

STAR results on strangeness and electric charge dependent splitting of rapidity-odd directed flow

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1 Rapidity-odd directed flow (v_1) of multi-strange baryons (Ξ and Ω) at mid-rapidity is
2 reported for Au+Au collisions as recorded by the STAR detector at the Relativistic
3 Heavy Ion Collider (RHIC). We focus on particle species where all constituent quarks
4 are produced, such as $K^-(\bar{u}s)$, $\bar{p}(\bar{u}\bar{u}\bar{d})$, $\bar{\Lambda}(\bar{u}\bar{d}\bar{s})$, $\phi(s\bar{s})$, $\Xi^+(\bar{d}\bar{s}\bar{s})$, $\Omega^-(sss)$ and $\bar{\Omega}^+(\bar{s}\bar{s}\bar{s})$,
5 and demonstrate using a novel analysis method that the coalescence sum rule holds in
6 a common kinematic region for hadron combinations with identical quark content. We
7 examine the coalescence sum rule as a function of rapidity for non-identical quark content
8 having the same quark-level mass but different strangeness (ΔS) and electric charge
9 (Δq). The difference in the directed flow of different quark and anti-quark combinations,
10 e.g., $v_1(\Omega^-(sss)) - v_1(\bar{\Omega}^+(\bar{s}\bar{s}\bar{s}))$, is a measure of coalescence sum rule violation, and we
11 call it directed flow splitting (Δv_1). We measure ΔS and Δq dependence of the Δv_1 slope
12 ($d\Delta v_1/dy$) between produced quarks and anti-quarks in Au+Au collisions at $\sqrt{s_{NN}} =$
13 27 GeV and 200 GeV. Measurements have been compared with A Multi-Phase Transport
14 (AMPT) and Parton-Hadron String Dynamics (PHSD) model with electromagnetic field
15 calculations.

16 *Keywords:* Heavy-ion collisions; multi-strange; directed flow; electro-magnetic field.

17 *PACS numbers:*

18 1. Introduction

19 The azimuthal anisotropic flow of emitted particles is one of the most important and
20 effective experimental observables for characterizing the matter formed in heavy-ion
21 collisions.¹⁻³ The anisotropic flow can be expressed in terms of Fourier coefficients
22 extracted from the azimuthal distribution of the final state particles. The first
23 harmonic coefficient of the Fourier expansion relative to the reaction plane (Ψ_{RP})
24 is defined as rapidity-odd directed flow, v_1 . Nuclear transport⁴ and hydrodynamic⁵
25 model calculations indicate that v_1 is sensitive to the early stages of the collisions.

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26 In high-energy collisions, strange quarks (s and \bar{s}) are produced through partonic
 27 interactions ($gg \rightarrow s\bar{s}$, $q\bar{q} \rightarrow s\bar{s}$) in an enhanced manner in the plasma phase and
 28 retain their identity during the hadronization phase which ensures the production
 29 of strange particles, such as K , Λ , $\bar{\Lambda}$, ϕ , Ξ and Ω , in the collisions.^{6,7} Multi-strange
 30 baryons (Ξ and Ω) have low scattering cross section, and early thermal freeze-out
 31 time compared to non- or single-strange particles.⁸ In other words, multi-strange
 32 particles are emitted almost directly from the phase boundary of the hadronizing
 33 fireball and hence they carry important information of the earlier stages of the
 34 collisions.⁹ Since v_1 is sensitive to the early stages too, the measurements of v_1 of
 35 multi-strange baryons might be a good probe to study early collision dynamics. It
 36 has also been argued that an extremely strong magnetic field (\vec{B}) is produced in
 37 the early stages of non-central heavy-ion collisions due to the motion of the charged
 38 spectators that pass each other rather. The presence of an early-time magnetic field
 39 has important implications for the motion of the final-state charged particles that
 40 we measure in experiments.¹⁰⁻¹² As the charged spectators fly away, the produced
 41 \vec{B} decays down quickly and generates an electric current in the plasma owing to the
 42 Faraday effect. The charged spectators can also exert an electric force on the charged
 43 constituents in the plasma due to Coulomb effect. Along with that, the plasma has a
 44 longitudinal expansion velocity along the beam direction and hence perpendicular to
 45 \vec{B} , and the Lorentz force pushes charged particles and anti-particles of the plasma in
 46 opposite directions, perpendicular to both the direction of the plasma's longitudinal
 47 velocity and \vec{B} . This is called the Hall effect. The combination of Faraday, Coulomb,
 48 and Hall effects greatly influence the v_1 of the different produced particles depending
 49 upon their charge,¹⁰⁻¹² which eventually leads to the splitting of v_1 . Hence, the
 50 study of charge-dependent v_1 and the splitting are deserving of focused attention
 51 among theorists and experimentalists.

