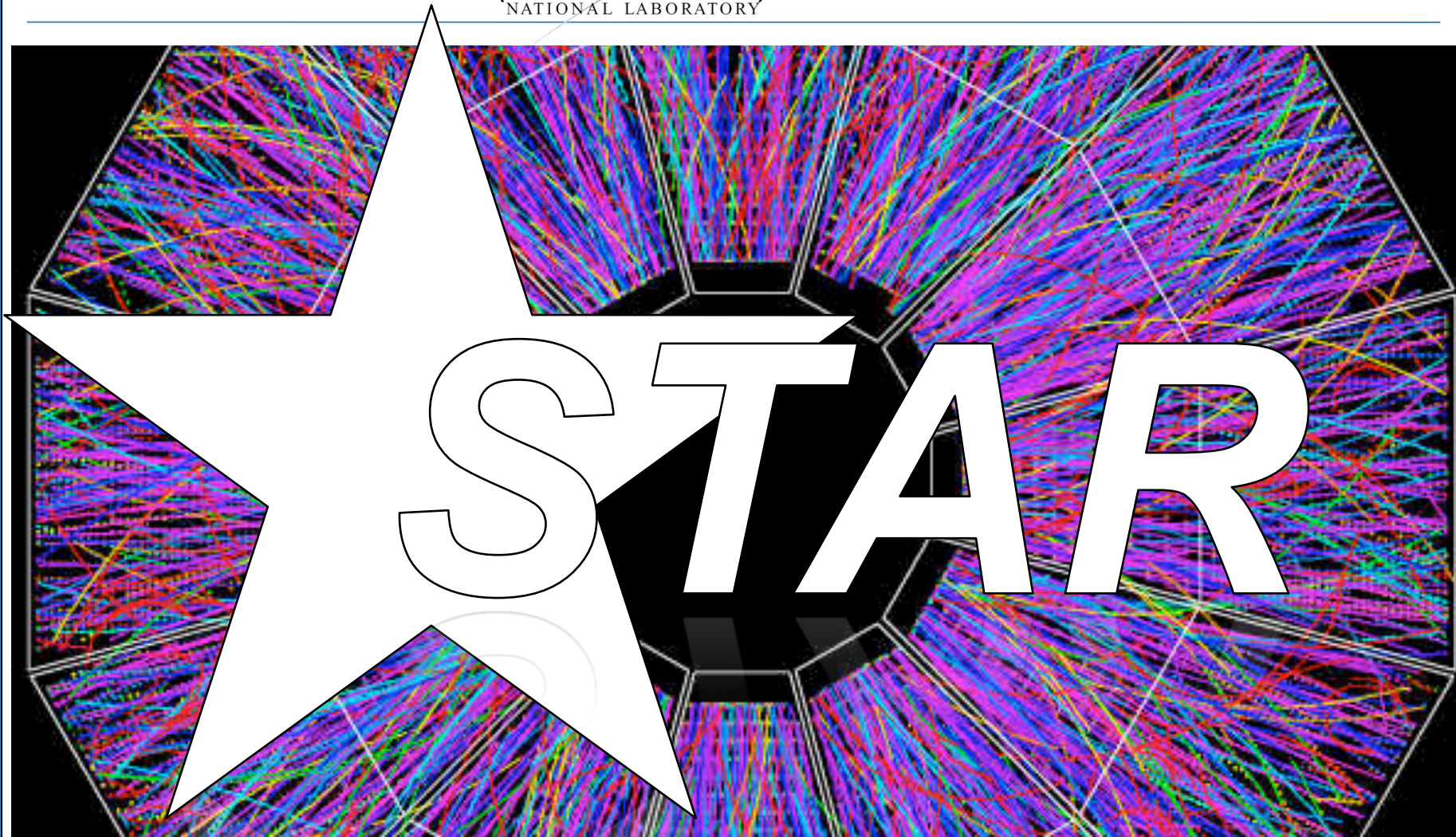


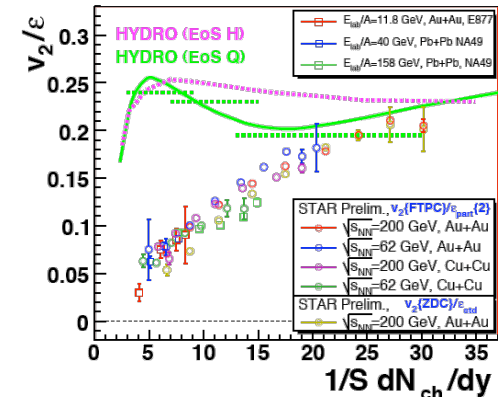
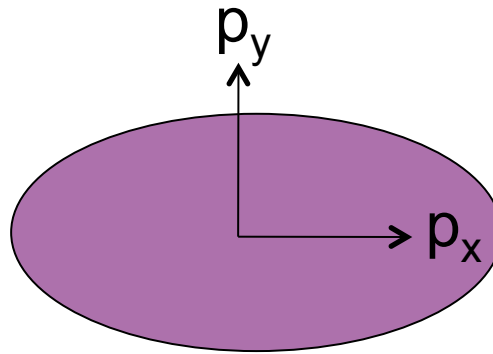
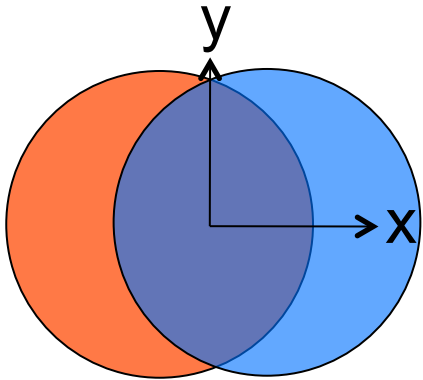
Higher Flow Harmonics from the STAR Collaboration at RHIC

Paul Sorensen (**BROOKHAVEN**) for the STAR Collaboration
NATIONAL LABORATORY



Why v_n Matters & What It Means

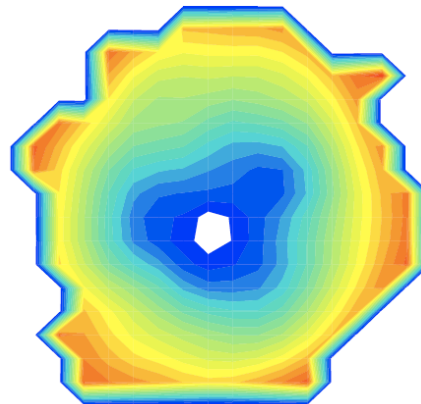
Voloshin, Poskanzer, Snellings, arXiv:0809.2949



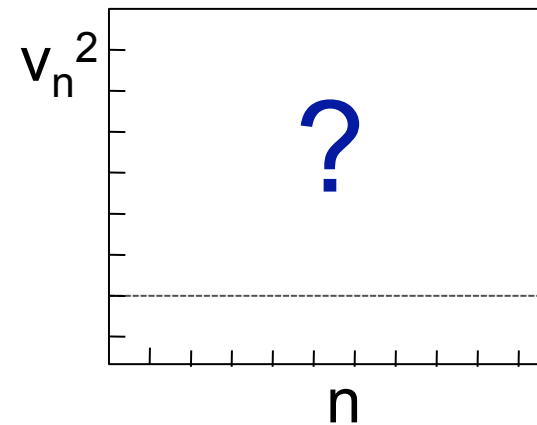
$$N_{\text{pairs}} \propto 1 + 2v_1^2 \cos \Delta\varphi + 2v_2^2 \cos 2\Delta\varphi + 2v_3^2 \cos 3\Delta\varphi + 2v_4^2 \cos 4\Delta\varphi + \dots$$



Kowalski, Lappi and Venugopalan, Phys.Rev.Lett. 100:022303



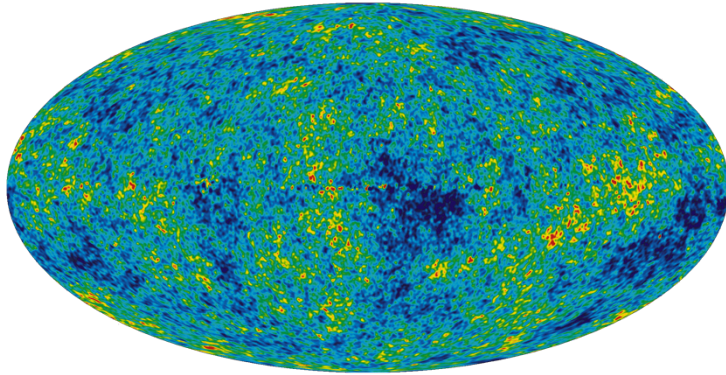
K. Werner, Iu. Karpenko, K. Mikhailov, T. Pierog, arXiv:11043269



