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# Measurements of $p$ - $\Xi$ , $\Lambda$ - $\Lambda$ , and $\Xi$ - $\Xi$ Correlation in Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV at RHIC-STAR

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# Physics Motivation



- Hyperon-Hyperon (Y-Y) and Hyperon-Nucleon (Y-N) interactions are important for study of exotic hadronic states such as H-dibaryon as well as to understand the Equation of State of neutron stars.
- Possible bound state of Y-N and Y-Y (S=-2) ?

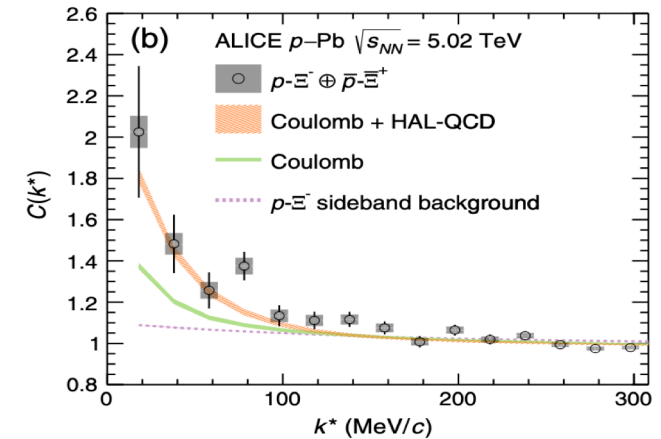
- Various hadrons including hyperons are abundantly produced in HIC.

- In ALICE, the attractive interaction of  $p-\Xi$  was observed in p+p and p+Pb collisions[1,2].

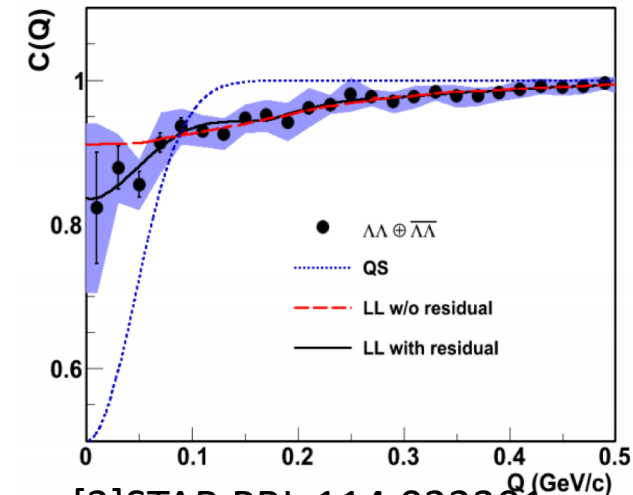
- In STAR, the anti-correlation of  $\Lambda-\Lambda$  was observed in Au+Au collisions with large uncertainty[3].



- In this study,  $p-\Xi$ ,  $\Lambda-\Lambda$ , and  $\Xi-\Xi$  correlations are studied at Au+Au  $\sqrt{s_{NN}} = 200$  GeV.



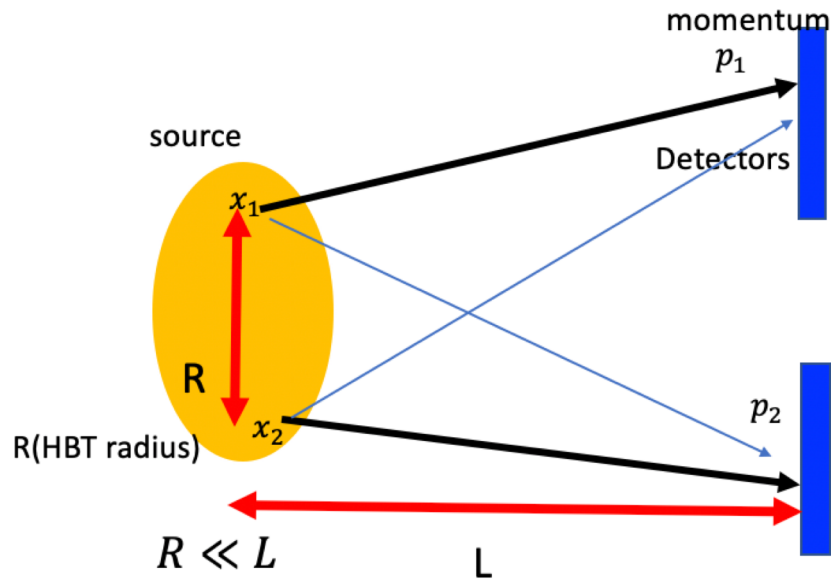
[1]ALICE PRL.123,112002



[3]STAR PRL.114.022301

[2]S. Acharya et al., Nature 588, 232 (2020)

# What's femtoscopy?



- Technique based on Bose-Einstein/Fermi-Dirac correlation has been used in heavy-ion collisions to probe the spatial and temporal extent of particle emitting source.
- Femtoscopic correlations arise due to **quantum statistical effects and final state (strong and Coulomb) interaction** (if present) at low relative momentum of two particles.

## Theory

$$C(q) = \int s(r) |\psi(q, r)|^2 dr^3$$

r: relative distance (of pair)

