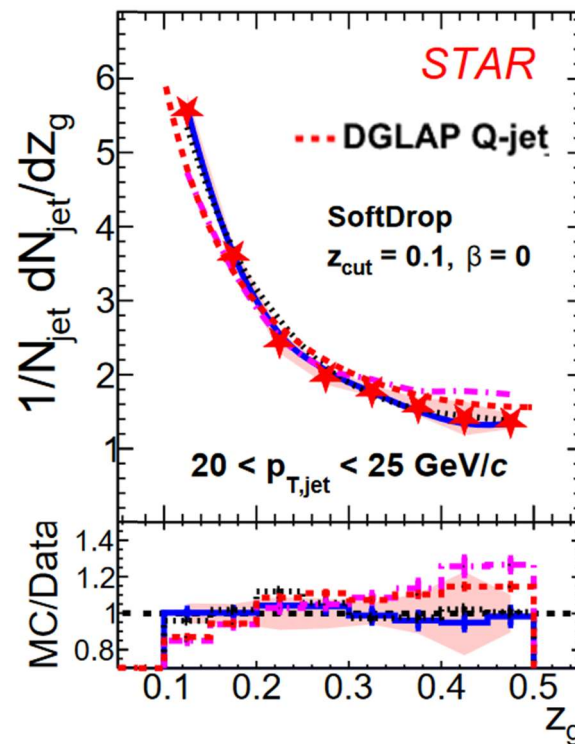
- STAR has measured SoftDrop jet substructures

R_g

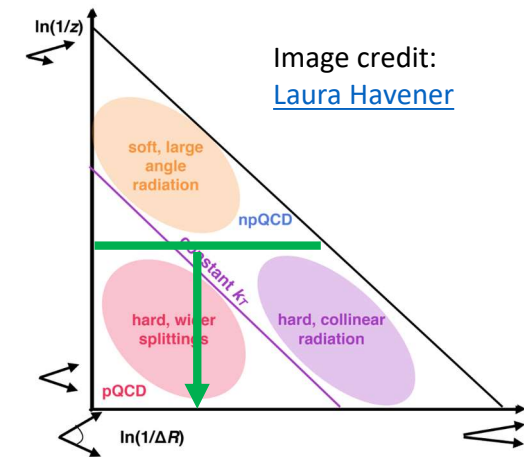
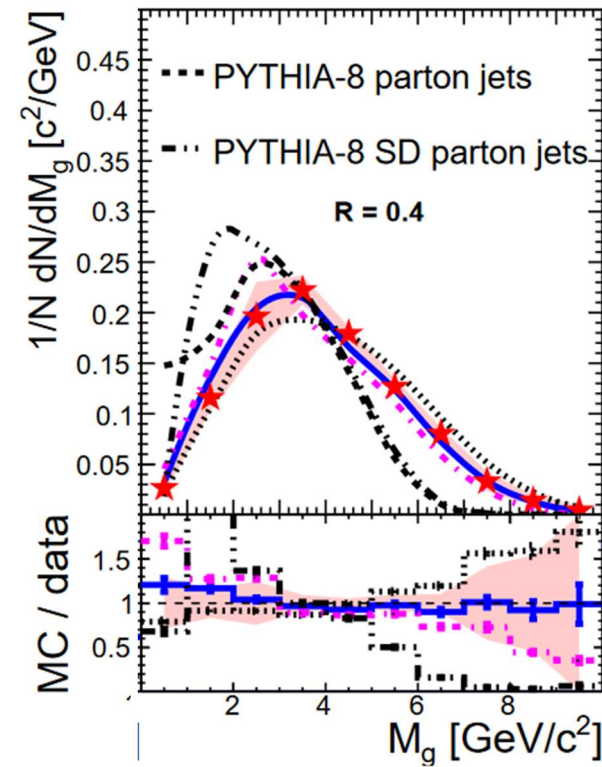


STAR. PLB 811 (2020) 135846, STAR. PRD 104, 052007(2021)

Z_g

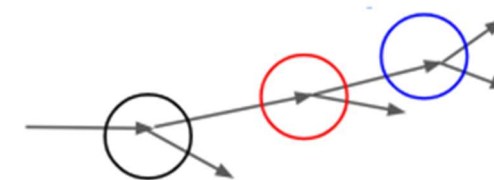
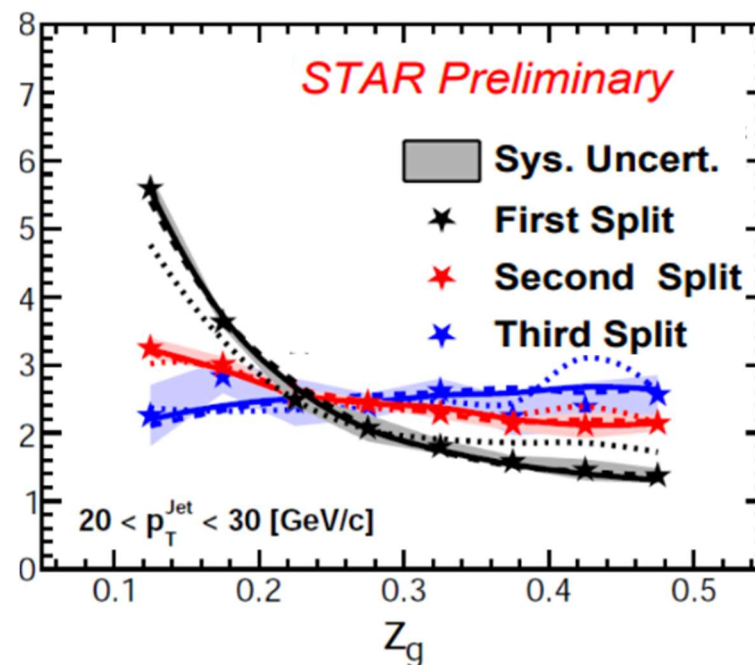
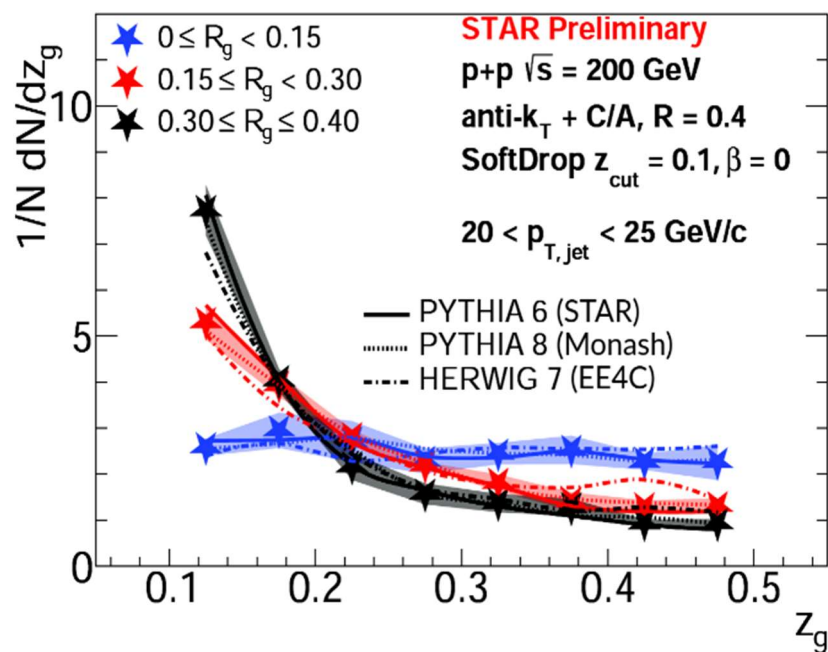


M_g

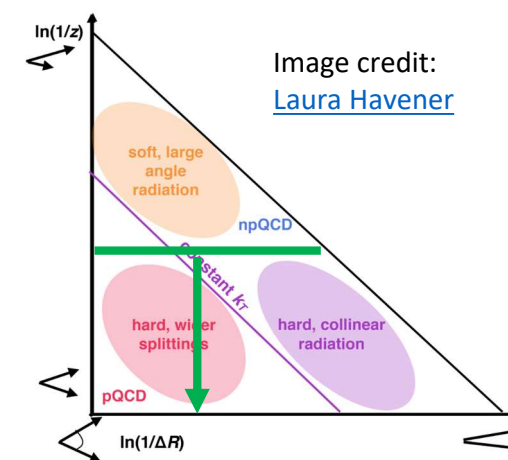


Jets and SoftDrop grooming

- STAR has measured SoftDrop jet substructures ... and in a multi-dimensional fashion!



→ study dynamics of the parton shower!



CollinearDrop grooming: probes the soft component

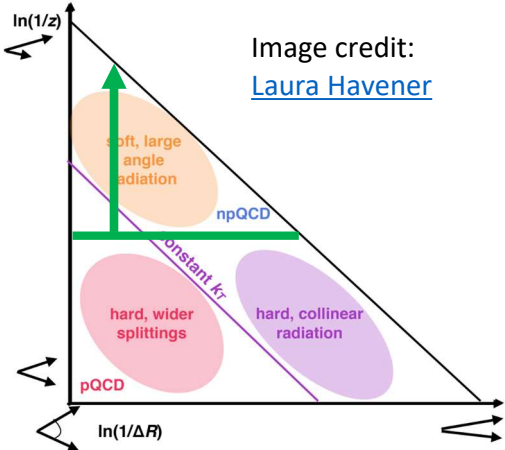
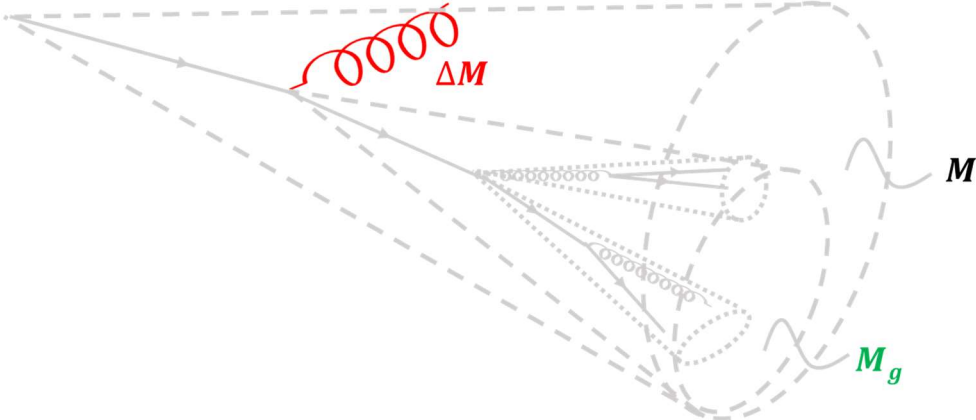
Chien and Stewart JHEP 06 (2020) 64.

