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**NATIONAL SCIENCE CENTRE  
POLAND**

# Correlations and fluctuations measured by the STAR experiment

**Daniel Wielanek for the STAR Collaboration**

*New Trends in High-Energy and Low-x Physics*

1-5th September 2024

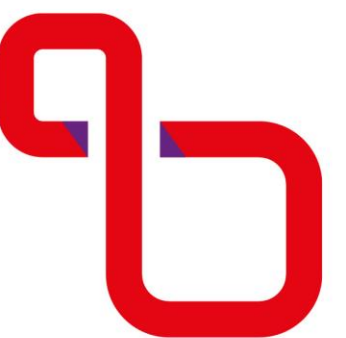
**Warsaw University  
of Technology**

partially funded by DoE



**U.S. DEPARTMENT OF  
ENERGY**

**Office of  
Science**



**RESEARCH  
UNIVERSITY**  
EXCELLENCE INITIATIVE

# Outline

- Motivation
- STAR experiment
- Results
  - Fluctuations & criticality
  - Femtoscopy & interactions
- Summary & plans





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# Motivation

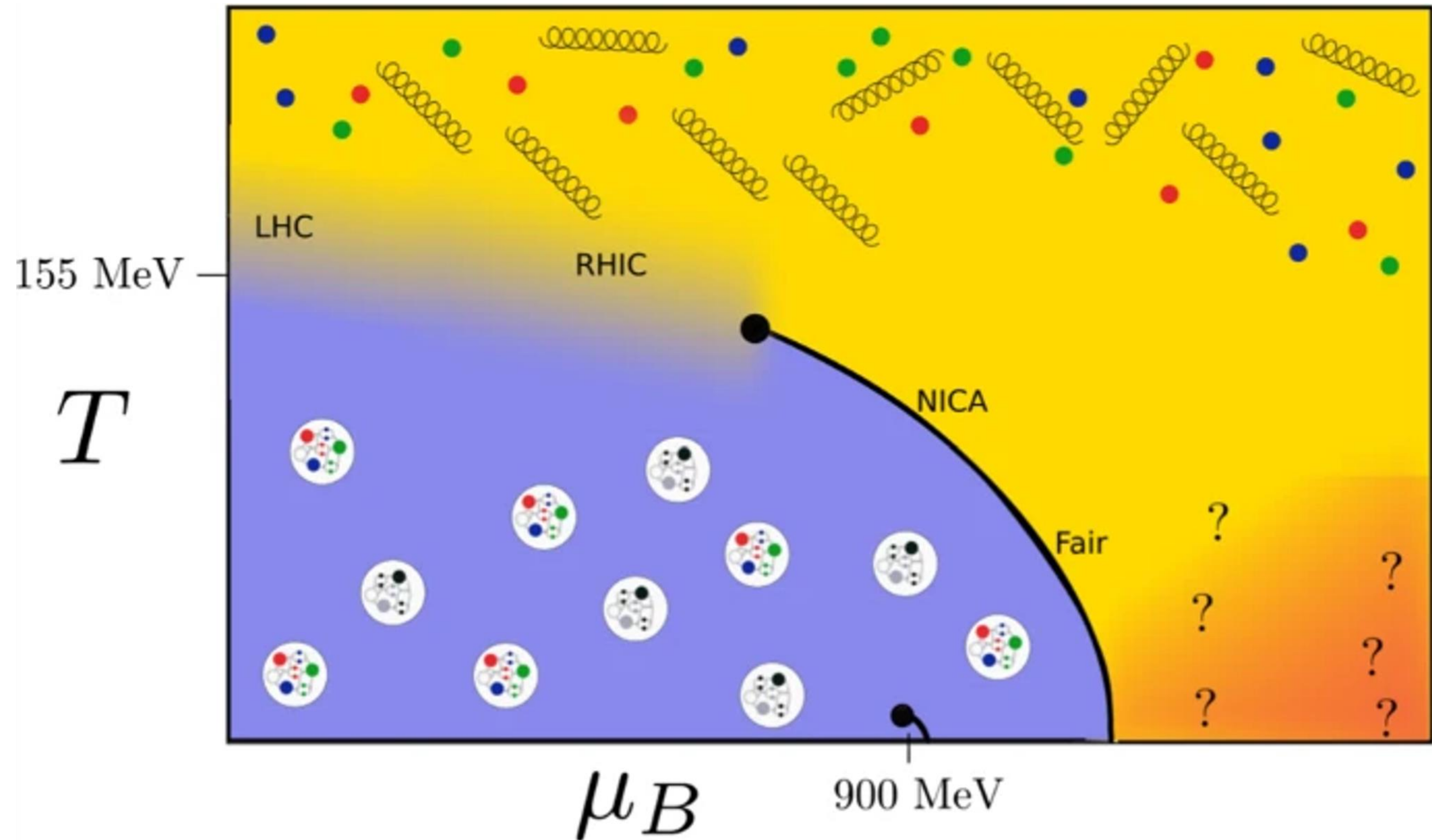
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# Motivation

Probing phase diagram of QCD matter

- High  $\sqrt{s_{NN}}$   $\rightarrow$  high  $T$ , low  $\mu_B$ 
  - Lattice QCD calculations available
  - Crossover transition
  - Early Universe
- Medium  $\sqrt{s_{NN}}$   $\rightarrow$  medium  $\mu_B$  &  $T$ 
  - Critical Point?
  - 1st order PT/crossover
- Low  $\sqrt{s_{NN}}$   $\rightarrow$  high  $\mu_B$ , low  $T$ 
  - Nature of neutron stars
  - Onset of deconfinement
- Different collision energies  $\rightarrow$  probing QCD phase diagram

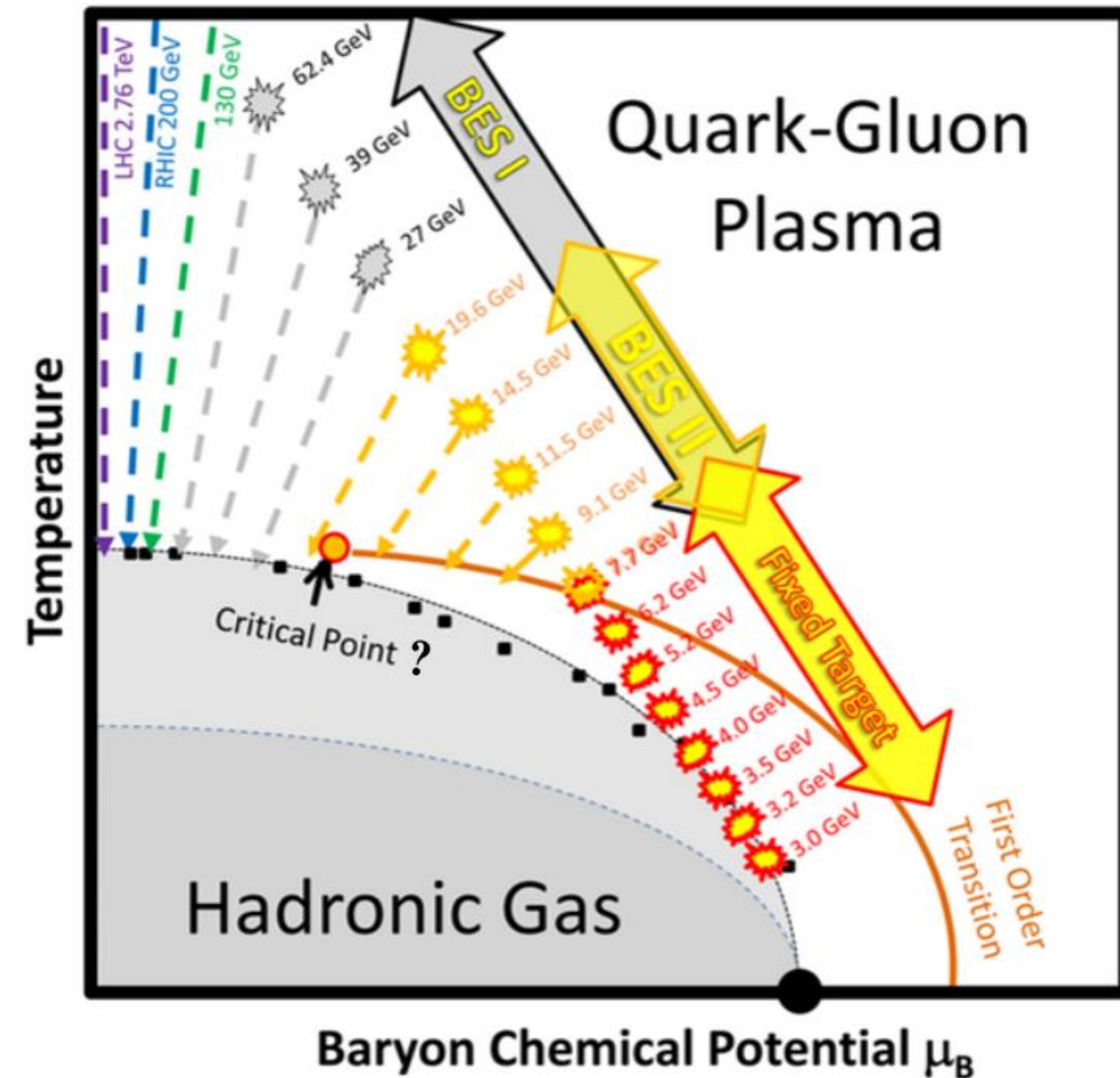


Overview of the QCD phase diagram, Recent progress from the lattice, The European Physical Journal A, •Volume 57, article number 136, (2021), Jana N. Guenther

# Motivation

STAR program:

- High collision energies -> QGP properties
- Beam Energy Scan I, II and Fixed Target
  - onset of deconfinement
  - 1st order phase transition signatures
  - Critical Point



The STAR detector upgrade and future plan, Chi Yang, ICNFP2017



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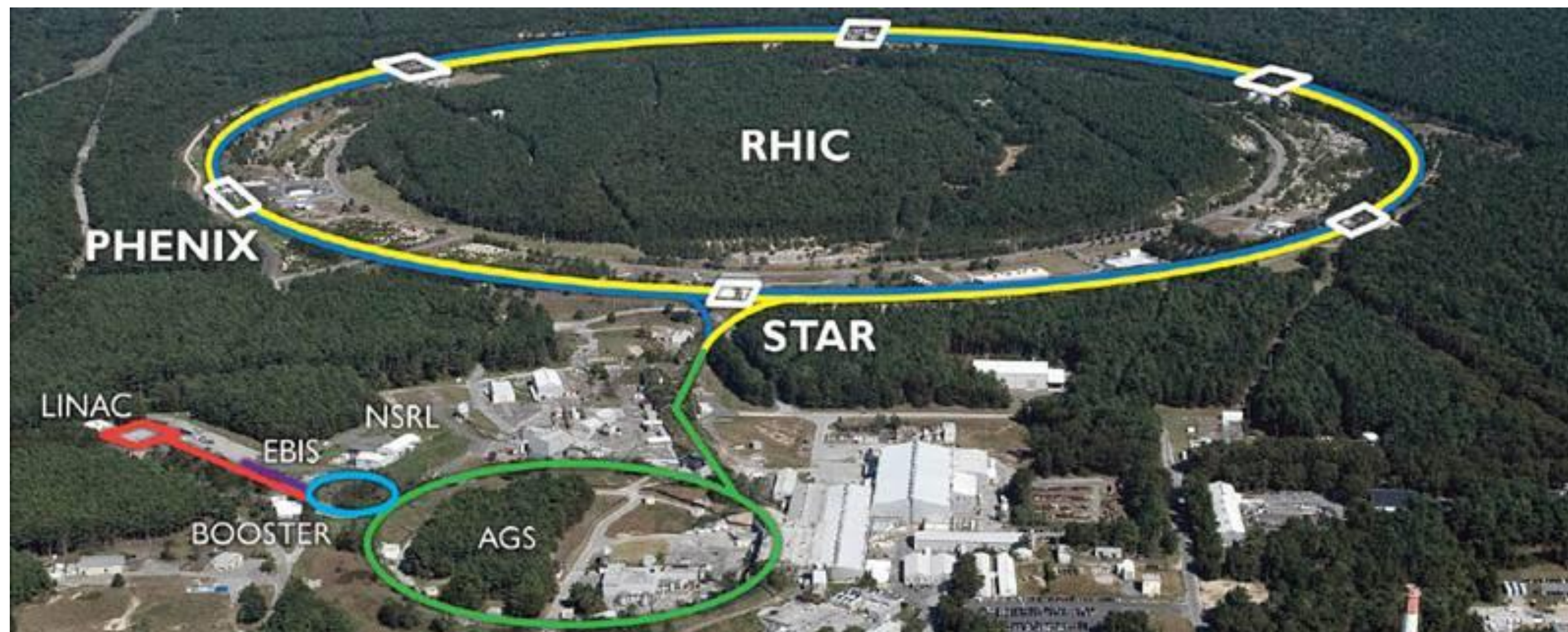
# STAR detector

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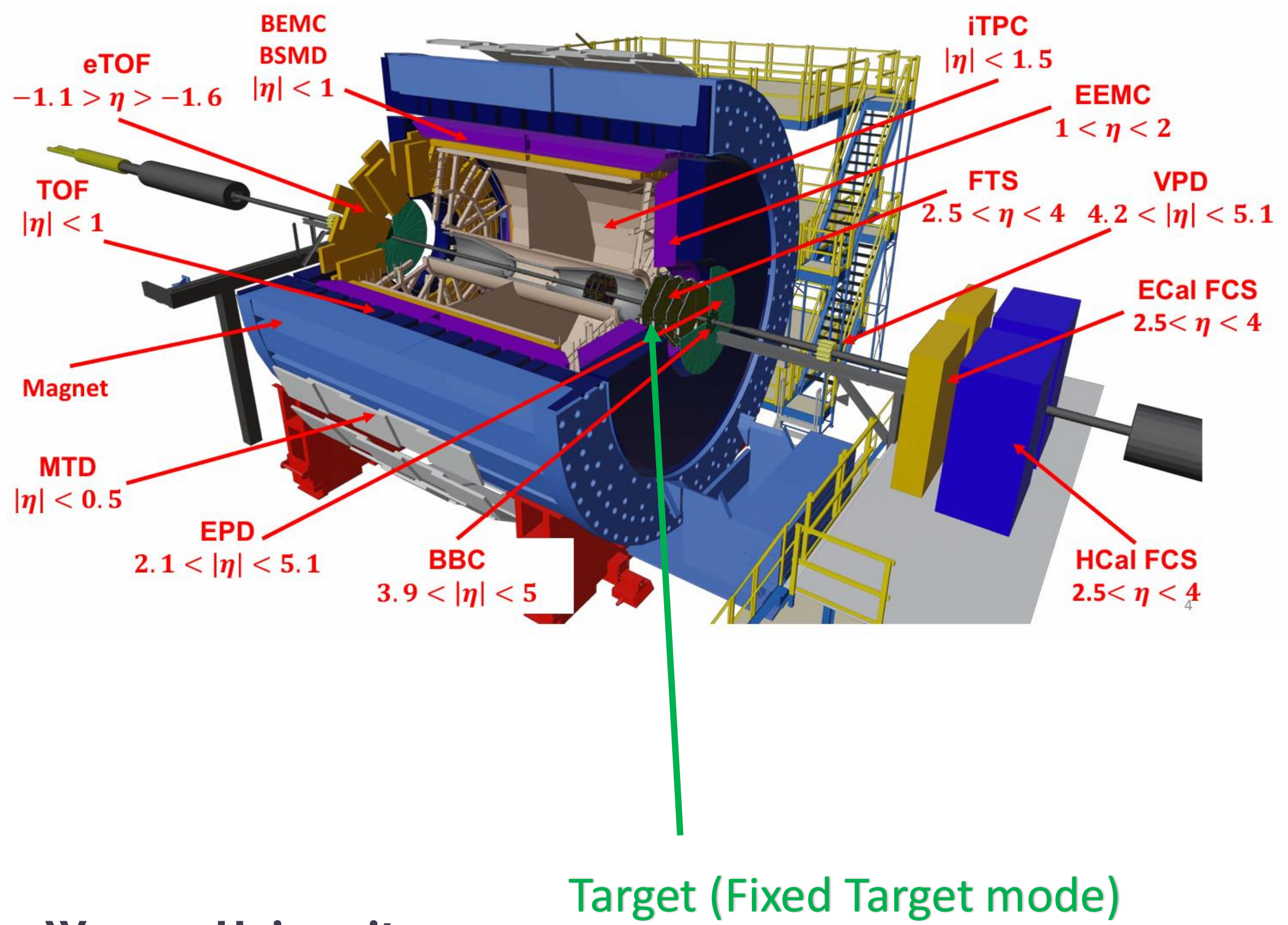
# STAR experiment

STAR = Solenoidal Tracker At RHIC

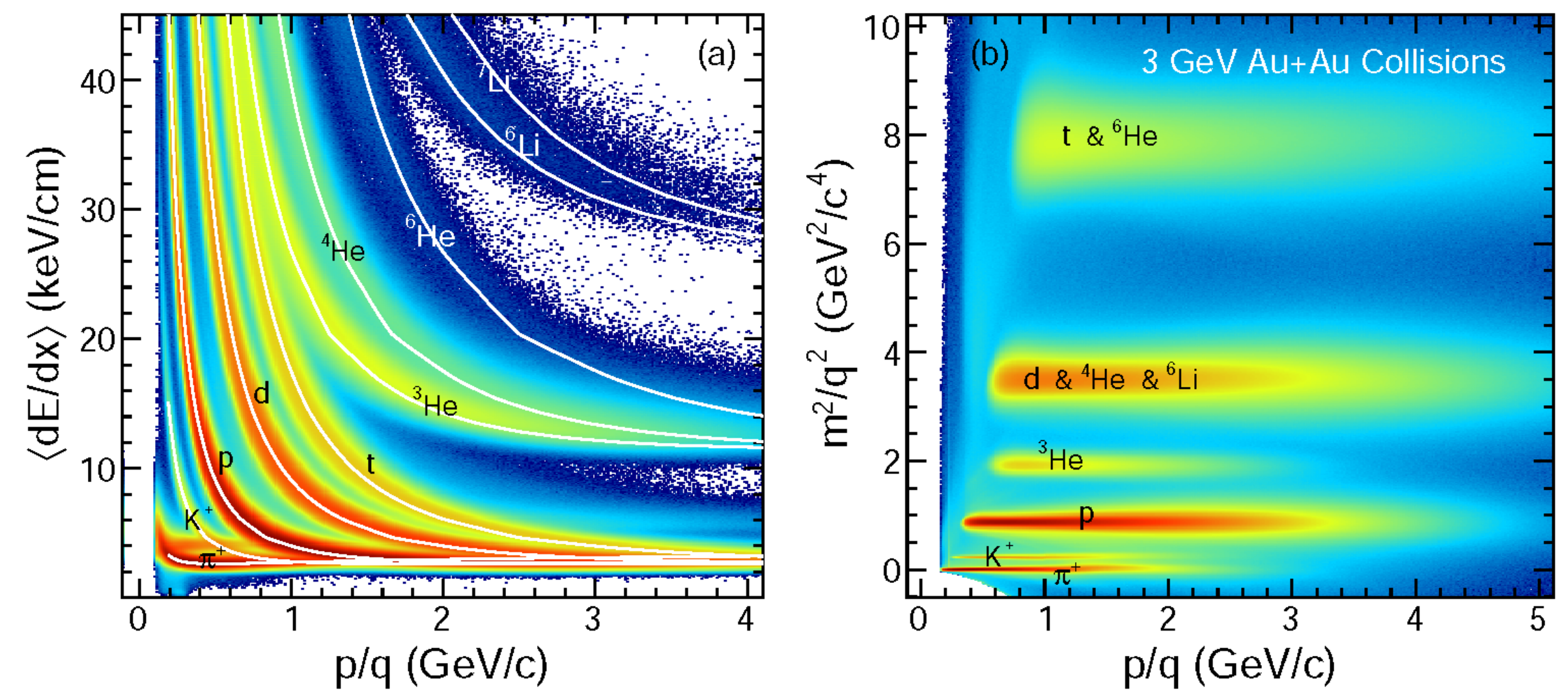


<https://science.osti.gov/np/Facilities/User-Facilities/RHIC>

# STAR detector



- Complex subdetectors system
- Excellent particle identification
- Numerous detectors upgrades tailored to achieve unique physics goals
- Full azimuthal acceptance



Light nuclei collectivity from  $\sqrt{s_{NN}} = 3$  GeV Au+Au collisions at RHIC, Physics Letters B Volume 827, STAR Collaboration



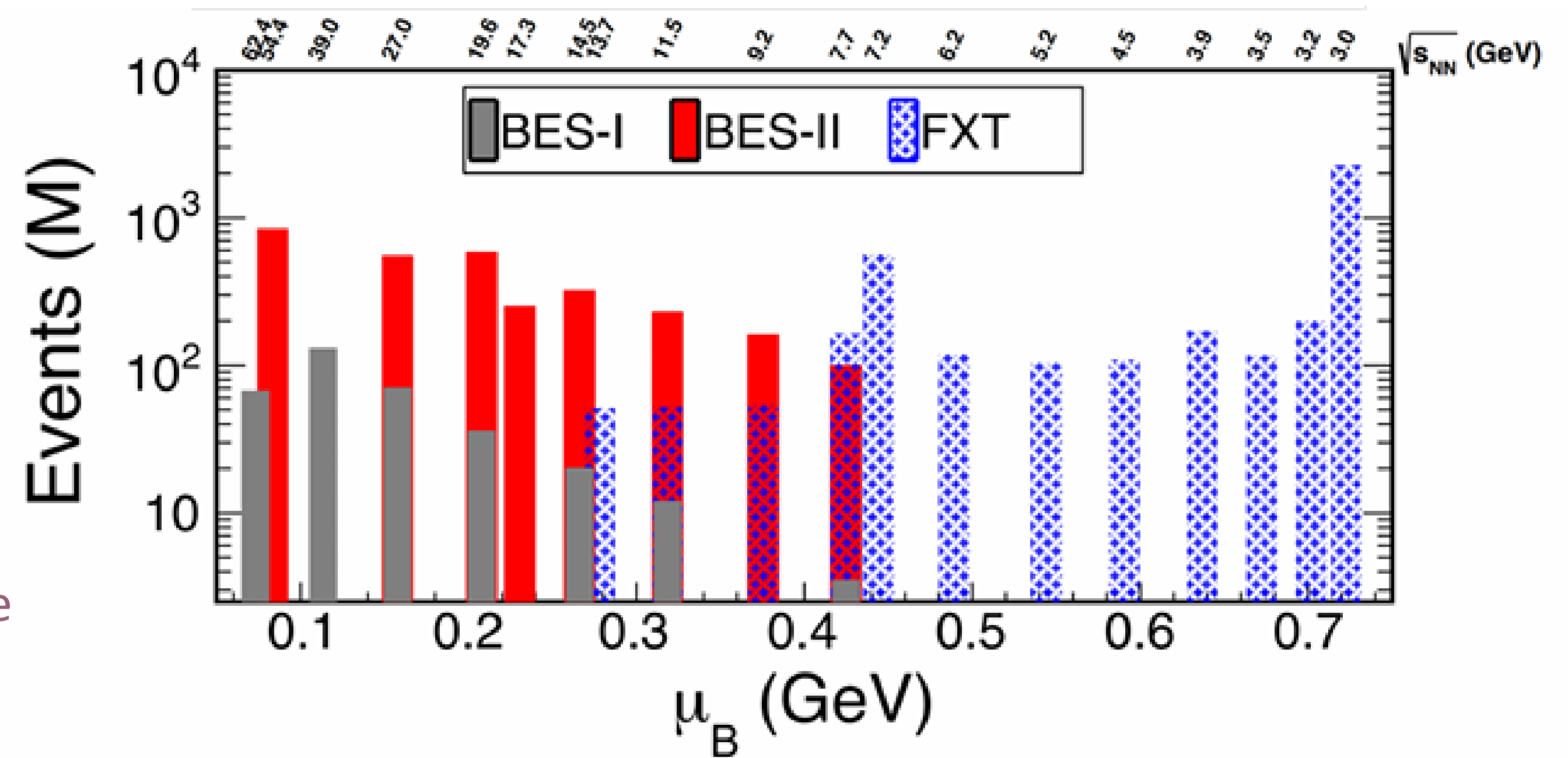
# BES program

## Beam Energy Scan I

- Scan of QCD phase diagram

## Beam Energy Scan II/Fixed Target (FXT)

- more events registered
- better data quality e.g., increased acceptance (detector improvements iTPC, eTOF, EPD...)
- lower collision energies- extending the  $\mu_B$  up to 750 MeV with FXT program



Korobitsyn, A. STAR Experiment Results from BES Program. *Phys. Part. Nuclei* **55**, 1037–1042 (2024).

