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# Event Plane and Beam Energy Dependence of the Balance Function at RHIC

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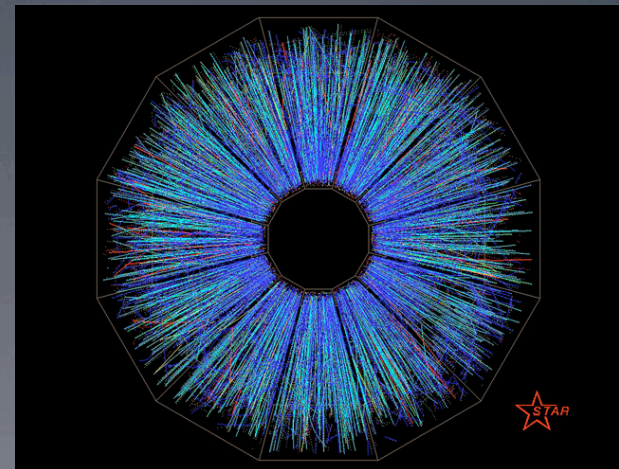
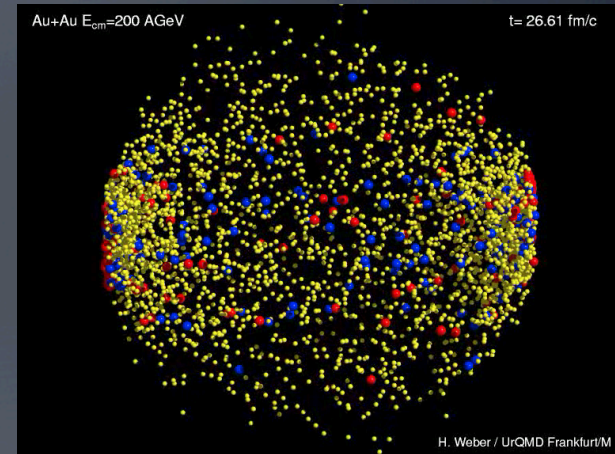
# Outline

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- Motivation
- Observable
- Balance Function with Respect to the Event Plane
- Beam Energy Dependent Balance Function
- Summary

# Motivation

- In heavy ion collisions, most of the detected charge is created during the evolution of the system.
- Charge creation could occur at any time before chemical freeze-out.
- Balance functions are sensitive to charge formation mechanisms and relative diffusion



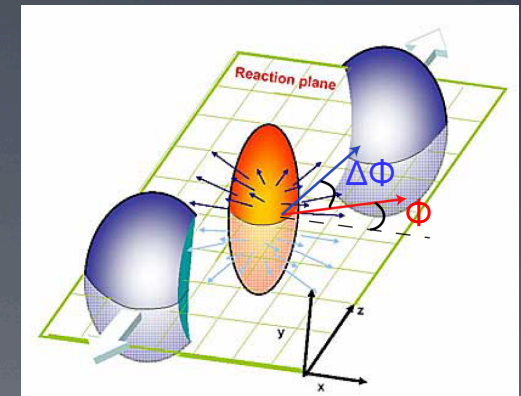
# Observable

- The balance function is a conditional probability that a particle  $a$  in the bin  $p_1$  will be accompanied by a particle  $b$  of opposite charge in the bin  $p_2$ .

$$B(p_2 | p_1) = \frac{1}{2} \{ \rho(b, p_2 | a, p_1) - \rho(b, p_2 | b, p_1) + \rho(a, p_2 | b, p_1) - \rho(a, p_2 | a, p_1) \}$$

- It can be written as

$$B(\Delta\phi) = \frac{1}{2} \left\{ \frac{N_{+-}(\Delta\phi) - N_{++}(\Delta\phi)}{N_+} + \frac{N_{-+}(\Delta\phi) - N_{--}(\Delta\phi)}{N_-} \right\}$$