52 The splitting between opposite-charge hadron pairs like π^\pm , K^\pm , $p(\bar{p})$, etc., has
 53 been calculated in the literature.^{10,13-15} The splitting between heavy (anti-)particle
 54 pairs ($D^0(c\bar{u}) - \bar{D}^0(\bar{c}u)$) has also been computed and found to be affected by the
 55 produced \vec{B} .¹⁶ This is due to the fact that charm and anti-charm are produced
 56 early and get the strongest kicks from the early-time strong \vec{B} field. From the ex-
 57 perimental side, there are many measurements of v_1 for different particle species
 58 at RHIC¹⁷⁻²¹ and the LHC.²² STAR measured charge-dependent v_1 splitting be-
 59 tween positively and negatively charged hadrons in Cu+Au and Au+Au collisions
 60 at $\sqrt{s_{NN}} = 200$ GeV.²³ Due to the larger Coulomb force in asymmetric Cu+Au
 61 collisions compared to the symmetric Au+Au case, a large v_1 splitting is observed in
 62 the Cu+Au system. ALICE measured v_1 splitting using inclusive charged hadrons in
 63 Pb+Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV.²² Also, the v_1 splitting between D^0 and \bar{D}^0
 64 mesons was reported by the STAR²⁴ and ALICE²² collaborations in $\sqrt{s_{NN}} = 200$
 65 GeV Au+Au and $\sqrt{s_{NN}} = 2.76$ TeV Pb+Pb collisions, respectively. Note that a
 66 stronger splitting between D^0 and \bar{D}^0 compared to the inclusive charged hadrons
 67 is seen at the LHC, however the splitting at STAR is consistent with zero within

68 large uncertainties. The large splitting at the LHC is attributed to the effect of the
69 early-stage strong \vec{B} .

70 In the STAR experiment, measurements of D^0 and \bar{D}^0 below $\sqrt{s_{NN}} = 200$ GeV
71 are difficult due to the lower heavy flavour production rate and the absence of the
72 Heavy Flavour Tracker (HFT) detector during Beam Energy Scan (BES) phase-II
73 data taking. Charge-dependent v_1 splitting can be measured using light hadrons,
74 since they are produced in abundance and there were suitable detectors installed
75 during the BES-II run periods. However, there are difficulties in interpreting the
76 splitting using light flavour, especially when the effects of electromagnetic fields
77 are concerned. For example, among light hadrons, there are many (anti-)particles
78 that contain u and d quarks, which can be either transported from beam rapidity²⁵
79 or produced in the collisions. The transported u and d quarks suffer a lot more
80 interactions than the produced quarks before ending up in a measured hadron, and
81 hence they have different v_1 from the produced quarks.²⁶ So, there is already a
82 splitting due to the transport, which act as a background for the electromagnetic-
83 field-driven splitting. Subtracting such contamination in experiment is very difficult.
84 Our experimental analysis approach bypasses the transported quarks and avoids the
85 contamination by choosing particles composed of produced constituent quarks only
86 (\bar{u} , \bar{d} , s and \bar{s}). The details of the approach can be found in Ref.²⁷ and will also be
87 discussed briefly in Section 2.2.

88 In these proceedings, we show the measurements of v_1 of multi-strange baryons
89 (Ξ and Ω). We also present the v_1 splitting as a function of electric charge difference
90 Δq and strangeness difference ΔS , using light hadrons from Au+Au collisions at
91 $\sqrt{s_{NN}} = 27$ and 200 GeV. These proceedings are organized as follows: In the
92 next section, we refer to the STAR experimental setup and the employed analysis
93 approach. We discuss results in Sec. 3. Section 4 is devoted to a summary.

