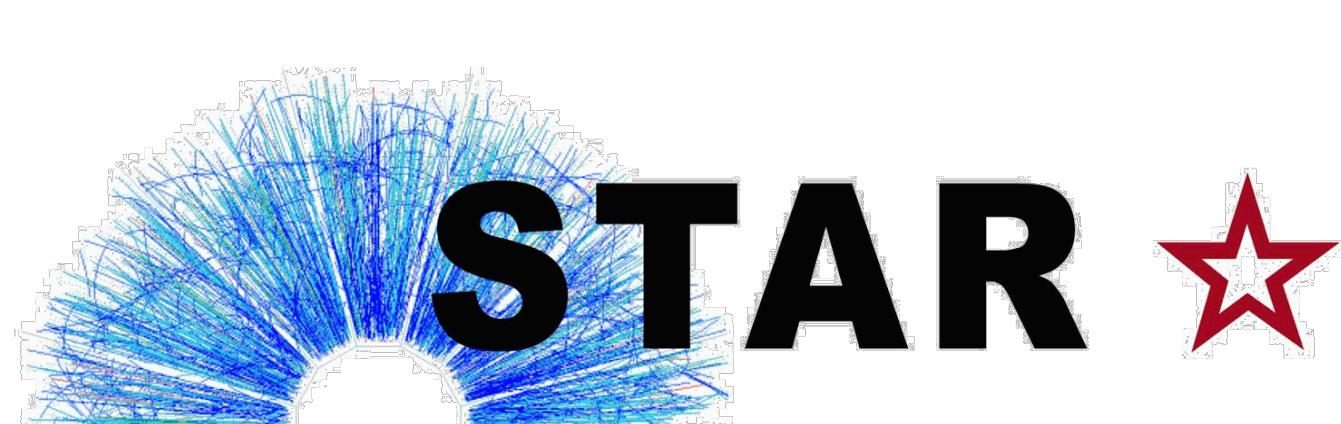
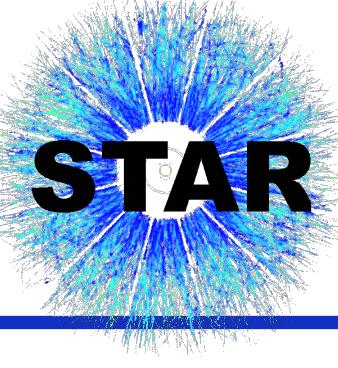


# **Measurement of the Sixth-Order Cumulant of Net-Particle Multiplicity Distributions at STAR**

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ATHIC2018, Hefei, China





# Outline

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## ✓ Introduction

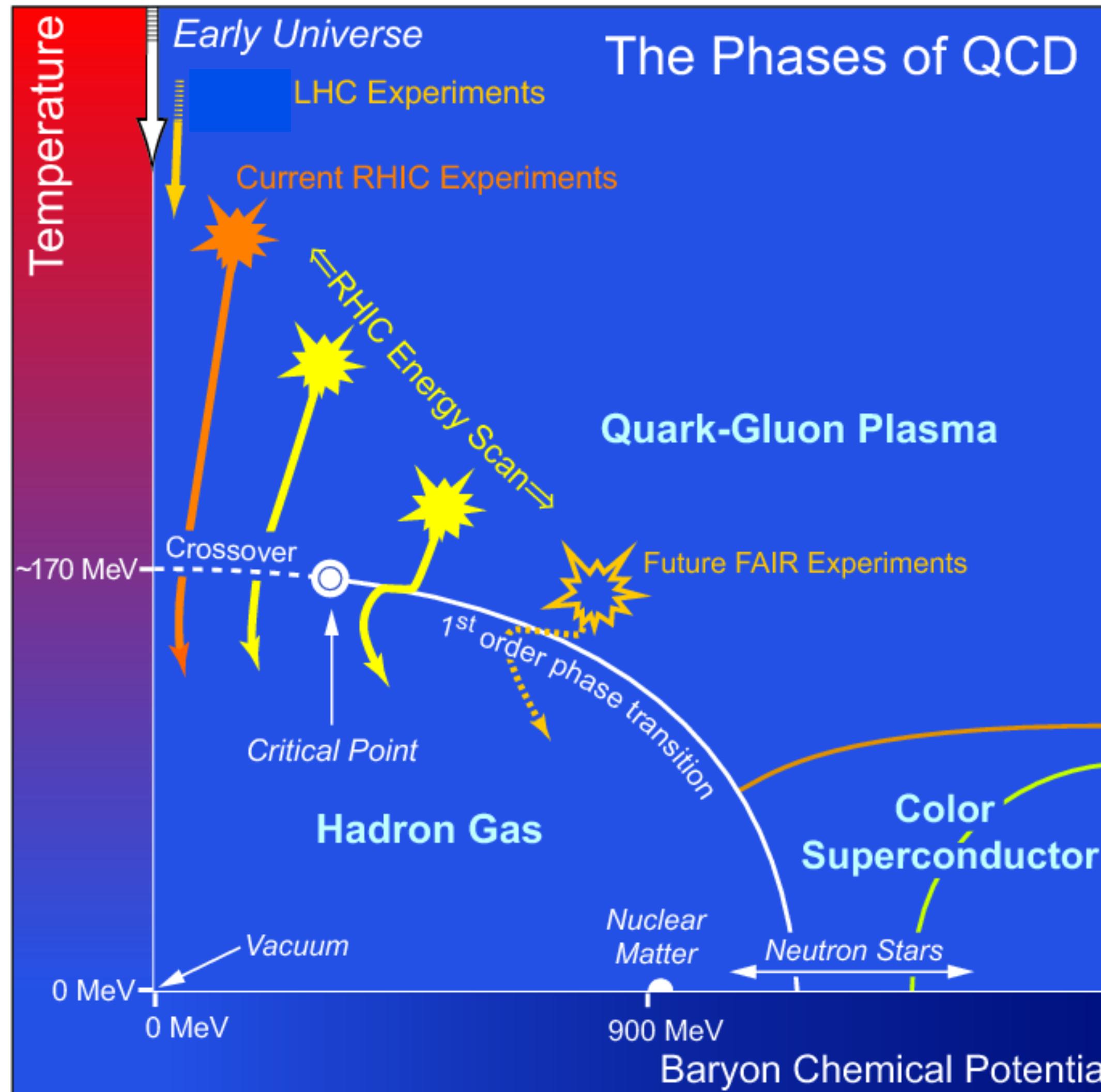
- Observables
- Analysis methods

## ✓ Experimental results

- Net-charge  $C_6/C_2$
- Net-proton  $C_6/C_2$

## ✓ Summary

# QCD phase diagram



✓ Higher-order fluctuations of net-particle distributions.

- **Crossover at  $\mu_B=0$**   
Y. Aoki, *Nature* 443, 675(2006)
- **1st-order phase transition at large  $\mu_B$ ?**
- **Critical point?**

# Fluctuations of conserved quantities

## ♦ Net-baryon, net-charge and net-strangeness

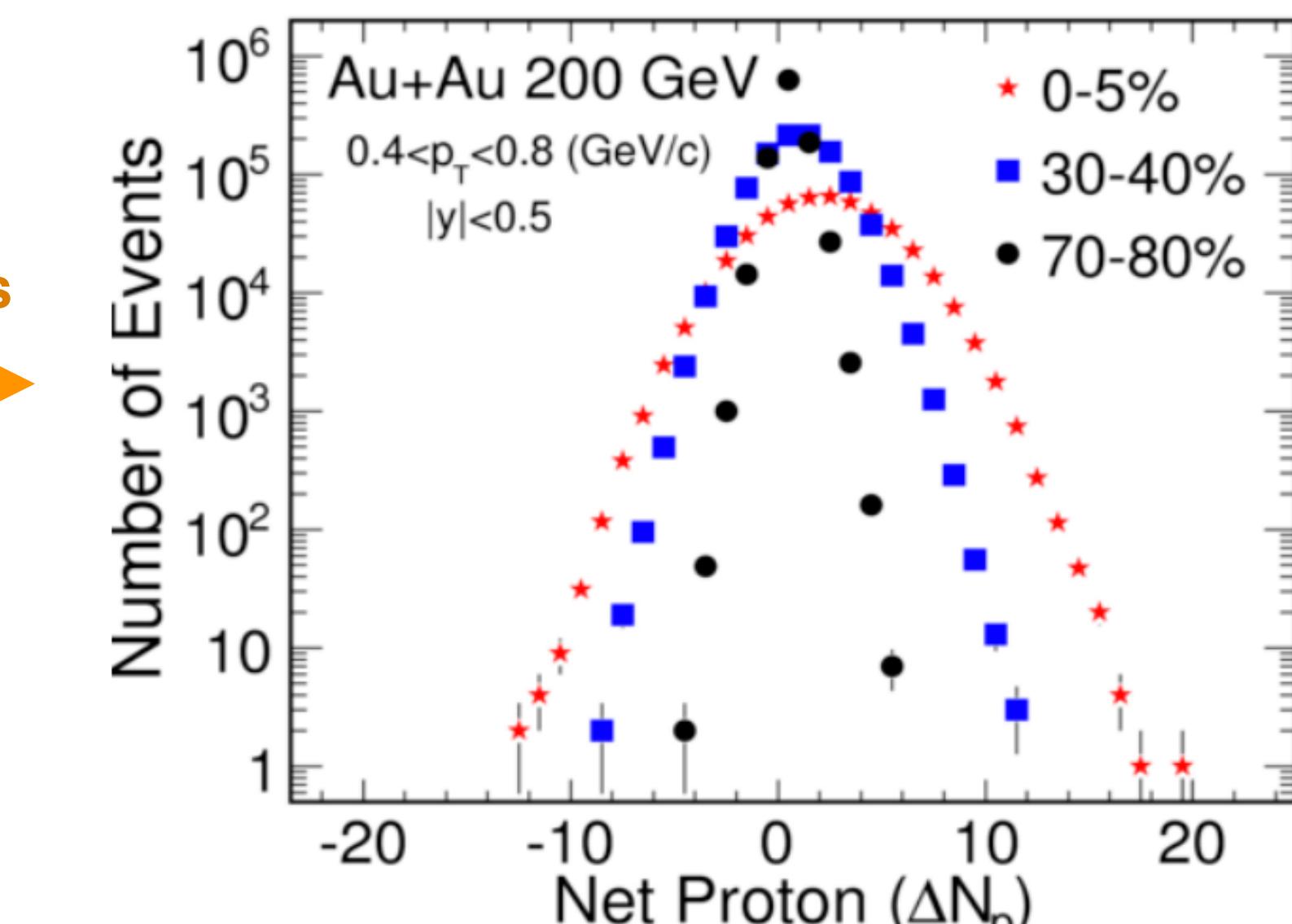
“Net” : positive - negative

$$\Delta N_q = N_q - N_{\bar{q}}, \quad q = B, Q, S$$

No. of positively charged particles in one collision

No. of negatively charged particles in one collision

Fill in histograms over many collisions



## (1) Sensitive to correlation length

$$C_2 = \langle (\delta N)^2 \rangle_c \approx \xi^2 \quad C_5 = \langle (\delta N)^5 \rangle_c \approx \xi^{9.5}$$

