

Novel approach to jet substructure measurement in pp collisions at $\sqrt{s} = 200$ GeV in STAR

Youqi Song (youqi.song@yale.edu) for the STAR Collaboration

APS DNP 2022, New Orleans, LA

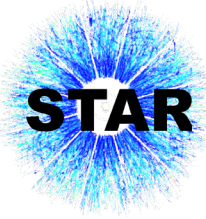
10/29/2022



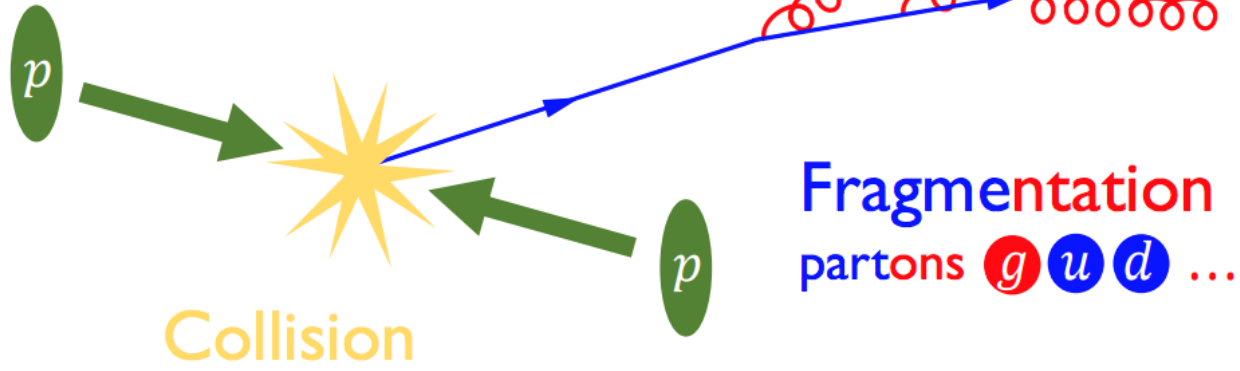
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Motivation



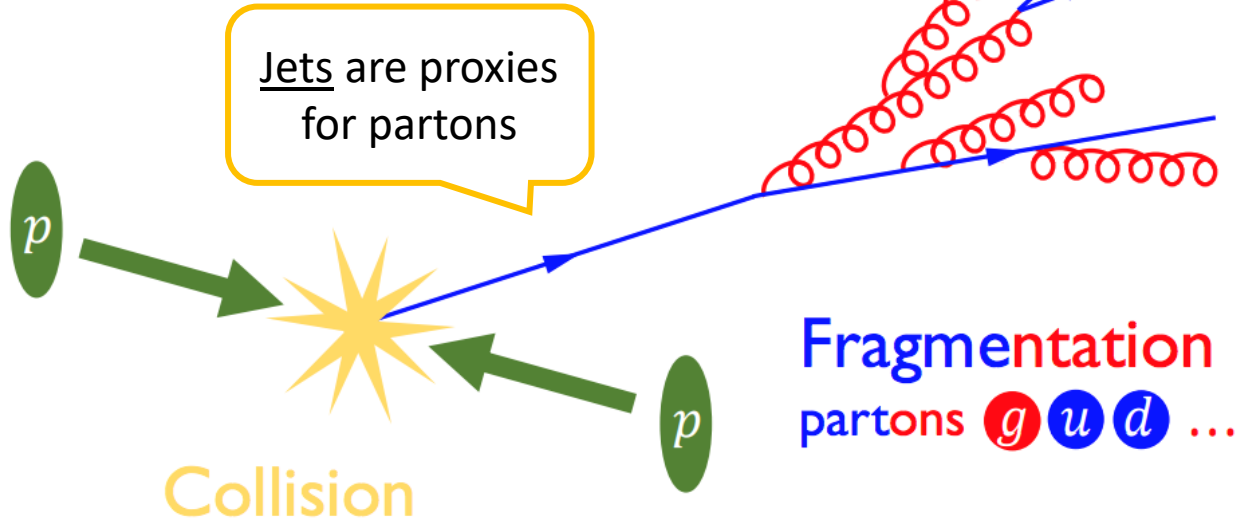
Hadronization

hadrons π^\pm K^\pm ...

Image credit: [Metodiev BOOST 2019](#)



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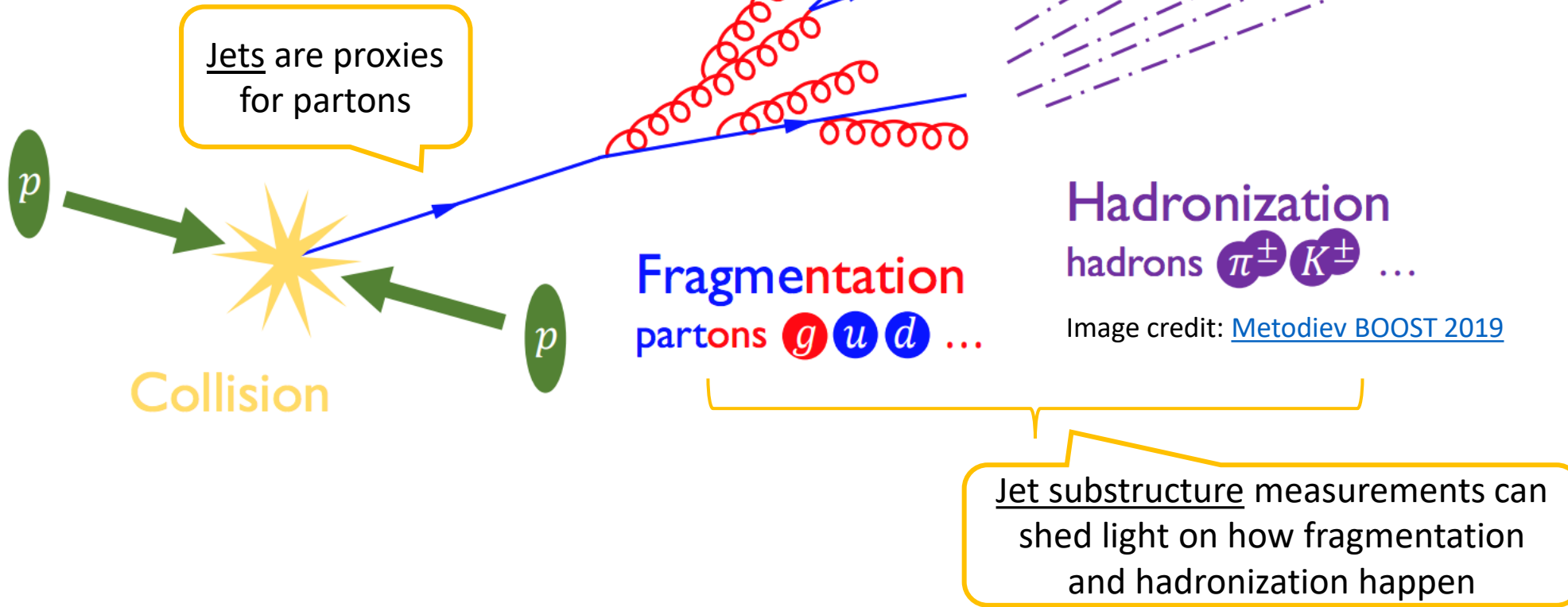


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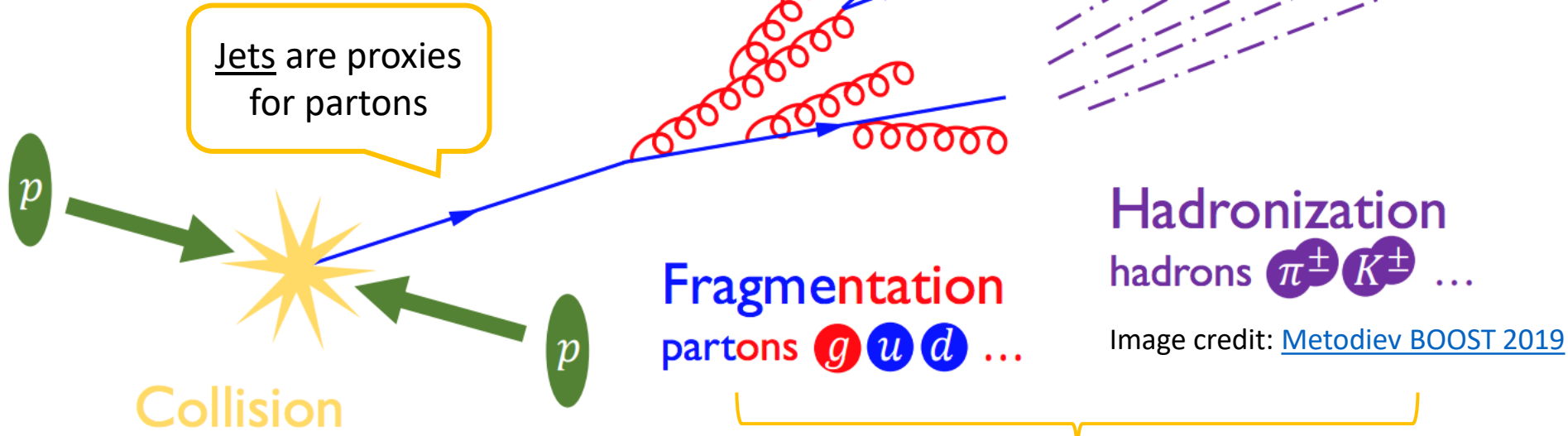
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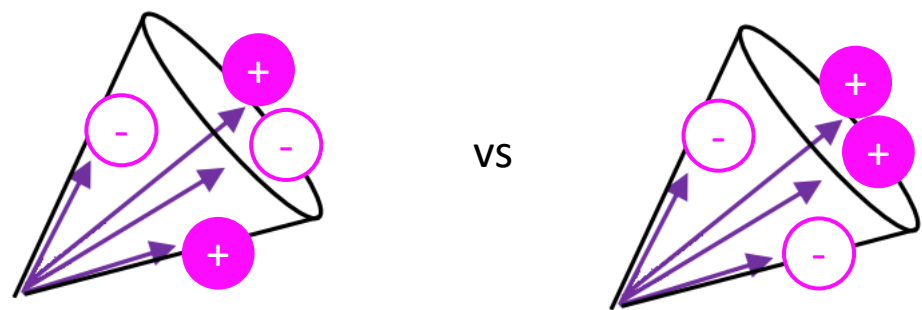


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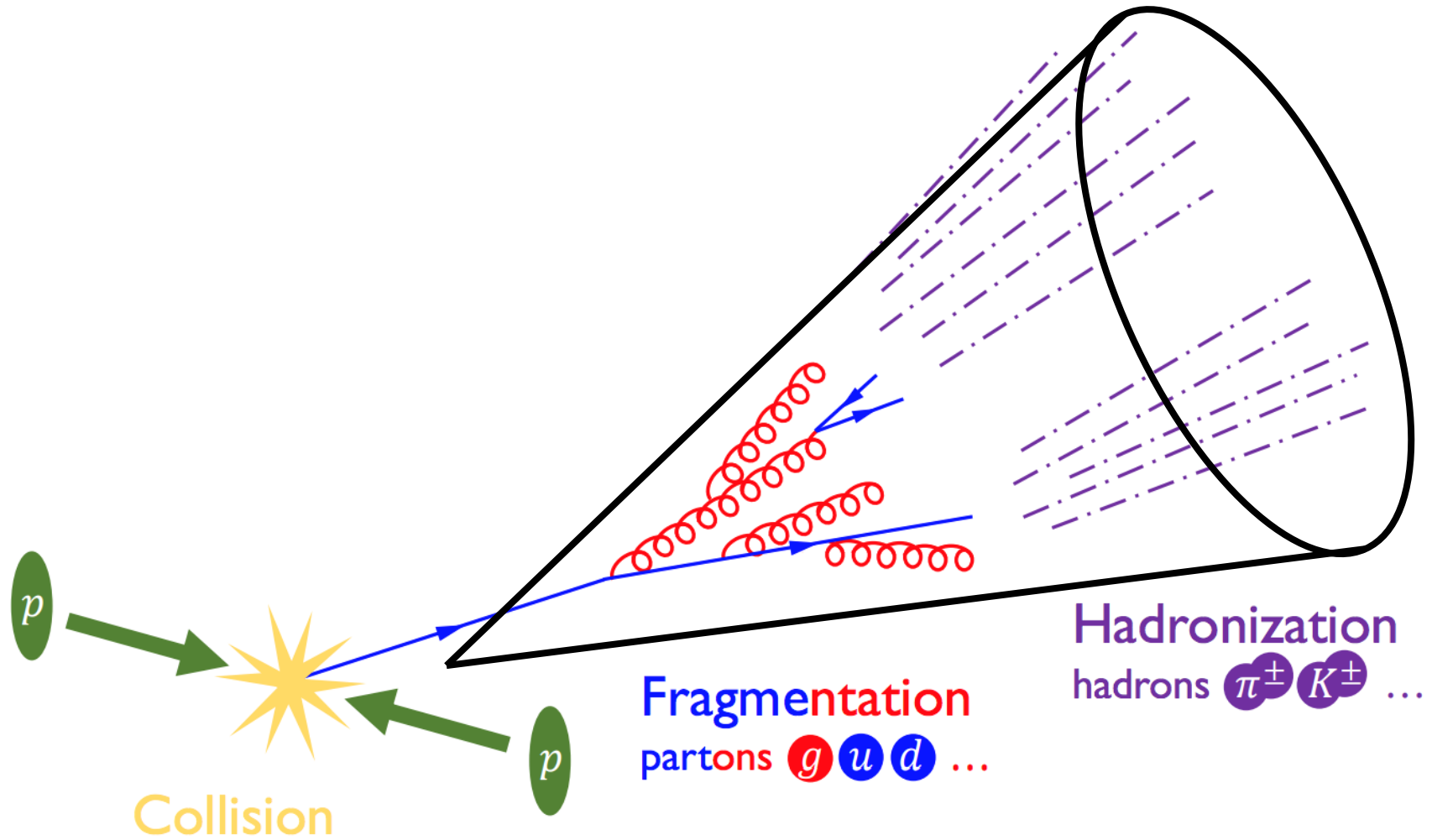
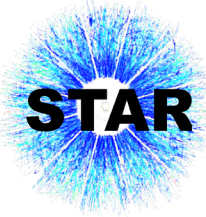
Multi-dimensional jet substructure measurements help us distinguish different fragmentation patterns

Jet substructure measurements can shed light on how fragmentation and hadronization happen

