

Novel approach to jet substructure measurement in pp collisions at $\sqrt{s} = 200$ GeV in STAR

Youqi Song (youqi.song@yale.edu) for the STAR Collaboration

Hot Quarks 2022, Estes Park, Colorado

10/15/2022



Supported in part by
U.S. DEPARTMENT OF
ENERGY

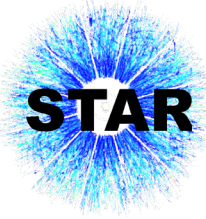
Office of
Science

Hot Quarks
2022

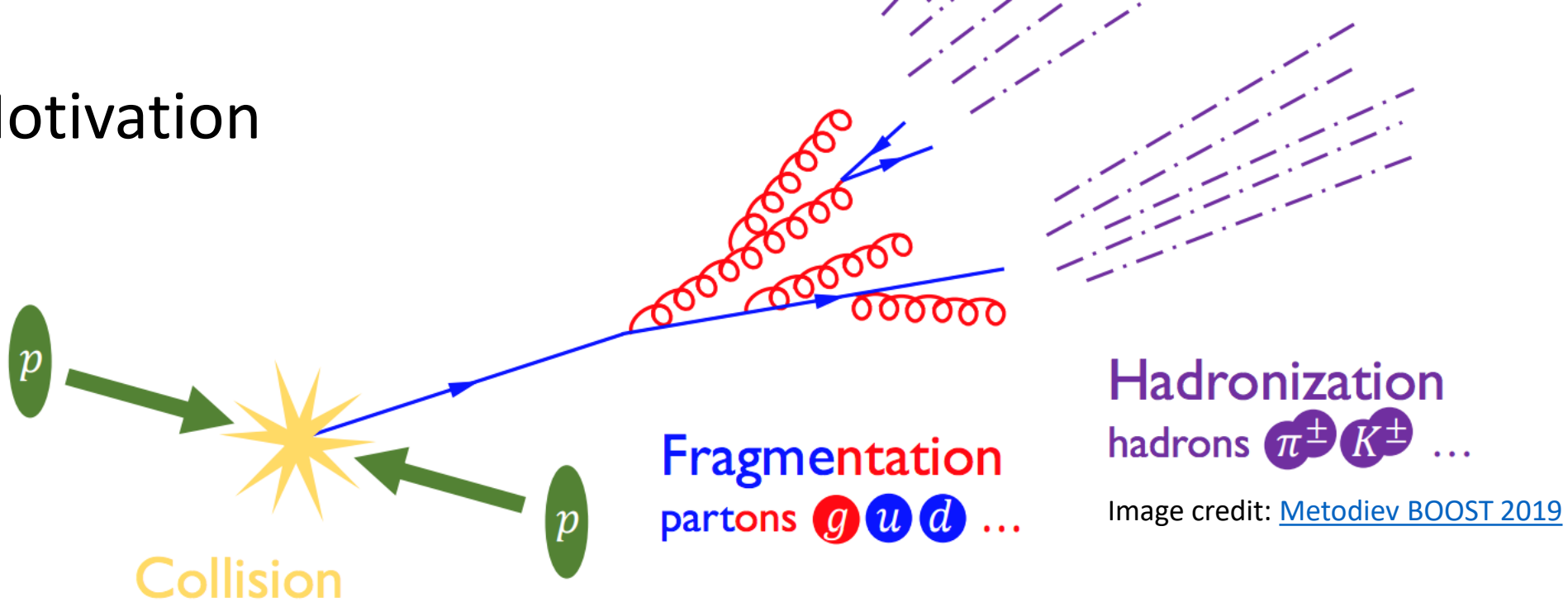
ROCKY MNT ADVENTURES

Get your QCD scout badge!



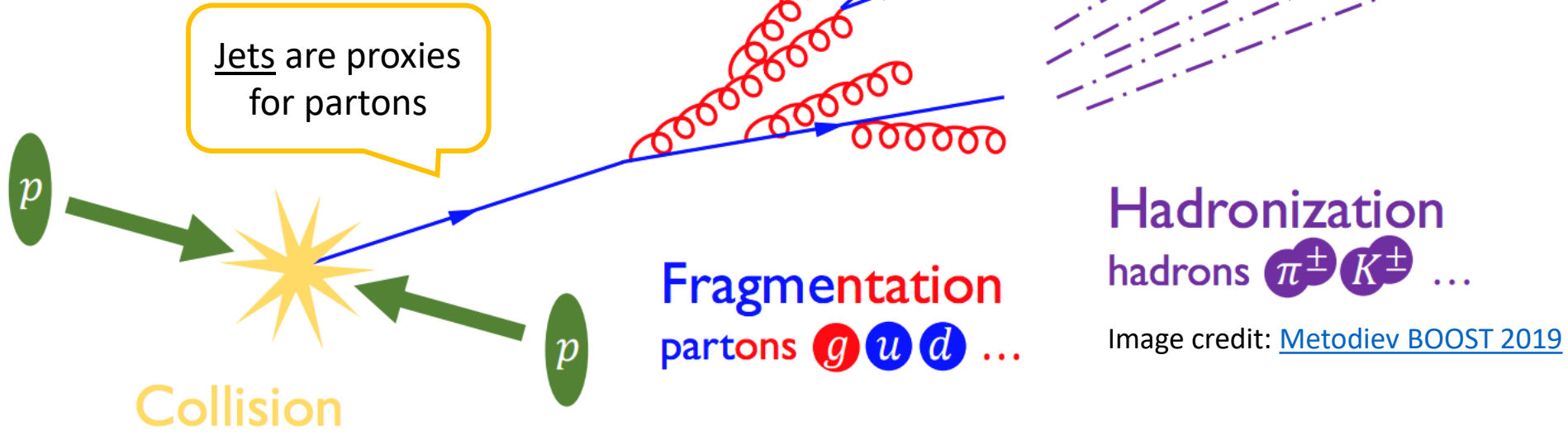


Motivation

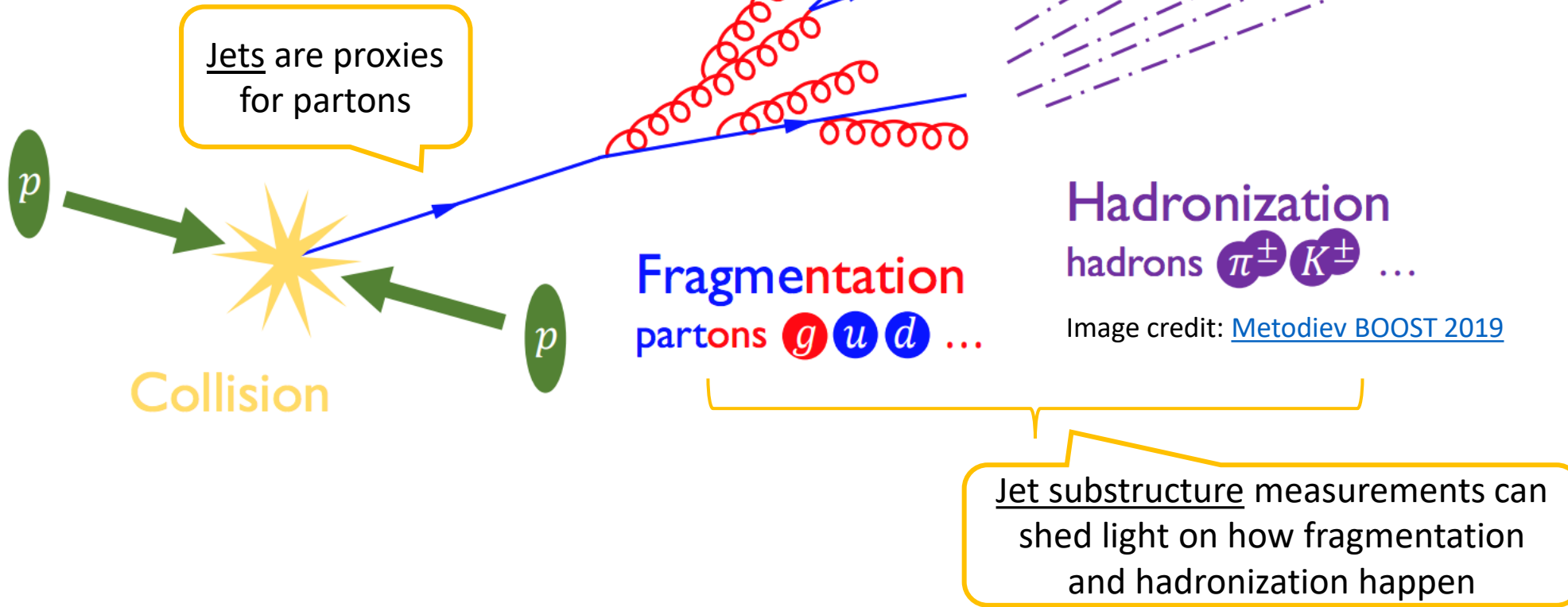




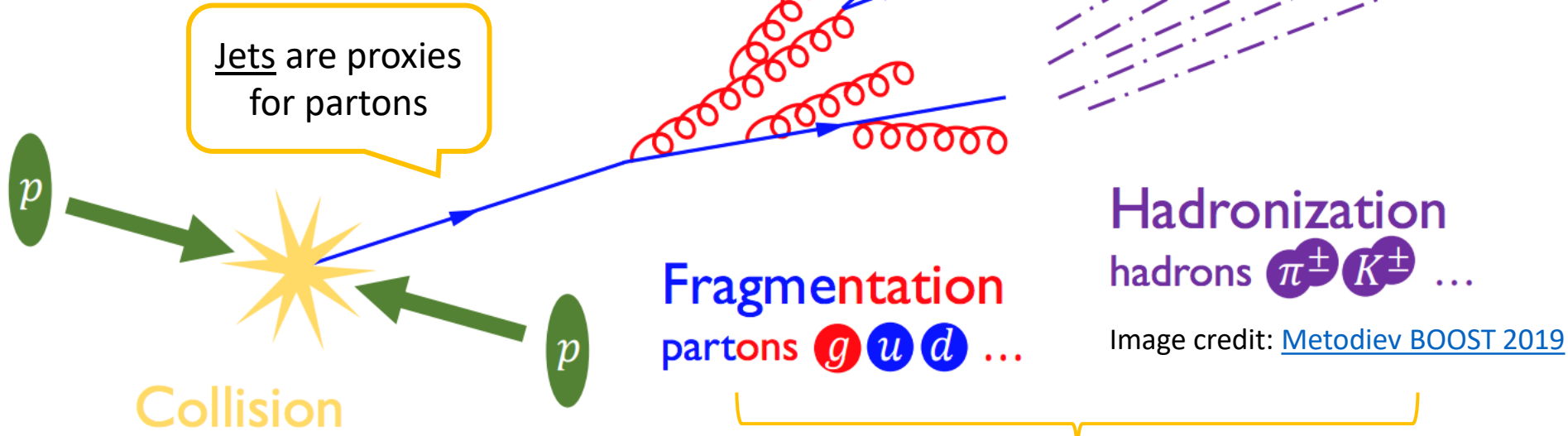
Motivation



Motivation

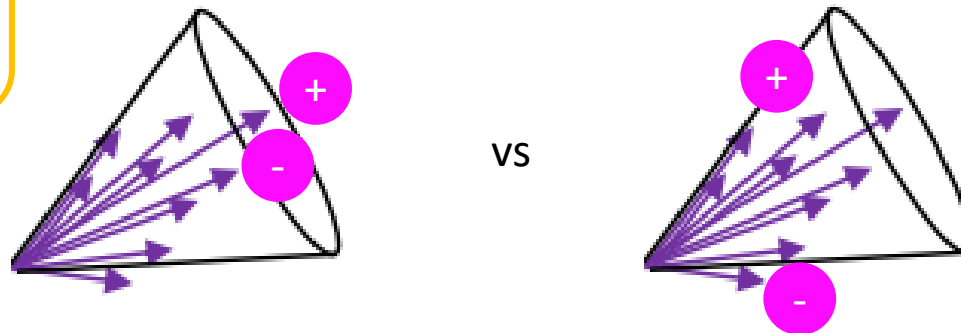


Motivation



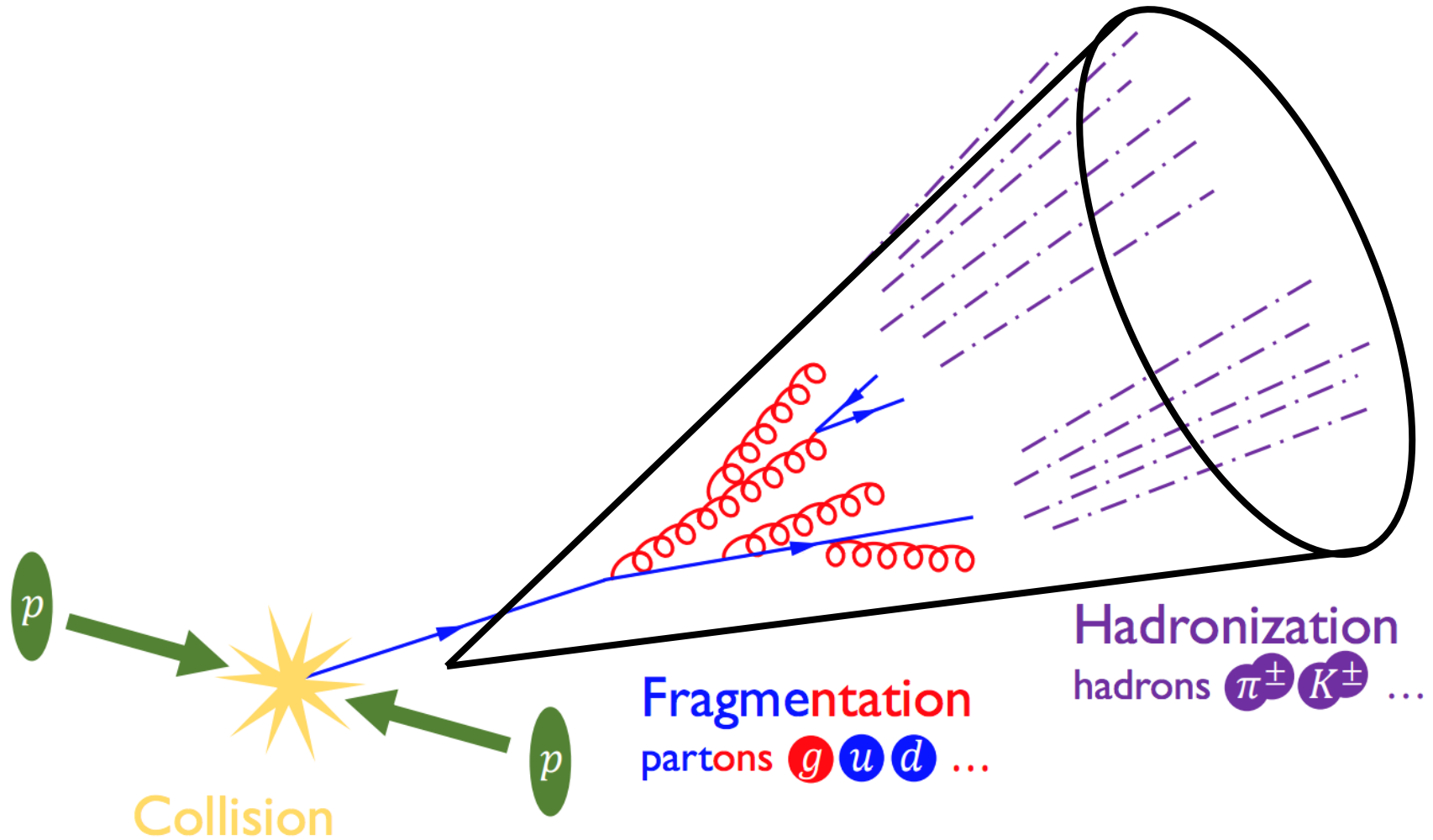
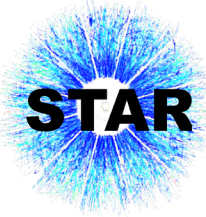
Multi-dimensional jet substructure measurements help us distinguish different fragmentation patterns

Jet substructure measurements can shed light on how fragmentation and hadronization happen