q: relative momentum  $q = \sqrt{q_x^2 + q_y^2 + q_z^2 - E_0^2}$

$s(r)$  source function     $\psi(q, r)$ : wave function of two-particles

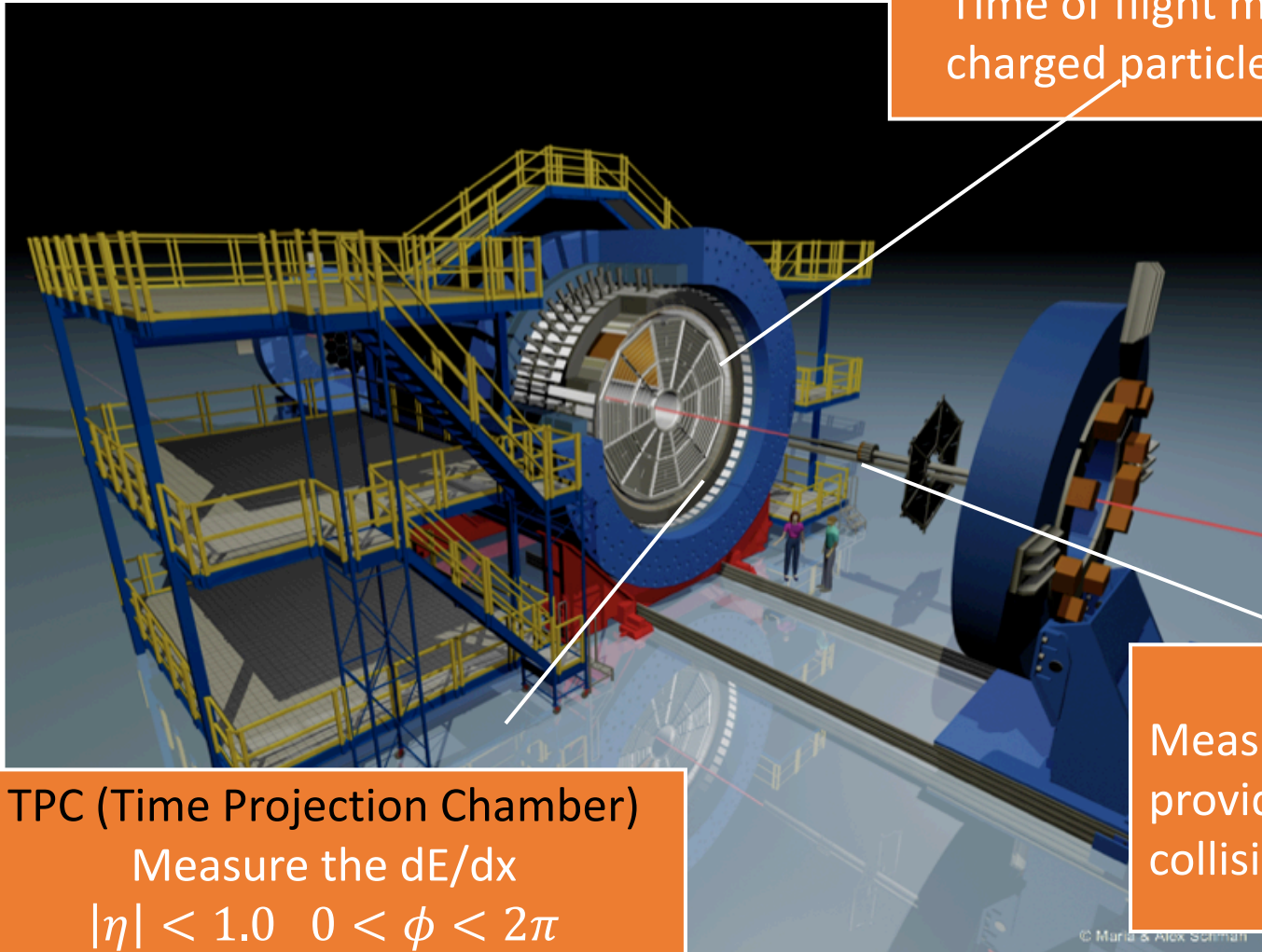
## Experiment

$$C(q) = \frac{A(q)}{B(q)}$$

A: actual pairs from same events

B: background pairs from mixed events

# STAR detectors



TOF (Time Of Flight)  
Time of flight measurement of  
charged particles,  $|\eta| < 0.9$

## Data Set

Au+Au  $\sqrt{s_{NN}} = 200$  GeV

	p-E	$\Lambda$ - $\Lambda$ and $\Xi$ - $\Xi$
Run year	2010, 2011, 2014	2011, 2014, 2016
Total events	1.5billion	2.8billion

TPC (Time Projection Chamber)

Measure the  $dE/dx$

$|\eta| < 1.0$   $0 < \phi < 2\pi$

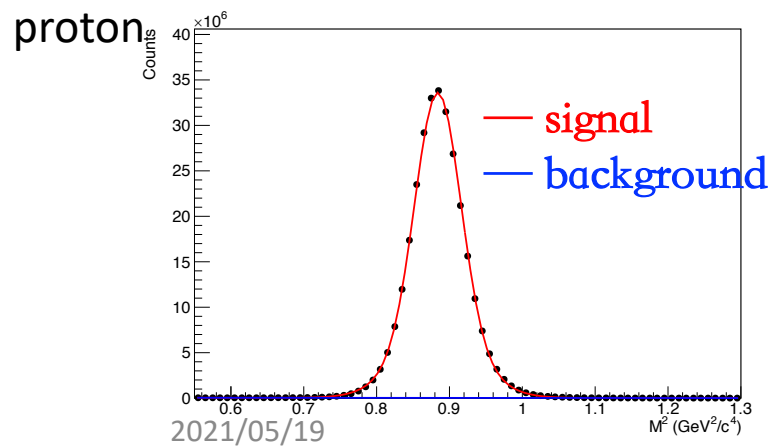
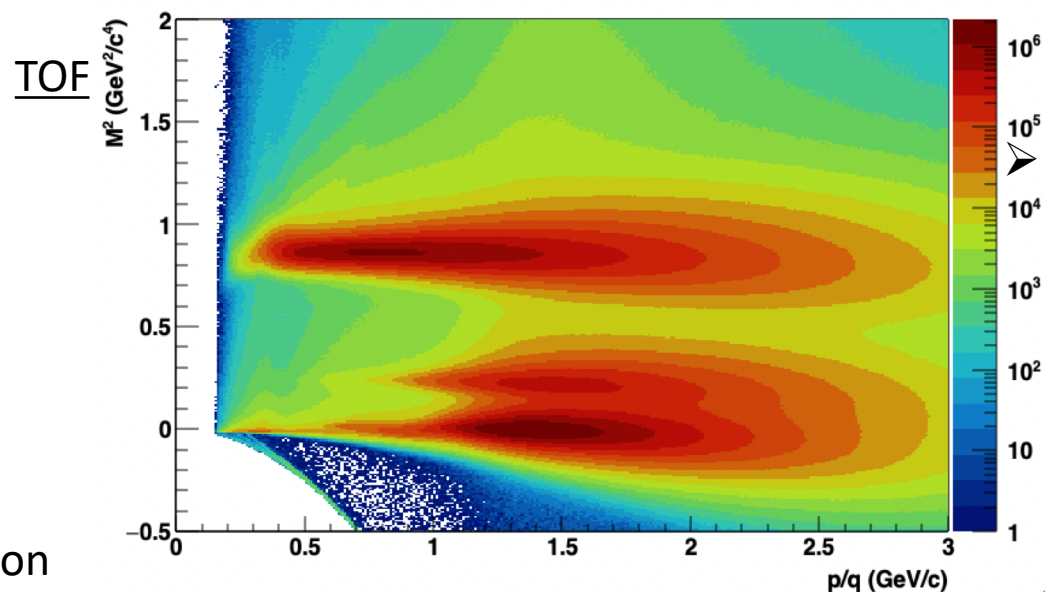
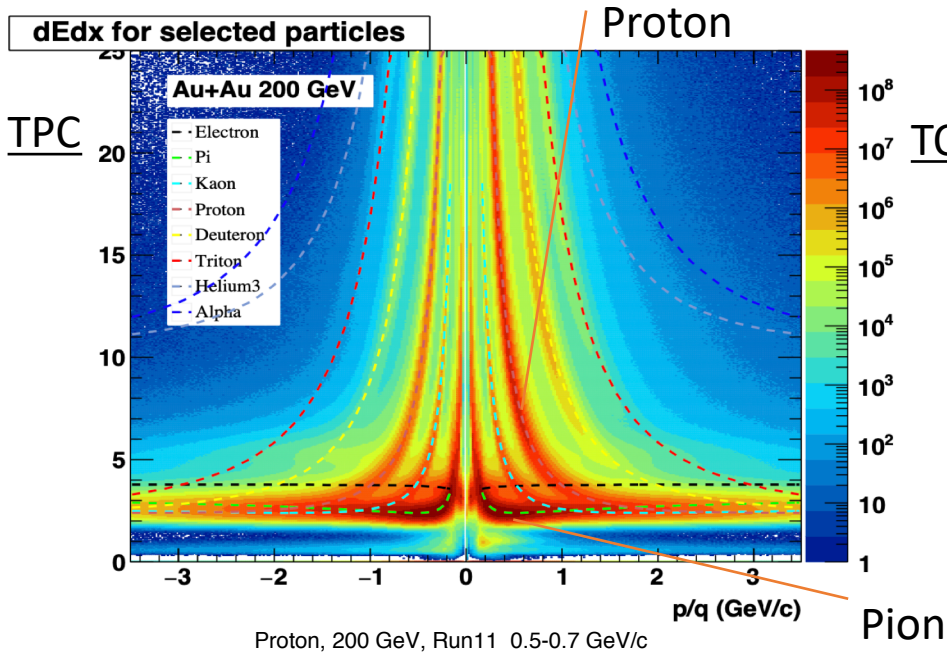
VPD (Vertex Position Detector)

Measure the start time,  
providing the minimum-bias trigger in Au+Au  
collisions.