94 2. Experimental setup and the analysis approach

95 2.1. STAR detector setup and analysis cuts

96 The STAR detector²⁸ system is an excellent experimental setup for track recon-
97 struction, vertexing, and particle identification at RHIC. The main tracking detec-
98 tor is located in a uniform magnetic field of maximum value 0.5 T, which provides
99 charged particle momentum measurements. A large volume Time Projection Cham-
100 ber (TPC),²⁹ covering a pseudo-rapidity range $|\eta| \leq 1$ is used for charged particle
101 tracking, vertexing, and particle identification using ionization energy loss. Time-of-
102 flight information from the TOF detector³⁰ is also used for particle identification.
103 There are forward-rapidity detectors, namely the Event-Plane Detectors (EPDs)
104 ($2.1 < |\eta| < 5.1$)³¹ and Zero-Degree Calorimeter with Shower-Maximum Detectors
105 (ZDC-SMDs) ($|\eta| > 6.3$),³² that can measure event planes of the collisions.

106 The analysis reported here is carried out using high statistics data samples for
107 Au+Au collisions at $\sqrt{s_{NN}} = 27$ GeV and 200 GeV, recorded by the STAR detector
108 in the years 2018 and 2016, respectively. We restrict the primary vertex position

of each event to be along the beam direction with $|V_z| < 40$ cm, and along the radial direction transverse to the beam axis with $V_r < 2$ cm at $\sqrt{s_{NN}} = 27$ GeV; and $|V_z| < 70$ cm, $V_r < 2$ cm at $\sqrt{s_{NN}} = 200$ GeV. The tracks are required to have $p_T > 0.2$ GeV/ c and a distance of closest approach (DCA) from the primary vertex, $DCA \leq 3$ cm. Additional requirements for track selection are: at least 15 space points in the TPC acceptance, and the ratio of the number of measured space points to the maximum possible number of space points should be greater than 0.52. Particles are identified using information from TPC and TOF detectors. Particle identification cuts applied are: $0.4 < p_T < 5$ GeV/ c , $|n_\sigma| \leq 2$ for protons and anti-protons; $p_T > 0.2$ GeV/ c , momentum < 1.6 GeV/ c and $|n_\sigma| \leq 2$ for charged pions and kaons, where n_σ denotes standard deviation from the most probable dE/dx for that particle type. Systematic uncertainties on the measurements are obtained by varying these analysis cuts and removing the effects of statistical fluctuations, as prescribed by Barlow.³³

We have reconstructed Λ , $\bar{\Lambda}$, Ξ^- , $\bar{\Xi}^+$, Ω^- , and $\bar{\Omega}^+$ within $0.2 < p_T < 5$ GeV/ c using a Kalman filter (KF) method.^{34,35} The KF-Particle package exploits the quality of the track fit as well as the decay topology. The decay channels used for the reconstruction are: $\Lambda(\bar{\Lambda}) \rightarrow p\pi^-(\bar{p}\pi^+)$, $\Xi^-(\bar{\Xi}^+) \rightarrow \Lambda\pi^-(\bar{\Lambda}\pi^+)$ and $\Omega^-(\bar{\Omega}^+) \rightarrow \Lambda K^-(\bar{\Lambda}K^+)$.³⁶ ϕ -mesons are reconstructed in K^+K^- channel using the invariant mass technique with pair rotation background subtraction.

2.2. Analysis approach

The analysis approach is based on the quark coalescence mechanism, where the anisotropic collective flow is assumed to be imparted before hadronization and the observed particles are assumed to form via coalescence of constituent quarks. This mechanism of particle formation implies a sum rule, called the coalescence-inspired sum rule,²¹ and the number-of-constituent-quark (NCQ) scaling of the measured flow immediately follows from there. Directed flow of a suitably-chosen hadron species is consistent with the sum of the directed flow of its constituent quarks:

$$v_1(\text{hadron}) = \sum_i v_1(q_i), \quad (1)$$

where the sum runs over the v_1 for the two constituent quarks q_i in a meson and the three in a baryon. These constituent quarks can either be produced in the collisions or transported from the incoming nuclei. There are many particle species composed of constituent u and d quarks, which might or might not be transported from the incoming nuclei. The v_1 of the transported quarks (u and d) in general is quite different from that of produced quarks (\bar{u} , \bar{d} , s and \bar{s}). This in turn leads to a difference between v_1 of a particle containing u or d quarks that could be either produced or transported, and v_1 of another particle containing produced quarks only (\bar{u} , \bar{d} , s and \bar{s}). This fact greatly complicates³⁷ the interpretation of v_1 splitting between positive and negative hadrons in terms of possible electromagnetic field effects. In experiment, it is hard to distinguish transported and produced