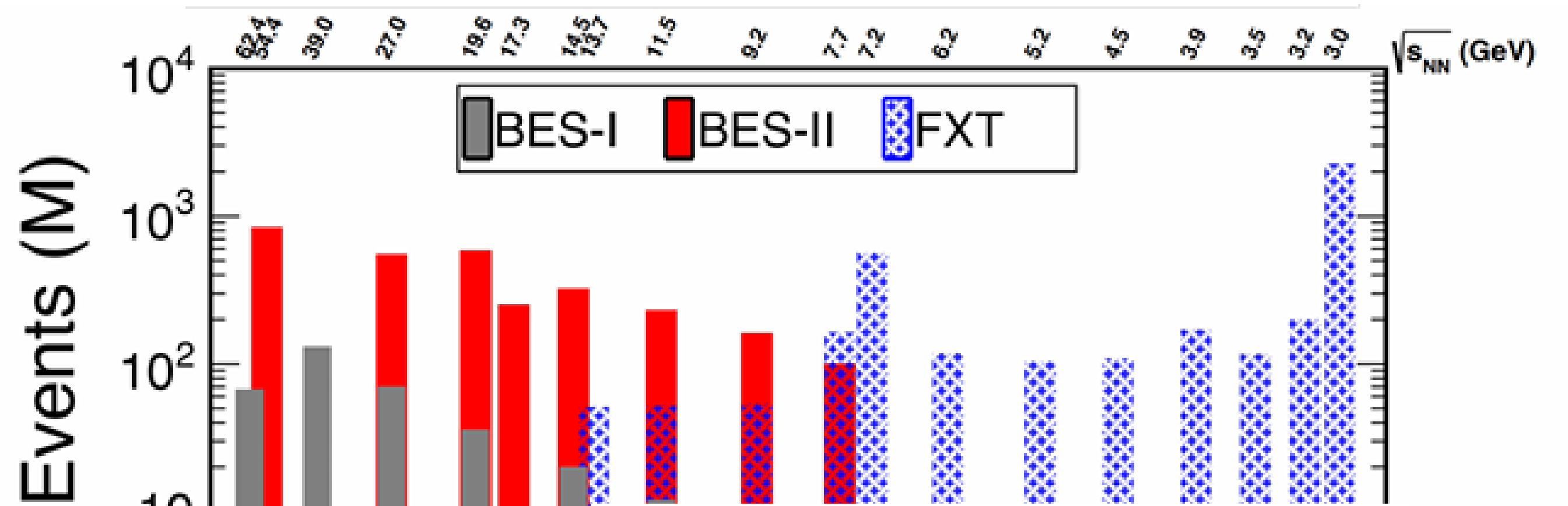
# BES program

## Beam Energy Scan I

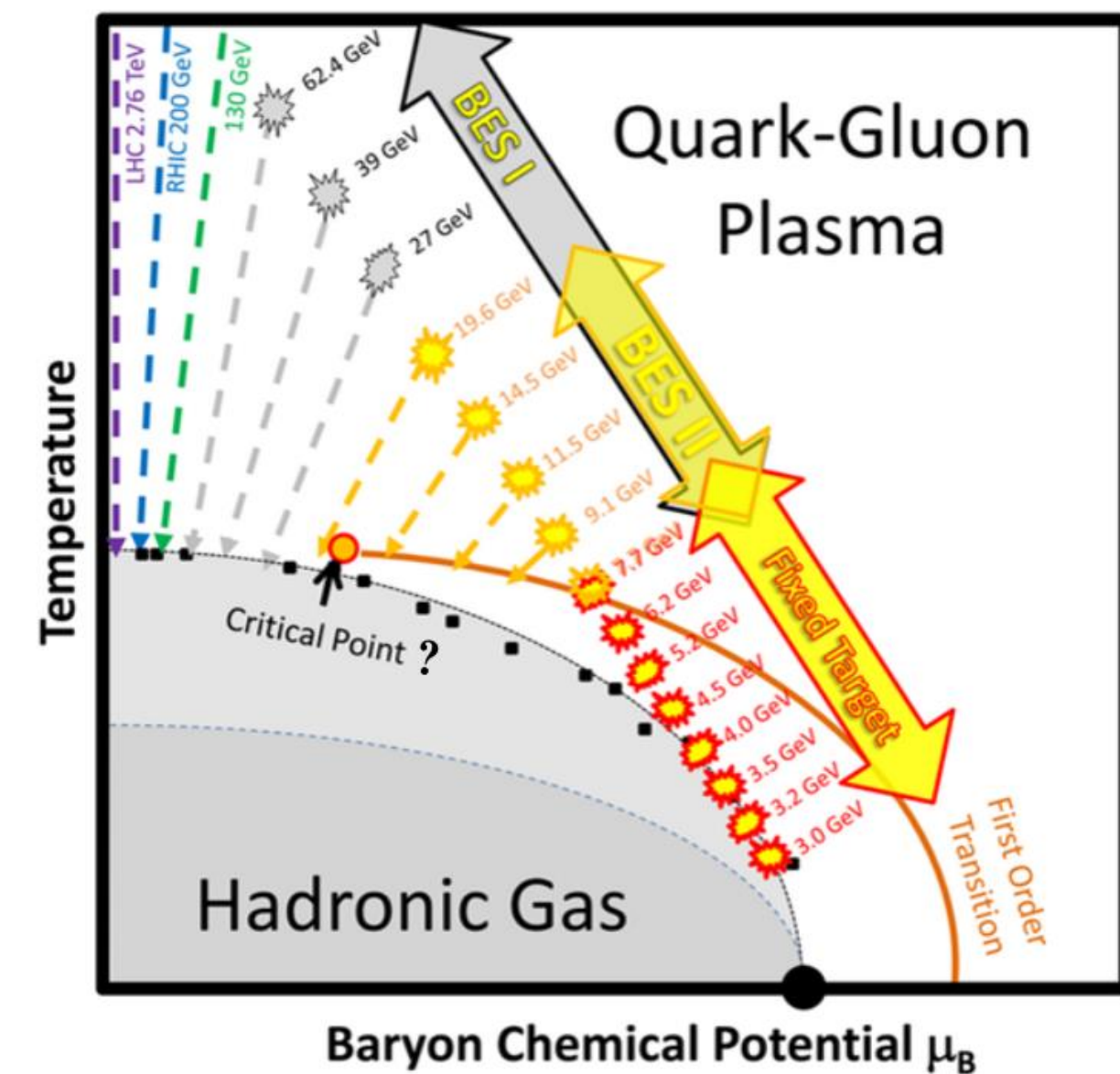
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Korobitsyn, A. STAR Experiment Re:



The STAR detector upgrade and future plan, Chi Yang, ICNFP2017



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# Fluctuations

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# Fluctuations

Fluctuations are sensitive to the correlation length ( $\xi$ ).

$$C_n^q = VT^3 \chi_n^q$$

Cumulants n=1-6:

$$C_1 = \langle N \rangle$$

$$C_2 = \langle \delta N^2 \rangle$$

$$C_3 = \langle \delta N^3 \rangle$$

$$C_4 = \langle \delta N^4 \rangle - 3\langle \delta N^2 \rangle^2$$

$$C_5 = \langle \delta N^5 \rangle - 5\langle \delta N^3 \rangle \langle \delta N^2 \rangle$$

$$C_6 = \langle \delta N^6 \rangle - 15\langle \delta N^4 \rangle \langle \delta N^2 \rangle - 10\langle \delta N^3 \rangle^2 + 30\langle \delta N^2 \rangle^3$$

$$\delta N = N - \langle N \rangle$$

Ratio of cumulants – no volume dependency -> cleaner signature of CP.

Some of them are well known:

$$\text{Variance : } \sigma = \langle \delta N^2 \rangle$$

Skewness:

$$S = \frac{\langle \delta N^3 \rangle}{(\langle \delta N^2 \rangle)^{3/2}} \quad S\sigma = \frac{C_3}{C_2}$$

Kurtosis:

$$\kappa = \frac{\langle \delta N^4 \rangle}{(\langle \delta N^2 \rangle)^2} \quad \kappa\sigma^2 = \frac{C_4}{C_2}$$

# Fluctuations

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$$C_n^q = VT^3 \chi_n^q$$

Cumulants n=1-6:

$$C_1 = \langle N \rangle$$

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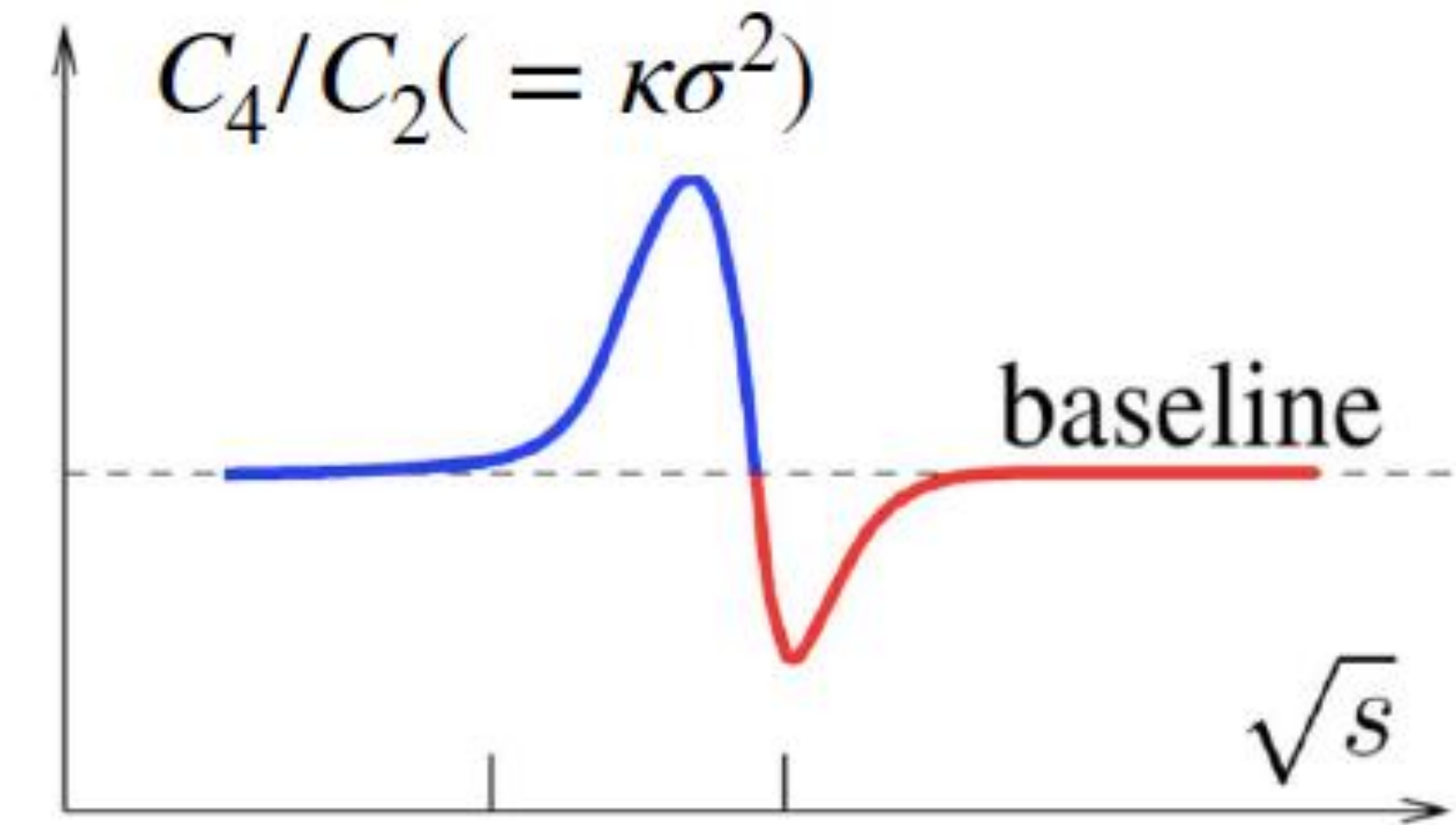
$$C_4 = \langle \delta N^4 \rangle - 3\langle \delta N^2 \rangle^2$$

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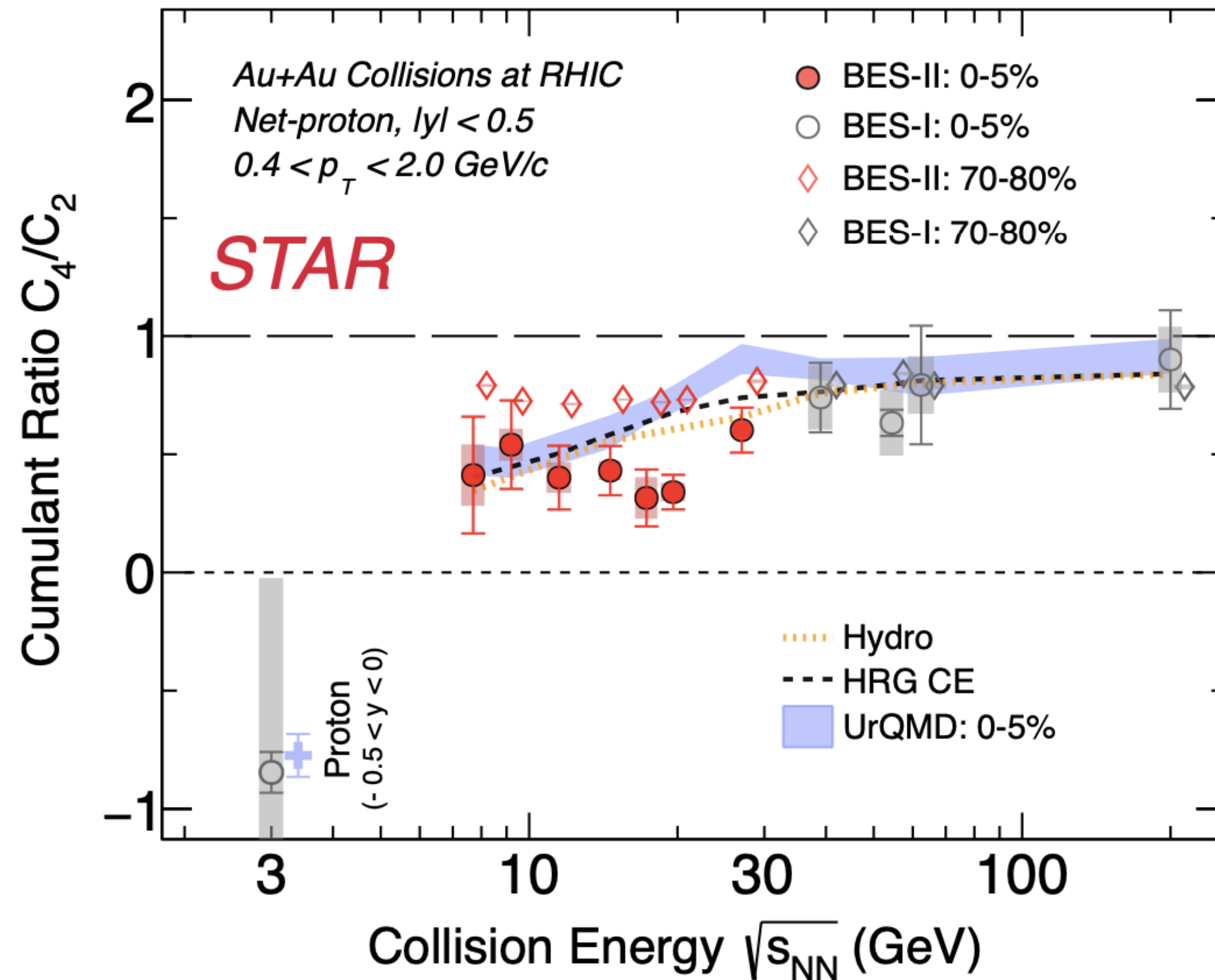
Ratio of cumulants – no volume dependency -> cleaner signature of CP.



*M. A. Stephanov, PRL 107 (2011) 052301*

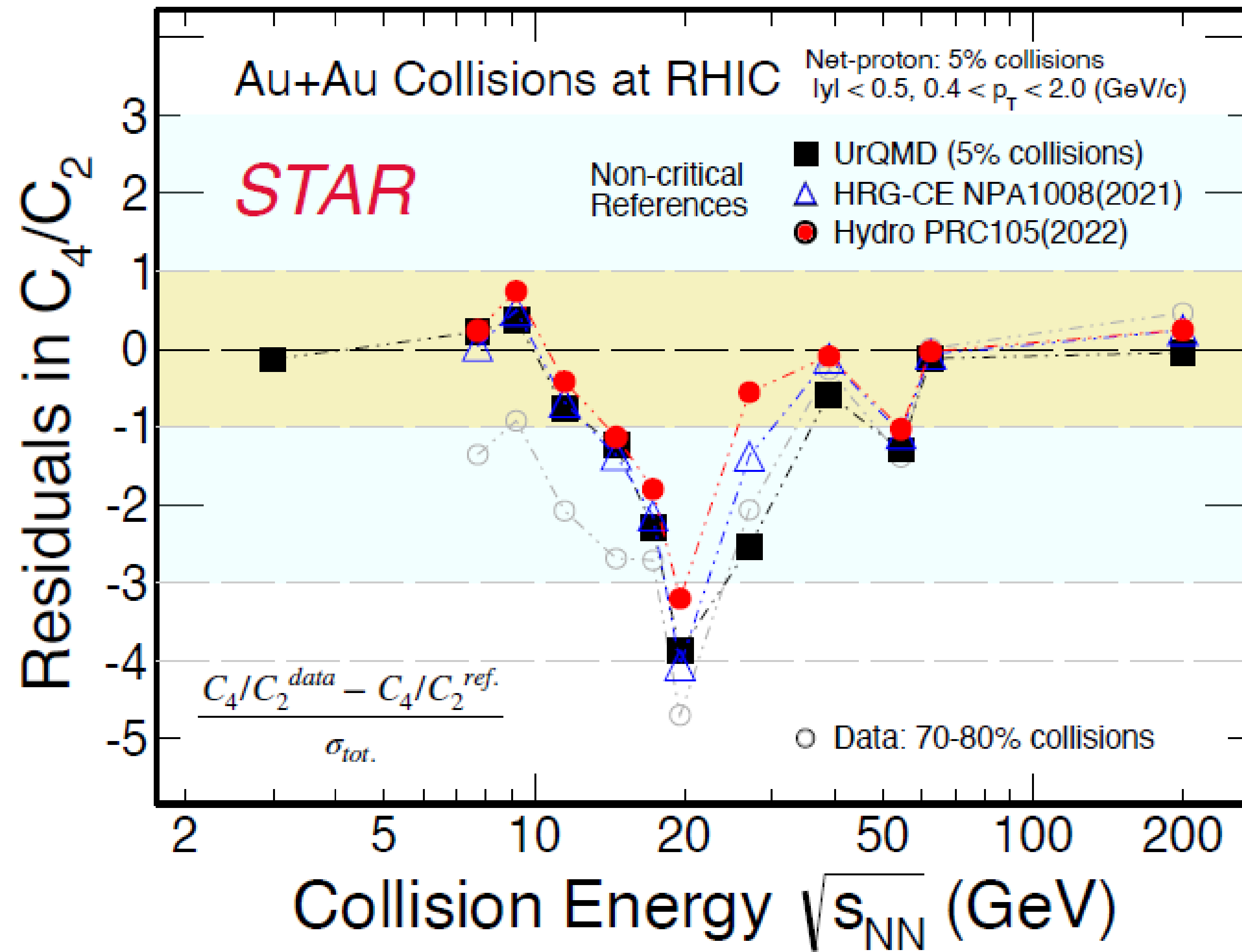
CP – non-monotonic behavior of  $C_4/C_2$  ratio.

# Fluctuations (net-proton)



- Comparison of STAR data with models without CP
- Greater measurement precision in BES-II
- **Deviation of data at  $\sqrt{s_{NN}} \approx 20$  GeV!**
- Analysis of FXT data ongoing

# Fluctuations (net-proton)



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# Femtoscscopy

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# How femtoscopy works? What can we measure with femtoscopy?