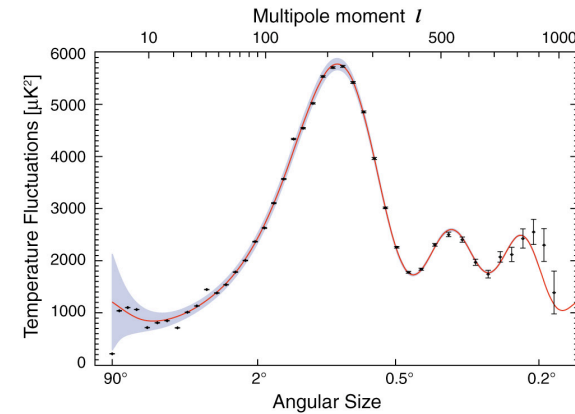
Fluctuations imply odd terms aren't necessarily zero and v_n^2 vs n will provide information about the system like lifetime, viscosity, etc.

A.P. Mishra, R. K. Mohapatra, P. S. Saumia, A. M. Srivastava, Phys. Rev. C77: 064902, 2008
 P. Sorensen, WWND, arXiv:0808.0503 (2008); J. Phys. G37: 094011, 2010

Why v_n Matters & What It Means



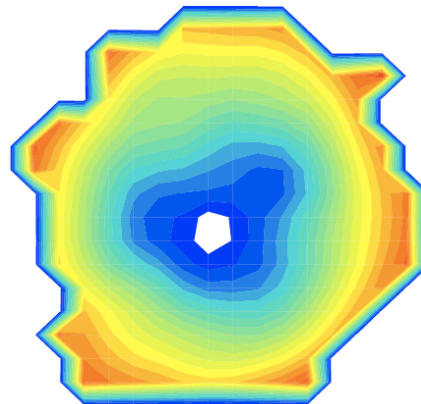
WMAP, *Astrophys.J.Suppl.* 170:288,2007



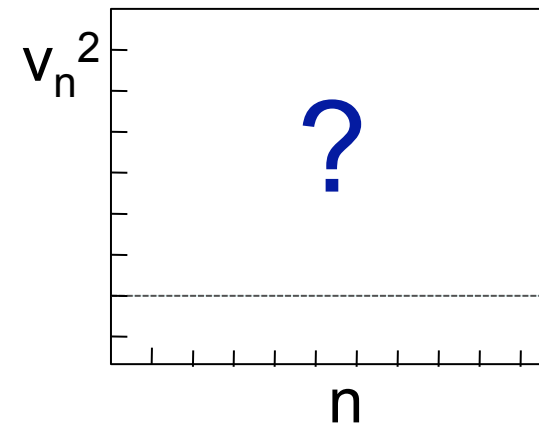
$$N_{pairs} \propto 1 + 2v_1^2 \cos \Delta\varphi + 2v_2^2 \cos 2\Delta\varphi + 2v_3^2 \cos 3\Delta\varphi + 2v_4^2 \cos 4\Delta\varphi + \dots$$



Kowalski, Lappi and Venugopalan,
Phys.Rev.Lett. 100:022303



K. Werner, Iu. Karpenko, K. Mikhailov, T. Pierog, arXiv:11043269



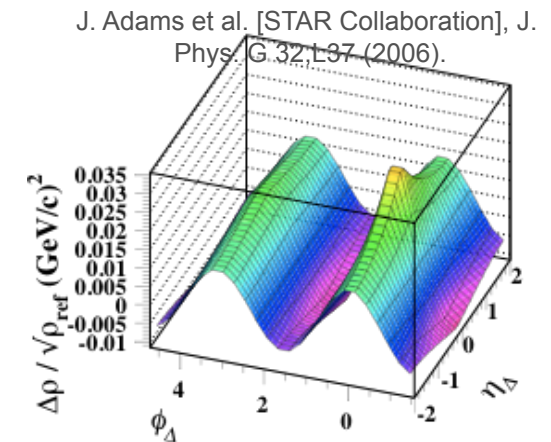
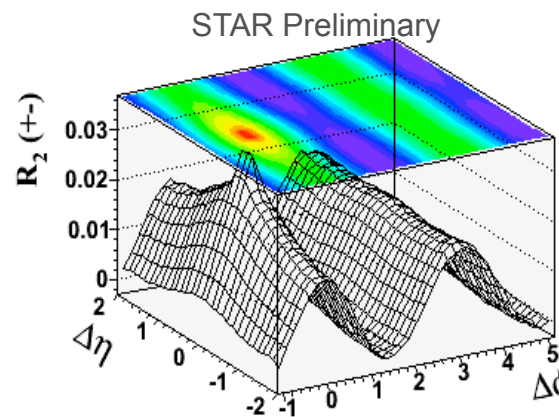
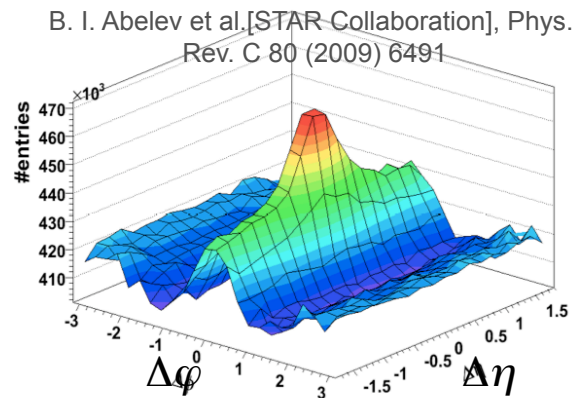
A. Mocsy, et. al. arXiv:1008.3381 [hep-ph]

Analogous to the Power Spectrum extracted from the Cosmic Microwave Background Radiation

A.P. Mishra, R. K. Mohapatra, P. S. Saumia, A. M. Srivastava, *Phys. Rev. C* 77: 064902, 2008
P. Sorensen, WWND, arXiv:0808.0503 (2008); *J. Phys. G* 37: 094011, 2010

Correlation Landscape at RHIC

The correlation landscape *–is rich in information–* on jets, jet modification, transport, early-times, and space-momentum correlations like flow