$$C_3 = \langle (\delta N)^3 \rangle_c \approx \xi^{4.5} \quad C_6 = \langle (\delta N)^6 \rangle_c \approx \xi^{12}$$

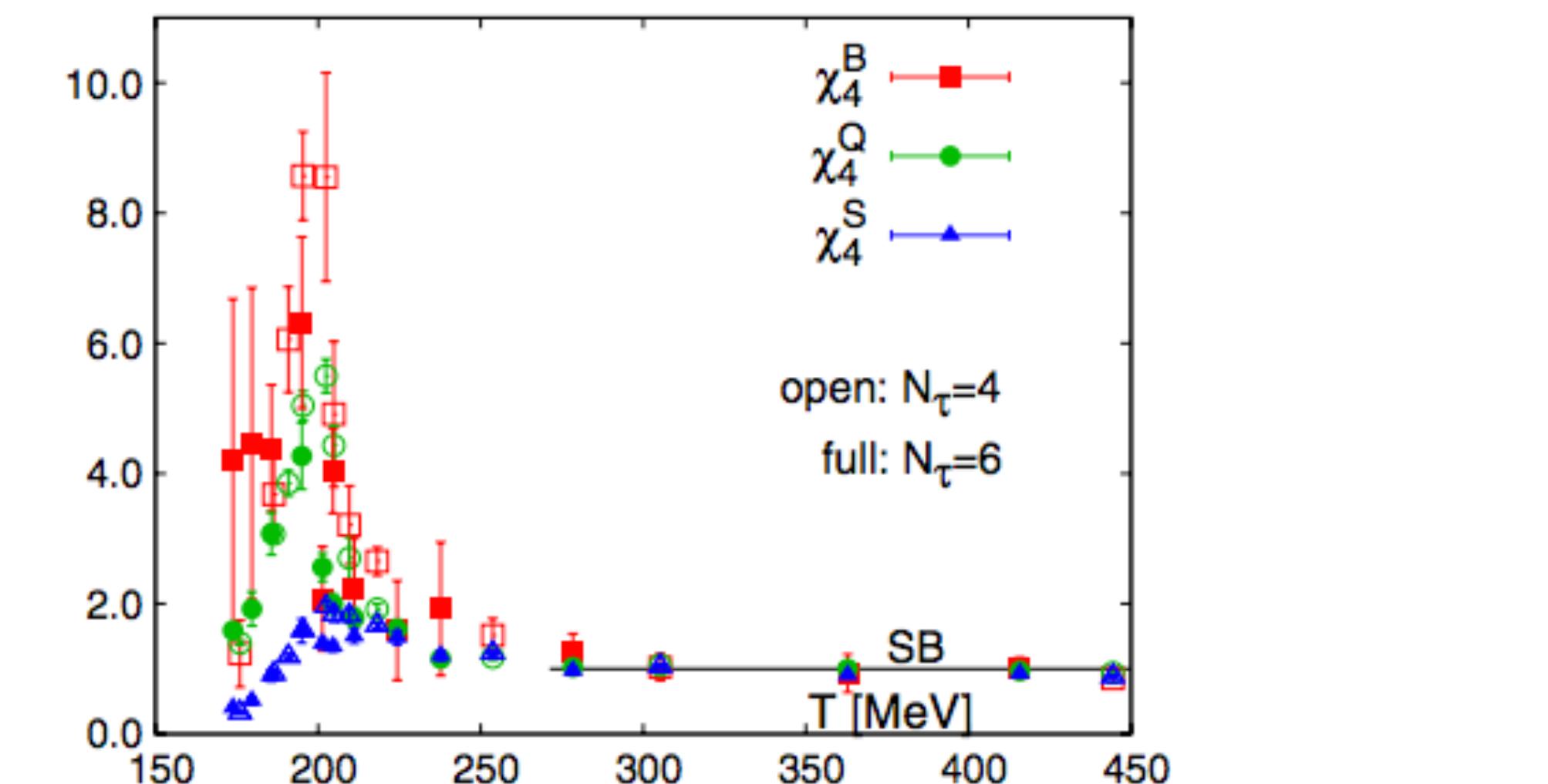
$$C_4 = \langle (\delta N)^4 \rangle_c \approx \xi^7$$

## (2) Direct comparison with susceptibilities.

$$S\sigma = \frac{C_3}{C_2} = \frac{\chi_3}{\chi_2} \quad \kappa\sigma^2 = \frac{C_4}{C_2} = \frac{\chi_4}{\chi_2} \quad \frac{C_6}{C_2} = \frac{\chi_6}{\chi_2}$$

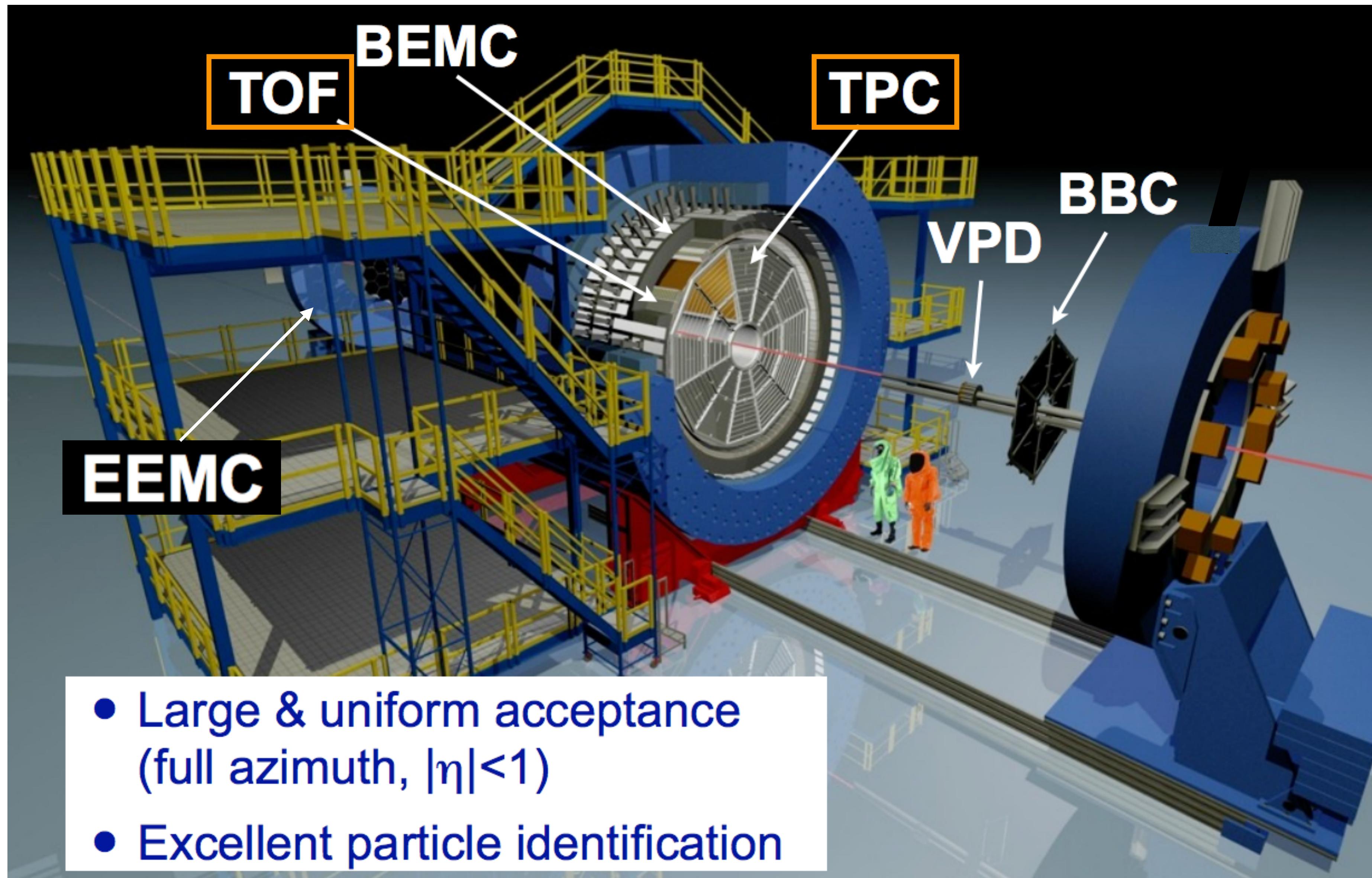
$$\chi_n^q = \frac{1}{VT^3} \times C_n^q = \frac{\partial^n p/T^4}{\partial \mu_q^n}, \quad q = B, Q, S$$

Volume dependence can be canceled by taking the ratio.