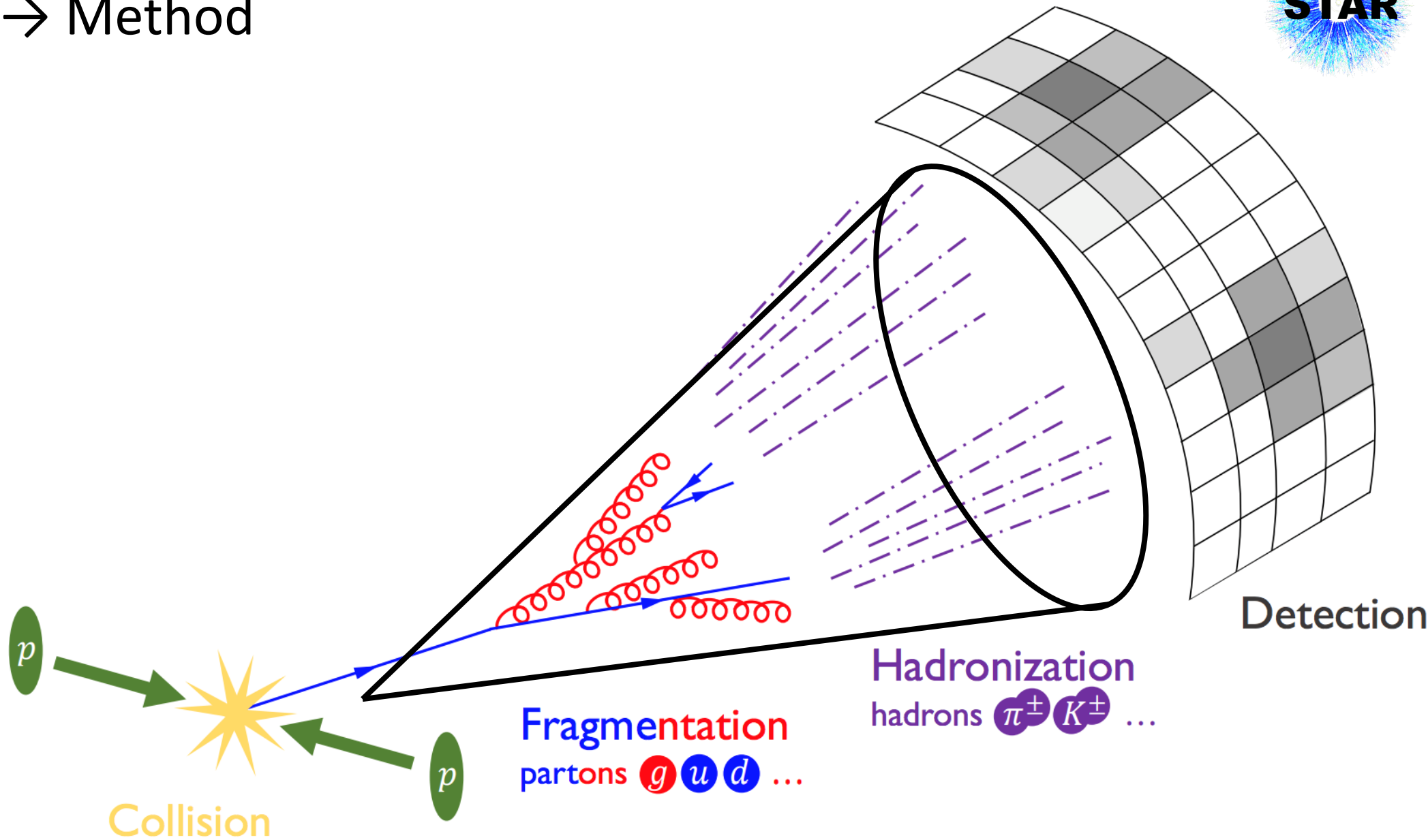


Same jet mass,
Different p_T -weighted jet charge

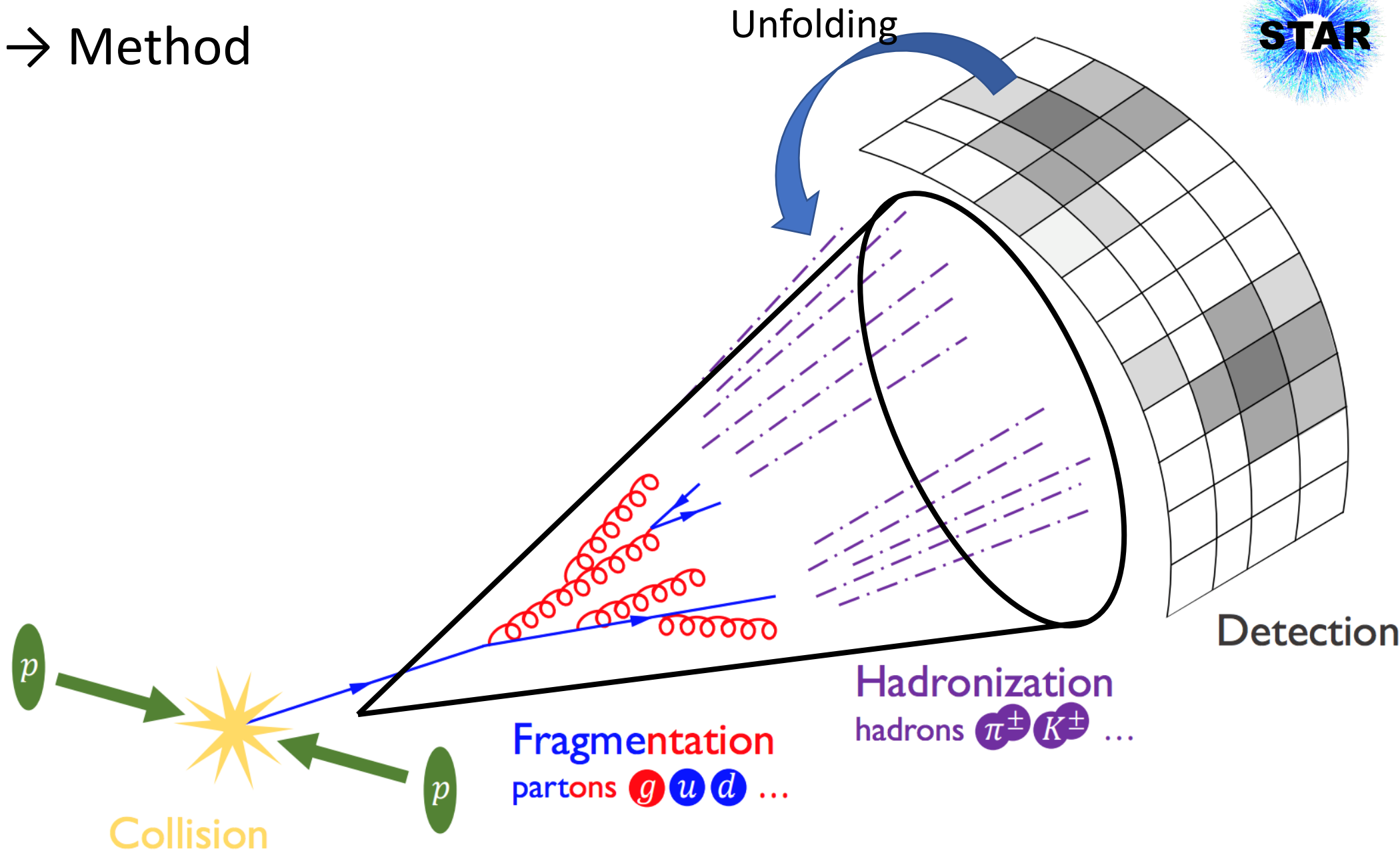
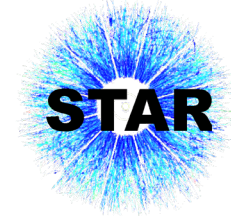
Motivation → Method

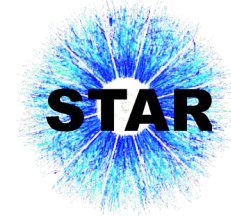


Motivation → Method



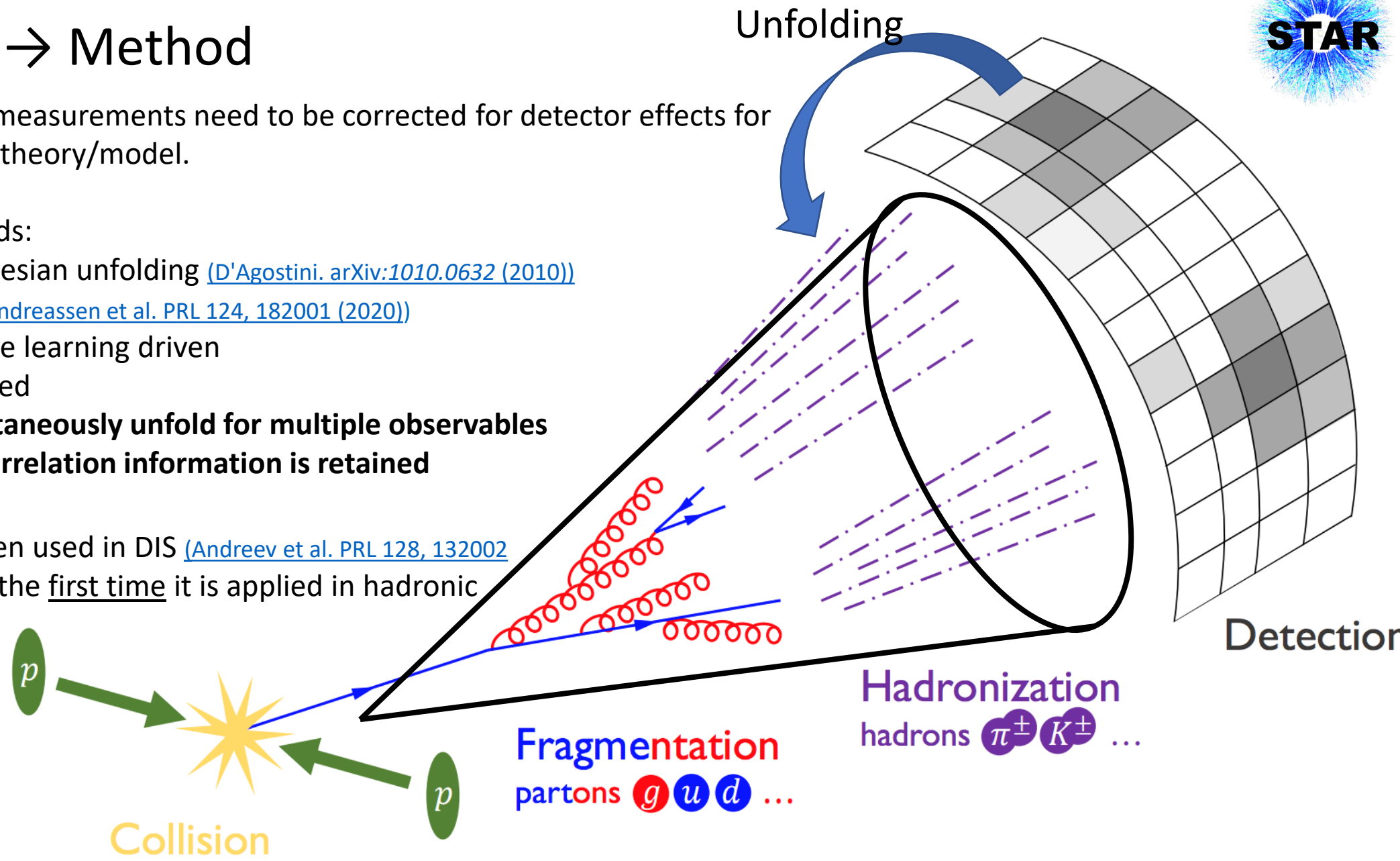
Motivation → Method

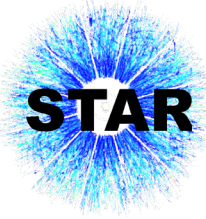




Motivation → Method

- Jet substructure measurements need to be corrected for detector effects for comparison with theory/model.
- Unfolding methods:
 - Iterative Bayesian unfolding ([D'Agostini. arXiv:1010.0632 \(2010\)](#))
 - **MultiFold** ([Andreassen et al. PRL 124, 182001 \(2020\)](#))
 - Machine learning driven
 - Unbinned
 - **Simultaneously unfold for multiple observables**
 - **Correlation information is retained**
- MultiFold has been used in DIS ([Andreev et al. PRL 128, 132002 \(2022\)](#)), but this is the first time it is applied in hadronic collision data.





Observables

- p_T : transverse momentum

- $Q^\kappa = \frac{1}{(p_{T\text{jet}})^\kappa} \sum_{i \in \text{jet}} q_i \cdot (p_{Ti})^\kappa \rightarrow$ Choose $K=2$

- $M = |\sum_{i \in \text{jet}} p_i| = \sqrt{E^2 - |\vec{p}|^2}$
4-momentum of the constituent i

Observables

- p_T : transverse momentum

- $Q^\kappa = \frac{1}{(p_{T\text{jet}})^\kappa} \sum_{i \in \text{jet}} q_i \cdot (p_{Ti})^\kappa \rightarrow$ Choose $K=2$

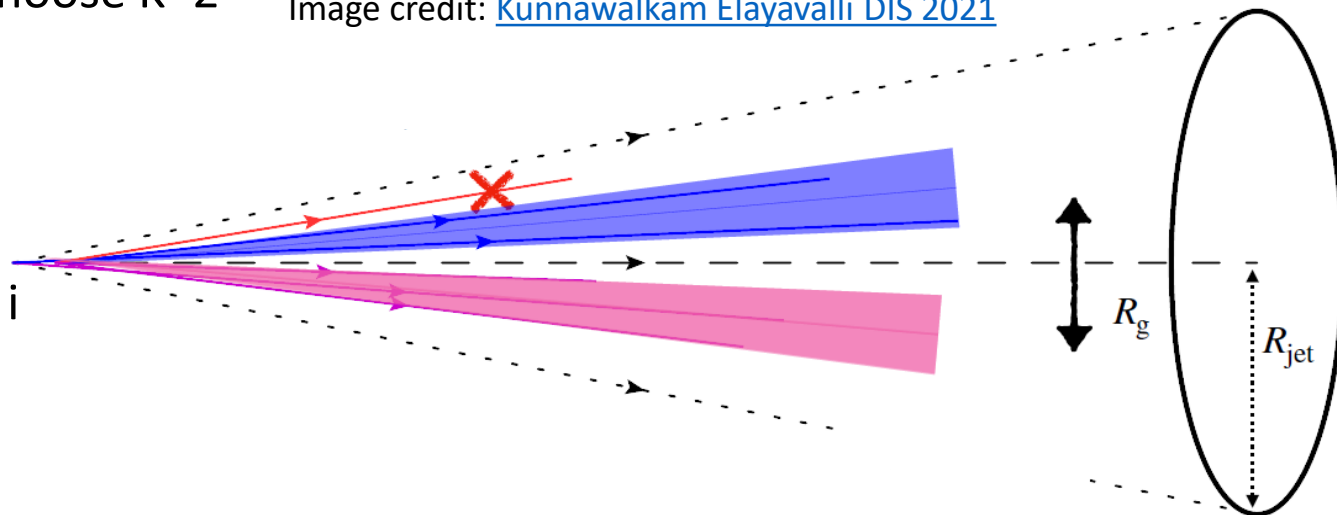
- $M = |\sum_{i \in \text{jet}} p_i| = \sqrt{E^2 - |\vec{p}|^2}$
 4-momentum of the constituent i

SoftDrop grooming

[Larkoski, et al. JHEP 2014, 146 \(2014\).](#)

[Dasgupta et al. JHEP 2013, 29 \(2013\).](#)

Image credit: [Kunnawalkam Elayavalli DIS 2021](#)



Require subjet momentum fraction to pass

$$z_g = \frac{\min(p_{T,1}, p_{T,2})}{p_{T,1} + p_{T,2}} > z_{\text{cut}} (R_g/R_{\text{jet}})^\beta$$

$$z_{\text{cut}} = 0.1$$

$$\beta = 0$$

Observables

- p_T : transverse momentum

- $Q^\kappa = \frac{1}{(p_{T\text{jet}})^\kappa} \sum_{i \in \text{jet}} q_i \cdot (p_{Ti})^\kappa \rightarrow$ Choose $K=2$

- $M = |\sum_{i \in \text{jet}} p_i| = \sqrt{E^2 - |\vec{p}|^2}$
4-momentum of the constituent i