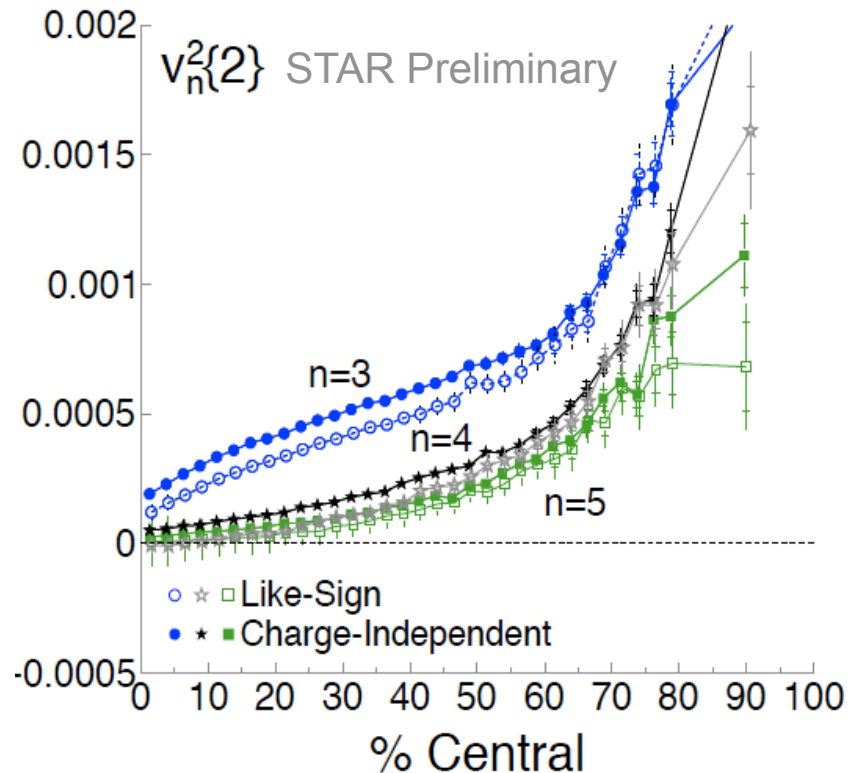
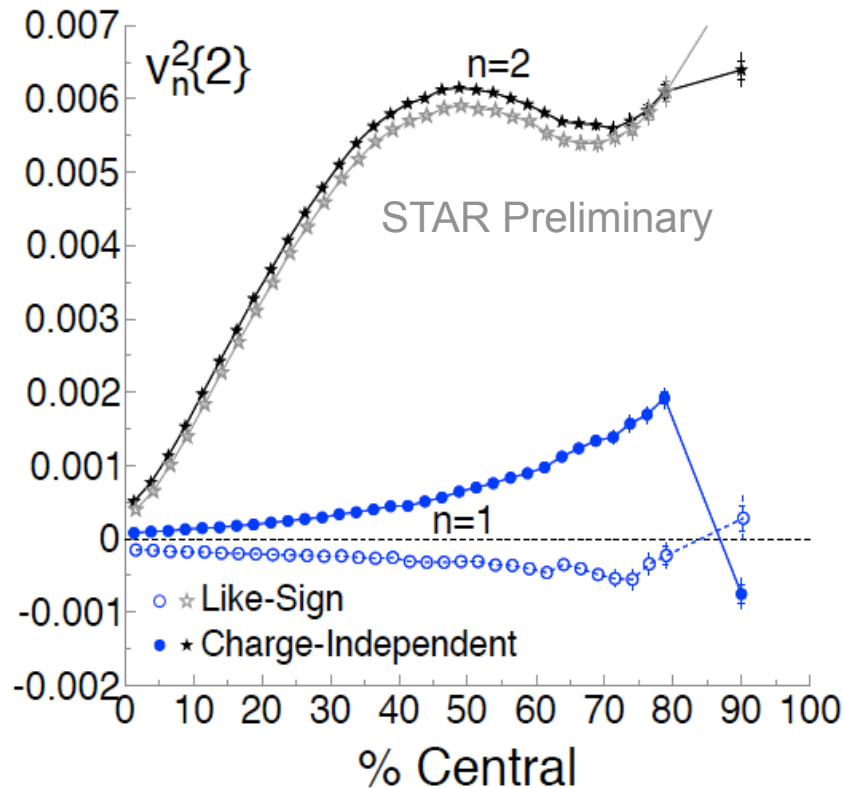
The understanding of higher harmonic v_n^2 is central to understanding the meaning of the correlations landscape in heavy ion collisions

- P. Sorensen, arXiv:0808.0503; J. Phys. G37: 094011, 2010;
- B. Alver, G. Roland Phys. Rev. C81:054905, 2010;
- B. Alver, Gombeaud, Luzum, Ollitrault, Phys.Rev.C82:034913,2010
- P. S., A. Mocsy, B. Bolliet, Y. Pandit, arXiv:1102.1403

We'll use correlations to extract the power spectrum from heavy-ions and investigate it's possible relationship to the early times

Higher v_n from 2 Particle Correlations

Q-Cumulants: 200 GeV Au+Au $|\eta| < 1.0$



$n=1$ shows large difference between LS and CI: charge and momentum conserv?

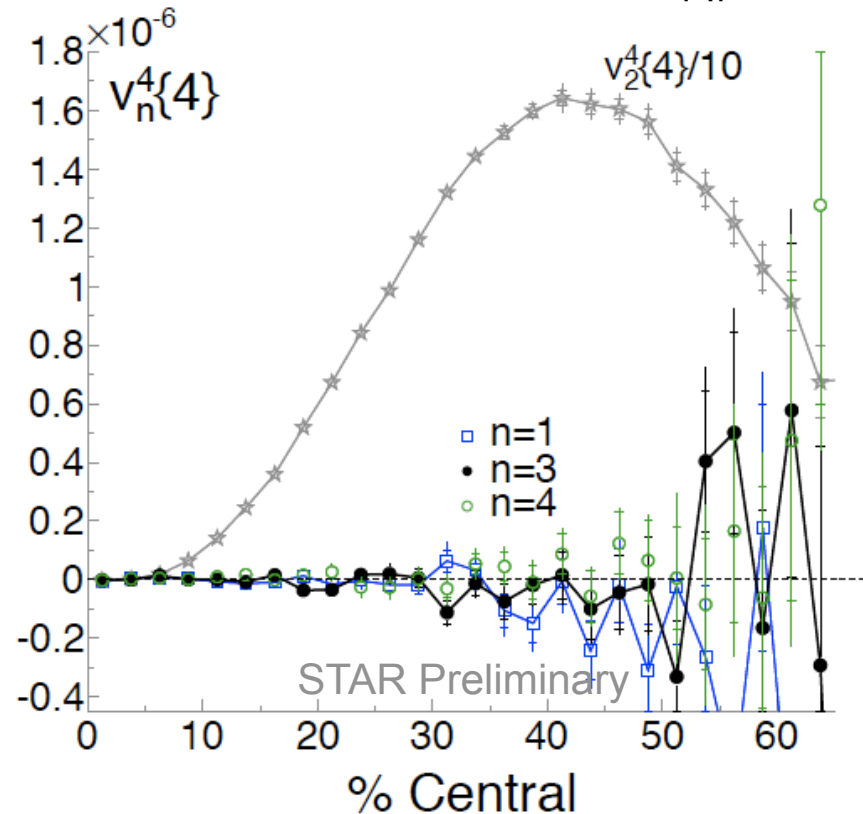
$n=3$ exhibits effects of elliptic overlap geometry

$n=4$ and larger show $1/N$ dependence typical of non-flow correlations

Q-Cumulants: A. Bilandzic, R. Snellings, S. Voloshin, Phys. Rev. C 83, 044913 (2011)

Higher v_n from 4 Particle Correlations

Q-Cumulants: 200 GeV Au+Au $|\eta| < 1.0$



v_4 from mixed harmonics is within errors of $v_4^4\{4\}$:
 $v_4 \sim v_2^2 \sim 0.1^2$
 $v_4^4 \sim 10^{-8}$

$v_n\{4\}$ consistent with zero for odd terms. Consistent with $v_3^2\{2\}$ being due to non-flow **and/or** with $v_n \propto \epsilon_{n,part}$: for $v_n \propto \epsilon_{n,part}$, $v_n\{4\} \propto \epsilon_{n,std}$