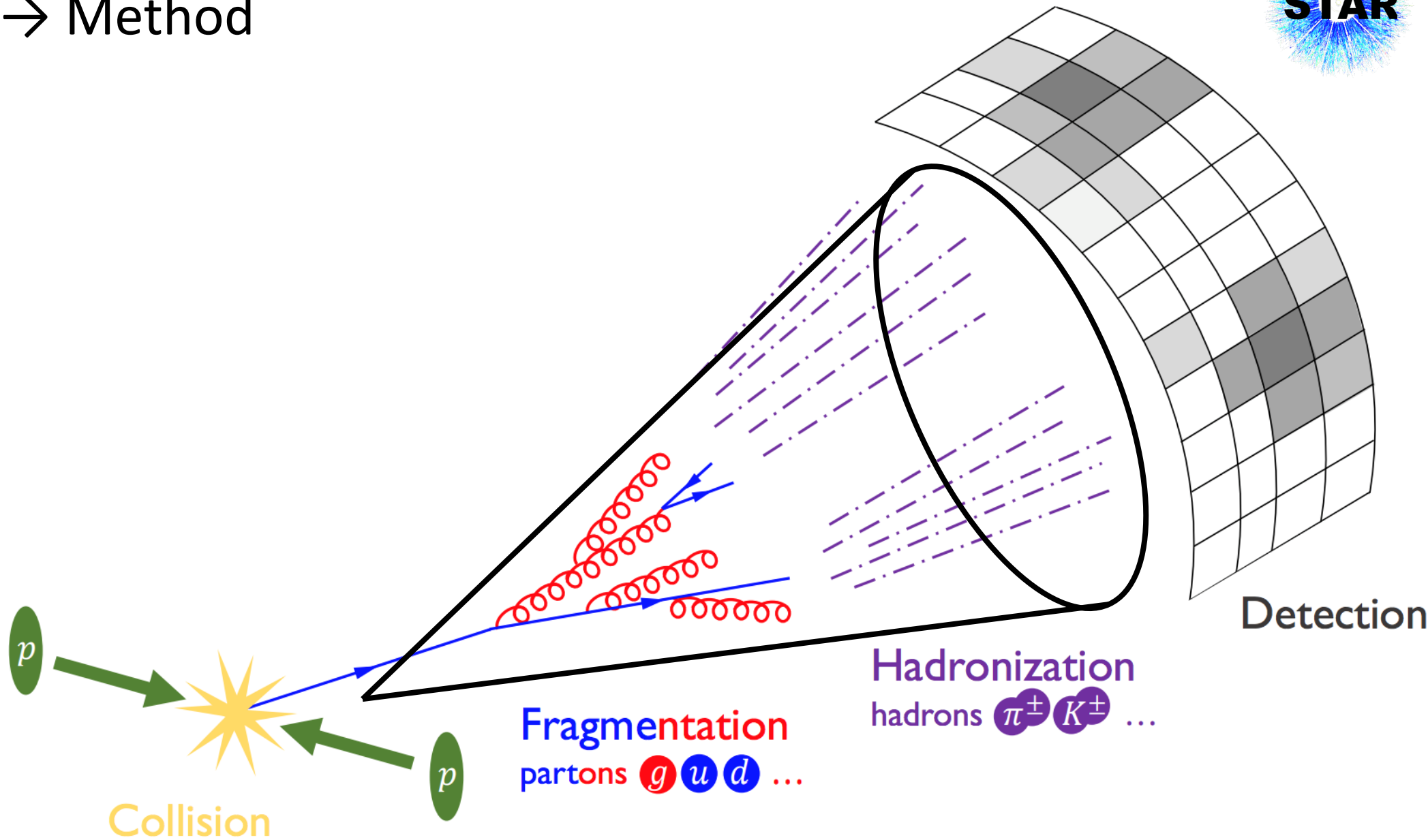


Same jet mass,
Different p_T -weighted jet charge

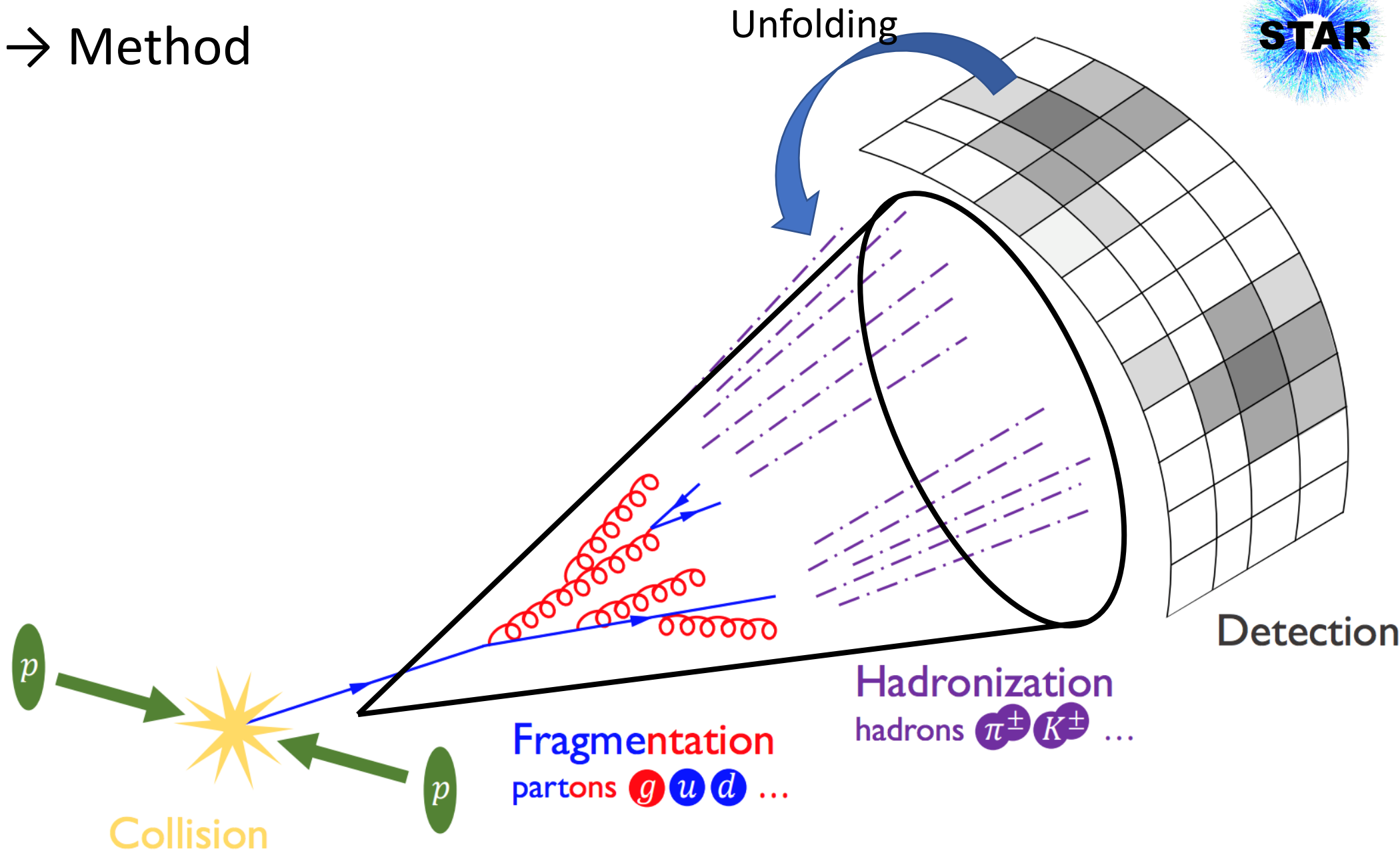
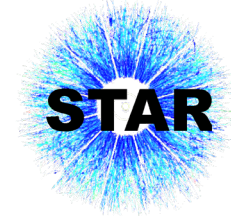
Motivation → Method

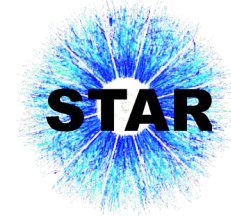


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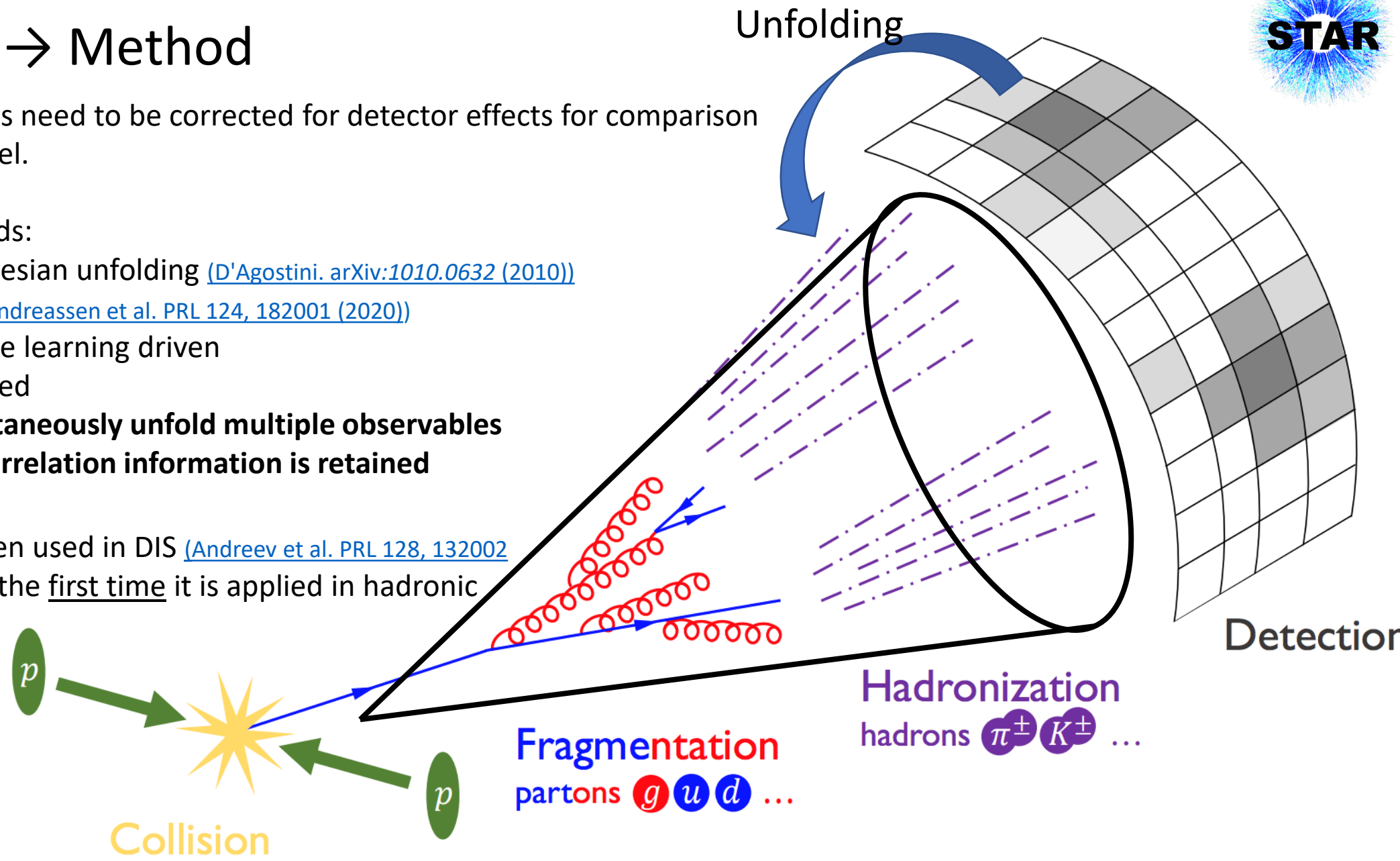
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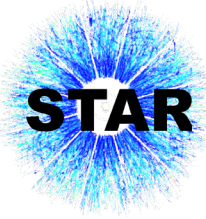




Motivation → Method

- Jet measurements need to be corrected for detector effects for comparison with theory/model.
- Unfolding methods:
 - Iterative Bayesian unfolding ([D'Agostini. arXiv:1010.0632 \(2010\)](#))
 - **MultiFold** ([Andreassen et al. PRL 124, 182001 \(2020\)](#))
 - Machine learning driven
 - Unbinned
 - **Simultaneously unfold multiple observables**
 - **Correlation information is retained**
- MultiFold has been used in DIS ([Andreev et al. PRL 128, 132002 \(2022\)](#)), but this is the first time it is applied in hadronic collision data.





Observables

- p_T : transverse momentum

- $Q^\kappa = \frac{1}{(p_{T\text{jet}})^\kappa} \sum_{i \in \text{jet}} q_i \cdot (p_{Ti})^\kappa \rightarrow$ Choose $\kappa=2$

- $M = |\sum_{i \in \text{jet}} p_i| = \sqrt{E^2 - |\vec{p}|^2}$
4-momentum of the constituent i

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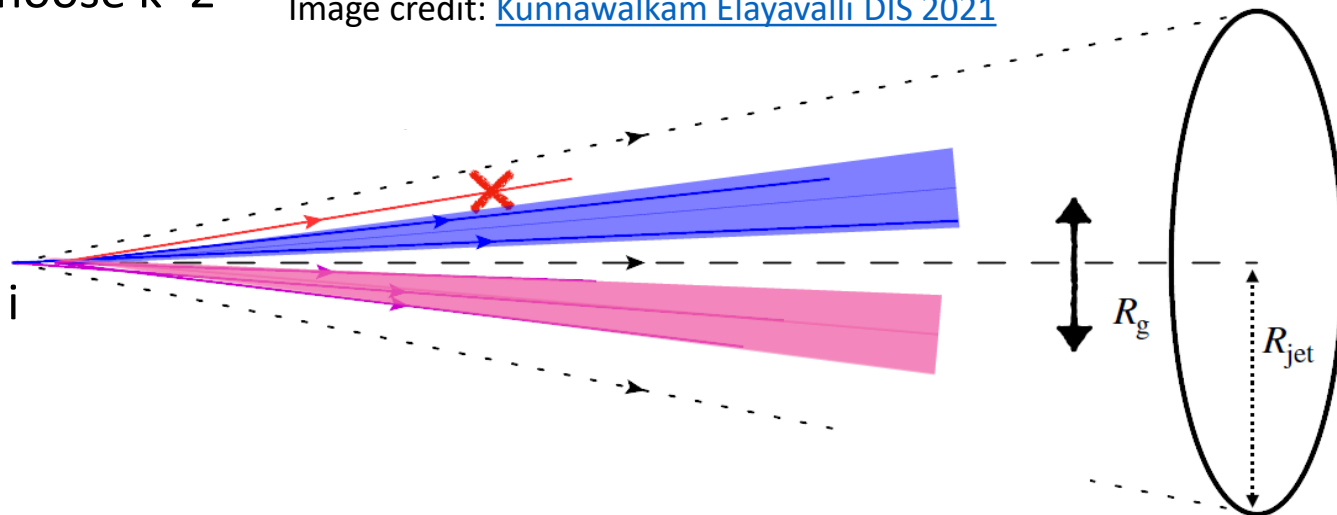
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SoftDrop grooming

[Larkoski, et al. JHEP 2014, 146 \(2014\).](#)

[Dasgupta et al. JHEP 2013, 29 \(2013\).](#)

Image credit: [Kunnawalkam Elayavalli DIS 2021](#)