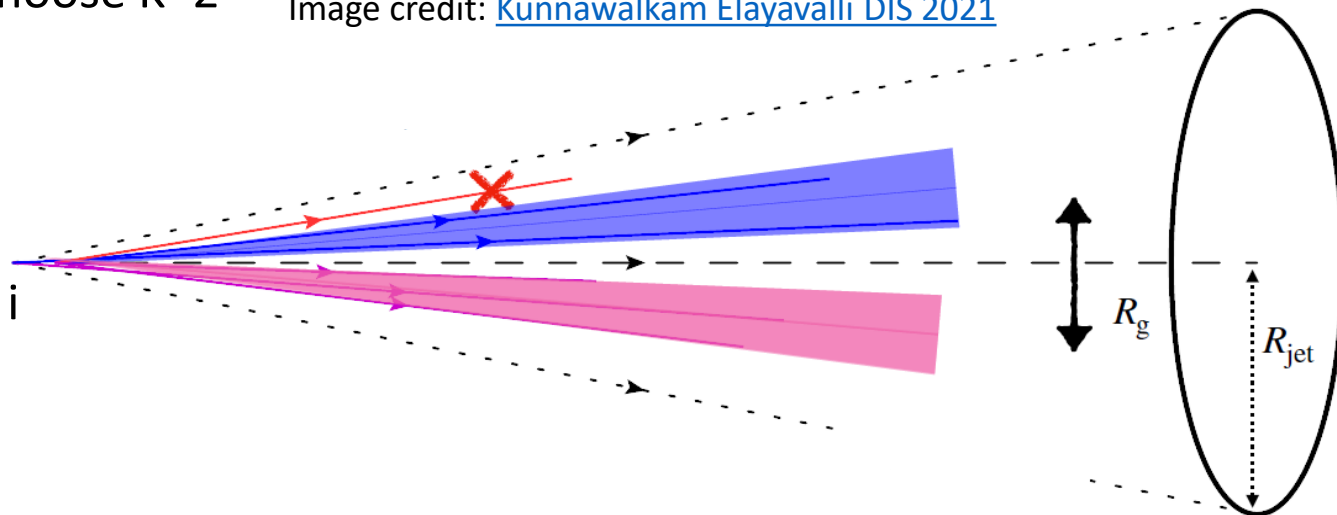
- R_g : groomed jet radius
- z_g : shared momentum fraction
- M_g : groomed jet mass

SoftDrop grooming

[Larkoski, et al. JHEP 2014, 146 \(2014\).](#)

[Dasgupta et al. JHEP 2013, 29 \(2013\).](#)

Image credit: [Kunnawalkam Elayavalli DIS 2021](#)



Require subjet momentum fraction to pass

$$z_g = \frac{\min(p_{T,1}, p_{T,2})}{p_{T,1} + p_{T,2}} > z_{\text{cut}} (R_g / R_{\text{jet}})^\beta$$

$$z_{\text{cut}} = 0.1$$

$$\beta = 0$$

Observables

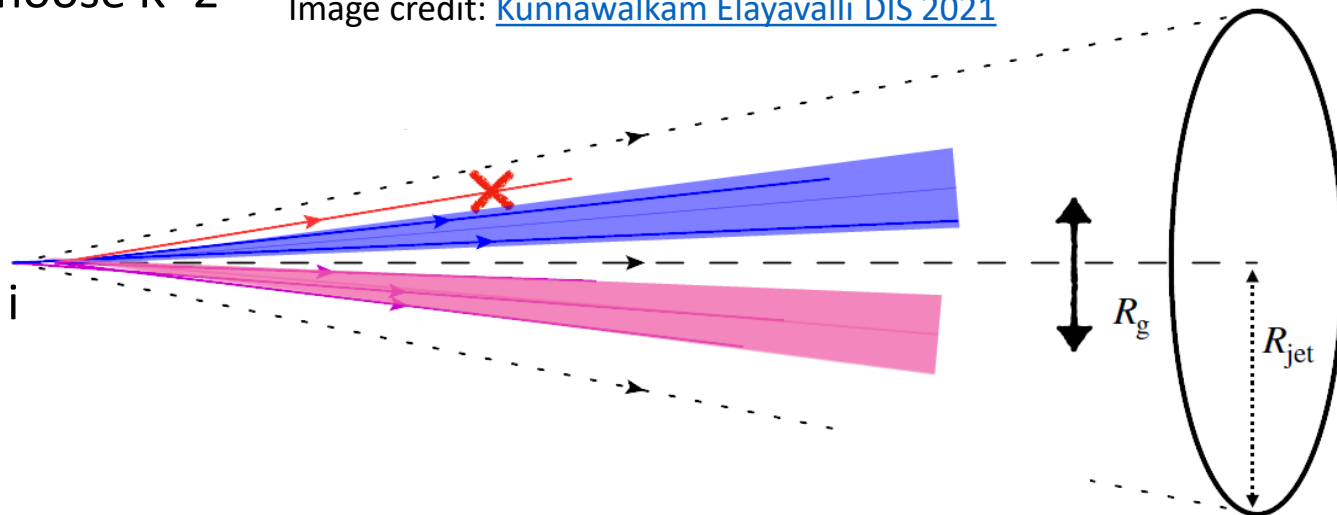
- p_T : transverse momentum
- $Q^\kappa = \frac{1}{(p_{T\text{jet}})^\kappa} \sum_{i \in \text{jet}} q_i \cdot (p_{Ti})^\kappa \rightarrow$ Choose $\kappa=2$
- $M = |\sum_{i \in \text{jet}} p_i| = \sqrt{E^2 - |\vec{p}|^2}$
↙
 4-momentum of the constituent i
- R_g : groomed jet radius
- z_g : shared momentum fraction
- M_g : groomed jet mass

SoftDrop grooming

[Larkoski, et al. JHEP 2014, 146 \(2014\).](#)

[Dasgupta et al. JHEP 2013, 29 \(2013\).](#)

Image credit: [Kunnawalkam Elayavalli DIS 2021](#)



Require subjet momentum fraction to pass

$$z_g = \frac{\min(p_{T,1}, p_{T,2})}{p_{T,1} + p_{T,2}} > z_{\text{cut}} (R_g / R_{\text{jet}})^\beta$$

$$z_{\text{cut}} = 0.1$$

$$\beta = 0$$

All 6 observables are simultaneously unfolded in an unbinned way!

Observables

- All 6 observables are **simultaneously unfolded!**
- Unfolding is **unbinned**. Binning is chosen afterward for illustration.

	weight	p_T	Q^{κ}	R_g	z_g	M	M_g
0	0.001282	12.478762	-0.340979	0.116877	0.363053	2.130296	1.754463
1	0.000711	20.699182	0.060520	0.124359	0.482597	3.381928	1.409338
2	0.001819	14.479642	0.049692	0.157490	0.478144	3.463364	3.463364
...
33707	0.001054	16.891453	-0.108731	0.251257	0.153995	2.508725	2.508725

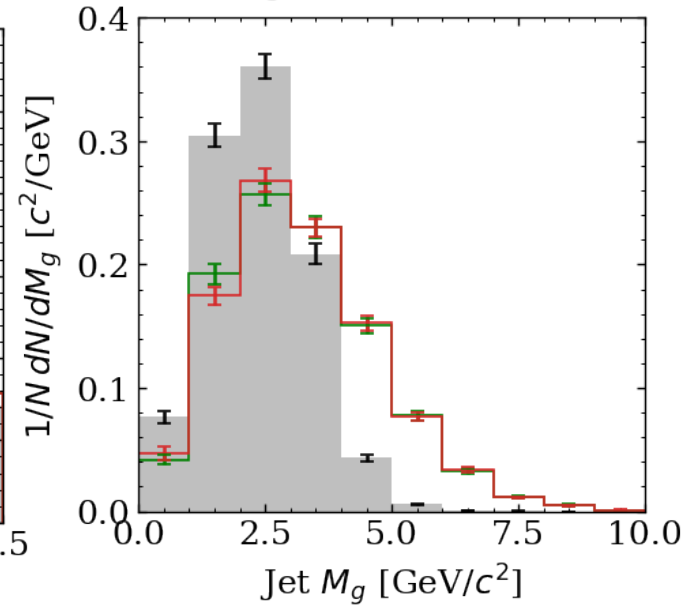
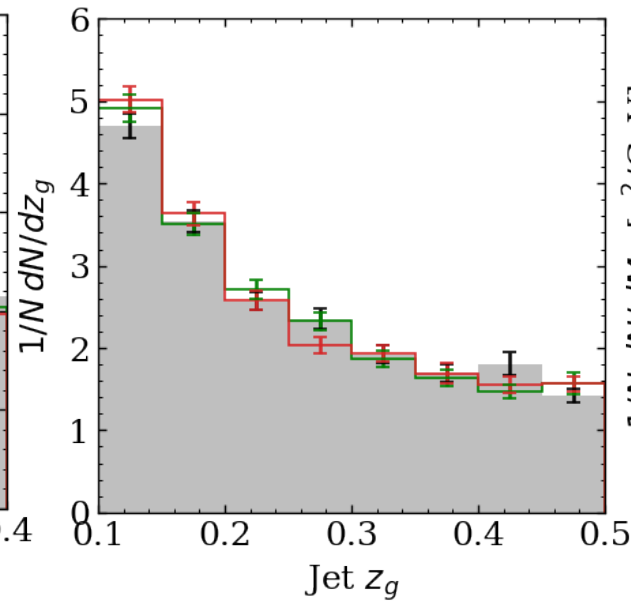
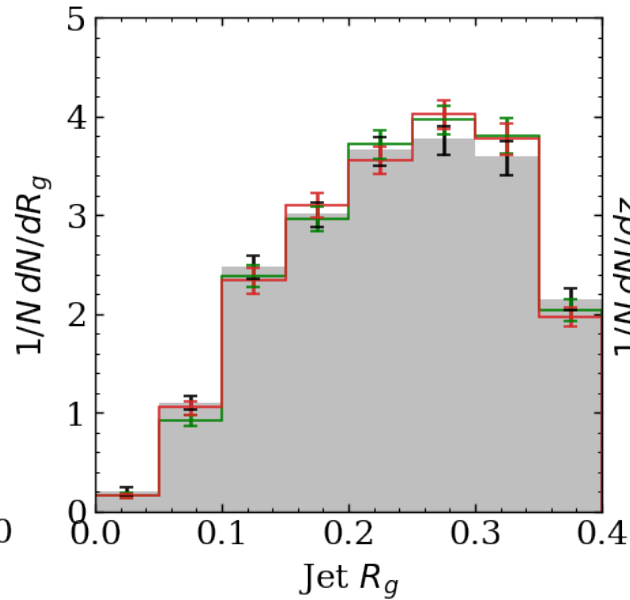
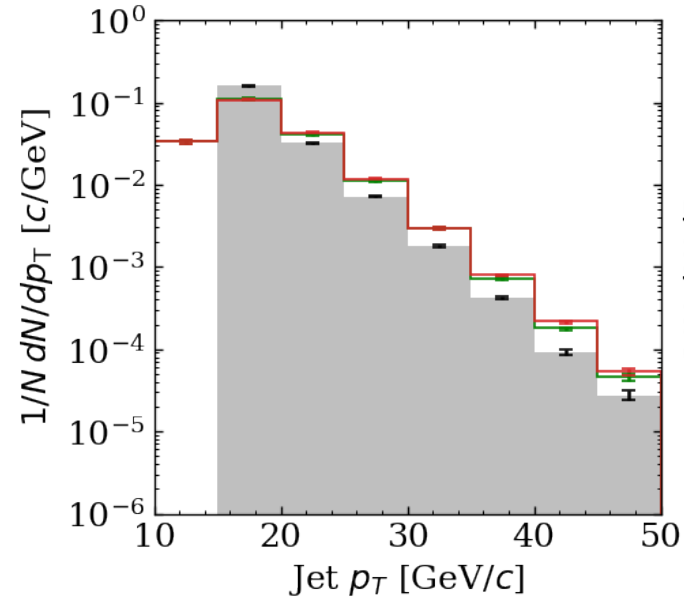
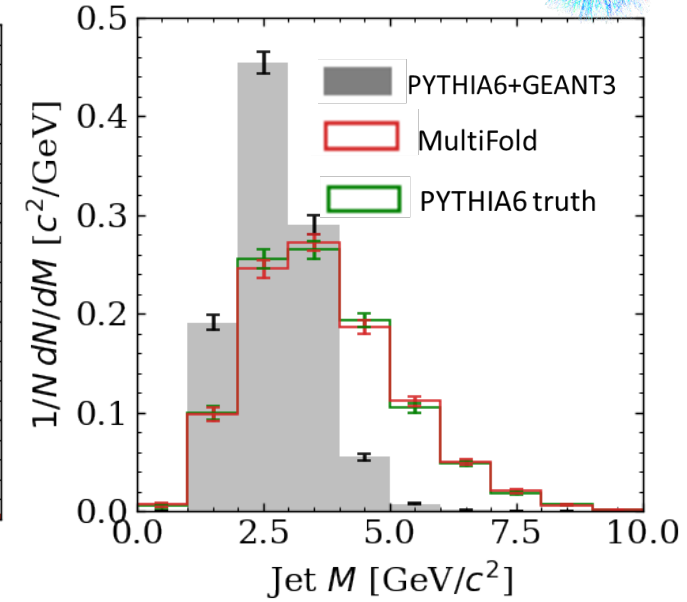
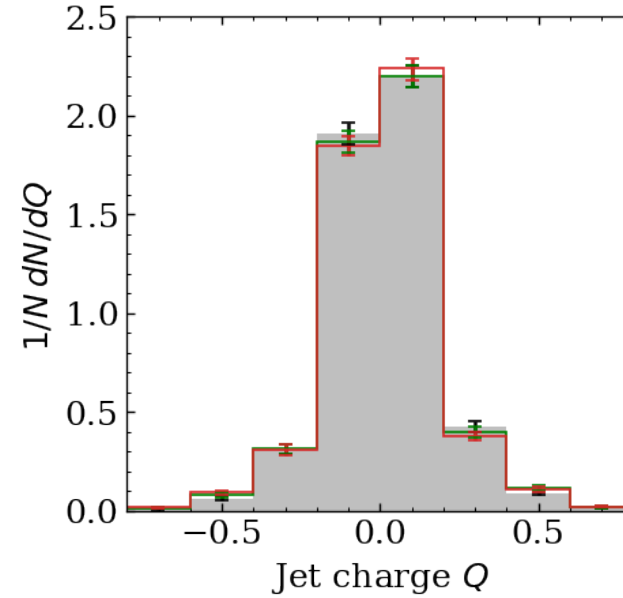


pp $\sqrt{s} = 200$ GeV

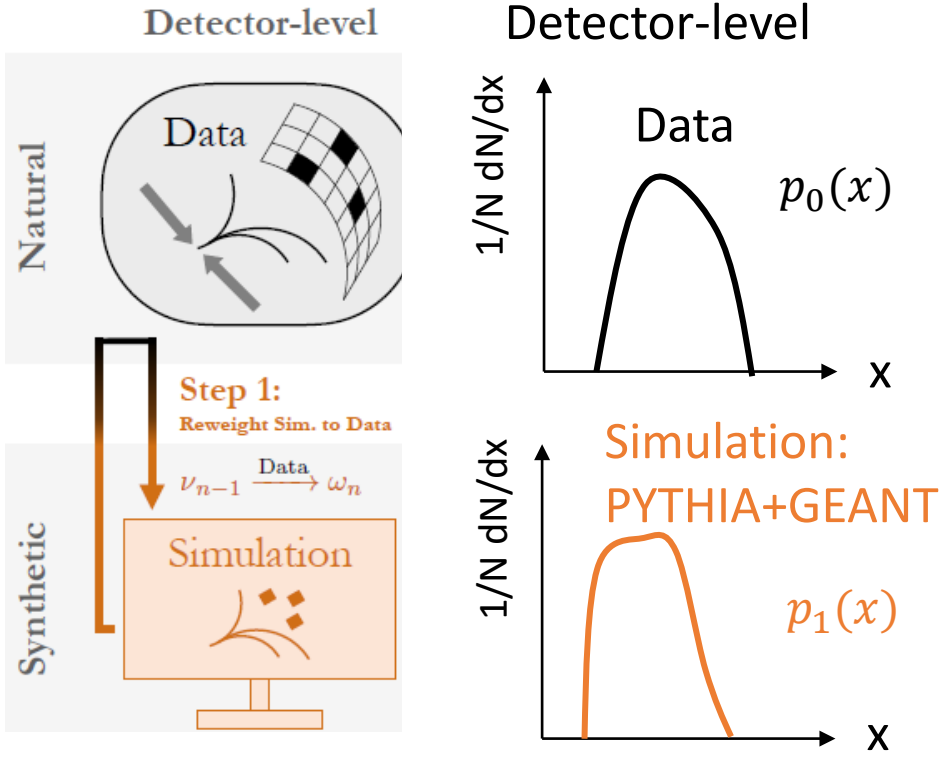
Observables

- All 6 observables are **simultaneously unfolded!**
- Unfolding is **unbinned**. Binning is chosen afterward for illustration.

	weight	p_T	Q^k	R_g	z_g	M	M_g
0	0.001282	12.478762	-0.340979	0.116877	0.363053	2.130296	1.754463
1	0.000711	20.699182	0.060520	0.124359	0.482597	3.381928	1.409338
2	0.001819	14.479642	0.049692	0.157490	0.478144	3.463364	3.463364
...
33707	0.001054	16.891453	-0.108731	0.251257	0.153995	2.508725	2.508725

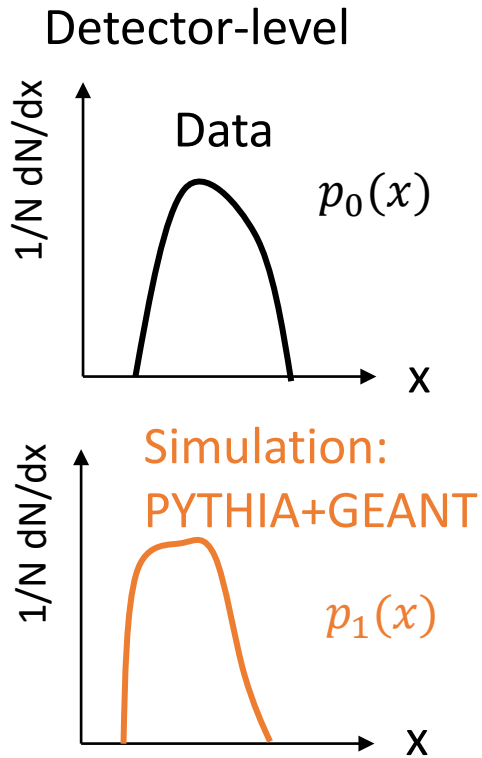
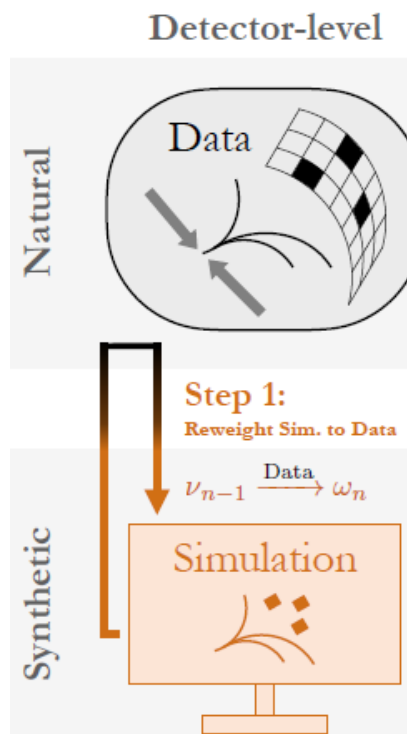


Method: machine learning



Where does the machine learning part come in?

