

Kaon Femtoscopy in $\sqrt{s_{NN}}=200$ GeV Au+Au Collisions at STAR

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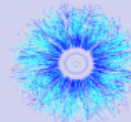


Nuclear Physics Institute
Czech Academy of Sciences

for the



Femtoscopy

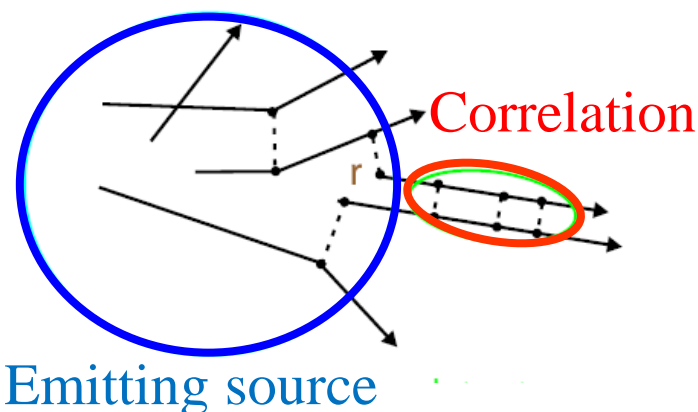


- **Boson emitting source:**

- Symmetric two-boson wave function

$$N_1(k_1) = \int S(x_1, k_1) |\Psi_1|^2 dx_1$$

$$N_2(k_1, k_2) = \int S(x_1, k_1) S(x_2, k_2) |\Psi_{1,2}|^2 dx_1 dx_2$$



Bose-Einstein Correlation / Hanbury-Brown-Twiss effect

Info about shape and evolution of the particle emitting source

- **Correlation function:**

$$C_2(k_1, k_2) = \frac{N_2(k_1, k_2)}{N_1(k_1)N_1(k_2)} \simeq 1 + \left| \frac{\tilde{S}(q, K)}{\tilde{S}(0, K)} \right|^2 \quad \tilde{S}(q, K) = \int dx S(x, k) e^{iqx}$$

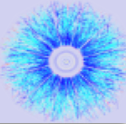
$$q = k_1 - k_2, K = 0.5(k_1 + k_2)$$

- **Final state interactions**

- Compensating the Coulomb force $C_0(q) = C_{\text{raw}}(q) K_{\text{coulomb}}^{-1}$
 - Strong FSI ...

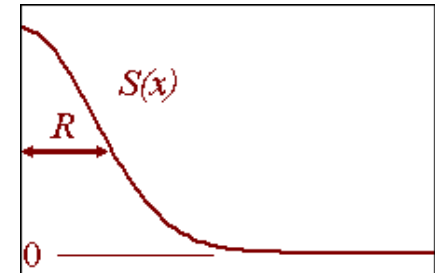
- **Solving for the source is difficult → assumptions**

Source approximation w/ Gaussian



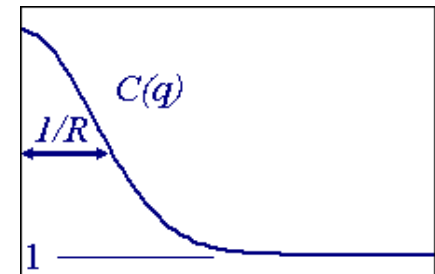
- If the source is approximated with Gaussian:

$$S(x) \sim \exp \left(-\frac{r_x^2}{2R_x^2} - \frac{r_y^2}{2R_y^2} - \frac{r_z^2}{2R_z^2} \right)$$



- Then the correlation function is also Gaussian:

$$C(q) - 1 \sim \exp \left(-q_x^2 R_x^2 - q_y^2 R_y^2 - q_z^2 R_z^2 \right)$$



- These radii are the so-called **HBT radii**
- Often specified in the LCMS system (not invariant)
 - **Out**: direction of the mean transverse momentum of the pair
 - **Side**: orthogonal to out
 - **Long**: beam direction

$$C(q) = 1 + \lambda \exp \left(-q_o^2 R_o^2 - q_s^2 R_s^2 - q_l^2 R_l^2 \right)$$

- Do not necessarily reflect the geometrical size

Source imaging



Physics in shape: dynamics, resonance decays, rescattering...

- Koonin-Pratt equation (1D)

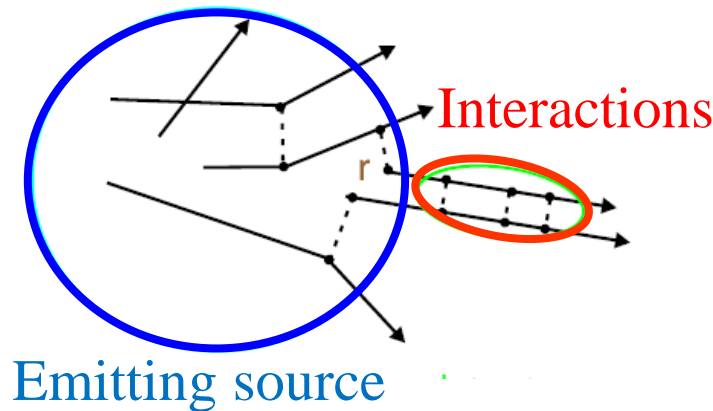
$$C(q) - 1 = 4\pi \int dr r^2 K(q, r) S(r)$$

- Imaging: Obtain $S(\mathbf{r})$ directly

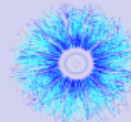
- No assumptions for the shape of source
- Kernel includes **all** interactions (QM, FSI)

- Numerical inversion of the equation

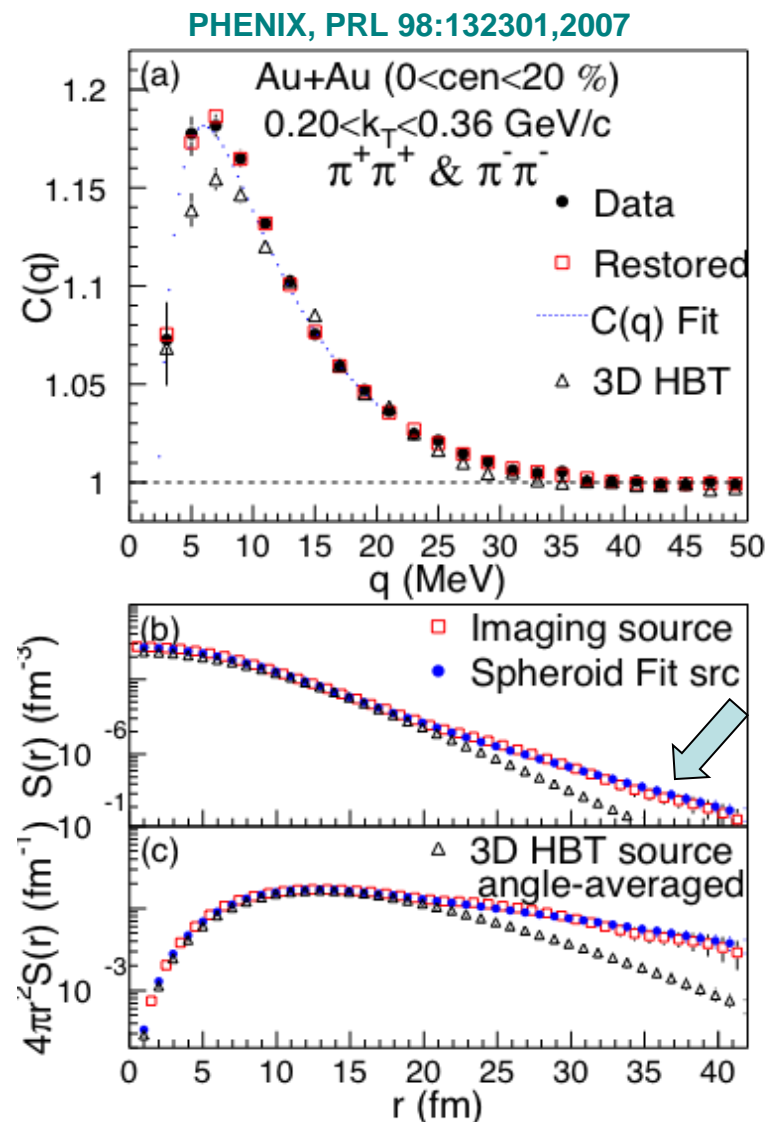
- No analytical solution, hence some limitations and approximations (integral cutoff, finite resolution ...)
- Assumptions (e.g. weak dependence in single particle sources)
- Needs statistics, stability is a question



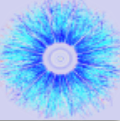
Why Kaons?