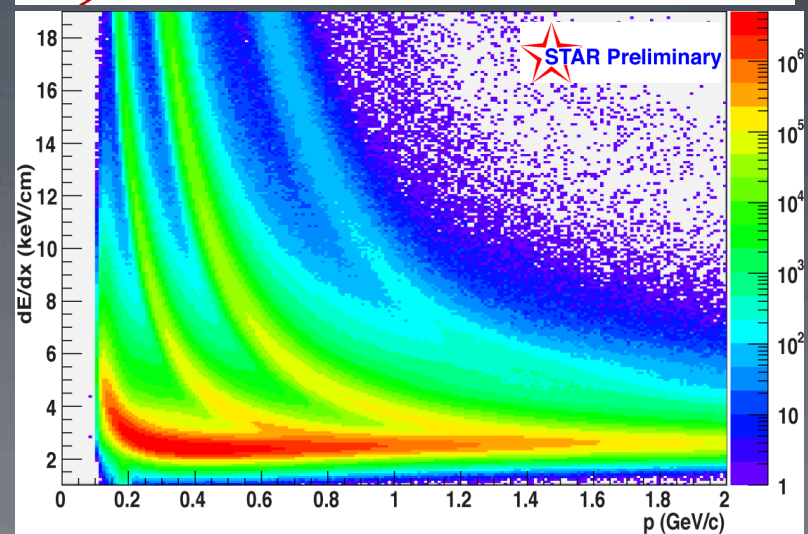
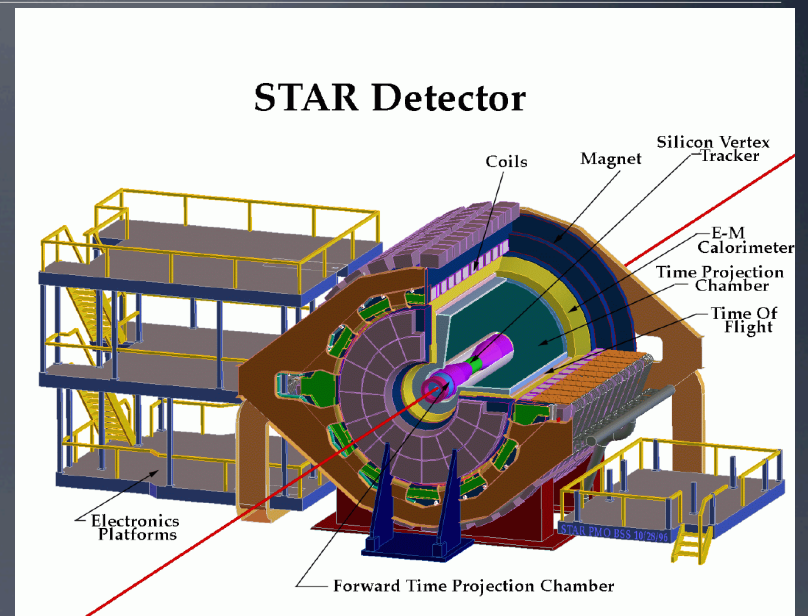
- If we specify first particle's position (azimuth)

$$B(\phi, \Delta\phi) = \frac{1}{2} \left\{ \frac{N_{+-}(\phi, \Delta\phi) - N_{++}(\phi, \Delta\phi)}{N_+(\phi)} + \frac{N_{-+}(\phi, \Delta\phi) - N_{--}(\phi, \Delta\phi)}{N_-(\phi)} \right\}$$