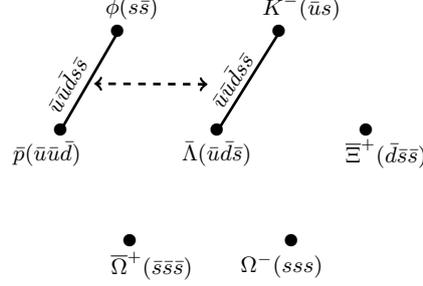


Fig. 1. Diagram²⁷ showing the seven produced particles composed of produced (non-transported) quarks only. We combine ϕ with \bar{p} and K^- with $\bar{\Lambda}$ so that these two combinations have identical constituent quarks $\bar{u}\bar{u}\bar{d}s\bar{s}$ that correspond to the same mass at the constituent level $\Delta m = 0$, the same strangeness $\Delta S = 0$ and the same electric charge $\Delta q = 0$. The measured directed flow of these two combinations must be similar if the coalescence sum rule holds. The geometric arrangement of the seven hadron species has no special significance and is chosen simply to facilitate illustration of the chosen combinations.

148 quarks and hence, here we study those particles which contain produced quarks
 149 only, namely, $K^-(\bar{u}s)$, $\bar{p}(\bar{u}\bar{u}\bar{d})$, $\bar{\Lambda}(\bar{u}\bar{d}\bar{s})$, $\phi(s\bar{s})$, $\bar{\Xi}^+(\bar{d}\bar{s}\bar{s})$, $\Omega^-(sss)$, and $\bar{\Omega}^+(\bar{s}\bar{s}\bar{s})$.

Index	Quark mass	Charge	Strangeness	Δv_1 combination
1	$\Delta m = 0$	$\Delta q = 0$	$\Delta S = 0$	$[\bar{p}(\bar{u}\bar{u}\bar{d}) + \phi(s\bar{s})] - [K^-(\bar{u}s) + \bar{\Lambda}(\bar{u}\bar{d}\bar{s})]$
2	$\Delta m \approx 0$	$\Delta q = \frac{2}{3}$	$\Delta S = 1$	$[\bar{\Lambda}(\bar{u}\bar{d}\bar{s})] - [\frac{1}{2}\phi(s\bar{s}) + \frac{2}{3}\bar{p}(\bar{u}\bar{u}\bar{d})]$
3	$\Delta m \approx 0$	$\Delta q = 1$	$\Delta S = 2$	$[\bar{\Lambda}(\bar{u}\bar{d}\bar{s})] - [\frac{1}{3}\Omega^-(sss) + \frac{2}{3}\bar{p}(\bar{u}\bar{u}\bar{d})]$
4	$\Delta m \approx 0$	$\Delta q = \frac{4}{3}$	$\Delta S = 2$	$[\bar{\Lambda}(\bar{u}\bar{d}\bar{s})] - [K^-(\bar{u}s) + \frac{1}{3}\bar{p}(\bar{u}\bar{u}\bar{d})]$
5	$\Delta m \approx 0$	$\Delta q = \frac{4}{3}$	$\Delta S = 2$	$[\bar{\Xi}^+(\bar{d}\bar{s}\bar{s})] - [\phi(s\bar{s}) + \frac{1}{3}\bar{p}(\bar{u}\bar{u}\bar{d})]$
6	$\Delta m = 0$	$\Delta q = 2$	$\Delta S = 6$	$[\bar{\Omega}^+(\bar{s}\bar{s}\bar{s})] - [\Omega^-(sss)]$
7	$\Delta m \approx 0$	$\Delta q = \frac{7}{3}$	$\Delta S = 4$	$[\bar{\Xi}^+(\bar{d}\bar{s}\bar{s})] - [K^-(\bar{u}s) + \frac{1}{3}\Omega^-(sss)]$

Table 1. This table shows differences between combinations formed from seven particle species composed of produced quarks only. For every combination, the constituent quark mass difference (Δm) is zero or near-zero, while the charge difference (Δq) and strangeness difference (ΔS) are varied as tabulated. Index 1 is illustrated in diagrammatic form in Fig. 1.