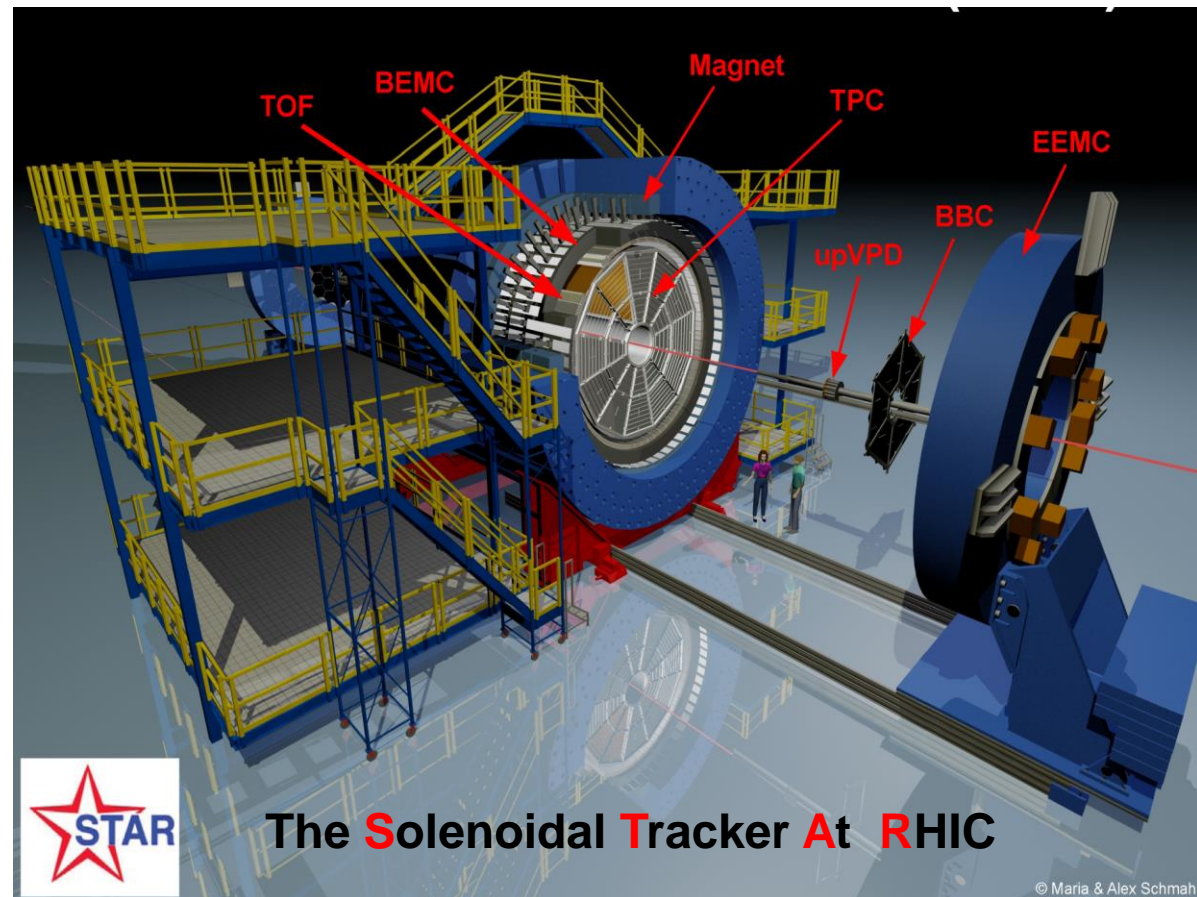
- Pion source shows a **heavy, non-Gaussian tail**
- Interpretation is problematic
Tail attributed to decays of long-lived resonances and/or non-zero emission duration
- Kaons: cleaner probe
less contribution from resonances



The STAR Experiment

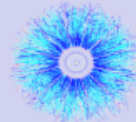


- **T**ime **P**rojection **C**hamber
 - ID via energy loss (dE/dx)
 - Momentum (p)
- Full azimuth coverage
- Uniform acceptance for different energies and particles



The **S**olenoidal **T**racker At **R**HIC

Kaon femtoscopy analyses



Au+Au @ $\sqrt{s_{NN}}=200$ GeV

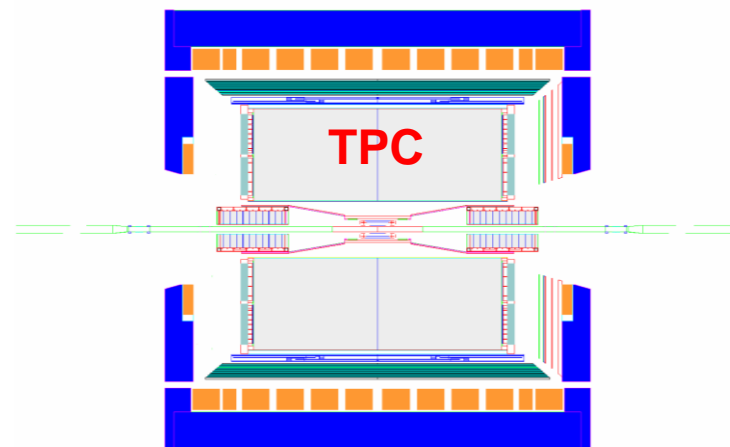
Mid-rapidity $|y|<0.5$

1. Source shape: 20% most central

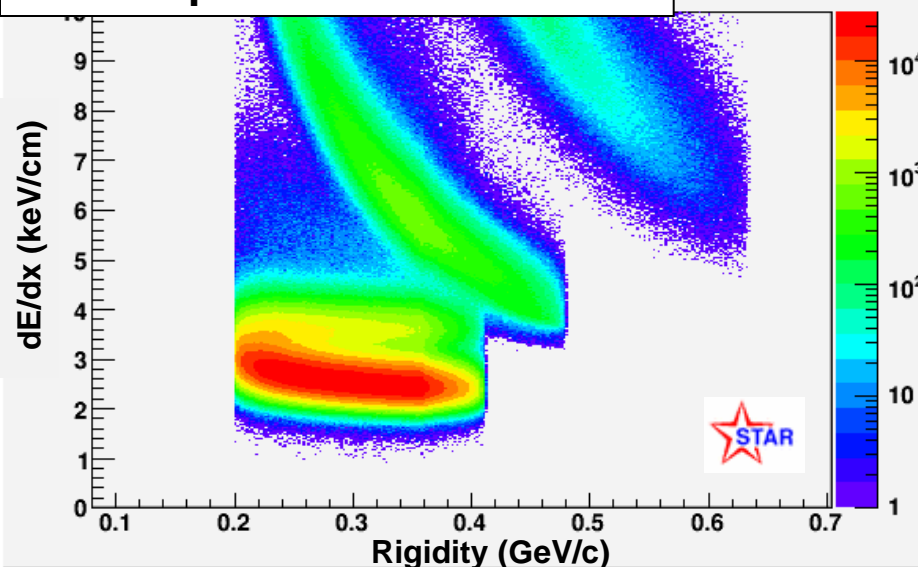
Run 4: 4.6 Mevts, Run 7: 16 Mevts

2. m_T -dependence: 30% most central

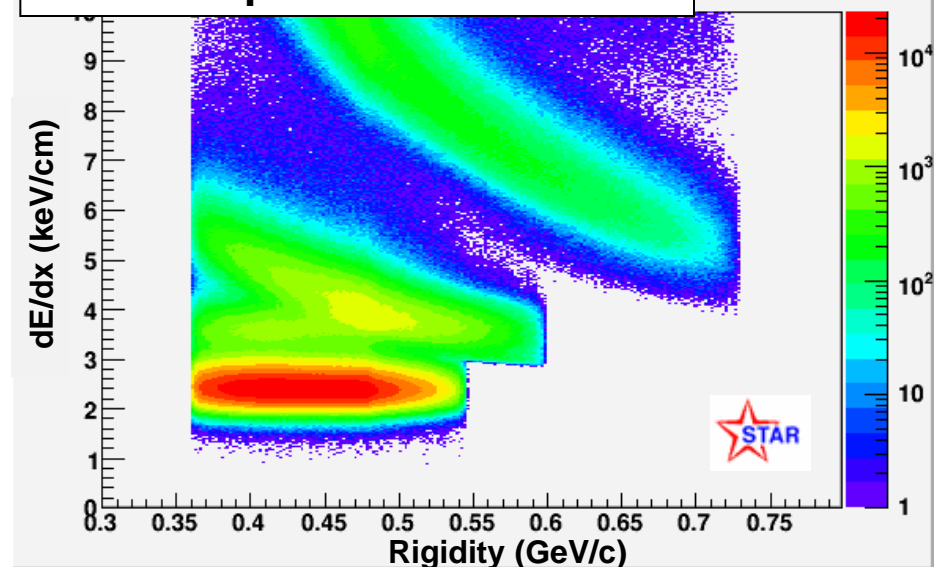
Run 4: 6.6 Mevts



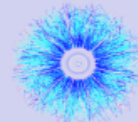
$0.2 < k_T < 0.36$ GeV/c



$0.36 < k_T < 0.48$ GeV/c



PID cut applied



1. Source shape analysis

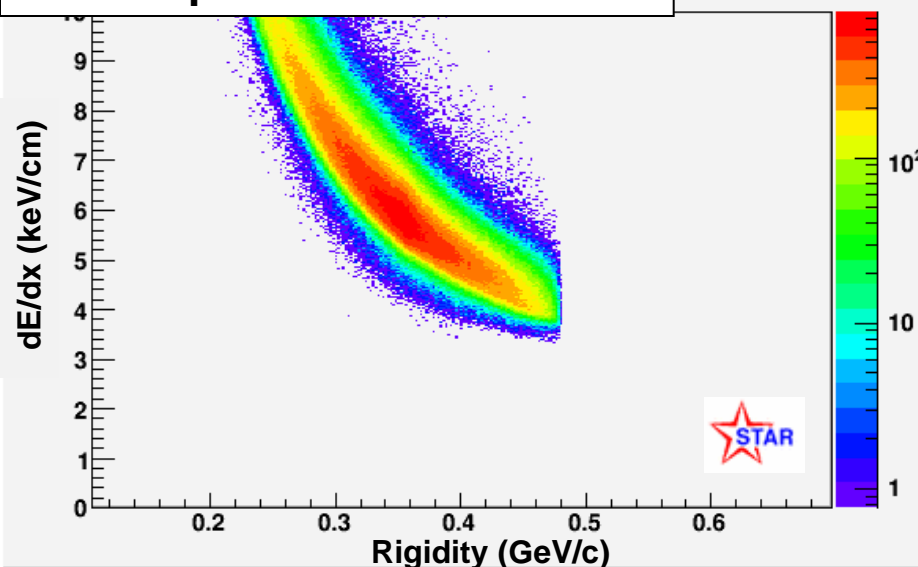
- dE/dx : $n\sigma(\text{Kaon}) < 2.0$ and $n\sigma(\text{Pion}) > 3.0$ and $n\sigma(\text{electron}) > 2.0$
 $n\sigma(X)$: deviation of the candidate dE/dx from the normalized distribution of particle type X at a given momentum
- $0.2 < p_T < 0.4 \text{ GeV}/c$