# TPC & TOF PID



Particle identification based on dE/dx and time-of-flight



-proton selection

- $|n_{\sigma,p}| < 2$
- $0.75 < \text{Mass}^2 < 1.15(\text{GeV}/c^2)^2$
- $0.5 < p_T < 2.5 \text{ GeV}/c$
- $|y| < 1.0$

# Reconstruction of $\Lambda$ and $\Xi$

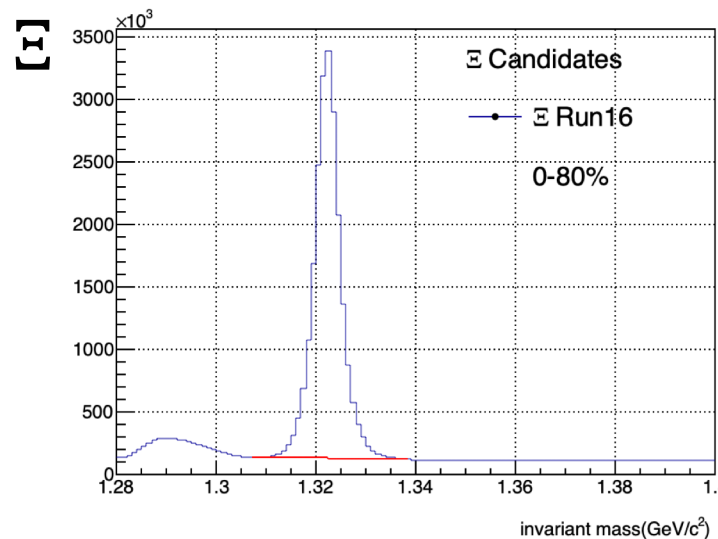
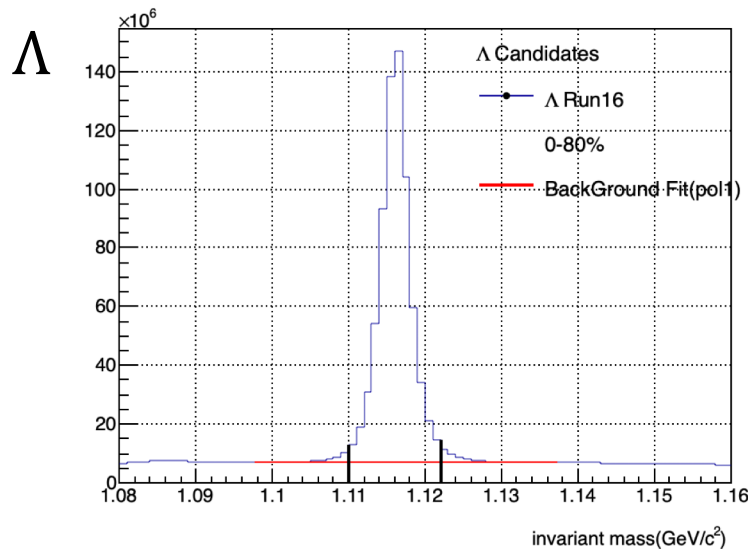


	Decay channel	Mass (from PDG 2018)
$\Lambda$ (uds) $\bar{\Lambda}$	$\Lambda \rightarrow \pi^- + p$ $\bar{\Lambda} \rightarrow \pi^+ + \bar{p}$ (63.9%)	1.115683 (GeV/c <sup>2</sup> )
$\Xi$ (dss) $\bar{\Xi}$	$\Xi \rightarrow \Lambda + \pi^+$ $\bar{\Xi} \rightarrow \bar{\Lambda} + \pi^-$ (99.87%)	1.32171 (GeV/c <sup>2</sup> )

- KFParticle package was used.  
KFParticle is based on Kalman filter.
- Very good Purity for  $\Lambda$ (~88%) and  $\Xi$ (~90%).

## Daughter particle selection for $\Lambda$ and $\Xi$

### Invariant mass



### For pion

- $|n_{\sigma,\pi}| < 3$
- $-0.15 < \text{Mass}^2 < 0.15 \text{ (GeV/c}^2\text{)}^2$

### For proton

- $|n_{\sigma,p}| < 3$
- $0.5 < \text{Mass}^2 < 1.5 \text{ (GeV/c}^2\text{)}^2$

### For $\Lambda$ and $\Xi$

- $p_T \geq 0.4 \text{ GeV}/c$
- $|y| < 1.0$

# Purity Correction



Correlation function is corrected for pair purity and feed-down as follows

$$C_{true}(q) = \frac{C_{measure}(q) - 1}{P(q) * F} + 1$$

**$P(q)$ : pair purity as a function of  $q$**

**F: Fraction of primary to inclusive particles**

$F(p) = 0.6 - 0.7$ ,  $F(\Xi^-) = 0.438$  (from Therminator2 model)

Residual correlation from background pairs is also studied.

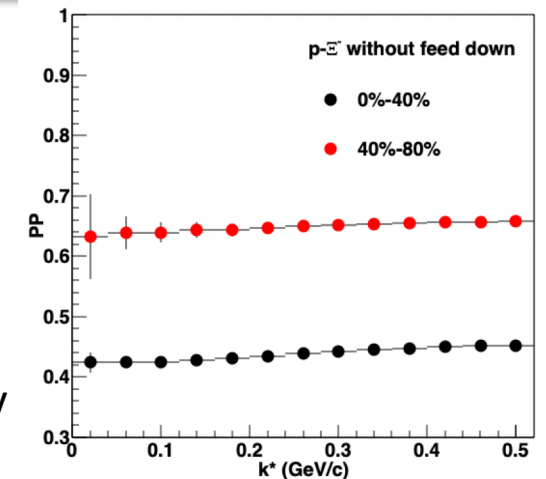
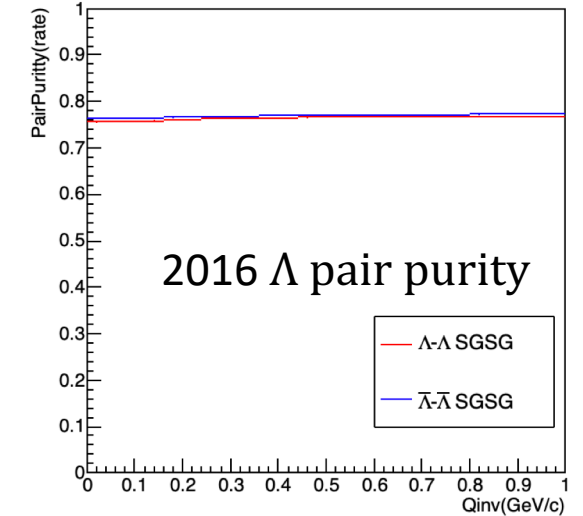
- Used for  $\Lambda$ - $\Lambda$  and  $\Xi$ - $\Xi$  study

$$C_{true}(q) = \frac{1}{P_{SGSG}(q)} \{ (C_{measured}(q) - 1) - 2 * (P_{SGBG}(q))(C_{SGBG}(q) - 1) - P_{BGBG}(q) * (C_{BGBG}(q) - 1) \} + 1$$