- General case: difference of an observable with two different SoftDrop selections $(z_{cut 1}, \beta_1)$ and $(z_{cut 2}, \beta_2)$
- For this analysis, $(z_{cut 1}, \beta_1) = (0,0)$ and $(z_{cut 2}, \beta_2) = (0.1,0)$: difference in the original and SoftDrop groomed observable

• Observables: e.g.,
$$\Delta M/M = \frac{M - M_g}{M}$$

where
$$M = |\sum_{i \in \text{jet}} p_i| = \sqrt{E^2 - |\vec{p}|^2}$$

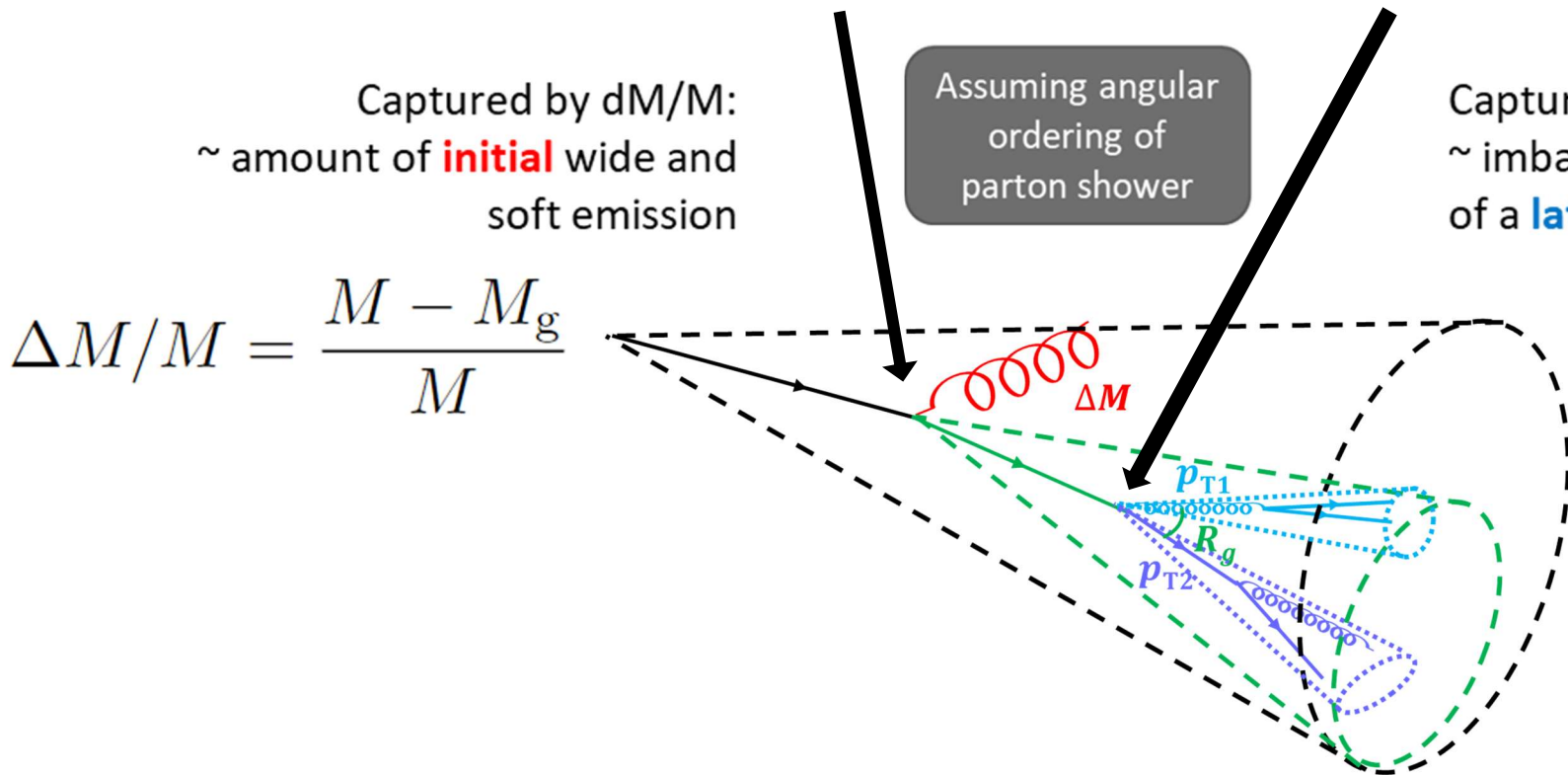
soft and wide-angle radiation:
interesting region of phase space
that deserves more study!



CollinearDrop vs SoftDrop correlation:

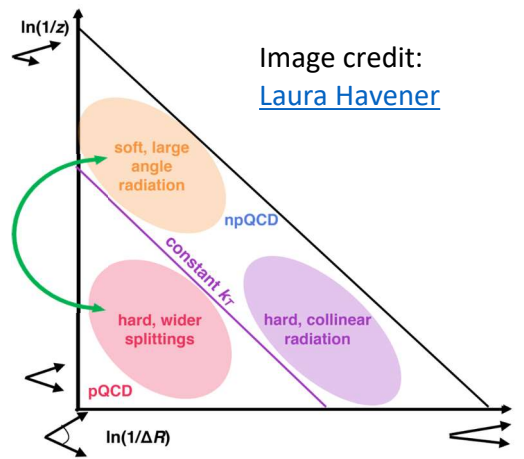
probes the soft-hard correlation

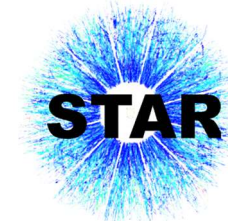
- How does the amount of soft radiation correlate with the angular and momentum scale of a hard splitting? → how an **early** emission affects a **later** splitting



$$\Delta M/M = \frac{M - M_g}{M}$$

Note: Hadronization effects smear the distribution but don't affect the correlations (see backup)





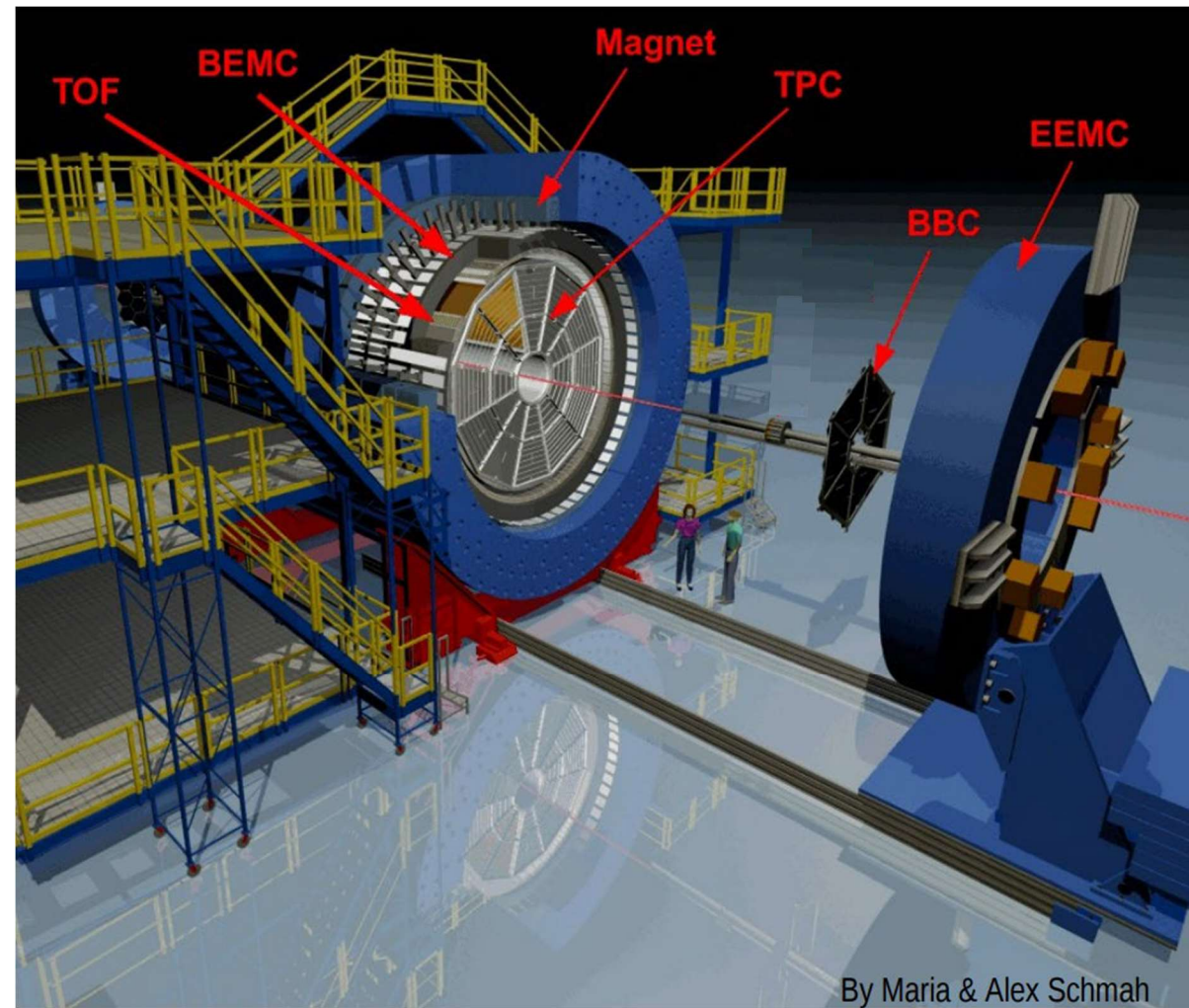
Jet reconstruction at STAR

Important subdetectors for **200 GeV pp** collisions data-taking during 2012 RHIC run

- **TPC** (Time Projection Chamber)
 - For **charged** particle track reconstruction
 - $|\eta| < 1$, full azimuthal coverage
- **BEMC** (Barrel ElectroMagnetic Calorimeter)
 - For **neutral** energy measurement and triggering
 - $|\eta| < 1$, full azimuthal coverage
- Reconstruct anti- k_T **full jets**
 - Jet resolution parameter **R=0.4**
 - $|\eta_{jet}| < 0.6$

Additional selections

- Tracks (Towers): $0.2 < p_T(E_T) < 30$ GeV/c
- Jets
 - $p_T > 15$ GeV/c, $M > 1$ GeV/c²
 - Passes SoftDrop with $z_{cut} = 0.1$ and $\beta = 0$



By Maria & Alex Schmah



Unfolding method

- Jet measurements need to be corrected for detector effects for comparison with theory/model
- Unfolding methods:
 - Iterative Bayesian unfolding ([D'Agostini. arXiv:1010.0632\(2010\)](#))
 - **MultiFold** ([Andreassen et al. PRL 124, 182001 \(2020\)](#))
 - Machine learning driven
 - Unbinned
 - **Simultaneously** unfolds many observables
→ **Correlation** information is retained!
- First application of MultiFold on RHIC data!

- Jet observables
 - p_T : transverse momentum
 - $Q^\kappa = \frac{1}{(p_{Tjet})^\kappa} \sum_{i \in jet} q_i \cdot (p_{Ti})^\kappa$
 - $M = |\sum_{i \in jet} p_i| = \sqrt{E^2 - |\vec{p}|^2}$
 - R_g : groomed jet radius
 - z_g : shared momentum fraction

$$z_g = \frac{\min(p_{T,1}, p_{T,2})}{p_{T,1} + p_{T,2}} > z_{cut} (R_g/R_{jet})^\beta$$

- M_g : groomed jet mass

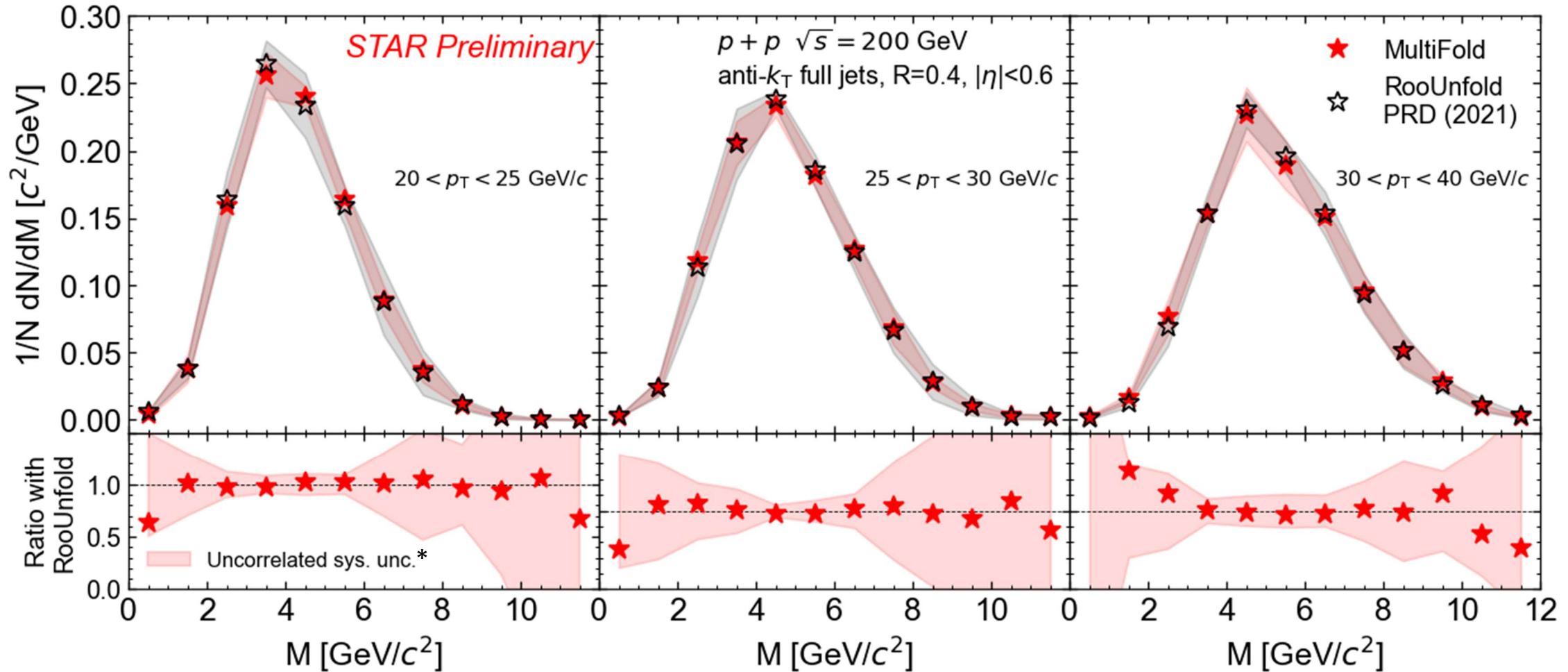
All 6 observables are simultaneously unfolded in an unbinned way!