# The STAR Experiment

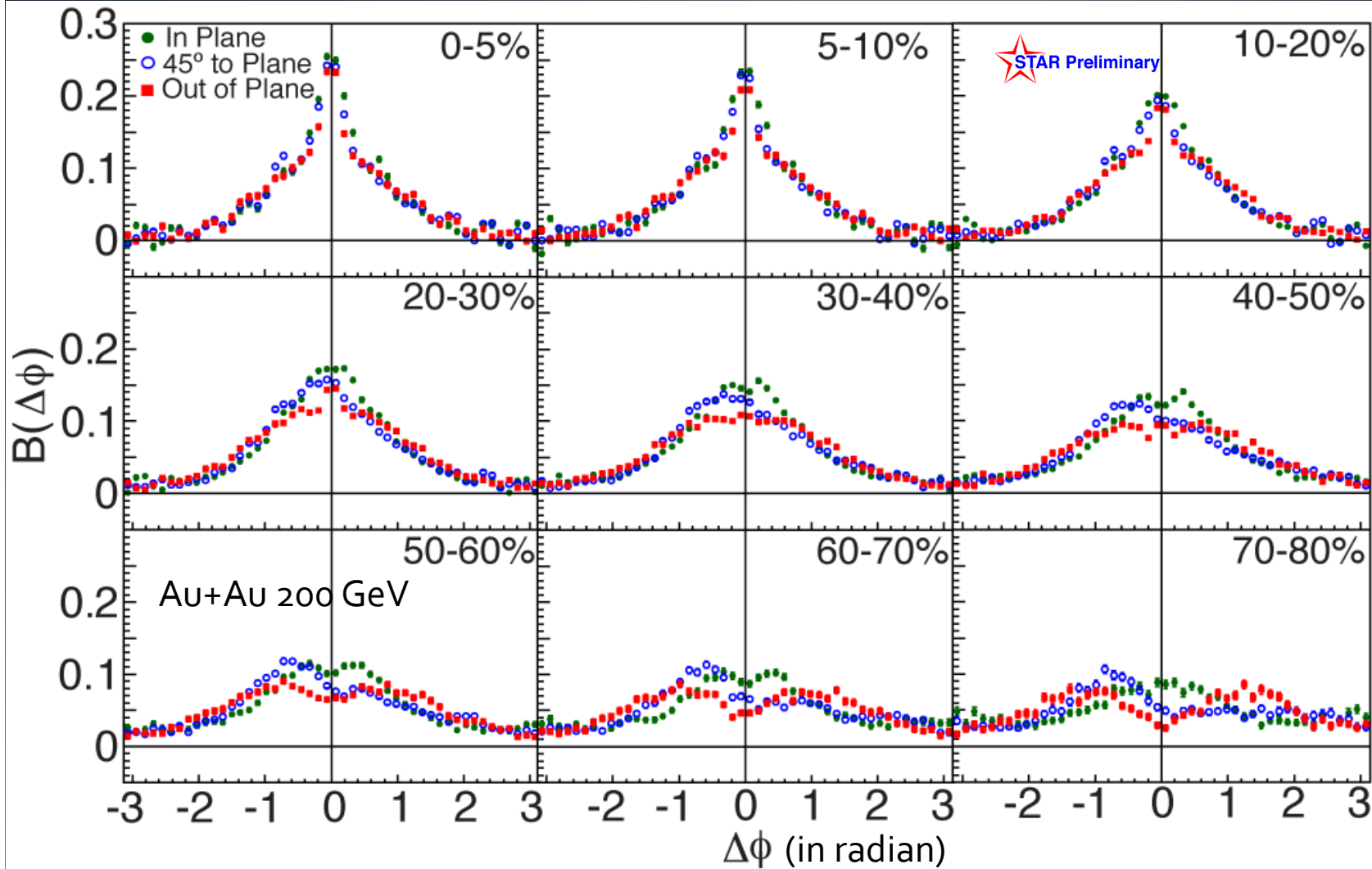
- STAR is ideal for balance function study
  - Full azimuthal coverage
  - Large  $\eta$  acceptance
- Particle identification is done using  $dE/dx$  from TPC
- TPC event plane is used for balance function calculation

$$\psi_2 = \left( \tan^{-1} \frac{\sum_i w_i \sin(2\phi_i)}{\sum_i w_i \cos(2\phi_i)} \right) / 2$$