**$P_{SGBG}(q)$ : pair fraction of signal-background pairs**

**$P_{BGBG}(q)$ : pair fraction of background-background pairs**

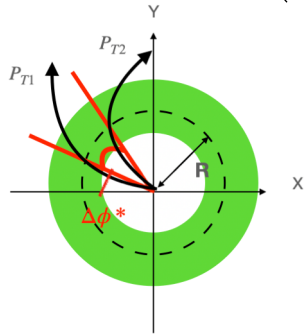
➤ the residual correlation was almost negligible on  $C(q)$ .



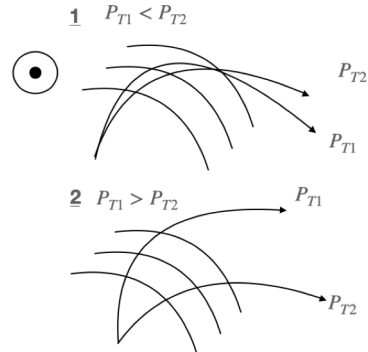
# Pair inefficiency and daughter sharing removal



$$\Delta\phi^* = \phi_1 - \phi_2 + \sin^{-1}\left(\frac{0.3eB_z R}{2p_{T1}}\right) - \sin^{-1}\left(\frac{0.3eB_z R}{2p_{T2}}\right)$$

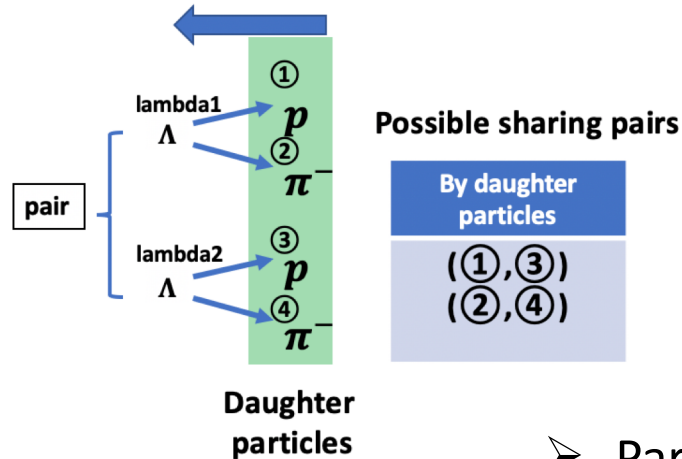


$p_{T1} < p_{T2}$



$p_{T1} > p_{T2}$

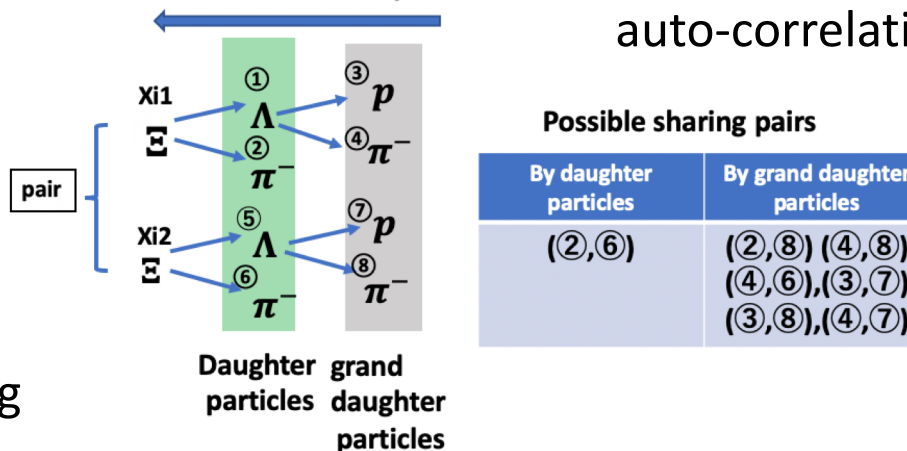
Particle reconstruction process



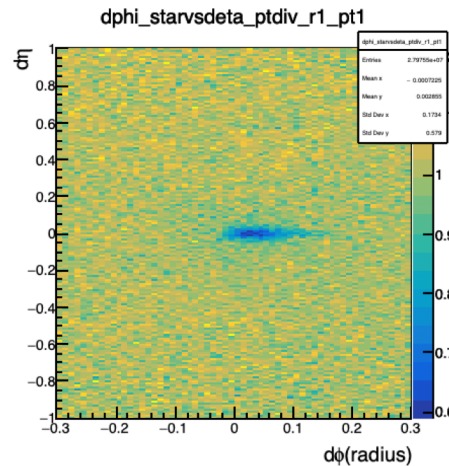
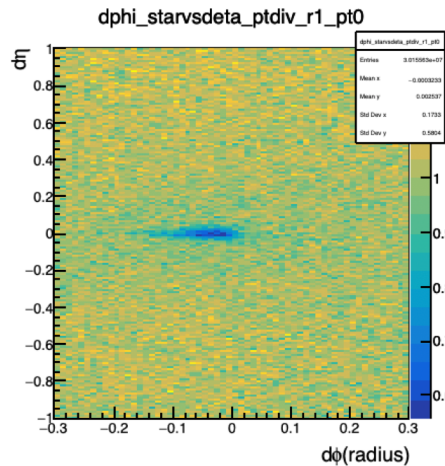
Daughter particles

➤ Particles sharing their daughters with others are removed to avoid auto-correlation.

Particle reconstruction process



Daughter grand daughter particles



daughter  
 $p - p$

➤ Pair inefficient region was removed considering B-field, particle charge, and  $p_T$ .