- Uncertainties due to prior choice accounted for through 6D reweighting based on PYTHIA8 or HERWIG (see backup)

Does MultiFold work on our data?

$$M = \left| \sum_{i \in \text{jet}} p_i \right| = \sqrt{E^2 - |\vec{p}|^2}$$

MultiFolded result agrees with **RooUnfolded** result ([STAR Collaboration. PRD 104, 052007\(2021\)](#)) [HEPData](#)

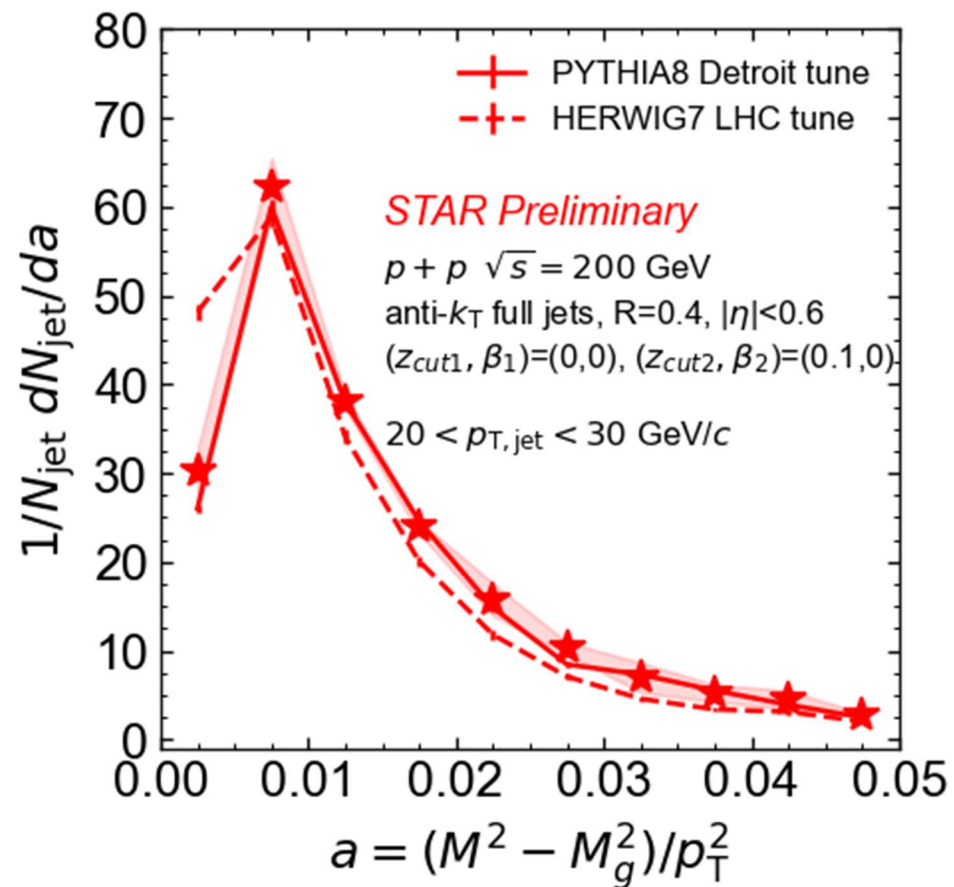
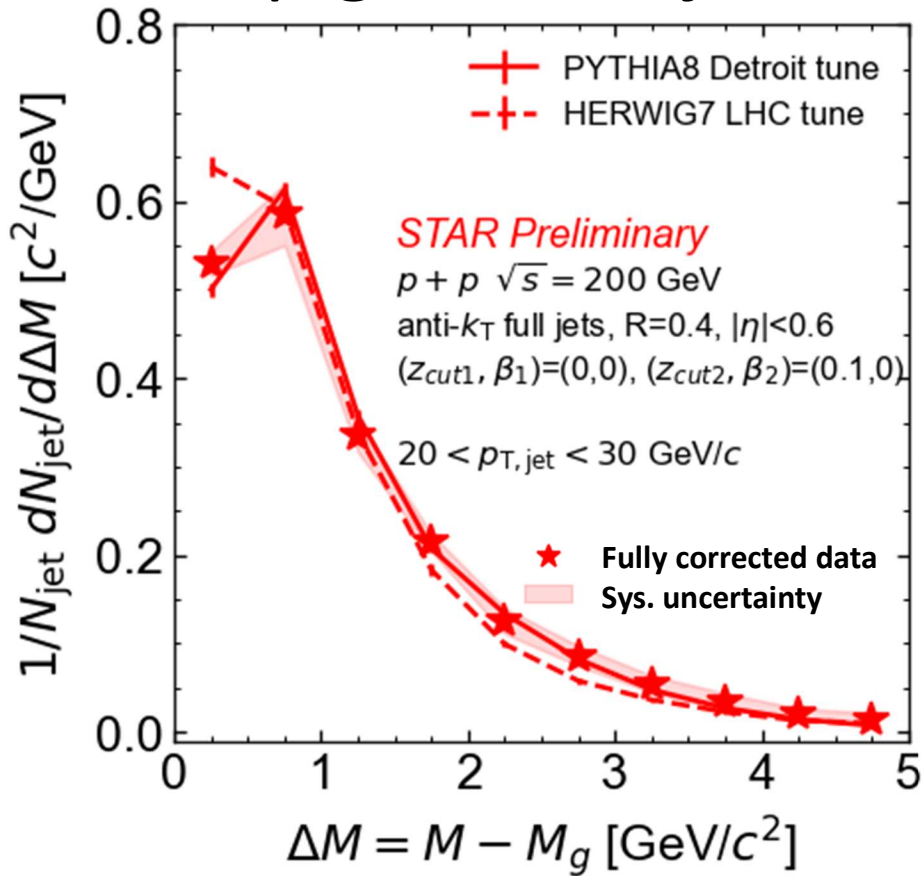


... but **MultiFold** also gives us high-dimensional correlation between observables!

* 2D reweighting used for prior variation, to be consistent with RooUnfolded measurement



CollinearDrop groomed jet mass

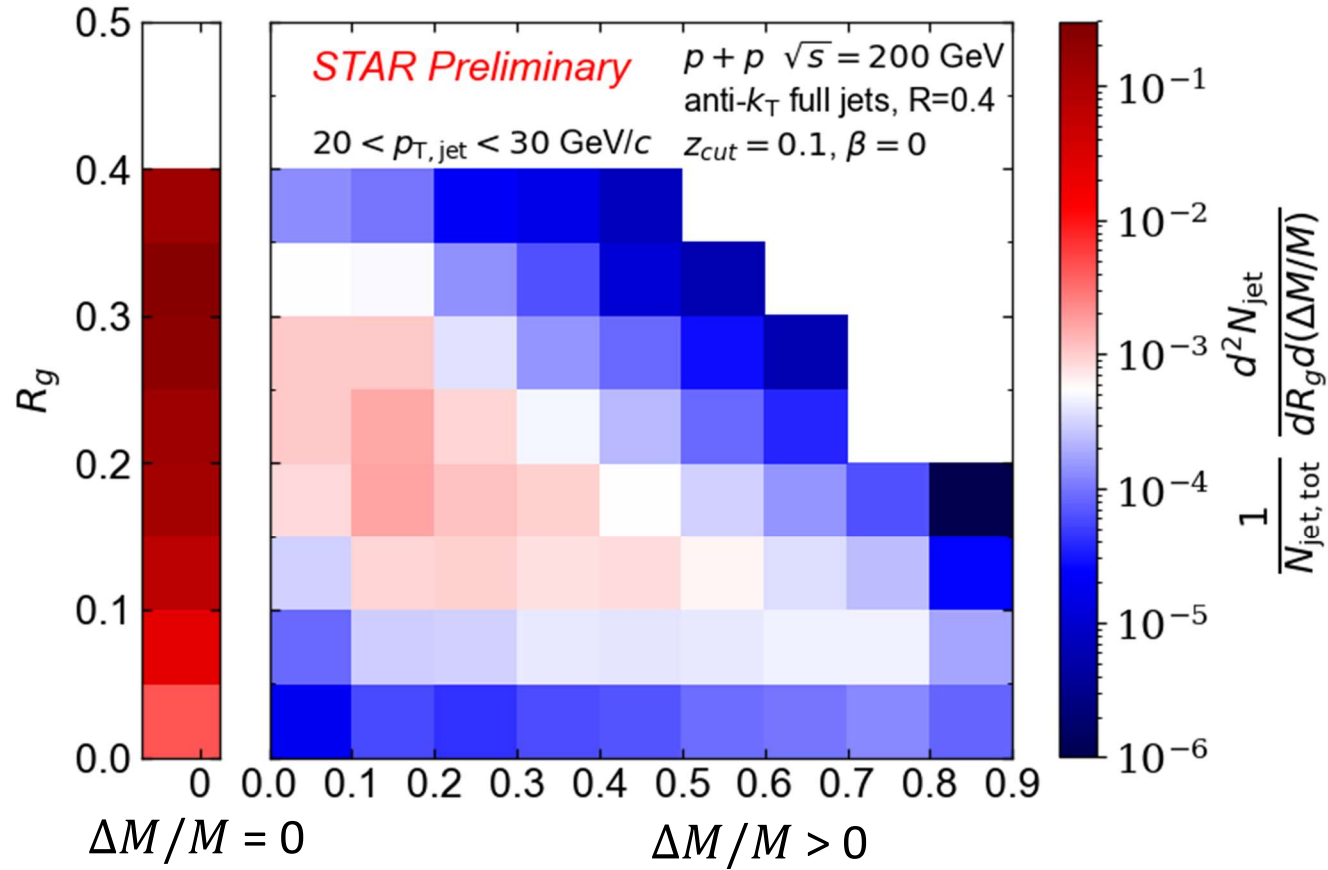


PYTHIA6 Perugia + STAR tune: Skands, PRD 82, 074018 (2010)
 J. K. Adkins, PhD thesis (Kentucky U., 2015)
 PYTHIA8 Detroit tune: Aguilar et al. PRD 105, 016011(2022)
 HERWIG7: Bellm, et al. PRC 76, 1-8 (2016)

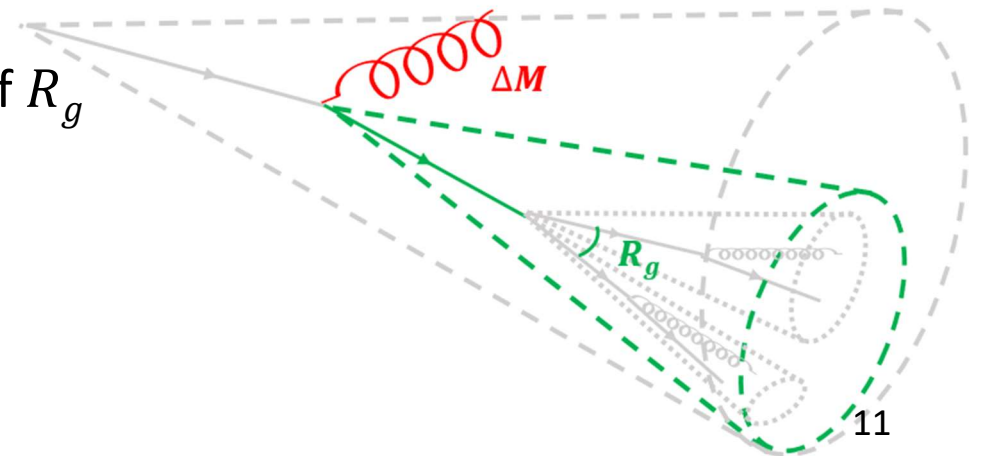
Measurement excludes jets with $\Delta M = 0$ (45.5% of jets in this jet p_T range)

- First CollinearDrop groomed jet measurement, sensitive to soft radiation within jets
- MC predictions qualitatively consistent with data; some tension from HERWIG7 in small ΔM region
- MultiFold allows us to correlate (combinations of) unfolded quantities