Require subjet momentum fraction to pass

$$z_g = \frac{\min(p_{T,1}, p_{T,2})}{p_{T,1} + p_{T,2}} > z_{\text{cut}} (R_g/R_{\text{jet}})^\beta$$

$$z_{\text{cut}} = 0.1$$

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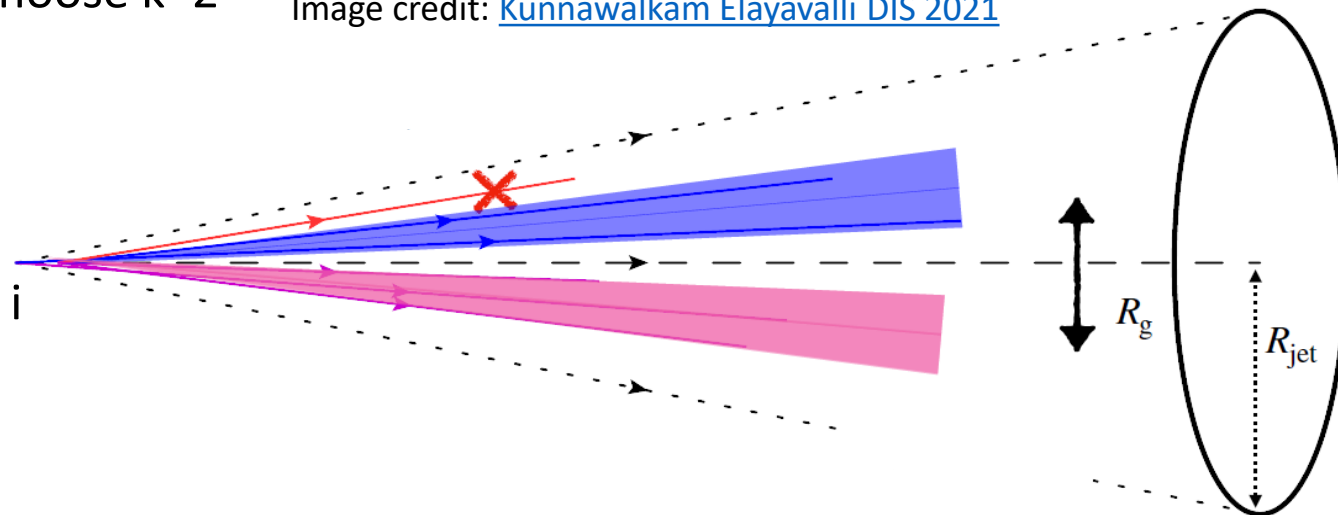
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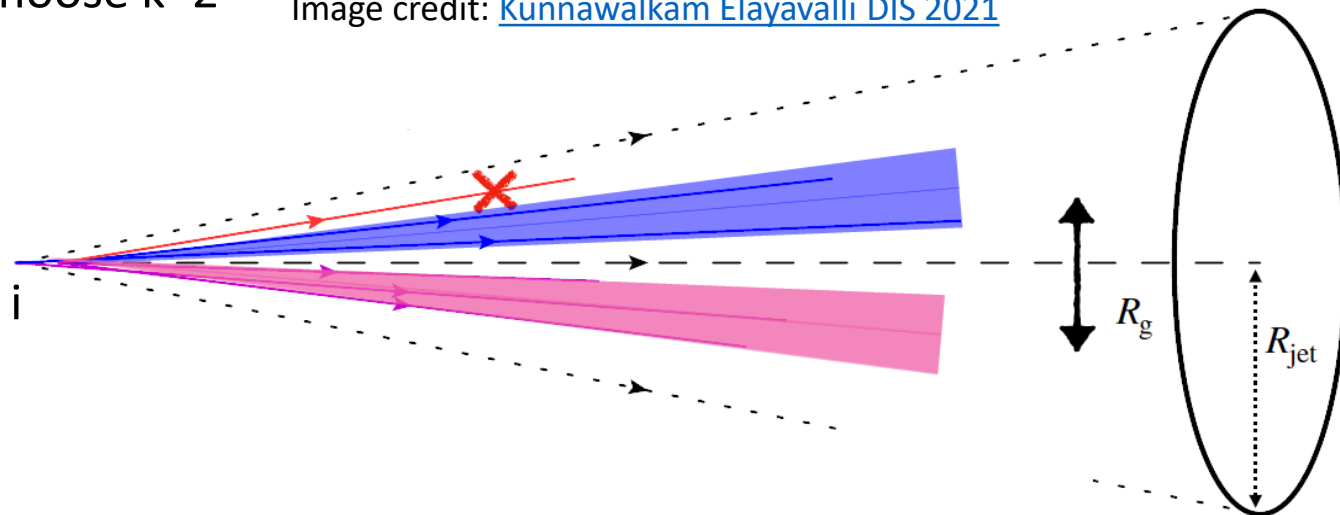
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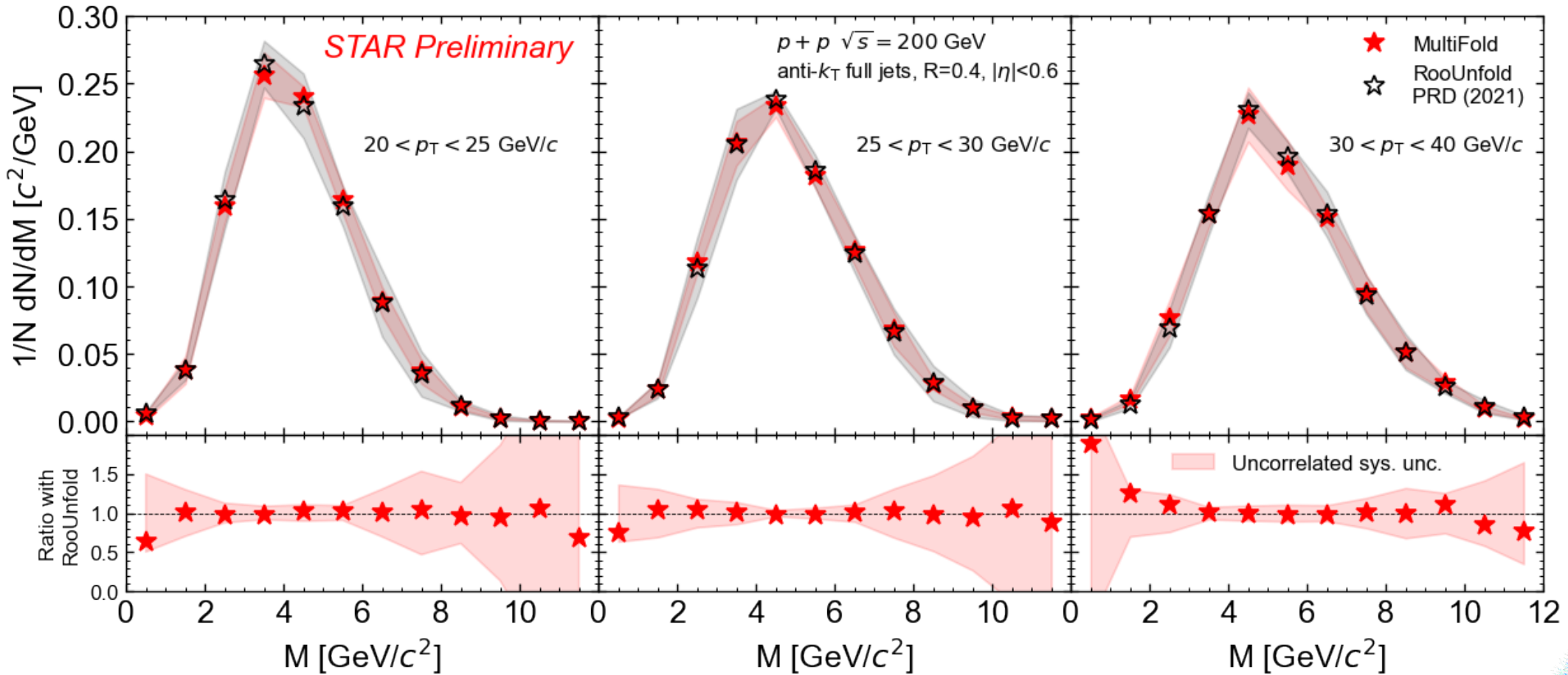
$$\beta = 0$$

All 6 observables are simultaneously unfolded in an unbinned way!

Fully corrected jet M

$$M = \left| \sum_{i \in \text{jet}} p_i \right| = \sqrt{E^2 - p^2}$$

MultiFold result agrees with **RooUnfold** result ([STAR Collaboration. PRD 104, 052007\(2021\)](#)) [HEPData](#)



... but **MultiFold** also gives us correlation between observables!

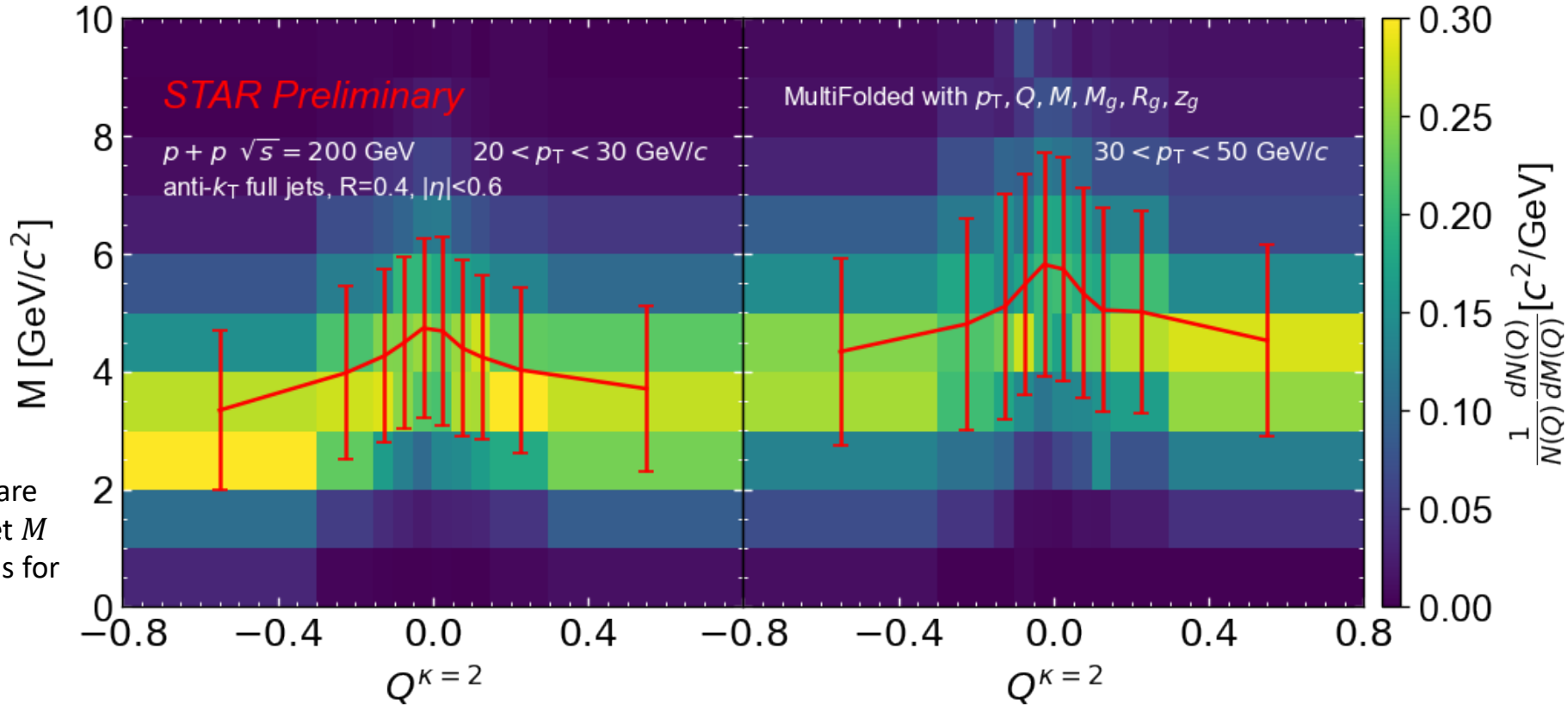
See backup slides for a breakdown of systematics.



Fully corrected jet M vs Q vs p_T

$$Q_J = \frac{1}{(p_{TJ})^\kappa} \sum_{i \in \text{Tracks}} q_i \times (p_{T,i})^\kappa \quad M = \left| \sum_{i \in \text{jet}} p_i \right| = \sqrt{E^2 - p^2}$$

(normalization is done per Q bin)



(Error bars are widths of jet M distributions for each Q bin)