150 The above seven particles have different flavour, electric charge (q) and mass
 151 (m). The v_1 is sensitive to quark flavour and mass. How do we compare the v_1 of
 152 these different particles and search for possible EM-field-driven splitting? Firstly, we
 153 choose a common kinematic region, $p_T/n_q - y$ (where n_q is the number of constituent
 154 quarks in the particle and y is the rapidity of the particle) for all seven particle
 155 species and test the coalescence sum rule (Eq. (1)) by combining the different

156 particles so that the combinations have identical quark content. In other words, we
 157 measure v_1 of the individual particle and test the following in the selected kinematic
 158 region,

$$v_1[\bar{p}(\bar{u}\bar{u}\bar{d})] + v_1[\phi(s\bar{s})] = v_1[K^-(\bar{u}s)] + v_1[\bar{\Lambda}(\bar{u}\bar{d}\bar{s})]. \quad (2)$$

159 In Eq. (2), both left and right sides have the identical constituent quark content of
 160 $\bar{u}\bar{u}\bar{d}\bar{s}\bar{s}$. However, the quarks are shared differently within the two pairs of hadrons.
 161 This is illustrated in Fig. 1 (taken from Ref.²⁷).

162 Secondly, after verifying that Eq. (2) holds within measured uncertainties in
 163 the selected kinematic region, we move on and form combinations among the seven
 164 particles in such a way that the combinations have the same or similar mass at
 165 the constituent quark level ($\Delta m \approx 0$), but non-zero electric charge difference Δq
 166 and non-zero strangeness difference ΔS . The difference Δv_1 of such combinations
 167 ($\Delta m \approx 0$), is called “splitting of v_1 ” and the slope of the Δv_1 is a measure of the
 168 splitting. For example, Eq. (2) can be expressed in terms of Δv_1 as follows:

$$\Delta v_1(\Delta q = 0, \Delta S = 0) = \{v_1[\bar{p}(\bar{u}\bar{u}\bar{d})] + v_1[\phi(s\bar{s})]\} - \{v_1[K^-(\bar{u}s)] + v_1[\bar{\Lambda}(\bar{u}\bar{d}\bar{s})]\}. \quad (3)$$

169 We obtain different combinations as shown in Table 1 where index 1 is the identical
 170 quark combination case ($\Delta q = 0$ and $\Delta S = 0$) (Eq. (2)) and indices 2-7 are non-
 171 identical quark combination cases ($\Delta q \neq 0$ and $\Delta S \neq 0$). In the combinations, we
 172 assume that masses of u and d are the same, and different from s and \bar{s} quarks, i.e.,
 173 $m_u \sim m_d \neq m_s (= m_{\bar{s}})$. Two degenerate combinations, indices 4 and 5, have the
 174 same $\Delta q = 4/3$ and $\Delta S = 2$. There are other possible combinations similar to the
 175 ones listed in Table 1. Measuring the Δv_1 of all the combinations in Table 1 enables
 176 us to measure the splitting with different Δq and ΔS . Of course, the increase in
 177 Δq in Table 1 is also associated with a change in ΔS . This is an unavoidable
 178 consequence of the quantum numbers carried by the constituent quarks.

179 3. Results and discussion

180 Figure 2 shows invariant mass distributions of Λ - π pairs (left plot) and Λ - K pairs
 181 (right plot) for 20%-80% centrality in Au+Au collisions at $\sqrt{s_{NN}} = 27$ GeV.

We employed the event plane method to measure v_1 of each particle:

$$v_1 = \langle \cos(\phi - \Psi_1) \rangle / \text{Res}\{\Psi_1\}, \quad (4)$$

182 where ϕ is the track azimuthal angle measured in the TPC and $\text{Res}\{\Psi_1\}$ is the
 183 event plane resolution with Ψ_1 being the event plane angle, estimated from EPDs
 184 or ZDC-SMDs. In Fig. 3, we display the first measurements of Ξ and Ω baryon v_1 for
 185 10%-40% centrality in Au+Au collisions at $\sqrt{s_{NN}} = 27$ and 200 GeV. We perform
 186 a fit to the results with a linear function, $v_1(y) = Cy$, where C being the fitting
 187 parameter, and y being the rapidity. We found, $C = -0.021 \pm 0.008$ (-0.006 ± 0.01)
 188 for Ω^- ($\bar{\Omega}^+$) and $C = -0.009 \pm 0.002$ (-0.015 ± 0.003) for Ξ^- ($\bar{\Xi}^+$) at $\sqrt{s_{NN}} = 27$
 189 GeV. For $\sqrt{s_{NN}} = 200$ GeV, $C = -0.003 \pm 0.006$ (-0.003 ± 0.005) for Ω^- ($\bar{\Omega}^+$)