Soft radiation vs hard splitting angle

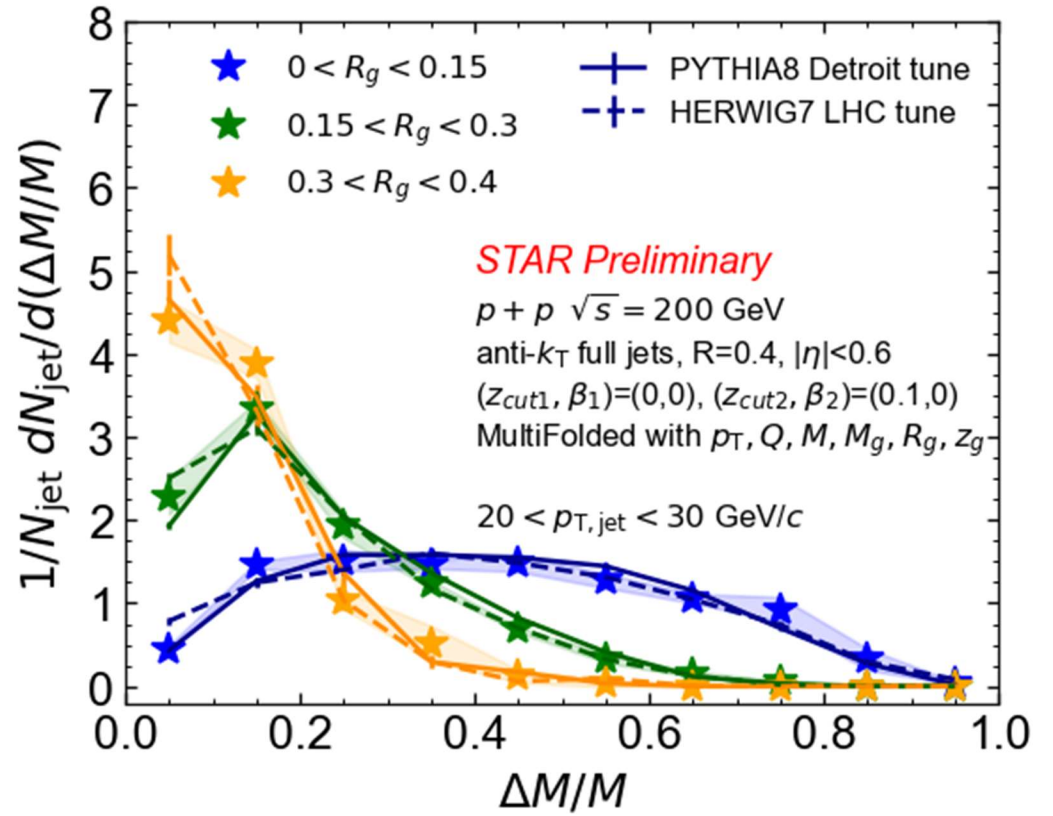
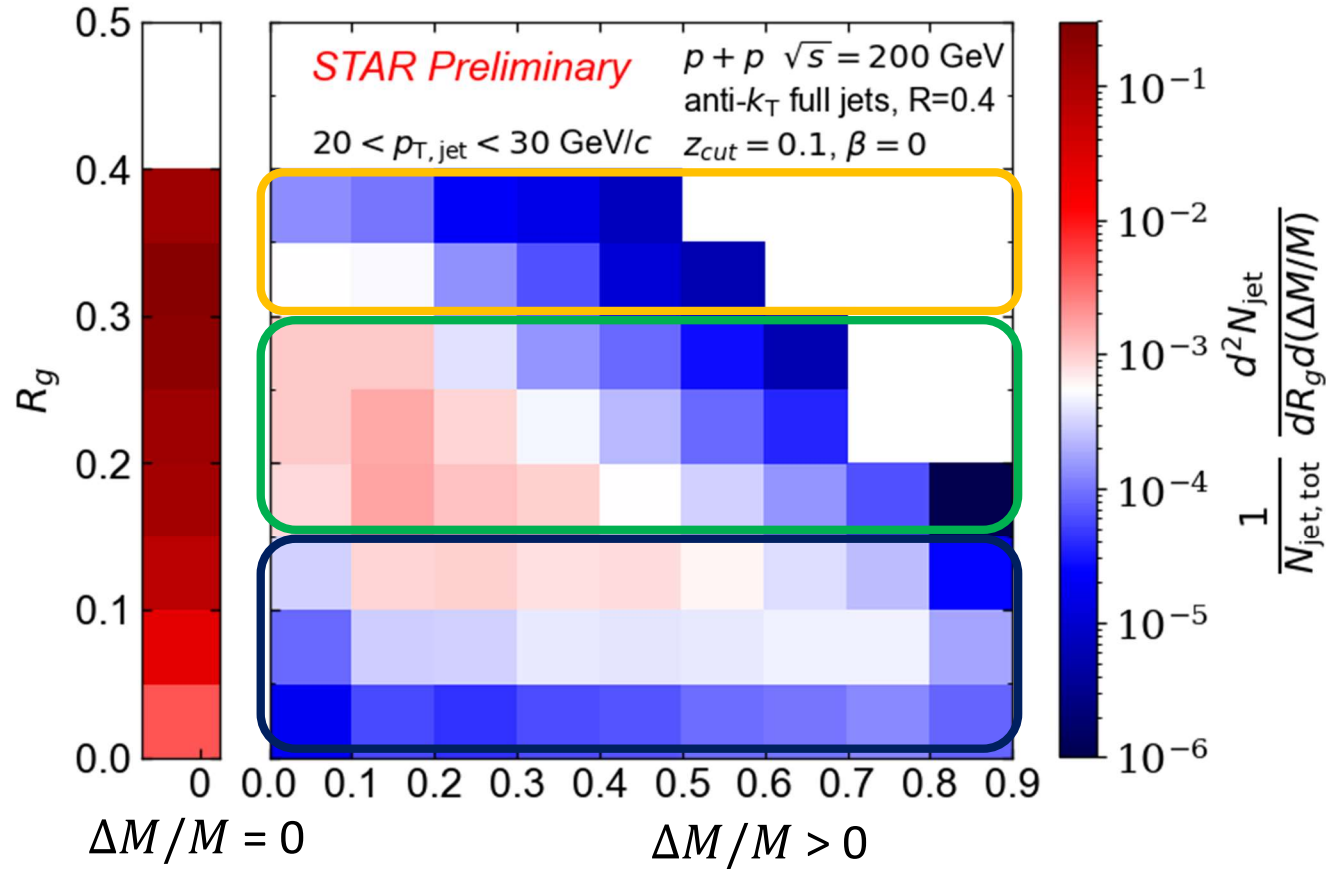


- The mean of $\Delta M/M$ distribution is anti-correlated with mean of R_g
 → consistent with angular ordered parton showers

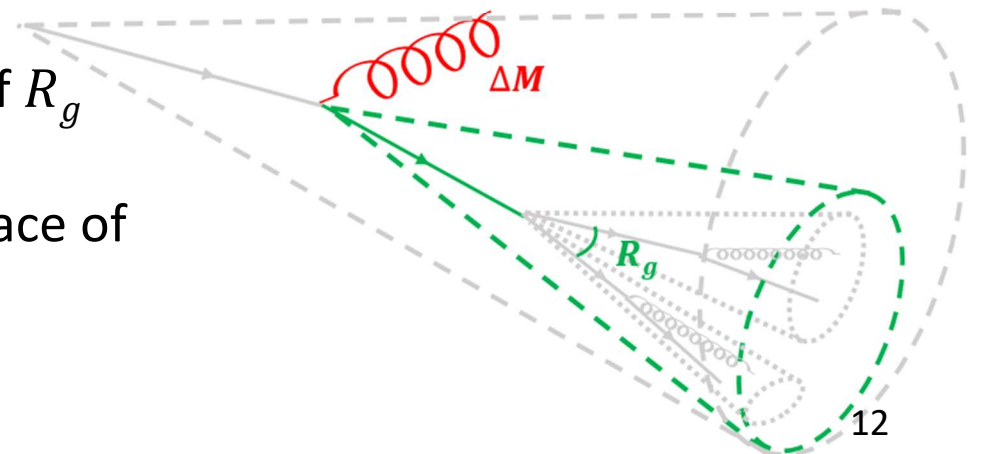




Soft radiation vs hard splitting angle



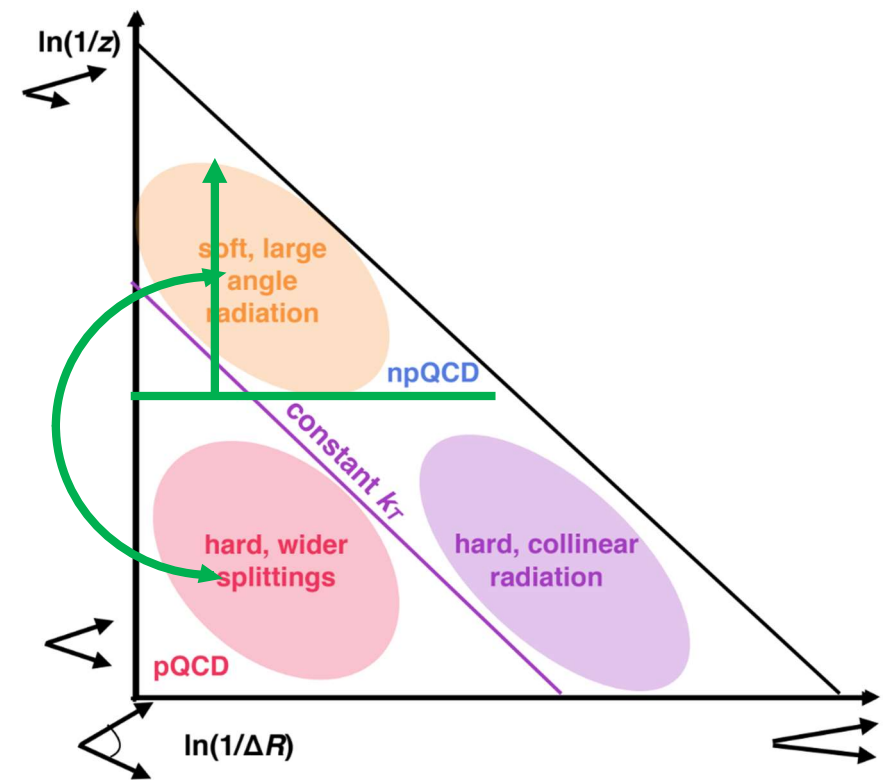
- The mean of $\Delta M/M$ distribution is anti-correlated with mean of R_g
 → consistent with angular ordered parton showers
- **Early** soft wide-angle radiation constrains the angular phase space of **later** splittings
- MC models describe the trend of data



Summary

- Probing **soft** wide-angle radiation within jets
 - Fully corrected CollinearDrop jet measurement is presented
- Probing **soft-hard** correlation within jets
 - MultiFold allows for access of multi-dimensional correlations on a jet-by-jet basis. First application to RHIC data!
 - Jets with a more asymmetric splitting are more likely to have small **early-stage radiation**
 - Anti-correlation between the amount of **early-stage radiation** and the angular scale of a **later-stage splitting** is observed

Improve understanding of jet substructure and the correlations between different substructure observables!





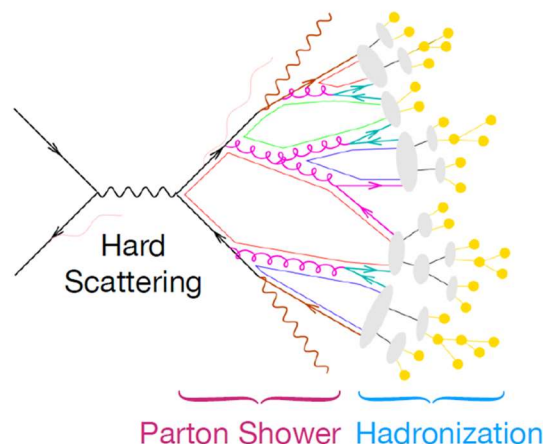
What's next?