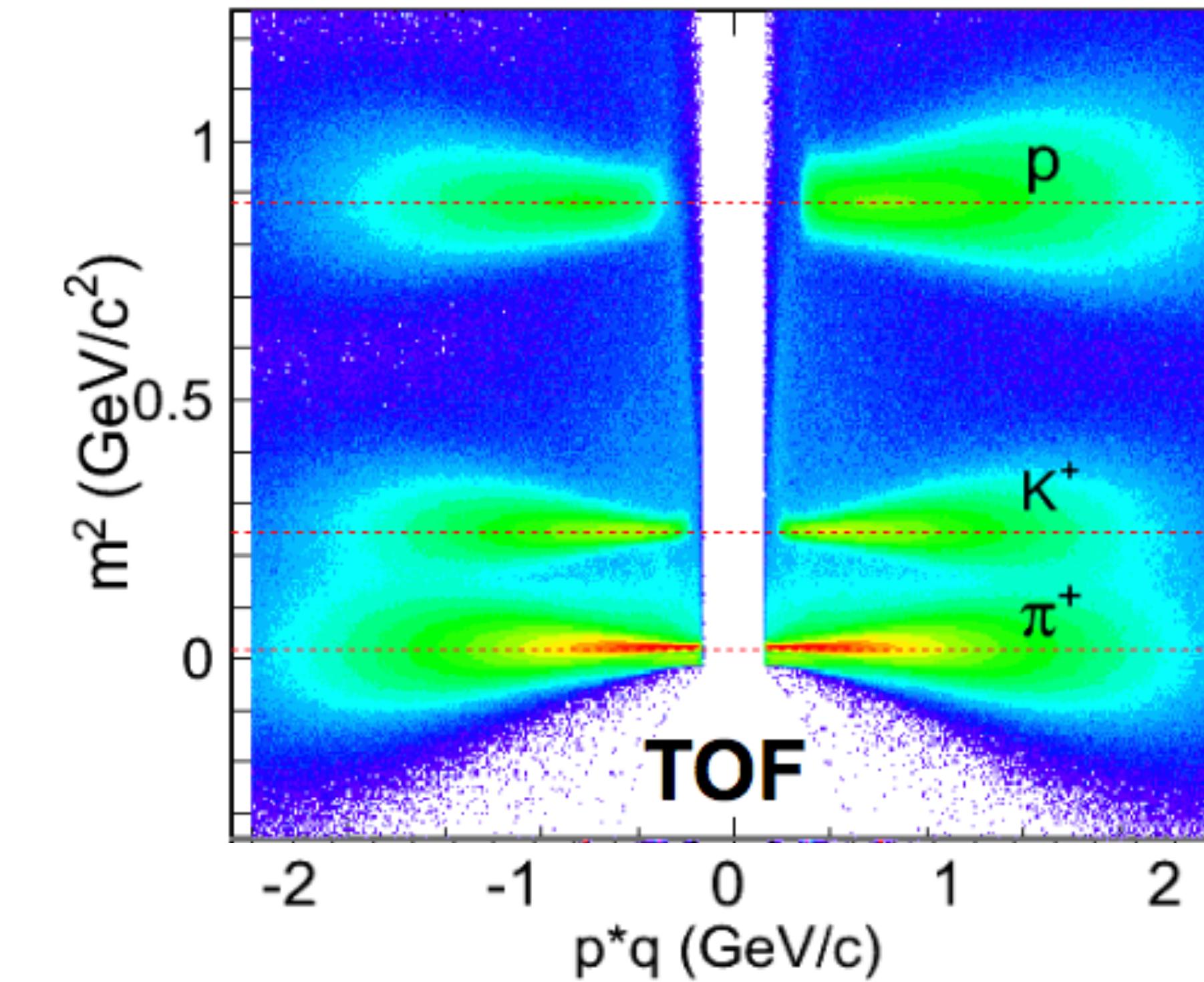
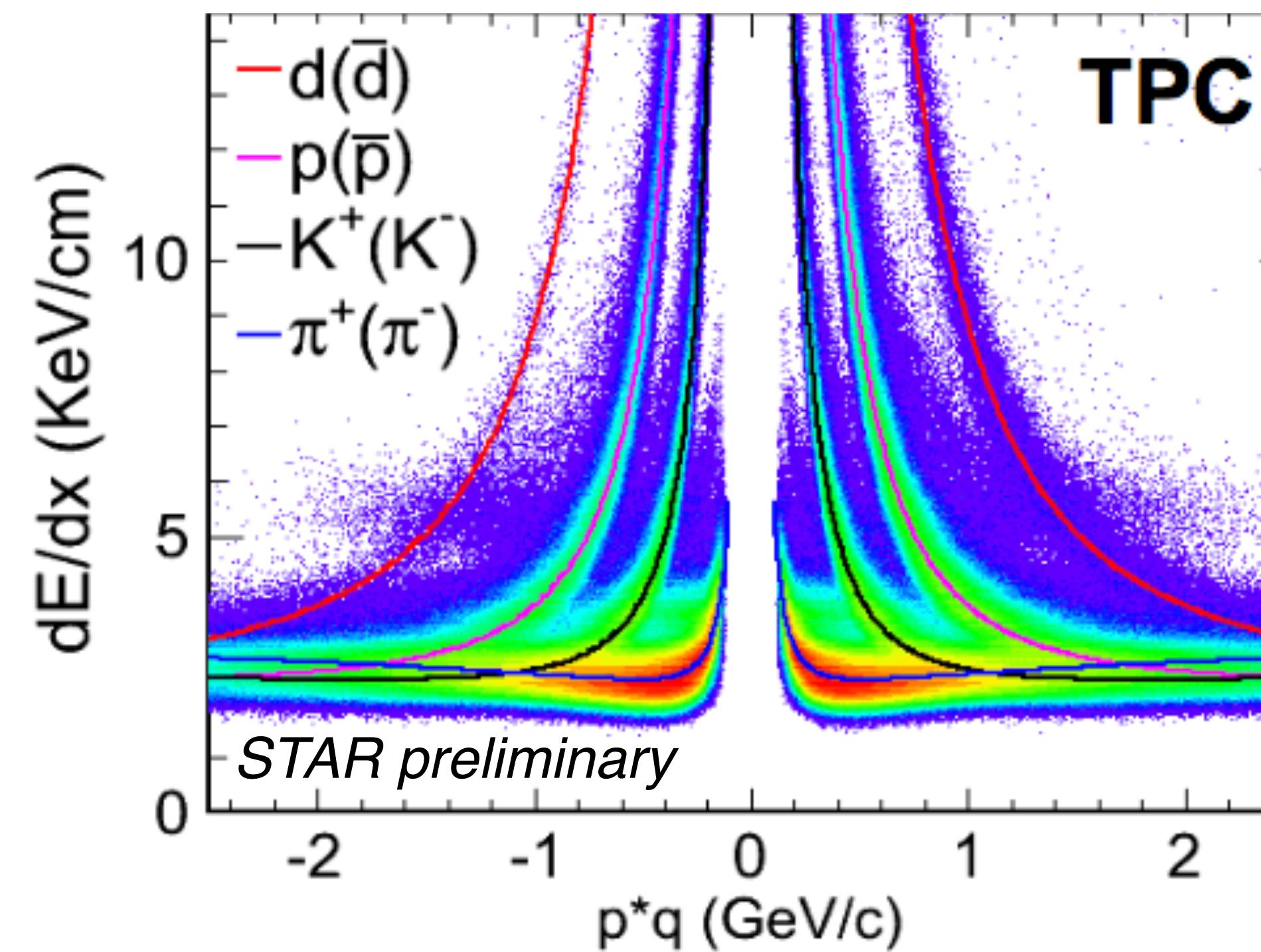
M. Cheng et al, PRD 79, 074505 (2009)