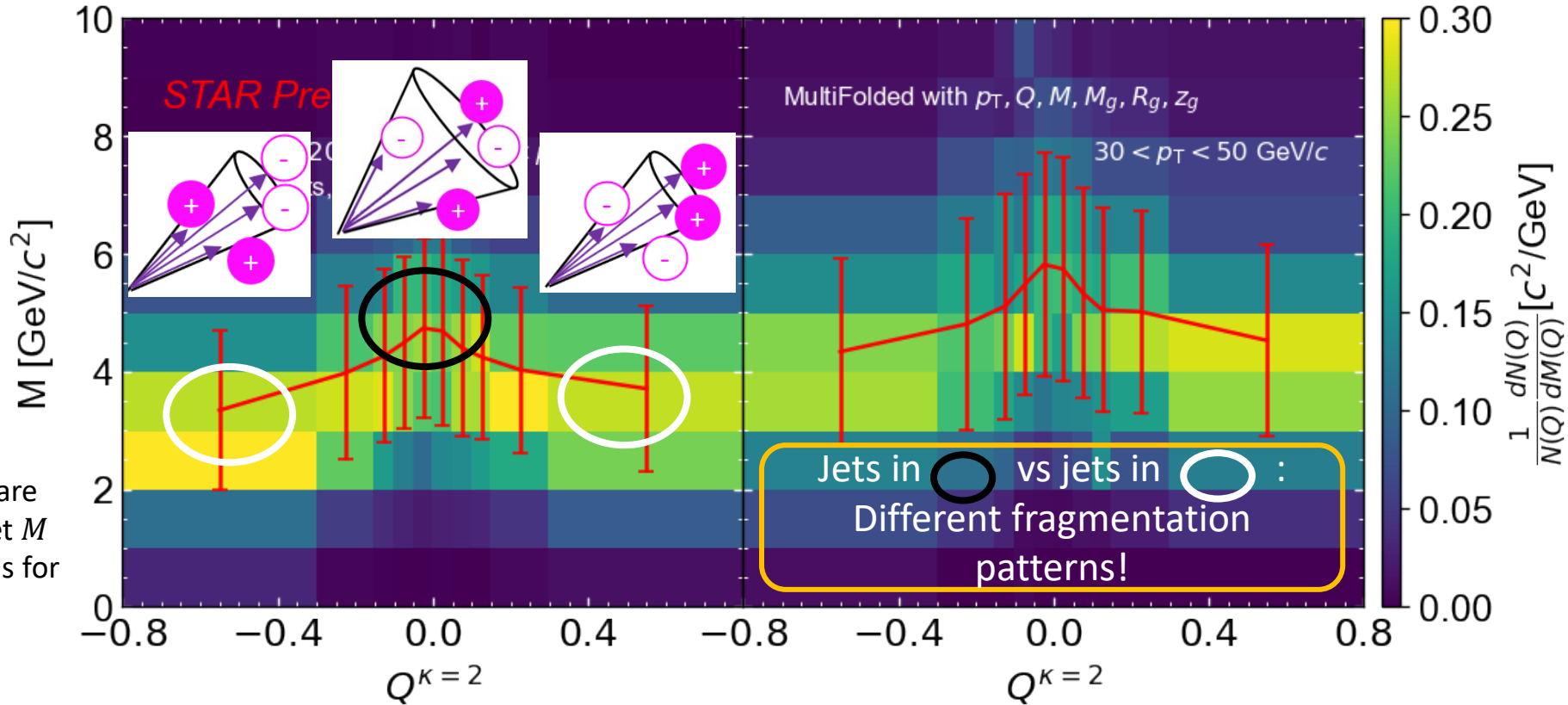
- Jet M increases with increasing jet p_T → Higher p_T means larger phase space for radiation
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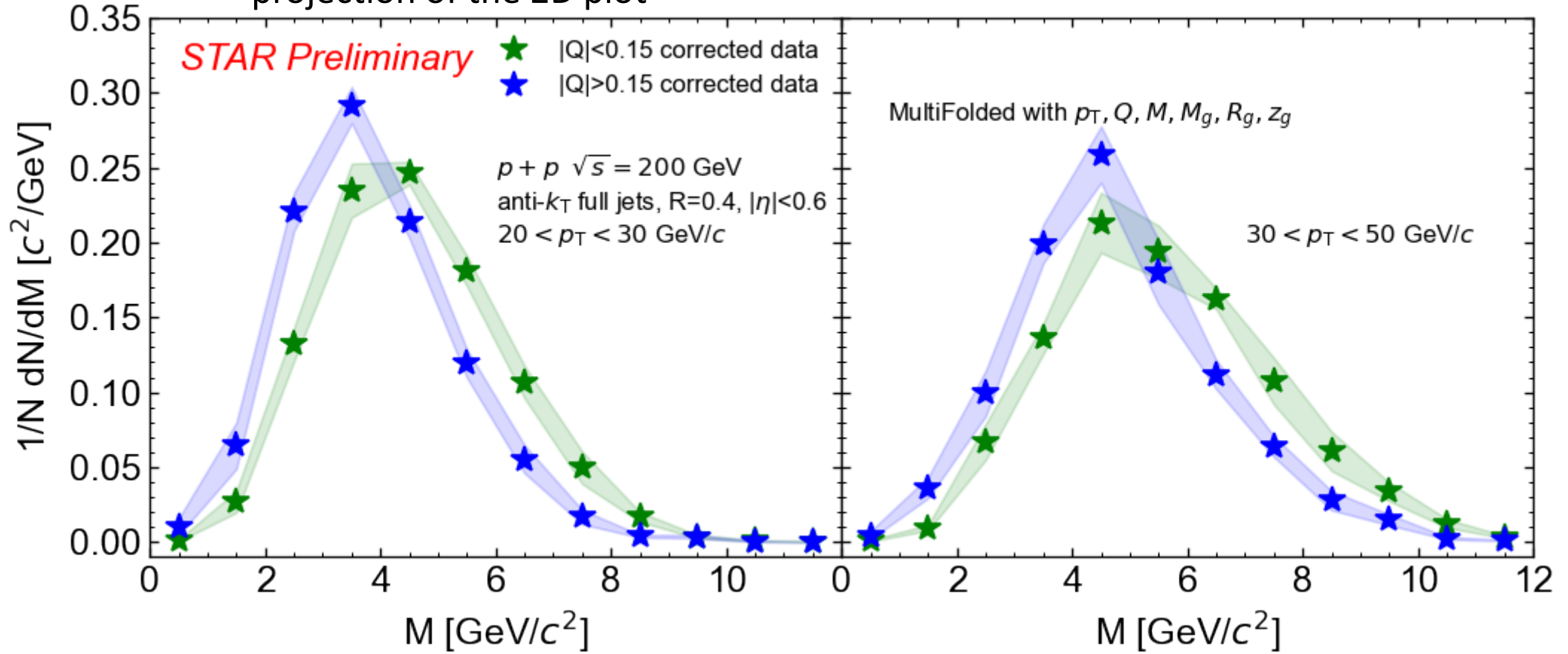
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projection of the 2D plot



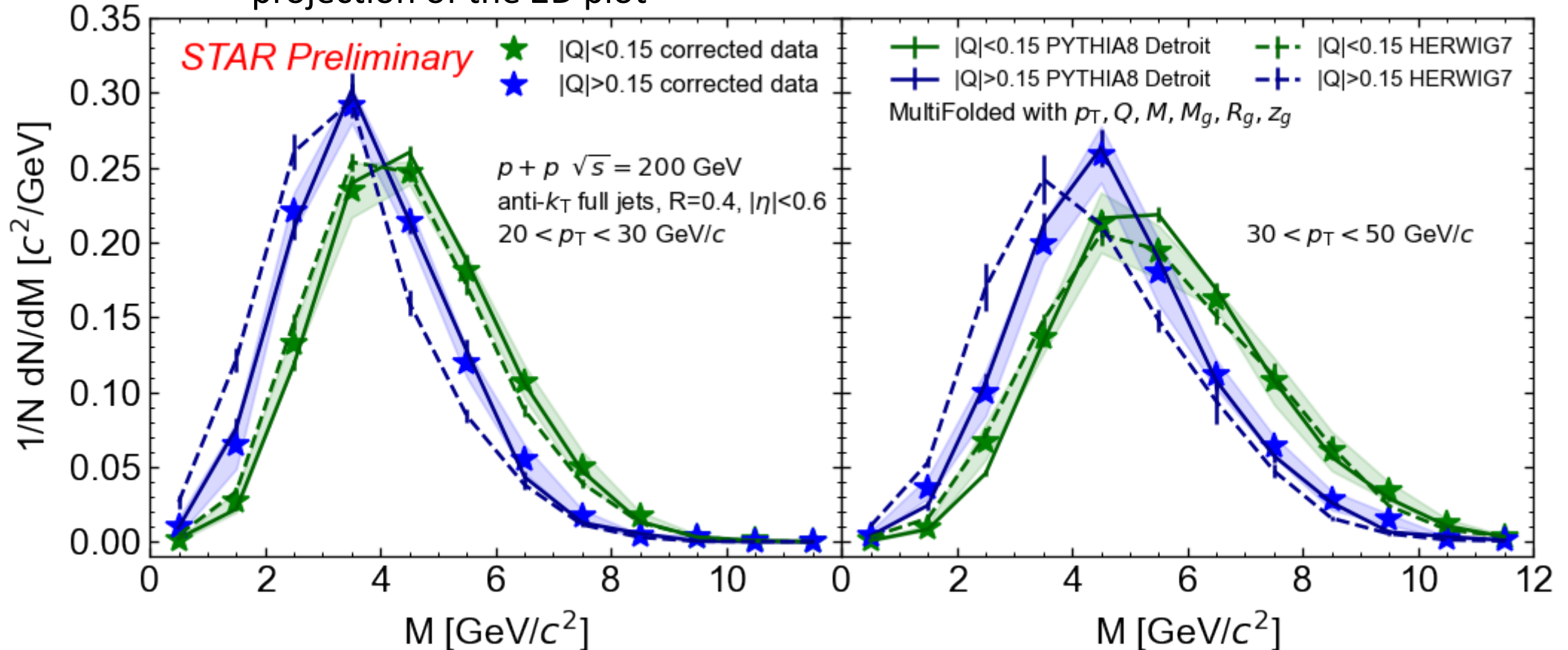
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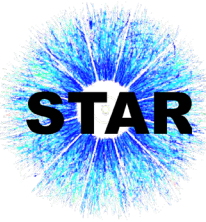
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PYTHIA8 Detroit tune: Describes jet M vs $|Q|$ well

HERWIG7: Underpredicts jet M for large $|Q|$ significantly

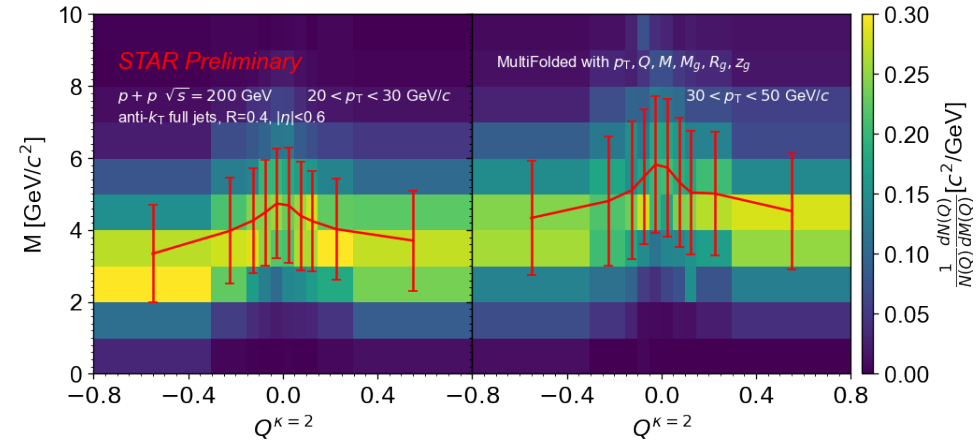
PYTHIA6 Perugia 2012 STAR tune: [Skands, PRD 82, 074018 \(2010\)](#)
 PYTHIA8 Detroit tune: [Aguilar et al. PRD 105, 016011\(2022\)](#)
 HERWIG7: [Bellm, et al. PRC 76, 1-8 \(2016\)](#)





Summary and outlook

- First measurement in pp that uses machine learning based method for unfolding
 - **Multi-dimensional** and unbinned
 - **Nice agreement with RooUnfold**

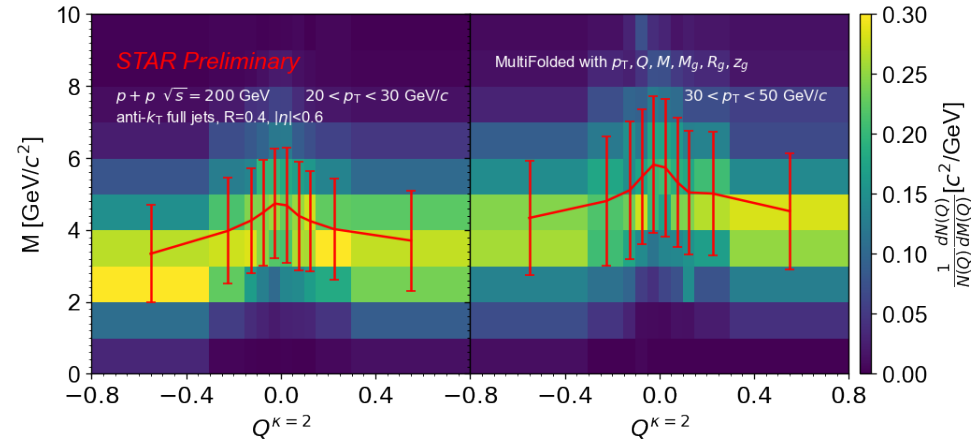


- Fully-corrected measurement of jet M vs Q vs p_T in $\sqrt{s} = 200$ GeV pp collisions.
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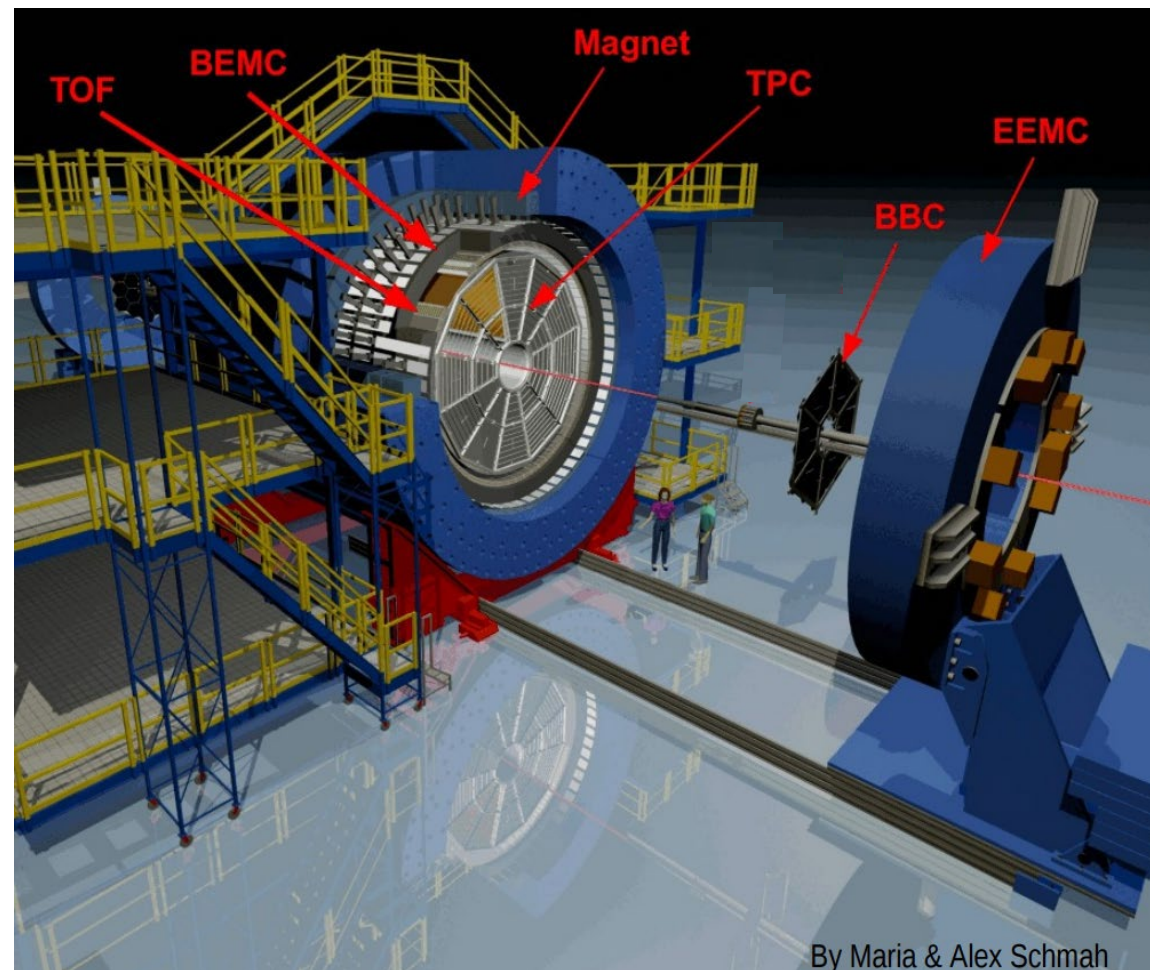
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 - Jet M increases with increasing p_T ; jet M increases with decreasing $|Q|$.
 - **PYTHIA8 Detroit tune** describes the data well; **HERWIG7** underpredicts jet M for large $|Q|$.
- Future directions
 - Selecting jets with different **fragmentation** patterns \rightarrow study **hadronization**
 - 6-dimensional jet information \rightarrow separate **quark vs gluon** jets