- Study hadronization with jet substructure by measuring r_c

$$r_c(X) = \frac{d\sigma_{h_1 h_2}/dX - d\sigma_{h_1 \bar{h}_2}/dX}{d\sigma_{h_1 h_2}/dX + d\sigma_{h_1 \bar{h}_2}/dX}$$

Chien et al. PRD 105
051502 (2022)

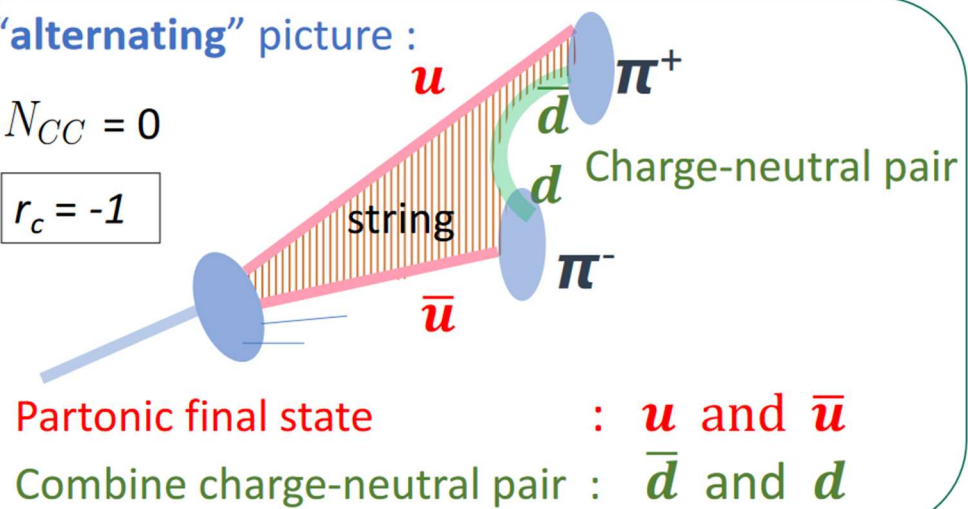
- $h_1 h_2$: same charge tracks, $h_1 \bar{h}_2$: opposite charge tracks



“alternating” picture :

$$N_{CC} = 0$$

$$r_c = -1$$



“random” picture :

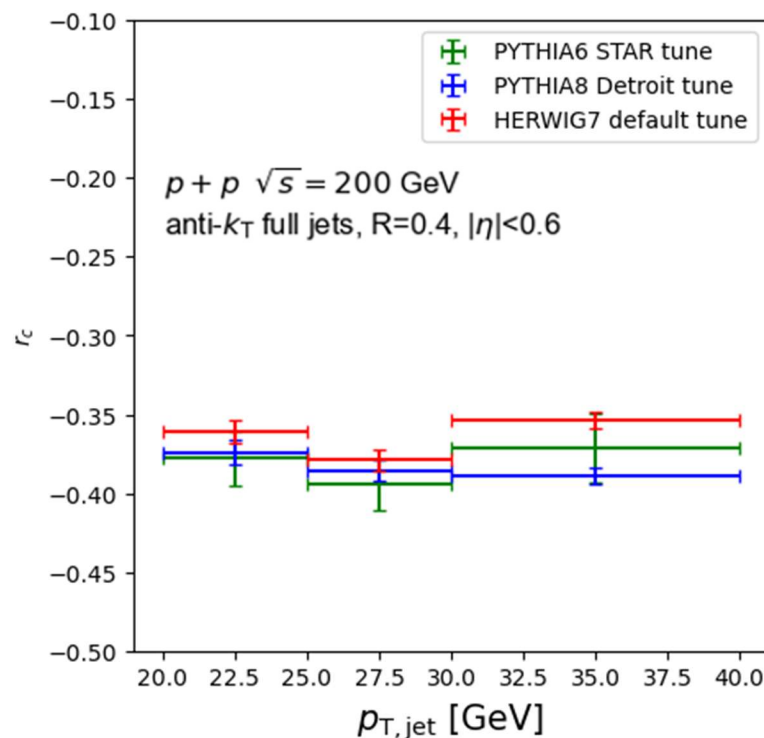
no charge correlation

$$N_{CC} = N_{CC\bar{}}$$

$$r_c = 0$$

r_c is a measure of the fraction of “string-like hadronization”

Mondal DIS 2022



BOOST, 08/02/2023

- To be validated with STAR data!



What's next?

- Correct for detector effects for r_c ?

Problem: pi0s (and other neutral hadrons) decay at the detector-level;

Example:

jet at truth level

pi+ 6 GeV
pi0 4 GeV
pi- 3 GeV
pi- 1 GeV

jet at detector level

track(+) 6 GeV
track(-) 3 GeV
neutral 2 GeV
neutral 2 GeV
track(-) 1 GeV

leading/subleading is neutral
→ don't consider this jet

leading/subleading are both charged
→ include this jet for analysis
→ mistagged jet (shouldn't include this jet for analysis, but cannot identify it from data)

- How should we account for the neutral background?
- Is a "charged jet" measurement meaningful?
- Discussions are welcomed!

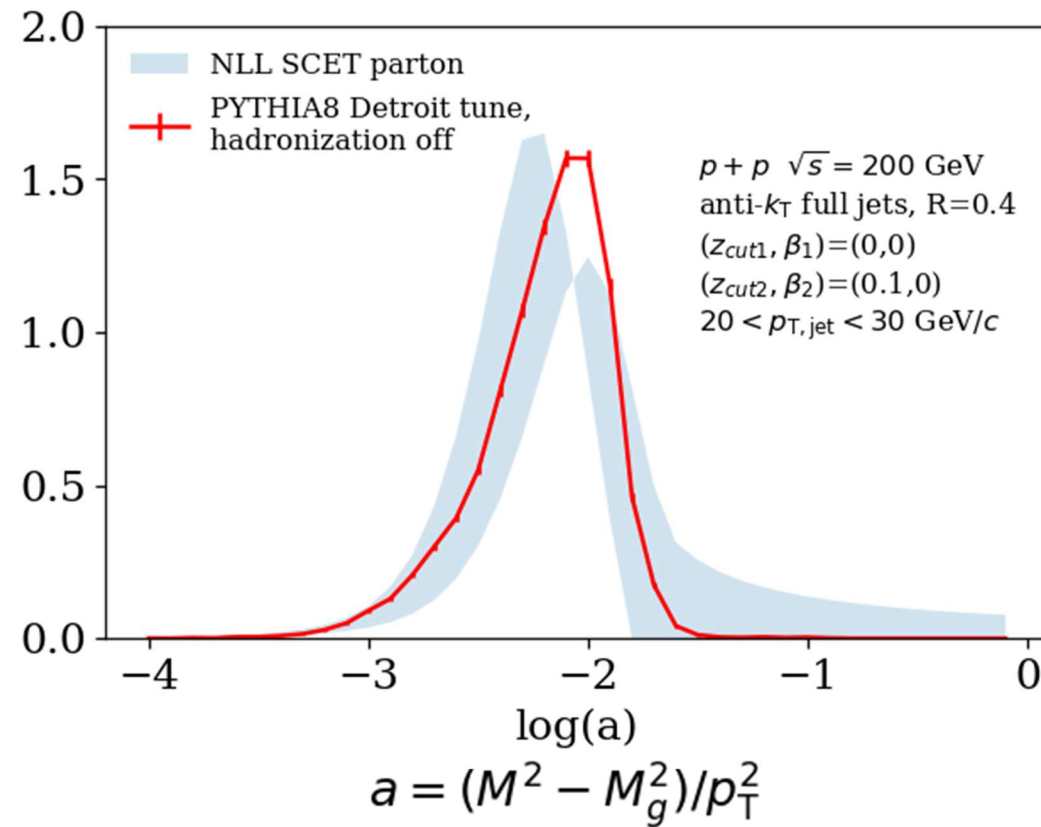


Jets at RHIC are great for the study of parton shower
... and have an enhanced sensitivity for non-perturbative
effects like hadronization!

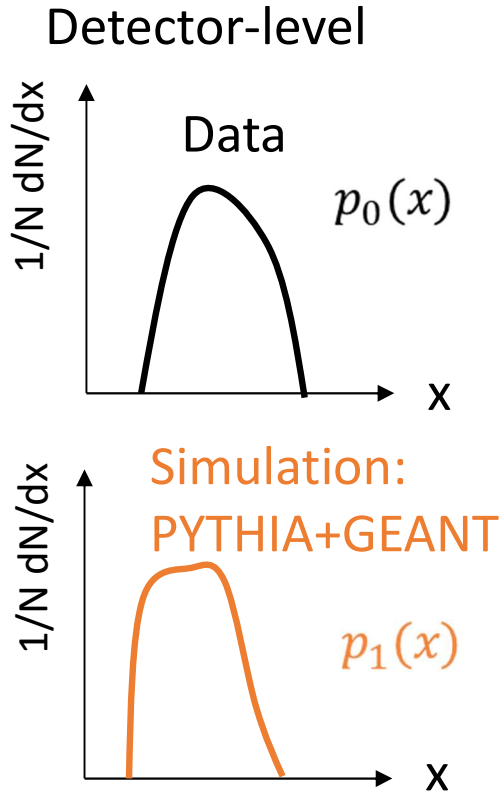
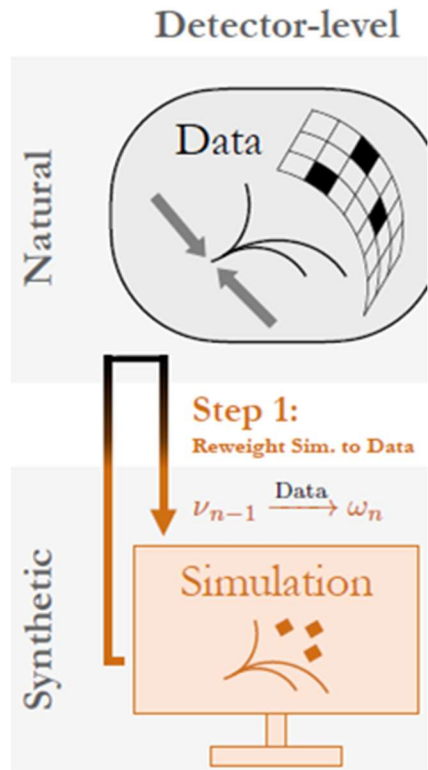
Backup

CollinearDrop groomed jet mass

- Theoretical calculation (next-to-leading log precision, using SCET calculational framework, and not including hadronization) agrees with PYTHIA8



Method: machine learning



E.g., Iteration 1, step 1:

Weights: $w(x) = p_0(x)/p_1(x)$

Ok for 1D

$$\approx f(x)/(1 - f(x))$$

[\(Andreassen and Nachman PRD 101, 091901 \(2020\)\)](#)

where $f(x)$ is a neural network and trained with the binary cross-entropy loss function

to distinguish jets coming from data vs from simulation

Unfolding \rightarrow Reweighting histograms \rightarrow Classification \rightarrow Neural network

Where does the machine learning part come in?



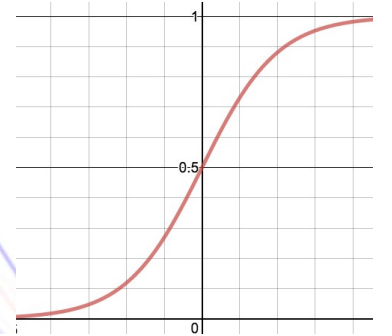
Method: machine learning

- Architecture: Dense neural network
- Activation function for dense layers: Rectified linear unit
- Activation function for output layer: Sigmoid
- Loss function: Binary cross entropy