# The STAR detector



# Particle identification

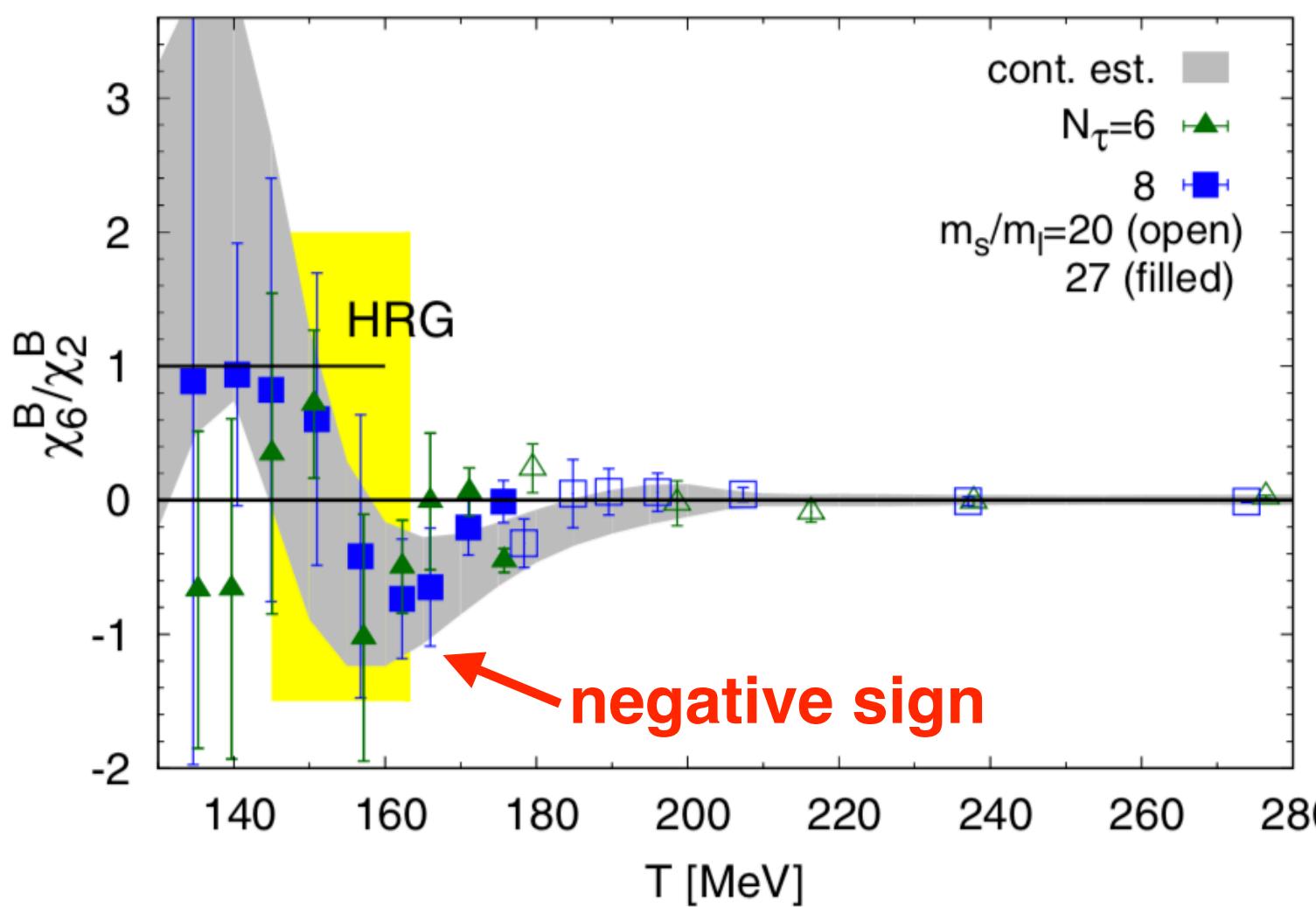
- ✓ **dE/dx measured with TPC is used for proton identification at low  $p_T$  region.**
- ✓ **The combined PID with  $m^2$  from TOF is used at high  $p_T$  region.**



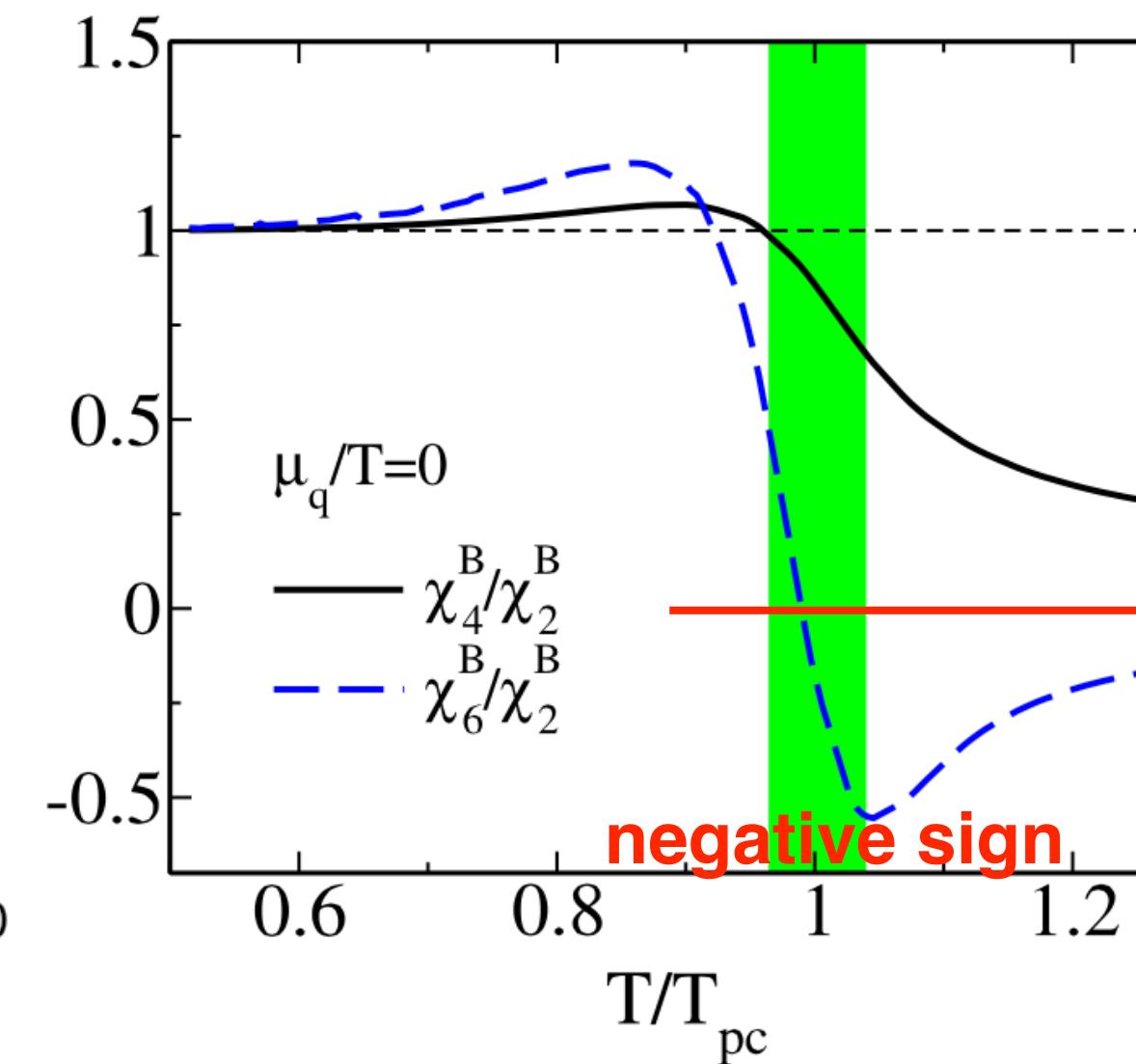
# The sixth-order cumulant

- ✓ There isn't yet any experimental evidence for the smooth crossover at  $\mu_B \sim 0$ .
- ✓ Sixth-order cumulants of net-charge and net-baryon distributions are predicted to be negative if the chemical freeze-out is close enough to the phase transition.

A. Bazavov et al, PhysRevD. 95.054504 : LQCD



Friman et al, Eur. Phys. J. C (2011)  
71:1694 : PQM model



C.Schmidt, Prog.Theor.Phys.Supp.186,563–566(2010)

Cheng et al, Phys. Rev. D 79, 074505 (2009)  
Friman et al, Eur. Phys. J. C (2011) 71:1694

Freeze-out conditions	$\chi_4^B/\chi_2^B$	$\chi_6^B/\chi_2^B$	$\chi_4^Q/\chi_2^Q$	$\chi_6^Q/\chi_2^Q$
HRG	1	1	$\sim 2$	$\sim 10$
QCD:	$T^{\text{freeze}}/T_{pc} \lesssim 0.9$	$\gtrsim 1$	$\gtrsim 1$	$\sim 2$
QCD:	$T^{\text{freeze}}/T_{pc} \simeq 1$	$\sim 0.5$	$< 0$	$\sim 1$
				$< 0$

Predicted scenario for this measurement

# Analysis methods

- ✓ Centrality bin width averaging is done for the reduction of the initial volume fluctuation.
- ✓ Calculate the cumulants at each value of the multiplicity used for centrality, then weighted-average these in each centrality bin.

- X.Luo, J. Xu, B. Mohanty and N. Xu. *J. Phys. G*40,105104(2013)

$$C_n = \frac{\sum_{r=N_1}^{N_2} n_r C_n^r}{\sum_{r=N_1}^{N_2} n_r} = \sum_{r=N_1}^{N_2} \omega_r C_n^r \quad \omega_r = n_r / \sum_{r=N_1}^{N_2} n_r$$

$N_1, N_2$  : lowest and highest multiplicity bin in the centrality  
 $n_r$  : # of events in rth multiplicity bin

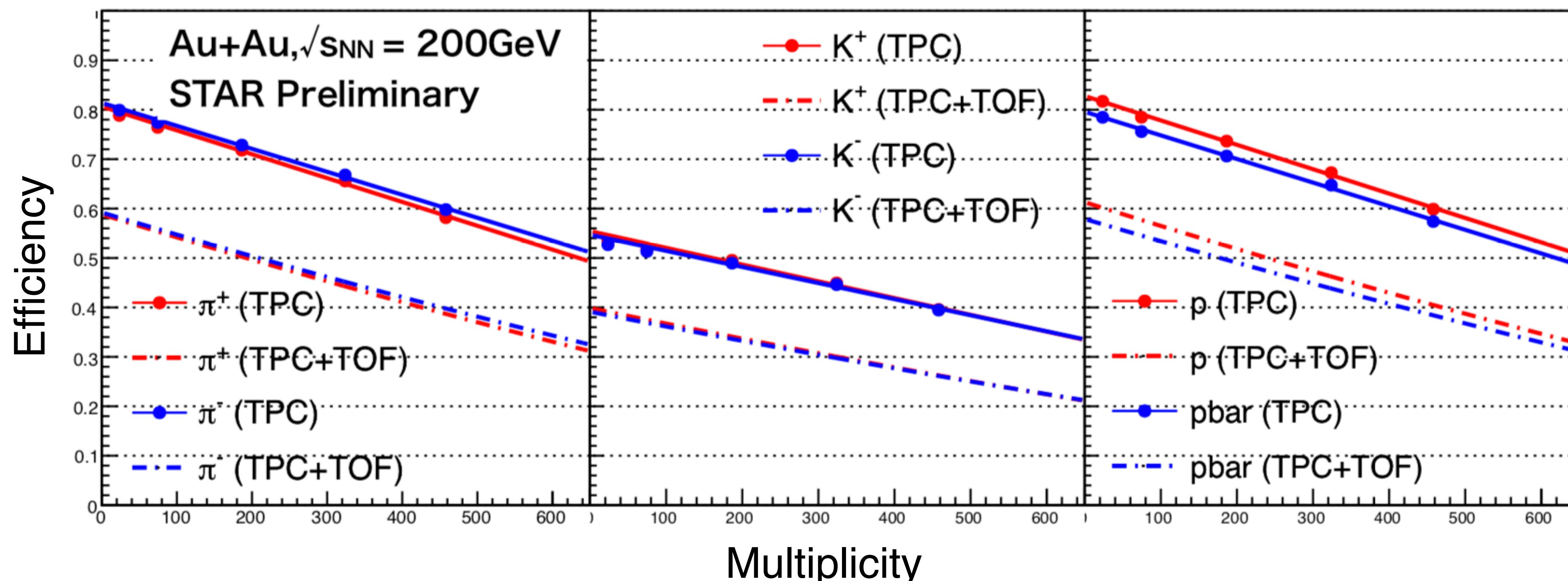
- ✓ Efficiency correction on cumulants have been done assuming the binomial efficiencies.