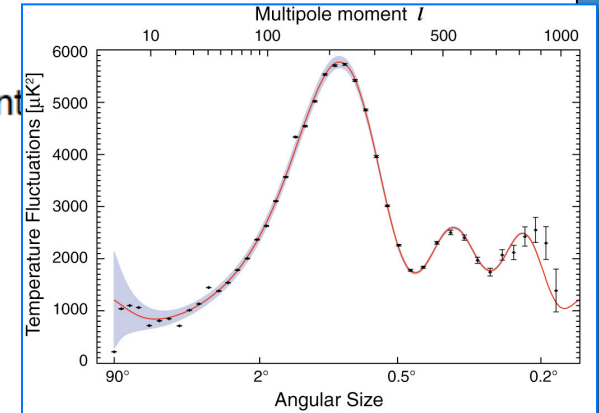
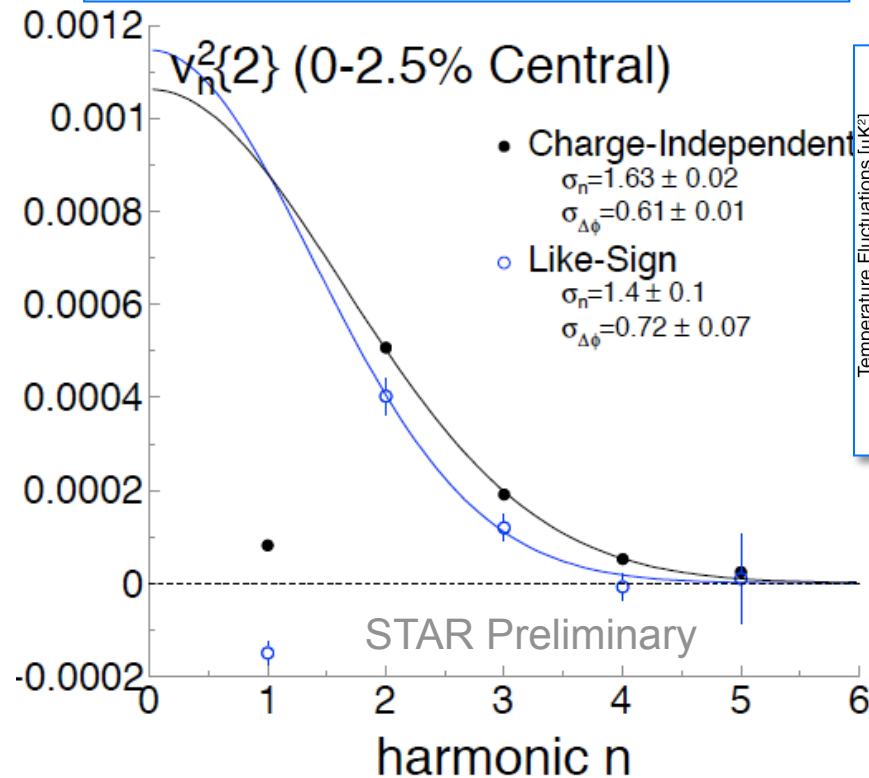
R.S. Bhalerao and J-Y. Ollitrault, Phys.Lett.B641:260-264 (2006)

S. Voloshin, A. Poskanzer, A. Tang, G. Wang, Phys.Lett.B659:537-541 (2008)

For 0-2.5% central $v_2\{4\} \approx 0$ indicates elliptic shape is nearly gone. We'll look at the shape of $v_n^2\{2\}$ vs n for nearly symmetric collisions

$v_n^2\{2\}$ vs n for 0-2.5% Central

This is the Power Spectrum of Heavy-Ion Collisions



$|\eta| < 1$

$v_n\{4\}$ is zero for 0-2.5% central: look at $v_2^2\{2\}$ vs n to extract power spectrum in nearly symmetric collisions

Fit by a Gaussian except for $n=1$ (momentum conservation): width can be related to length scales: viscous, acoustic horizon, $1/2\pi T \dots$

P. Staig and E. Shuryak, arXiv:1008.3139 [nucl-th]

A. Mocsy, P. S., arXiv:1008.3381 [hep-ph]

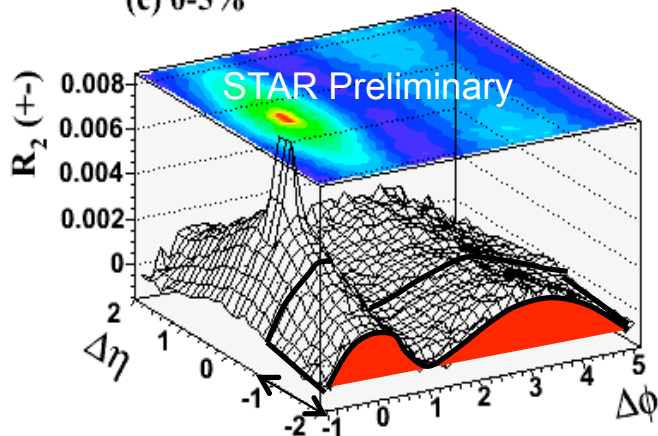
A. Adare [PHENIX], arXiv:1105.3928

Integrates all $\Delta\eta$ within acceptance: we can look more differentially to assess non-flow

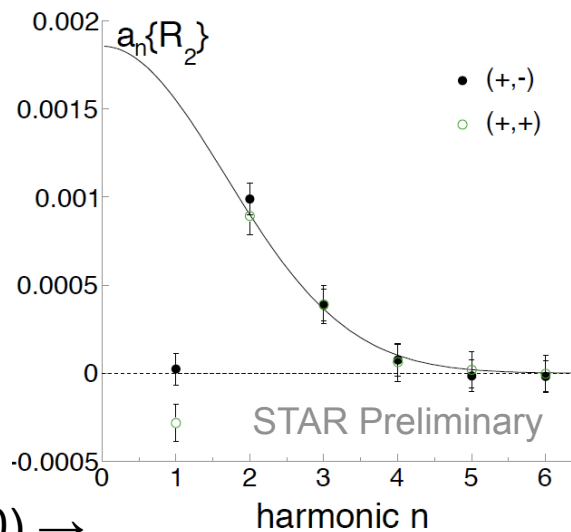
Large $\Delta\eta$ Power Spectrum a_n necy

$$R_2 = \frac{\rho_{12}}{\rho_1 \rho_2} - 1$$

(c) 0-5%



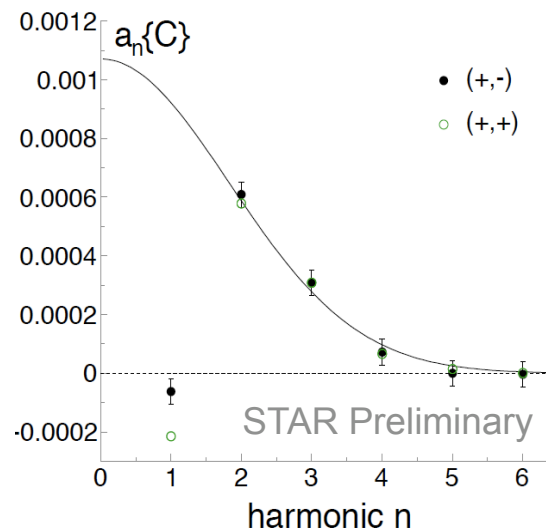
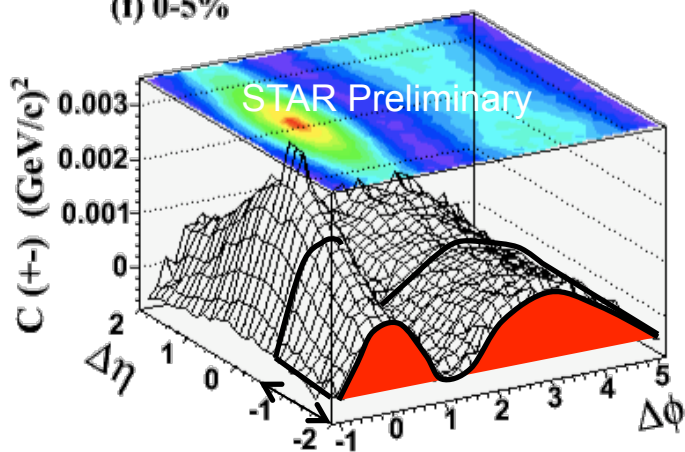
if flow dominates the correlations $a_n \approx v_n^2$



→ Fourier Tr. ($0.7 < \Delta\eta < 2.0$) →

$$C = \frac{\left\langle \sum_{i=1}^{n_1} \sum_{j=1 \neq i}^{n_2} p_{T,i} p_{T,j} \right\rangle}{\bar{n}_1 \bar{n}_2} - \bar{p}_{T,1} \bar{p}_{T,2}$$