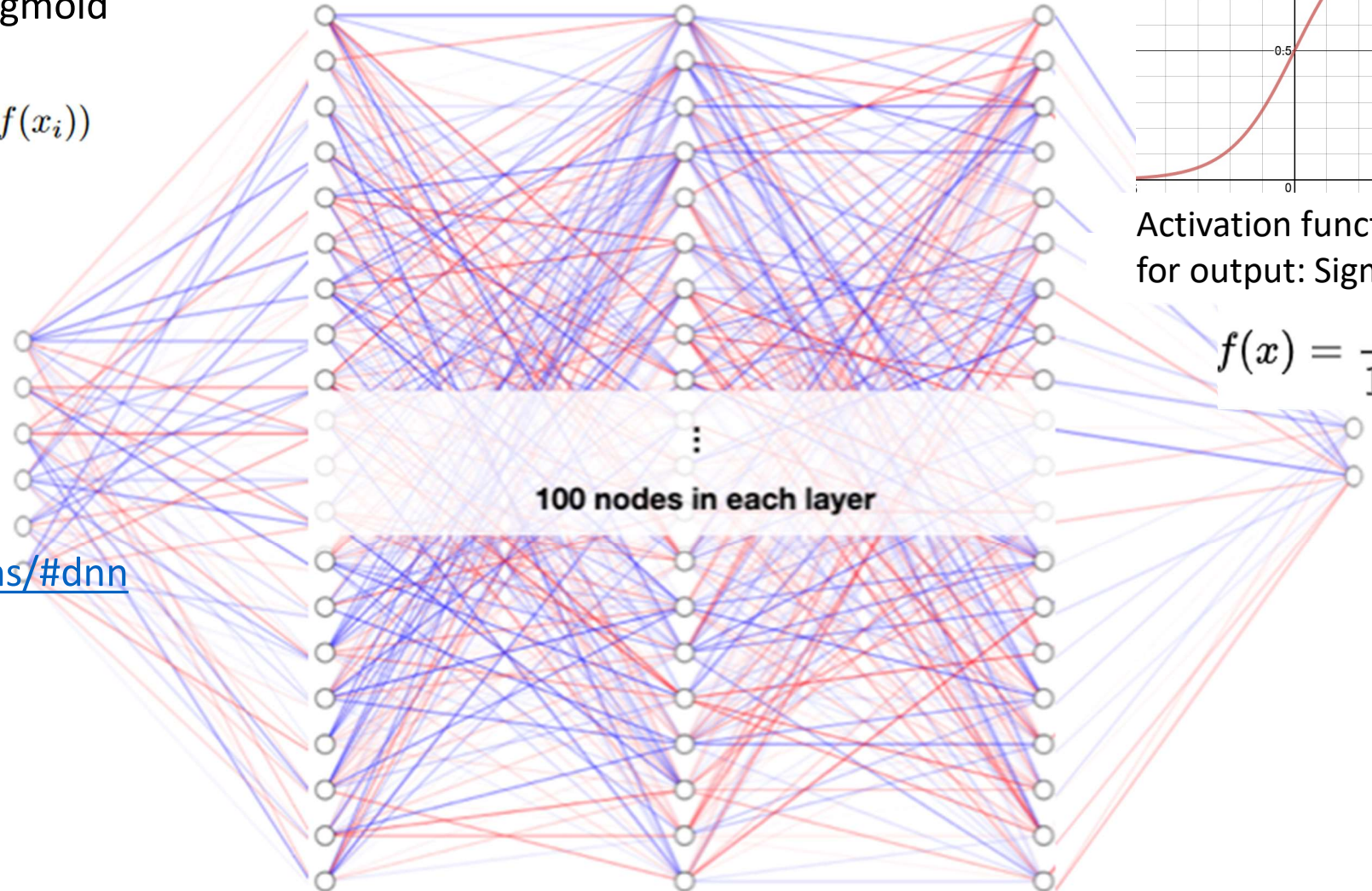
$$\text{loss}(f(x)) = - \sum_{i \in 0} \log f(x_i) - \sum_{i \in 1} \log(1 - f(x_i))$$

- Optimization algorithm: Adam
<https://arxiv.org/pdf/1412.6980.pdf>
- Nodes per dense layer: [100,100,100]
- Output dimension: 2
- Input dimension: 6
- All hyperparameters are default:
<https://energyflow.network/docs/archs/#dnn>

Activation function for dense layers: Rectified linear unit
 $f(x) = x^+ = \max(0, x)$



Activation function for output: Sigmoid
 $f(x) = \frac{1}{1 + e^{-x}}$



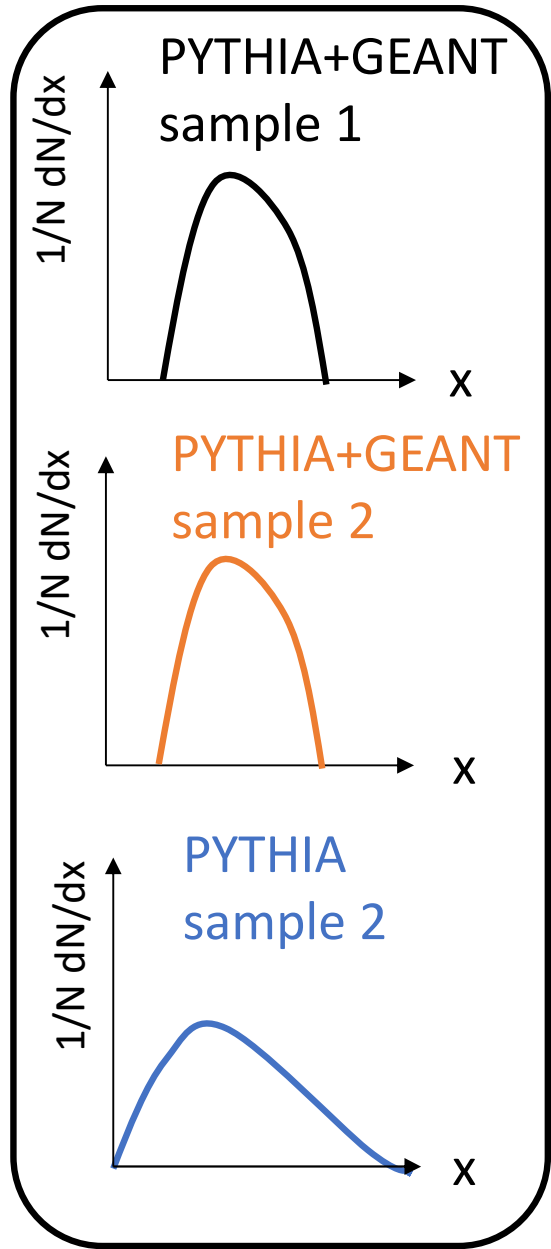
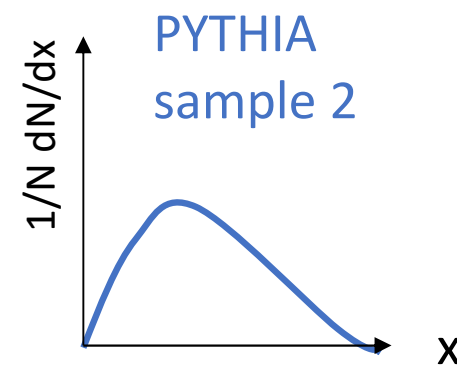
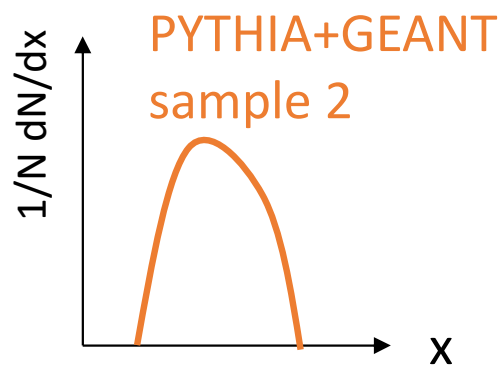
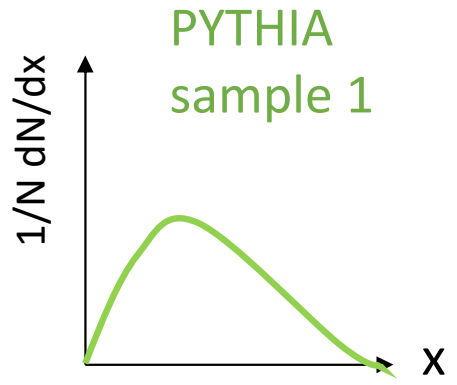
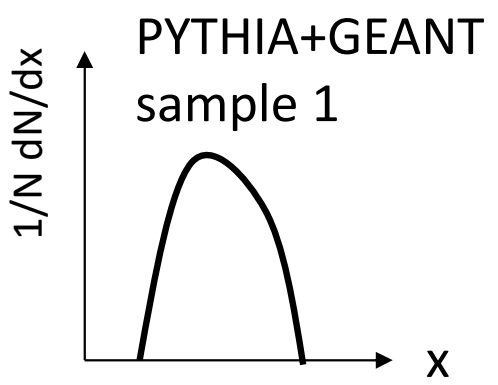


Closure test for unfolding

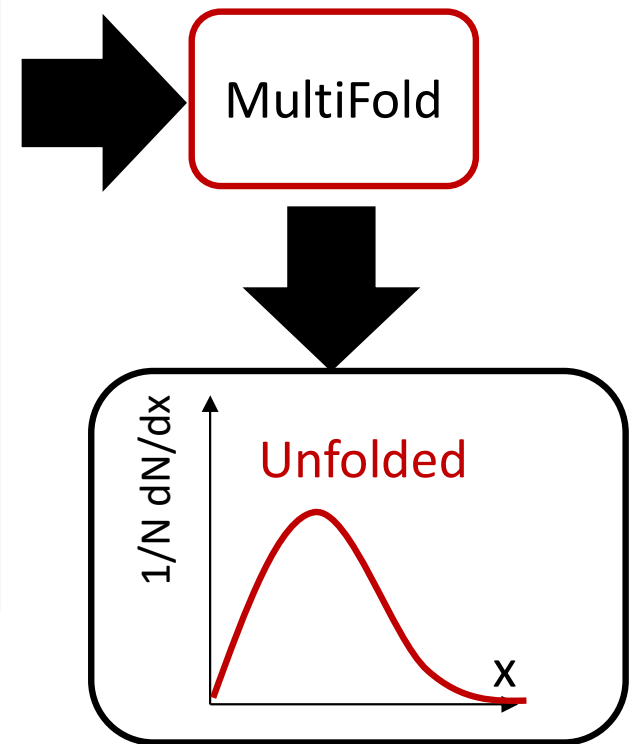
- Step 1: Separate matched jets from PYTHIA and PYTHIA+GEANT into 2 samples

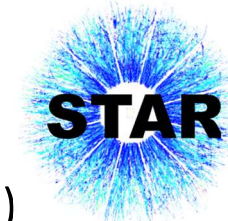
Detector-level

Particle-level



- Step 2: Unfold

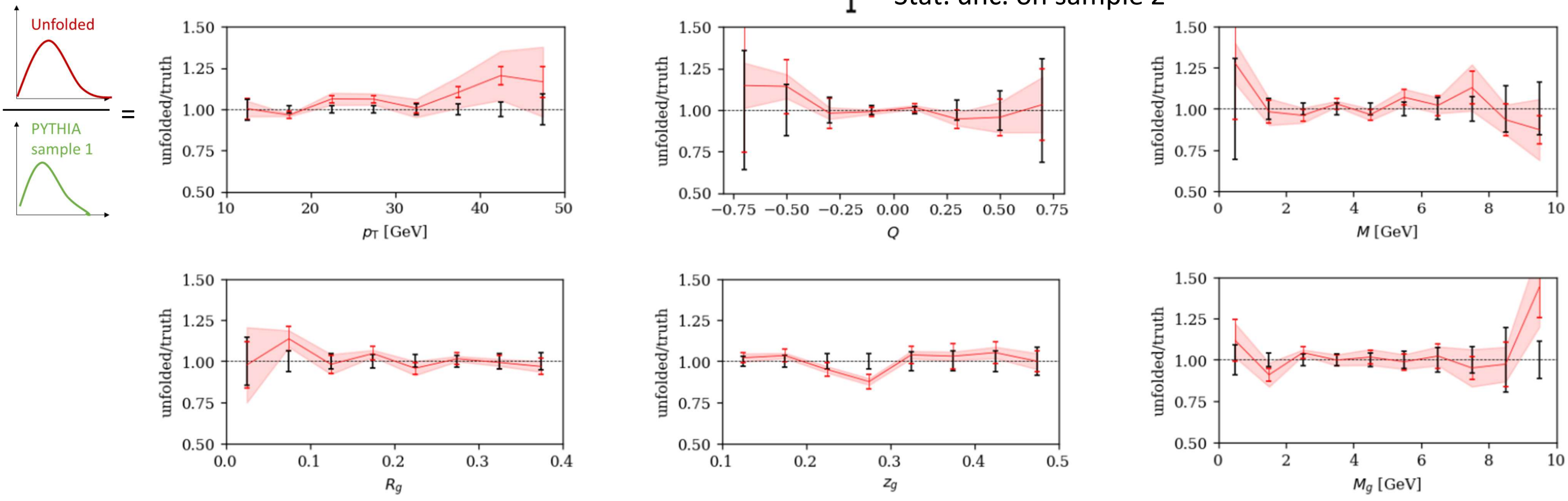




Closure test for unfolding

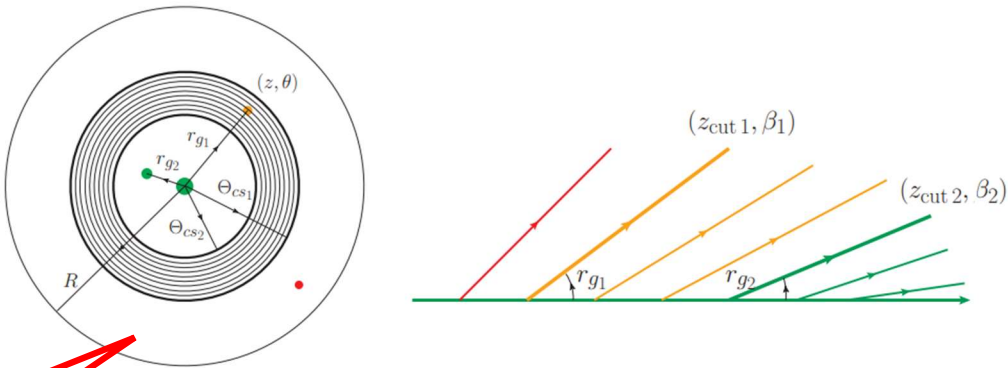
- Decent **closure** for all substructure observables