- M. Kitazawa : PRC.86.024904, M. Kitazawa and M. Asakawa : PRC.86.024904
- A. Bzdak and V. Koch : PRC.86.044904, PRC.91.027901, X. Luo : PRC.91.034907
- T. Nonaka, M. Kitazawa, S. Esumi : PRC.95.064912

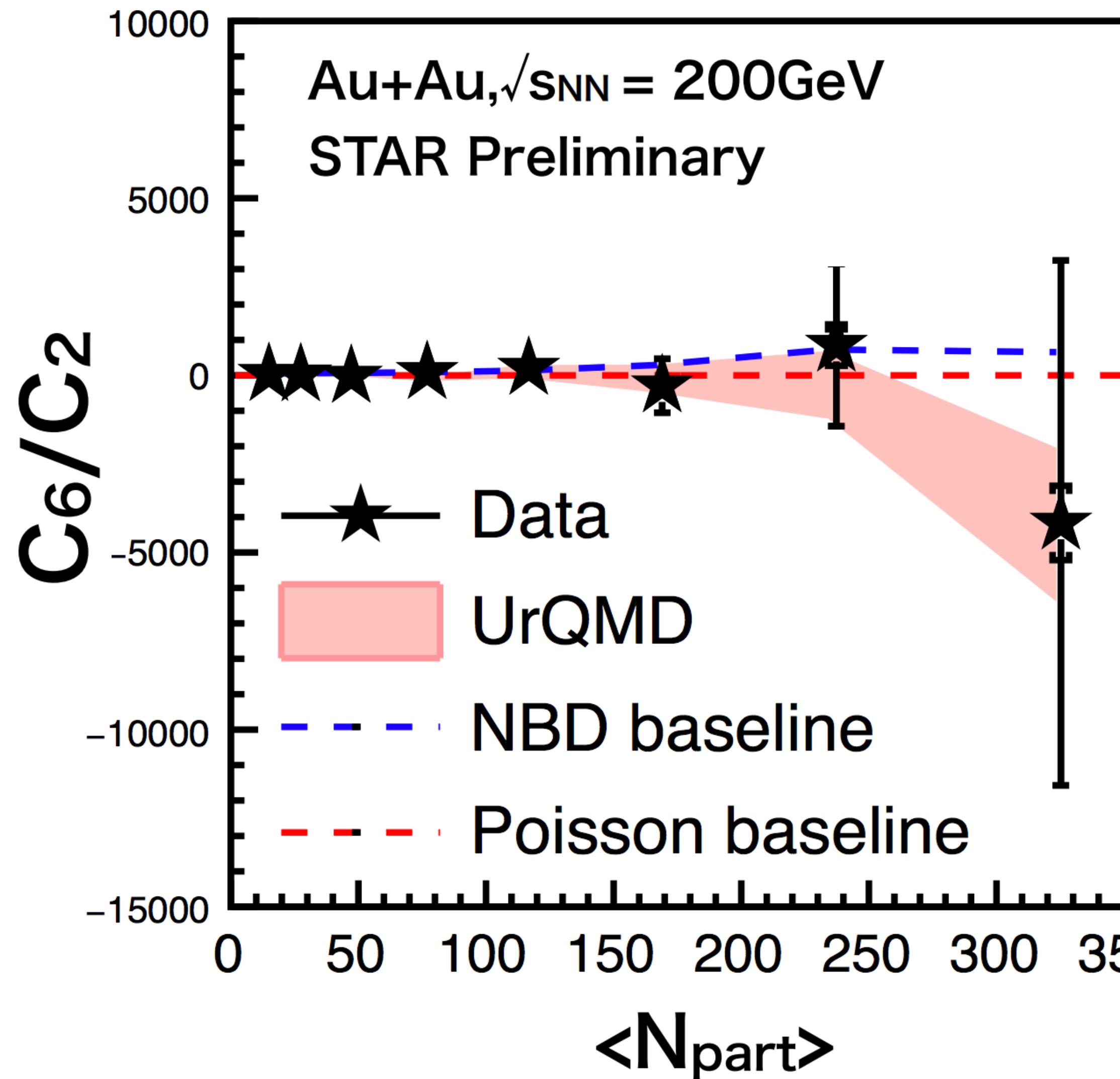
$$B_{p,N}(n) = \frac{N!}{n!(N-n)!} p^n (1-p)^n$$

# Efficiency

- ✓ Single-particle tracking efficiencies for  $\pi/K/p$  have been estimated by embedding simulation.
- ✓ TOF matching efficiency is obtained from the real data.



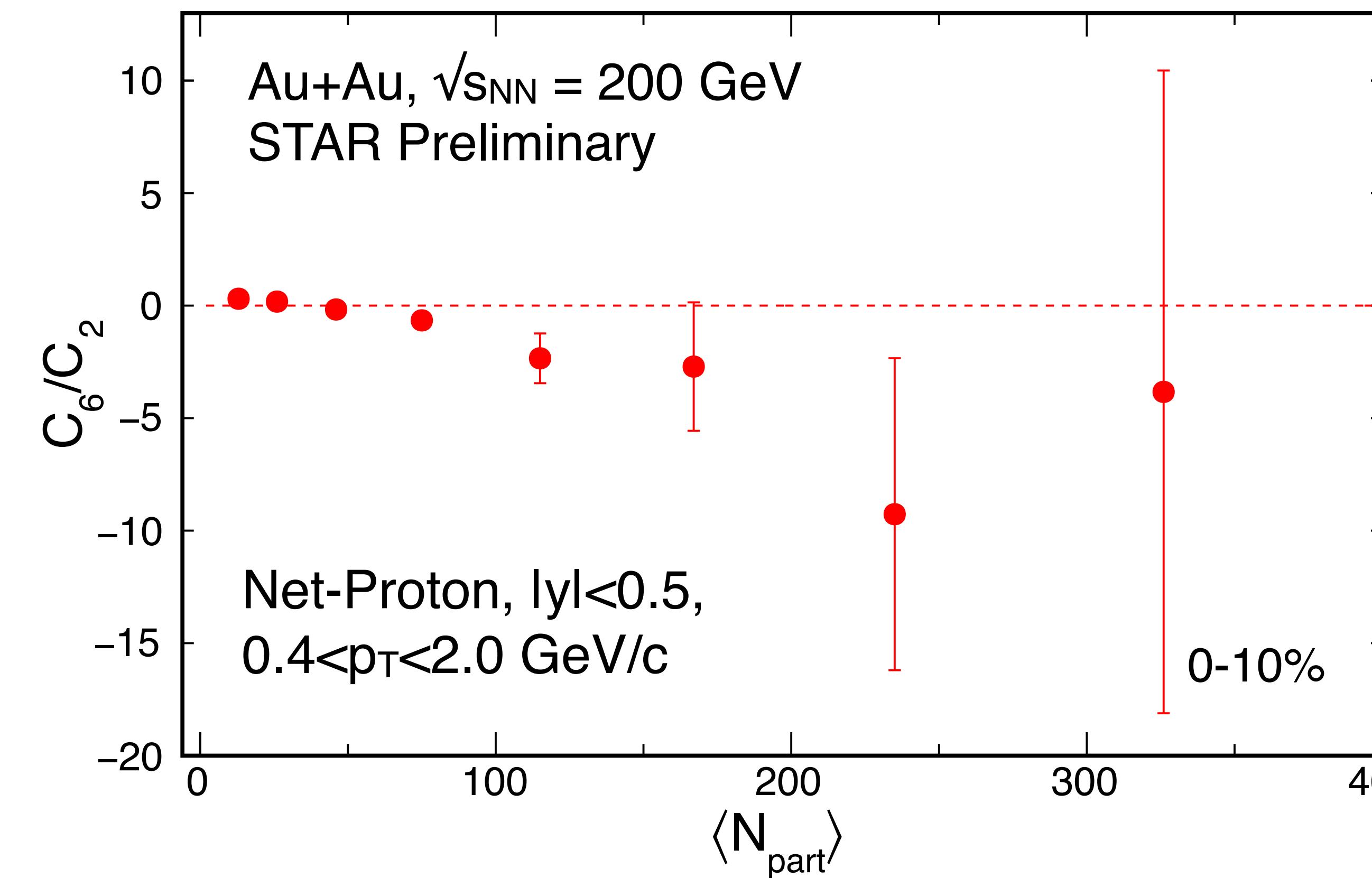
# Net-charge at $\sqrt{s_{NN}} = 200 \text{ GeV}$



✓ Results of net-charge  $C_6/C_2$  are consistent with zero within large statistical uncertainties.