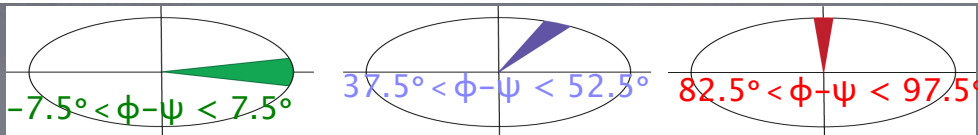
39 GeV  $dE/dx$  vs.  $p$

# Balance Function



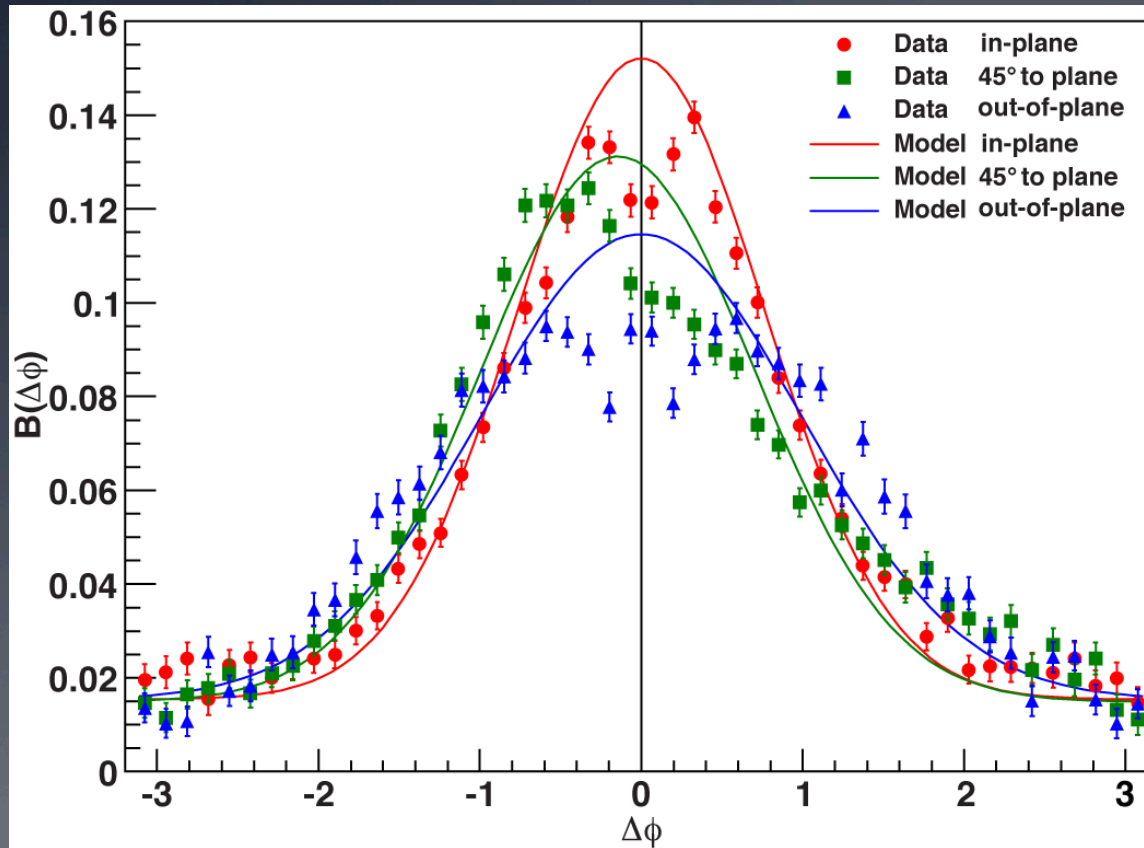
- 45° to event plane balance function is biased toward negative  $\Delta\eta$  region