2. m_T -dependent analysis

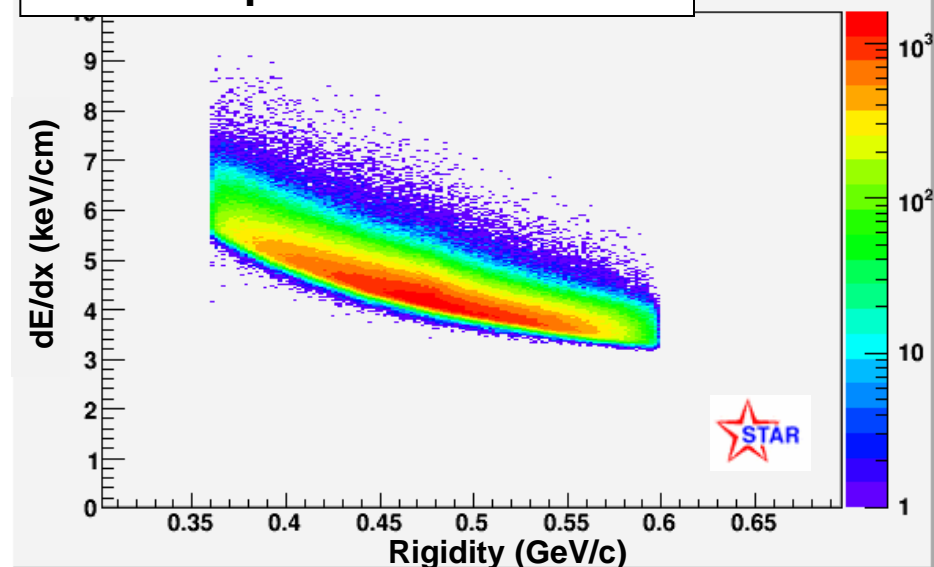
$$-1.5 < n\sigma(\text{Kaon}) < 2.0$$

$$-0.5 < n\sigma(\text{Kaon}) < 2.0$$

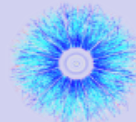
$0.2 < k_T < 0.36 \text{ GeV}/c$



$0.36 < k_T < 0.48 \text{ GeV}/c$



3D source shapes



Expansion of $R(\mathbf{q})$ and $S(\mathbf{r})$ in Cartesian Harmonic basis

Danielewicz and Pratt, Phys.Lett. B618:60, 2005

$$R(\mathbf{q}) = \sum_l \sum_{\alpha_1 \dots \alpha_l} R_{\alpha_1 \dots \alpha_l}^l(q) A_{\alpha_1 \dots \alpha_l}^l(\Omega_q) \quad (1)$$

$$S(\mathbf{r}) = \sum_l \sum_{\alpha_1 \dots \alpha_l} S_{\alpha_1 \dots \alpha_l}^l(r) A_{\alpha_1 \dots \alpha_l}^l(\Omega_q) \quad (2)$$

$\alpha_i = \mathbf{x}, \mathbf{y}$ or \mathbf{z}

$\mathbf{x} =$ out-direction

$\mathbf{y} =$ side-direction

$\mathbf{z} =$ long-direction

3D Koonin-Pratt:

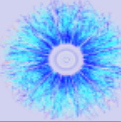
$$R(\mathbf{q}) = C(\mathbf{q}) - 1 = 4\pi \int dr^3 K(\mathbf{q}, \mathbf{r}) S(\mathbf{r}) \quad (3)$$

$$\text{Plug (1) and (2) into (3)} \Rightarrow R_{\alpha_1 \dots \alpha_l}^l(q) = 4\pi \int dr^3 K_l(q, r) S_{\alpha_1 \dots \alpha_l}^l(r) \quad (4)$$

$$\text{Invert (1)} \Rightarrow R_{\alpha_1 \dots \alpha_l}^l(q) = \frac{(2l+1)!!}{l!} \int \frac{d\Omega_q}{4\pi} A_{\alpha_1 \dots \alpha_l}^l(\Omega_q) R(\mathbf{q})$$

$$\text{Invert (2)} \Rightarrow S_{\alpha_1 \dots \alpha_l}^l = \frac{(2l+1)!!}{l!} \int \frac{d\Omega_q}{4\pi} A_{\alpha_1 \dots \alpha_l}^l(\Omega_q) S(\mathbf{q})$$

Shape analysis



- $\ell=0$ moment agrees 1D $C(q)$

Higher moments relatively small

- Trial functional form for $S(r)$:
4-parameter ellipsoid (3D Gauss)

$$S^G(x, y, z) \equiv \frac{\lambda}{(2\sqrt{\pi})^3 r_x r_y r_z} \exp\left[-\left(\frac{x^2}{4r_x^2} + \frac{y^2}{4r_y^2} + \frac{z^2}{4r_z^2}\right)\right]$$