# $\Delta\phi$ vs $\Delta\eta$ correlation function

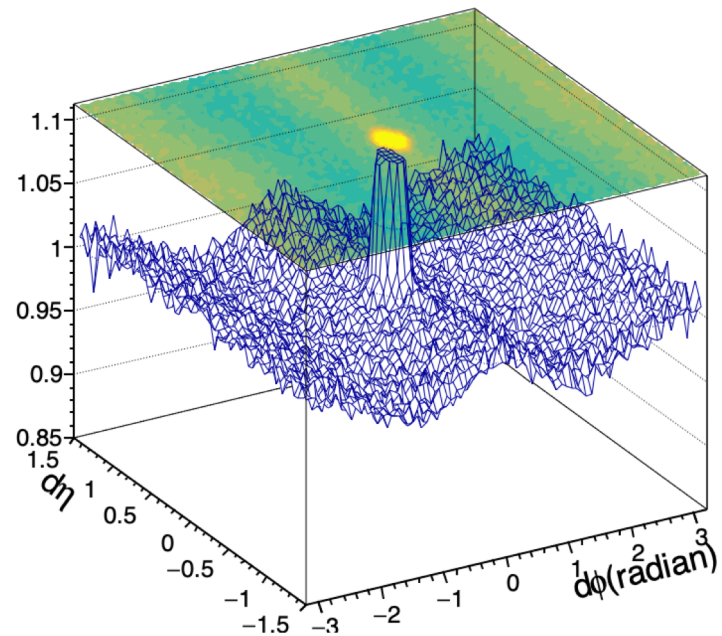


$$C_2(\Delta\phi, \Delta\eta) = \frac{N_{mix}^{pair} Y_{real}(\Delta\phi, \Delta\eta)}{N_{real}^{pair} Y_{mix}(\Delta\phi, \Delta\eta)}$$

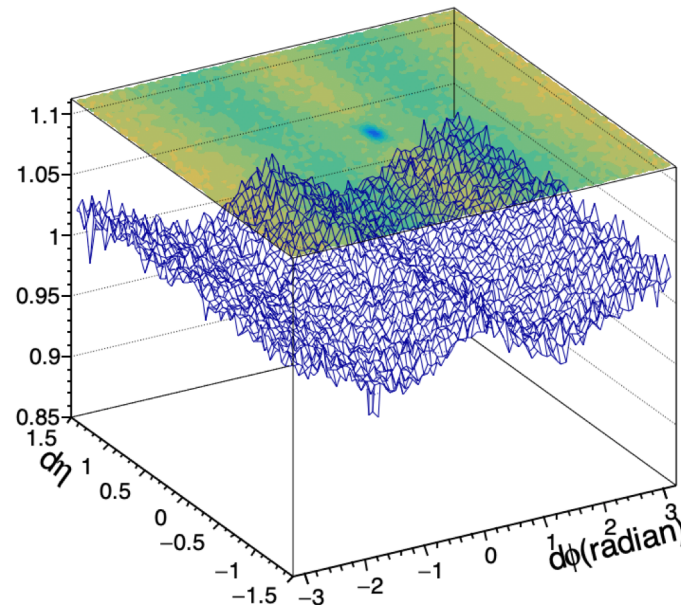
$$\Delta\eta = \eta_2 - \eta_1 \quad Y = \text{yield of pairs}$$

$$\Delta\phi = \phi_2 - \phi_1$$

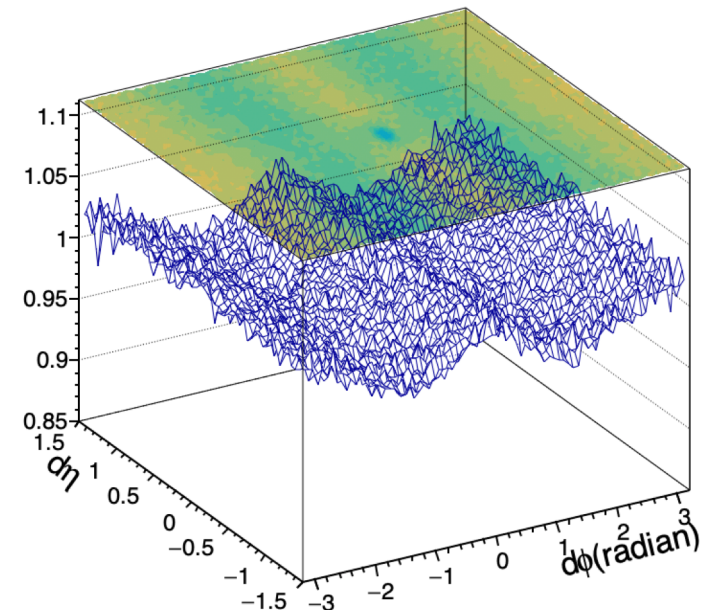
Before sharing cut  $\Lambda$ - $\Lambda$



After sharing cut  $\Lambda$ - $\Lambda$



After sharing cut  $\Lambda$ - $\Lambda$  + pair cut ( $\Delta\phi^*$  vs  $\Delta\eta$ )



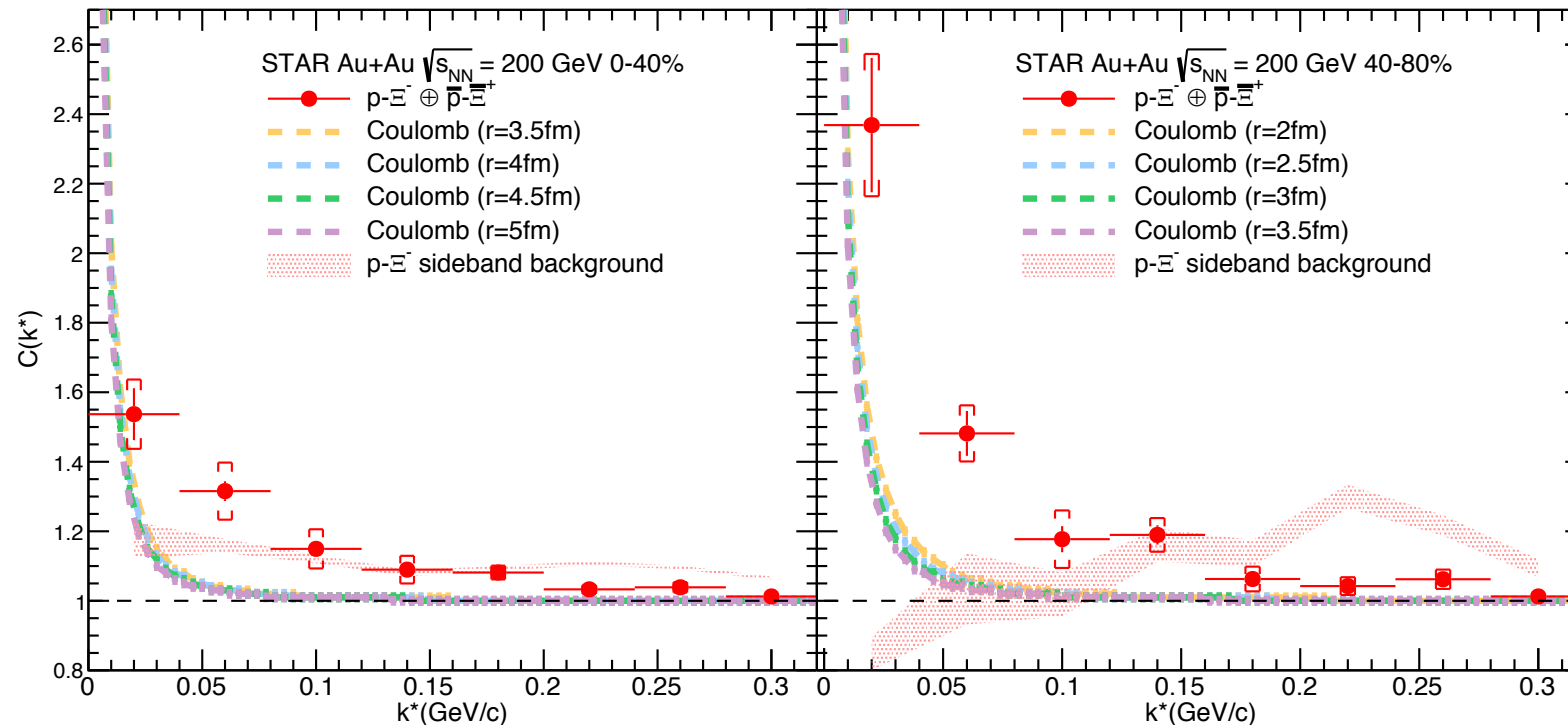
- The peak due to auto-correlation is gone after daughter sharing cut.
- The anti-correlation by detector inefficiency was largely mitigated.