- The out-of-plane balance function is wider than the in-plane balance function



- Balance function narrows in central collision due to collective flow

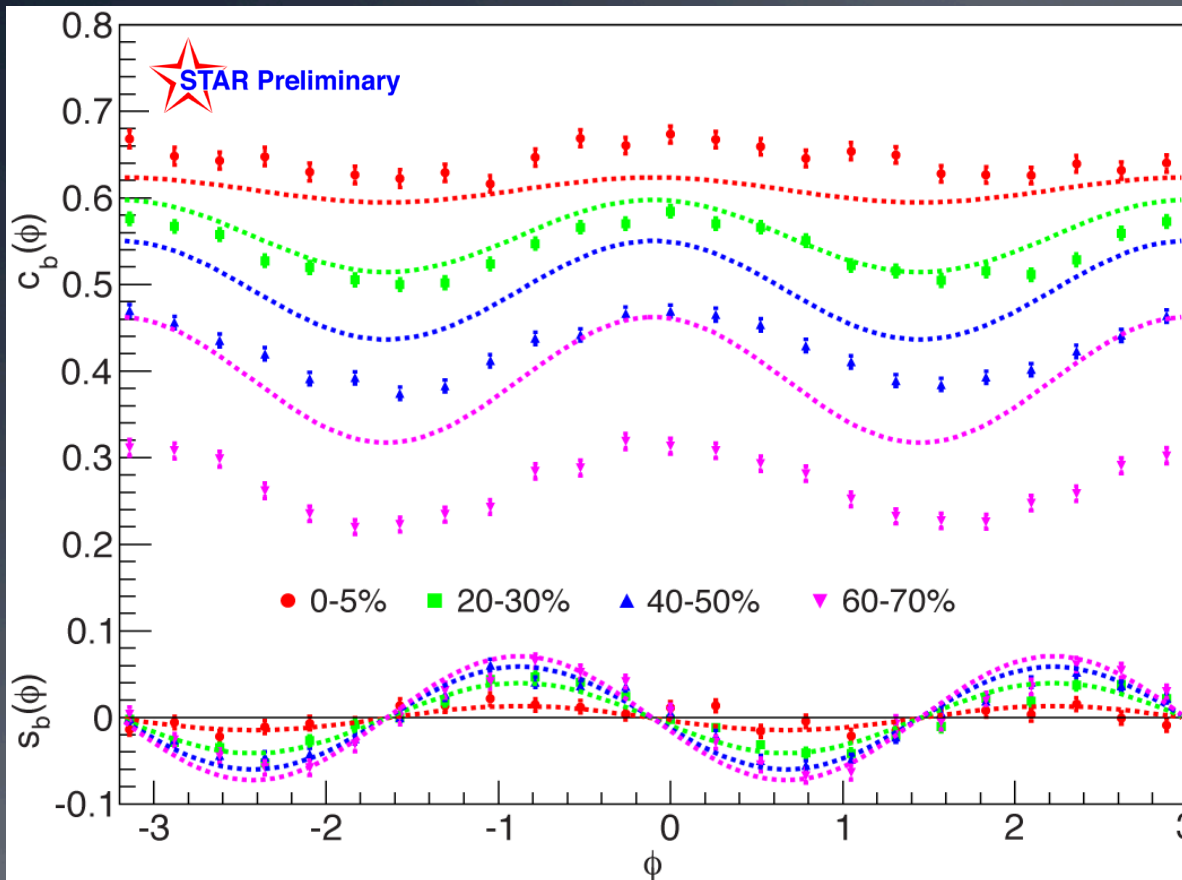
# Balance Function



- 40-50% Centrality
- Compare to blast wave model calculations<sup>1</sup>
- HBT/Coulomb effects are observed at  $\Delta\Phi$  close to zero

<sup>1</sup>S. Schlichting and S. Pratt, arXiv:1009.4283v1

# Weighted Average



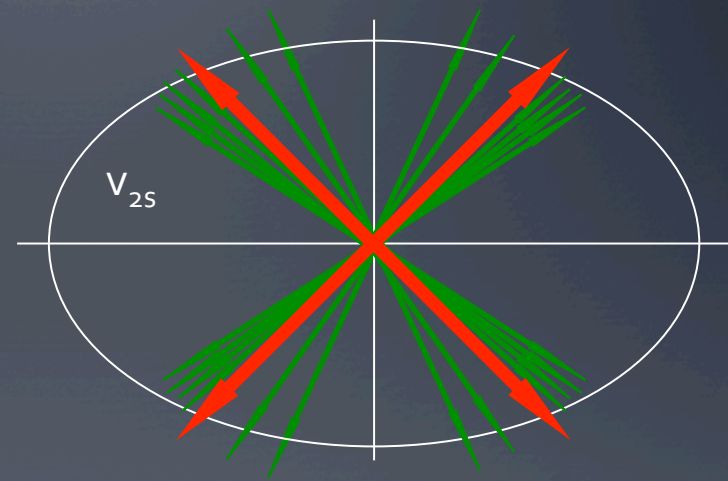
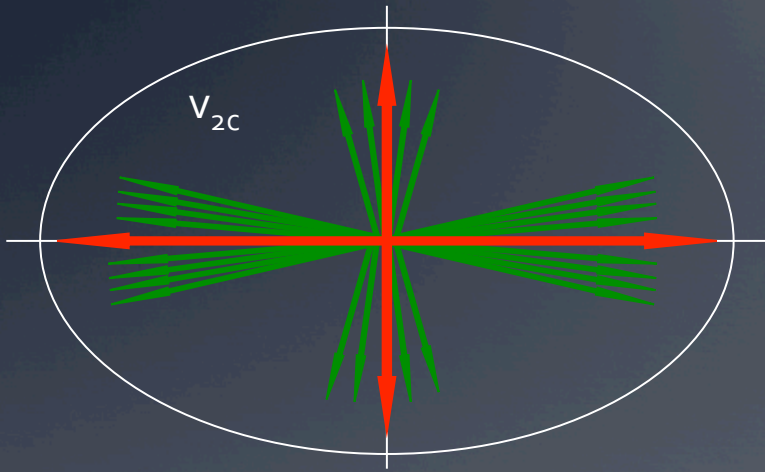
- Compare to blast wave model calculations
- $c_b$  is related to the balance function width, while  $s_b$  can quantify the asymmetry of balance function
- Data show a stronger collective behavior in plane, while the asymmetry is most significant  $45^\circ$  to the reaction plane

$$c_b(\phi) \equiv \frac{1}{z_b(\phi)} \int d\Delta\phi B(\phi, \Delta\phi) \cos(\Delta\phi)$$

$$s_b(\phi) \equiv \frac{1}{z_b(\phi)} \int d\Delta\phi B(\phi, \Delta\phi) \sin(\Delta\phi) \quad z_b(\phi) \equiv \int d\Delta\phi B(\phi, \Delta\phi)$$