- Fit to $C(q)$: technically a simultaneous fit on 6 independent moments

$$R_{\alpha_1 \dots \alpha_\ell}^\ell, \quad 0 \leq \ell \leq 4$$

- Result: statistically good fit

Run4+Run7

200 GeV Au+Au

Centrality <20%

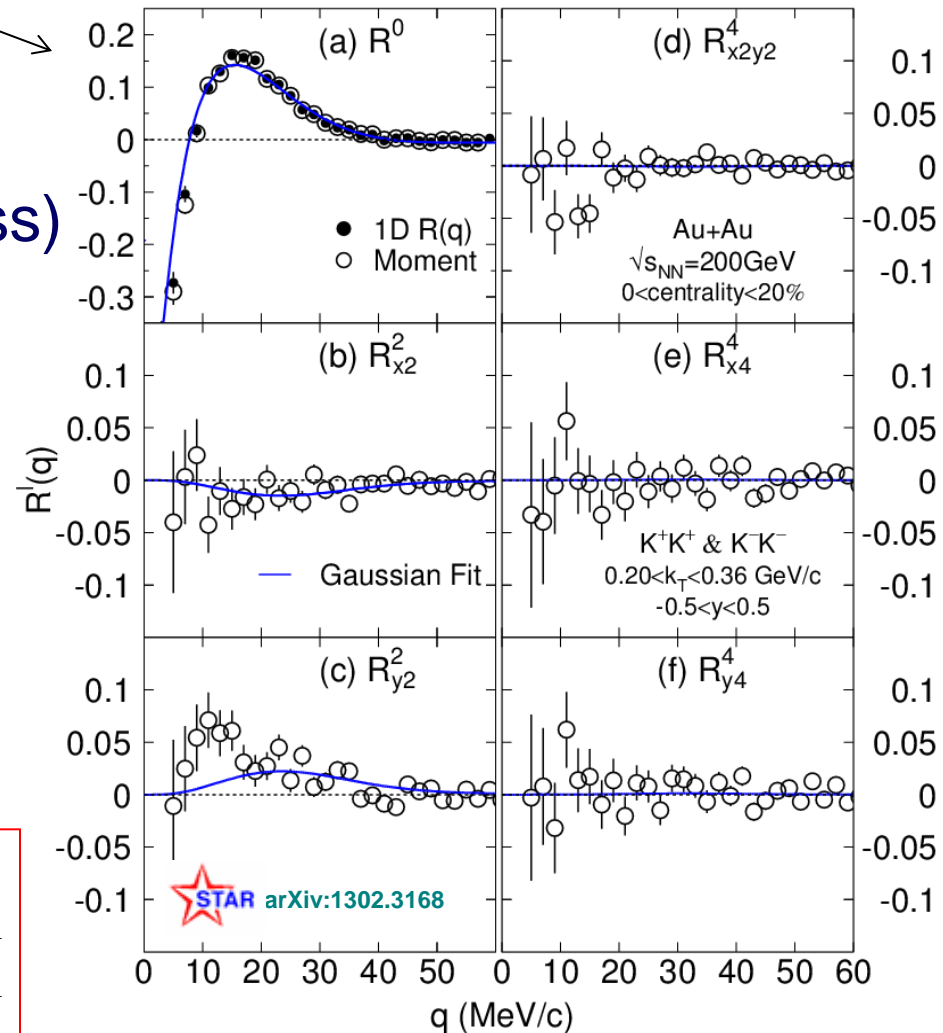
$0.2 < k_T < 0.36$ GeV/c

$$\lambda = 0.48 \pm 0.01$$

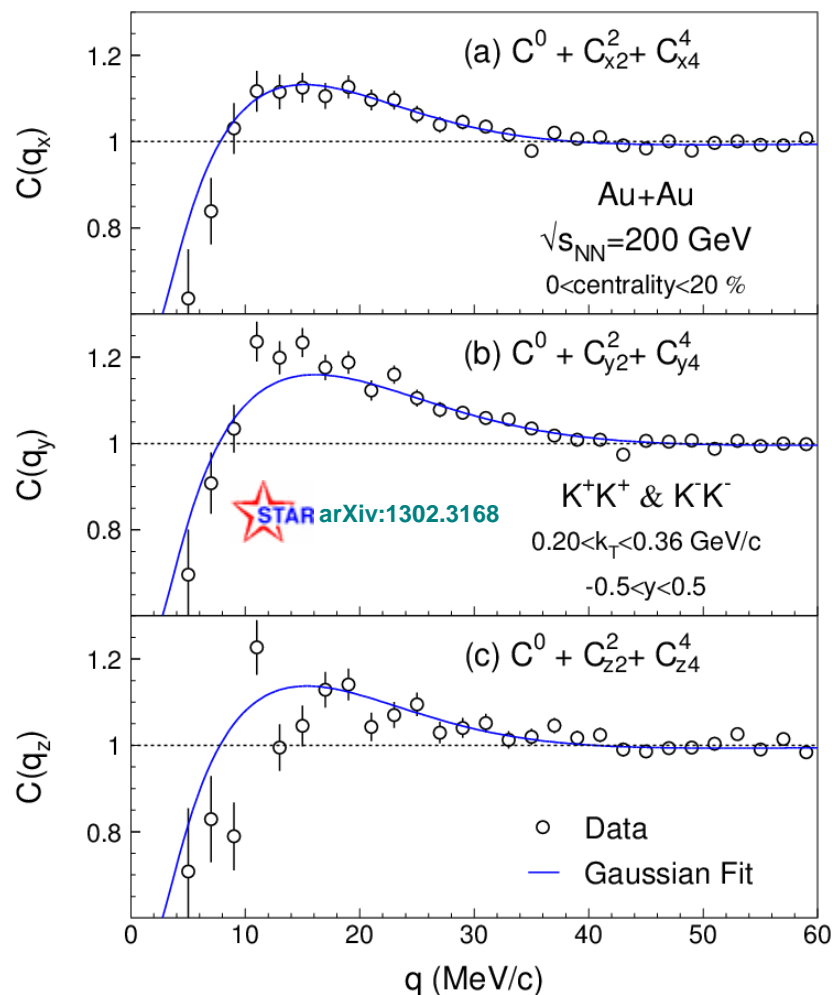
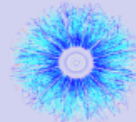
$$r_x = (4.8 \pm 0.1) \text{ fm}$$

$$r_y = (4.3 \pm 0.1) \text{ fm}$$

$$r_z = (4.7 \pm 0.1) \text{ fm}$$



Correlation profiles and source

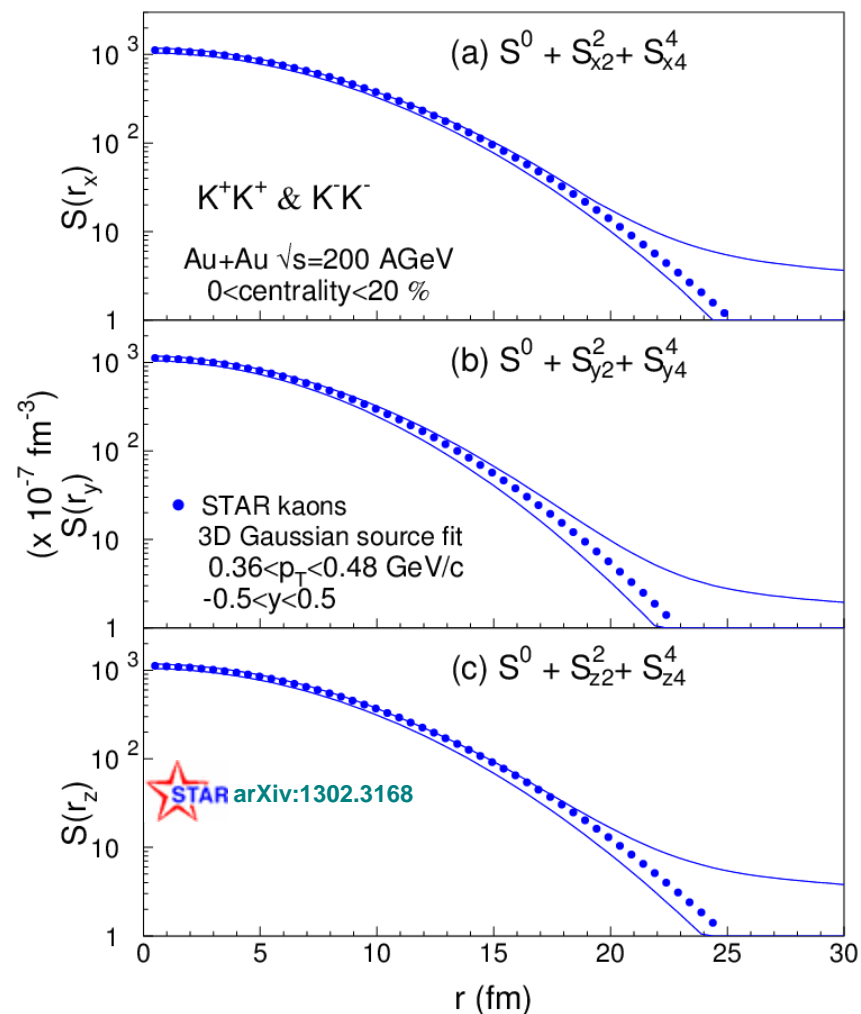


Correlation profiles

$$C(q_x) \equiv C(q_x, 0, 0)$$

$$C(q_y) \equiv C(0, q_y, 0)$$

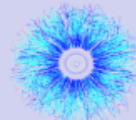
$$C(q_z) \equiv C(0, 0, q_z)$$



Gaussian source fit with error band

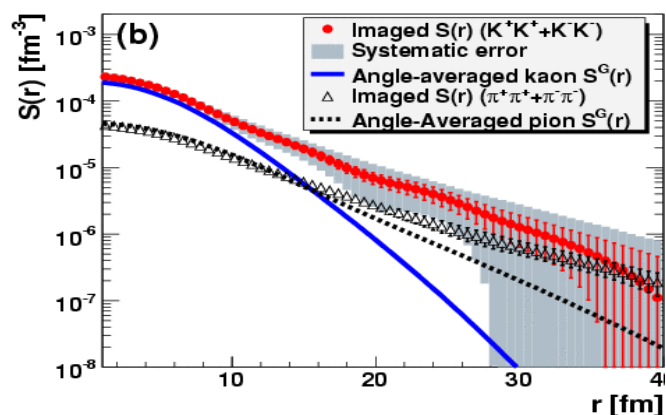
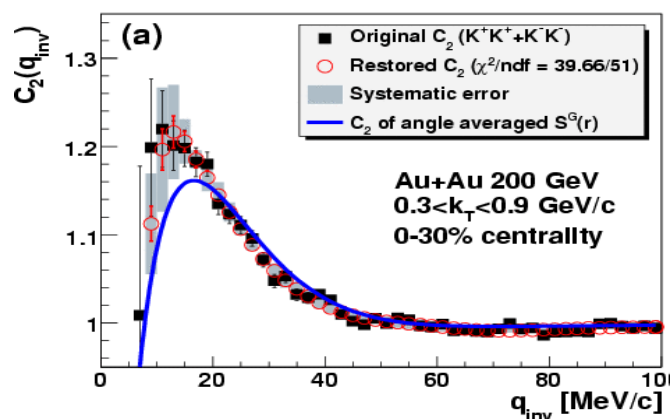
Note: Low statistics shows up as systematic uncertainty on shape assumption

Source: Data comparison

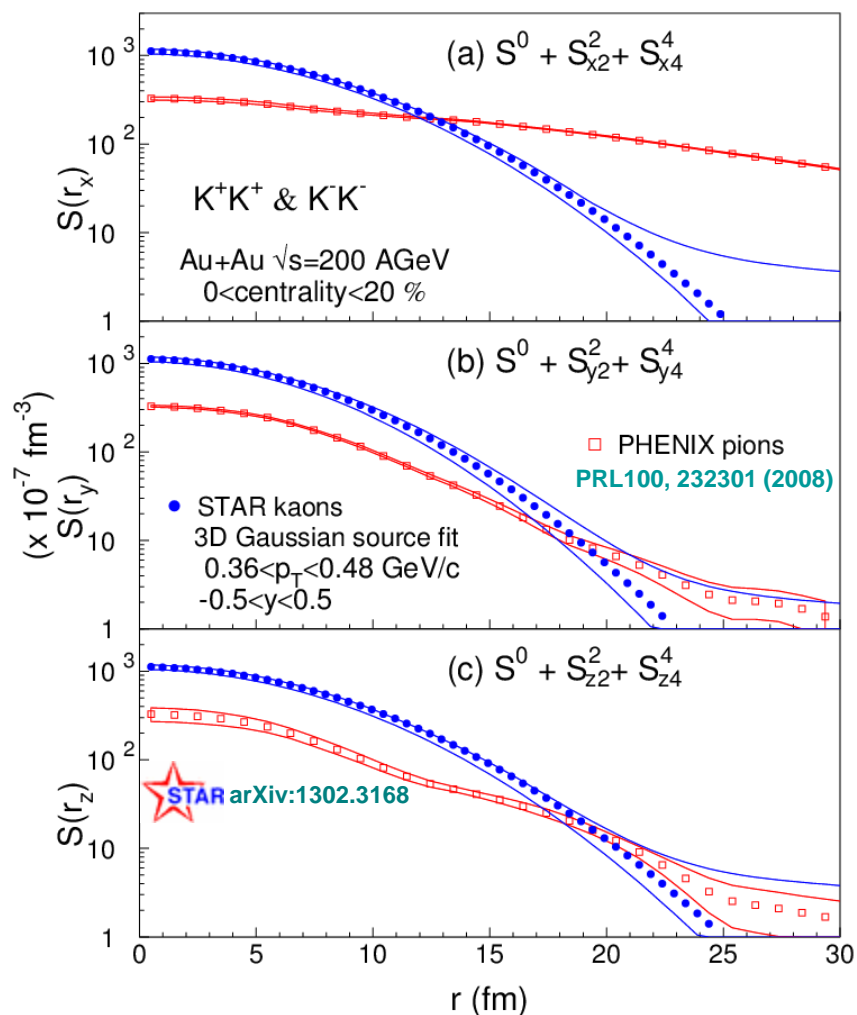


1D PHENIX kaon:

- Observed long tail, possibly due to wide k_T bin ($0.3 < k_T < 0.9$ GeV)



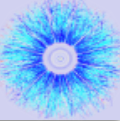
PHENIX, PRL 103, 142301 (2009)



Kaon vs. Pion: different shape

- Long pion tail caused by resonances?
- Sign of different freeze-out dynamics?

Source: Model comparison

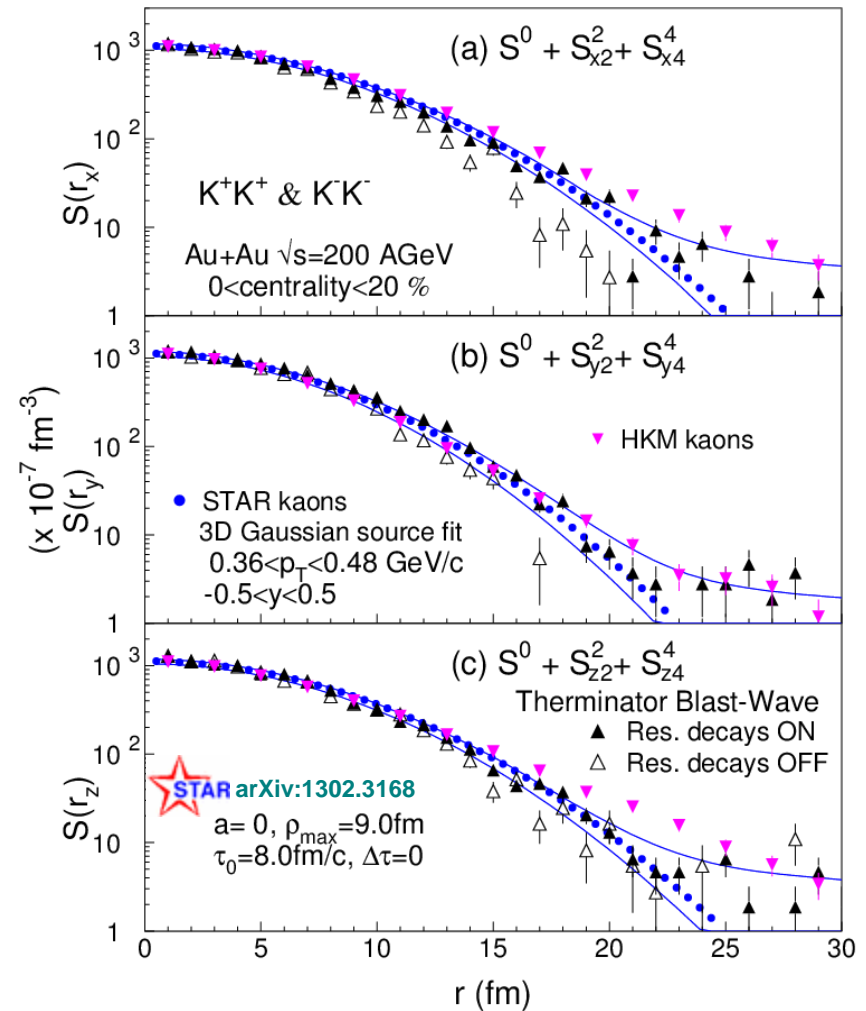


Therminator

- Blast-wave model (STAR tune):
 - Expansion: $v_t(\rho) = (\rho/\rho_{\max}) / (\rho/\rho_{\max} + v_t)$
 - Freeze-out occurs at $\tau = \tau_0 + a\rho$.
 - Finite emission time $\Delta\tau$ in lab frame
- Kaons: Instant freeze-out ($\Delta\tau = 0$, compare to $\Delta\tau \sim 2$ fm/c of pions) at $\tau_0 = 0.8$ fm/c
- Resonances are needed for proper description

Hydrokinetic model

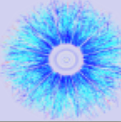
- Hybrid model
 - Glauber initial+Hydro+uRQMD
- Consistent in “side”
- Slightly more tail ($r > 15$ fm) in “out” and “long”



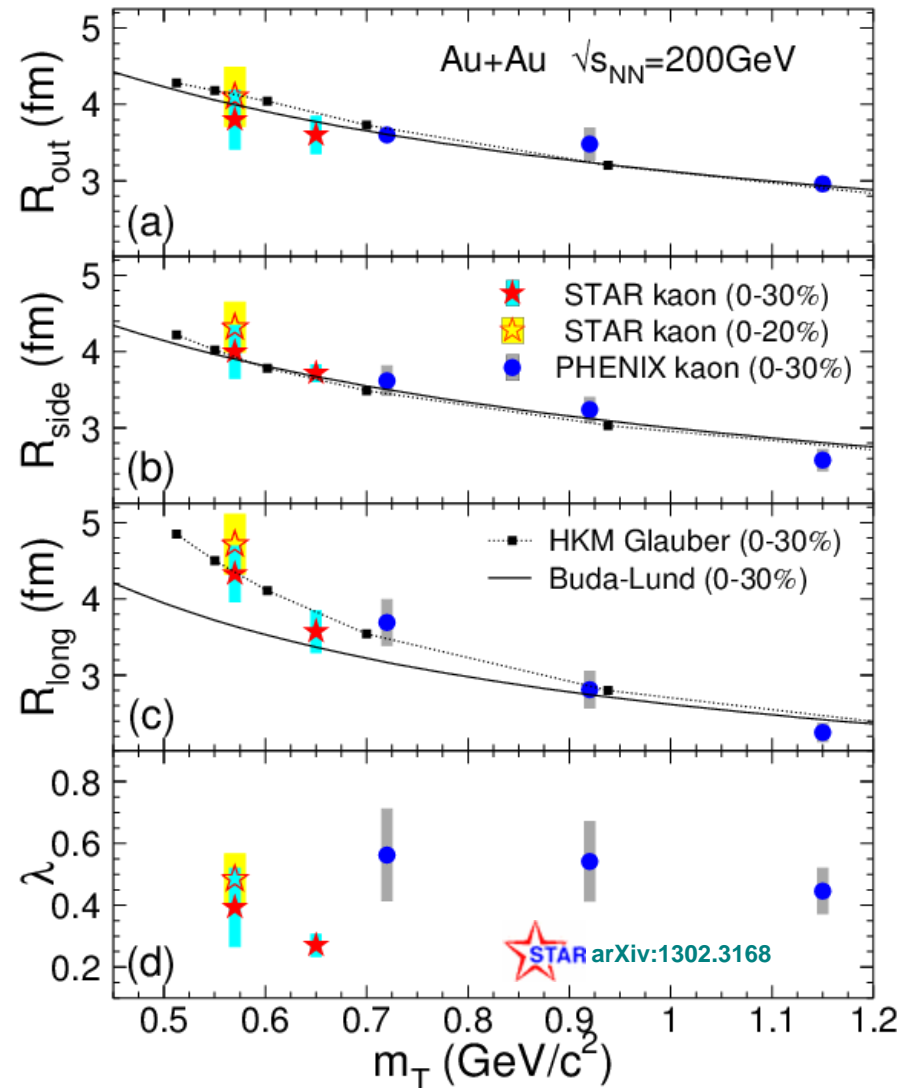
Therminator: Kisiel, Taluc, Broniowski, Florkowski,
 Comput. Phys. Commun. 174 (2006) 669.

HKM: PRC81, 054903 (2010)
 data from Shapoval, Sinyukov, private communication

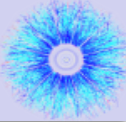
Transverse mass dependence



- Radii: rising trend at low m_T
 - Strongest in “long”
- Buda-Lund model
 - Perfect hydrodynamics, inherent m_T -scaling
 - Works perfectly for pions
 - Deviates from kaons in the “long” direction in the lowest m_T bin
- HKM (Hydro-kinetic model)
 - Describes all trends
 - Some deviation in the “out” direction
 - Note the different centrality definition

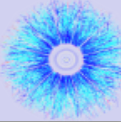


Summary



- First model-independent extraction of kaon 3D source shape presented
- No significant non-Gaussian tail is observed in RHIC $\sqrt{s_{NN}}=200$ GeV central Au+Au data
- Model comparison indicates that kaons and pions may be subject to different dynamics
- The m_T -dependence of the Gaussian radii indicates that m_T -scaling is broken in the “long” direction

Thank You!