# Femtoscscopy

Femtoscscopy uses the Correlation Function defined as:

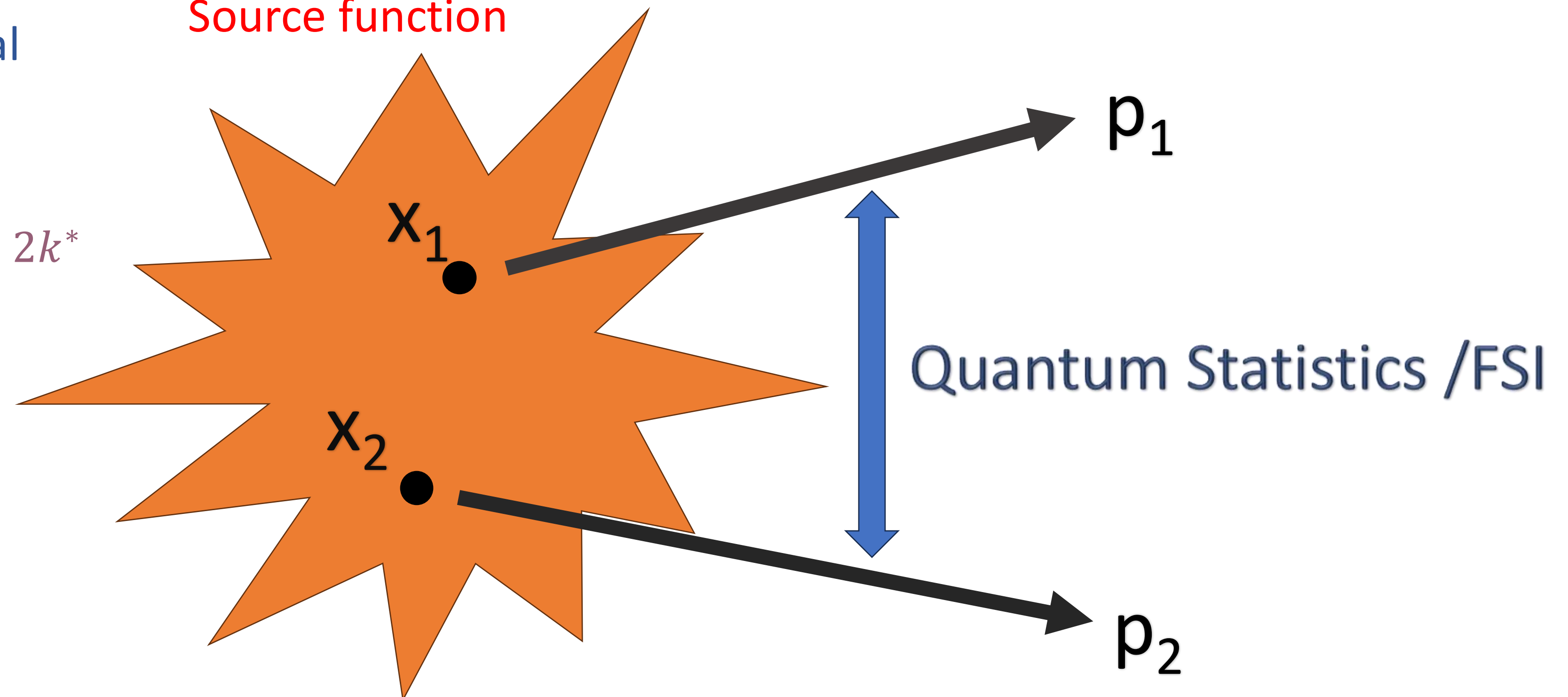
$$C(q) = \frac{P(p_1, p_2)}{P(p_1)P(p_2)} = \int \rho(x_1, p_1) \rho(x_2, p_2) |\Psi(x_1, p_1, x_2, p_2)|^2 dx_1 dx_2$$

Experimental  
definition

Source function

Two particle interactions/quantum  
statistics effect

$$q = \sqrt{(p_1 - p_2)^2 - (E_1 - E_2)^2} = 2k^*$$



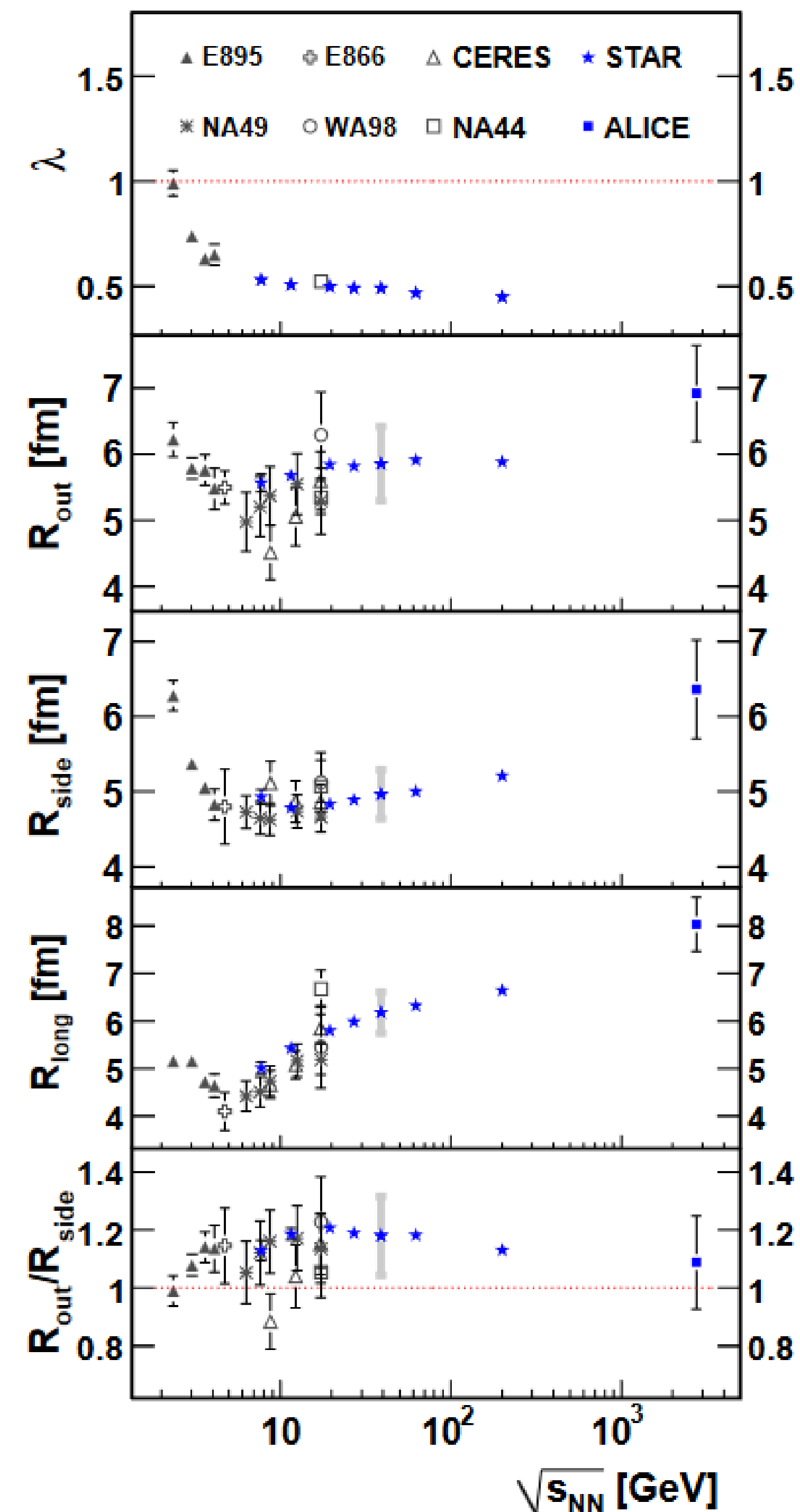
# Femtoscscopy

- Probing spatio-temporal structure of the collision
  - STAR measurements done for various energies, estimated the sizes of the sources in Au+Au collisions at RHIC
  - Maximum of  $R_{out}/R_{side}$  ratio visible at  $\sqrt{s_{NN}} \approx 20\text{GeV}$ , critical behavior?
  - Minimum of  $R_{long}$  at  $\sqrt{s_{NN}} \approx 5\text{-}10\text{GeV}$  – transition from QGP to HG?
  - **Currently working with analysis of data for lower energies**

$R_{long}$  - size parallel the beam

$R_{out}$  - size perpendicular to beam

$R_{side}$  - size perpendicular to out/long



# Femtoscscopy

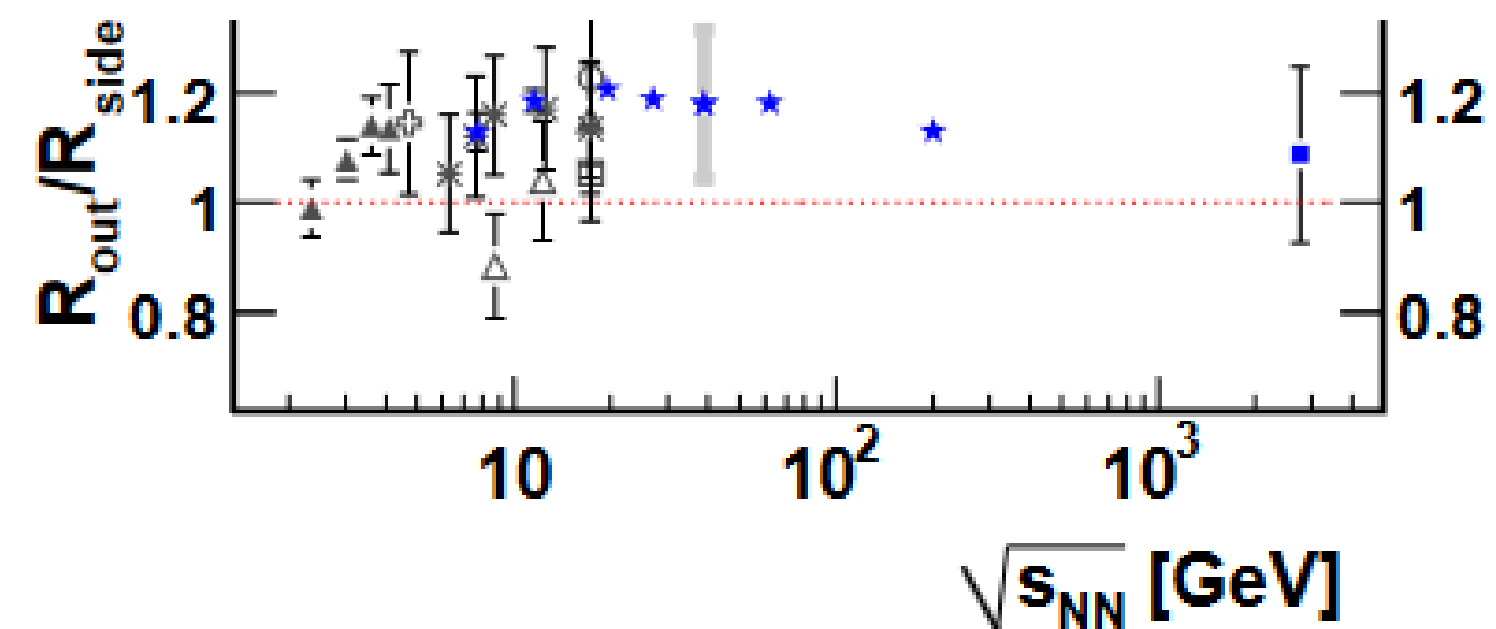
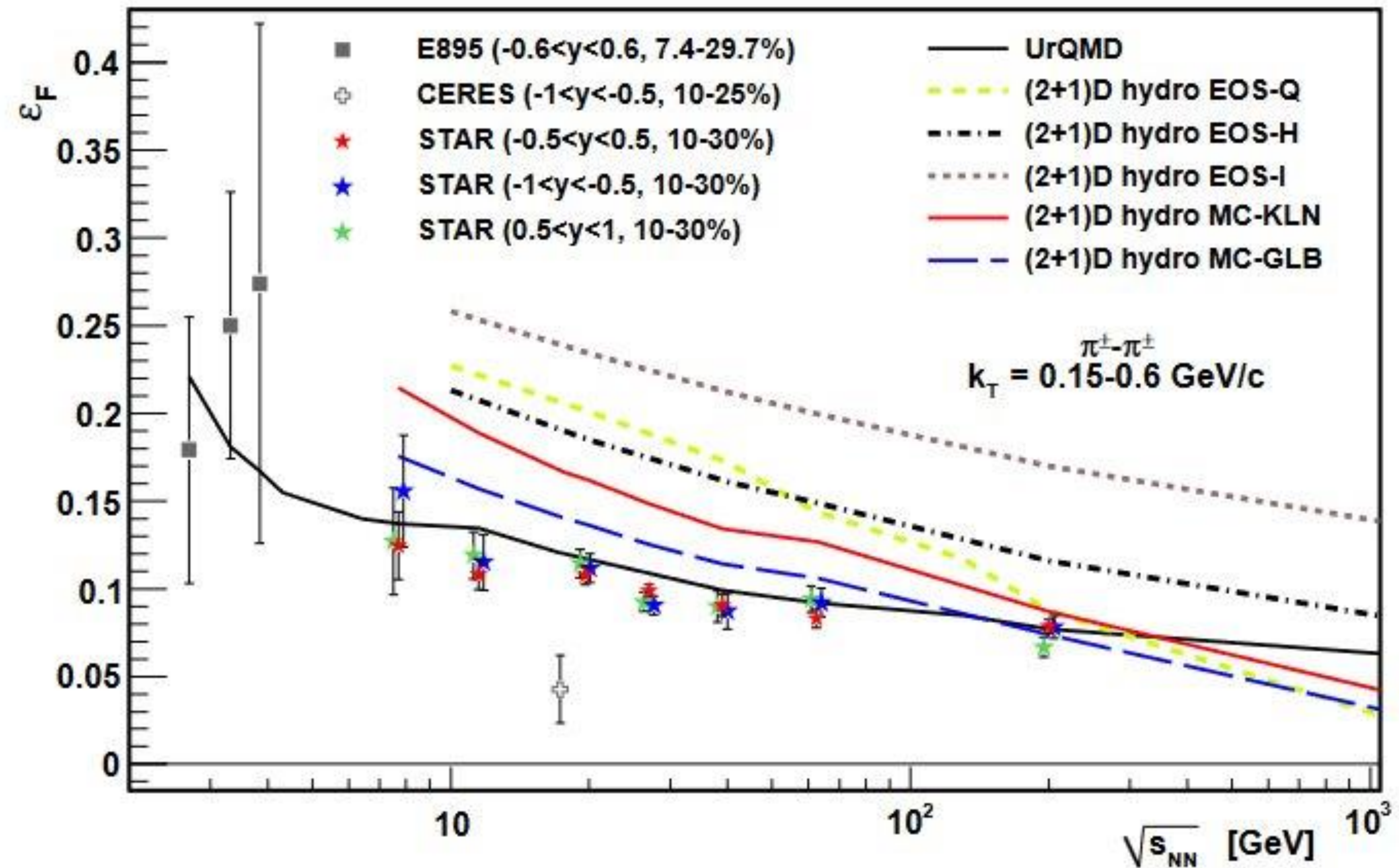
Eccentricity measured by STAR compared to various theoretical models.

Size of fireball:

$\sigma_x$  – in the reaction plane

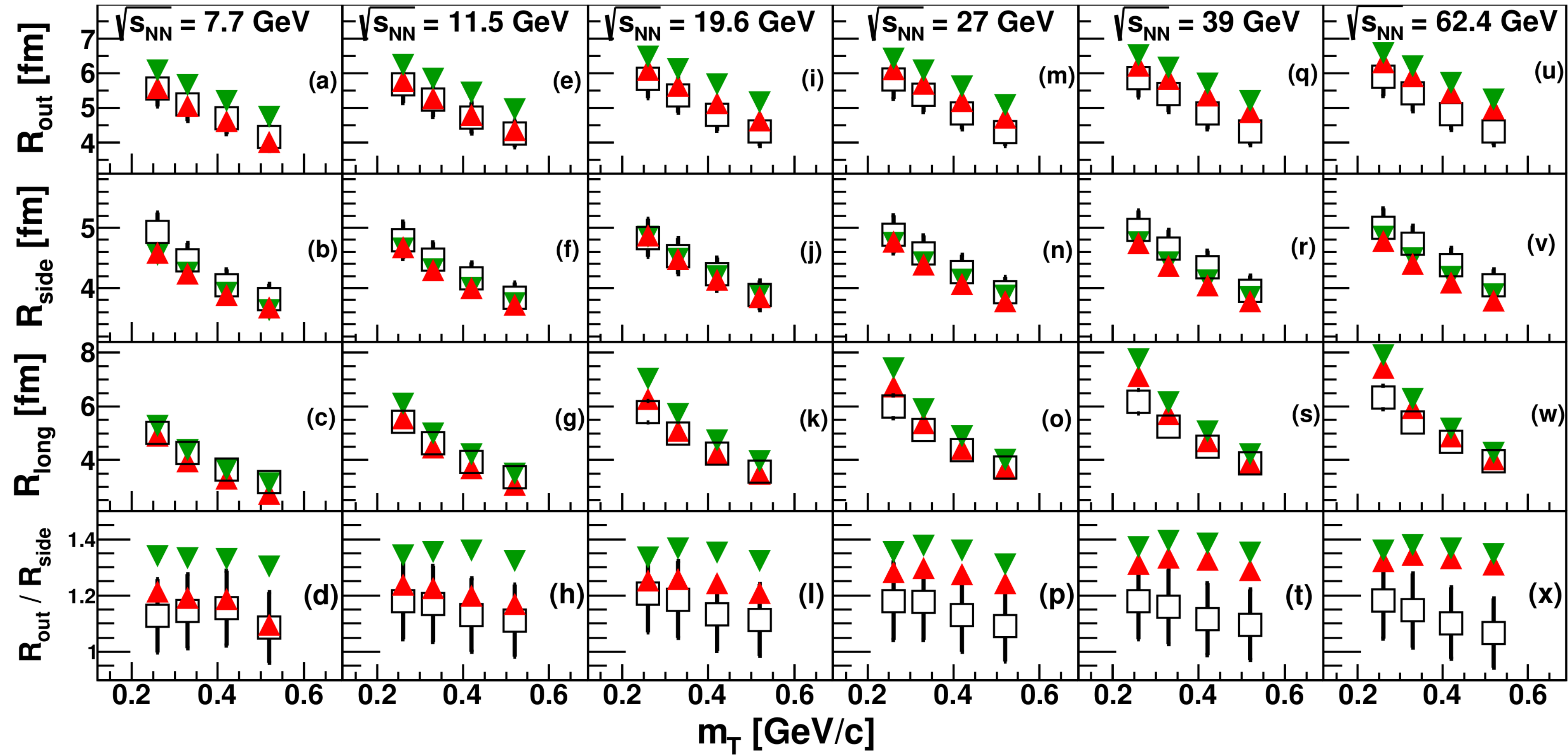
$\sigma_y$  – out of the reaction plane

$$\epsilon_F = \frac{\sigma_y'^2 - \sigma_x'^2}{\sigma_y'^2 + \sigma_x'^2}$$



# Femtoscscopy

vHLL+UrQMD calculations with different Equation of State gives different femtoscopic radii.



Crossover EoS  
1st order EoS  
STAR data

J. Steinheimer, S. Schramm, and H. Stöcker, J. Phys. G 38, 035001 (2011)

1PT EoS P. F. Kolb, J. Sollfrank, and U. W. Heinz, Phys. Rev. C 62, 054909 (2000).

Correlation femtoscopy study at energies available at the JINR Nuclotron-based Ion Collider Facility and the BNL Relativistic Heavy Ion Collider within a viscous hydrodynamic plus cascade model, P. Batyuk et al. Phys. Rev. C 96, 024911



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Recent results from STAR.

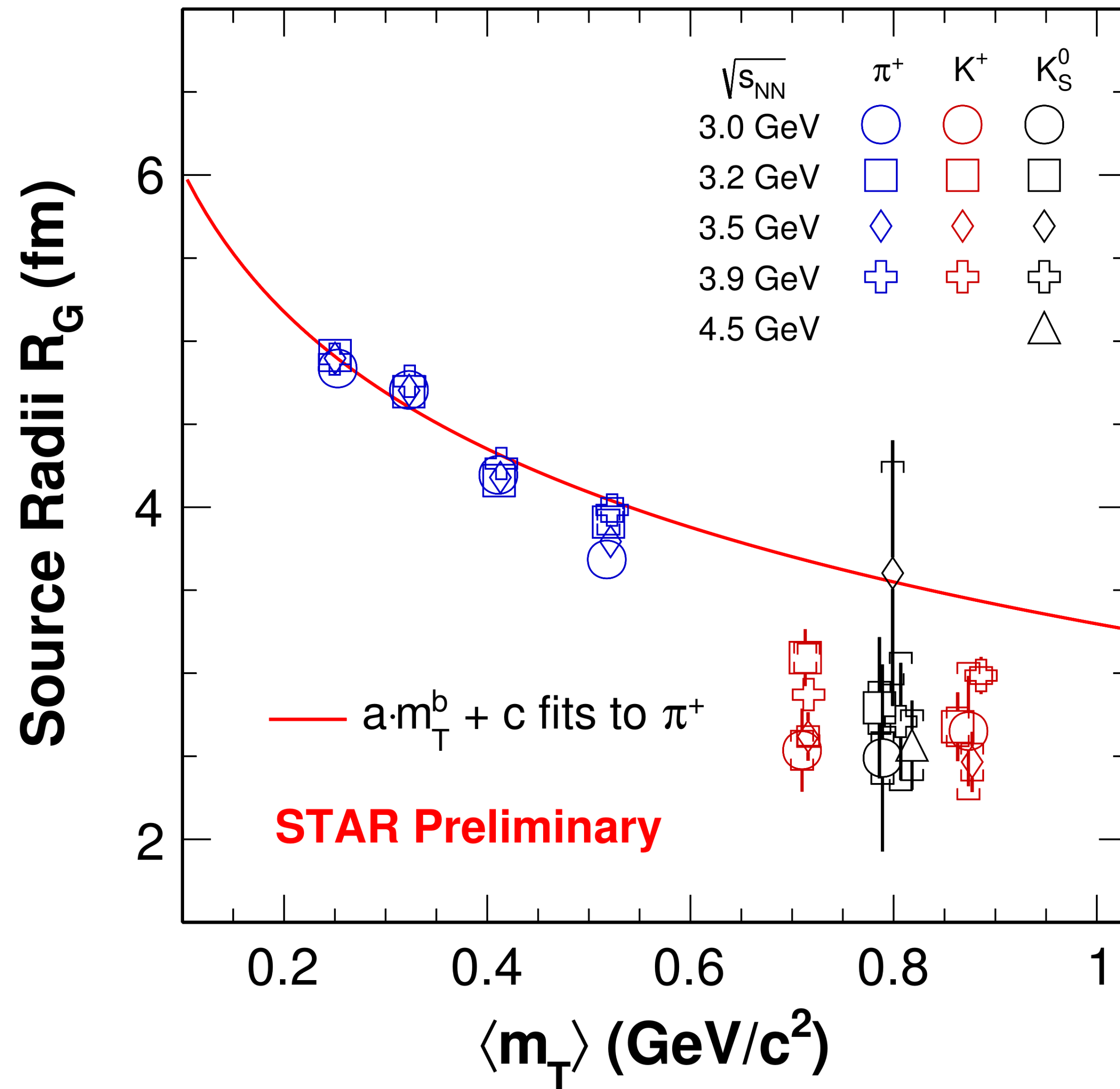
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# Femtoscopy

## Kaon Femtoscopy:

- Kaons are less contaminated by resonances than pions
- It is observed that Kaons  $R_G$  do not follow the power-law distributions extracted from pions at the same collisions implying lack of equilibrium among different particle species in such collisions