# Net-proton at $\sqrt{s_{NN}} = 200 \text{ GeV}$

- ✓ Much better precision compared to net-charge.
- ✓ Negative values are observed systematically from mid-central to central collisions, which seems consistent with theoretical prediction.



$$\text{error}(C_r) \propto \frac{\sigma^r}{\sqrt{N_{\text{eve}}}}$$

Used statistics

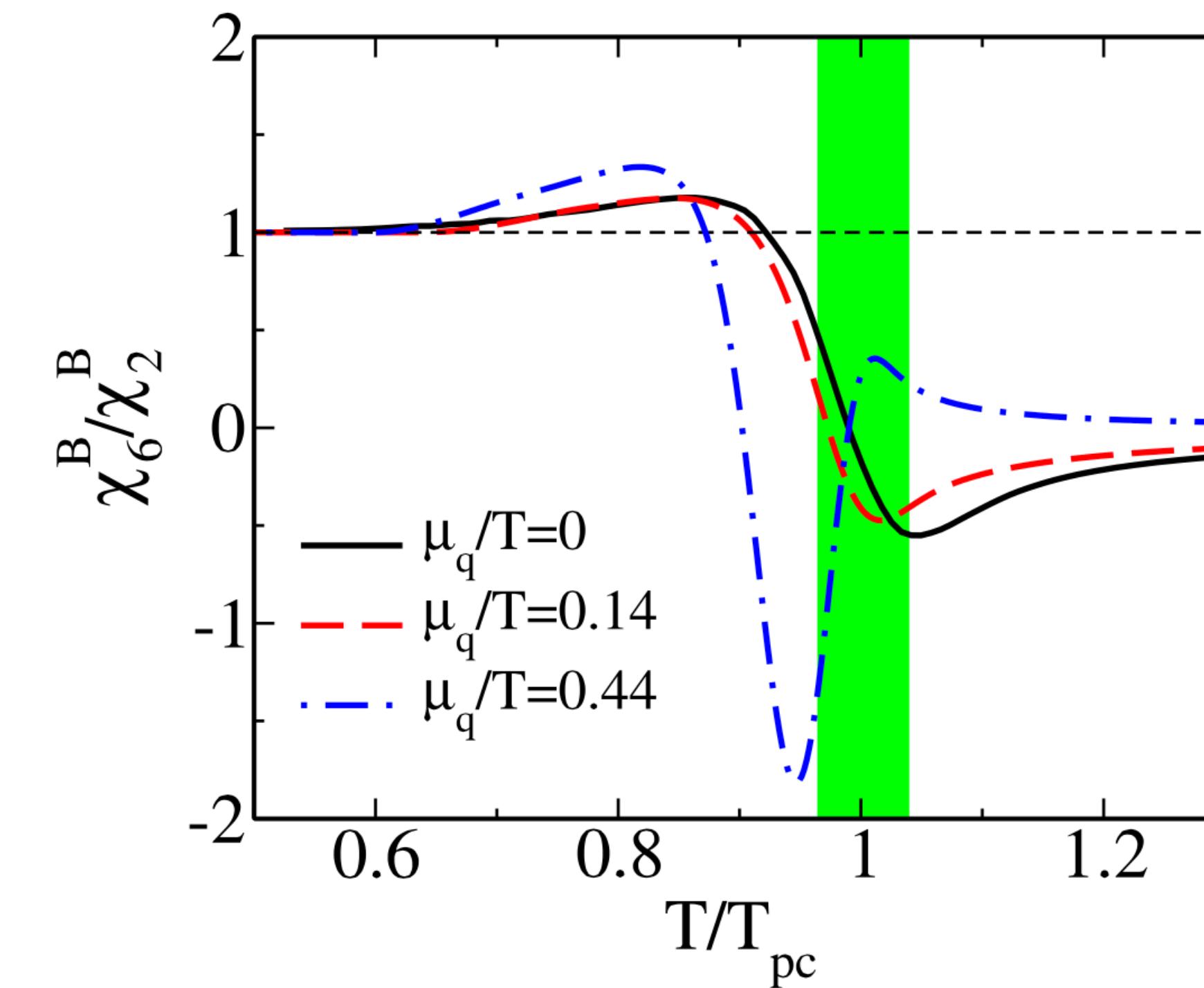
	0-10%	10-80%
Run10	~160M	~200M
Run11	~50M	~450M

# Lower beam energy?

- ✓ Positive  $C_6$  is predicted in  $\sqrt{s_{NN}} < 60$  GeV ( $\mu_B/T < 0.5$ ).
- ✓ STAR collected ~1B minimum bias events (500M good events) at  $\sqrt{s_{NN}} = 54.4$  GeV in 2017.

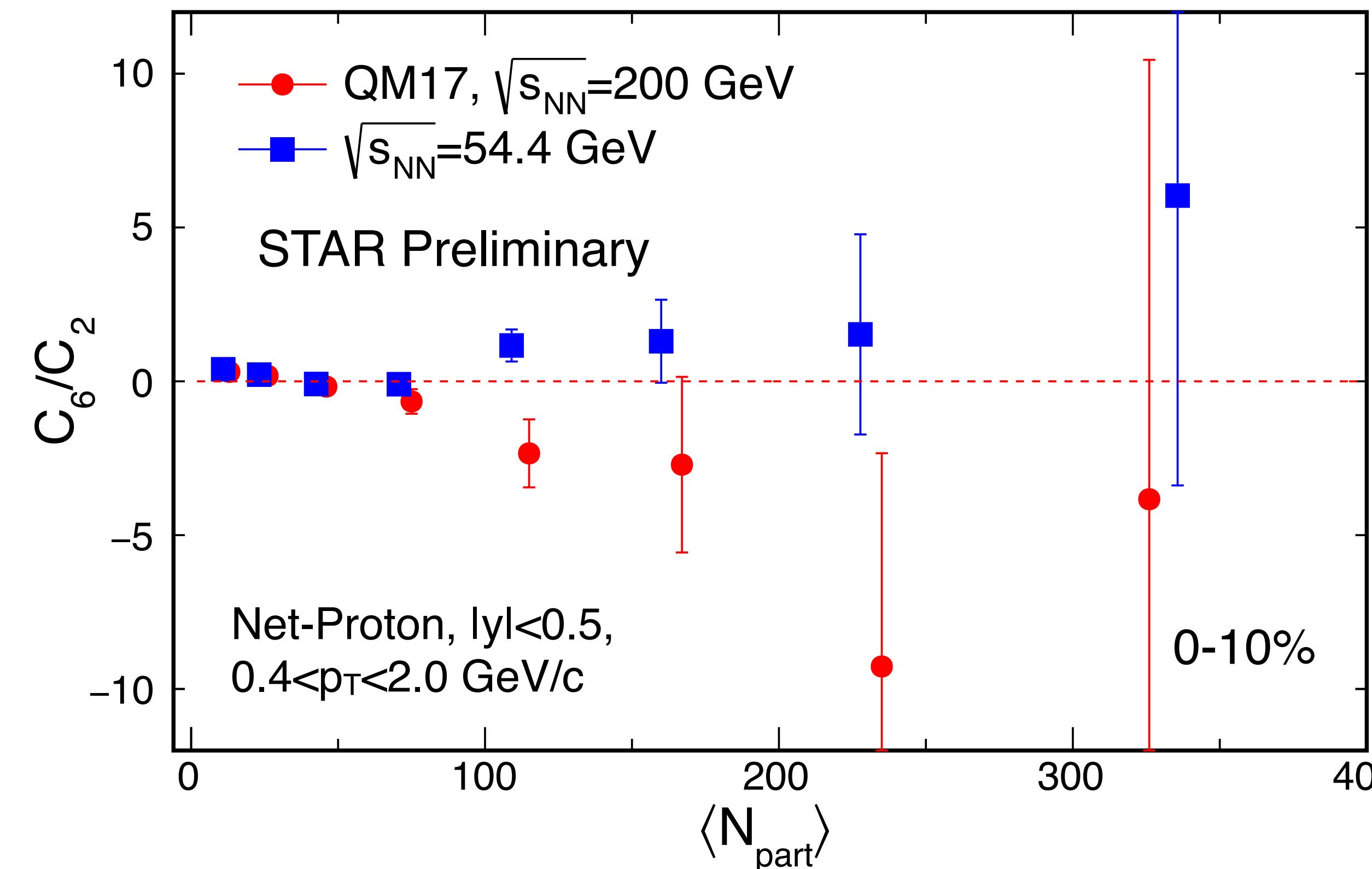
Friman et al, Eur. Phys. J. C (2011) 71:1694

If freeze-out occurs close to the chiral crossover temperature the sixth order cumulant of the net baryon number fluctuations will be negative at LHC energies as well as for RHIC beam energies  $\sqrt{s_{NN}} \gtrsim 60$  GeV, corresponding to  $\mu_B/T \lesssim 0.5$ . This is in contrast to hadron resonance gas model calculations which yield a positive sixth order cumulant.