Backup

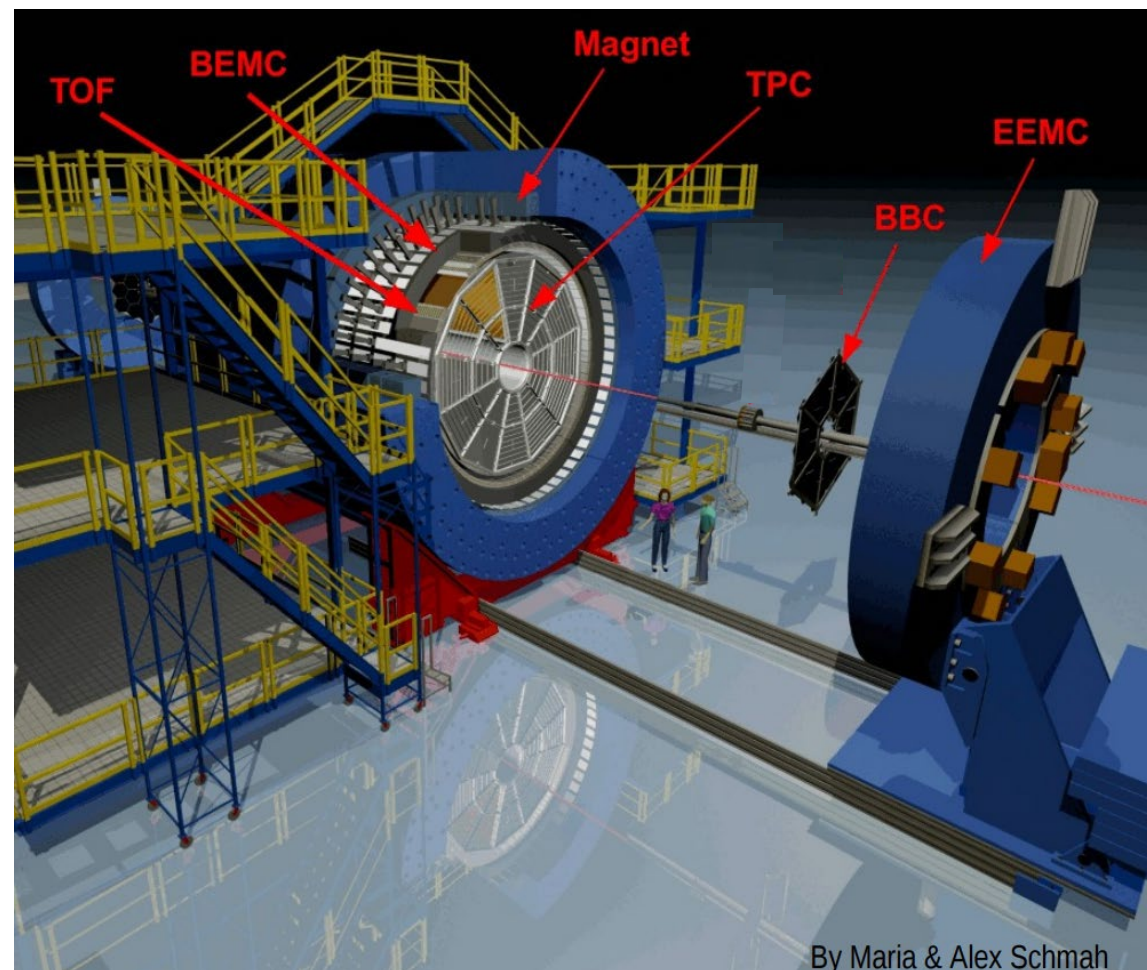
Jet reconstruction at STAR



Jet reconstruction at STAR

Important subdetectors for $pp \sqrt{s} = 200 \text{ GeV}$ collisions data-taking during 2012 RHIC run

- **TPC** (Time Projection Chamber)
 - For **charged** particle track reconstruction
 - $|\eta| < 1$, full azimuthal coverage
- **BEMC** (Barrel ElectroMagnetic Calorimeter)
 - For **neutral** energy measurement and triggering
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- Reconstruct anti- k_T **full jets**
 - Jet resolution parameter **R=0.4**
 - $|\eta_{\text{jet}}| < 0.6$



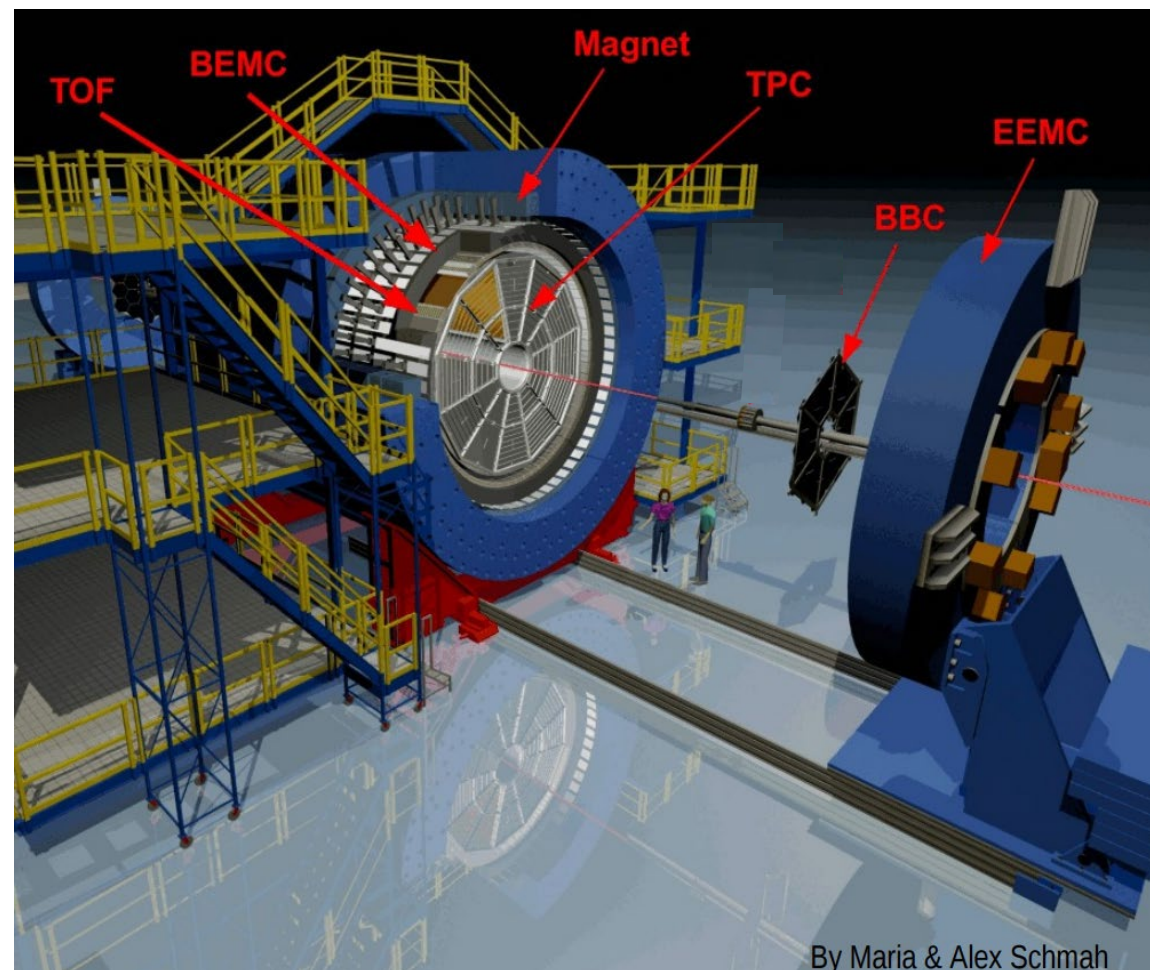
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Additional selections

- Tracks (Towers): $0.2 < p_T(E_T) < 30 \text{ GeV}$
- Jets
 - $p_T > 15 \text{ GeV}/c$, $M > 1 \text{ GeV}/c^2$, neutral p_T fraction < 0.9
 - Passes SoftDrop with $z_{\text{cut}} = 0.1$ and $\beta = 0$





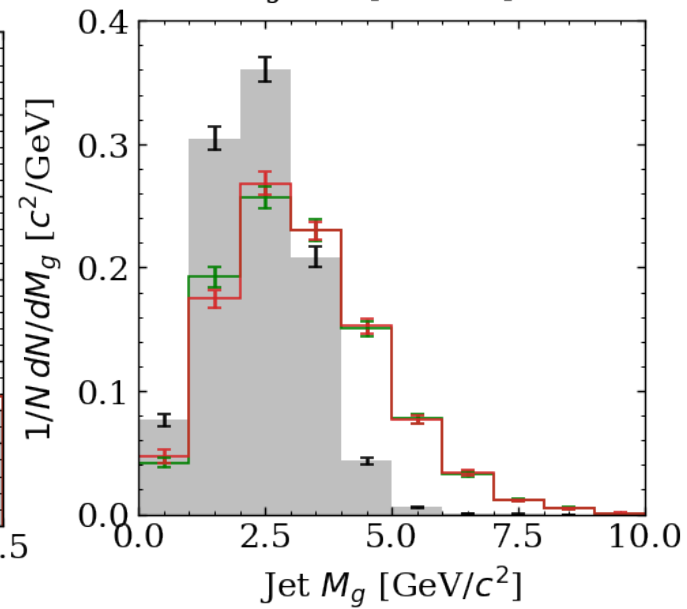
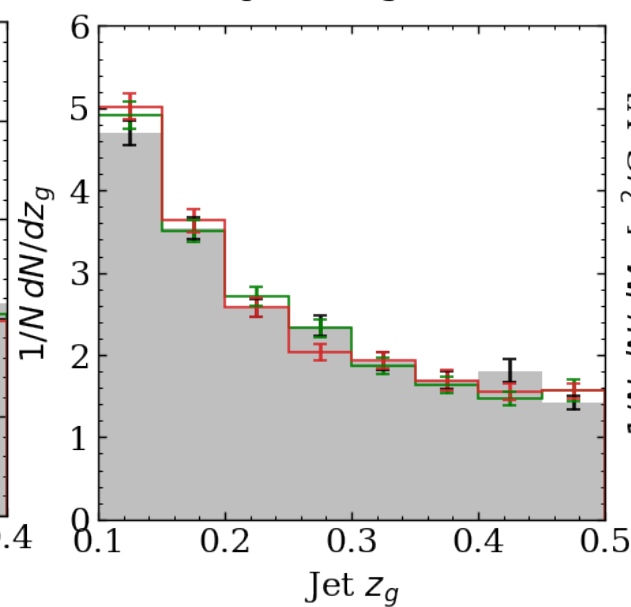
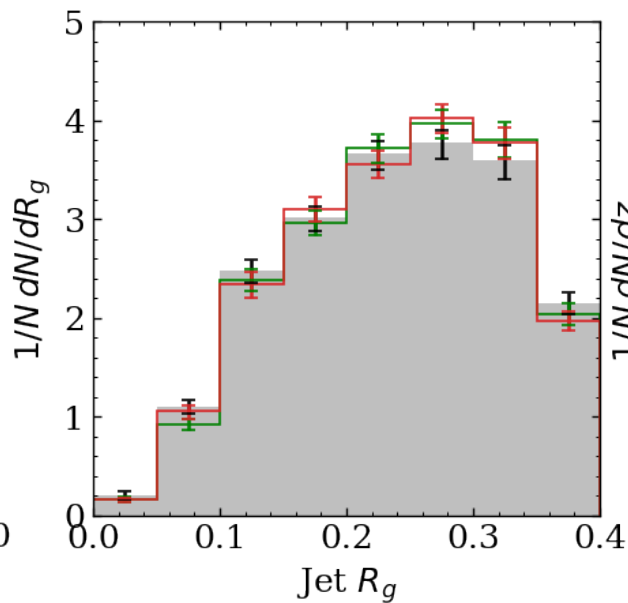
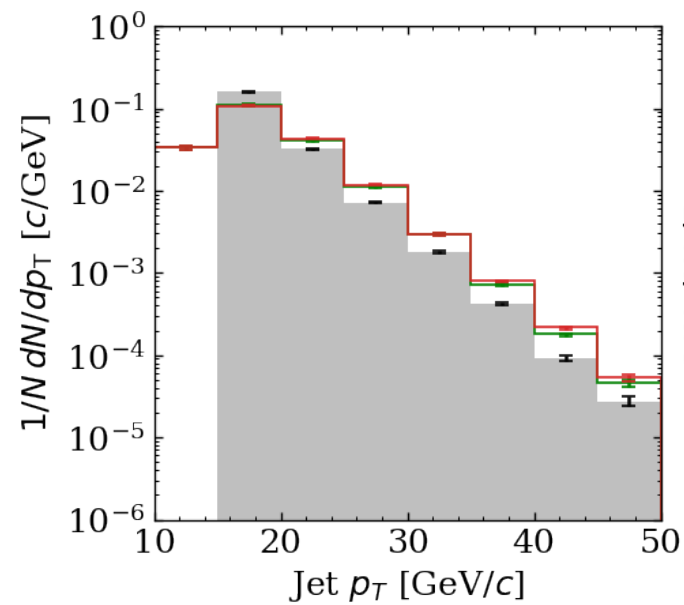
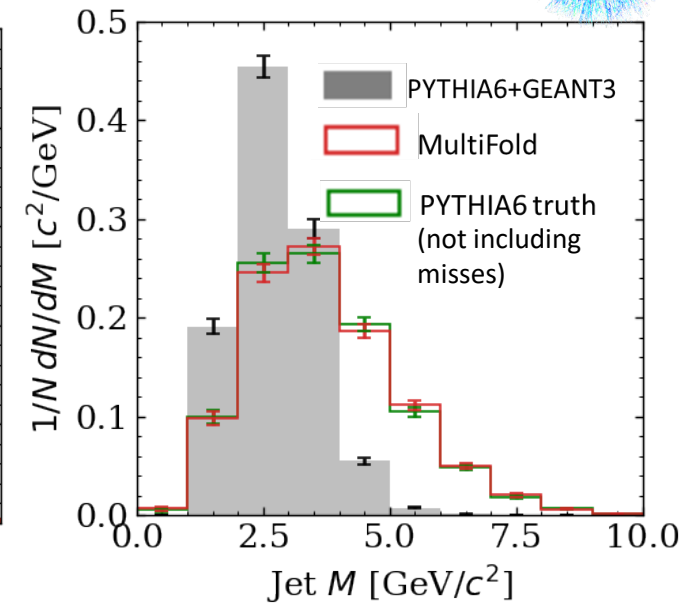
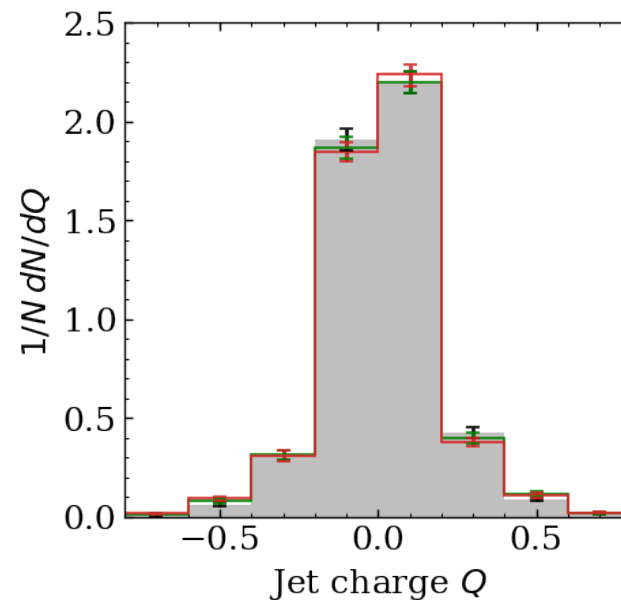
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- Unfolding is **unbinned**. Binning is chosen afterward for illustration.