Method: machine learning

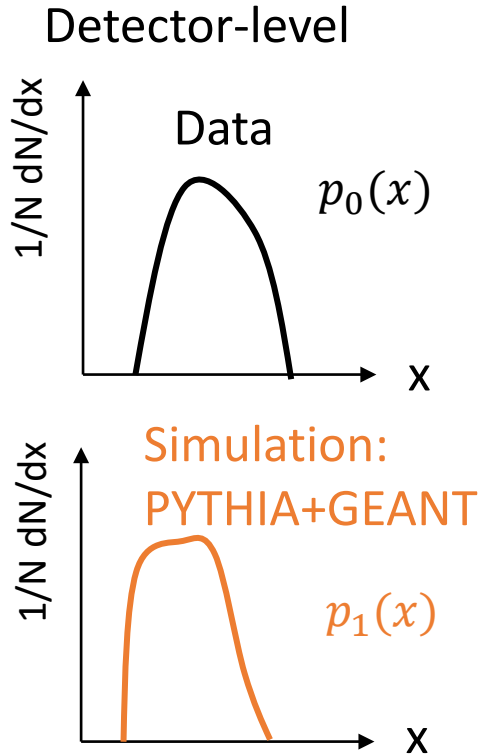
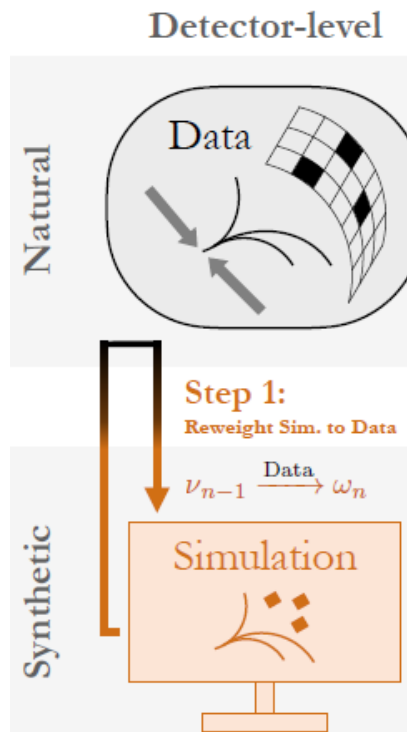


E.g., Iteration 1, step 1:

Weights: $w(x) = p_0(x)/p_1(x)$

Where does the machine learning part come in?

Method: machine learning



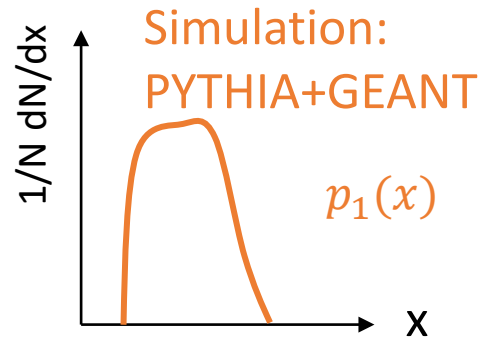
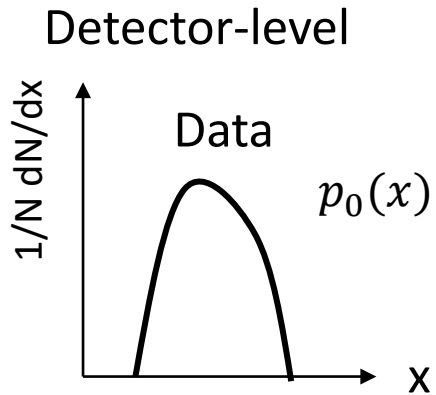
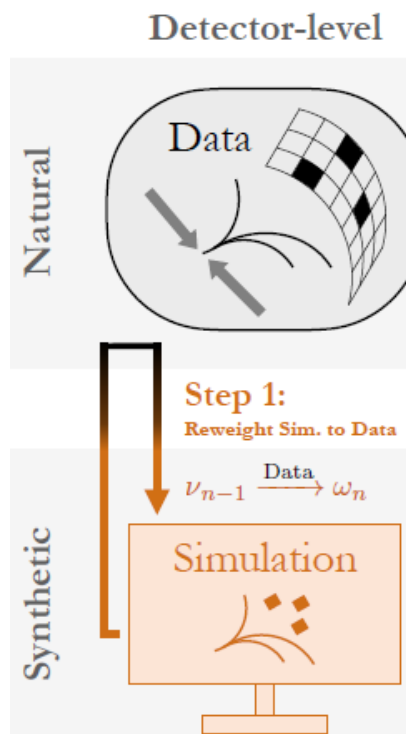
E.g., Iteration 1, step 1:

Weights: $w(x) = p_0(x)/p_1(x)$

Ok for 1D

Where does the machine learning part come in?

Method: machine learning



E.g., Iteration 1, step 1:

Weights: $w(x) = p_0(x)/p_1(x)$

Ok for 1D

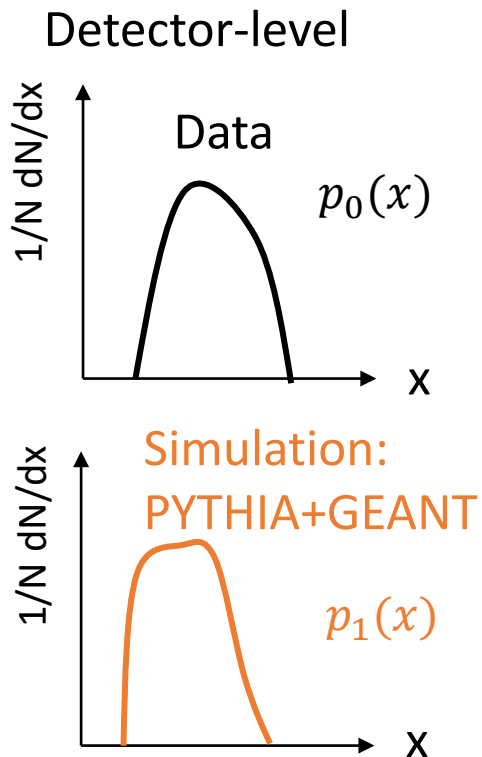
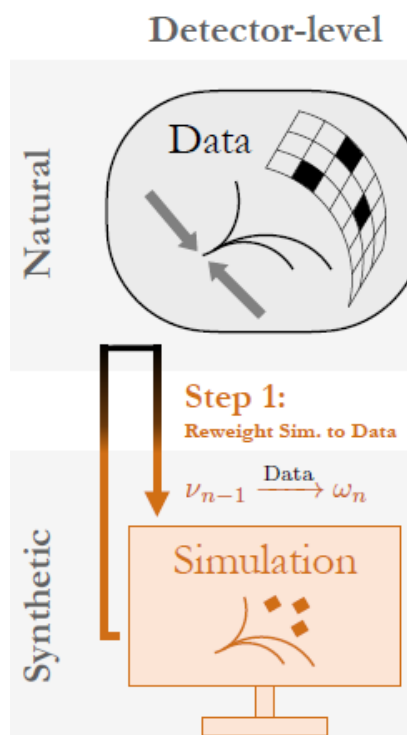
$$\approx f(x)/(1 - f(x))$$

[\(Andreassen and Nachman PRD 101, 091901 \(2020\)\)](#)

where $f(x)$ is a neural network and trained with the binary cross-entropy loss function

Where does the machine learning part come in?

Method: machine learning



E.g., Iteration 1, step 1:

Weights: $w(x) = p_0(x)/p_1(x)$

Ok for 1D

$$\approx f(x)/(1 - f(x))$$

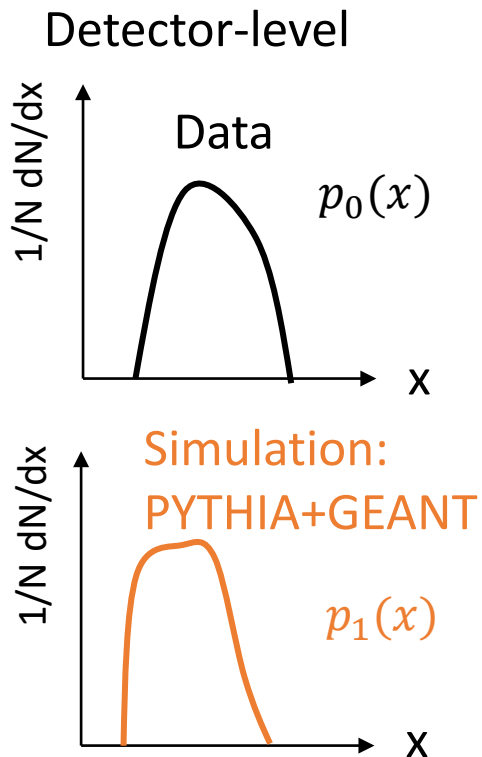
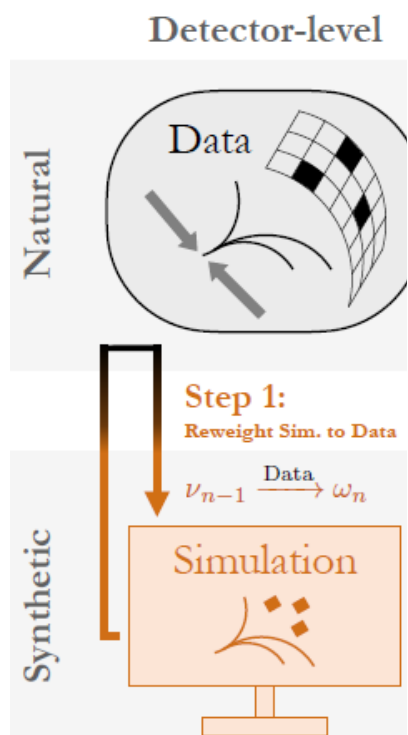
[\(Andreassen and Nachman PRD 101, 091901 \(2020\)\)](#)

where $f(x)$ is a neural network and trained with the binary cross-entropy loss function

to distinguish jets coming from data vs from simulation

Where does the machine learning part come in?

Method: machine learning



E.g., Iteration 1, step 1:

Weights: $w(x) = p_0(x)/p_1(x)$

Ok for 1D

$$\approx f(x)/(1 - f(x))$$

[\(Andreassen and Nachman PRD 101, 091901 \(2020\)\)](#)

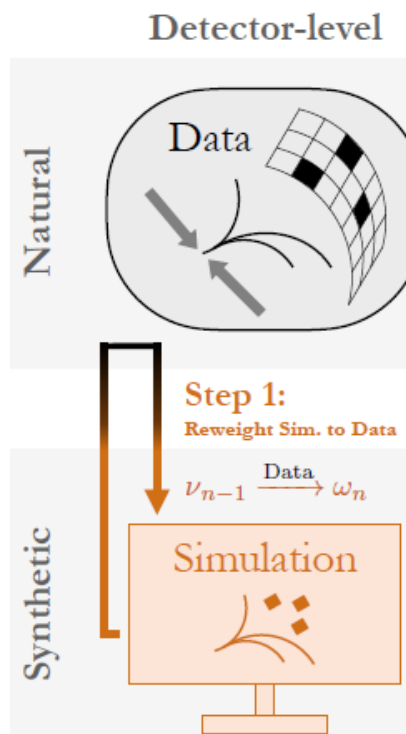
where $f(x)$ is a neural network and trained with the binary cross-entropy loss function

to distinguish jets coming from data vs from simulation

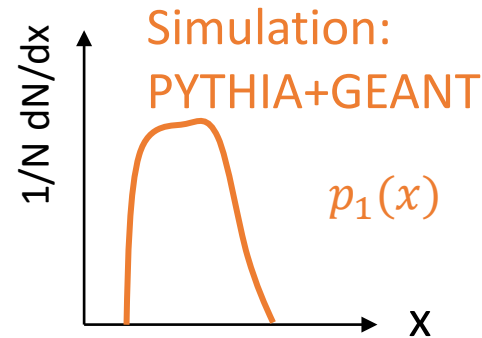
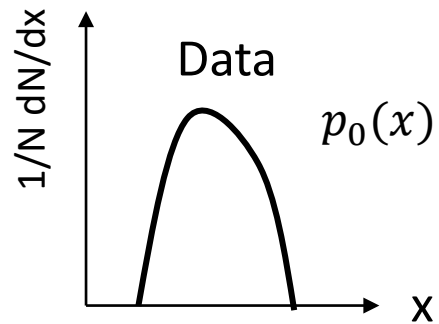
Unfolding \rightarrow Reweighting histograms \rightarrow Classification \rightarrow Neural network

Where does the machine learning part come in?