**p-ε**

# p-Ξ correlation function



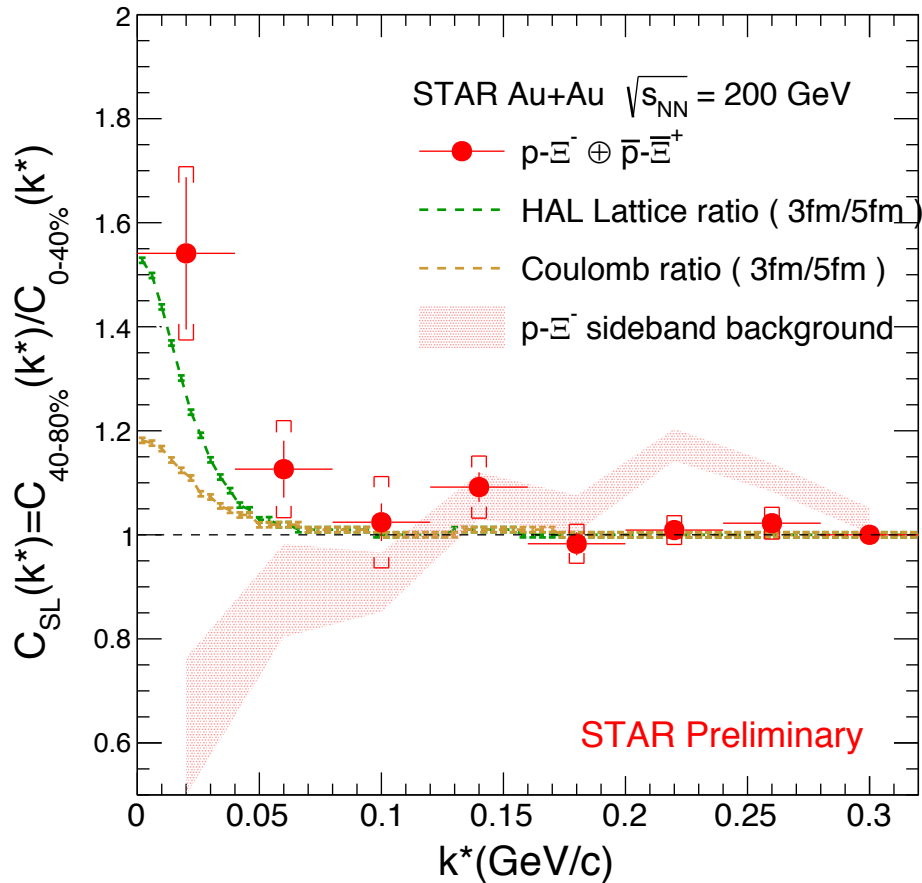
First measurement of p-Ξ correlation in Au+Au collisions at RHIC



$k^*$ : half of relative momentum in pair rest frame

- Feed-down is corrected using Theminator2 model, but residual correlation is not corrected yet.
- p-Ξ correlation shows enhancement above Coulomb interaction  
->Hints presence of strong interaction, and can not be described by sideband background.
- Sensitive to system size, more attractive in peripheral collisions (smaller collision system).

# p- $\Xi$ correlation function



$C(k^*)$  ratio of small to large systems,

$$C_{SL}(k^*) = \frac{C(k^*)_{40-80\%}}{C(k^*)_{0-40\%}}$$

$C_{SL}(k^*)$  is more sensitive to strong interaction with largely canceled Coulomb interaction[1].

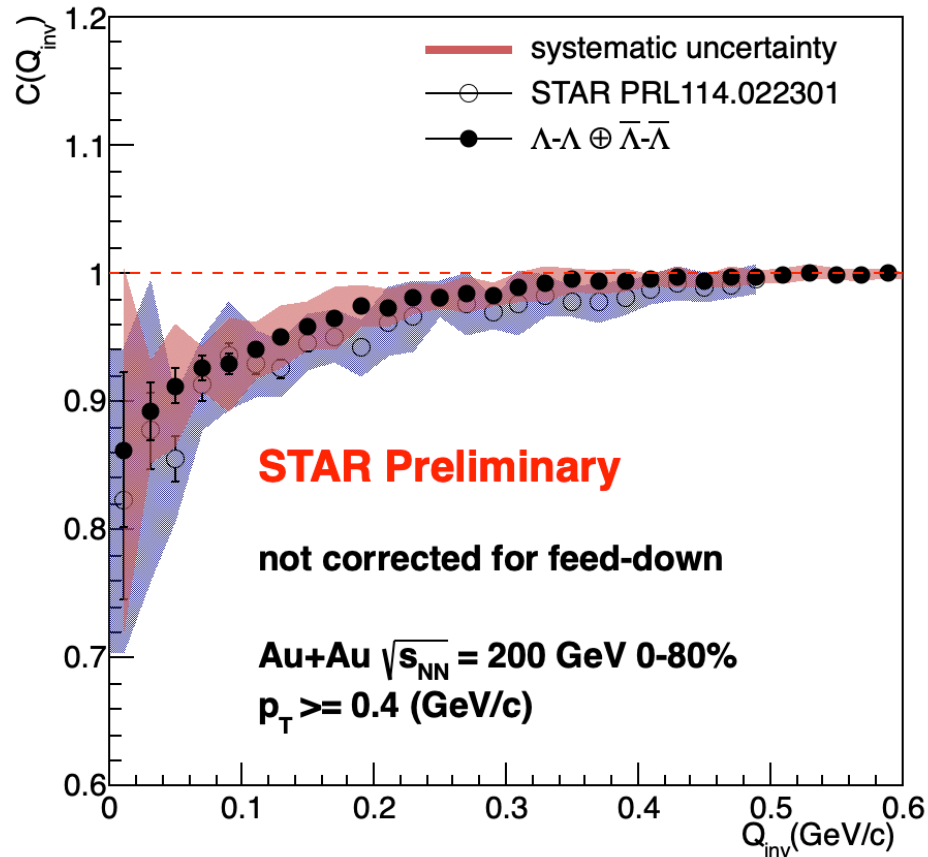
- Below  $k^* = 0.1$  GeV/c, the signal is enhanced beyond the Coulomb interaction and background.
- Similar to lattice QCD calculation [2] which suggests an attractive strong interaction between p and  $\Xi^-$ .