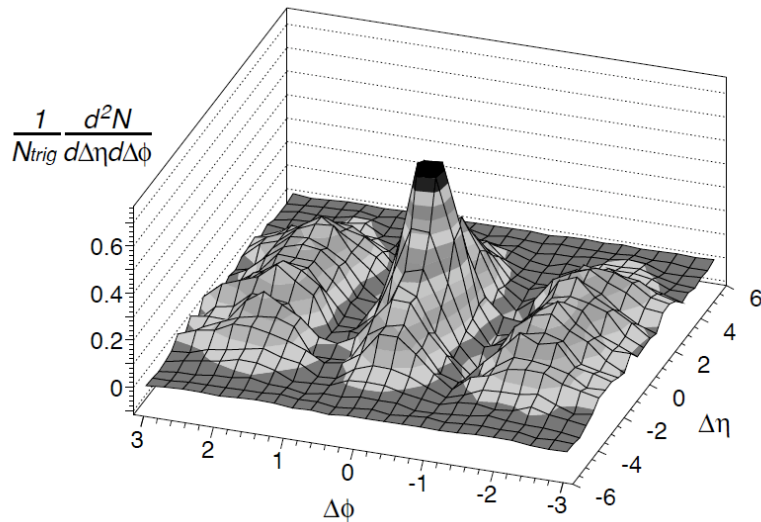
(f) 0-5%



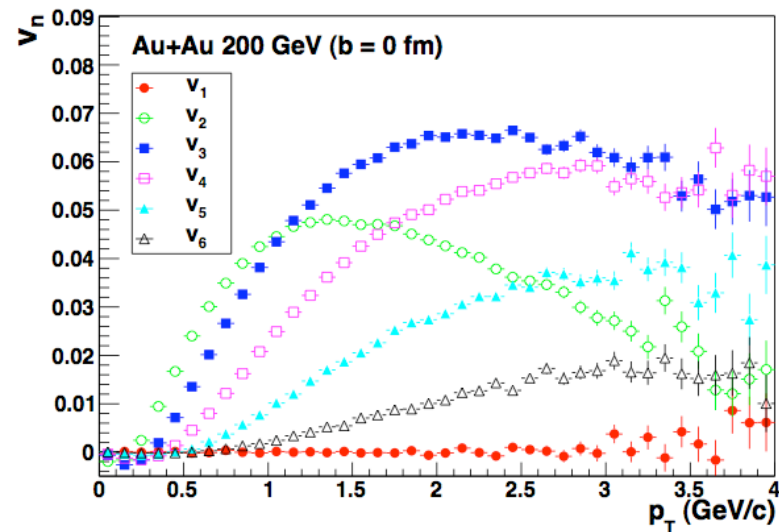
See also: A. Mocsy, P. S., arXiv:1008.3381 [hep-ph]

Recent Theoretical Developments

In a system where space-momentum correlations develop, the initial density fluctuations can manifest in momentum space



J.Takahashi, B.Tavares, W.Qian, F.Grassi, Y.Hama, T.Kodama & N.Xu and many others



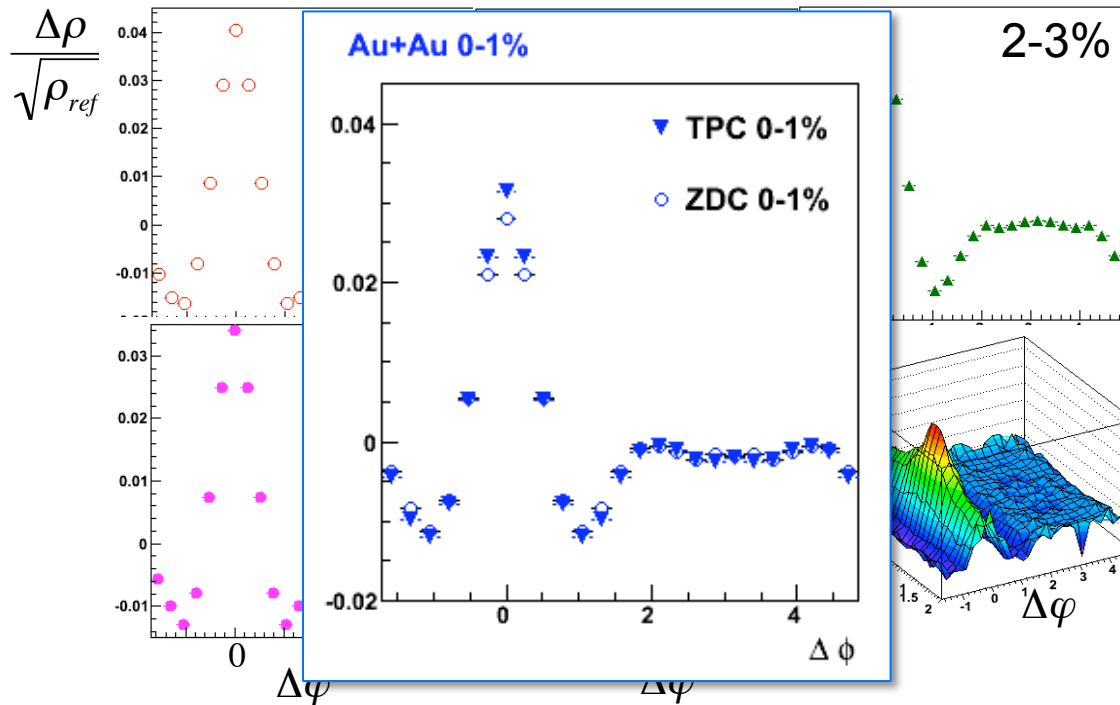
G. L. Ma and X. N. Wang, PRL106, 162301 (2011)

Ridge appears in hydro calculations with fluctuating initial conditions: doesn't require a jet explanation

For $b=0$ fm, at low p_T , v_n drops with n , but at intermediate p_T , $v_3 > v_2$

Correlations at Intermediate p_T

v_3 should be most evident at intermediate p_T and for central collisions where the overlap geometry is most symmetric



See Poster: C. de Silva
(255, Board 15)

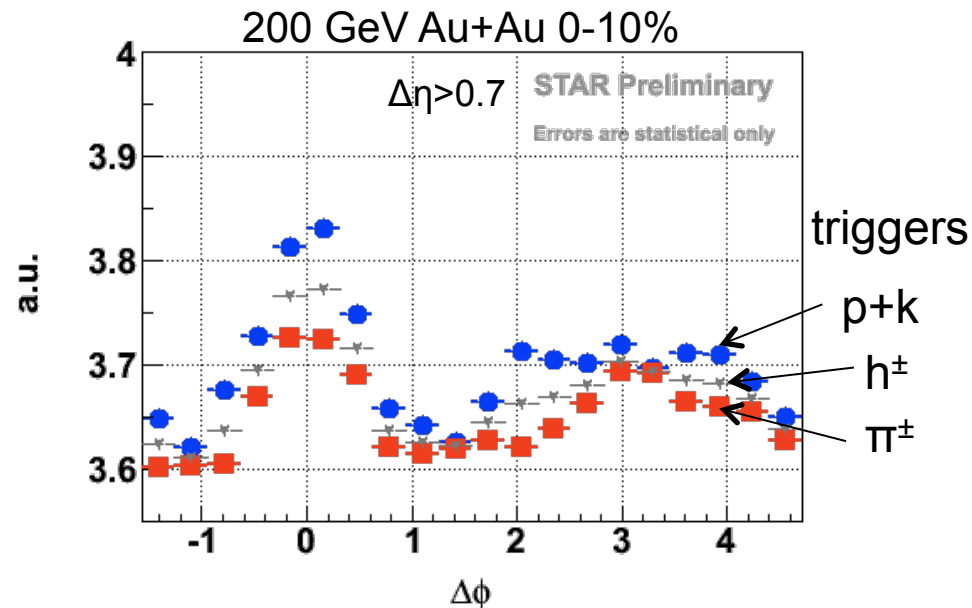
For 0-1% central, $n=3$ double hump is present on the away-side **without v_2 subtraction**

We see effects consistent with expectations, we'll investigate further by looking at various measurements related to v_n

Correlations at Intermediate p_T

v_3 should be most evident at intermediate p_T and for central collisions where the overlap geometry is most symmetric