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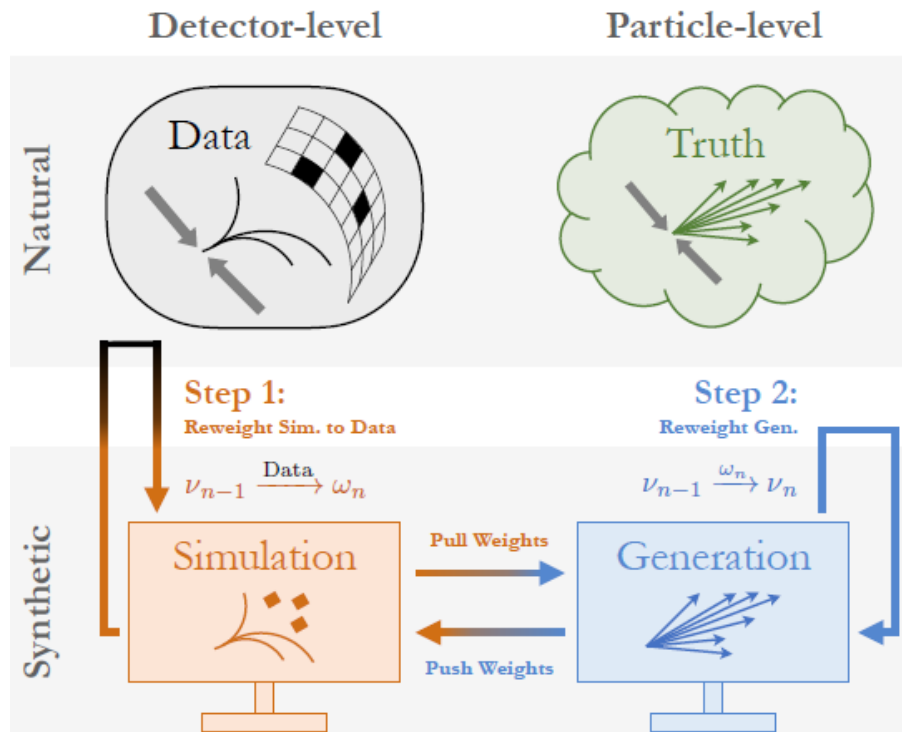
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pp $\sqrt{s} = 200$ GeV

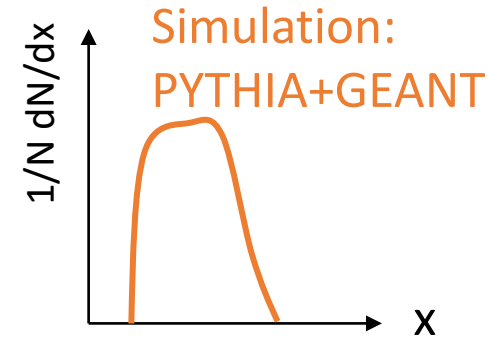
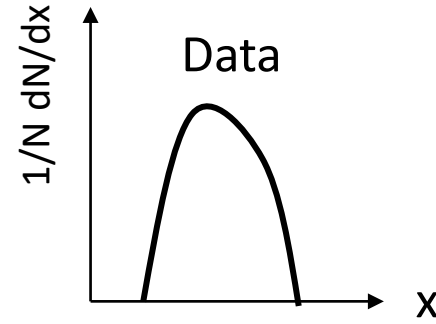




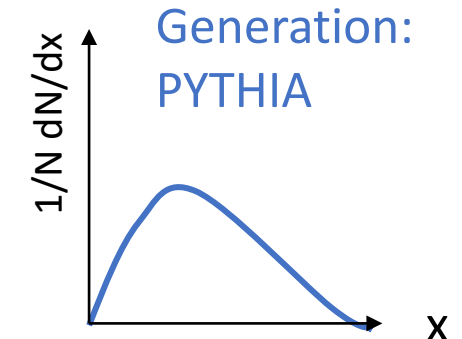
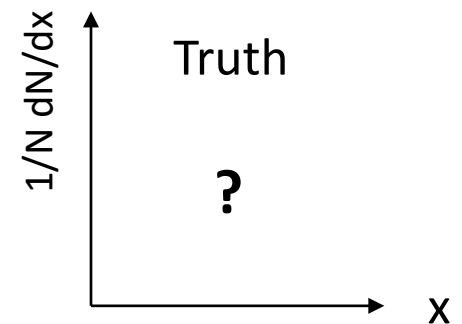
Method



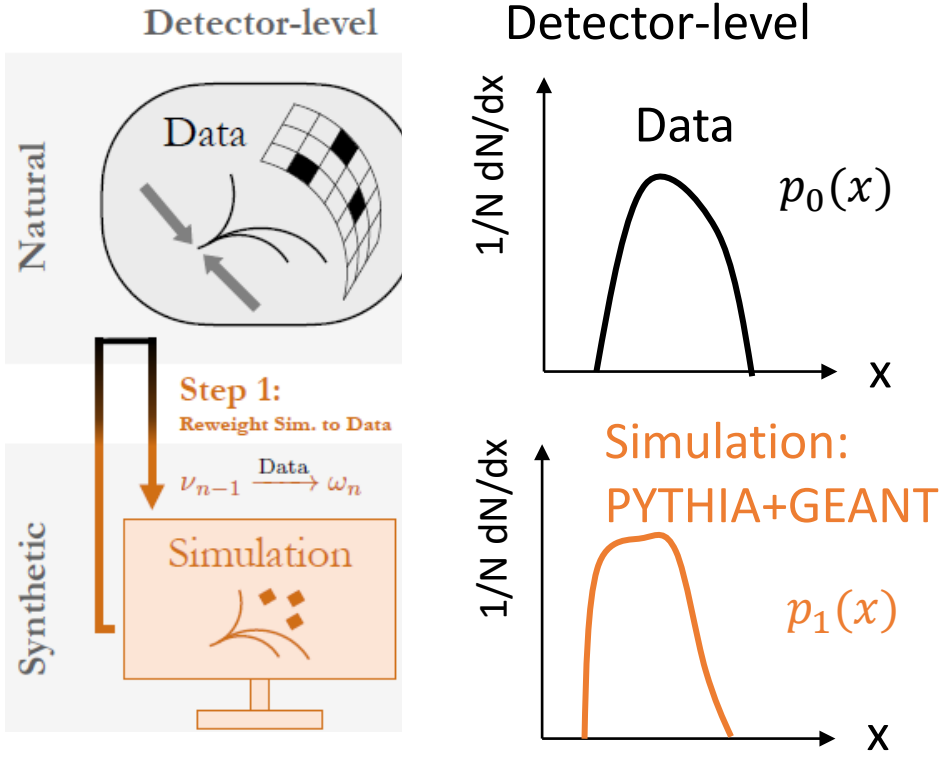
Detector-level



Particle-level

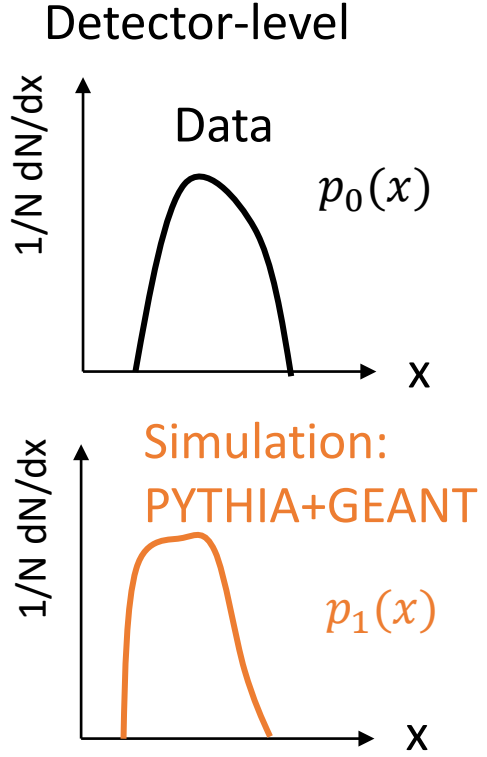
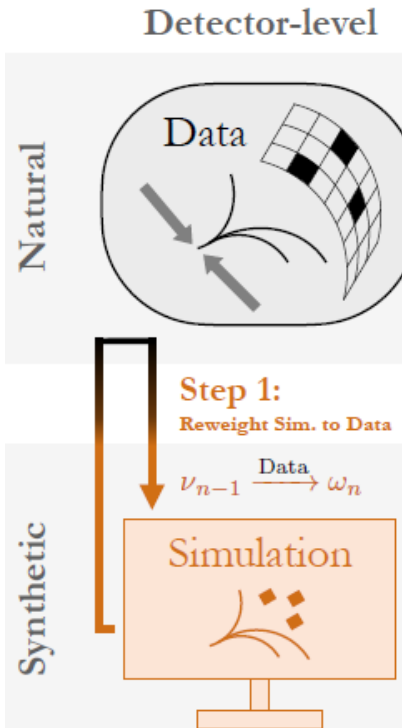


Method: machine learning



Where does the machine learning part come in?

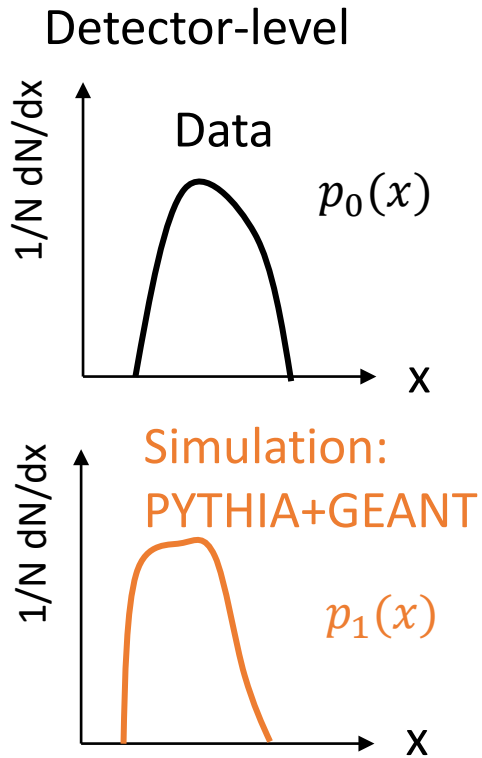
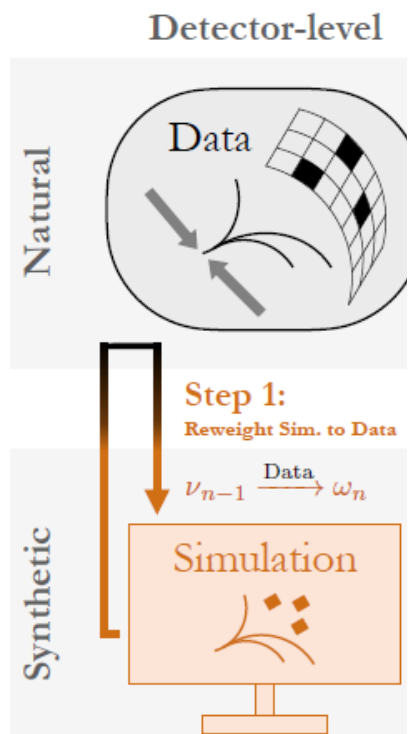
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E.g., Iteration 1, step 1:
 Weights: $w(x) = p_0(x)/p_1(x)$

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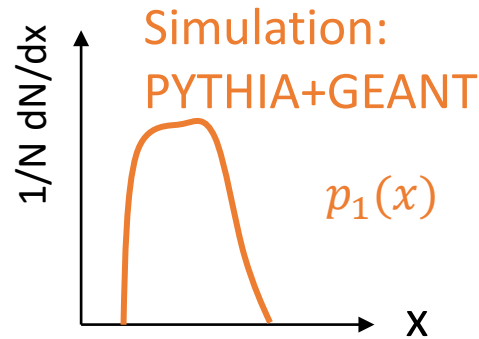
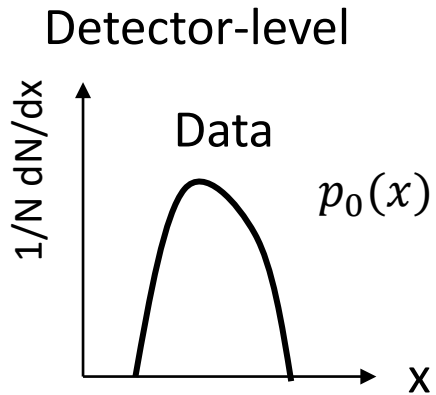
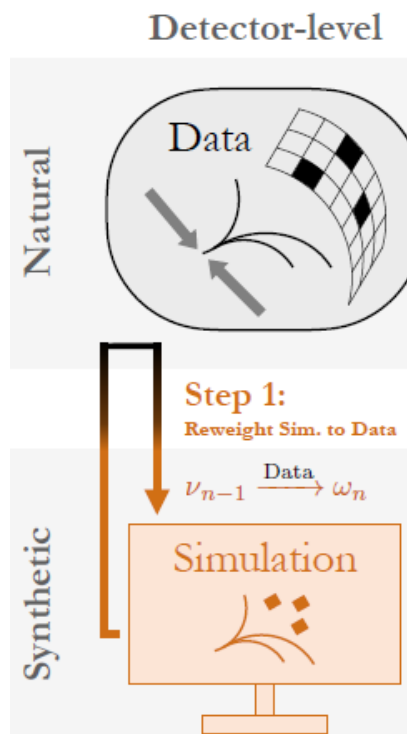
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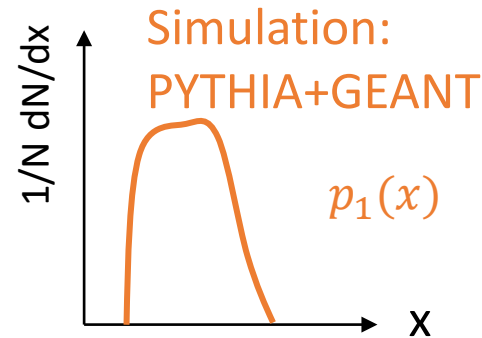
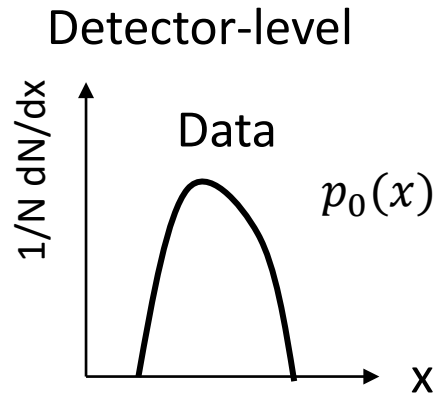
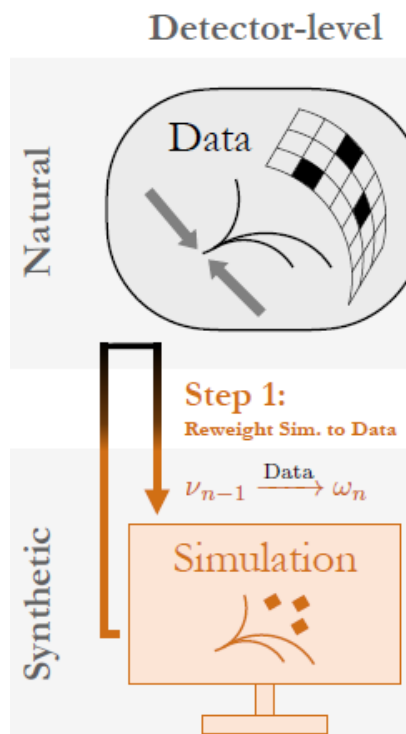
$$\approx f(x)/(1 - f(x))$$