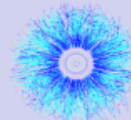


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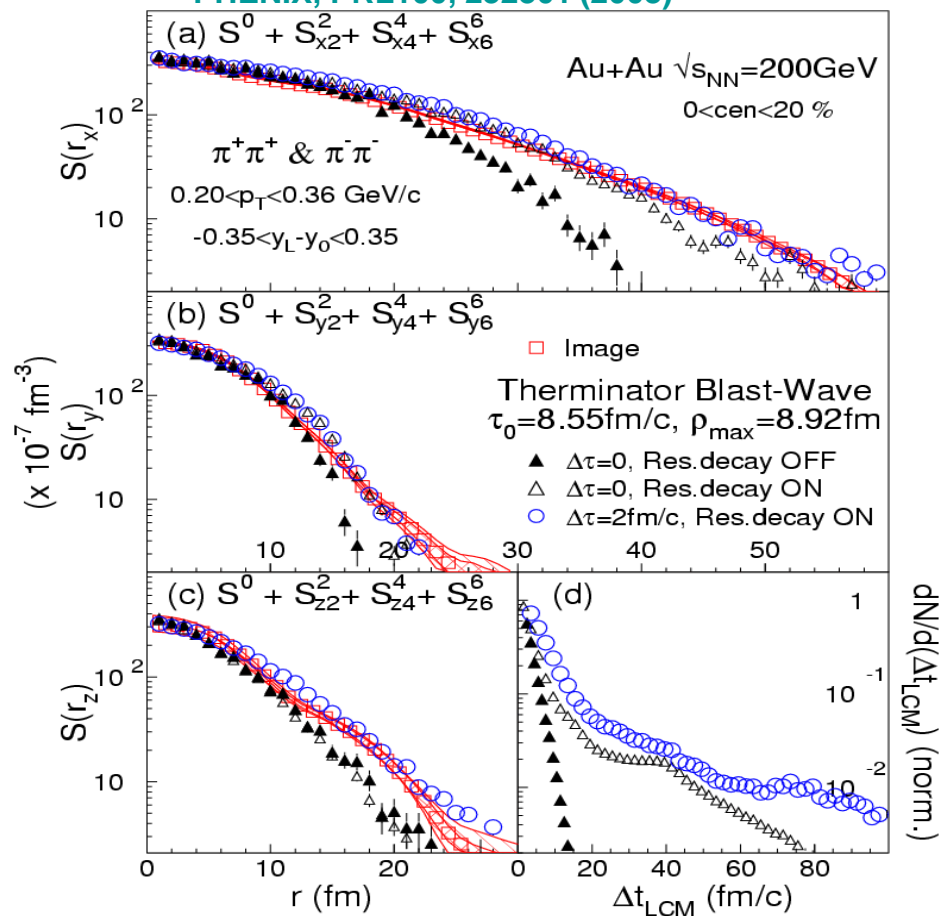
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 University of Zagreb, Zagreb, HR-10002, Croatia

STAR Collaboration

3D pions, PHENIX and STAR



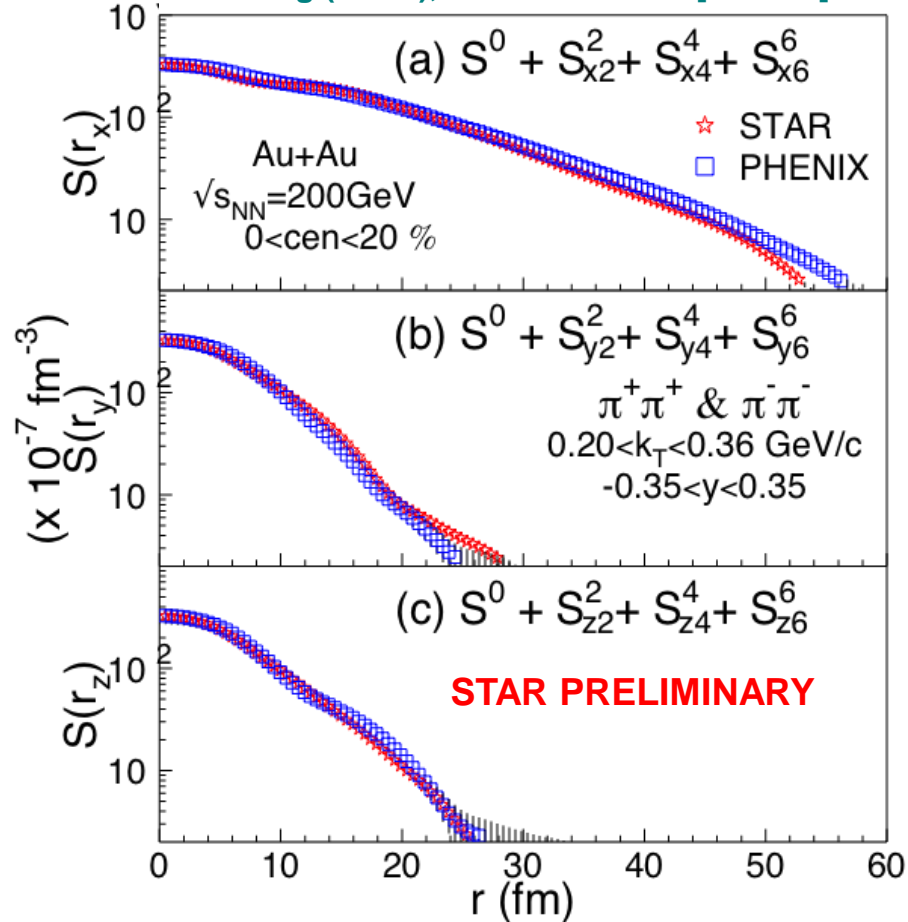
PHENIX, PRL100, 232301 (2008)



Elongated source in “out” direction

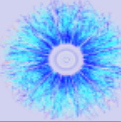
Therminator Blast Wave model suggests non-zero emission duration

P. Chung (STAR), arXiv:1012.5674 [nucl-ex]



Very good agreement of PHENIX and STAR 3D pion source images

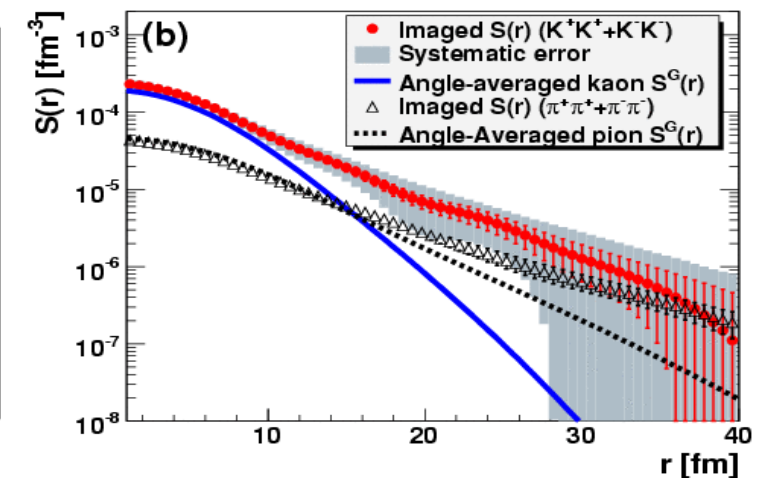
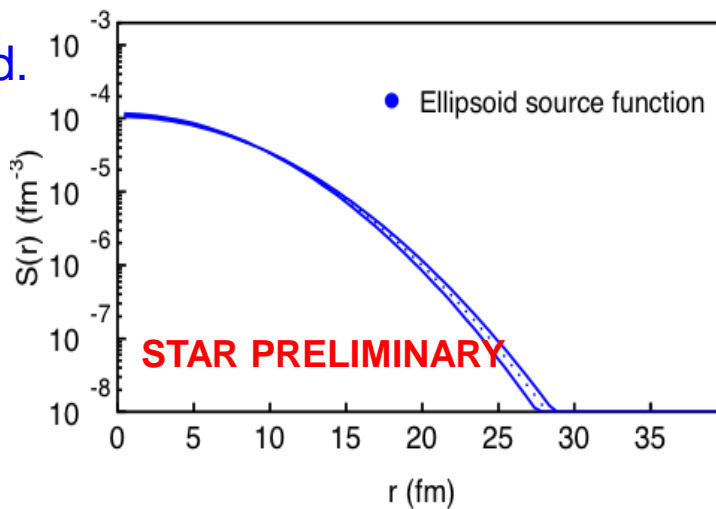
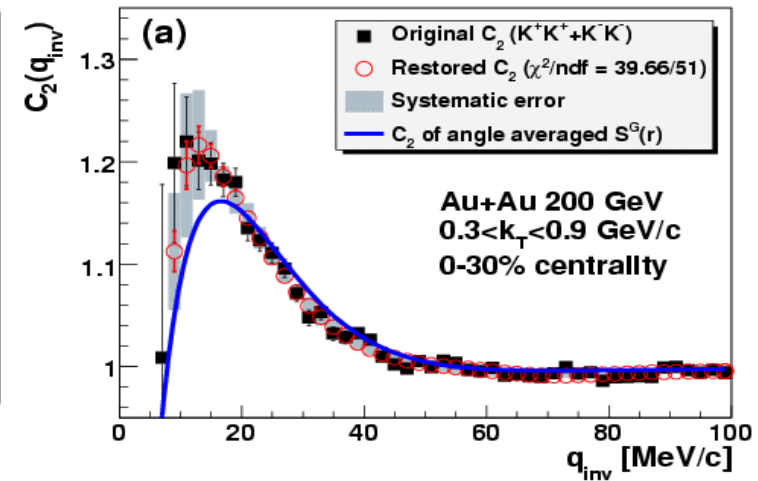
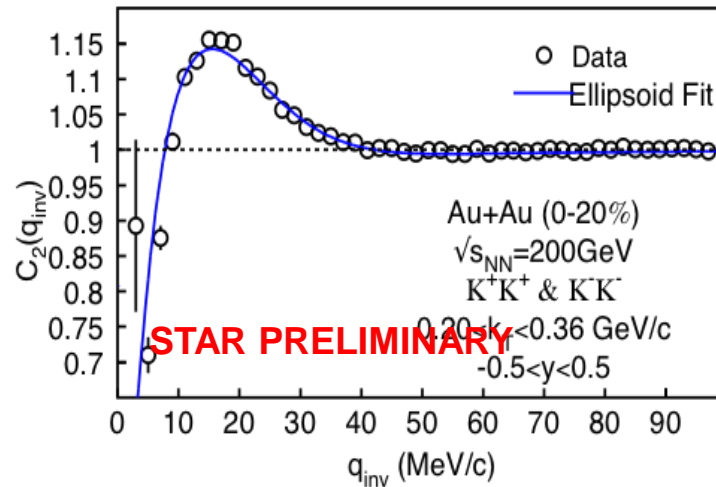
STAR 1D kaons