Method: machine learning



Detector-level



E.g., Iteration 1, step 1:

Weights: $w(x) = p_0(x)/p_1(x)$

Ok for 1D

$$\approx f(x)/(1 - f(x))$$

[\(Andreassen and Nachman PRD 101, 091901 \(2020\)\)](#)

where $f(x)$ is a neural network and trained with the binary cross-entropy loss function

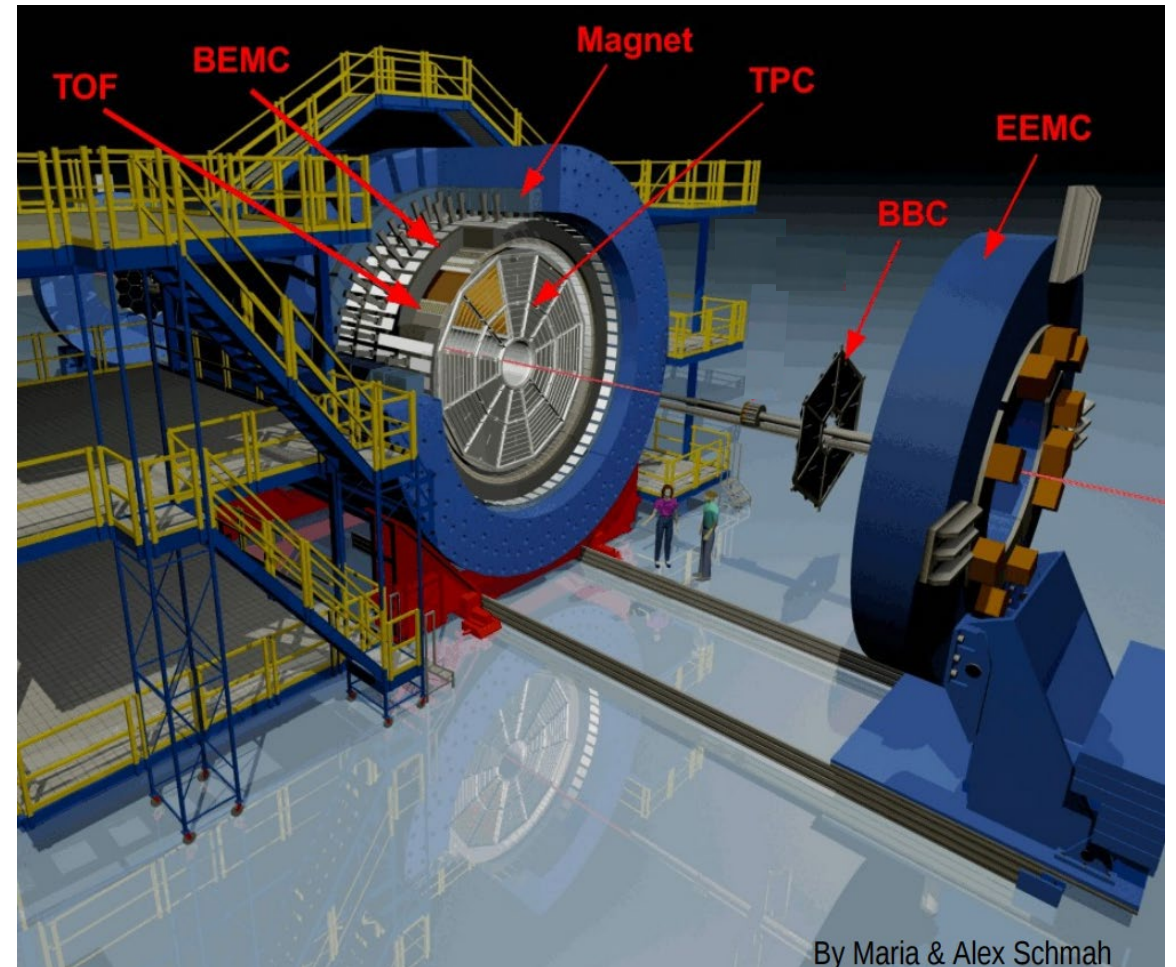
to distinguish jets coming from data vs from simulation

Unfolding \rightarrow Reweighting histograms
 \rightarrow Classification \rightarrow Neural network

See backup slides for details of the neural networks.

Where does the machine learning part come in?

Jet reconstruction at STAR

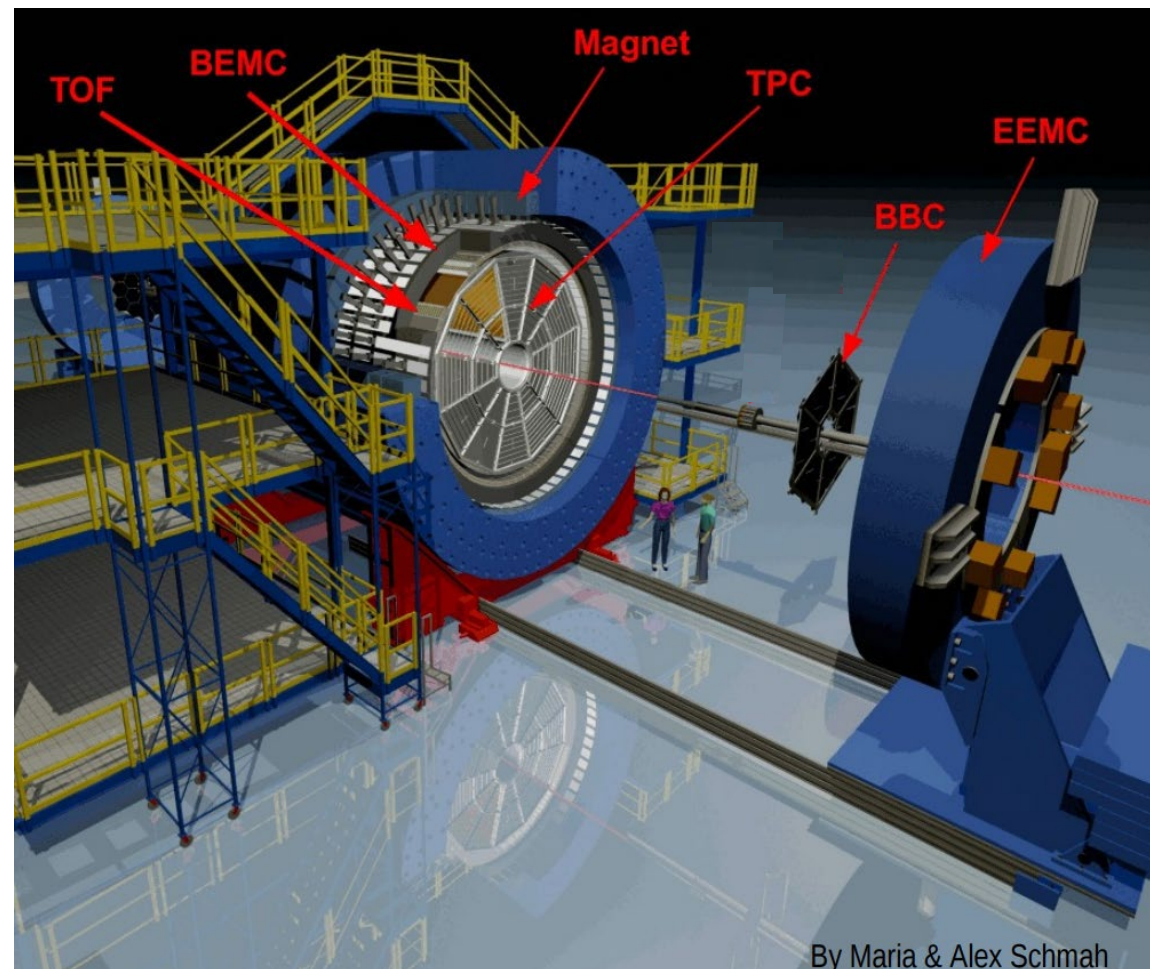


By Maria & Alex Schmah

Jet reconstruction at STAR

Important subdetectors for $pp \sqrt{s} = 200 \text{ GeV}$ collisions data-taking during 2012 RHIC run

- **TPC** (Time Projection Chamber)
 - For **charged** particle track reconstruction
 - $|\eta| < 1$, full azimuthal coverage
- **BEMC** (Barrel ElectroMagnetic Calorimeter)
 - For **neutral** energy measurement and triggering
 - $|\eta| < 1$, full azimuthal coverage
- Reconstruct anti- k_T **full jets**
 - Jet resolution parameter **R=0.4**
 - $|\eta_{\text{jet}}| < 0.6$



By Maria & Alex Schmah

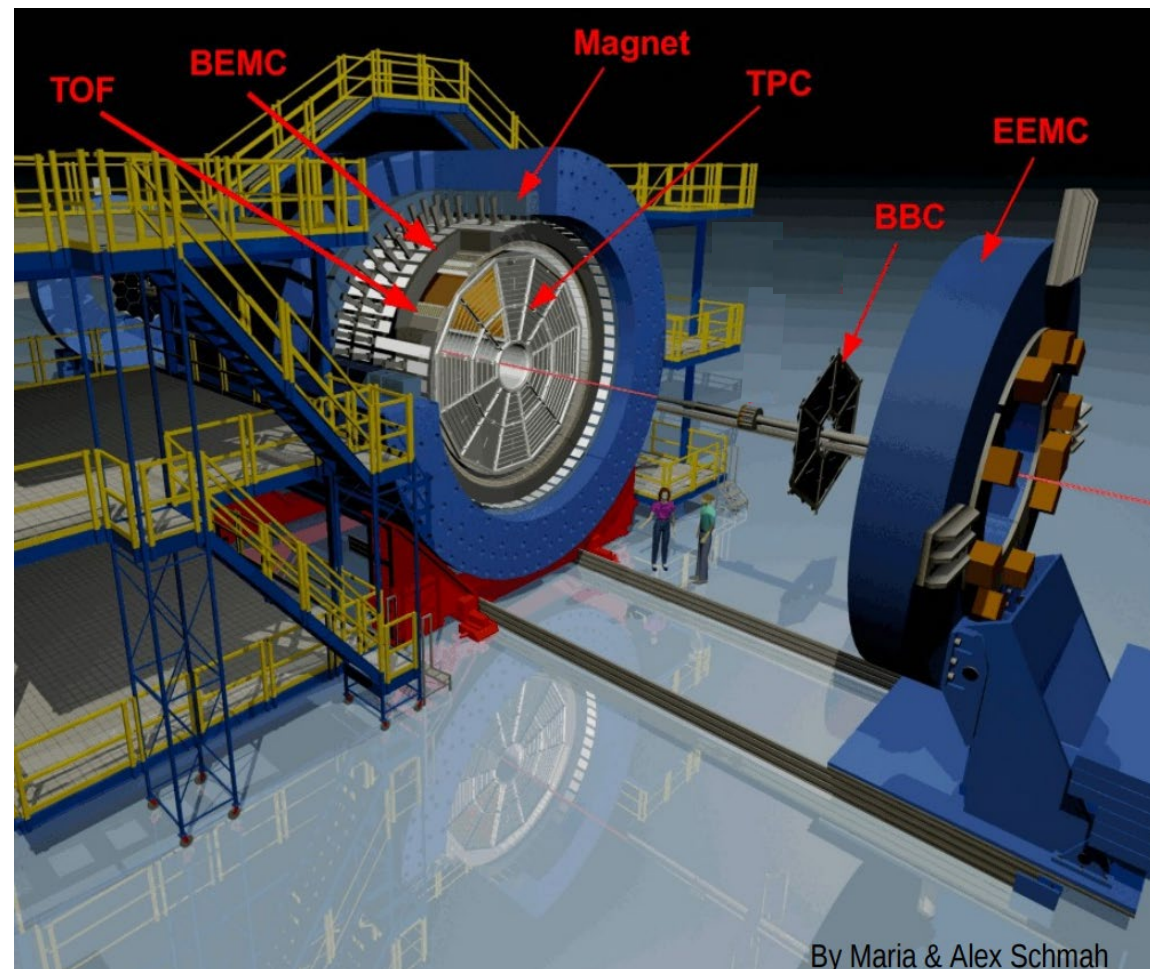
Jet reconstruction at STAR

Important subdetectors for $pp \sqrt{s} = 200 \text{ GeV}$ collisions data-taking during 2012 RHIC run

- **TPC** (Time Projection Chamber)
 - For **charged** particle track reconstruction
 - $|\eta| < 1$, full azimuthal coverage
- **BEMC** (Barrel ElectroMagnetic Calorimeter)
 - For **neutral** energy measurement and triggering
 - $|\eta| < 1$, full azimuthal coverage
- Reconstruct anti- k_T **full jets**
 - Jet resolution parameter **R=0.4**
 - $|\eta_{\text{jet}}| < 0.6$

Additional selections

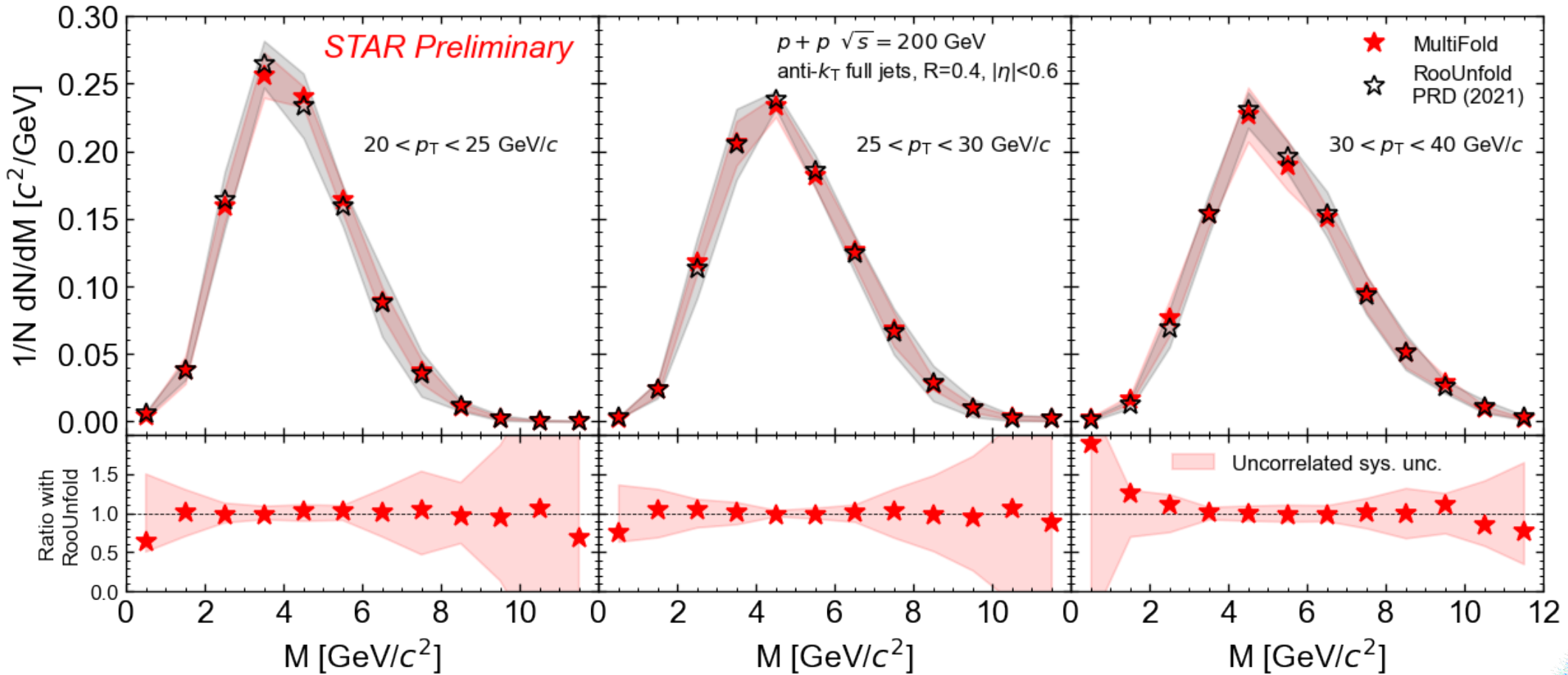
- Tracks (Towers): $0.2 < p_T(E_T) < 30 \text{ GeV}$
- Jets
 - $p_T > 15 \text{ GeV}/c$, $M > 1 \text{ GeV}/c^2$, neutral p_T fraction < 0.9
 - Passes SoftDrop with $z_{\text{cut}} = 0.1$ and $\beta = 0$



Fully corrected jet M

$$M = \left| \sum_{i \in \text{jet}} p_i \right| = \sqrt{E^2 - p^2}$$

MultiFold result agrees with **RooUnfold** result ([STAR Collaboration. PRD 104, 052007\(2021\)](#)) [HEPData](#)



... but **MultiFold** also gives us correlation between observables!

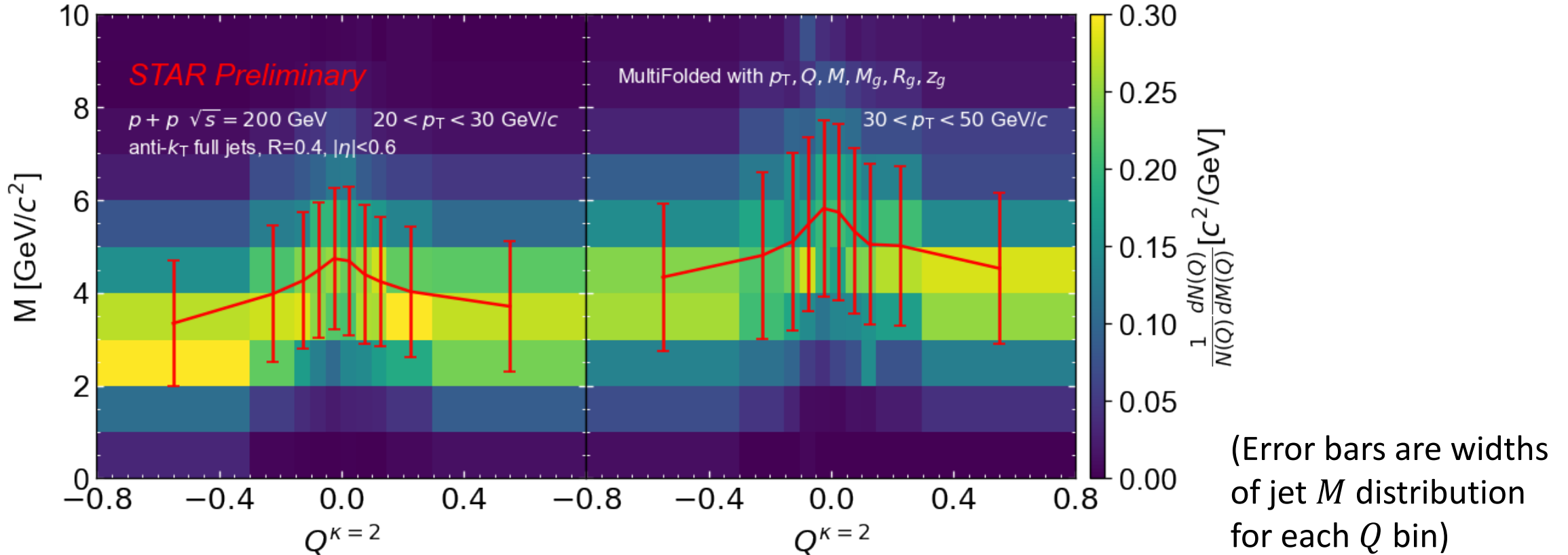
See backup slides for a breakdown of systematics.