See Talk: K. Kauder



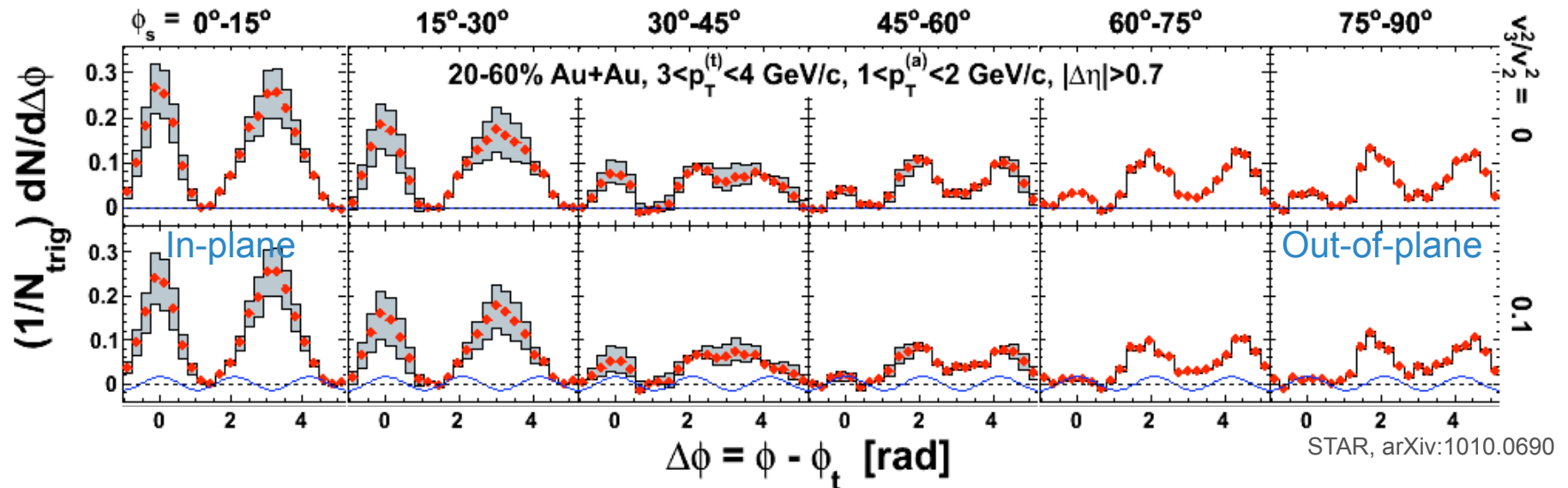
Trigger $p_T > 4-6$ GeV and associate hadron $p_T > 1.5$ GeV (Trigger is highest p_T particle in the event)

Interesting structure is also seen in **raw** correlations for non-pion triggers (mostly protons) at $\Delta\eta > 0.7$

We see effects consistent with expectations, we'll investigate further by looking at various measurements related to v_n

Non-flow or Flow

v_2 subtracted di-hadron correlations: v_2 estimated using $\Psi_{EP}(2.8 < |\eta| < 3.8)$



Subtracting v_2 measured relative to the event-plane at large η leads to residual structure: **adding v_3 doesn't account for residual**

Unless there's a $\Delta\eta$ -dependence to $\langle \Psi_{EP,1} \cdot \Psi_{EP,2} \rangle$, these structures are non-flow

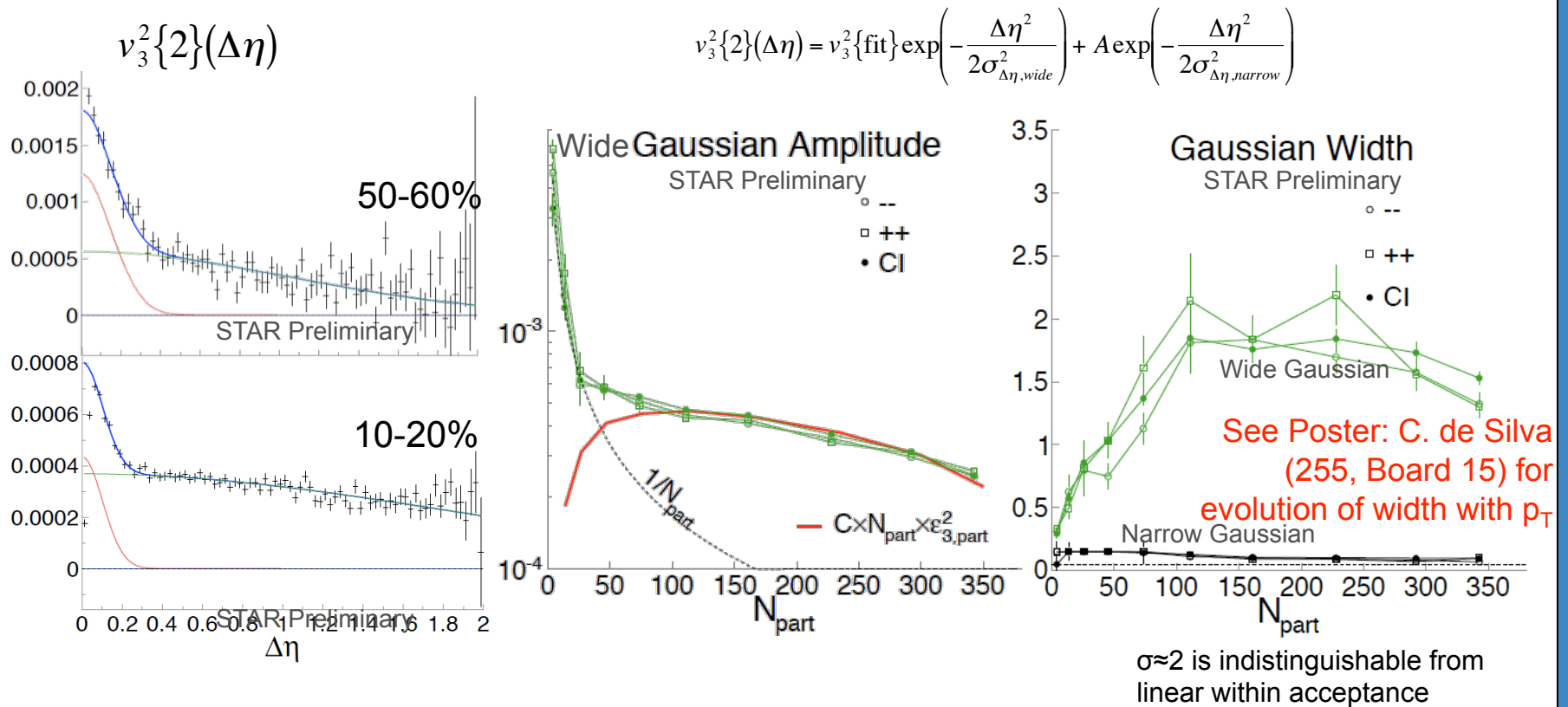
Dusling, Gelis, Lappi & Venugopalan, Nucl. Phys. A 836, 159 (2010); Petersen, Greiner, Bhattacharya & Bass, arXiv:1105.0340

M. Luzum, Phys.Rev.C83:044911,2011

If $\langle \Psi_{EP}(\eta_1) \cdot \Psi_{EP}(\eta_1 + \Delta\eta) \rangle$ depends on $\Delta\eta$ then v_2 measured with a forward reaction plane underestimates the v_2 for dihadrons at smaller $\Delta\eta$.

Let's look at the $\Delta\eta$ dependence of v_3 from a Fourier Trans. of 2 particle correlations

$v_3^2\{2\}$ vs $\Delta\eta$ and Non-flow



Initial state density correlations may drop with Δy : interesting physics $\sigma_{\Delta y} \sim 1/\alpha_s$?

Dusling, Gelis, Lappi & Venugopalan, Nucl. Phys. A 836, 159 (2010)

Petersen, Greiner, Bhattacharya & Bass, arXiv:1105.0340

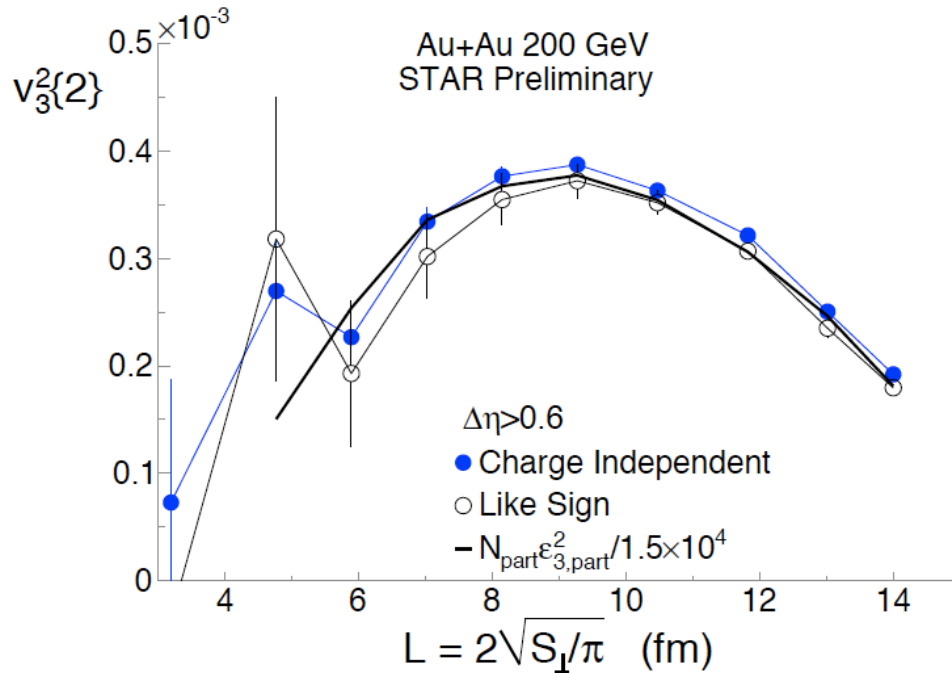
Fit with a wide and a narrow peak. Wide peak amplitude first drops with $1/N$ but then deviates from trend near $N_{\text{part}}=50$. Above that it follows an $N_{\text{part}} \epsilon_{3,\text{part}}^2$ trend