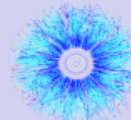
34M+83M=117M
K⁺K⁺ & K⁻K⁻ pairs

STAR data are well described by Gaussian, contrary to PHENIX no non-gaussian tails are observed.

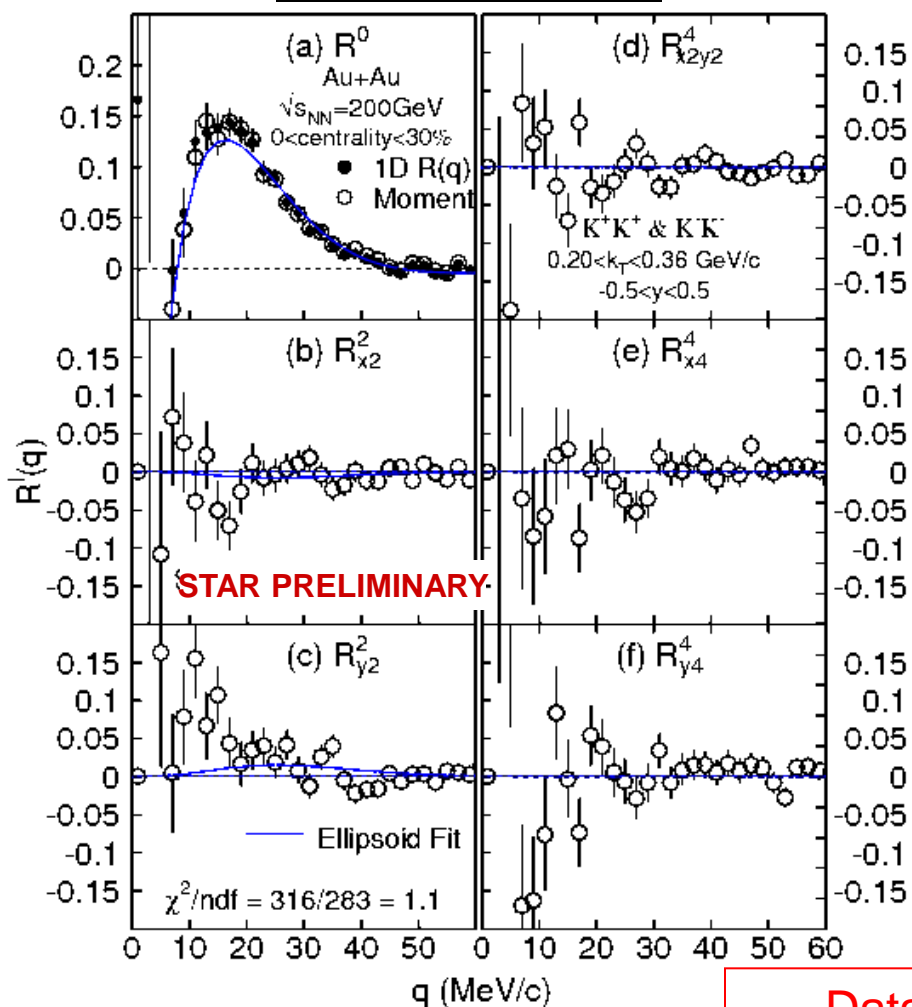
May be due to a different k_T -range:
STAR bin is 4x narrower.



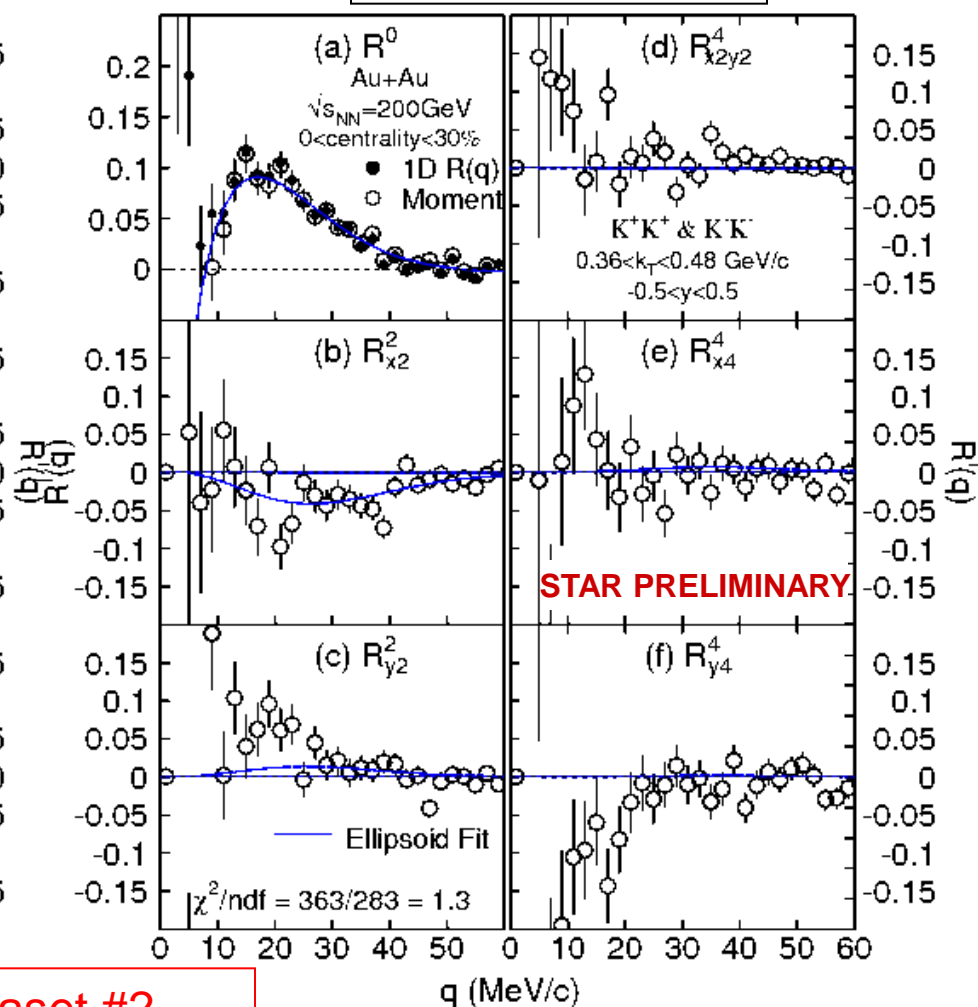
Fit to correlation moments #2



0.2 < k_T < 0.36 GeV/c

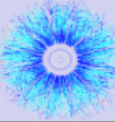


0.36 < k_T < 0.48 GeV/c



Dataset #2
Run4 Cent<30%

Model comparison: thermal BW



Therminator

(A Thermal Heavy Ion Generator)