[\(Andreassen and Nachman PRD 101, 091901 \(2020\)\)](#)

where $f(x)$ is a neural network and trained with the binary cross-entropy loss function

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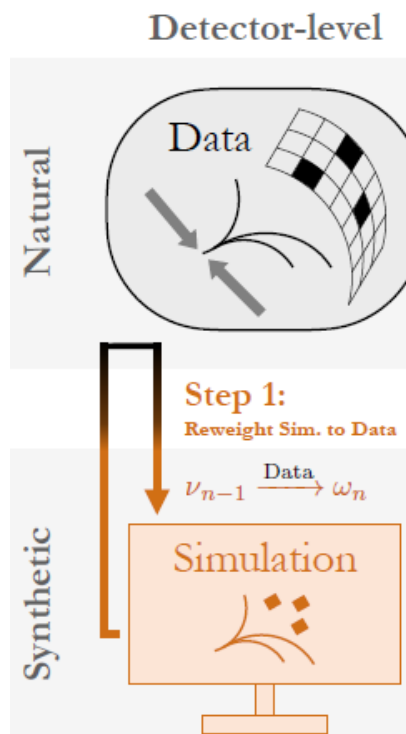
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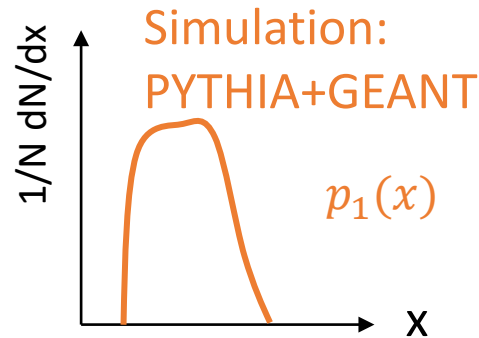
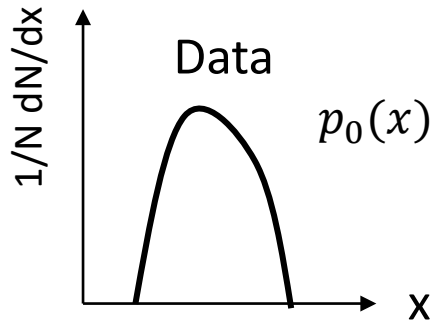
to distinguish jets coming from data vs from simulation

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Detector-level



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to distinguish jets coming from data vs from simulation

Unfolding \rightarrow Reweighting histograms
 \rightarrow Classification \rightarrow Neural network

Where does the machine learning part come in?

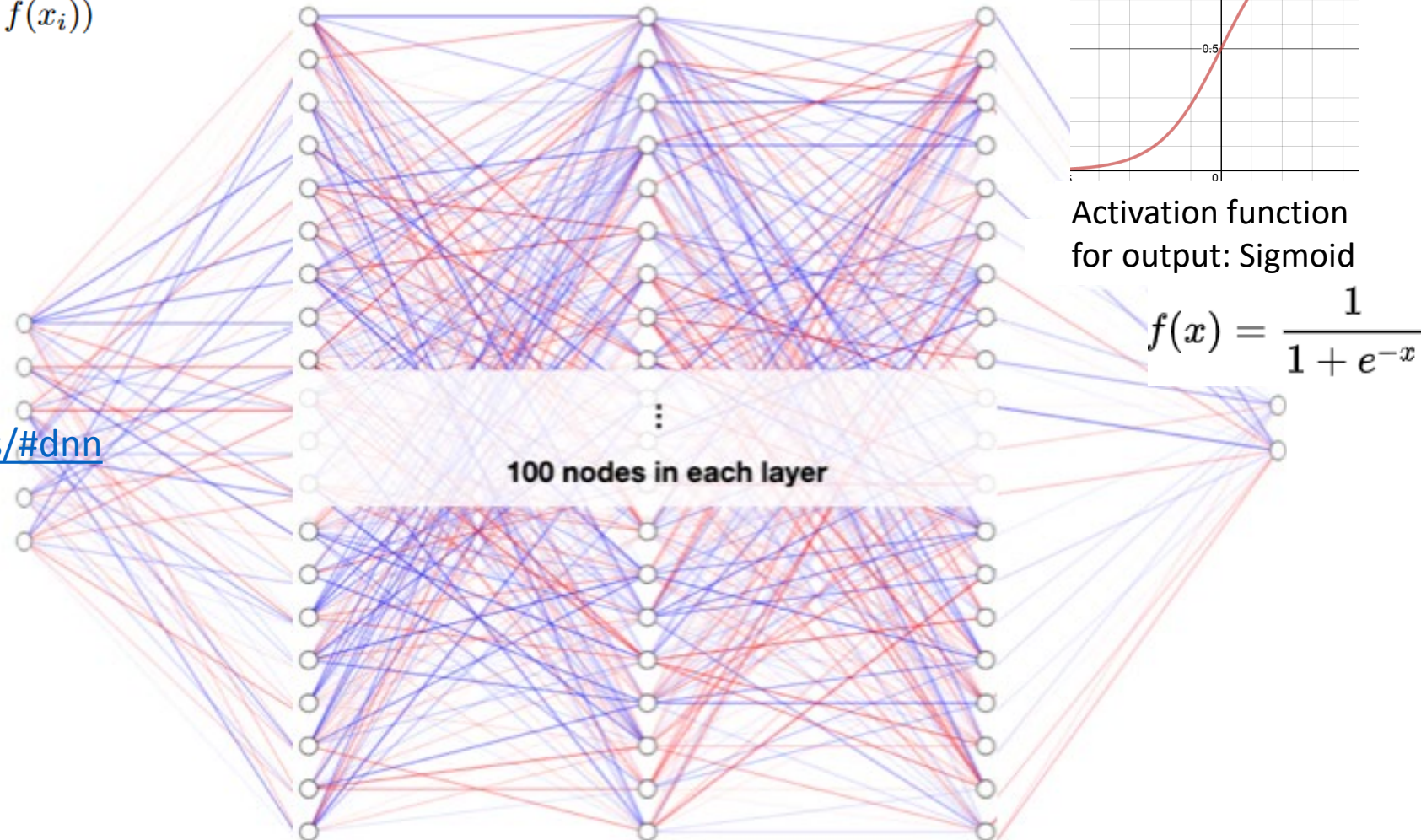
Method

- Architecture: Dense neural network
- Activation function for dense layers: Rectified linear unit
- Activation function for output layer: Sigmoid
- Loss function: Binary cross entropy

$$\text{loss}(f(x)) = - \sum_{i \in 0} \log f(x_i) - \sum_{i \in 1} \log(1 - f(x_i))$$

- Optimization algorithm: Adam
<https://arxiv.org/pdf/1412.6980.pdf>
- Nodes per dense layer: [100,100,100]
- Output dimension: 2
- Input dimension: 6
- All hyperparameters are default:
<https://energyflow.network/docs/archs/#dnn>

Activation function for dense layers: Rectified linear unit
 $f(x) = x^+ = \max(0, x)$



Method

- <https://energyflow.network/docs/archs/>

Compilation Options

- `loss= 'categorical_crossentropy' : str`
 - The loss function to use for the model. See the [Keras loss function docs](#) for available loss functions.
- `optimizer= 'adam' : Keras optimizer or str`
 - A [Keras optimizer](#) instance or a string referring to one (in which case the default arguments are used).
- `metrics= ['accuracy'] : list of str`
 - The [Keras metrics](#) to apply to the model.
- `compile_opts= {} : dict`
 - Dictionary of keyword arguments to be passed on to the `compile` method of the model. `loss`, `optimizer`, and `metrics` (see above) are included in this dictionary. All other values are the Keras defaults.

Output Options

- `output_dim= 2 : int`
 - The output dimension of the model.
- `output_act= 'softmax' : str or Keras activation`
 - Activation function to apply to the output.

Callback Options

- `filepath= None : str`
 - The file path for where to save the model. If `None` then the model will not be saved.
- `save_while_training= True : bool`
 - Whether the model is saved during training (using the `ModelCheckpoint` callback) or only once training terminates. Only relevant if `filepath` is set.
- `save_weights_only= False : bool`
 - Whether only the weights of the model or the full model are saved. Only relevant if `filepath` is set.
- `modelcheck_opts= {'save_best_only':True, 'verbose':1} : dict`
 - Dictionary of keyword arguments to be passed on to the `ModelCheckpoint` callback, if it is present. `save_weights_only` (see above) is included in this dictionary. All other arguments are the Keras defaults.
- `patience= None : int`
 - The number of epochs with no improvement after which the training is stopped (using the `EarlyStopping` callback). If `None` then no early stopping is used.
- `earlystop_opts= {'restore_best_weights':True, 'verbose':1} : dict`
 - Dictionary of keyword arguments to be passed on to the `EarlyStopping` callback, if it is present. `patience` (see above) is included in this dictionary. All other arguments are the Keras defaults.

Method

- <https://energyflow.network/docs/archs/#dnn>

Required DNN Hyperparameters

- `input_dim` : `int = 6`
 - The number of inputs to the model.
- `dense_sizes` : `{tuple, list} of int=[100,100,100]`
 - The number of nodes in the dense layers of the model.

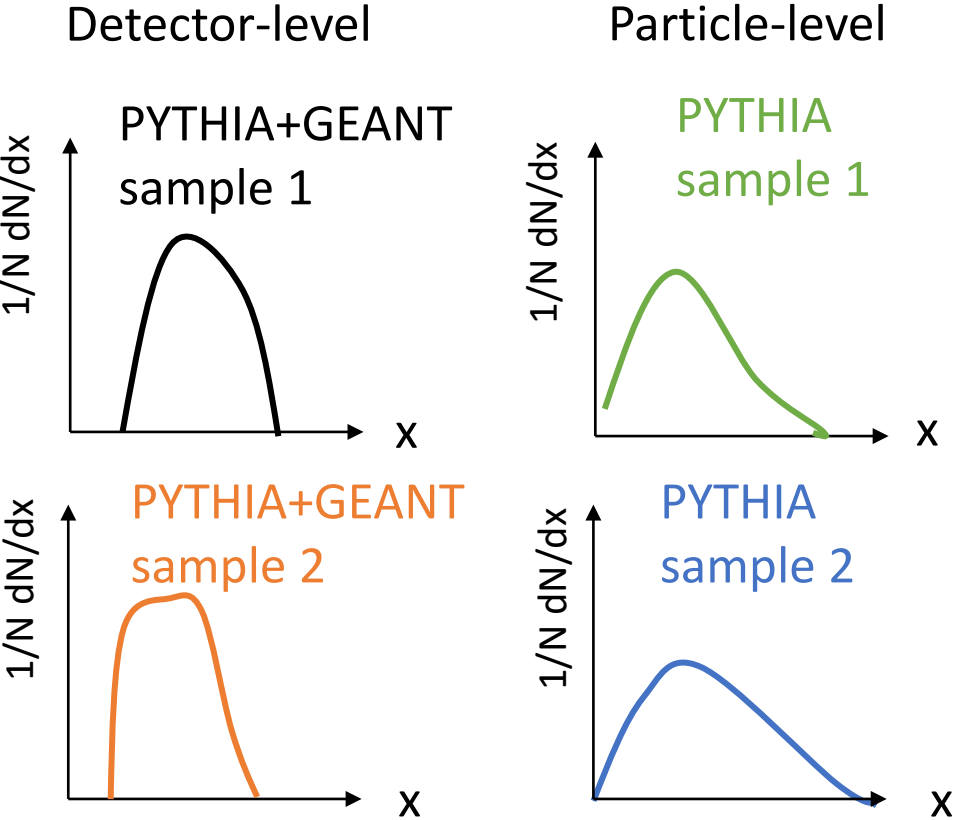
Default DNN Hyperparameters

- `acts`=`'relu'` : `{tuple, list} of str` or Keras activation
 - Activation function(s) for the dense layers. A single string or activation layer will apply the same activation to all dense layers. Keras advanced activation layers are also accepted, either as strings (which use the default arguments) or as Keras `Layer` instances. If passing a single `Layer` instance, be aware that this layer will be used for all activations and may introduce weight sharing (such as with `PReLU`); it is recommended in this case to pass as many activations as there are layers in the model. See the [Keras activations docs](#) for more detail.
- `k_inits`=`'he_uniform'` : `{tuple, list} of str` or Keras initializer
 - Kernel initializers for the dense layers. A single string will apply the same initializer to all layers. See the [Keras initializer docs](#) for more detail.
- `dropouts`=`0` : `{tuple, list} of float`
 - Dropout rates for the dense layers. A single float will apply the same dropout rate to all layers. See the [Keras Dropout layer](#) for more detail.
- `l2_regs`=`0` : `{tuple, list} of float`



Closure test for unfolding

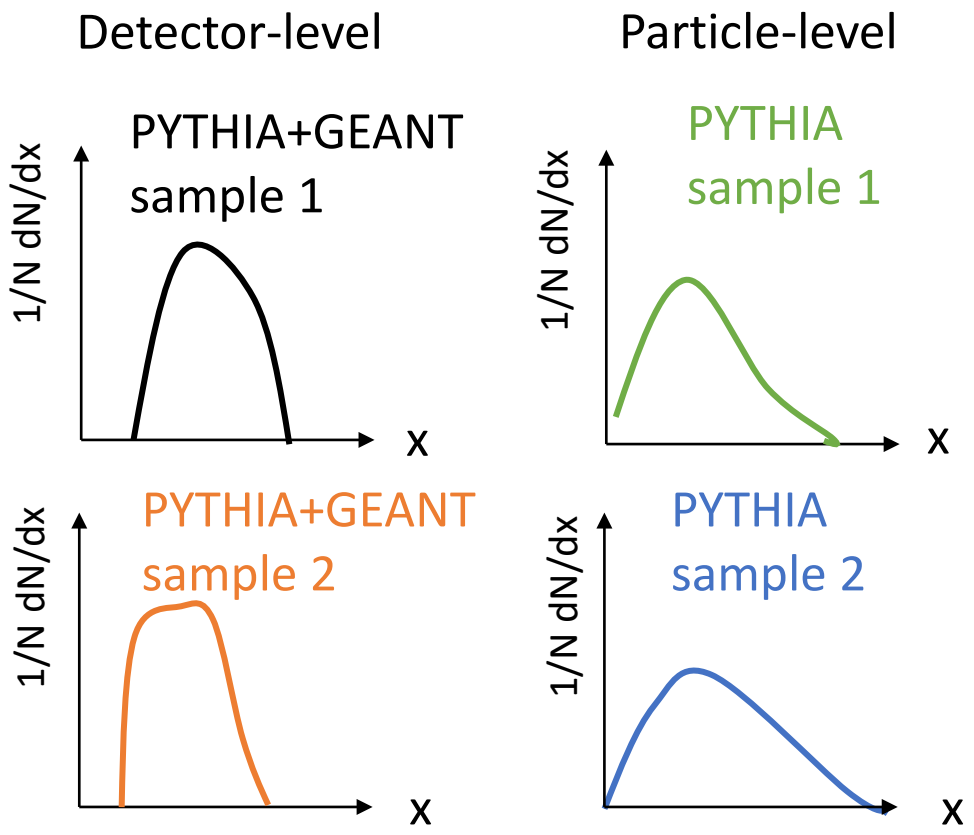
- Step 1: Separate matched jets from PYTHIA and PYTHIA+GEANT into 2 samples