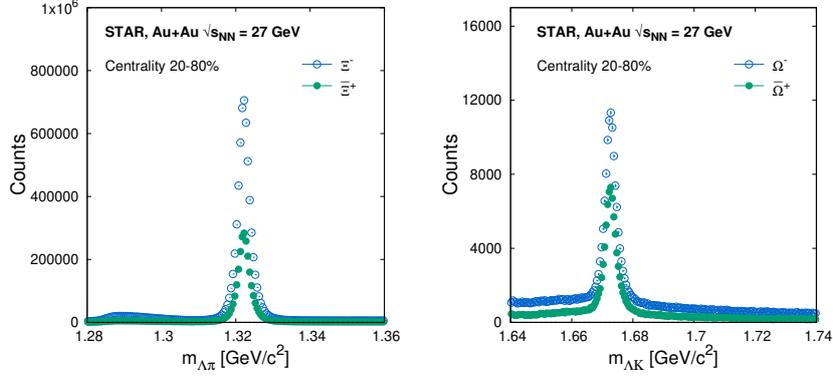


Fig. 2. Invariant mass distributions of Λ - π (left) and Λ - K (right) pairs for 20%-80% centrality in Au+Au collisions at $\sqrt{s_{NN}} = 27$ GeV.

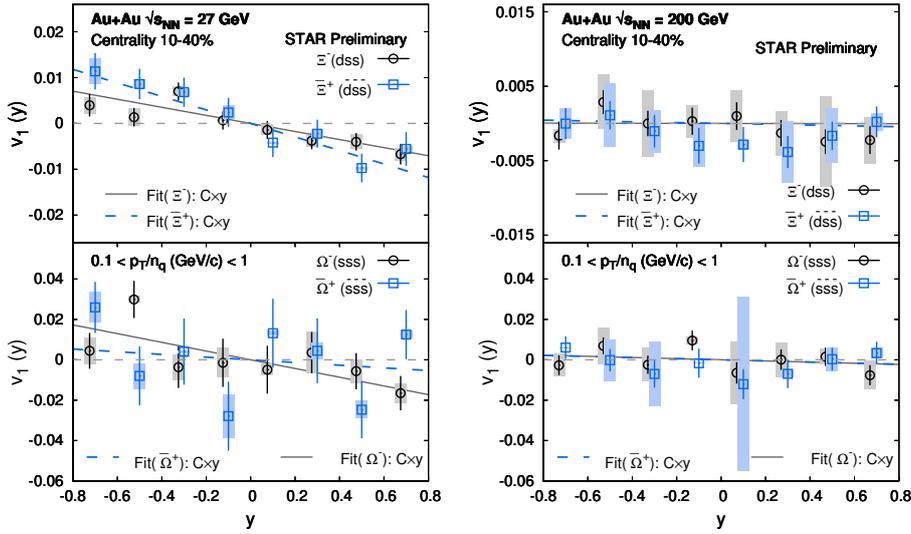


Fig. 3. Directed flow (v_1) of Ξ^- , Ξ^+ , Ω^- and Ω^+ as a function of rapidity (y) for 10%-40% centrality in Au+Au collisions at $\sqrt{s_{NN}} = 27$ and 200 GeV.

190 and $C = -0.000 \pm 0.002$ (-0.0005 ± 0.002) for Ξ^- (Ξ^+). Note that the slopes at
 191 $\sqrt{s_{NN}} = 200$ GeV have large errors. There is a hint of a larger v_1 for Ω^- compared
 192 to Ξ baryons at $\sqrt{s_{NN}} = 27$ GeV, but statistical uncertainties are also large here.