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# Femtoscscopy

Asymmetry in kaon production:

We measure  $K^0_S$  or  $K^0_L$  states, they are mixtures of  $K^0$  and anti- $K^0$

Correlation function for kaons\*:

$$C(q) = \lambda \left[ e^{-q^2 R^2} + \frac{1-\epsilon^2}{2} SI(q) \right]$$

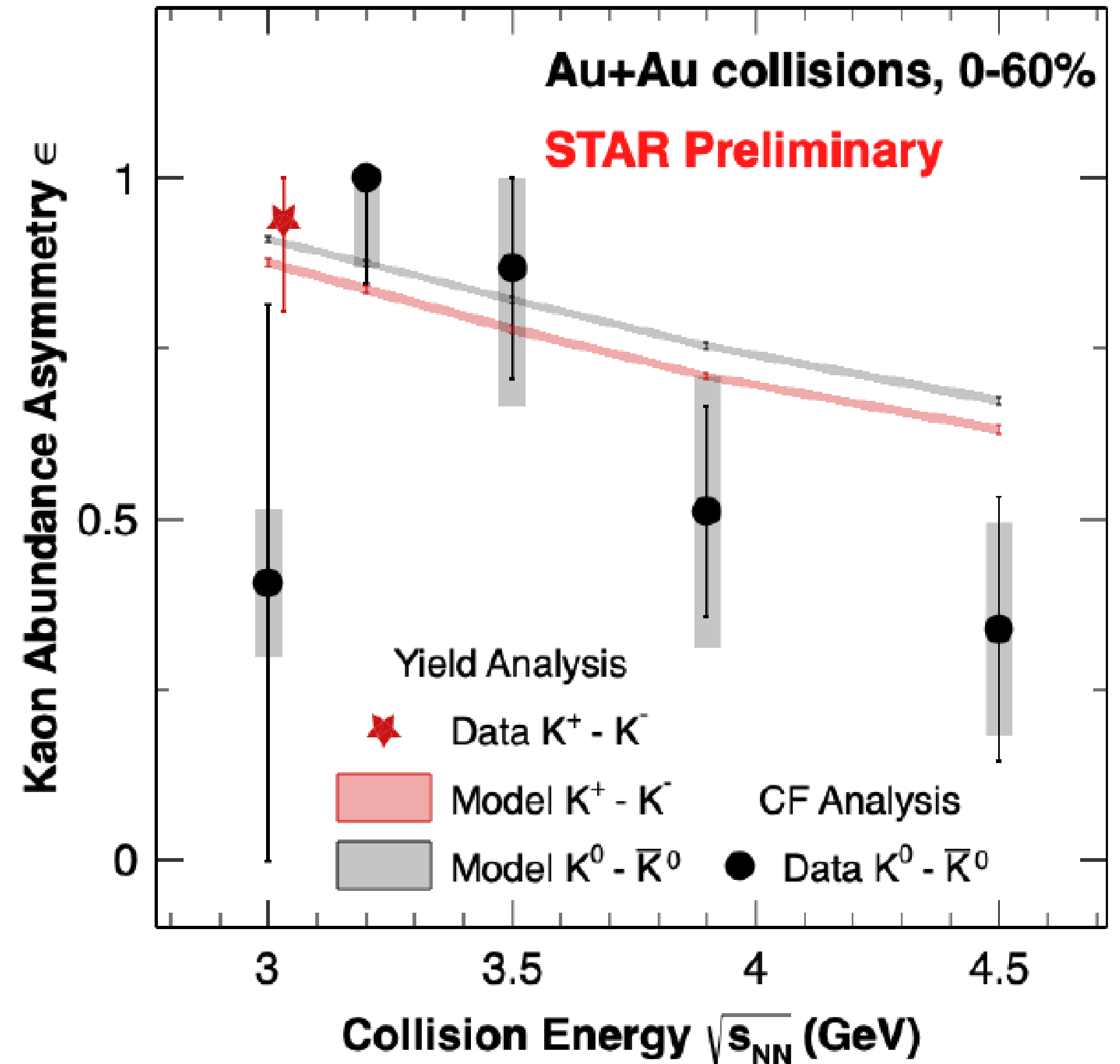
*Quantum statistic*

*SI(q) – Strong Interaction*

$$\epsilon = \frac{K - \bar{K}}{K + \bar{K}}$$

STAR data show that asymmetry increases when collision energy decreases; this trend can be reproduced by models.

*\*full formula in backup slides*





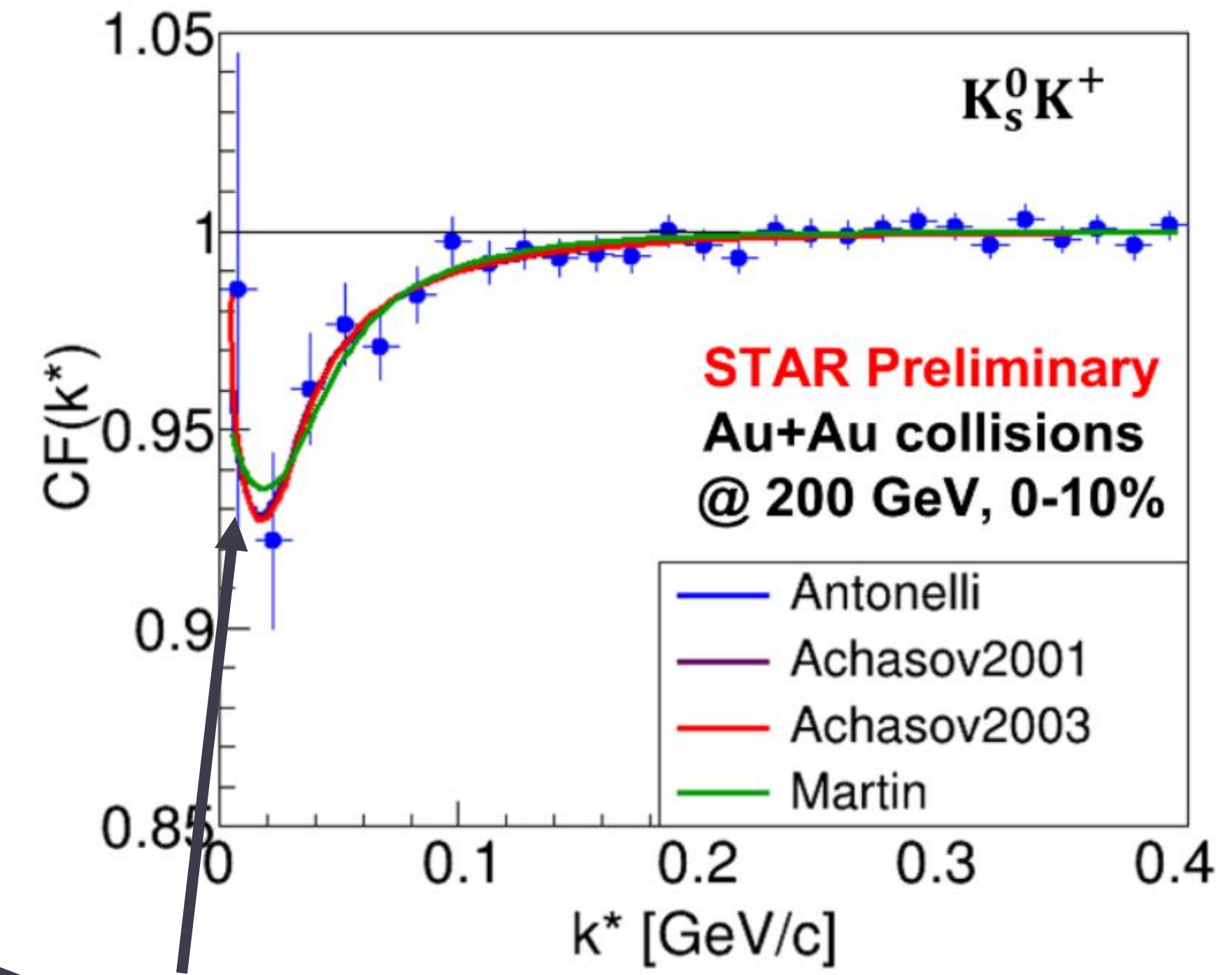
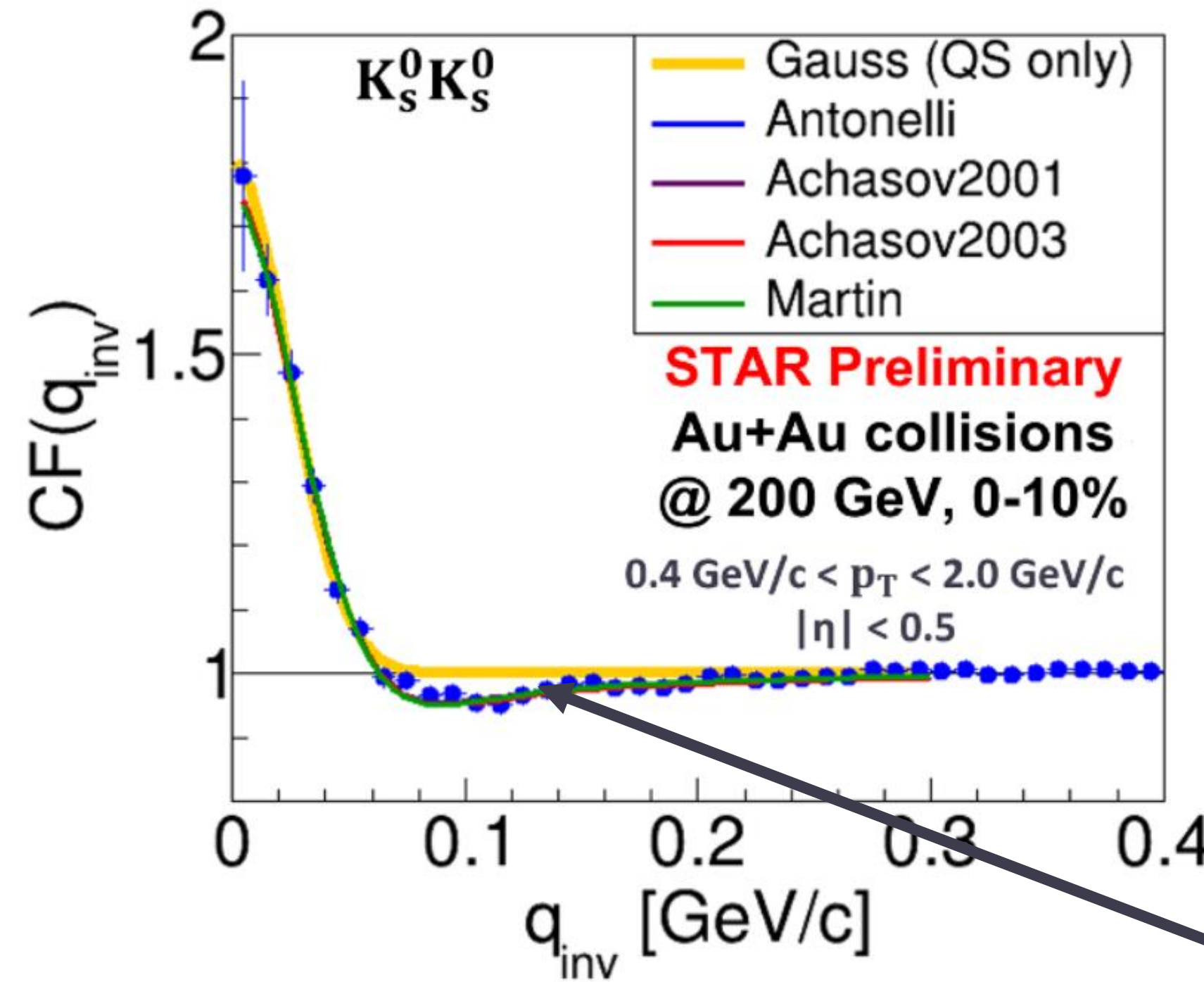
# Femtoscscopy

	$m_{f_0} \left[ \frac{GeV}{c^2} \right]$	$\gamma_{f_0 K \bar{K}}$	$\gamma_{f_0 \pi \pi}$	$m_{a_0} \left[ \frac{GeV}{c^2} \right]$	$\gamma_{a_0 K \bar{K}}$	$\gamma_{a_0 \pi \pi}$
Antonelli [1]	0.973	2.763	0.5283	0.985	0.4038	0.3711
Achasov2001 [2]	0.996	1.305	0.2684	0.992	0.5555	0.4401
Achasov2003 [3]	0.996	1.305	0.2684	1.003	0.8365	0.4580
Martin [4]	0.978	0.792	0.1990	0.974	0.3330	0.2220

[1] eConf C020620, THAT06 (2002), [2] Phys. Rev. D 63, 094007 (2001)  
 [3] Phys. Rev. D 68, 014006 (2003), [4] Nucl. Phys. B 121, 514–530 (1977)

- Neutral kaons interact by  $a_0(980)$  resonance
- CF shape  $\rightarrow a_0$  properties
- Is  $a_0$  a  $(q_1, \bar{q}_2)$  or tetraquark state  $(q_1, \bar{q}_2, s, \bar{s})^*$ ?
- Current data suggest that  $a_0$  is a tetraquark

\* $q_1, q_2$  – u or d quark



Strong interaction

Femtoscscopy measurements of two-kaon combinations in Au+Au collisions at the STAR experiment, D. Pawłowska, EPJ Web of Conferences 276, 01016 (2023)

# Femtoscscopy - baryons

Lednický-Lyuboshitz:

$$C(k^*) \approx 1 + \frac{|f(k^*)|}{2R^2} F(d_0) + \frac{2\text{Re}(f(k^*))}{\sqrt{\pi}R} F_1(2k^*R) - \frac{\text{Im}(f(k^*))}{R} F_2(2k^*R)$$

$$f(k^*)^{-1} = \frac{1}{f_0} + \frac{d_0 k^*}{2} - ik^*$$

\*R. Lednický and V. L. Lyuboshitz, Final State Interaction Effect on Pairing Correlations Between Particles with Small Relative Momenta, Yad. Fiz. 35 (1981) 1316, JINR-E2-81-453

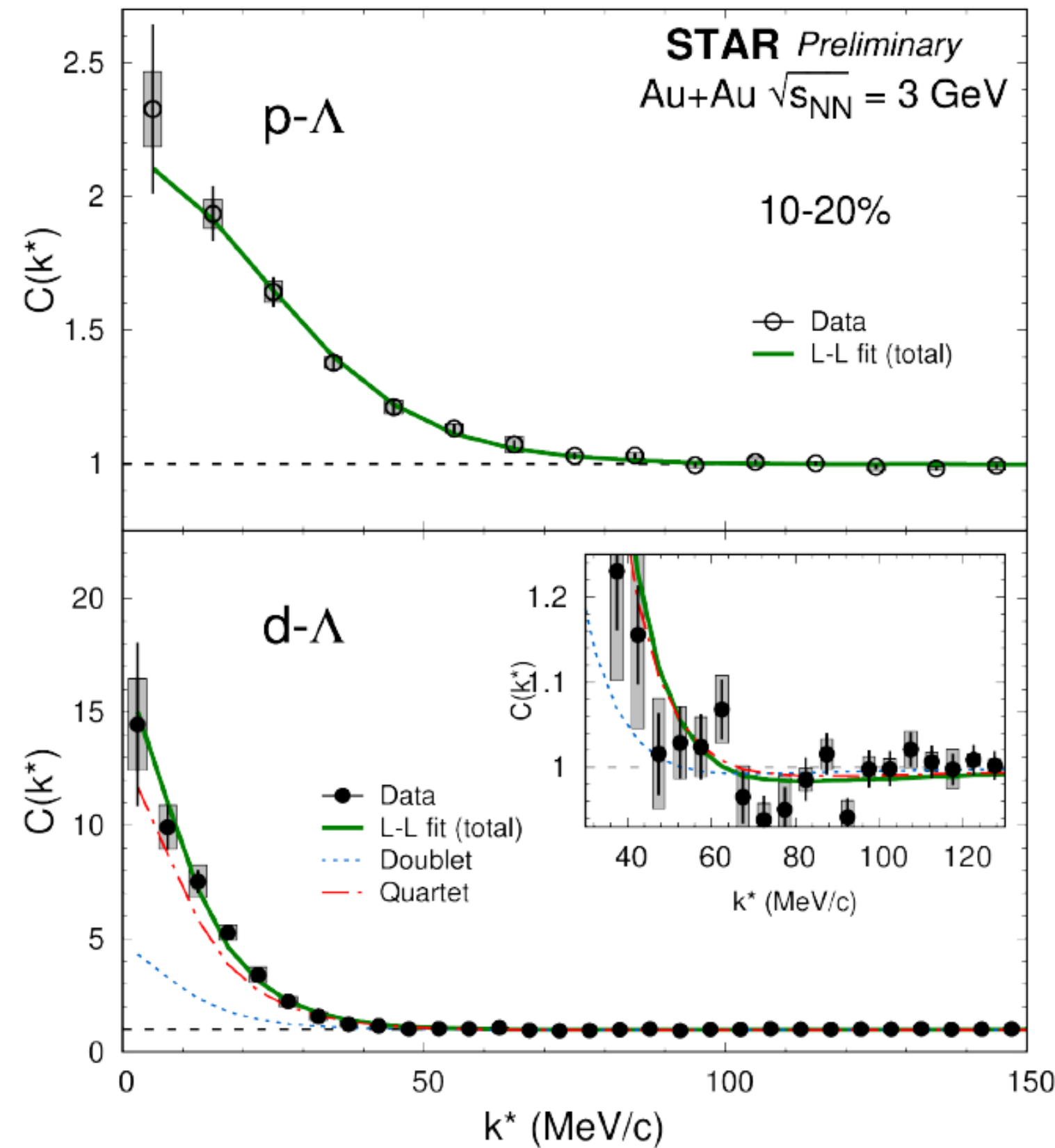
$d_0, f_0$  – effective range, scattering length – parameters that describe the interaction

$R$  – size of source

$p$ - $\Lambda$  = 1/4 singlet + 3/4 triplet

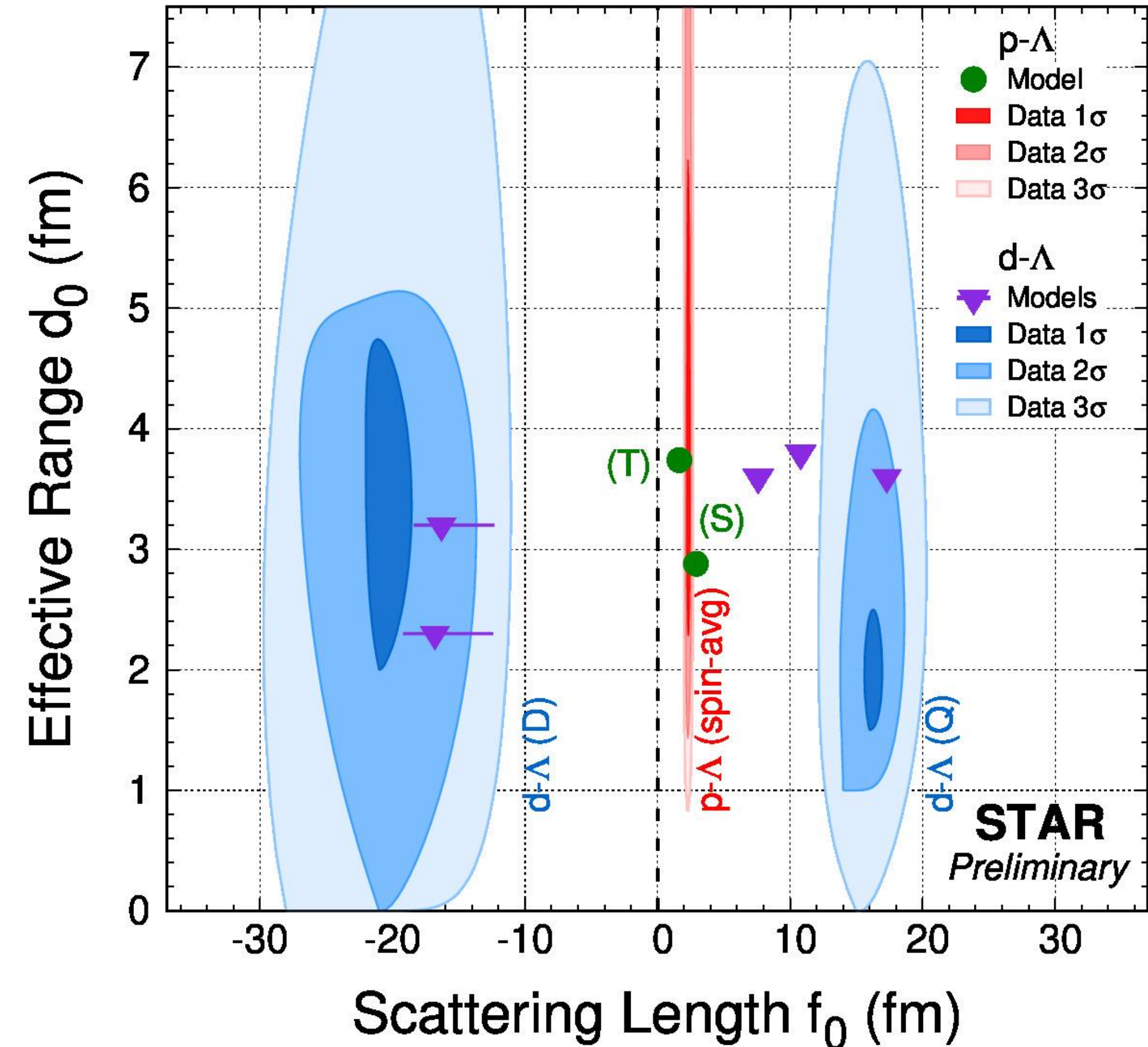
$d$ - $\Lambda$  = 1/3 doublet + 2/3 quartet – statistic big enough to perform spin-separated fits

# p-d and d-Λ system



First extraction of the strong interaction parameters for d-Λ. Measured spin separated parameters for d-Λ and spin averaged for p-Λ.