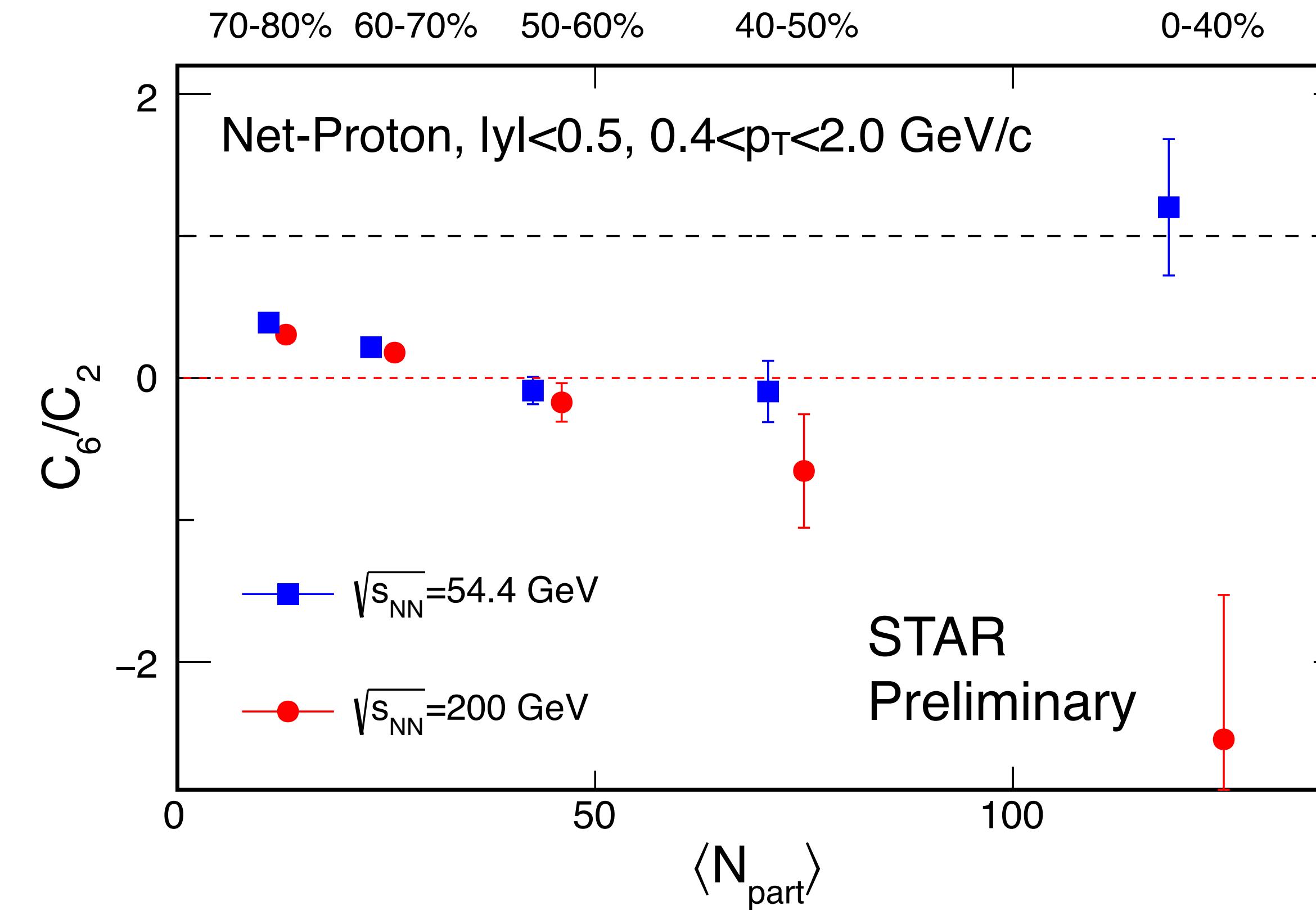
# Net-proton at $\sqrt{s_{NN}} = 54.4 \text{ GeV}$

✓ Positive values are observed systematically from peripheral to central collisions.

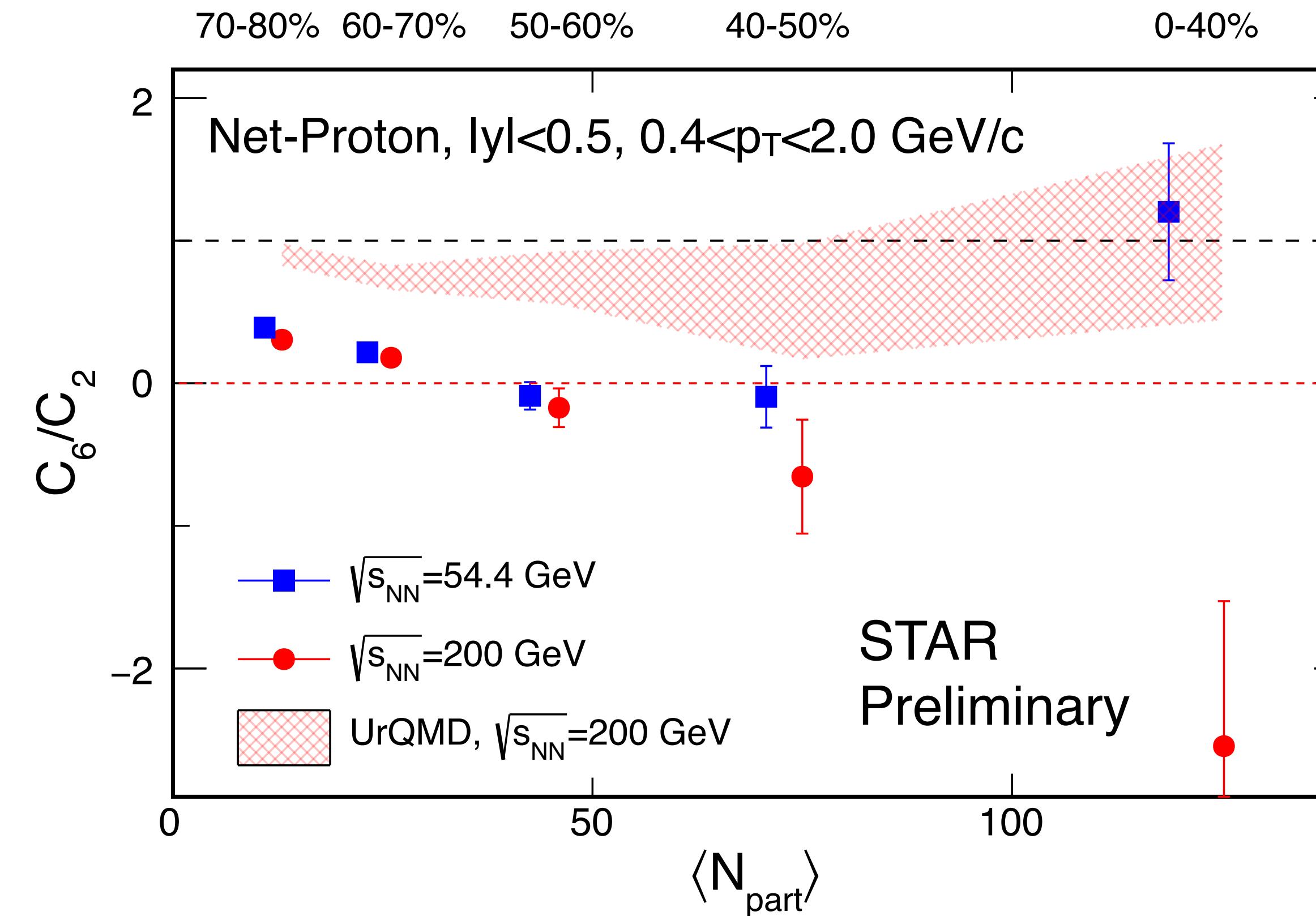


# 0-40% centrality

- ✓ Clear separation and opposite signs between two energies in 0-40%.

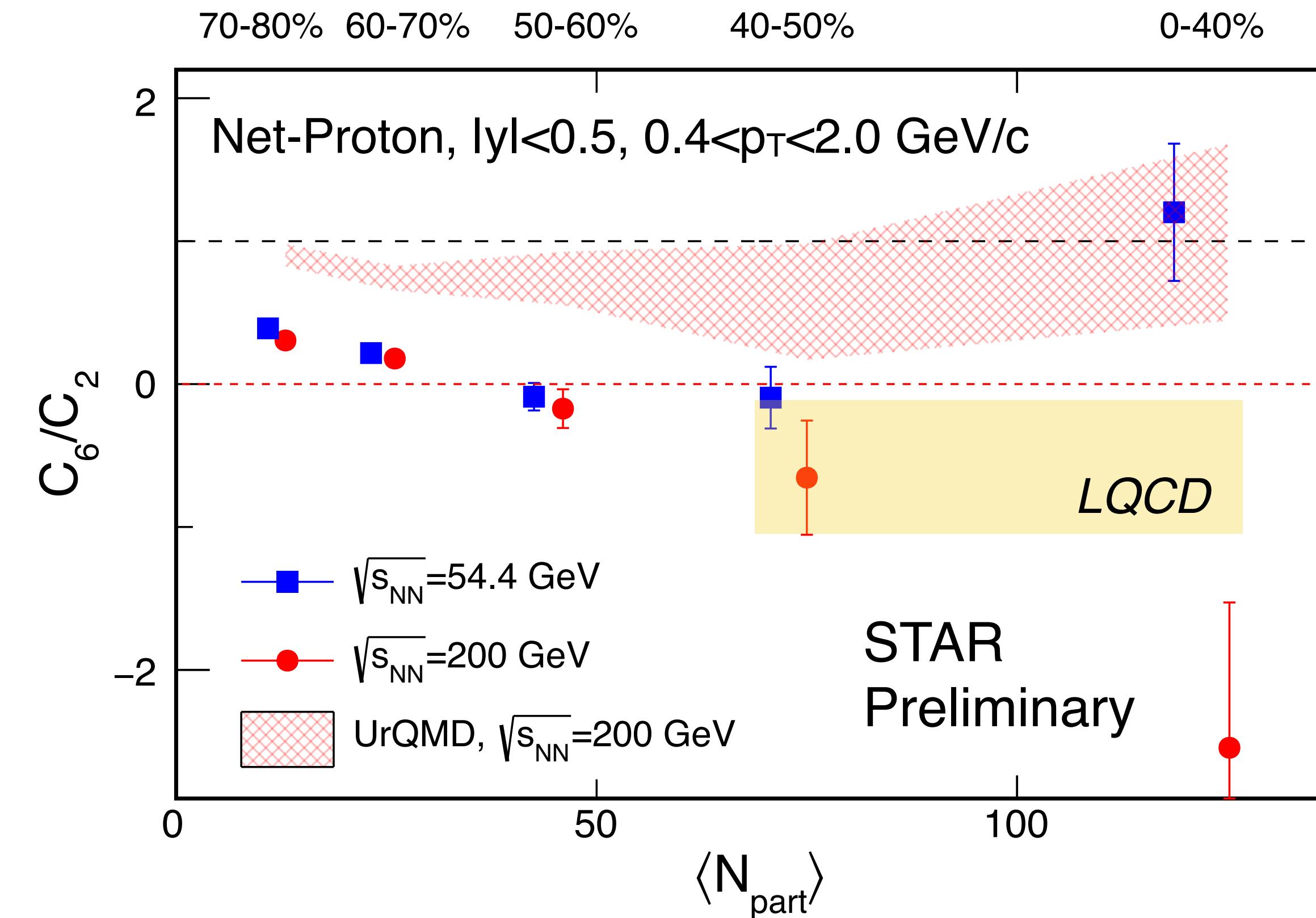


- ✓ Clear separation and opposite signs between two energies in 0-40%.
- ✓ UrQMD result shows positive signs for all centralities at  $\sqrt{s_{NN}} = 200$  GeV.