[1] K. Morita et al, Phys. Rev. C94(2016) 031901

[2] T.Hatsuda Nuclear Physics A 967 (2017) 856–859

**$\Lambda$ - $\Lambda$  and  $\Xi$ - $\Xi$**

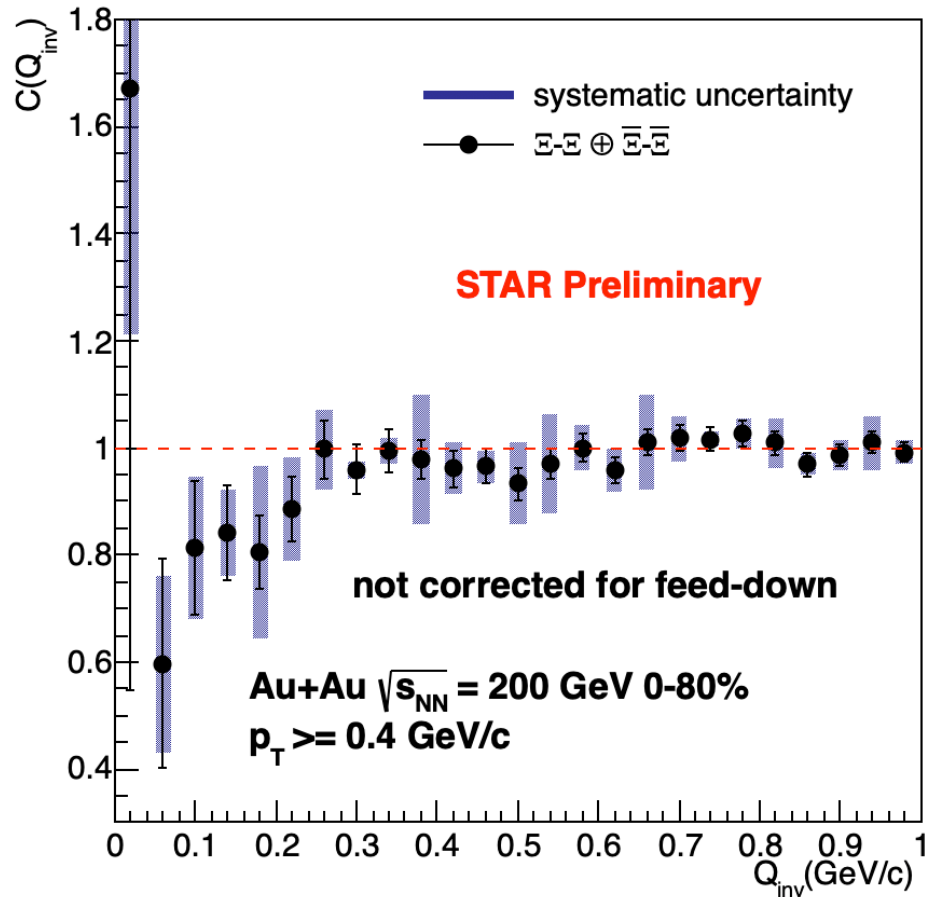
# $\Lambda$ - $\Lambda$ correlation function



- New result with high statistics data  $\sim 4$  times larger than that in previous study.
  - Not corrected for feed-down.
- Anti-correlation of  $\Lambda$ - $\Lambda$  is observed in Au+Au at  $\sqrt{s_{NN}} = 200$  GeV.
  - New result with better precision is consistent with previous result within systematic uncertainty.
  - There is a long tail of residual correlation in high  $Q_{inv}$ .

$$\text{relative momentum } Q_{inv} = \sqrt{q_x^2 + q_y^2 + q_z^2 - E_0^2}$$

# $\Xi$ - $\Xi$ correlation function



- First measurement of  $\Xi$ - $\Xi$  correlation in Au+Au collisions.
- Lattice QCD/chiral EFT calculations indicate an attractive interaction, but not strong enough to form a bound state [1,2].
- The result shows anti-correlation at  $Q_{inv} < 0.25$  GeV/c.  
- combination of quantum statistics, strong interaction, and Coulomb interaction.
- Feed-down and Coulomb effects need to be evaluated for further discussion.
- More events will be taken in 2023 and 2025.

[1] J. Haidenbauer et al., Eur. Phys. J. A 51: 17 (2015)  
[2] T, Doi et al., EPJ Web Conf. 175 (2018) 05009

# Summary

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- We presented the first measurements of p- $\Xi$  and  $\Xi$ - $\Xi$  correlations in Au+Au collisions at 200 GeV and also revisited  $\Lambda$ - $\Lambda$  correlations with high statistics data.
- **p- $\Xi$  correlation**
  - Attractive interaction is observed.
  - $C(k^*)$  ratio between peripheral and central collisions,  $C_{SL}(k^*)$ , is enhanced above the Coulomb interaction.
  - Similar to lattice QCD calculation which suggests an attractive strong interaction between p and  $\Xi^-$ .
- **$\Lambda$ - $\Lambda$  correlation function**
  - New result with high statistics data is consistent with previous result.
  - Anti-correlation is observed.
- **$\Xi$ - $\Xi$  correlation**
  - Anti-correlation seems to be observed for the first time.

## Outlook

- Feed-down and possible residual correlation are being studied.
- Extraction of the scattering parameters with Lednicky- Lyuboshitz model is ongoing (scattering length, effective range).



Back up

# 2 particle correlation analysis



## Analysis

- $A(\vec{q}, \vec{k})$  ----- distribution of pairs (same events)
- $B(\vec{q}, \vec{k})$  ----- distribution of Back ground pairs (mix events)
- $\vec{q} = \vec{p}_1 - \vec{p}_2$  -- Relative momentum of 2 particles
- $\vec{k} = \frac{(\vec{p}_1 + \vec{p}_2)}{2}$  - The average values of 2 particles momentums

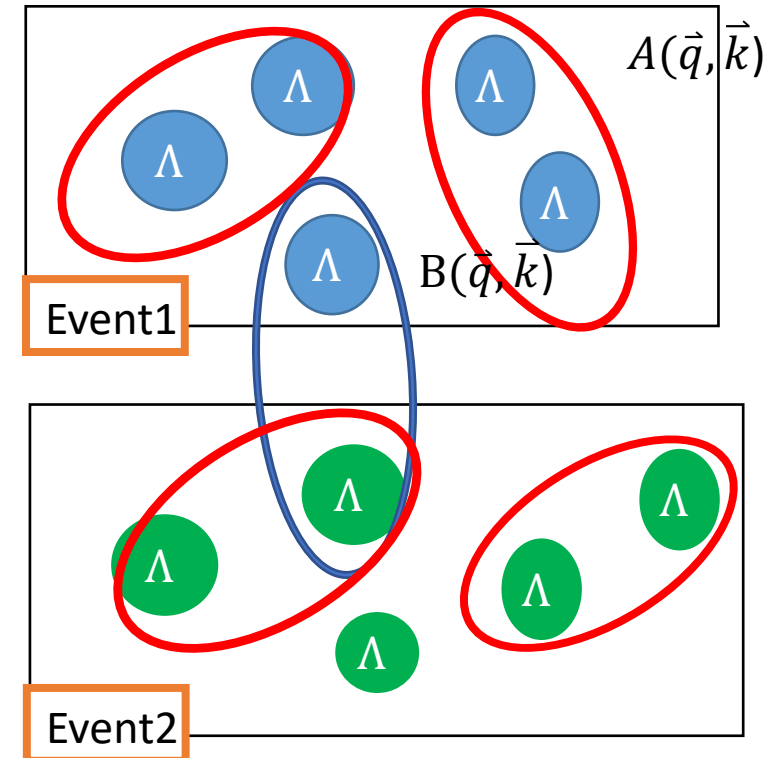
correlation function 
$$C(\vec{q}, \vec{k}) = \frac{A(\vec{q}, \vec{k})}{B(\vec{q}, \vec{k})}$$

## Event mixing method

mixed the events which close to Zvertex and centrality

- Real Event includes the physics correlation between 2 particles.
- Event mixing is used to make uncorrelated pairs as background.