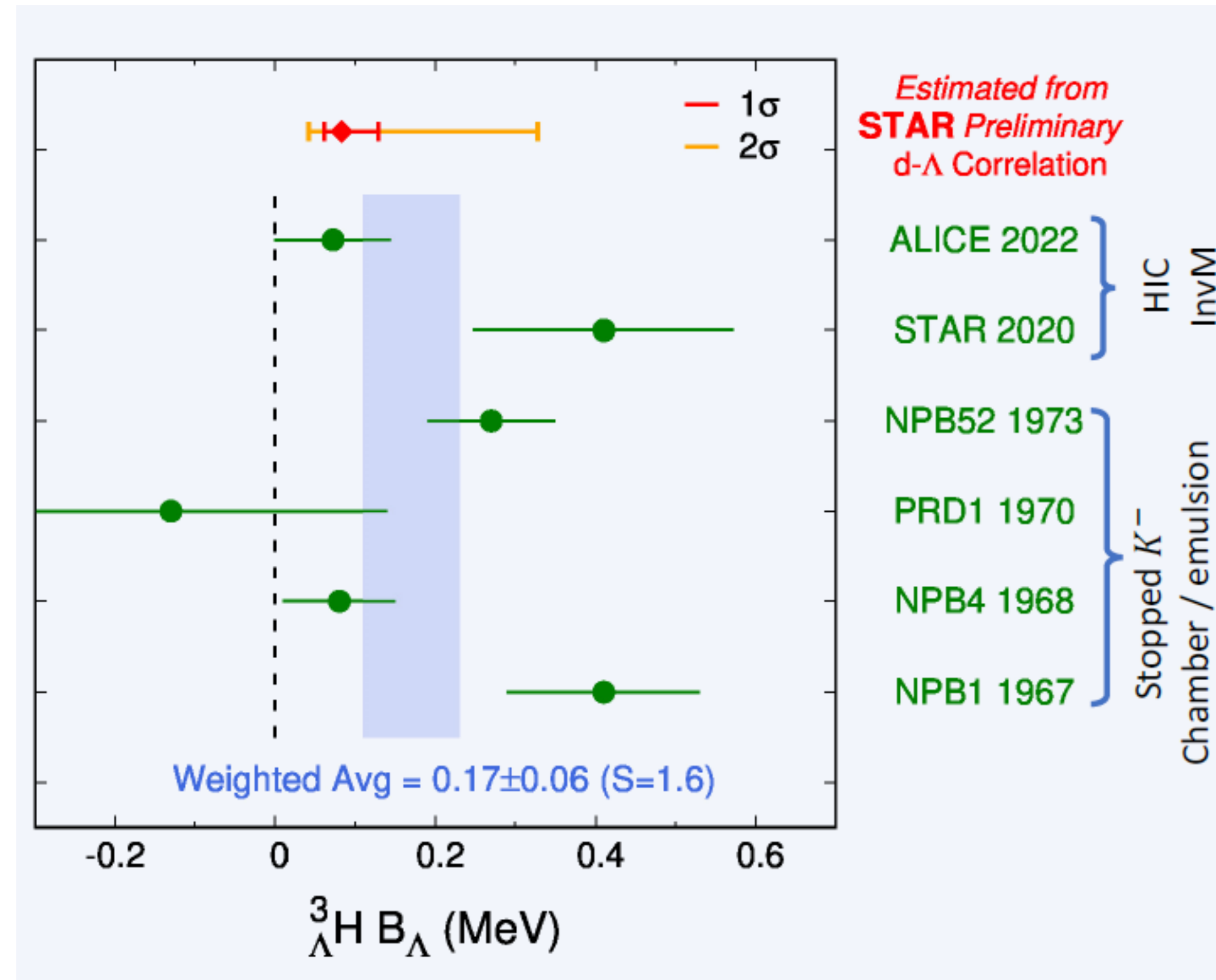
- p-Λ
- $f_0 = 2.32^{+0.12}_{-0.11} \text{ fm}$
  - $d_0 = 3.5^{+2.7}_{-1.3} \text{ fm}$
- d-Λ
- $f_0(D) = -20^{+3}_{-3} \text{ fm}$
  - $d_0(D) = 3^{+2}_{-1} \text{ fm}$
  - $f_0(Q) = 16^{+2}_{-1} \text{ fm}$
  - $d_0(Q) = 2^{+1}_{-1} \text{ fm}$



Measurements of p-Λ and correlations in 3 GeV Au+Au collisions at STAR, Yu Hu, QM 2023

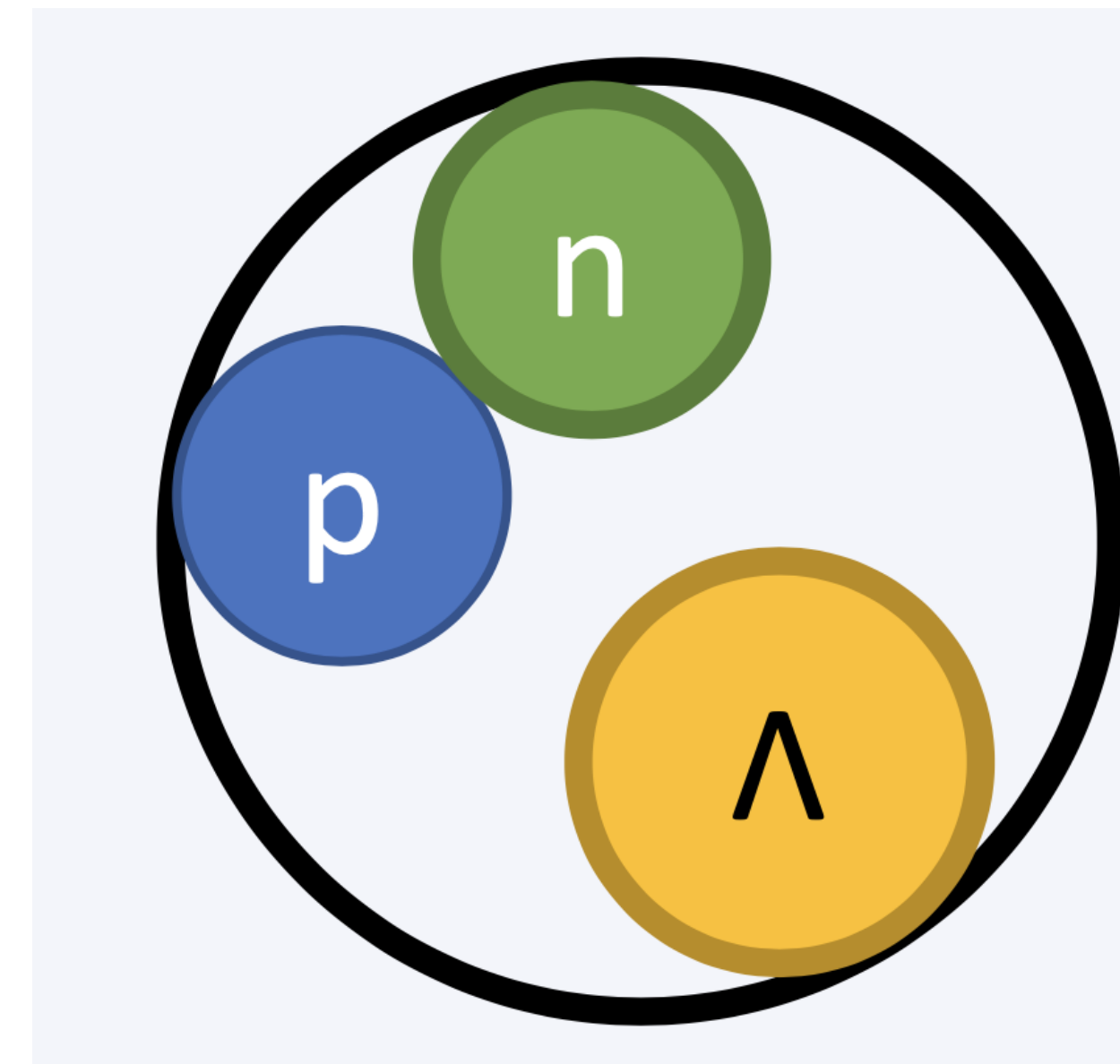
Measurements of p-Λ and correlations in 3 GeV Au+Au collisions at STAR, Yu Hu, QM 2023

# p-d and d- $\Lambda$ system



Measurements of p- $\Lambda$  and correlations in 3 GeV Au+Au collisions at STAR, Yu Hu, QM 2023

Measurements of d- $\Lambda$  correlations allow to extract the binding Energy of  ${}^3_{\Lambda}\text{H}$ .  
Result consistent with previous measurements.





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# Summary

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# Summary

STAR highlights on fluctuations and correlations were shown:

- **Fluctuations**
  - The  $C_4/C_2$  cumulants were measured, BES-II allowed to increase the precision of measurements
  - There is a visible "no deviation" from non-CP models around  $\sqrt{s_{NN}} \approx 20$  GeV
  - Plans: complete analysis of FXT data ( $\sqrt{s_{NN}} = 3-4.5$  GeV)
- **Correlations**
- Kaons measurements at FXT program were reported:
  - Scaling of  $R_{inv}$  with  $m_T$  with kaons is broken between pions and kaons
  - Charged and neutral kaons gives similar results as expected
  - Measurement of kaon abundance asymmetry at low energies
- p- $\Lambda$  and d- $\Lambda$  correlations were measured:
  - For the first time interaction parameters were extracted for d- $\Lambda$
  - Spin averaged parameters extracted for p- $\Lambda$
  - Binding Energy of  $^3_\Lambda\text{H}$  was extracted
  - $\sqrt{s_{NN}} = 3$  GeV data with higher statistics will be analyzed to improve precision of the measurements and measure correlations with heavier baryons

Thank you!

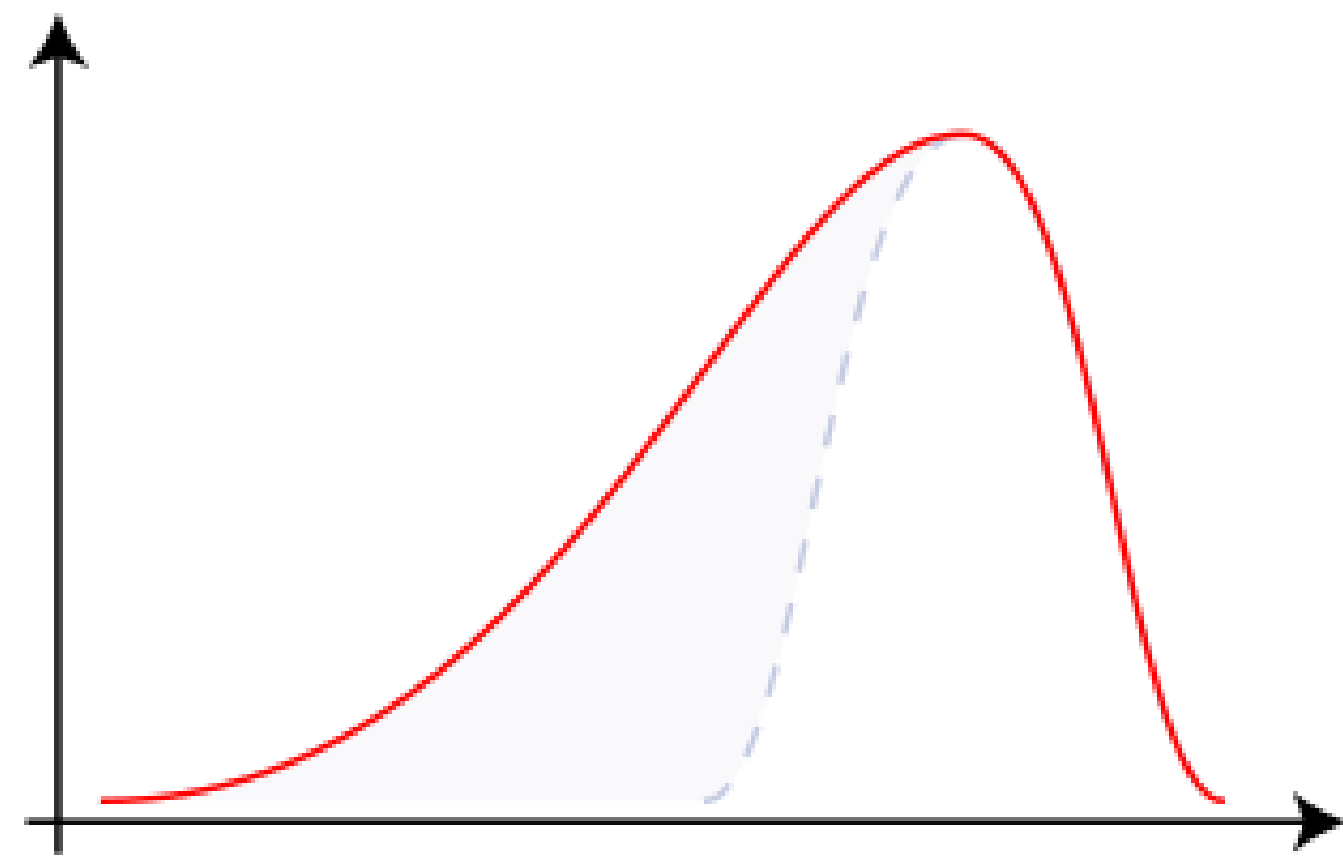
# Backup slides



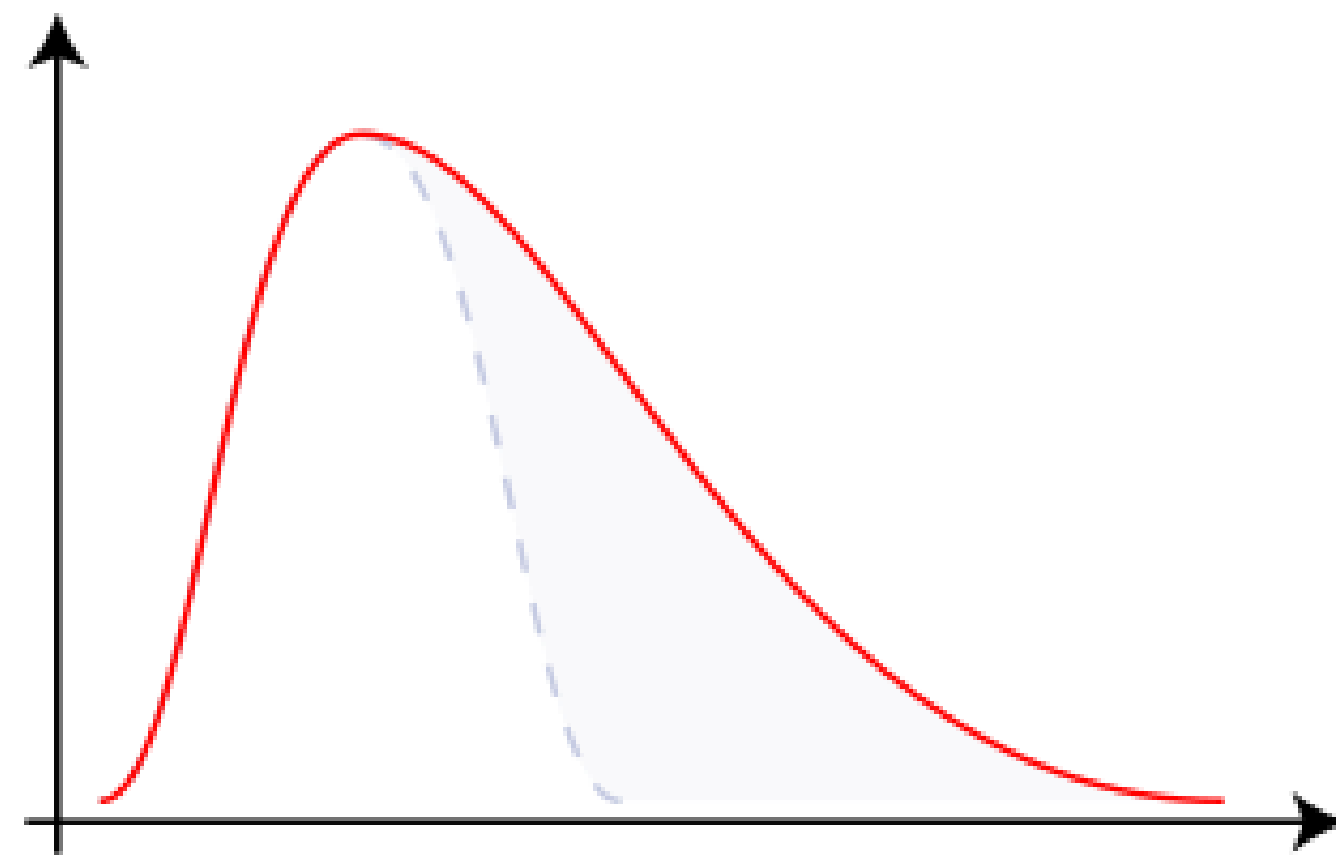
# STAR experiment

Au+Au Collisions at RHIC							
Collider Runs				Fixed-Target Runs			
Sl. no.	$\sqrt{s_{NN}}$ (GeV)	No. of collected events (millions)	$\mu_B$ (MeV)	Sl. no.	$\sqrt{s_{NN}}$ (GeV)	No. of collected events (millions)	$\mu_B$ (MeV)
1	200	380	25	1	13.7 (100)	50	280
2	62.4	46	75	2	11.5 (70)	50	316
3	54.4	1200	85	3	9.2 (44.5)	50	372
4	39	86	112	4	7.7 (31.2)	260	420
5	27	585	156	5	7.2 (26.5)	470	440
6	19.6	595	206	6	6.2 (19.5)	120	490
7	17.3	256	230	7	5.2 (13.5)	100	540
8	14.6	340	262	8	4.5 (9.8)	110	590
9	11.5	257	316	9	3.9 (7.3)	120	633
10	9.2	160	372	10	3.5 (5.75)	120	670
11	7.7	104	420	11	3.2 (4.59)	200	699
				12	3.0 (3.85)	260 + 2000	750