Unfolding unc. on data (not including misses)
Stat. unc. on sample 1
Stat. unc. on sample 2



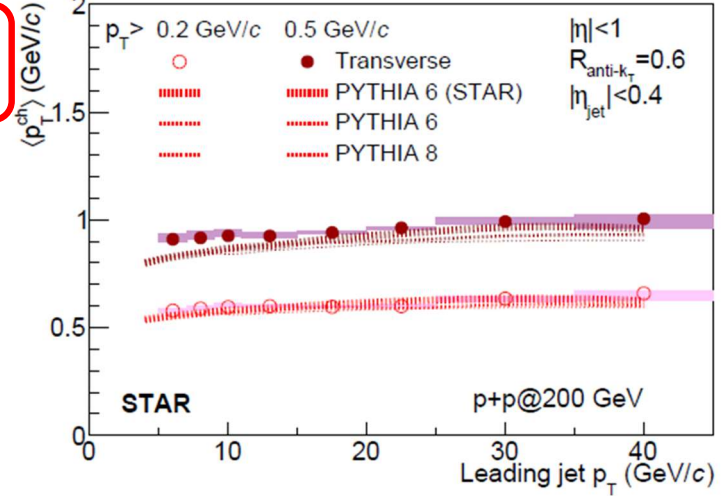
* 2D reweighting used for prior variation

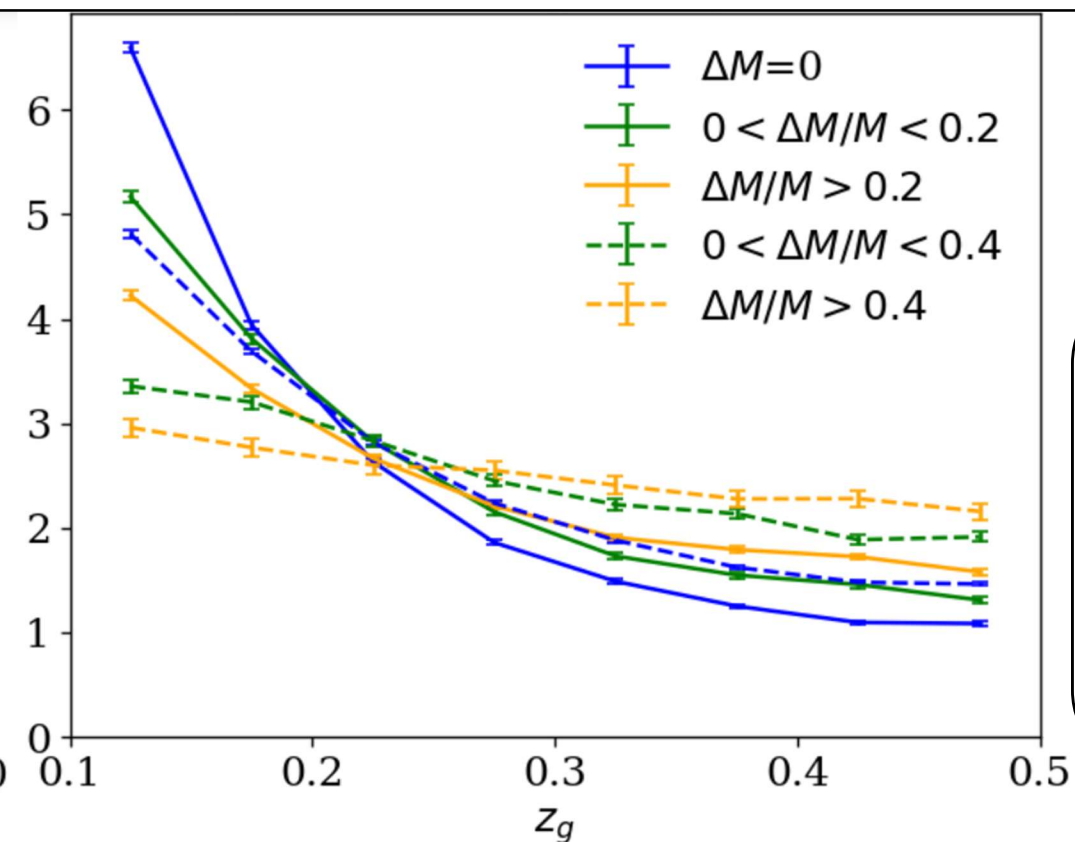
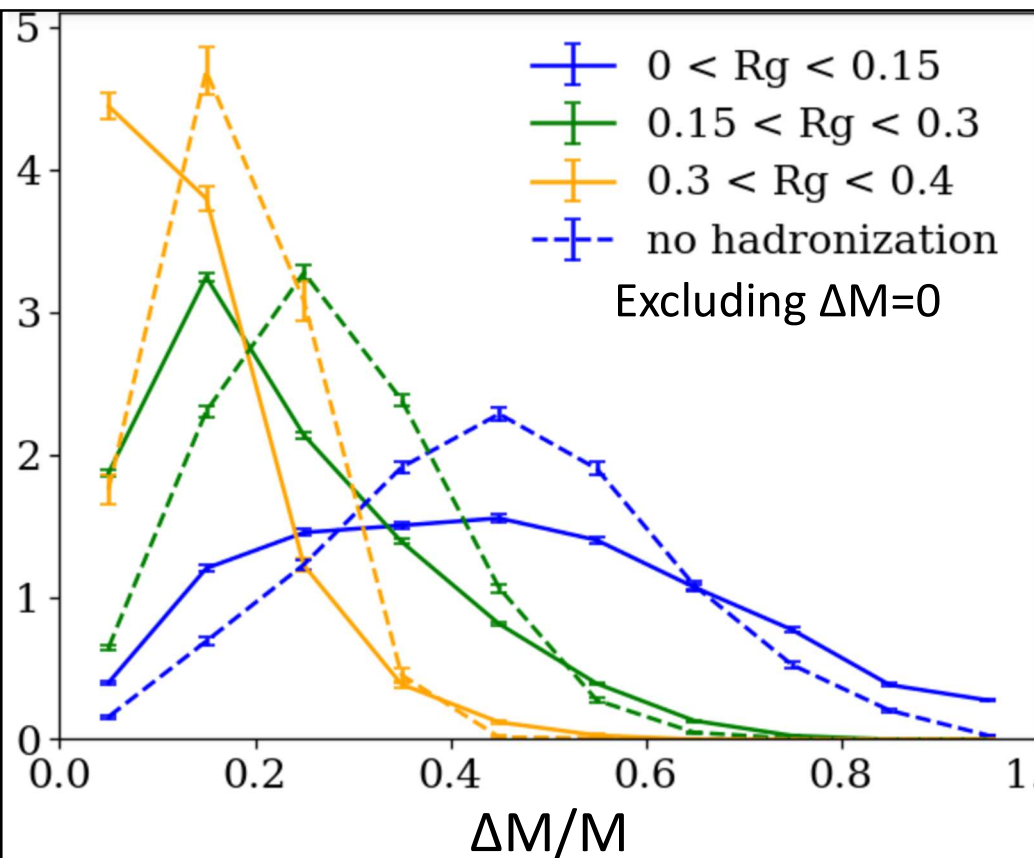
Underlying event



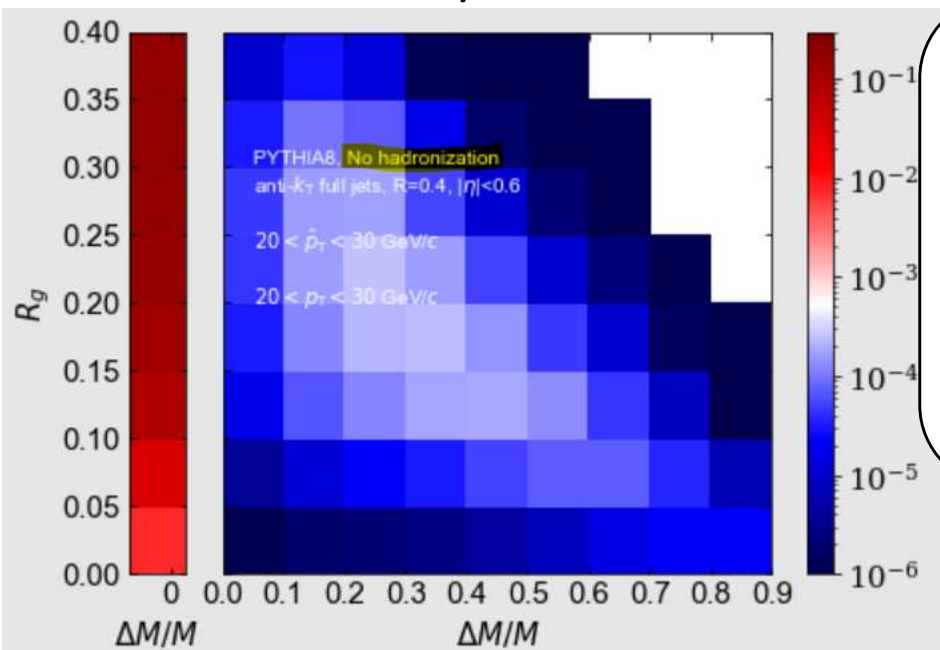
Remove underlying effects and pileup, not necessary for 200 GeV collisions

STAR Collaboration. PRD 101, 052004(2020)



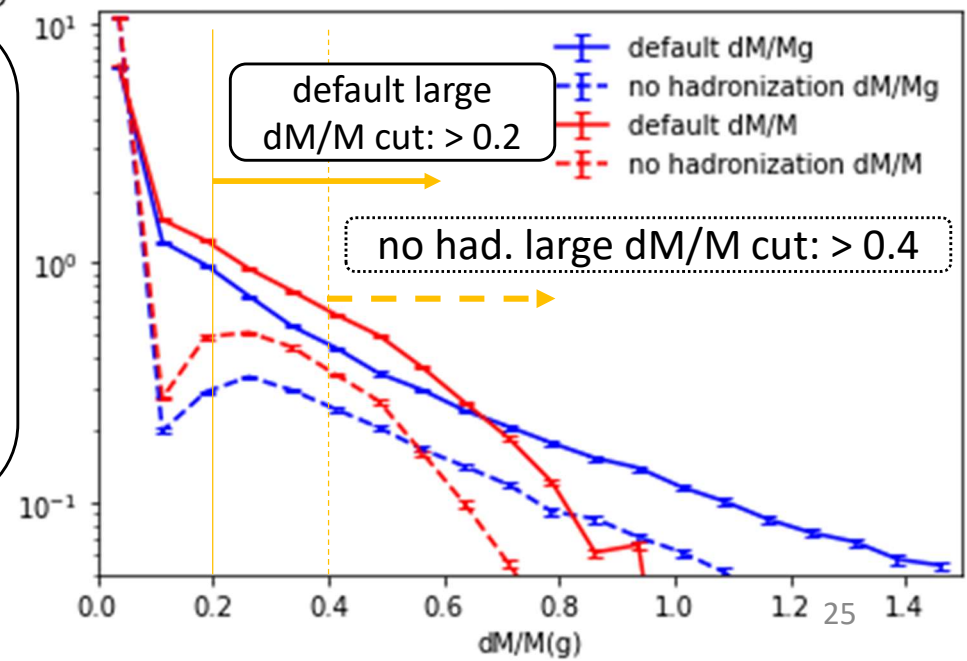


PYTHIA8 Detroit tune
 $20 < p_{T,jet} < 30$ GeV



Hadronization effects study:
Hadronization smears/shifts the distributions, but the correlation with and without hadronization is the same.