Fully corrected jet M vs Q vs p_T

$$Q_J = \frac{1}{(p_{TJ})^\kappa} \sum_{i \in \text{Tracks}} q_i \times (p_{T,i})^\kappa \quad M = \left| \sum_{i \in \text{jet}} p_i \right| = \sqrt{E^2 - p^2}$$

(normalization is done per Q bin)



Jet M increases with increasing jet p_T → Higher p_T means larger phase space for radiation

Jet M increases with decreasing jet $|Q|$ → High p_T track contributes more to jet $|Q|$

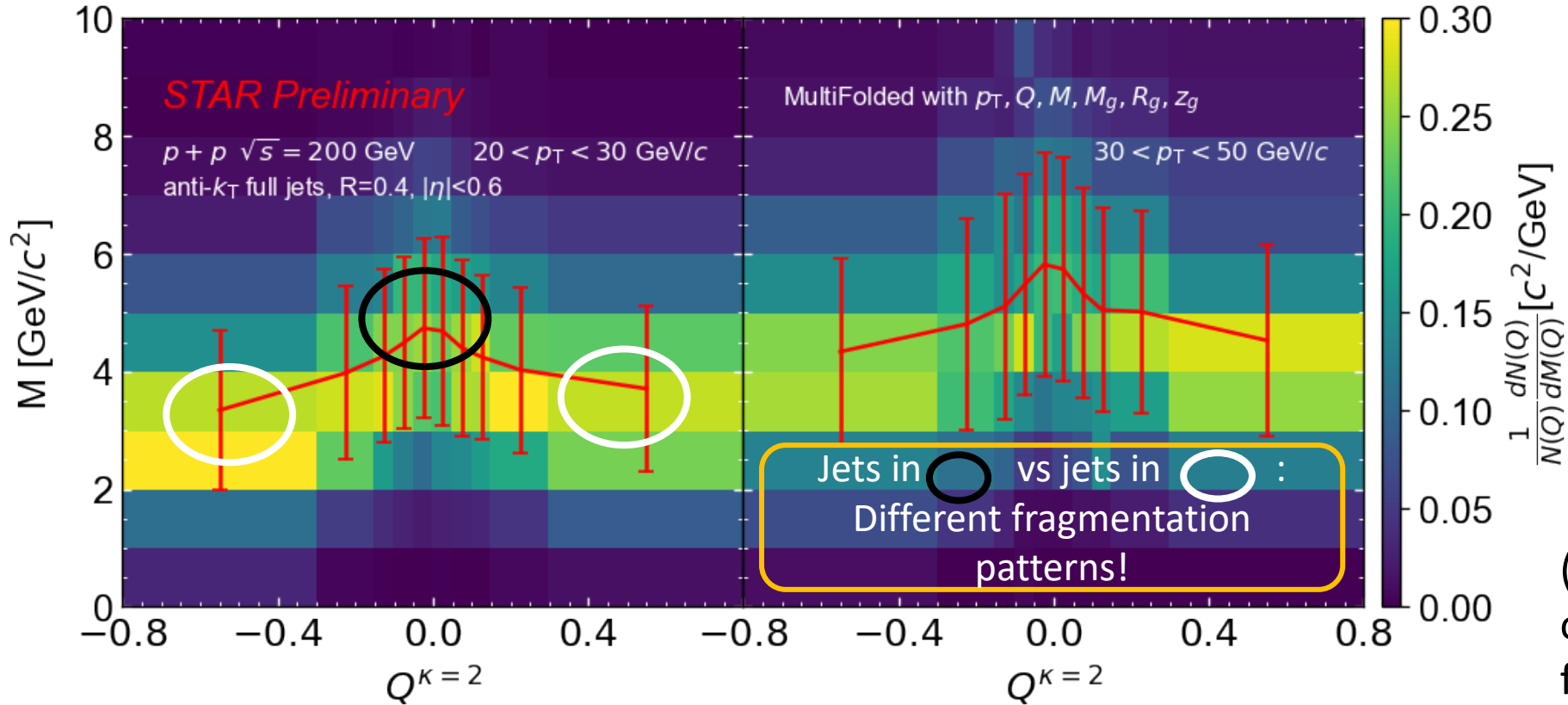
→ Wider jets tend to have lower $|Q|$



Fully corrected jet M vs Q vs p_T

$$Q_J = \frac{1}{(p_{T,J})^\kappa} \sum_{i \in \text{Tracks}} q_i \times (p_{T,i})^\kappa \quad M = \left| \sum_{i \in \text{jet}} p_i \right| = \sqrt{E^2 - p^2}$$

(normalization is done per Q bin)



Jet M increases with increasing jet p_T → Higher p_T means larger phase space for radiation

Jet M increases with decreasing jet $|Q|$ → High p_T track contributes more to jet $|Q|$

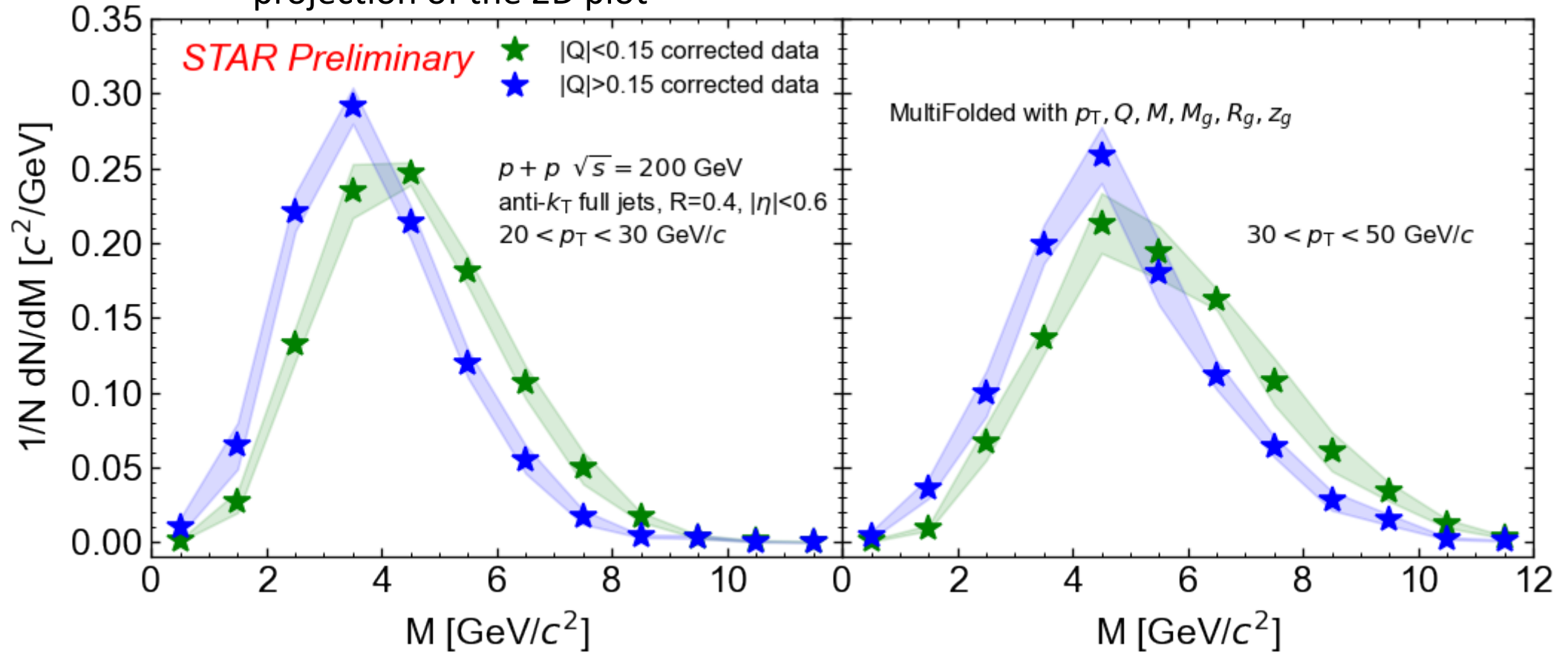
→ Wider jets tend to have lower $|Q|$



Fully corrected jet M vs Q vs p_T

$$Q_J = \frac{1}{(p_{TJ})^\kappa} \sum_{i \in \text{Tracks}} q_i \times (p_{T,i})^\kappa \quad M = \left| \sum_{i \in \text{jet}} p_i \right| = \sqrt{E^2 - \mathbf{p}^2}$$

projection of the 2D plot



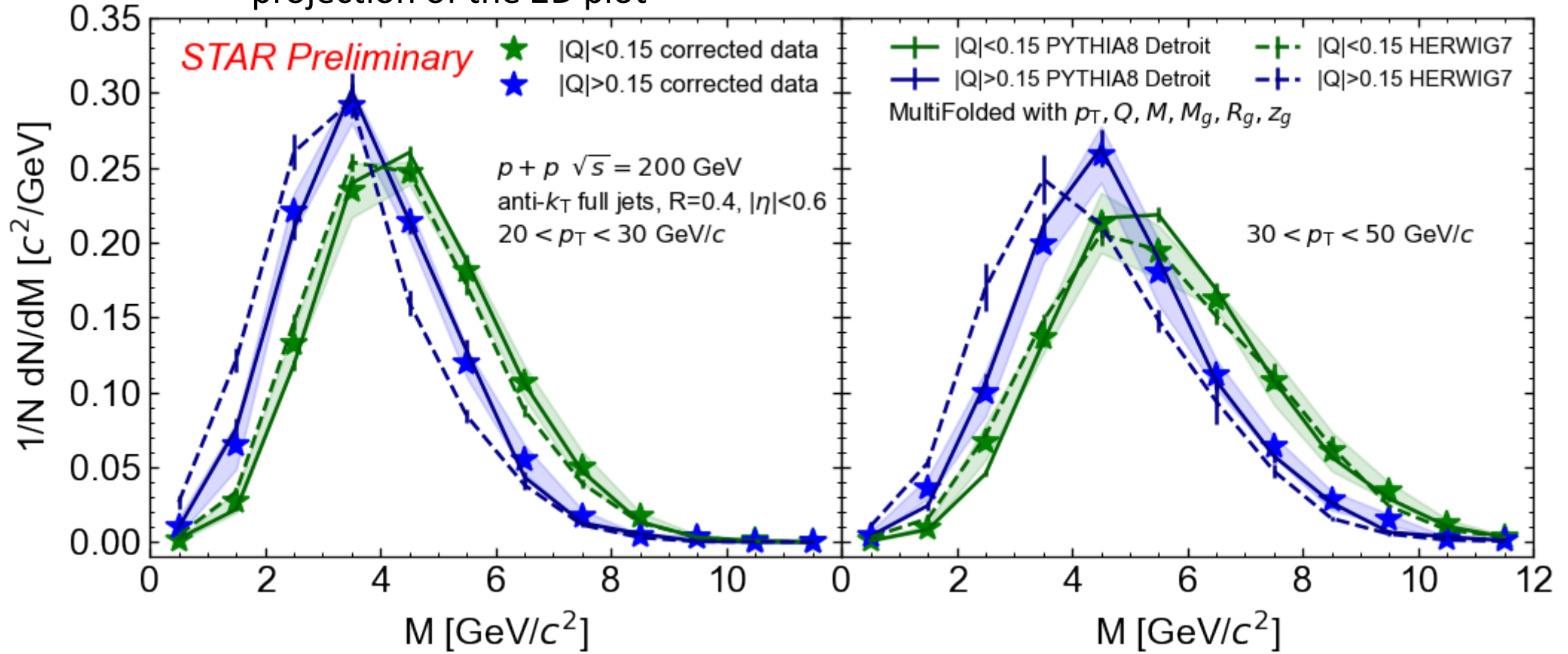
Mean and spread of jet M distribution both increase with decreasing $|Q|$



Fully corrected jet M vs Q vs p_T

$$Q_J = \frac{1}{(p_{T,J})^\kappa} \sum_{i \in \text{Tracks}} q_i \times (p_{T,i})^\kappa \quad M = \left| \sum_{i \in \text{jet}} p_i \right| = \sqrt{E^2 - p^2}$$

projection of the 2D plot



Mean and spread of jet M distribution both increase with decreasing $|Q|$

PYTHIA8 Detroit tune: Describes jet M vs $|Q|$ well

HERWIG7: Underpredicts jet M for large $|Q|$ significantly

PYTHIA6 Perugia 2012 STAR tune: [Skands, PRD 82, 074018 \(2010\)](#)
 PYTHIA8 Detroit tune: [Aguilar et al. PRD 105, 016011\(2022\)](#)
 HERWIG7: [Bellm, et al. PRC 76, 1-8 \(2016\)](#)



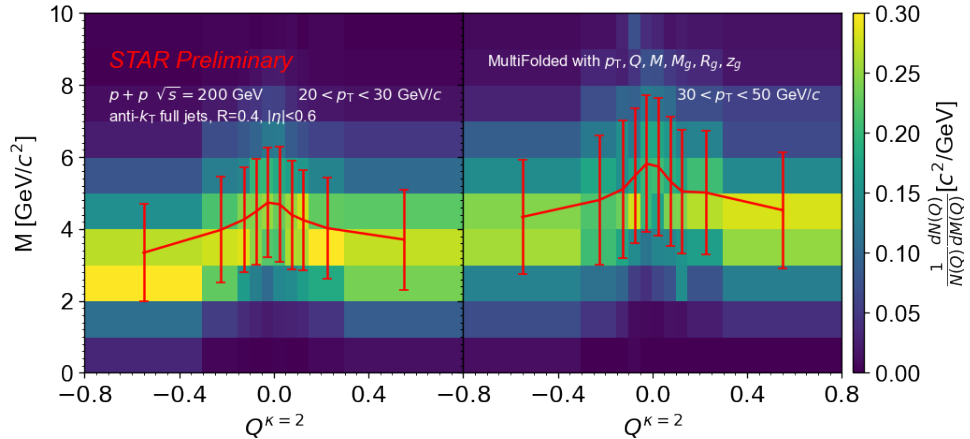


Summary and outlook

- First measurement in pp that uses machine learning based method for unfolding
 - **Multi-dimensional** and unbinned
 - Nice **agreement with RooUnfold**
 - Ideal for correlation measurement

Summary and outlook

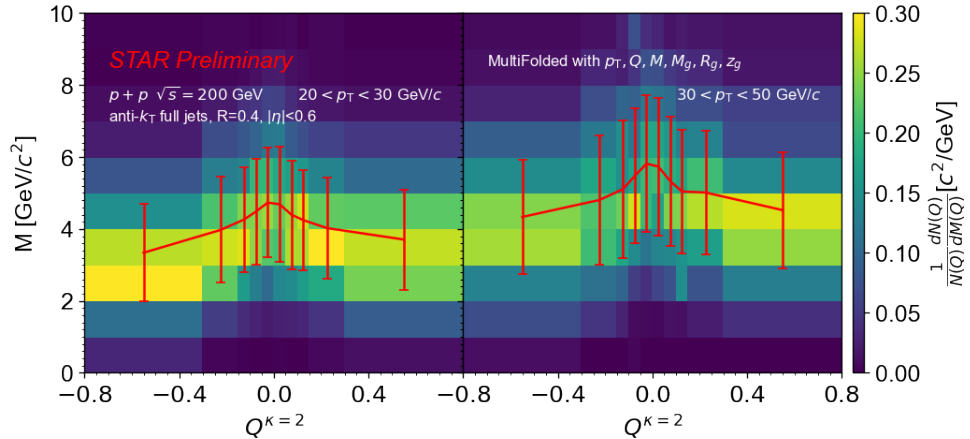
- First measurement in pp that uses machine learning based method for unfolding
 - **Multi-dimensional** and unbinned
 - Nice agreement with **RooUnfold**
 - Ideal for correlation measurement



- Fully-corrected measurement of jet M vs Q vs p_T in $\sqrt{s} = 200 \text{ GeV}$ pp collisions.
 - Jet M increases with increasing p_T ; jet M increases with decreasing $|Q|$.
 - **PYTHIA8 Detroit tune** describes the data well; **HERWIG7** underpredicts jet M for large $|Q|$.