BES II

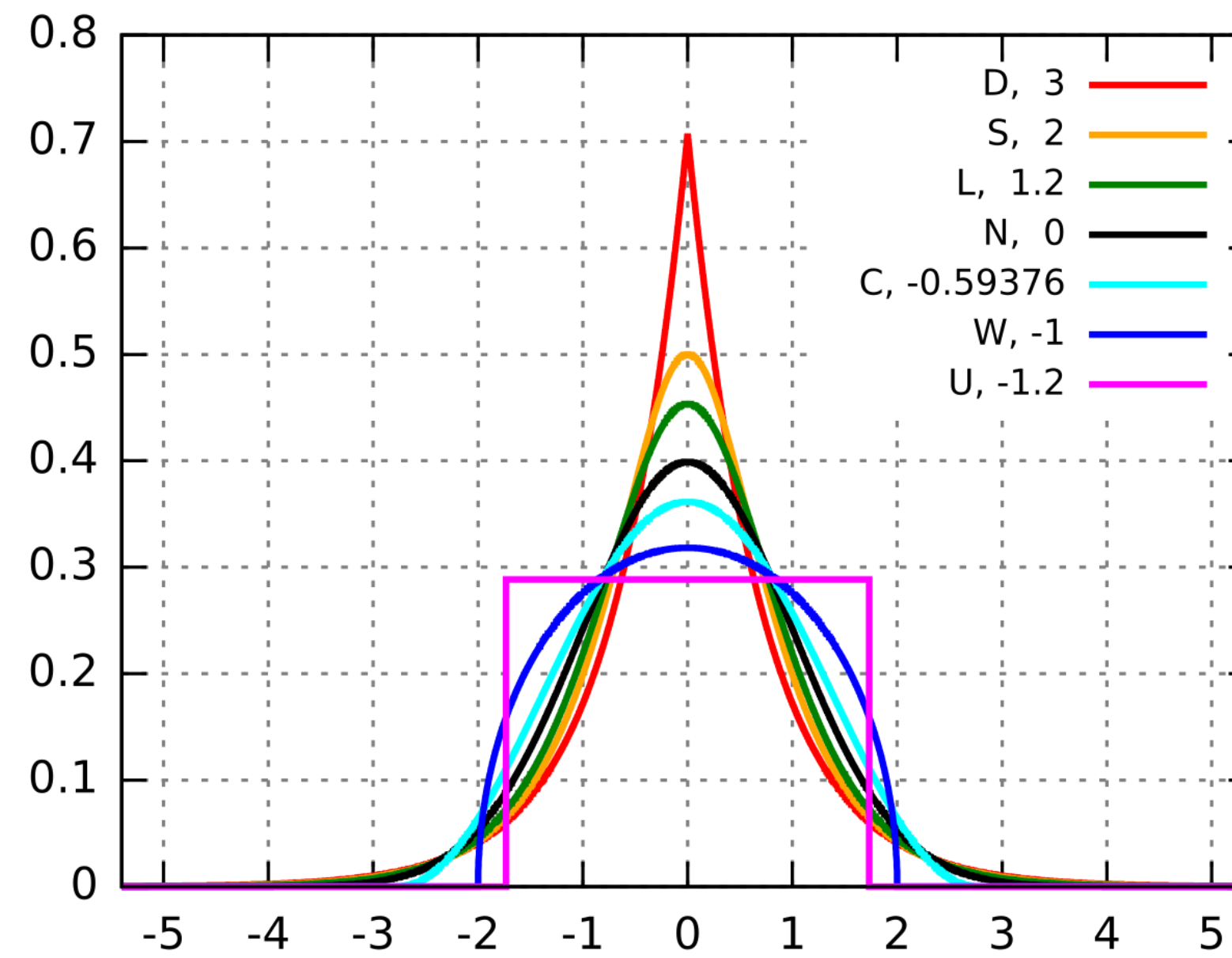


Negative skew



Positive skew

<https://en.wikipedia.org/wiki/Skewness>

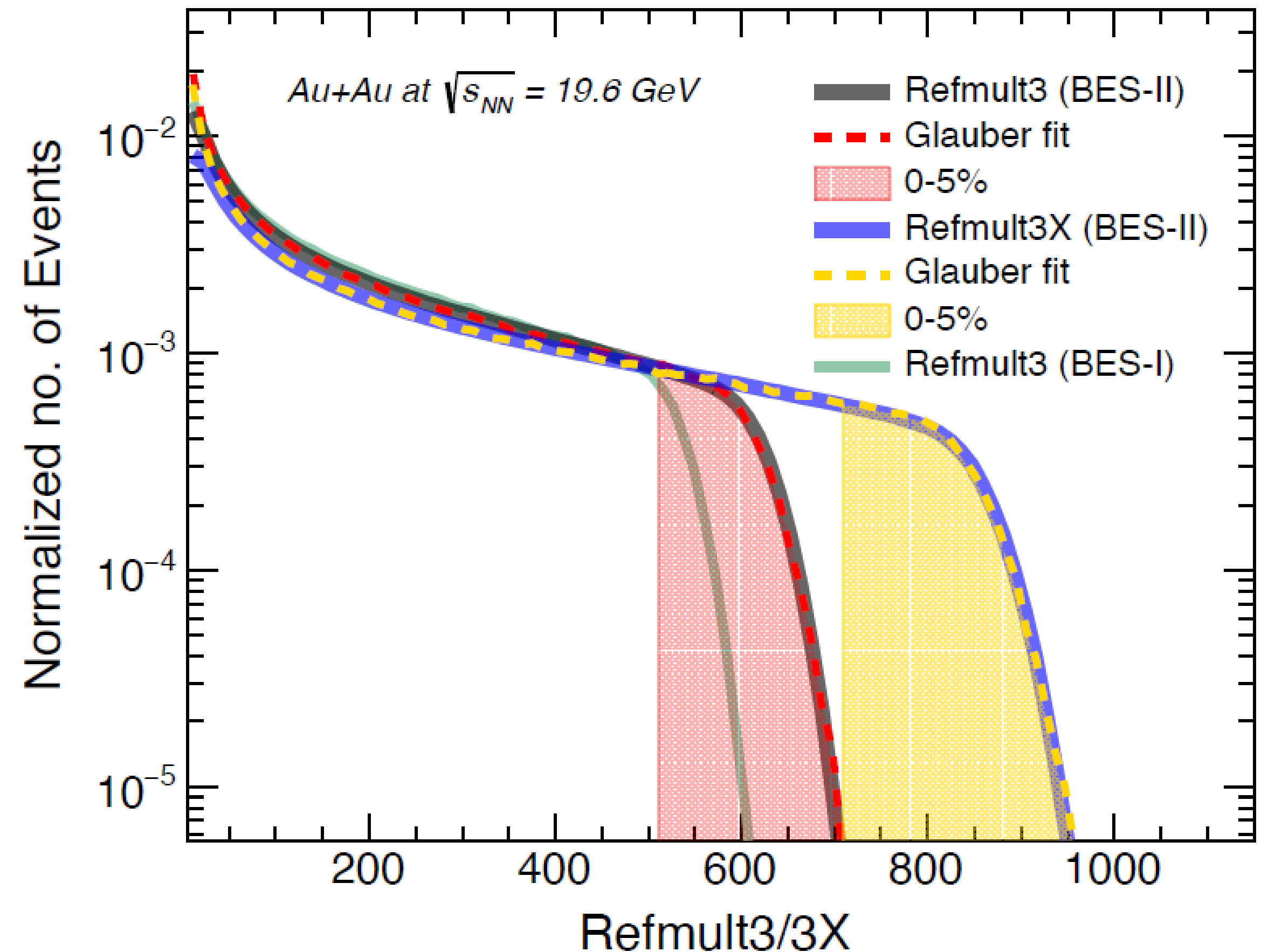


<https://en.wikipedia.org/wiki/Kurtosis>

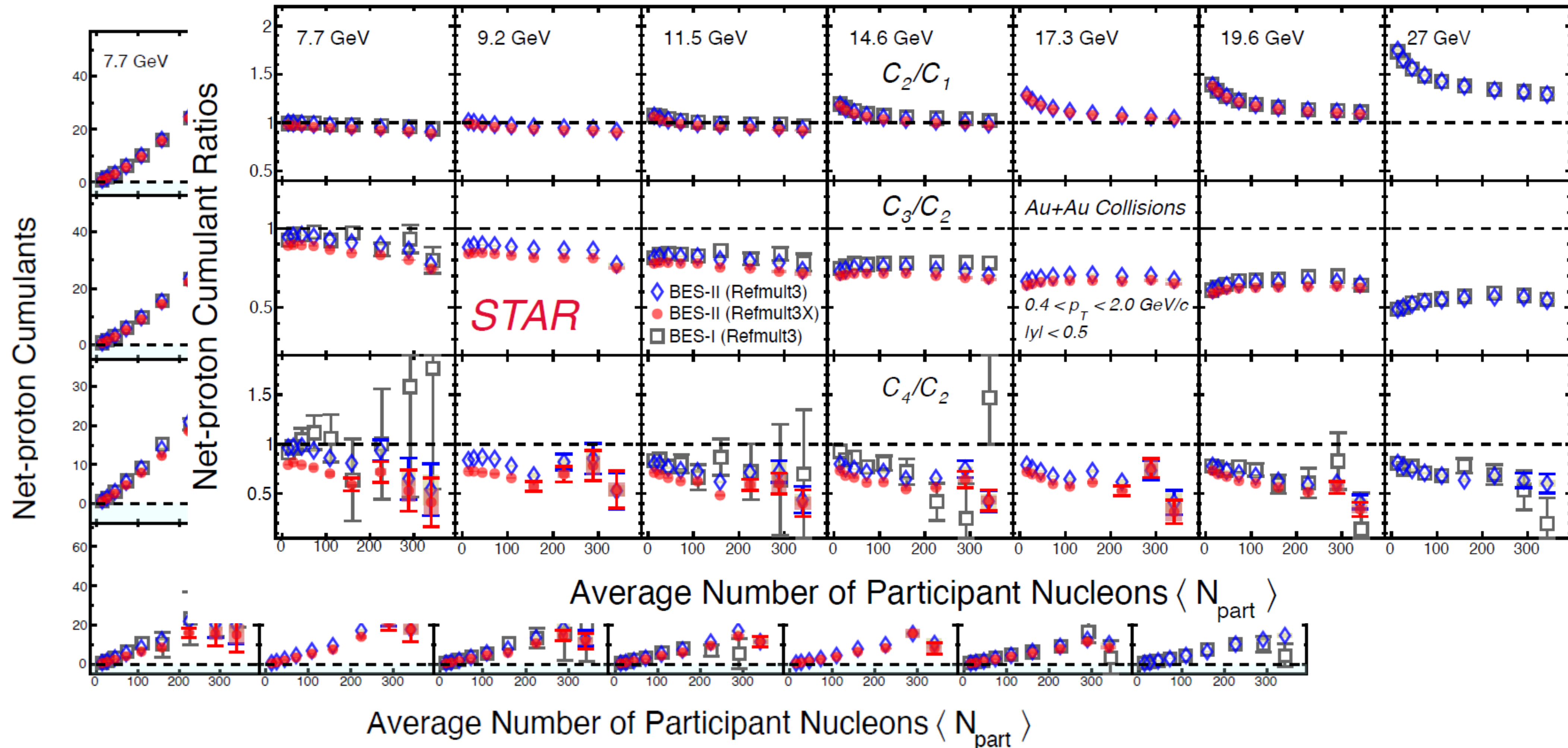
# Fluctuations (net-proton measurements)

Centrality definitions at STAR used to study fluctuations:

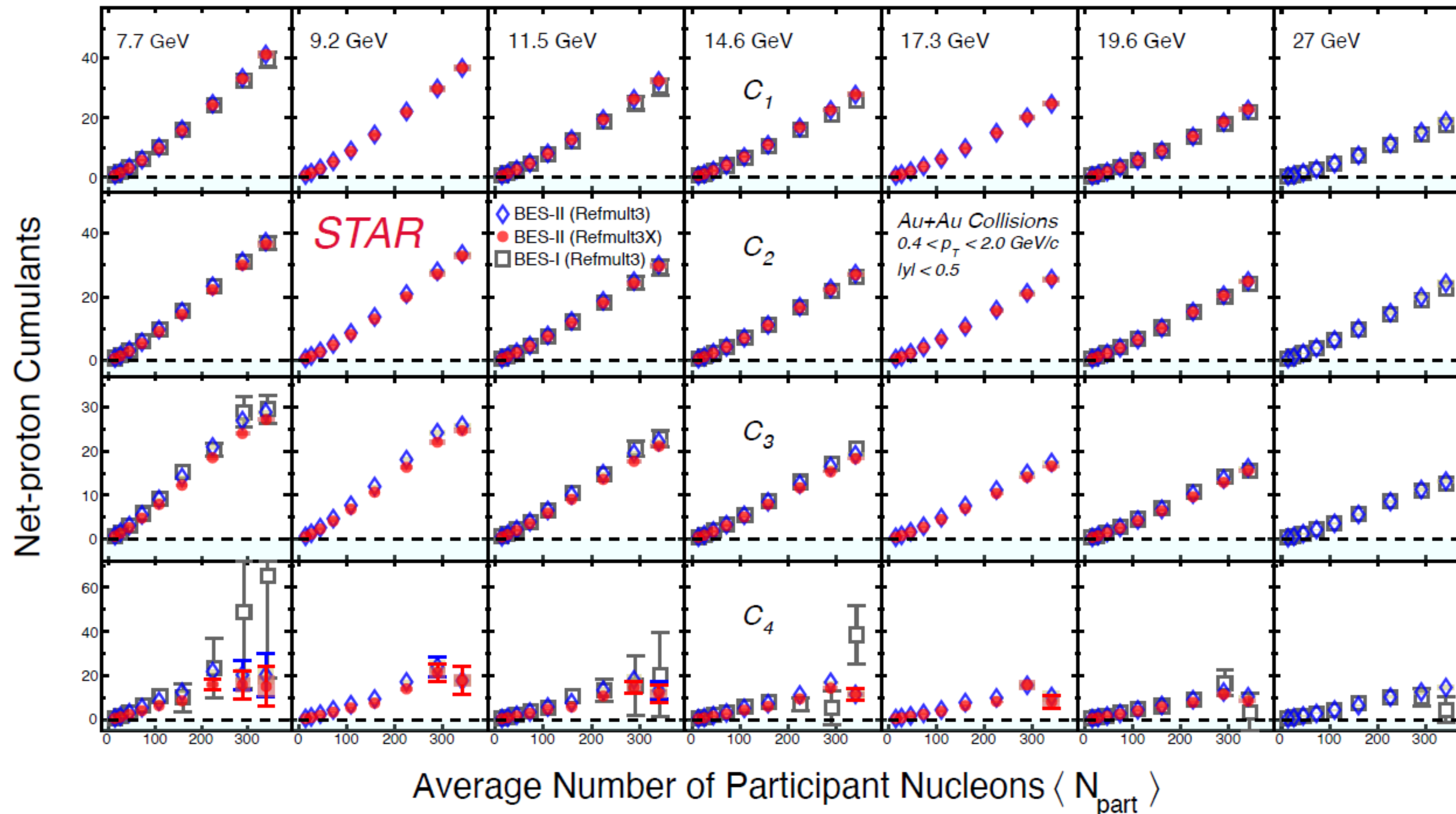
- Refmult3 = charged particle multiplicity (excluding protons to avoid autocorrelations)  $|\eta| < 1$
- Refmult3X -  $|\eta| < 1.6$  due to iTPC upgrade



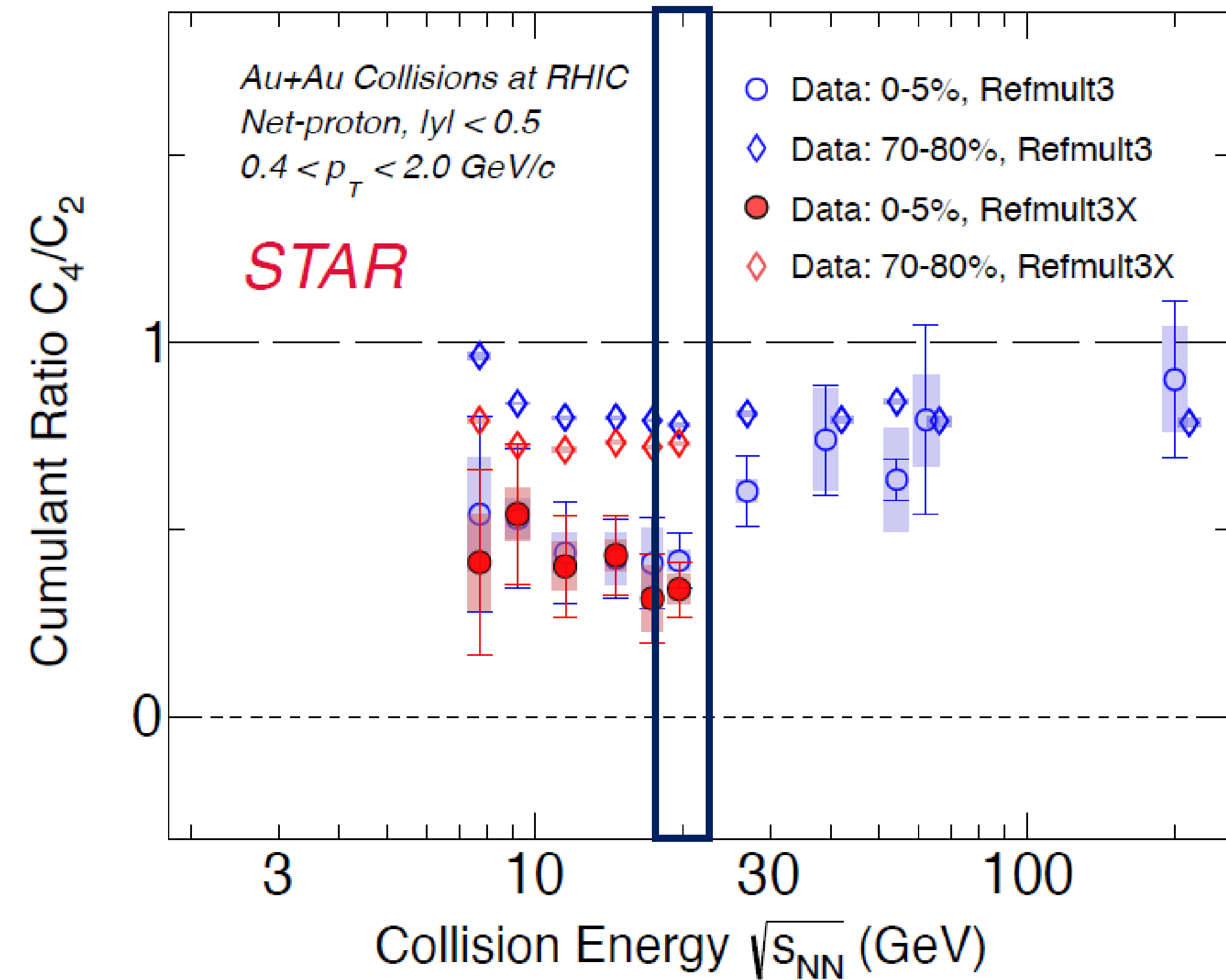
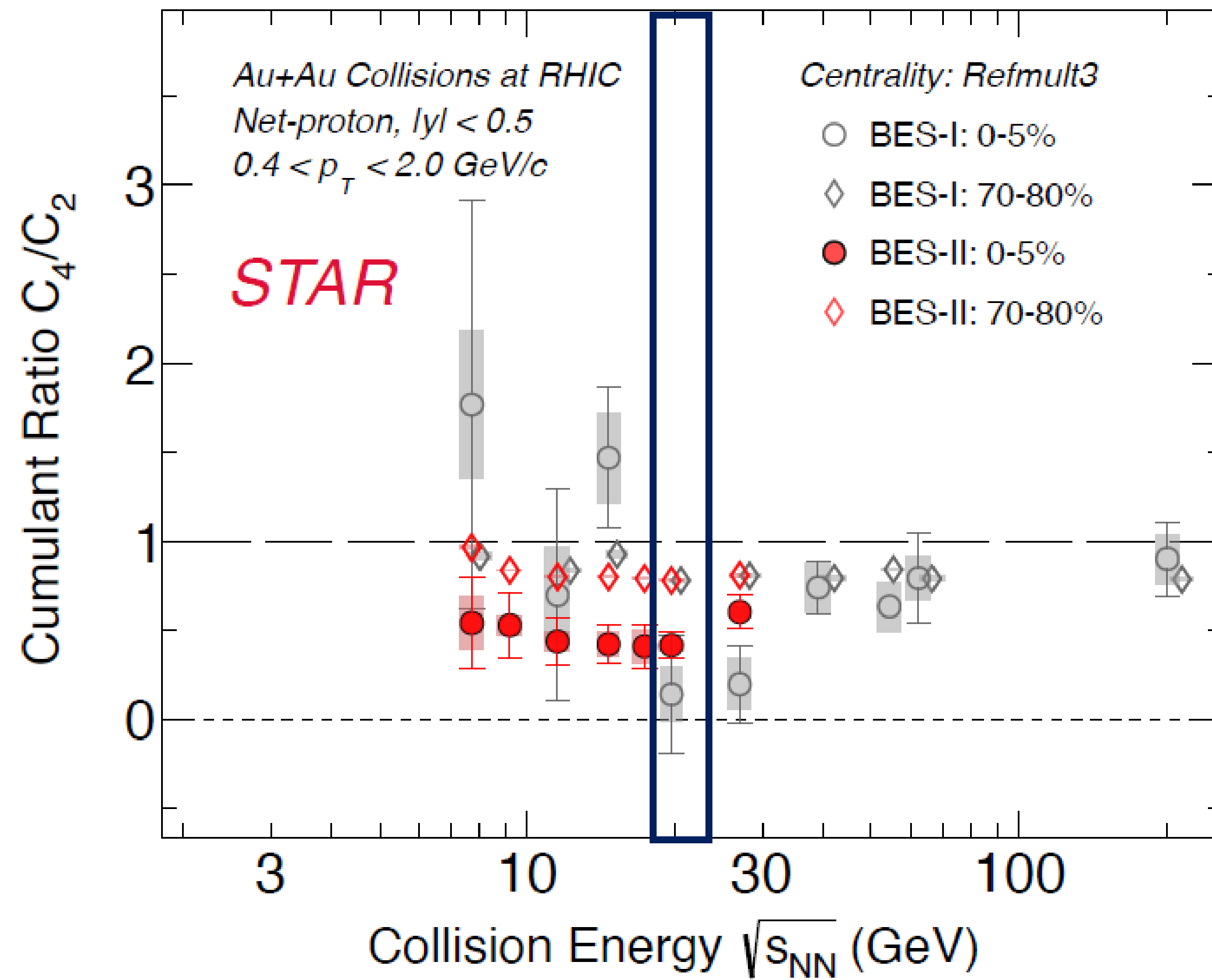
# Centrality dependence of cumulants (net-proton)

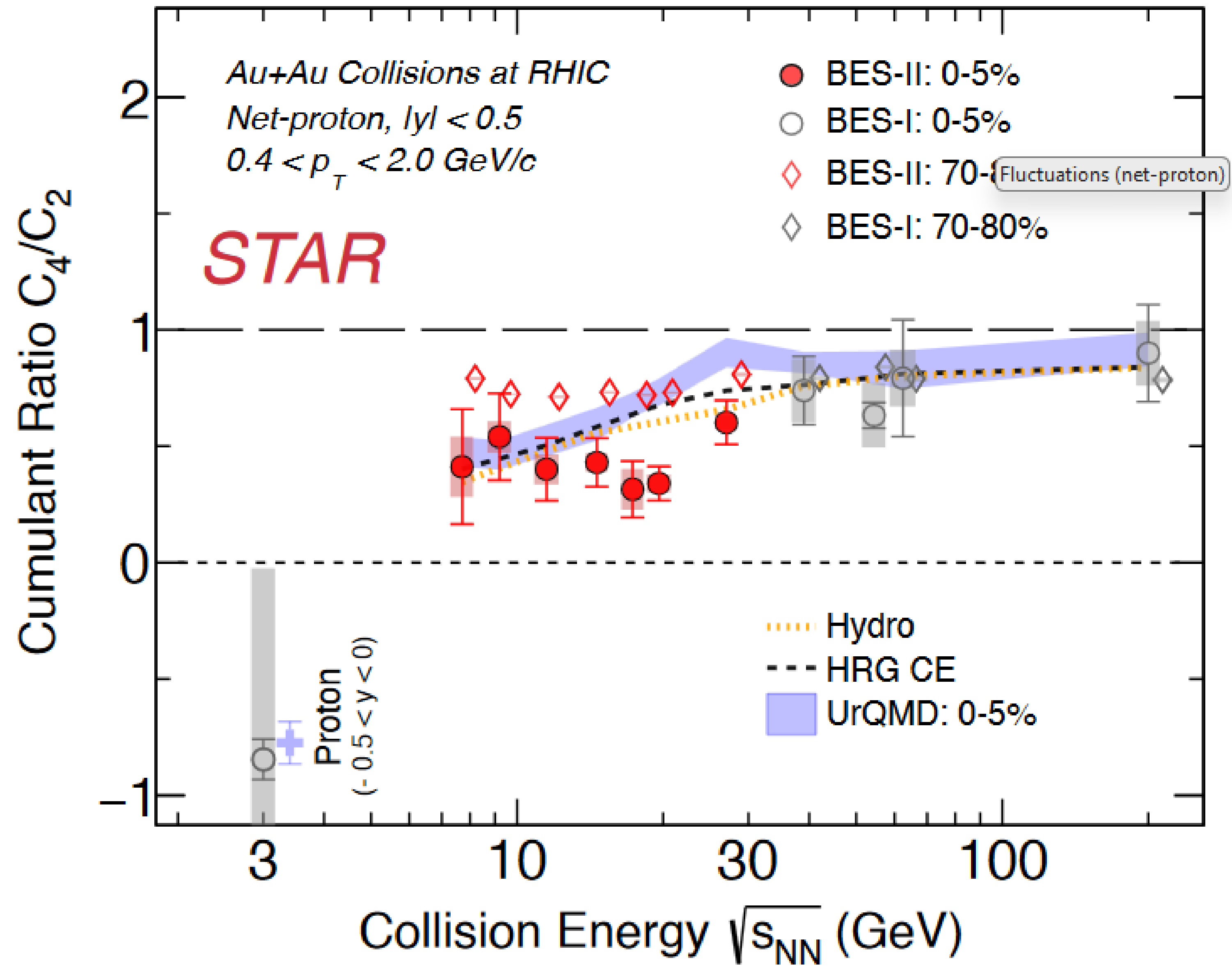


# Centrality dependence of cumulants (net-proton)



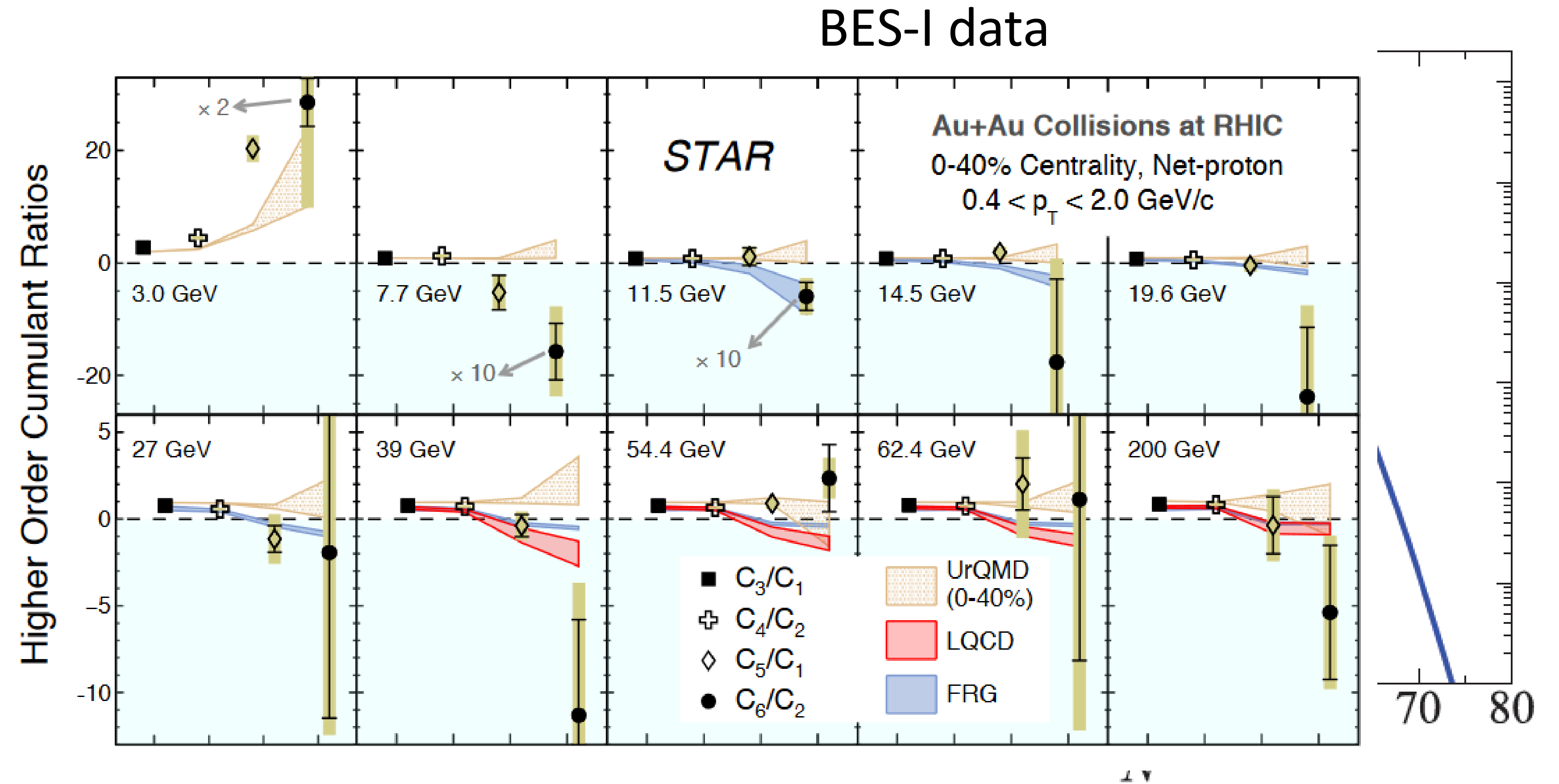
# Fluctuations (net-proton)