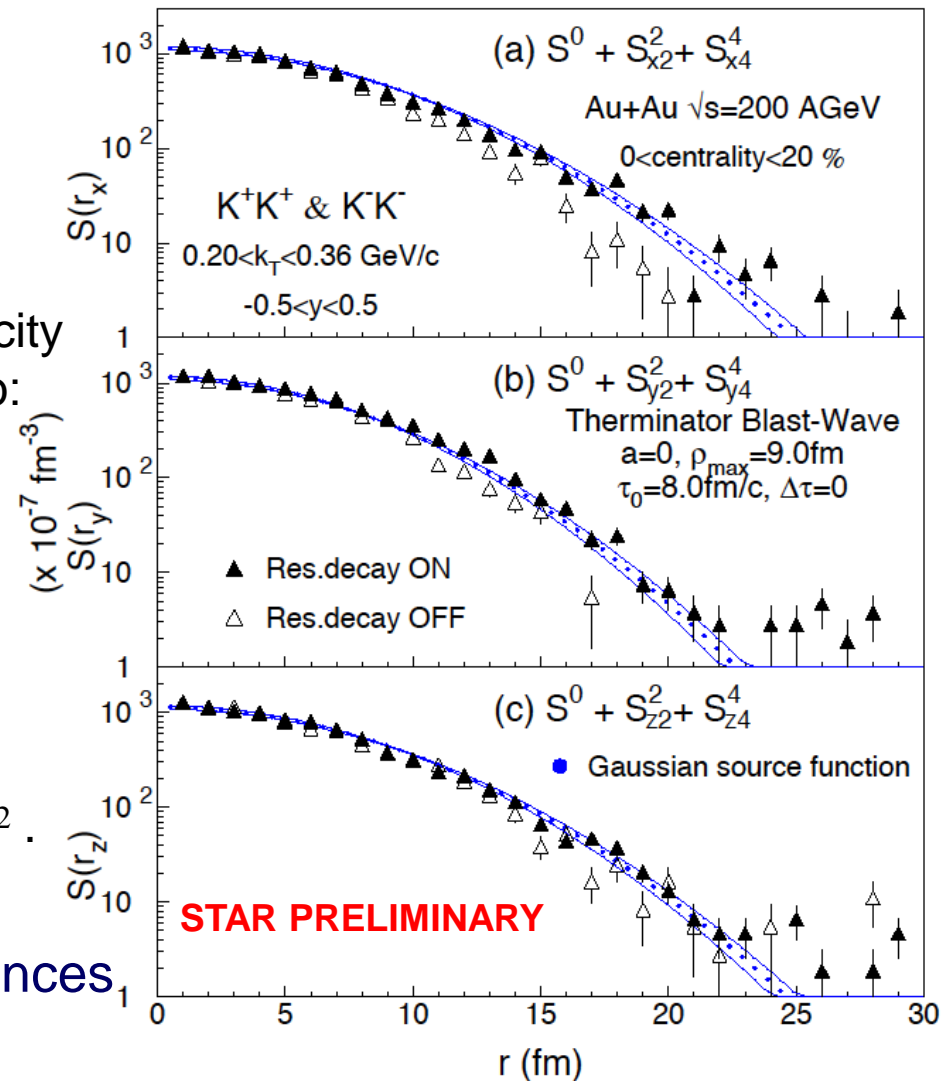
A. Kisiel et al., Phys. Rev. C 73:064902 2006

- Longitudinal boost invariance
- Blast-wave** expansion: transverse velocity profile semi-linear in transverse radius ρ :

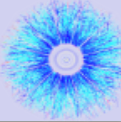
$$v_t(\rho) = (\rho/\rho_{\max}) / (\rho/\rho_{\max} + v_t) \quad ; \quad v_t = 0.445$$
 from BW fits to particle spectra
- Thermal emission at proper time τ , from an infinite cylinder radius ρ_{\max}
- Freeze-out occurs at $\tau = \tau_0 + a\rho$.
- Particles which are emitted at (z, ρ) have LAB emission time $\tau^2 = (\tau_0 + a\rho)^2 + z^2$.
- Finite emission duration $\Delta\tau$

Source consistent with BW and resonances

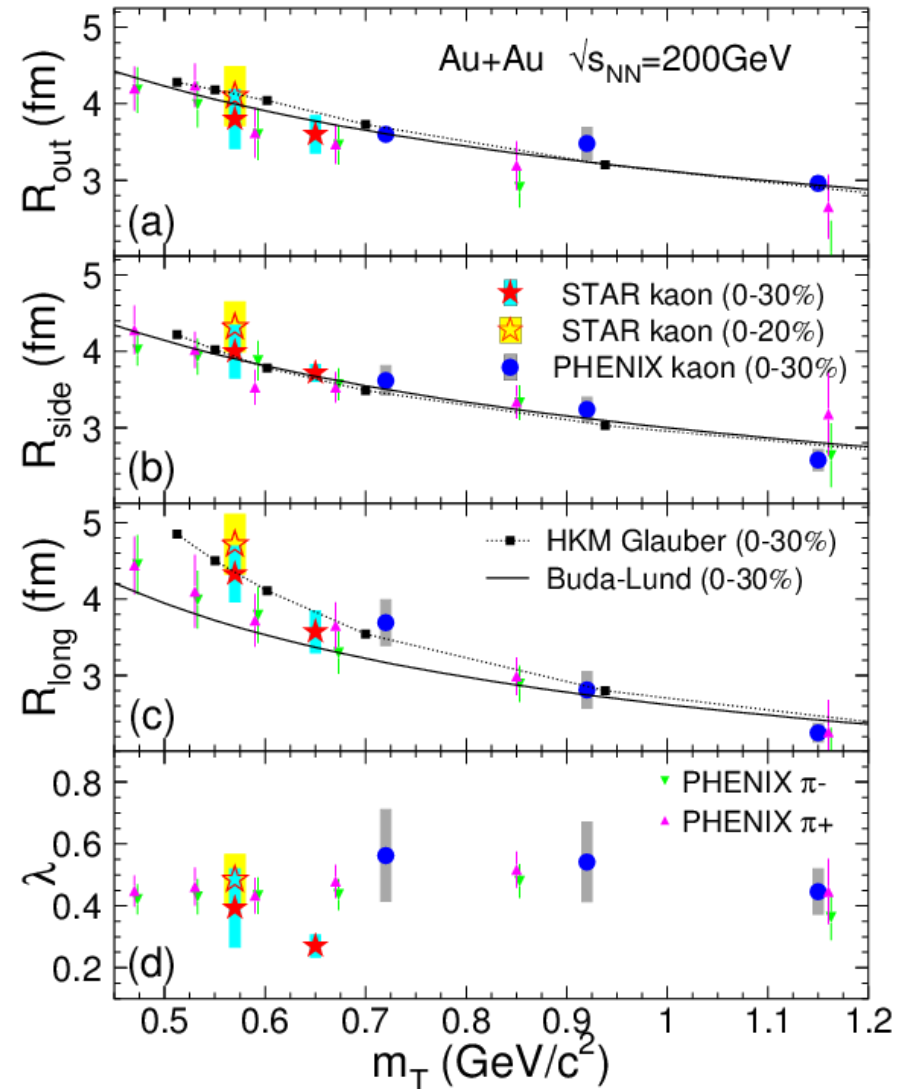
- Instant freeze-out at $\tau_0 = 0.8$ fm/c
- Zero emission duration



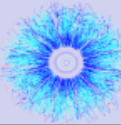
Radii vs. m_T , pion, kaon



- STAR kaons
- PHENIX pions $+,-$
- Buda-Lund
- HKM



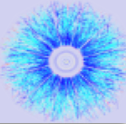
The RHIC facility



- Two independent rings
 - 3,9 km long each
- Collides heavy ions...
 - **Au+Au, Cu+Cu, U+U...**
 - $\sqrt{s_{NN}} = 7,7 - 200 \text{ GeV}$
- ...and protons
 - **p+p** up to $\sqrt{s} = 500 \text{ GeV}$
 - Different polarization patterns
- Asymmetric setups
 - **d+Au, Cu+Au ...**
- 4 experiments
 - All different capabilities
 - PHENIX, STAR (the „large” ones)
 - PHOBOS, BRAHMS (completed)



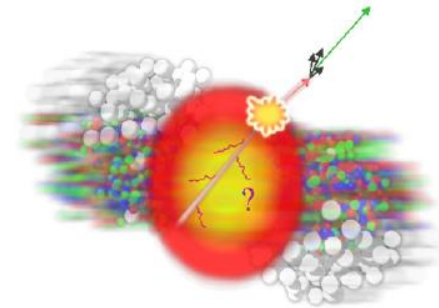
Hot nuclear matter



Nucl. Phys. A 757 (2005) p1 ; p28; p102 ; p184 [white papers]

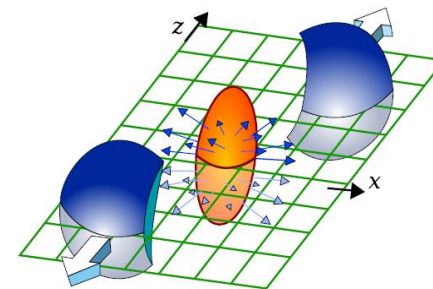
- Extremely dense

- Au+Au: jet suppression
No effect in d+Au
- Strongly interacting, new state of matter
 $\lambda \sim 3$ fm (5 GeV jet)



- Perfect fluid of quarks

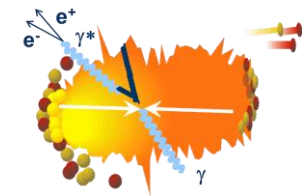
- Contradicts expectations
- Degrees of freedom: quarks
- Viscosity consistent with theoretical limit
 $\eta/s \sim \hbar/4\pi$, $c_s = 0.35c$



- Quark Gluon Plasma (sQGP)

Phys.Rev.Lett. 104, 132301 (2010)

- Thermal radiation, $T_{\text{init}} \sim 4 \times 10^{12}$ K
 $T_{\text{init}} > 300$ MeV $\gg T_{\text{Hagedorn}}$, $\epsilon_{\text{init}} \sim 15$ GeV/fm³, $p_{\text{init}} \geq 1.5$ GeV/fm³



- Evolution of the particle source?

- Dynamics, space-time extent ← correlations