Summary and outlook

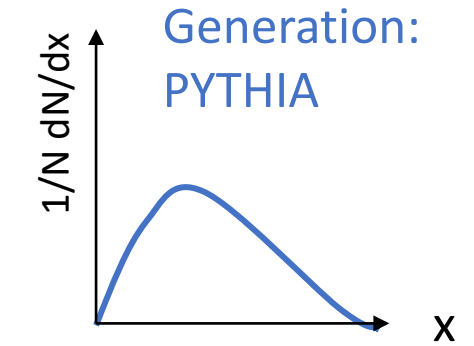
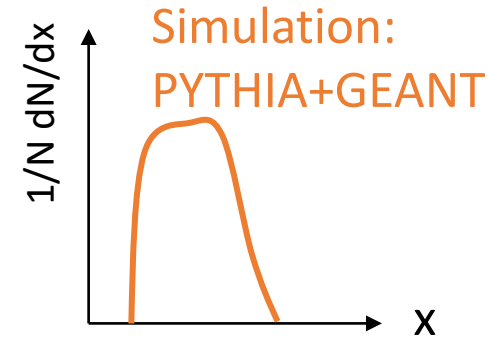
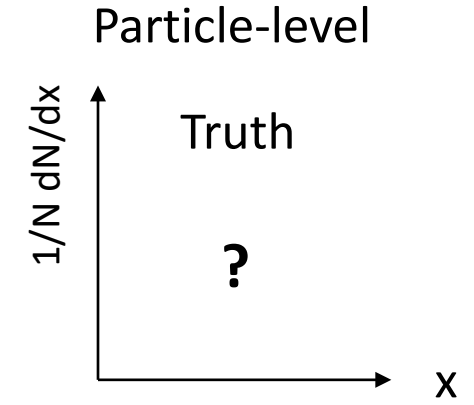
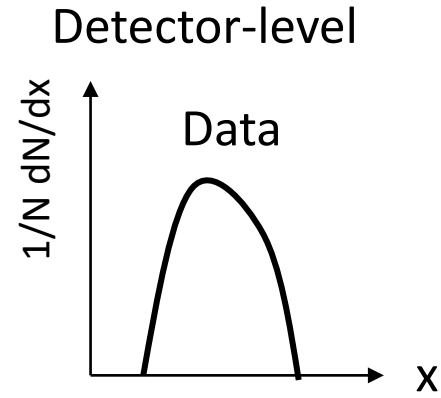
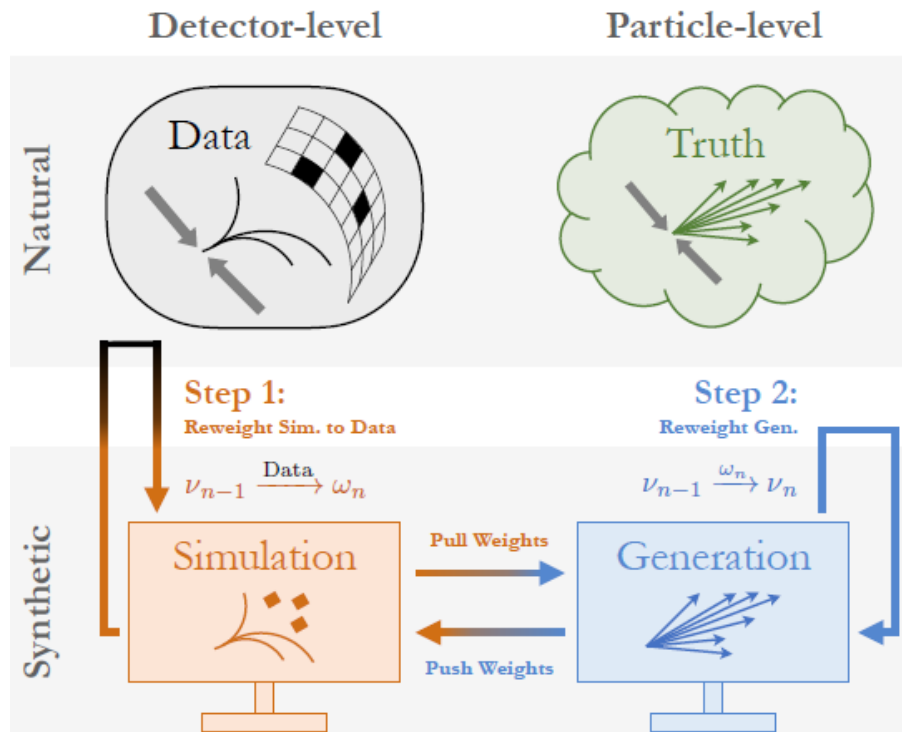
- First measurement in pp that uses machine learning based method for unfolding
 - **Multi-dimensional** and unbinned
 - Nice **agreement with RooUnfold**
 - Ideal for correlation measurement



- Fully-corrected measurement of jet M vs Q vs p_T in $\sqrt{s} = 200$ GeV pp collisions.
 - Jet M increases with increasing p_T ; jet M increases with decreasing $|Q|$.
 - **PYTHIA8 Detroit tune** describes the data well; **HERWIG7** underpredicts jet M for large $|Q|$.
- Future directions
 - Jet substructure correlation measurements allow separation of jets with different **fragmentation** patterns \rightarrow measure formation time, charge-charge correlator, collinear SoftDrop mass...
 - 6-dimensional jet information may allow us to separate **quark vs gluon** jets \rightarrow apply additional machine learning for classification...

Backup

Method



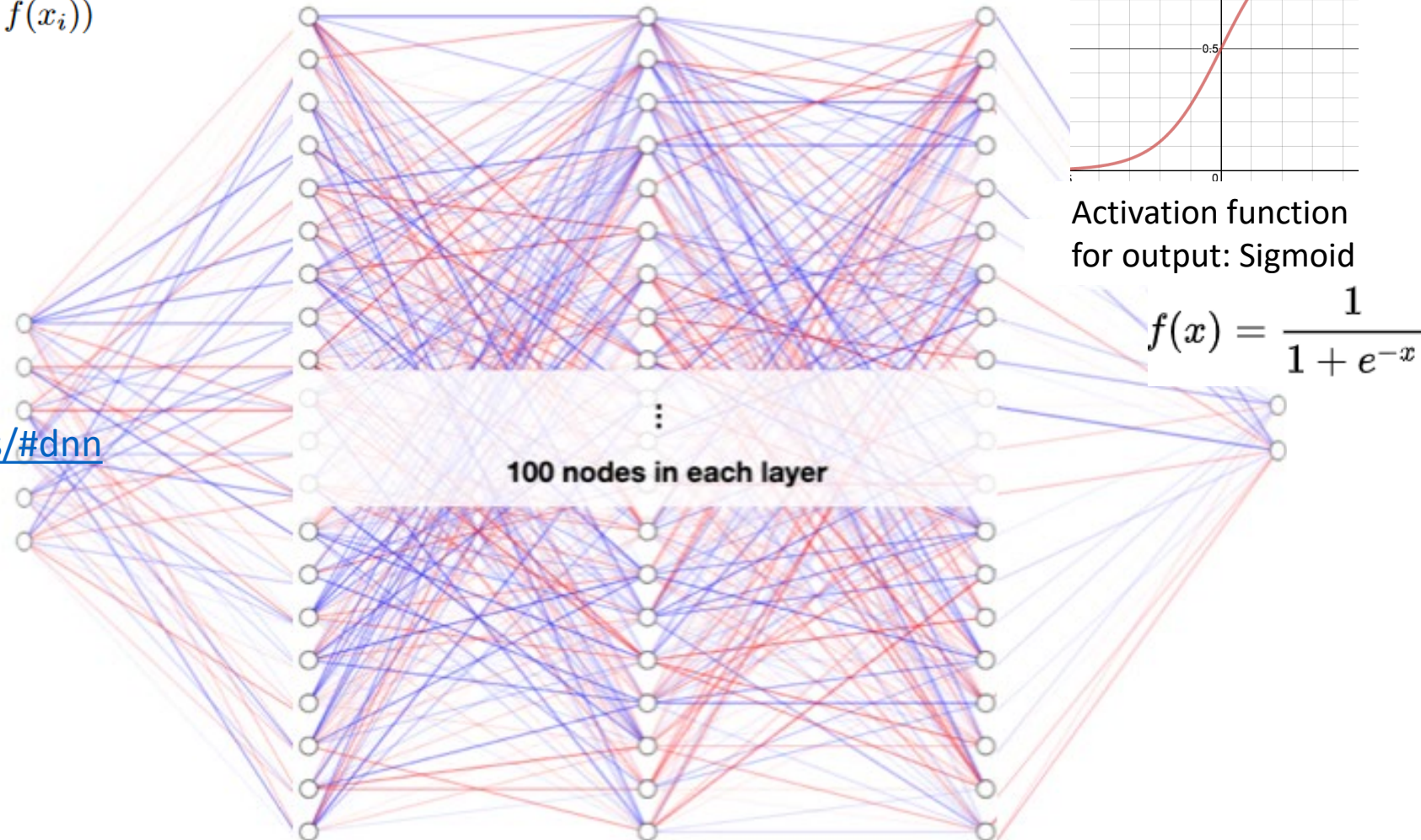
Method

- Architecture: Dense neural network
- Activation function for dense layers: Rectified linear unit
- Activation function for output layer: Sigmoid
- Loss function: Binary cross entropy

$$\text{loss}(f(x)) = - \sum_{i \in 0} \log f(x_i) - \sum_{i \in 1} \log(1 - f(x_i))$$

- Optimization algorithm: Adam
<https://arxiv.org/pdf/1412.6980.pdf>
- Nodes per dense layer: [100,100,100]
- Output dimension: 2
- Input dimension: 6
- All hyperparameters are default:
<https://energyflow.network/docs/archs/#dnn>

Activation function for dense layers: Rectified linear unit
 $f(x) = x^+ = \max(0, x)$



Method

- <https://energyflow.network/docs/archs/>

Compilation Options

- **loss**= `'categorical_crossentropy'` : *str*
 - The loss function to use for the model. See the [Keras loss function docs](#) for available loss functions.
- **optimizer**= `'adam'` : Keras optimizer or *str*
 - A [Keras optimizer](#) instance or a string referring to one (in which case the default arguments are used).
- **metrics**= `['accuracy']` : *list of str*
 - The [Keras metrics](#) to apply to the model.
- **compile_opts**= `{}` : *dict*
 - Dictionary of keyword arguments to be passed on to the `compile` method of the model. `loss`, `optimizer`, and `metrics` (see above) are included in this dictionary. All other values are the Keras defaults.

Output Options

- **output_dim**= `2` : *int*
 - The output dimension of the model.
- **output_act**= `'softmax'` : *str* or Keras activation
 - Activation function to apply to the output.

Callback Options

- **filepath**= `None` : *str*
 - The file path for where to save the model. If `None` then the model will not be saved.
- **save_while_training**= `True` : *bool*
 - Whether the model is saved during training (using the `ModelCheckpoint` callback) or only once training terminates. Only relevant if `filepath` is set.
- **save_weights_only**= `False` : *bool*
 - Whether only the weights of the model or the full model are saved. Only relevant if `filepath` is set.
- **modelcheck_opts**= `{'save_best_only':True, 'verbose':1}` : *dict*
 - Dictionary of keyword arguments to be passed on to the `ModelCheckpoint` callback, if it is present. `save_weights_only` (see above) is included in this dictionary. All other arguments are the Keras defaults.
- **patience**= `None` : *int*
 - The number of epochs with no improvement after which the training is stopped (using the `EarlyStopping` callback). If `None` then no early stopping is used.
- **earlystop_opts**= `{'restore_best_weights':True, 'verbose':1}` : *dict*
 - Dictionary of keyword arguments to be passed on to the `EarlyStopping` callback, if it is present. `patience` (see above) is included in this dictionary. All other arguments are the Keras defaults.

Method

- <https://energyflow.network/docs/archs/#dnn>

Required DNN Hyperparameters

- `input_dim` : `int = 6`
 - The number of inputs to the model.
- `dense_sizes` : `{tuple, list} of int=[100,100,100]`
 - The number of nodes in the dense layers of the model.

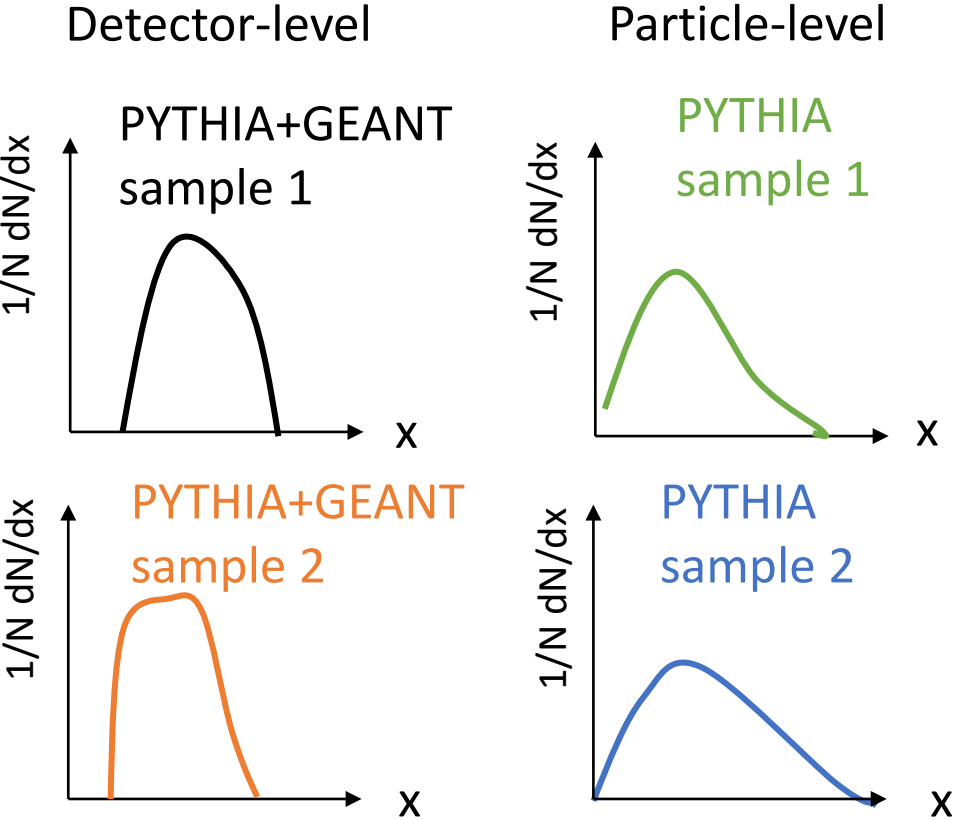
Default DNN Hyperparameters

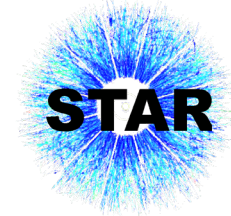
- `acts`= `'relu'` : `{tuple, list} of str` or Keras activation
 - Activation function(s) for the dense layers. A single string or activation layer will apply the same activation to all dense layers. Keras advanced activation layers are also accepted, either as strings (which use the default arguments) or as Keras `Layer` instances. If passing a single `Layer` instance, be aware that this layer will be used for all activations and may introduce weight sharing (such as with `PReLU`); it is recommended in this case to pass as many activations as there are layers in the model. See the [Keras activations docs](#) for more detail.
- `k_inits`= `'he_uniform'` : `{tuple, list} of str` or Keras initializer
 - Kernel initializers for the dense layers. A single string will apply the same initializer to all layers. See the [Keras initializer docs](#) for more detail.
- `dropouts`= `0` : `{tuple, list} of float`
 - Dropout rates for the dense layers. A single float will apply the same dropout rate to all layers. See the [Keras Dropout layer](#) for more detail.
- `l2_regs`= `0` : `{tuple, list} of float`