# Higher-order cumulants (n=5,6)

- 1st order PT
- mixed phase
- two phases
- two distributions
- higher order cumulant
- Analysis status: to be done

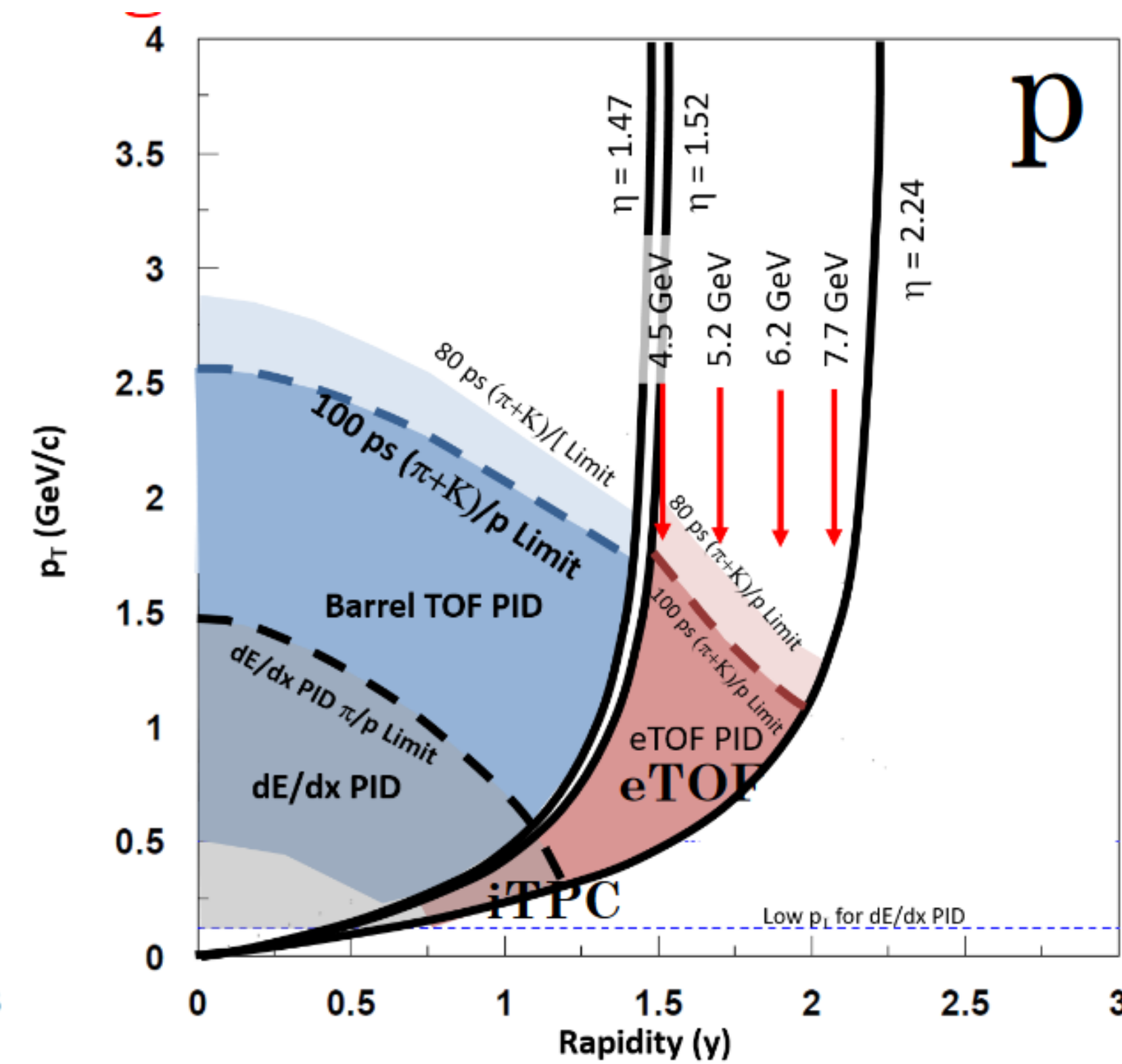
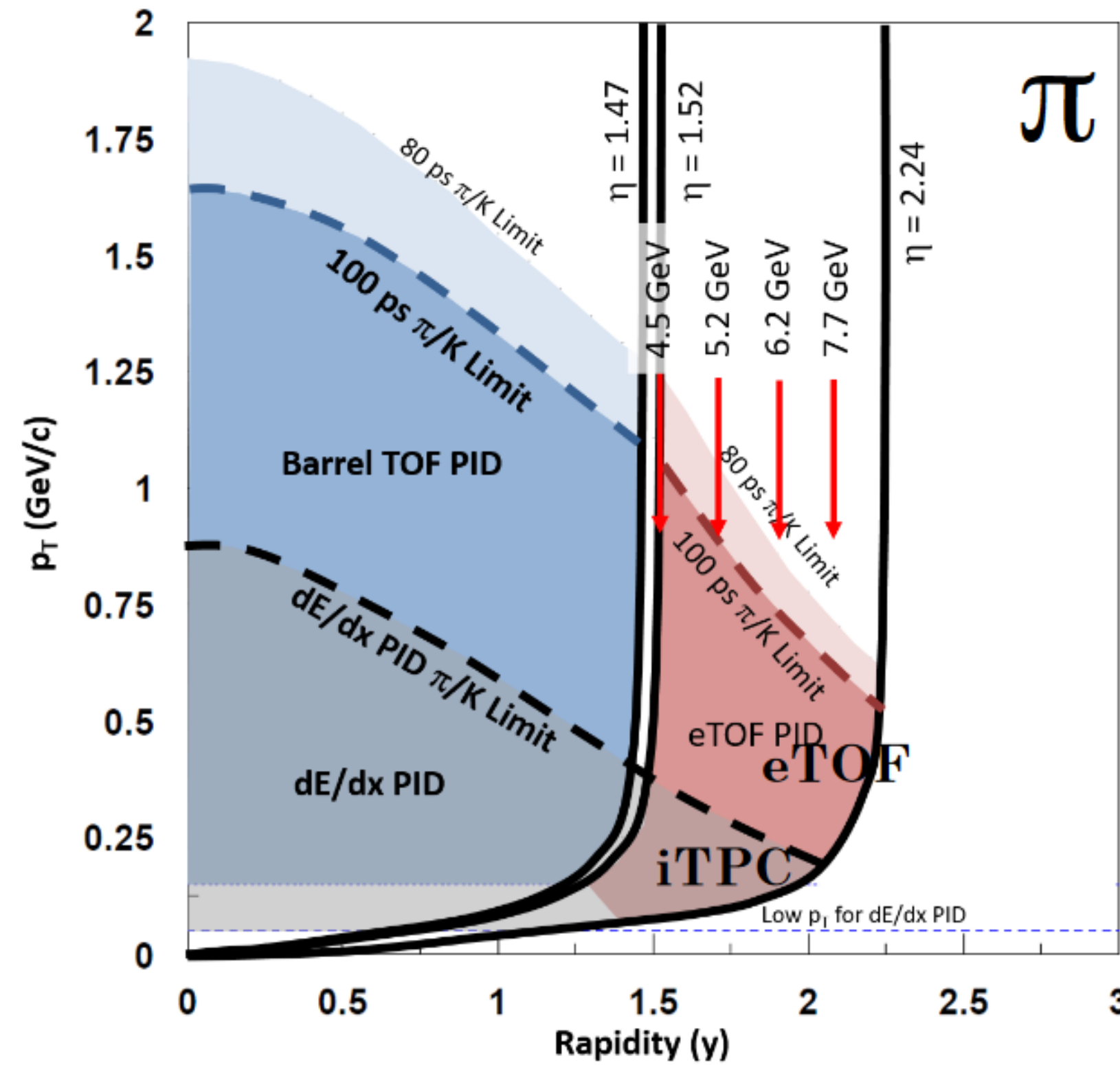


Beam Energy Dependence of Fifth and Sixth-Order Net-proton Number Fluctuations in Au+Au Collisions at RHIC- STAR Collaboration, 202



# Fluctuations

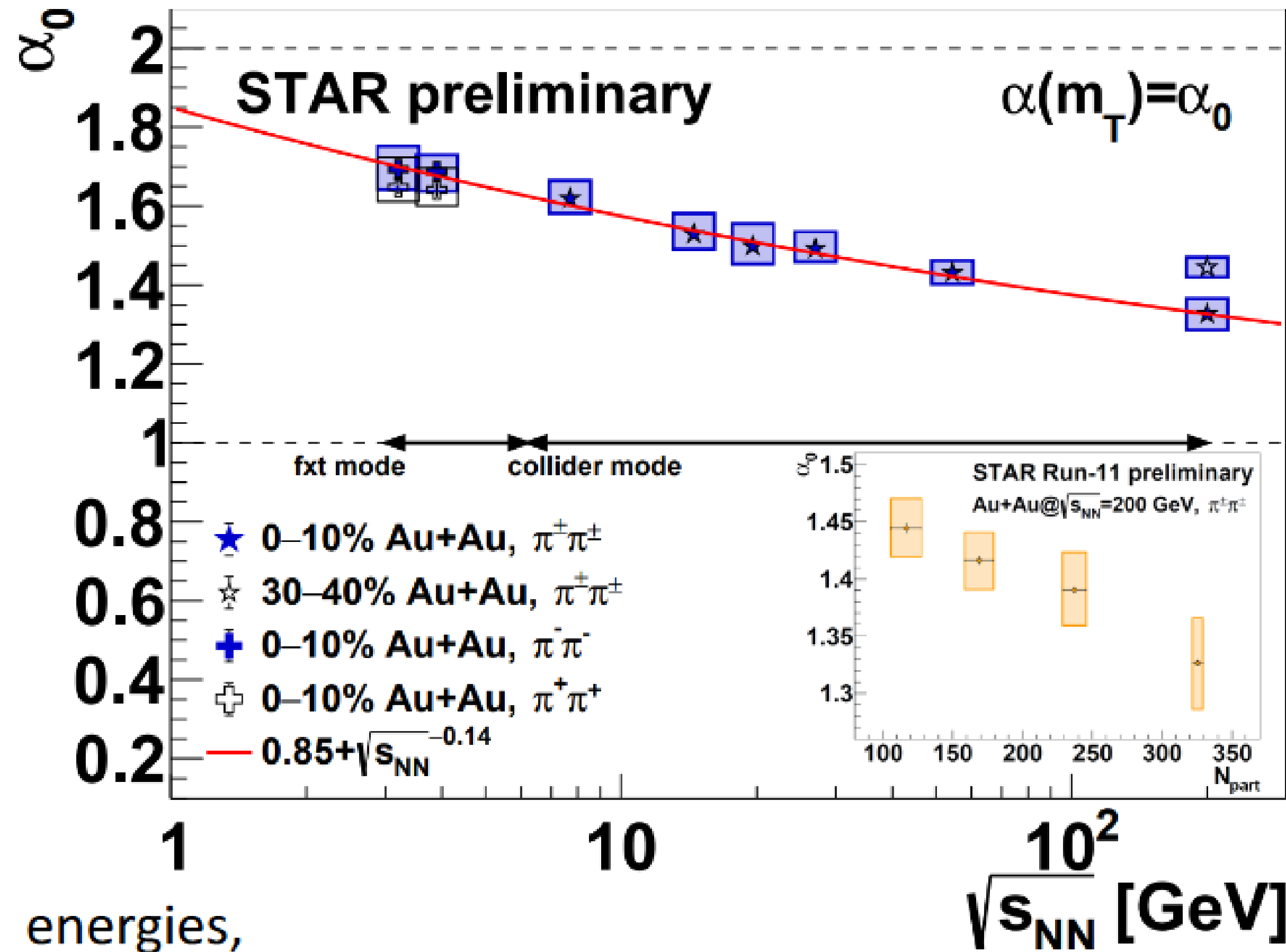
- BES-I – hint of possible non-monoton behavior of  $\kappa\sigma^2$
- BES-II :
  - Better statistic
  - Larger acceptance:
    - iTPC measurements of particles with lower  $p_T$  ( $125 \rightarrow 60$  MeV/c), extend rapidity coverage ( $|1| \rightarrow |1.6|$ )
    - eTOF PID measurements from  $\eta=1.1$  to 1.5
    - EPD – better reaction plane resolution, better event triggering



The STAR detector upgrade and future plan, Chi Yang for the STAR collaboration, 6th International Conference on New Frontiers in Physics (ICNFP2027)

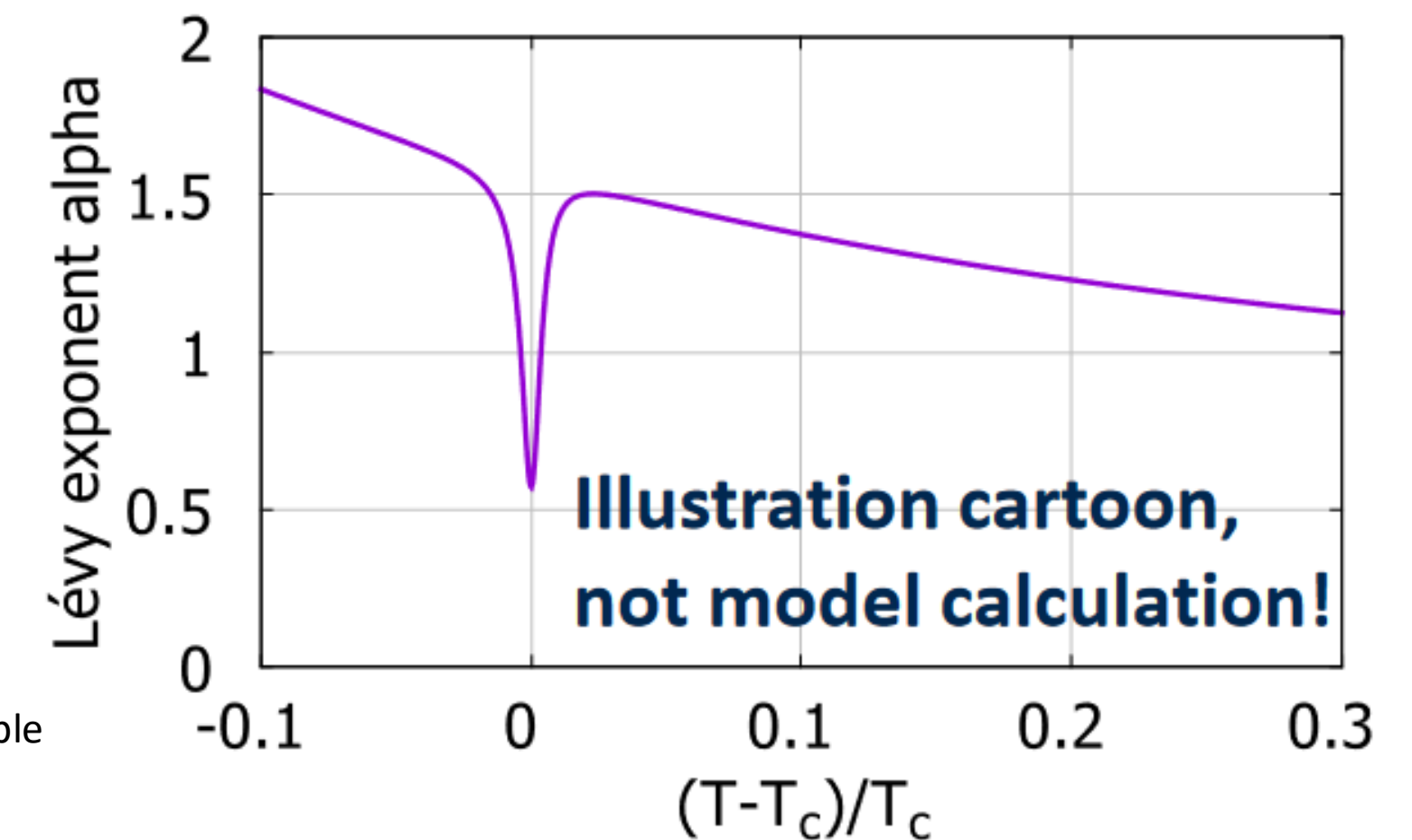
c

# EoS, Critical Point



- Study of the shape of the source (not only the size) - (Lévy parametrization):\*  

$$C(q) = 1 + \lambda e^{-|R_L q|^\alpha}$$
- $\alpha = 2 \rightarrow$  Gaussian source (standard parametrization)
- Strong decrease of  $\alpha$  near the CP suggested\*\* but not visible in analyzed data



Beam-Energy Dependent Pion Interferometry with Levy-Stable Sources at STAR, D. Kincses, CPOD 2024

\*\*Bose-Einstein correlations for Levy stable source distributions, T. Csorgo, S. Hegyi, W. A. Zajc, Eur.Phys.J. C36 (2004) 67-78

\* for clearance: neglected coulomb interaction

# Neutral kaons correlation functions:

$$C(q) = \lambda(e^{-q^2 R^2} + \frac{1 - \epsilon^2}{2} \left[ \left| \frac{f(k^*)}{R} \right|^2 + \frac{4\text{Re}(f(k^*))}{\sqrt{\pi}R} F_1(qR) + \frac{2\text{Im}(f(k^*))}{R} F_2(qR) \right]) \quad F_2(z) = \frac{1 - e^{-z^2}}{z}$$

\*R. Lednicky and V. L. Lyuboshits, Final State Interaction Effect on Pairing Correlations Between Particles with Small Relative Momenta, Yad. Fiz. 35 (1981) 1316, JINR-E2-81-453