# Calculate $v_{2c}$ and $v_{2s}$



- Red arrows are the first particle in balance function calculation
- $v_2 \langle c_b \rangle$  would be positive if more charges pairs are found in plane
- $v_{2c}$  would be positive if charges are more correlated in plane
- $v_{2s}$  would be negative if charges are more correlated on the in plane side

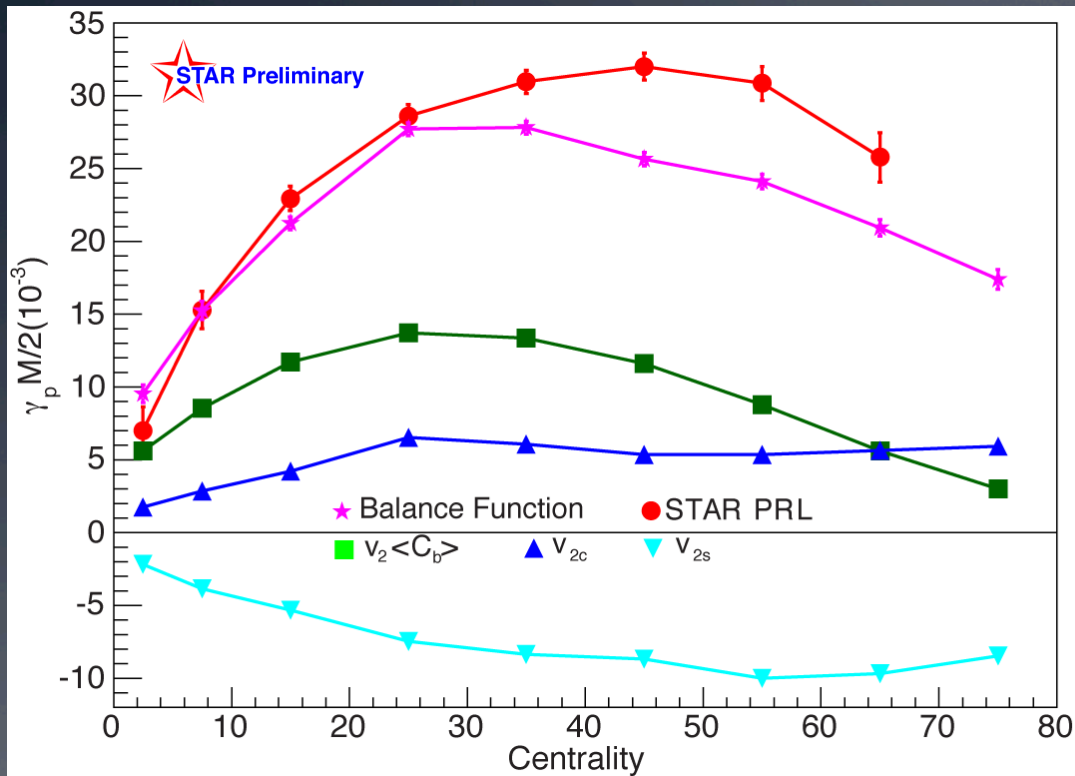
$$v_{2c} \equiv \langle c_b(\phi) \cos(2\phi) \rangle - v_2 \langle c_b(\phi) \rangle$$

$$v_{2s} \equiv \langle s_b(\phi) \sin(2\phi) \rangle$$

$$\langle f(\phi) \rangle \equiv \frac{1}{M} \int d\phi \frac{dM}{d\phi} z_b(\phi) f(\phi)$$

Explaining Angular Correlations Observed at RHIC with Flow and Local Charge Conservation, Soeren Schlichting, Scott Pratt, arXiv:1005.5341