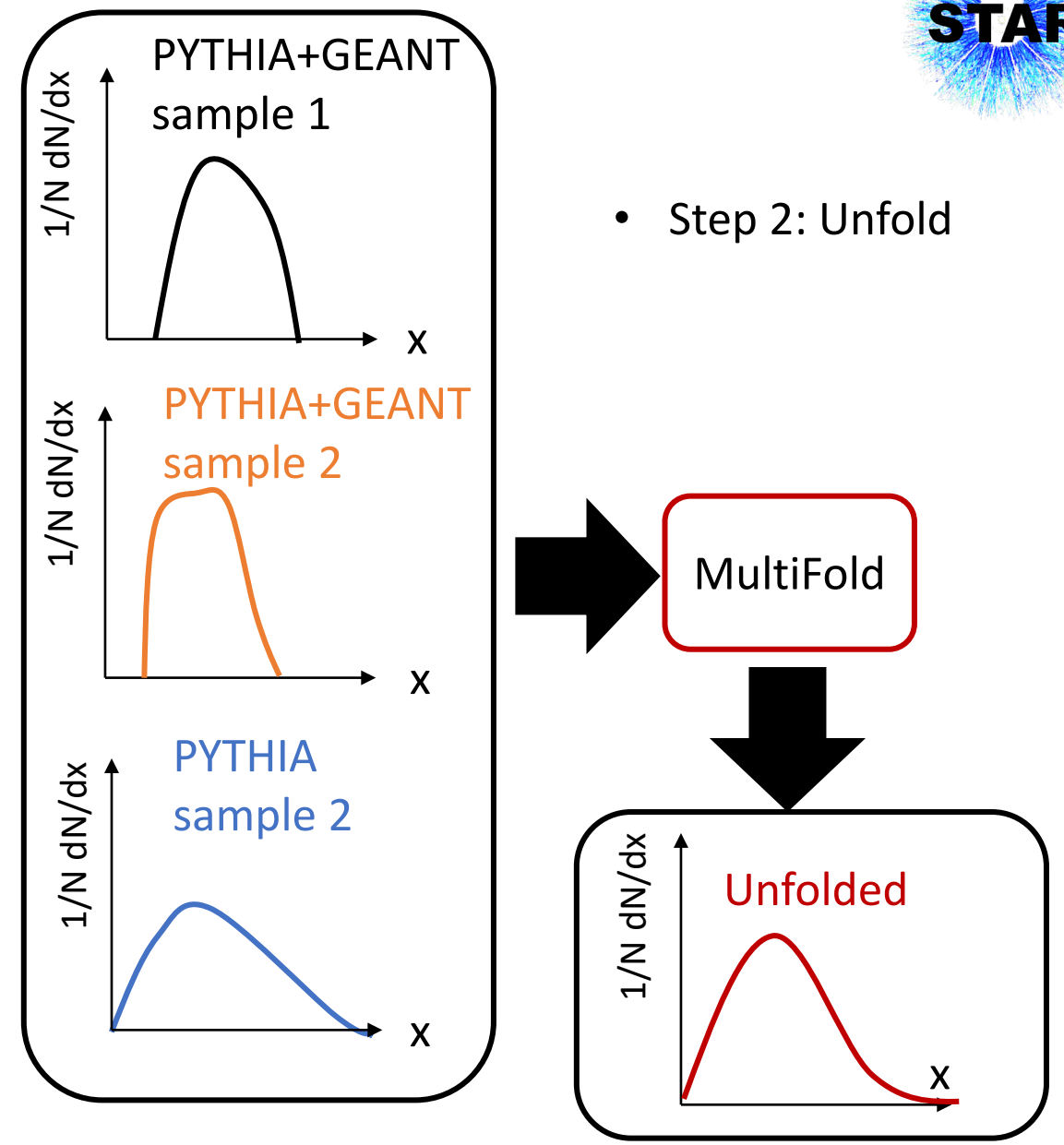


Closure test for unfolding

- Step 1: Separate matched jets from PYTHIA and PYTHIA+GEANT into 2 samples

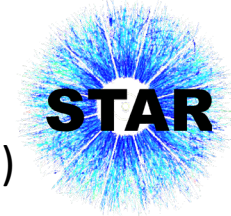


DNP, 10/29/22



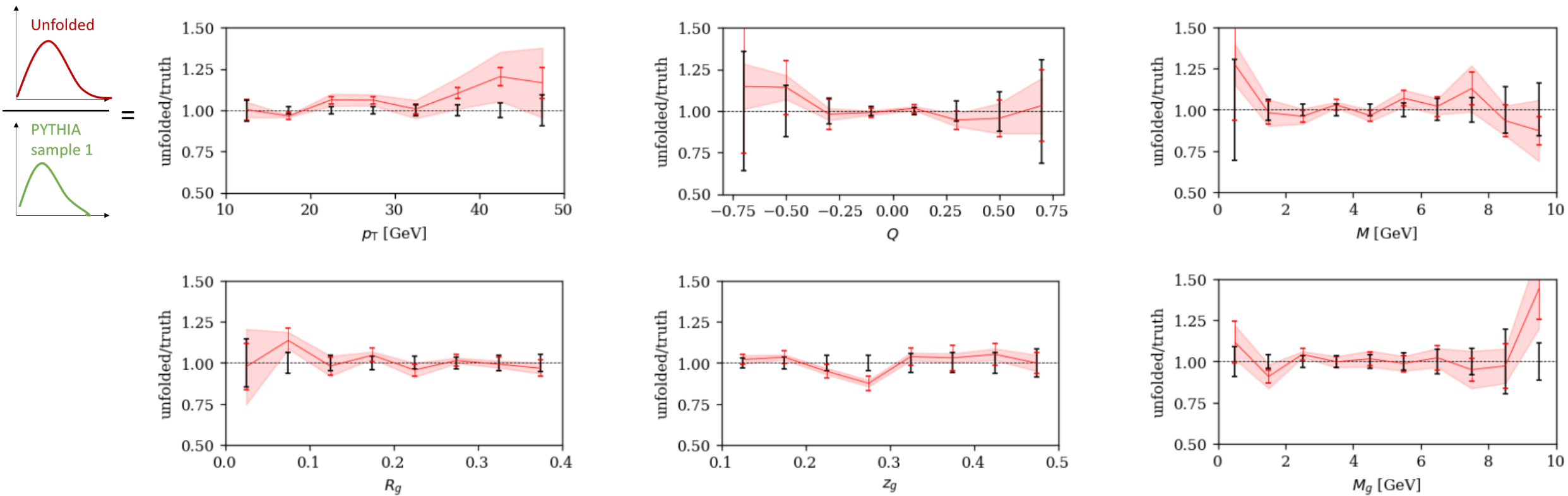
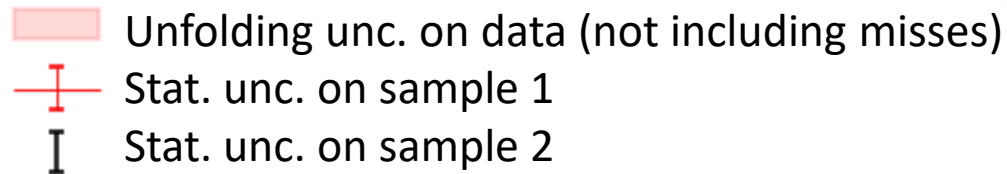
- Step 2: Unfold

Youqi Song



Closure test for unfolding: results

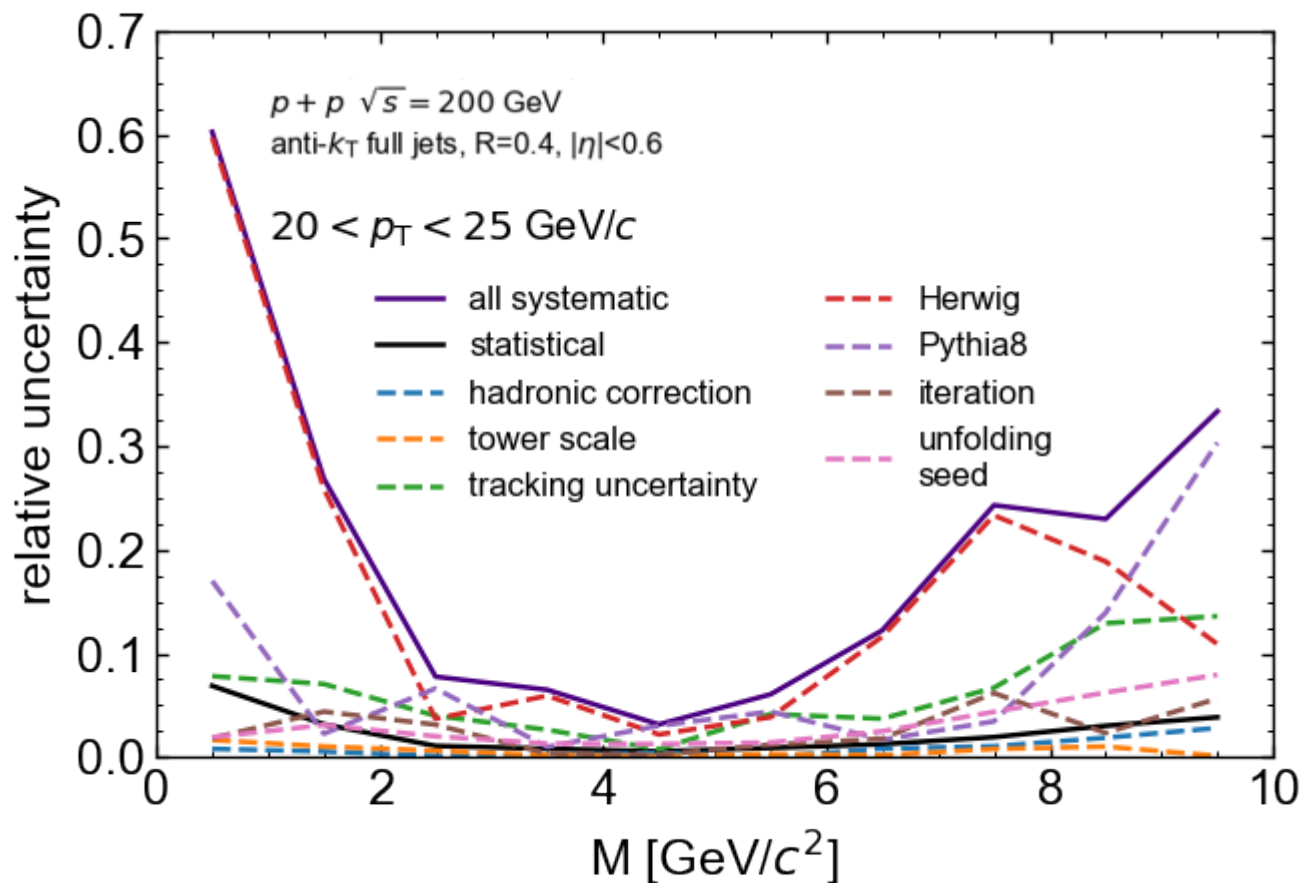
- Decent **closure** for all substructure observables



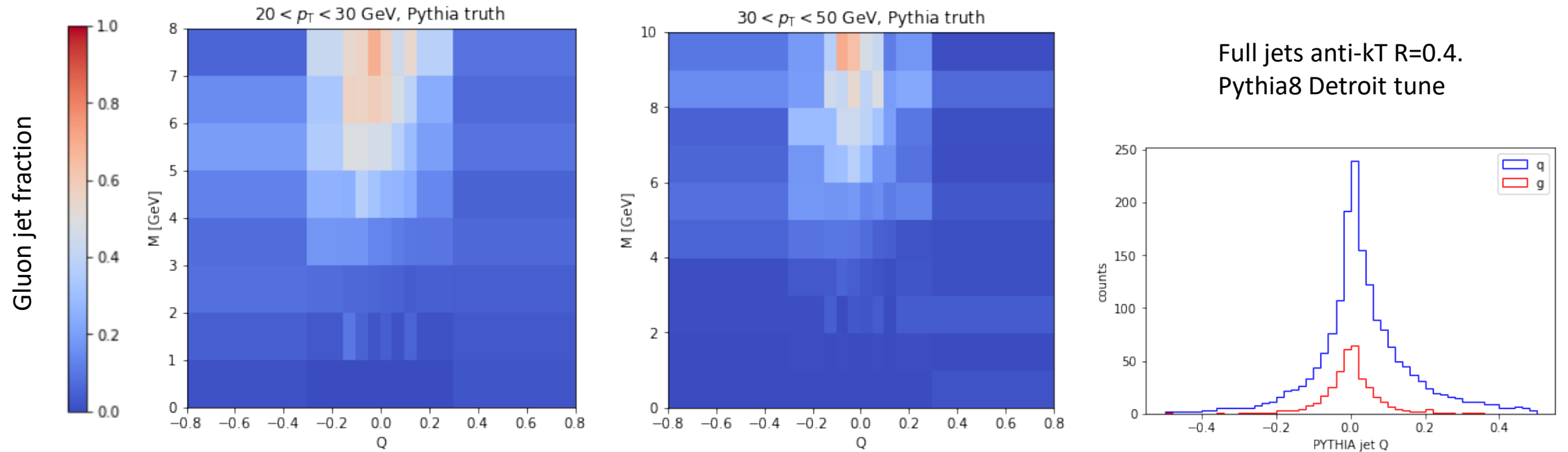


Systematic uncertainties

- Detector uncertainties (correlated with RooUnfold)
 - Hadronic correction 100% -> 50%
 - Tower scale +3.8%
 - Tracking efficiency -4%
- Unfolding uncertainties
 - Prior shape variation: Reweight jet mass distributions by HERWIG7 (LHC-UE-EE-4-CTEQ6L1 tune) and PYTHIA8 (Detroit tune)
 - Unfolding seed variation: Due to randomization of the initial weights
 - Iteration number variation



What's the best purity we can achieve for q vs g separation?



- In $20 < p_T < 30$ GeV, **gluon fraction** ~ 35%
- To select a jet population with **gluon fraction** = 67%, cut on $-0.025 < Q < 0$ AND $M > 7$ GeV. (1.1% of all jets).
 - If we only cut on $M > 7$ GeV, **gluon fraction** = 58%. (Although we will have higher statistics).
 - If we want to reach **gluon fraction** = 67% with just a M cut, need $M > 8.6$ GeV. (0.8% of all jets).
- In $30 < p_T < 50$ GeV, **gluon fraction** ~ 20%
- To select a jet population with **gluon fraction** = 65%, cut on $-0.08 < Q < -0.01$ AND $M > 9$ GeV. (1.1%).
 - No cut on jet M/Q alone can achieve such a purity.