Closure test for unfolding

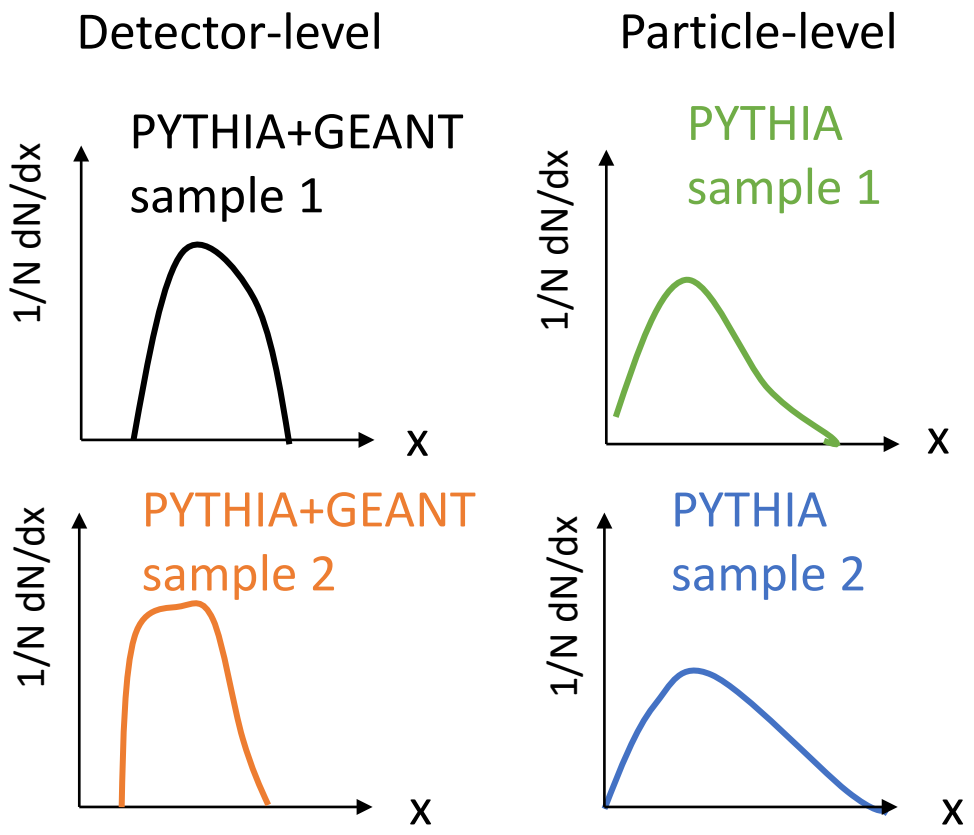
- Step 1: Separate matched jets from PYTHIA and PYTHIA+GEANT into 2 samples



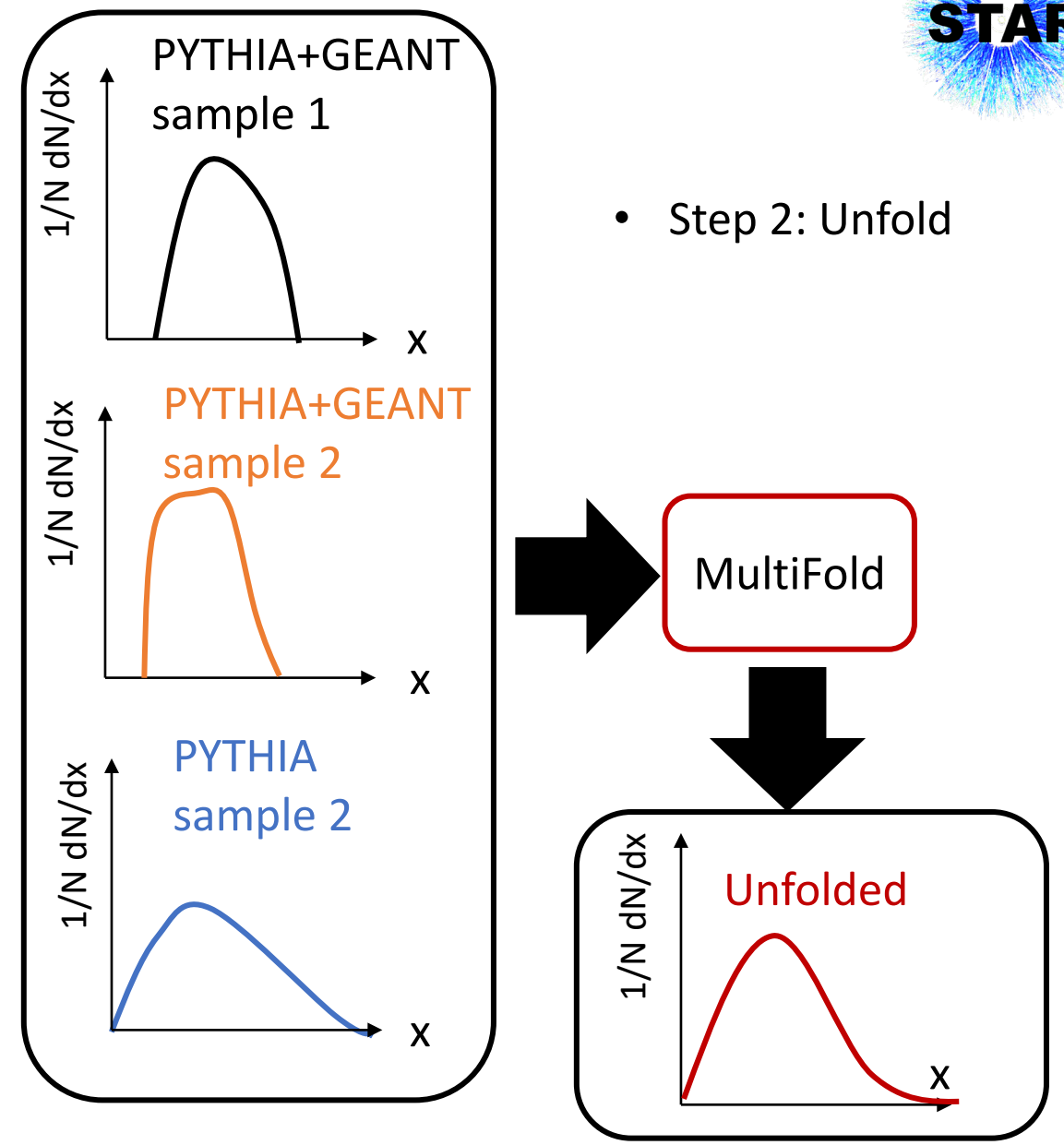


Closure test for unfolding

- Step 1: Separate matched jets from PYTHIA and PYTHIA+GEANT into 2 samples

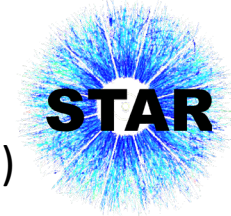


Hot Quarks, 10/15/22



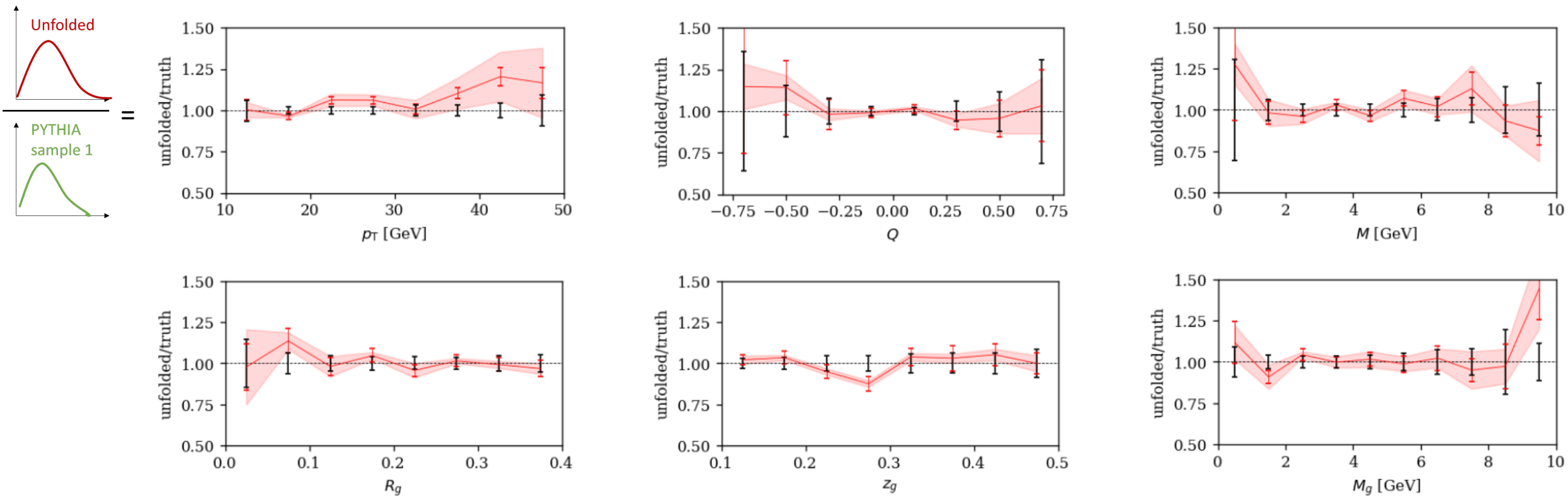
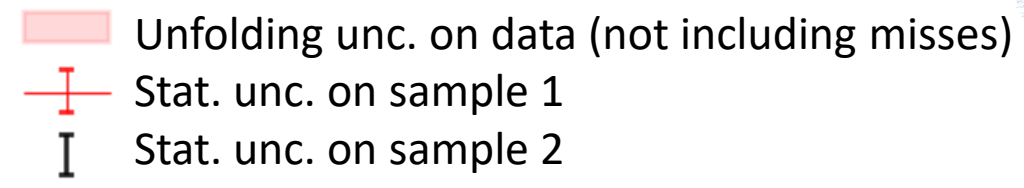
- Step 2: Unfold

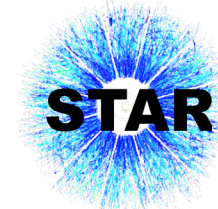
Youqi Song



Closure test for unfolding: results

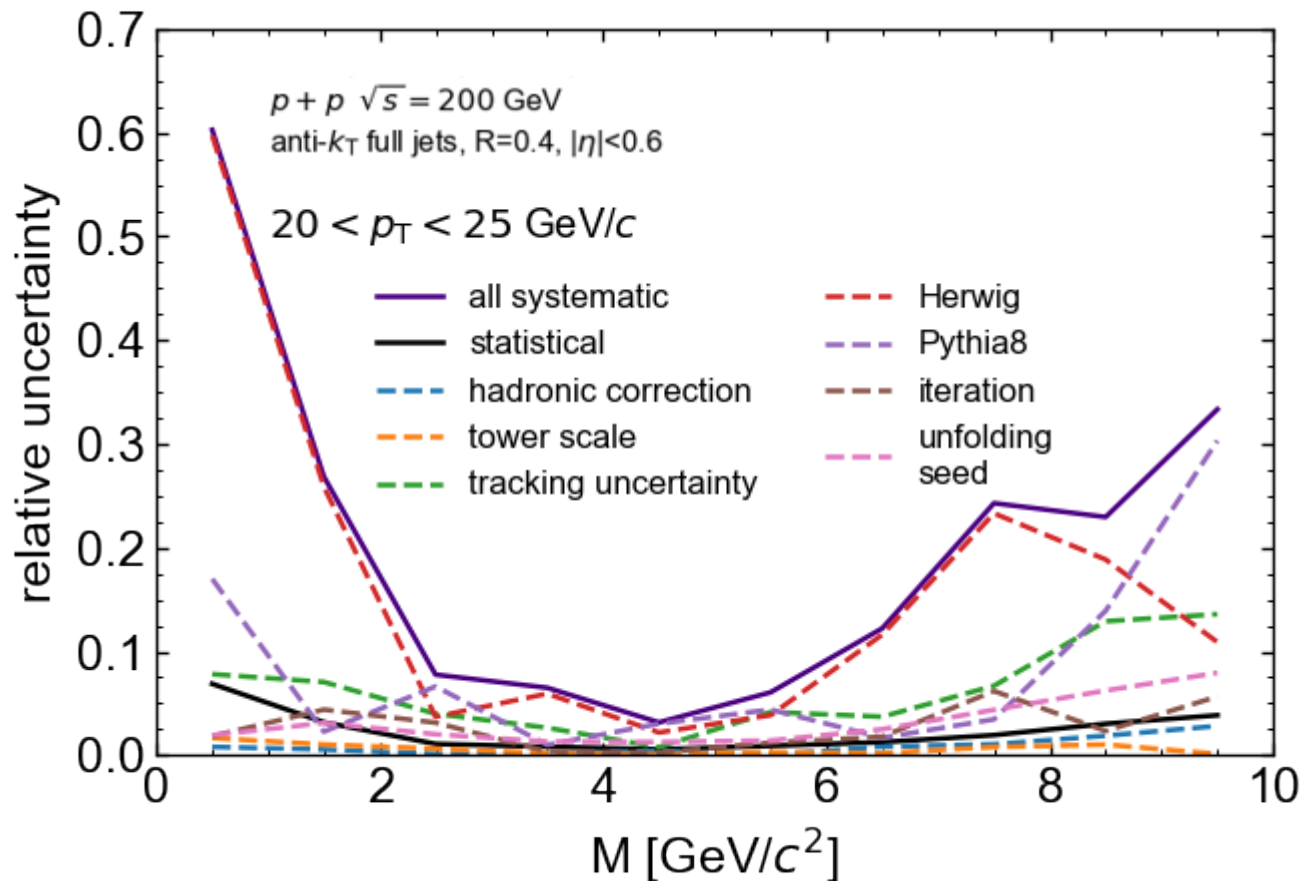
- Decent **closure** for all substructure observables



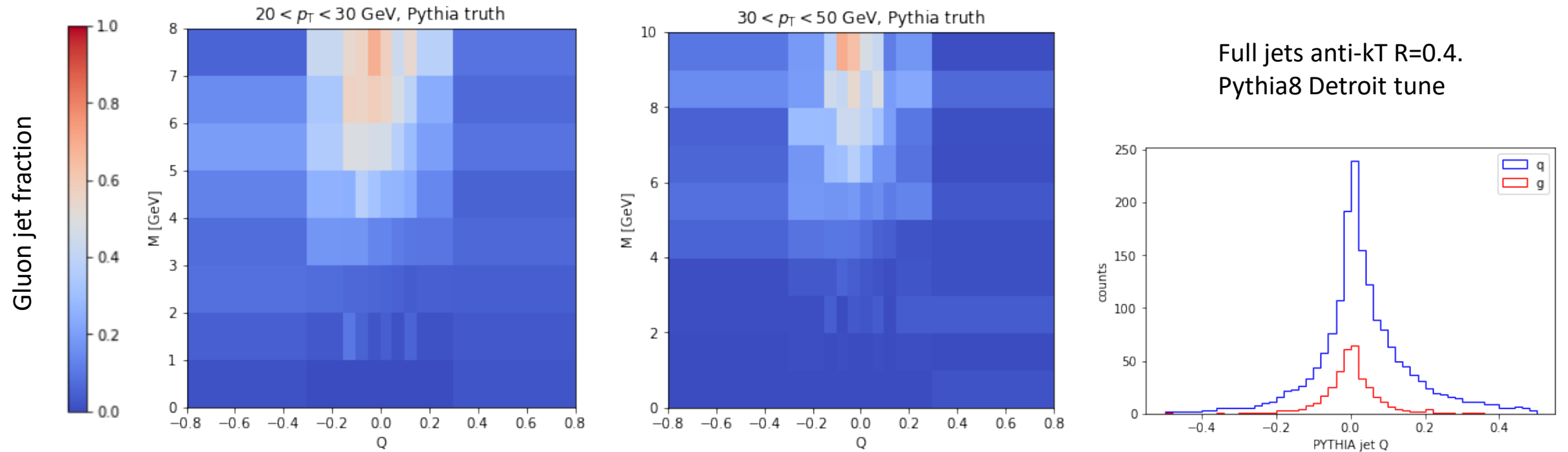


Systematic uncertainties

- Detector uncertainties (correlated with RooUnfold)
 - Hadronic correction 100% -> 50%
 - Tower scale +3.8%
 - Tracking efficiency -4%
- Unfolding uncertainties
 - Prior shape variation: Reweight jet mass distributions by HERWIG7 (LHC-UE-EE-4-CTEQ6L1 tune) and PYTHIA8 (Detroit tune)
 - Unfolding seed variation: Due to randomization of the initial weights
 - Iteration number variation



What's the best purity we can achieve for q vs g separation?



- In $20 < p_T < 30$ GeV, **gluon fraction** $\sim 35\%$
- To select a jet population with **gluon fraction** = **67%**, cut on $-0.025 < Q < 0$ AND $M > 7$ GeV. (1.1% of all jets).
 - If we only cut on $M > 7$ GeV, **gluon fraction** = **58%**. (Although we will have higher statistics).
 - If we want to reach **gluon fraction** = **67%** with just a M cut, need $M > 8.6$ GeV. (0.8% of all jets).
- In $30 < p_T < 50$ GeV, **gluon fraction** $\sim 20\%$
- To select a jet population with **gluon fraction** = **65%**, cut on $-0.08 < Q < -0.01$ AND $M > 9$ GeV. (1.1%).
 - **No cut on jet M/Q alone can achieve such a purity.**