Youqi Song

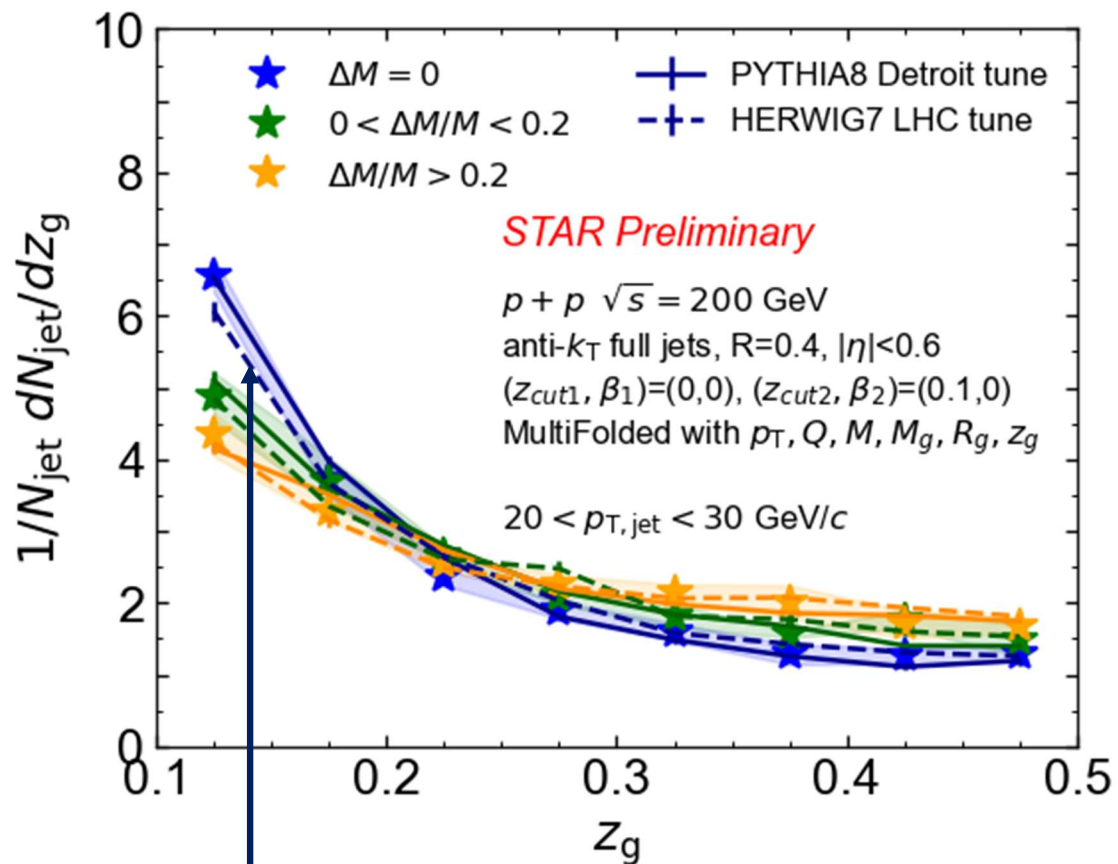




- Among truth jets with $20 < p_T < 30$ GeV, 44% of PYTHIA6 jets, 48% of PYTHIA8 jets, and 43% of HERWIG jets have $dM=0$.
- Among reco jets with $20 < p_T < 30$ GeV, 36% of PYTHIA6 embedding jets and 37% of data jets have $dM=0$. (Higher p_T jets have a smaller fraction of $dM=0$).



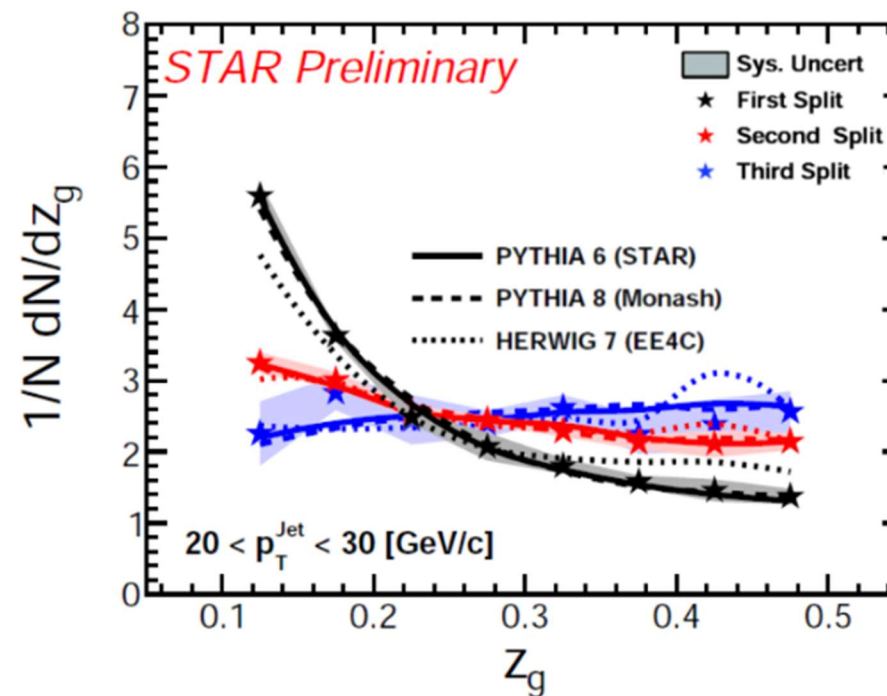
Soft radiation vs hard splitting momentum imbalance



Steeply falling \sim DGLAP $1/z$: pQCD

→ The first splitting that passes SoftDrop can still be non-perturbative, but if we apply the $\Delta M = 0$ selection, we can filter out some npQCD contribution due to the parton splitting

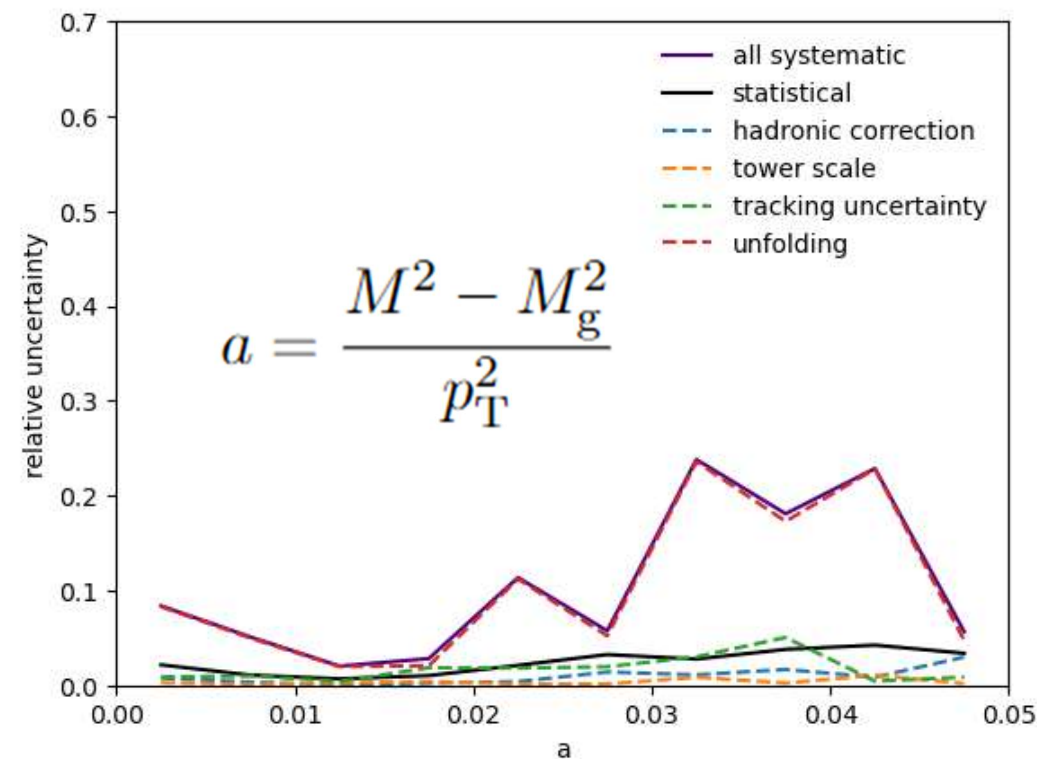
- The more mass that is groomed away relative to the original mass, the flatter the Z_g distribution is
 - Demonstrates that **early** soft wide angle radiation constrains the momentum imbalance of & the amount of npQCD contributions to **later** splittings
- MC models describe the trend of data



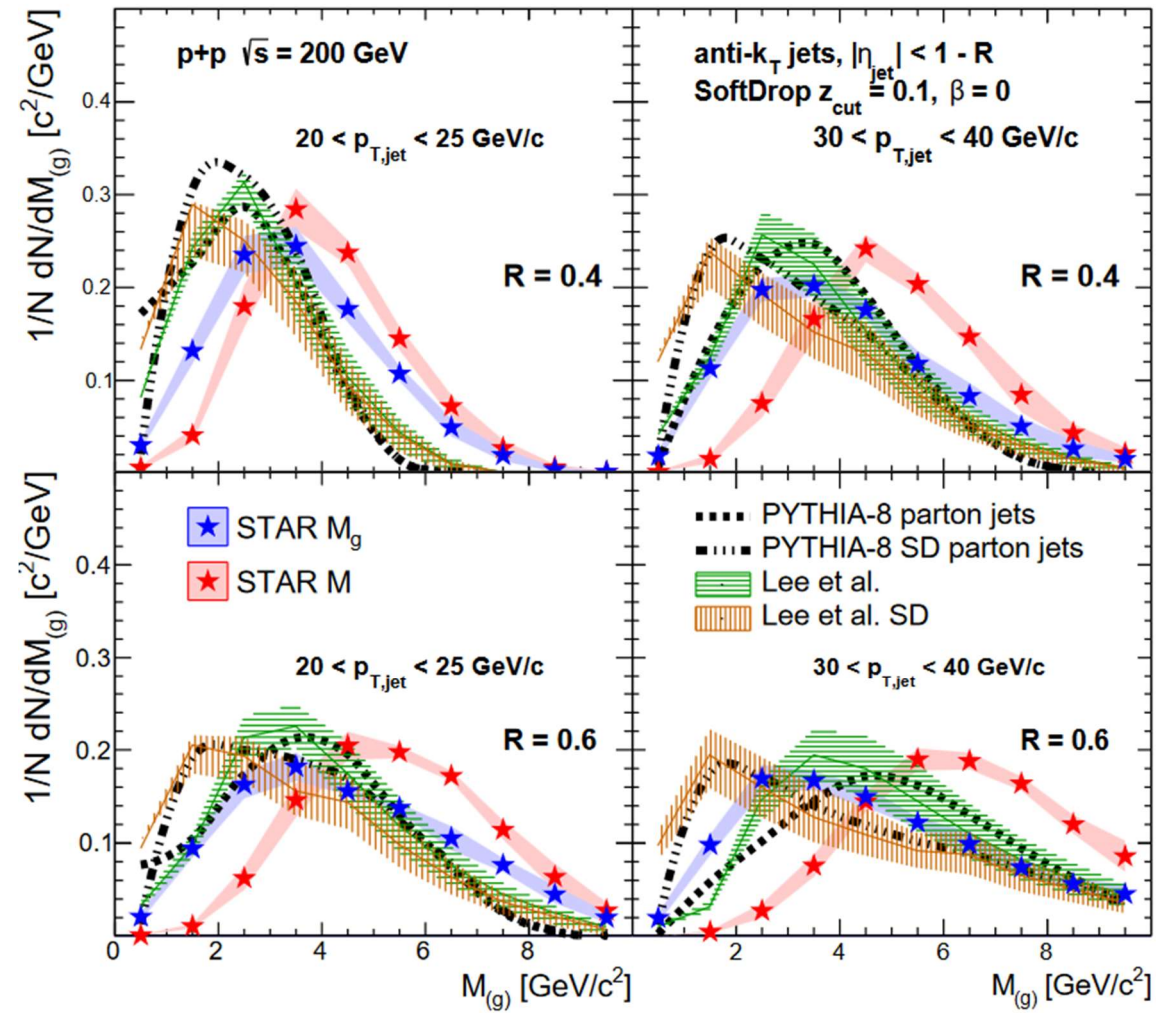


Systematic uncertainties

- Detector systematics
 - Hadronic correction 100% \rightarrow 50%
 - Tower scale +3.8%
 - Tracking uncertainty -4%
- Unfolding systematics
 - Unfolding seed
 - Iteration number variation
 - Prior shape variation to HERWIG7 and PYTHIA8
 - Nominal: prior = (generation, simulation)
= (PYTHIA6, PYTHIA6 + GEANT3 + embedding)
 - Varied to: prior \rightarrow reweight \otimes nominal prior ,
with $\text{reweight}(p_T, Q, M, M_g, R_g, z_g) = \frac{\text{Herwig truth}(p_T, Q, M, M_g, R_g, z_g)}{\text{Pythia6 truth}(p_T, Q, M, M_g, R_g, z_g)}$



Jet mass: Comparison with models and calculations



[STAR Collaboration. PRD 104, 052007\(2021\)](#)