Is the wide Gaussian non-flow as in previous interpretations* and/or $\Delta\eta$ dependence of initial density fluctuations?

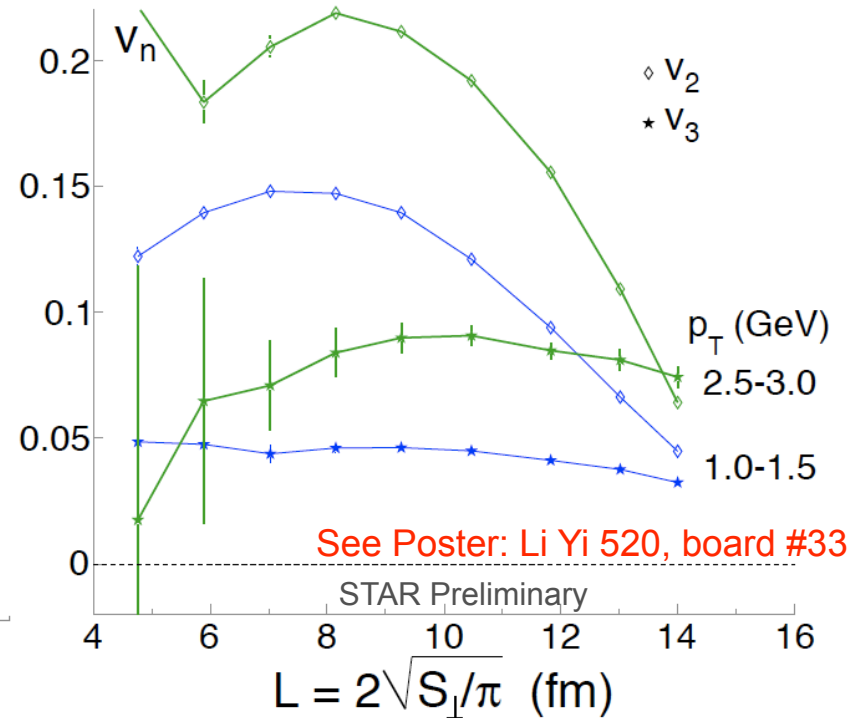
* Trainor, Kettler RefInt.J.Mod.Phys.E17:1219,2008

v_3^2 at Large $\Delta\eta$

$\langle \cos 3(\varphi_1 - \varphi_2) \rangle$ for $|\eta_1 - \eta_2| > 0.6$



$\eta_1 > 0.5$ & $\eta_2 < -0.5$



Centrality variable L estimates the transverse size of the system

v_3^2 for $\Delta\eta > 0.6$ rises then falls with centrality as the overlap shape becomes symmetric. Similar to v_2

Almond shape of the overlap area appears to couple to $n=3$

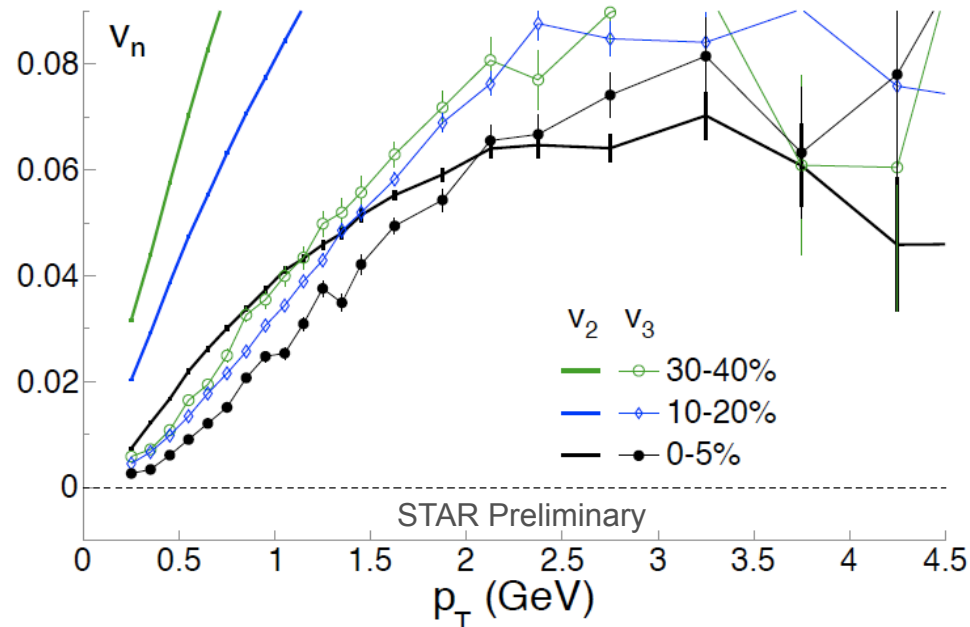
See Poster: J. Thomas
(576, Board #43)