# 0-40% centrality

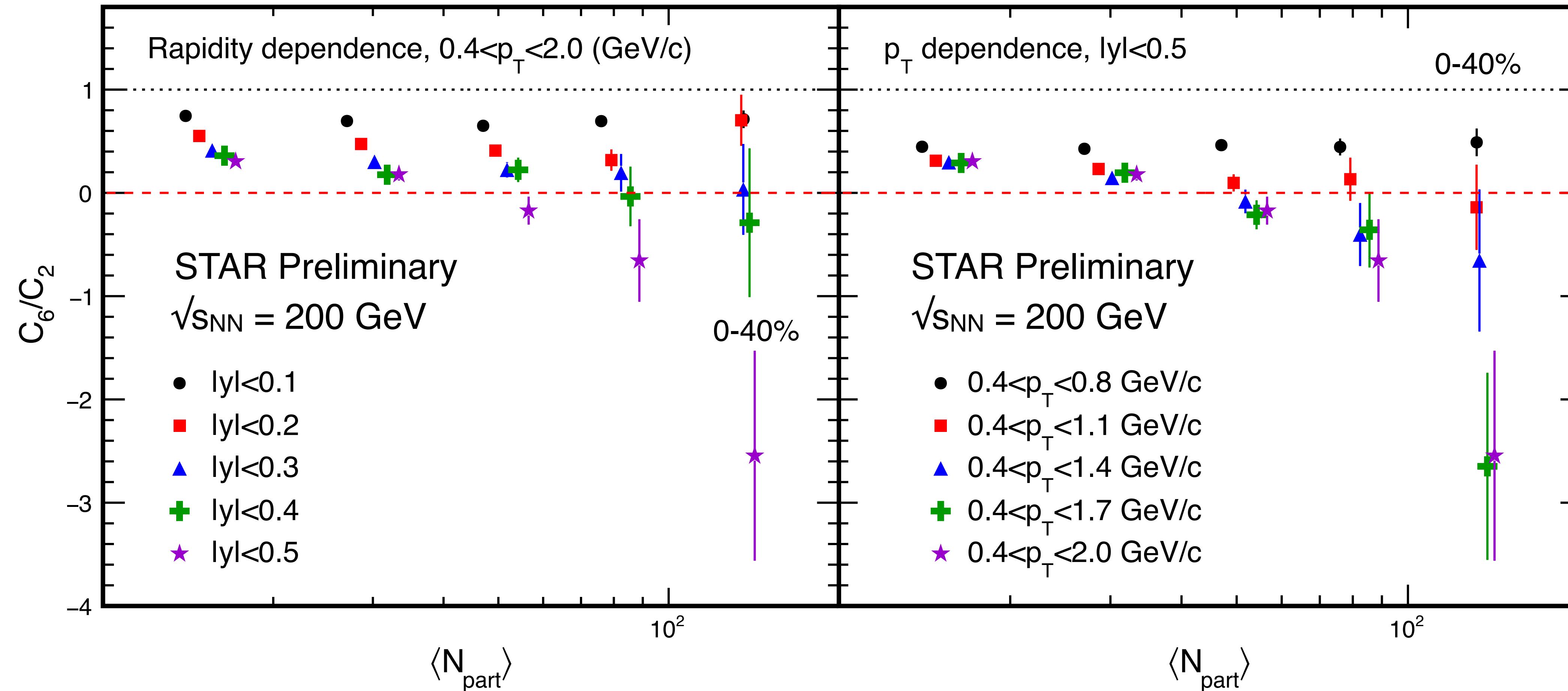
- ✓ Clear separation and opposite signs between two energies in 0-40%.
- ✓ UrQMD result shows positive signs for all centralities at  $\sqrt{s_{NN}} = 200$  GeV.
- ✓ 200 GeV results are consistent with the LQCD results.



LQCD : A. Bazavov et al,  
PhysRevD.95.054504

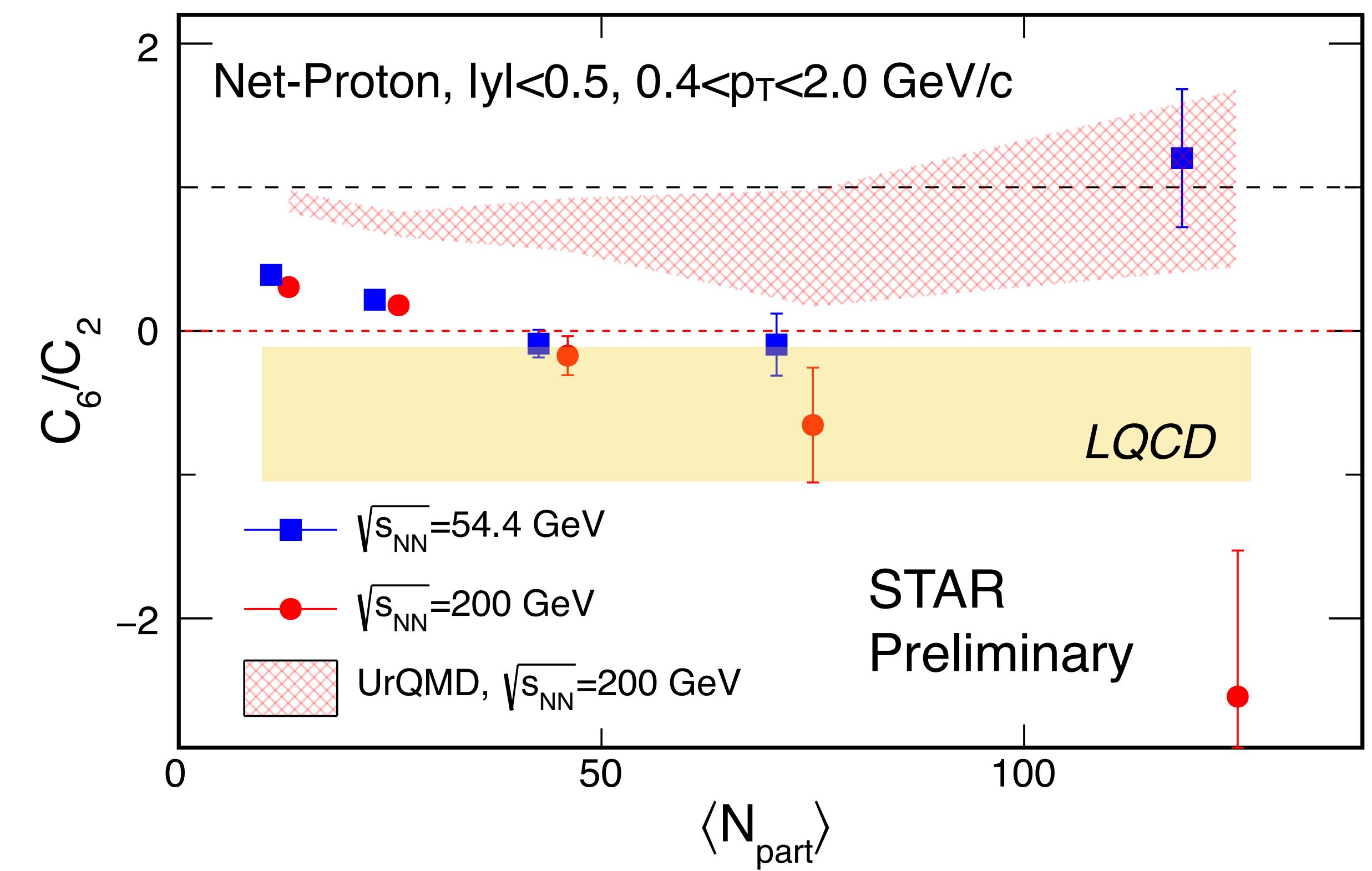
# Acceptance dependence

- ✓ Monotonic decrease with enlarging the acceptance.
- ✓  $p_T$  dependence seems to be saturated at  $0.4 < p_T < 1.7 \text{ GeV}/c$ .



# Summary

- ✓  $C_6/C_2$  of net-charge multiplicity distributions show zero within large uncertainties.
- ✓  $C_6/C_2$  of net-proton multiplicity distributions show
  - negative value in 0-40% centrality at  $\sqrt{s_{NN}} = 200 \text{ GeV}$
  - positive value in 0-40% centrality at  $\sqrt{s_{NN}} = 54.4 \text{ GeV}$
  - linear decrease with respect to  $p_T$  and rapidity coverage.



Thank you for your attention

# Back up