$f(k^*)$  – scattering amplitude

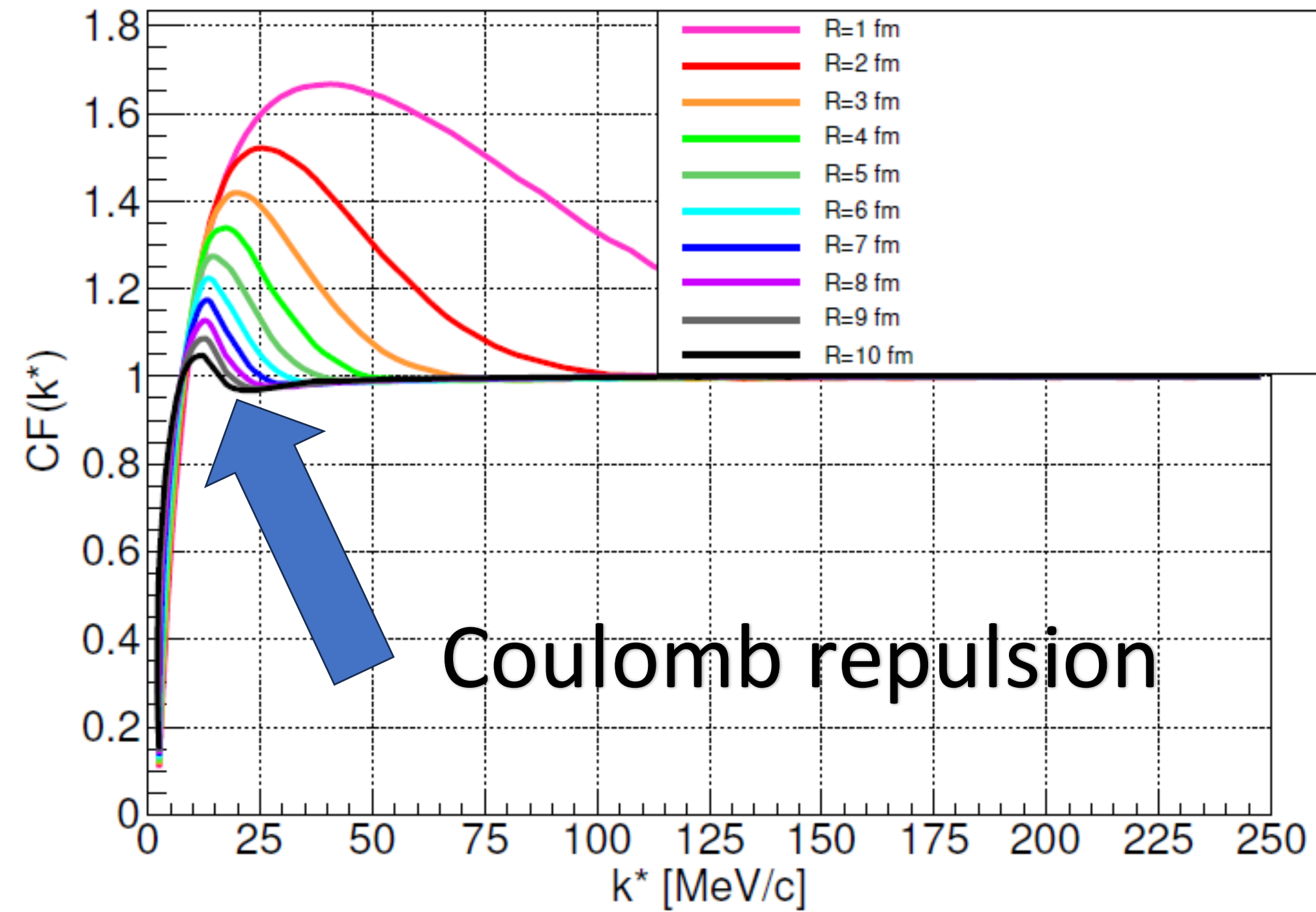
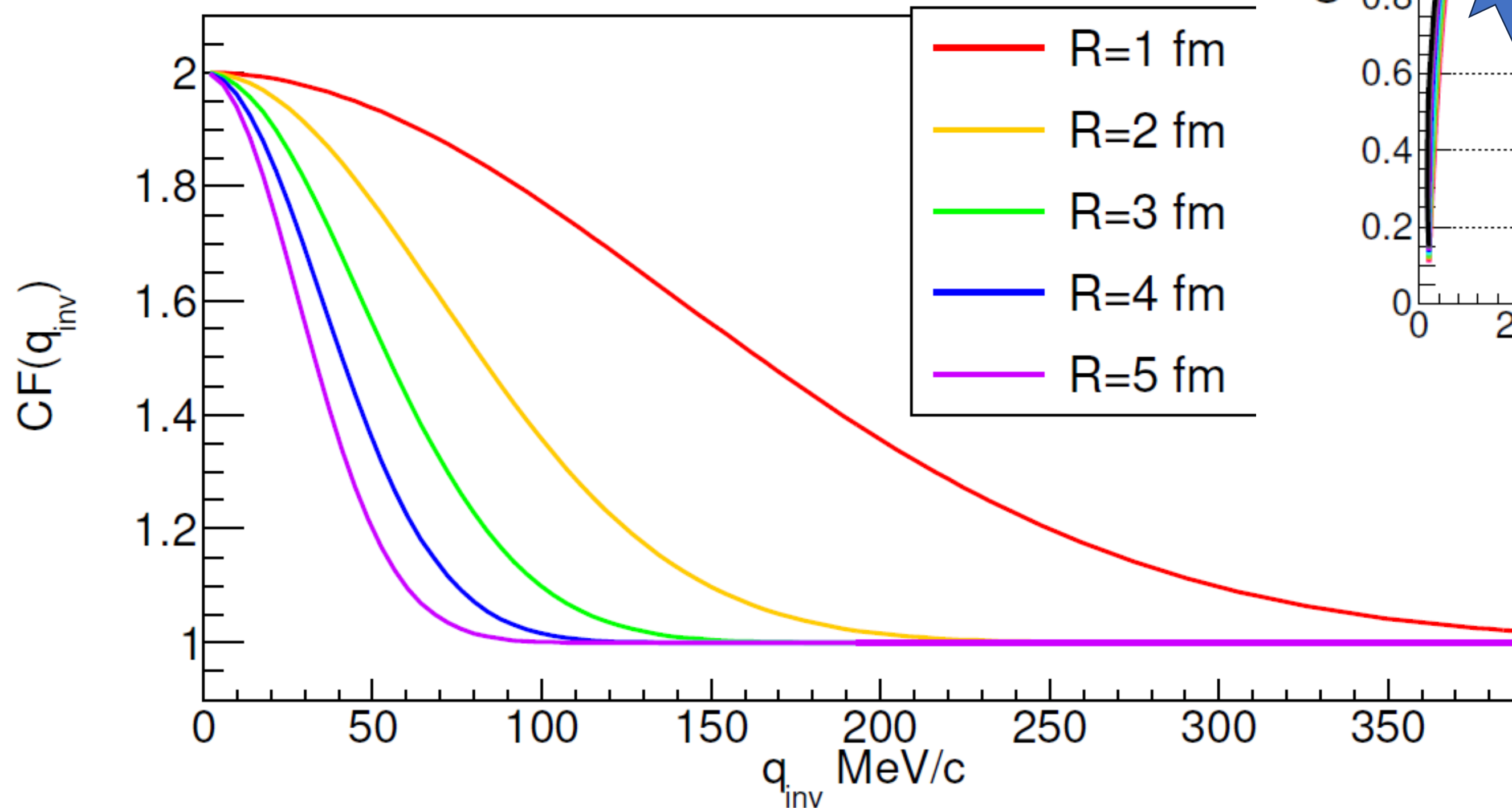
$R$  – size of source

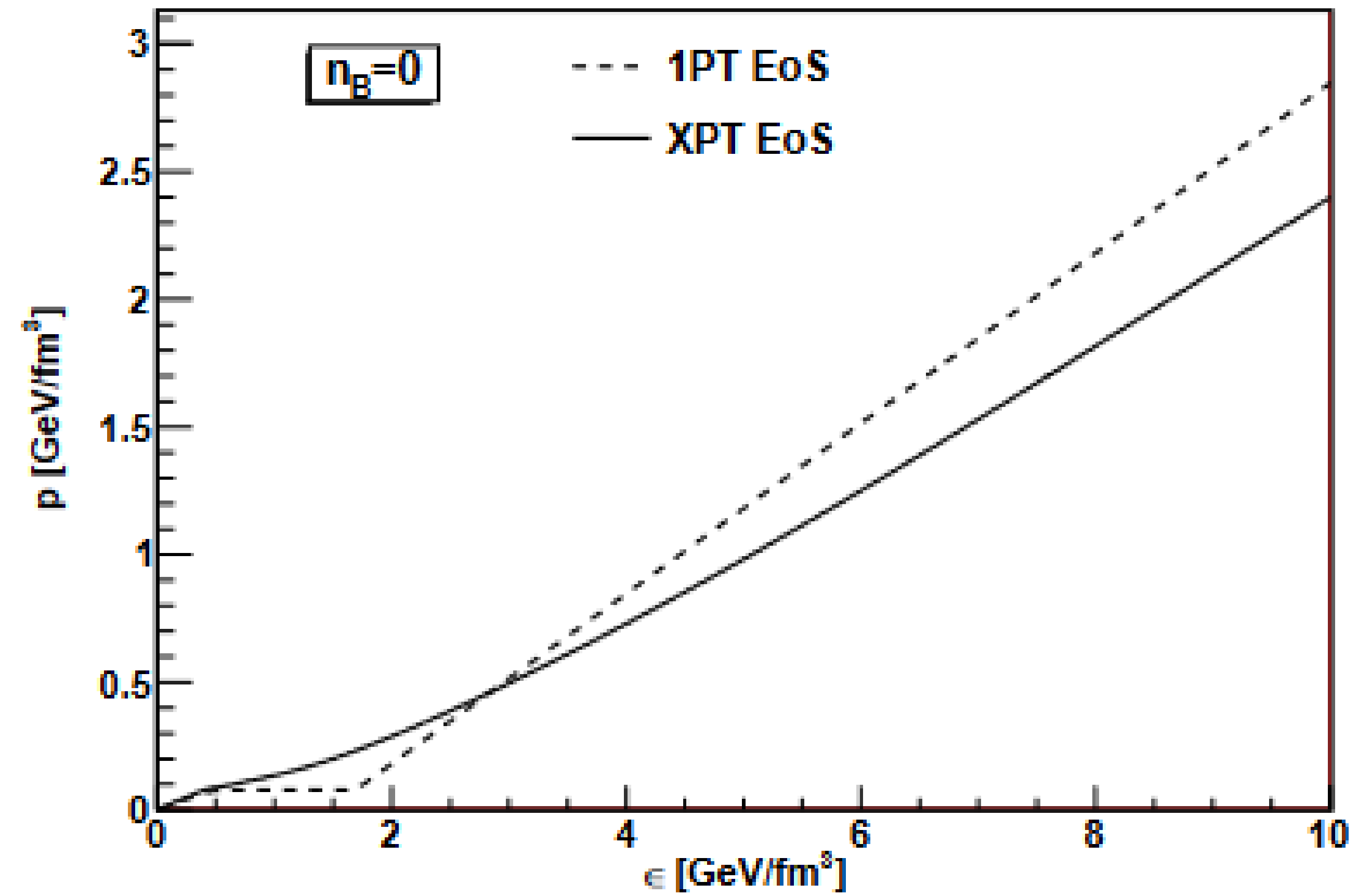
$\epsilon$  – asymmetry in kaon production (see next slides)

$q = 2k^* = p_1 - p_2$

$$F_1(z) = \int_0^z \frac{e^{x^2 - z^2}}{z} dx$$

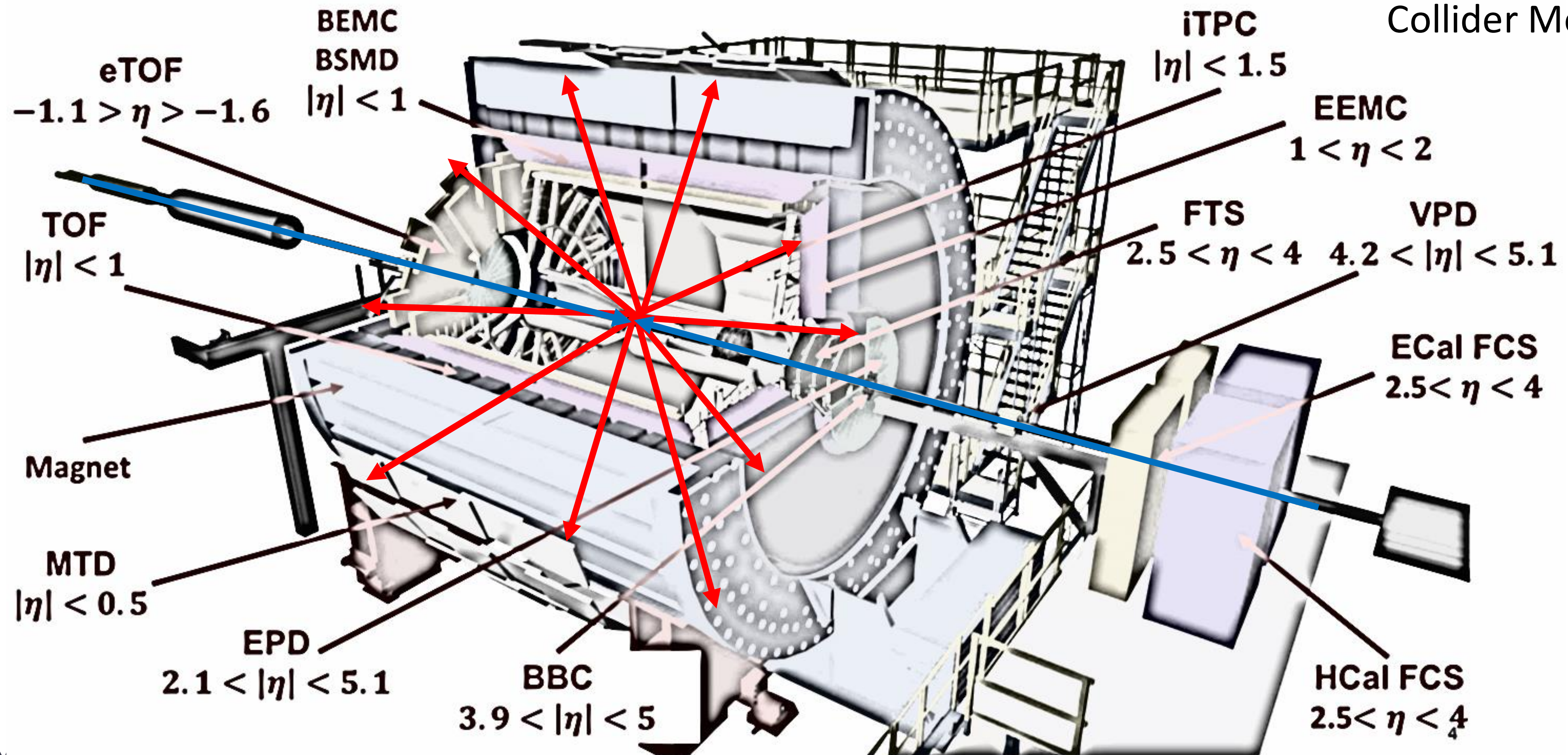
# Femtoscscopy



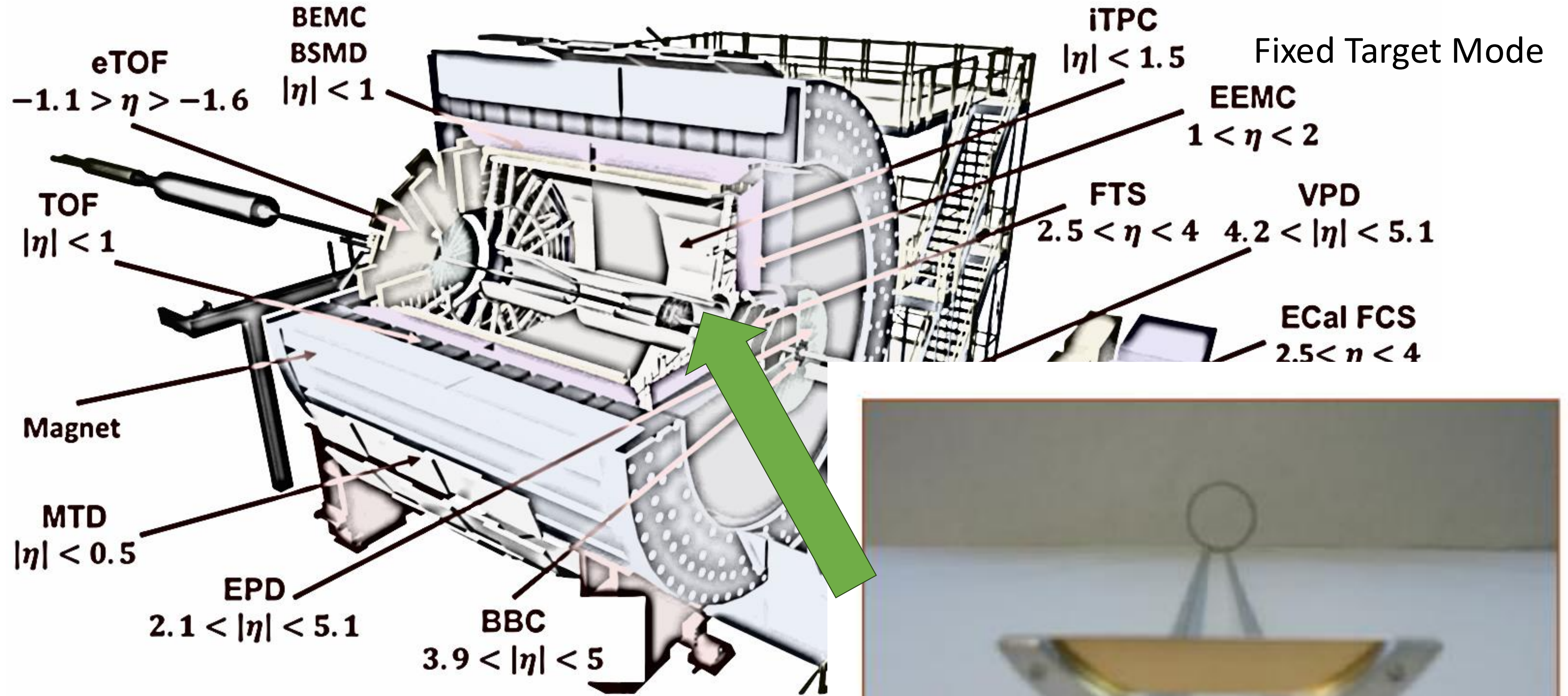


# STAR experiment

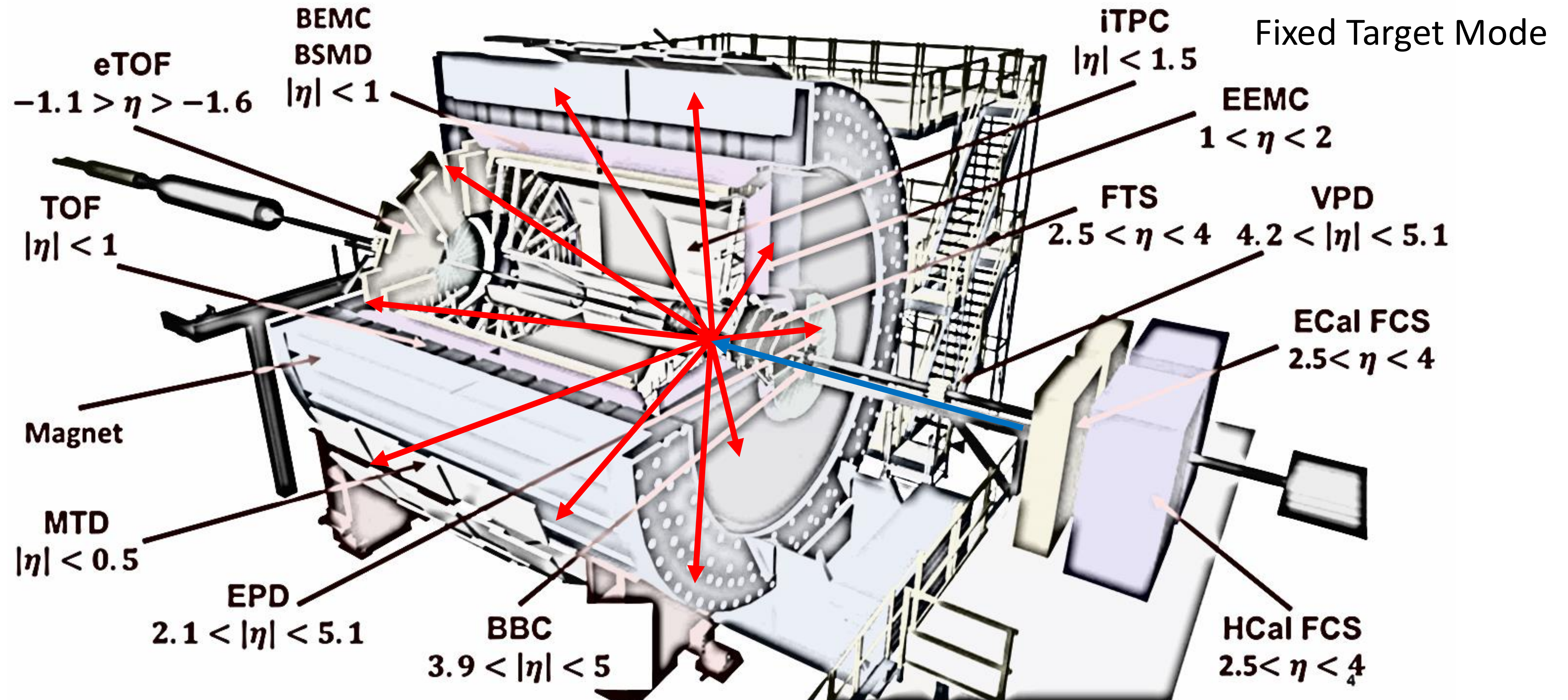
Original design:  
Collider Mode



# STAR experiment



# STAR experiment

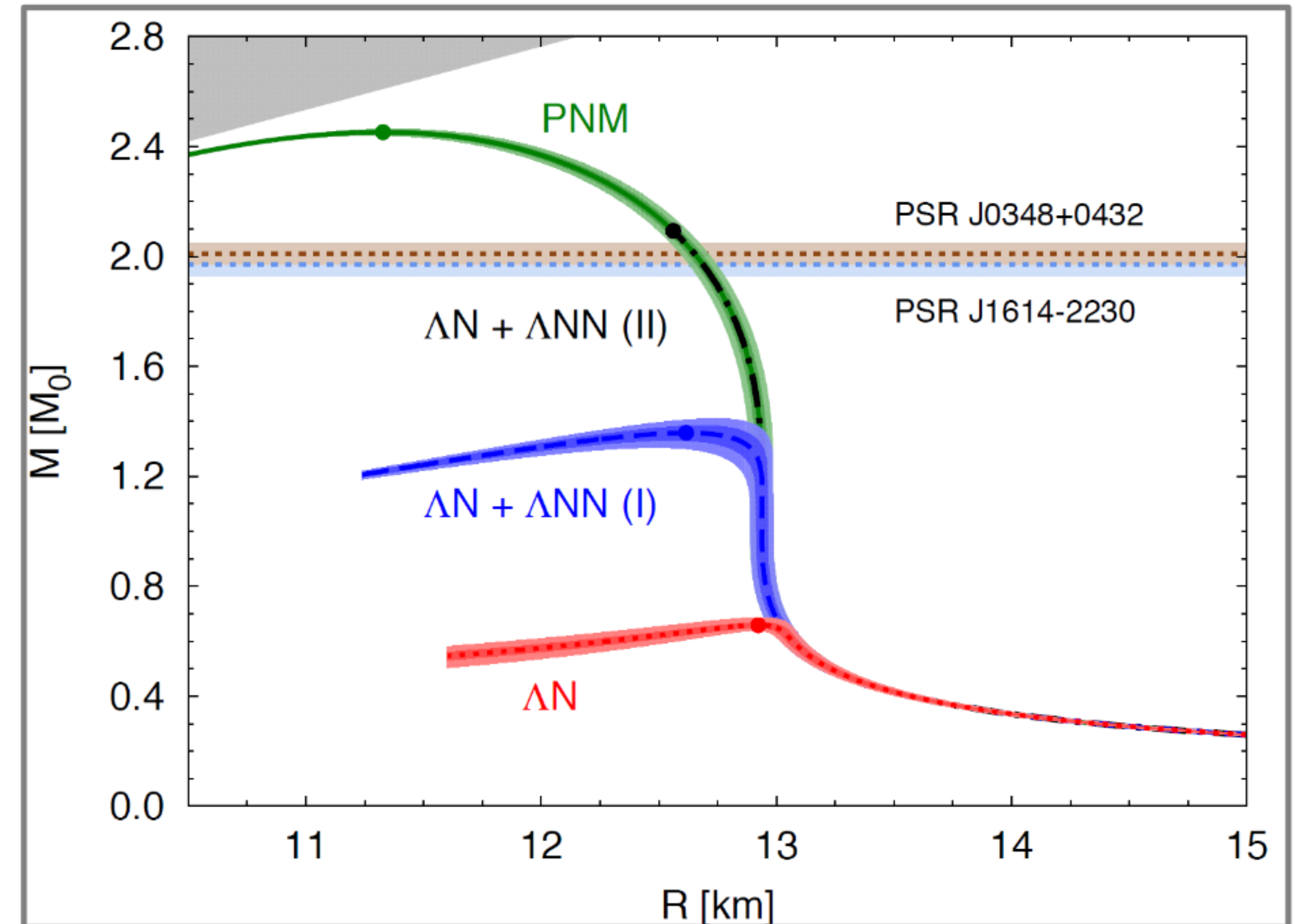




# Femtoscscopy

Probing interactions between particles:

- Protons, pions – possible to probe interactions by scattering experiments
- More exotic particles e.g., lambda, kaon –cannot produce a target/beam → **femtoscscopy!**
- Interactions:
  - Attractive or repulsive?
  - Probing bound states (if exists)
  - Probing EoS of matter → better understanding of neutron stars



D. Lonardoni, A. Lovato, S. Gandolfi, F. Pederiva Phys. Rev. Lett. 114, 092301 (2015)