193 We also measure v_1 of the other produced particle species (K^- , \bar{p} , $\bar{\Lambda}$, and ϕ) and
 194 calculate Δv_1 for all seven combinations as shown in Table 1. Figure 4 displays the
 195 measured $\Delta v_1(y)$ for $\Delta q = 0, 2/3, 4/3$ and $\Delta S = 0, 1, 2$ in 10%-40% central Au+Au

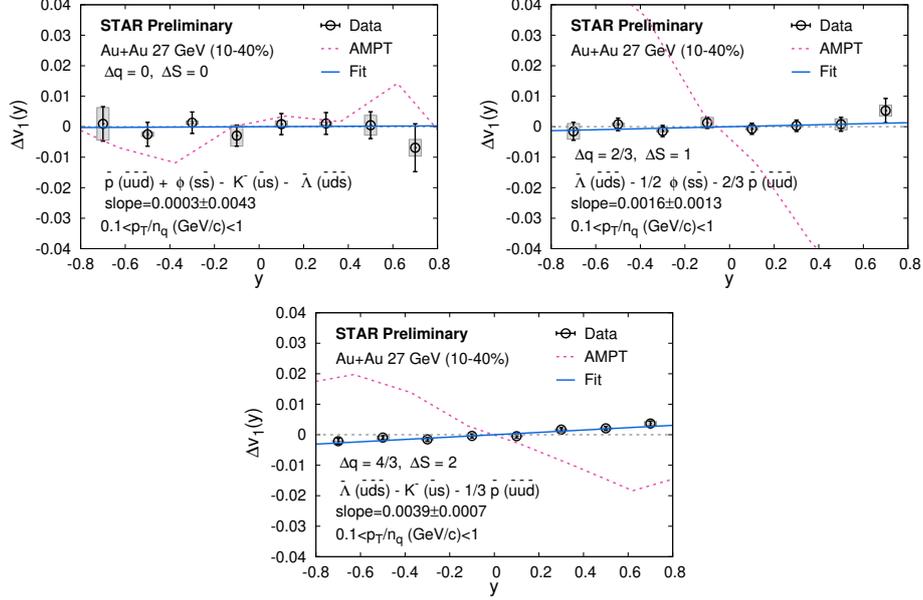


Fig. 4. Δv_1 as a function of rapidity (y) for $\Delta q = 0, 2/3, 4/3$ and $\Delta S = 0, 1, 2$ in 10%-40% central Au+Au collisions at $\sqrt{s_{NN}} = 27$ GeV. AMPT model calculations³⁹ are compared with the measurements.

196 collisions at $\sqrt{s_{NN}} = 27$ GeV. The measurements are fitted with a linear function
 197 and the slope parameter is extracted. For $\Delta q = 0$ and $\Delta S = 0$ (identical quark
 198 combination case), the value of the slope is a minimum compared to $\Delta q = 2/3$ and
 199 $4/3$ and $\Delta S = 1$ and 2 cases. This minimum deviation from zero indicates that
 200 the coalescence sum rule holds with the identical quark combination as mentioned
 201 above in Eqs. (2) and (3). The slope deviates more from zero as we move to Δq
 202 $= 2/3$ and $4/3$ and $\Delta S = 1$ and 2 . This deviation is presumably caused by the
 203 non-zero Δq and ΔS .

204 A Multi-Phase Transport (AMPT)³⁸ model calculations are compared with the
 205 measured Δv_1 . We took the AMPT results for individual particle v_1 from Ref.³⁹ and
 206 calculated the Δv_1 for different Δq and ΔS . It seems that the model calculations can
 207 describe the measured Δv_1 for the $\Delta q = 0, \Delta S = 0$ case, although the calculations
 208 show unexpected fluctuations around zero. For $\Delta q = 2/3$ and $4/3$ and $\Delta S = 1$ and
 209 2 , AMPT shows a completely opposite trend compared to the data.

210 Figure 5 depicts the Δv_1 -slope ($d\Delta v_1/dy$) at mid-rapidity as a function of Δq
 211 and ΔS for 10%-40% centrality in Au+Au collisions at $\sqrt{s_{NN}} = 27$ GeV and
 212 $\sqrt{s_{NN}} = 200$ GeV. Note that there are two data points at $\Delta q = 4/3$ and $\Delta S =$
 213 2 for each collision energy. These two points are the degenerate points (index 4
 214 and 5 in Table 1), plotted here to show the consistency between them. We fit
 215 the measurements at both collision energies with a linear function and show the