D. Teaney, L. Yan, arXiv:1010.1876 [nucl-th]
P. S., A. Mocsy, B. Bolliet, Y. Pandit, arXiv:1102.1403

v_3 and $(v_3/v_2)^2$ vs centrality and p_T

$v_3\{2\}$ using separate η ranges: $\eta_1 < -0.5$ and $\eta_2 > 0.5$

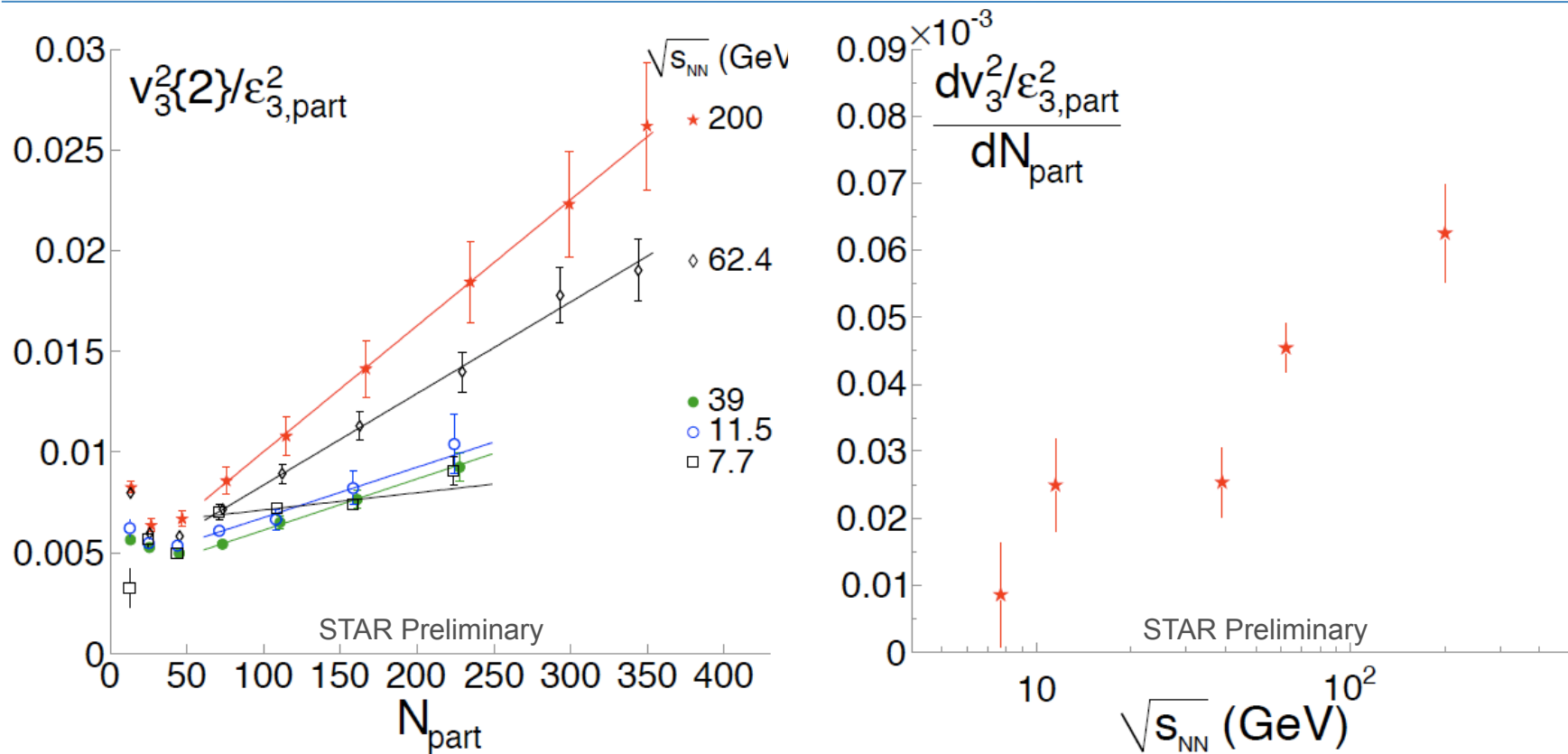
See Poster: Li Yi 520, board #33



For central collisions at intermediate p_T , $v_3\{2\} \geq v_2\{2\}$: what non-flow source would give such a behavior?

Weak $v_3\{2\}$ centrality dependence & $v_3 \geq v_2$ in central were predicted by models based on initial state density inhomogeneity \Leftrightarrow leading explanation

$v_3^2/\epsilon_{3,\text{part}}^2$ vs Beam Energy



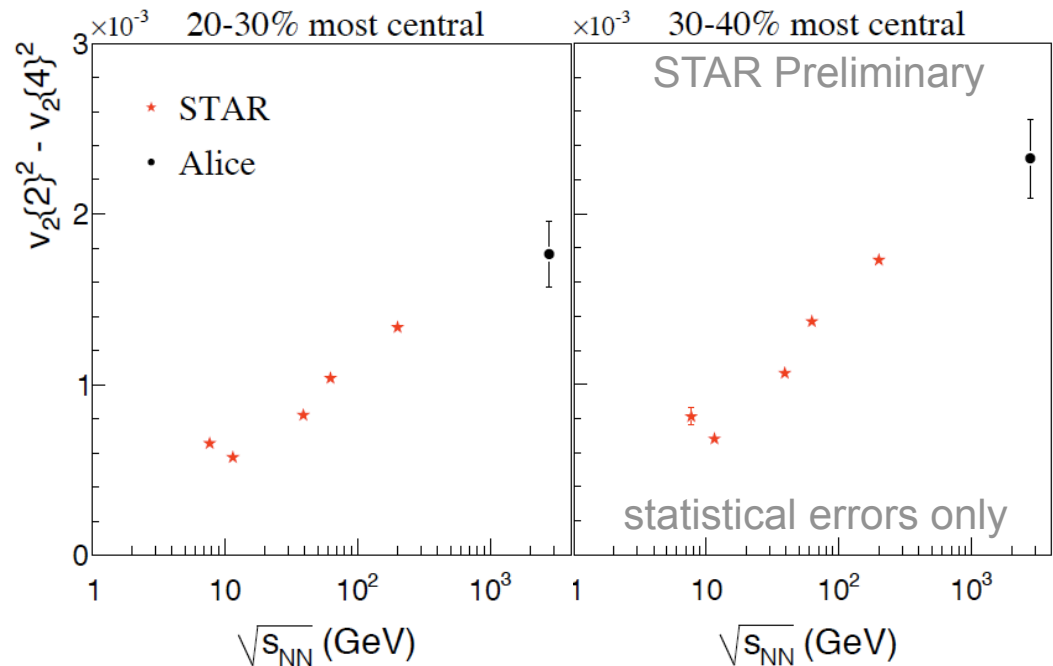
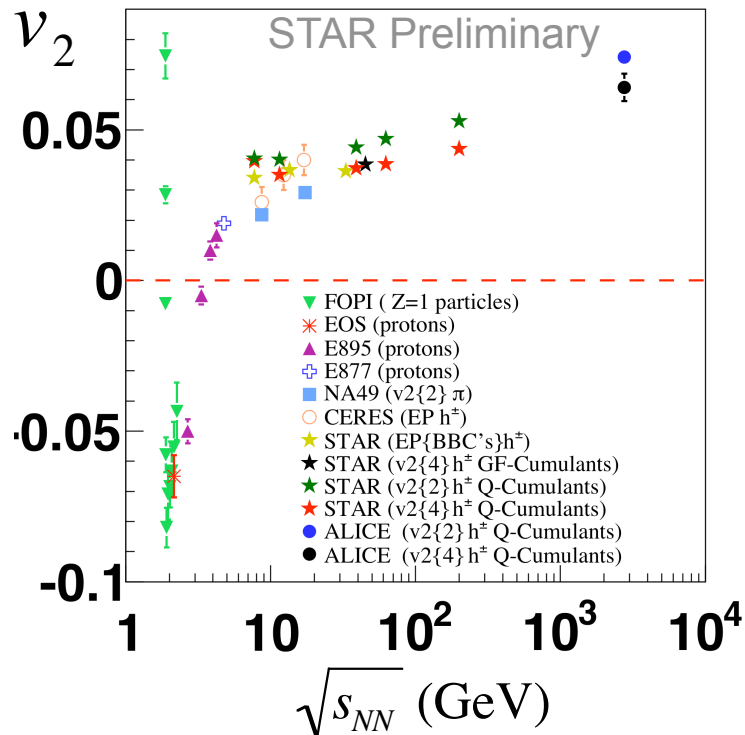
Analysis based on Q-Cumulants for all charges and $-1 < \eta < 1$

$v_3^2/\epsilon_{3,\text{part}}^2$ follows a simple trend with N_{part} : consistent with fits to $v_3^2\{2\}$ vs $\Delta\eta$

Slope of $v_3^2/\epsilon_{3,\text{part}}^2$ is increasing with beam energy: what about the difference between $v_2^2\{2\} - v_2^2\{4\}$

$v_2\{2\}^2$, $v_2\{4\}^2$ and $v_2\{2\}^2 - v_2\{4\}^2$ vs Energy

See Posters: Michael Mitrovski (291, Board #19)
and Shusu Shi (281, Board #16)



$v_2^2\{2\} - v_2^2\{4\} \approx \delta + 2\sigma_v^2$ also shows an intriguing energy dependence: rise of jets or increase in conversion of initial anisotropy into momentum space?

Possible sensitivity to EOS needs to be further investigated

Data at 5, 19.6 (taken) and 27 GeV are needed

Conclusions

We presented the 2 & 4 particle cumulants for v_n up to $n=6$: results are consistent with $v_n \propto \epsilon_{\text{part},n}$ and/or non-flow

Indications of higher harmonic flow seen in RAW dihadron correlations (consistent with initial density fluctuation models)

We examined the $\Delta\eta$ dependence of $v_3\{2\}$ and decomposed it into a narrow and wide Gaussian: the centrality evolution of the amplitude of the wide Gaussian follows $N_{\text{part}}\epsilon_{\text{part},n}^2$

In central collisions, $v_3\{2\}$ at intermediate p_T becomes larger than $v_2\{2\}$ also consistent with models of fluctuating initial conditions

Data appear to favor $v_n^2 \propto \epsilon_{\text{part},n}^2$ and non-negligible higher harmonics; where v_n^2 drops with n as a Gaussian. Other non-flow interpretations are also being pursued