## Event Mixing method



# Lednicky Fit



$$C(Q)_{Lednicky} = N \left[ 1 + \lambda \left( \underbrace{-\frac{1}{2} \exp(-r_0^2 Q^2)}_{\text{Quantum Statistic term}} + \underbrace{\frac{1}{4} \frac{|f(k)|^2}{r_0^2} \left( 1 - \frac{1}{2\sqrt{\pi}} \frac{d_0}{r_0} \right) + \frac{\text{Re}f(k)}{\sqrt{\pi} r_0} F_1(Qr_0) - \frac{\text{Im}f(k)}{2r_0} F_2(Qr_0)}_{\text{FSI(Final state interaction) term}} \right) + \underbrace{a_{res} \exp(-r_{res}^2 Q^2)}_{\text{Residual term}} \right]$$

(introduced by STAR to account for residual effect)

$k = \frac{Q}{2}, F_1(z) = \int_0^z \frac{e^{x^2-z^2}}{z} dx \dots \dots$  Approximate formula  $F_1(z) \cong \frac{1}{z} (1 - e^{-z^2}),$

$F_2(z) = (1 - e^{-z^2})/z$

$N$  : Normalization factor

$\lambda$  : chaotic parameter

$f_0$  : scattering length

$d_0$  : effective range

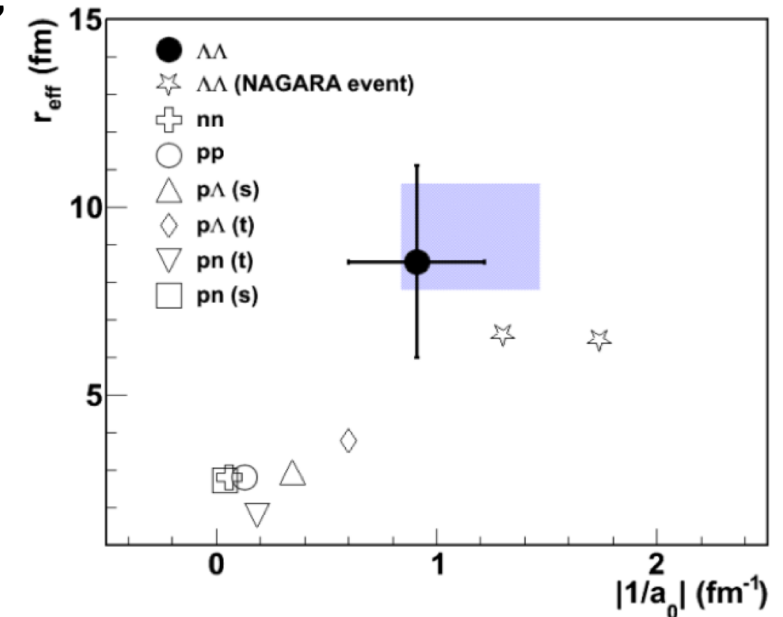
Physical quantity to study a bound state

$r_0$  : source size

$a_{res}$  : residual amplitude

$r_{res}$  : width of the Gaussian

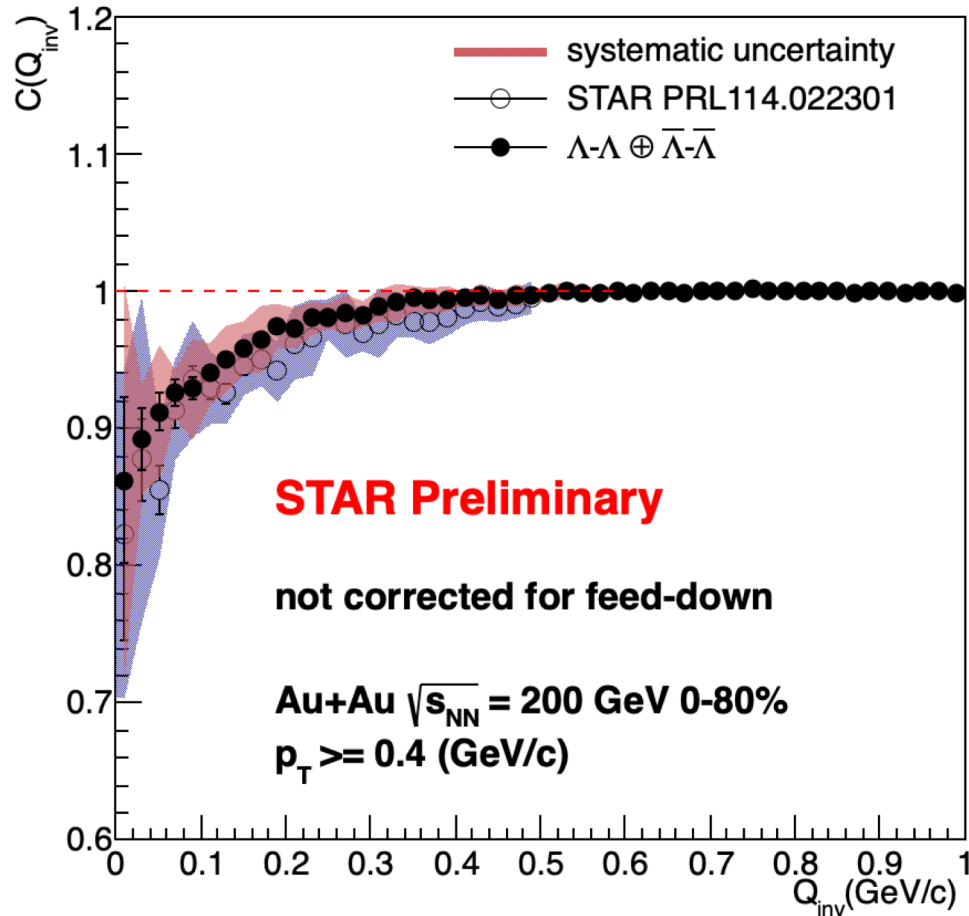
Scattering Amplitude:  $f(k) = \left( \frac{1}{f_0} + \frac{1}{2} d_0 k^2 - ik \right)^{-1}$



L. Adamczyk for the STAR Collaboration PhysRevLett.114.022301

Fitting method: ROOT default fitting(minimization)

# $\Lambda$ - $\Lambda$ correlation function



- New result with high statistics data  $\sim 4$  times larger than previous study.
  - Not corrected for feed-down.
- Anti-correlation is observed in  $\Lambda$ - $\Lambda$ .
  - New result with better precision is consistent with previous result within systematic uncertainty.
  - There seems to be residual correlation in high  $Q_{inv}$ .