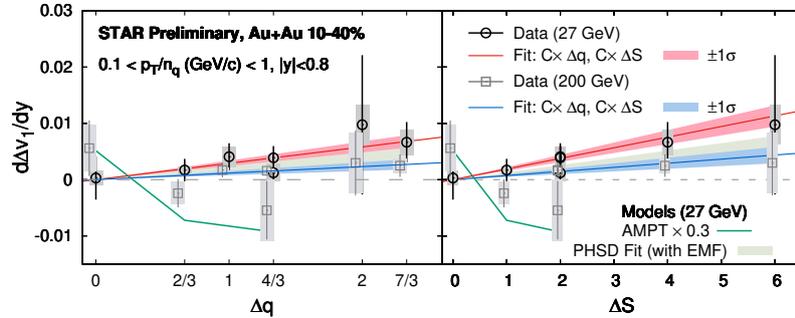


Fig. 5. Left panel: Δv_1 slope ($d\Delta v_1/dy$) at mid-rapidity as a function of electric charge difference (Δq , see Table 1) for 10%-40% centrality in Au+Au collisions at $\sqrt{s_{NN}} = 27$ GeV and $\sqrt{s_{NN}} = 200$ GeV. AMPT and PHSD+EM field model calculations are also plotted here.

Right panel: The same as the left panel, but as a function of strangeness (ΔS , see Table 1).

Note that the data points for $\sqrt{s_{NN}} = 200$ GeV in both panels are staggered horizontally for better visualization.

216 one- σ band of the fits around each fitted line. The red and blue lines are the
 217 fits to the $\sqrt{s_{NN}} = 27$ and 200 GeV data points, respectively. We observe when
 218 $\Delta q = 0$ and $\Delta S = 0$, the $d\Delta v_1/dy$ is close to zero within uncertainties. The identical
 219 quark combination (index 1 of Table 1) leads to $\Delta q = 0$ and $\Delta S = 0$ which
 220 seems to be the best scenario to verify the coalescence-inspired sum rule. For non-
 221 identical quark combinations ($\Delta q \neq 0$ and $\Delta S \neq 0$), the $d\Delta v_1/dy$ seems to deviate
 222 from zero and reaches a maximum when Δq and ΔS are a maximum. In other
 223 words, there is an increasing trend of $d\Delta v_1/dy$ with Δq and ΔS . The strength
 224 of the Δv_1 slope is stronger at $\sqrt{s_{NN}} = 27$ GeV than at $\sqrt{s_{NN}} = 200$ GeV. The
 225 AMPT and Parton-Hadron String Dynamics (PHSD)+electromagnetic field (EMF)
 226 model^{40,41} calculations have also been compared here with the data. The AMPT
 227 model predictions at $\sqrt{s_{NN}} = 27$ GeV are displayed by the green line, and they do
 228 not agree with the measurements. The PHSD+EMF calculations are shown by the
 229 light green band, and the calculations can explain the data within uncertainties. The
 230 PHSD model with EMF assumes that all electric charges are affected by the strong
 231 EMF and this results in a splitting of v_1 between positive and negative particles as
 232 observed in Fig 5. This splitting increases as the electric charge difference between
 233 positive and negative particles increases.

234 4. Summary

235 In summary, we report the first measurements of directed flow, $v_1(y)$, of multi-
 236 strange baryons (Ξ and Ω) in Au+Au collisions at $\sqrt{s_{NN}} = 27$ GeV and 200 GeV.
 237 We find that there is a hint of a relatively larger v_1 -slope for Ω^- compared to
 238 the Ξ baryons, however the statistical significance of the difference is 2.68σ . We
 239 focus on the produced particle species (K^- , \bar{p} , $\bar{\Lambda}$, ϕ , $\bar{\Xi}^-$, Ω^- , and $\bar{\Omega}^+$), and test the
 240 coalescence sum rule by using a novel analysis technique. Then we measure directed

241 flow splitting as a function of Δq and ΔS . The Δv_1 slope $d\Delta v_1/dy$, a measure
 242 of splitting, increases with Δq and ΔS . The strength of the splitting increases
 243 going from $\sqrt{s_{NN}} = 200$ GeV to $\sqrt{s_{NN}} = 27$ GeV. The observed $d\Delta v_1/dy$ is
 244 compared with AMPT and PHSD model calculations. AMPT model predictions
 245 do not agree with the measurements. Measurements are consistent with the PHSD
 246 model calculations that include the effect of the electromagnetic field.

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