# Parity Observable



- $\gamma_p$  is the difference between unlike- and like-sign azimuthal correlations
- $\gamma_p$  scaled by multiplicity can be written as the combination of  $v_2 \langle c_b(\Phi) \rangle$ ,  $v_{2c}$  and  $v_{2s}$
- Compare with STAR published data<sup>1</sup>
- The balance function reproduces most of the observed difference between unlike- and like-sign azimuthal correlations

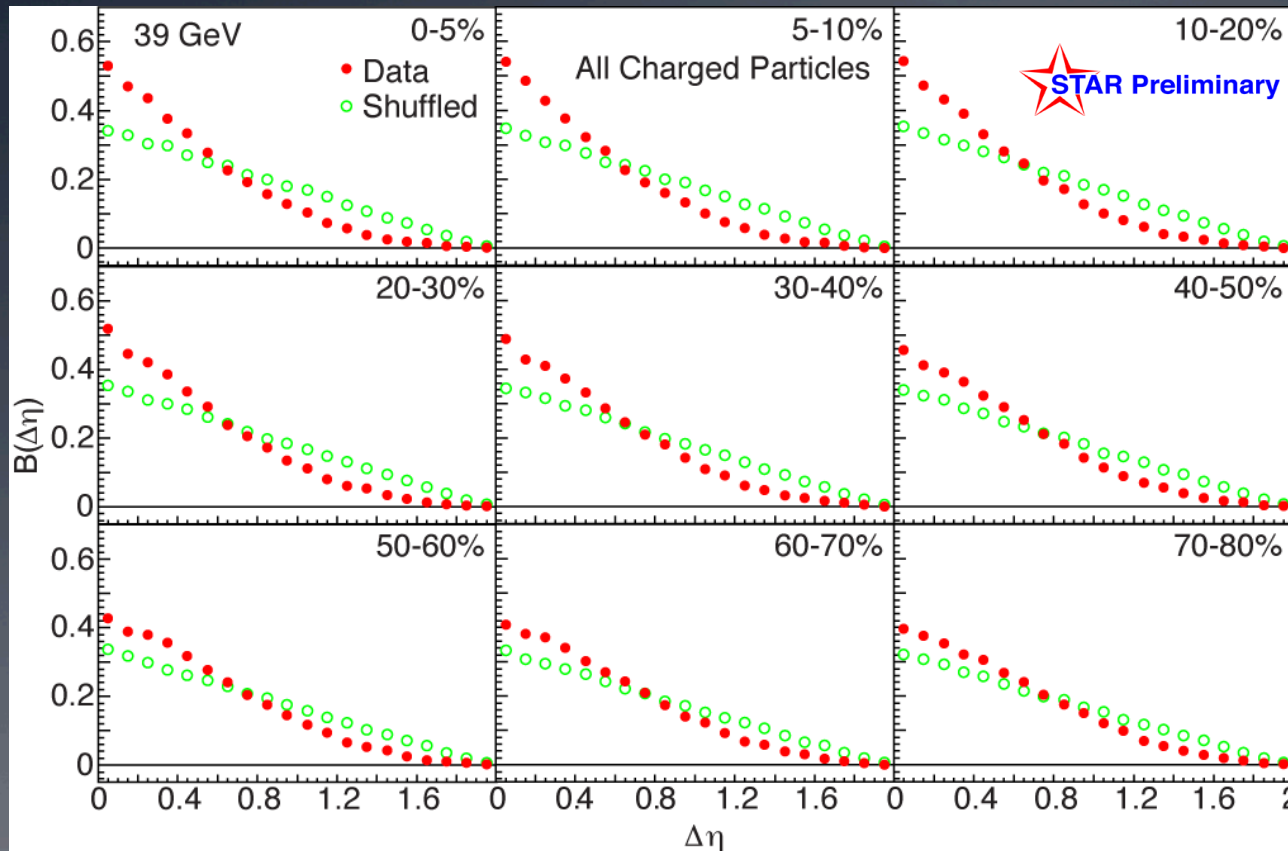
$$\gamma = \langle \cos(\phi_\alpha + \phi_\beta - 2\Psi_{RP}) \rangle$$

$$\gamma_p = \frac{1}{2}(2\gamma_{+-} - \gamma_{++} - \gamma_{--}) = \frac{2}{M}[v_2 \langle c_b(\phi) \rangle + v_{2c} - v_{2s}]$$

<sup>1</sup>10.1103/PhysRevLett.103.251601

# Balance Functions Study with RHIC Beam Energy Scan Data

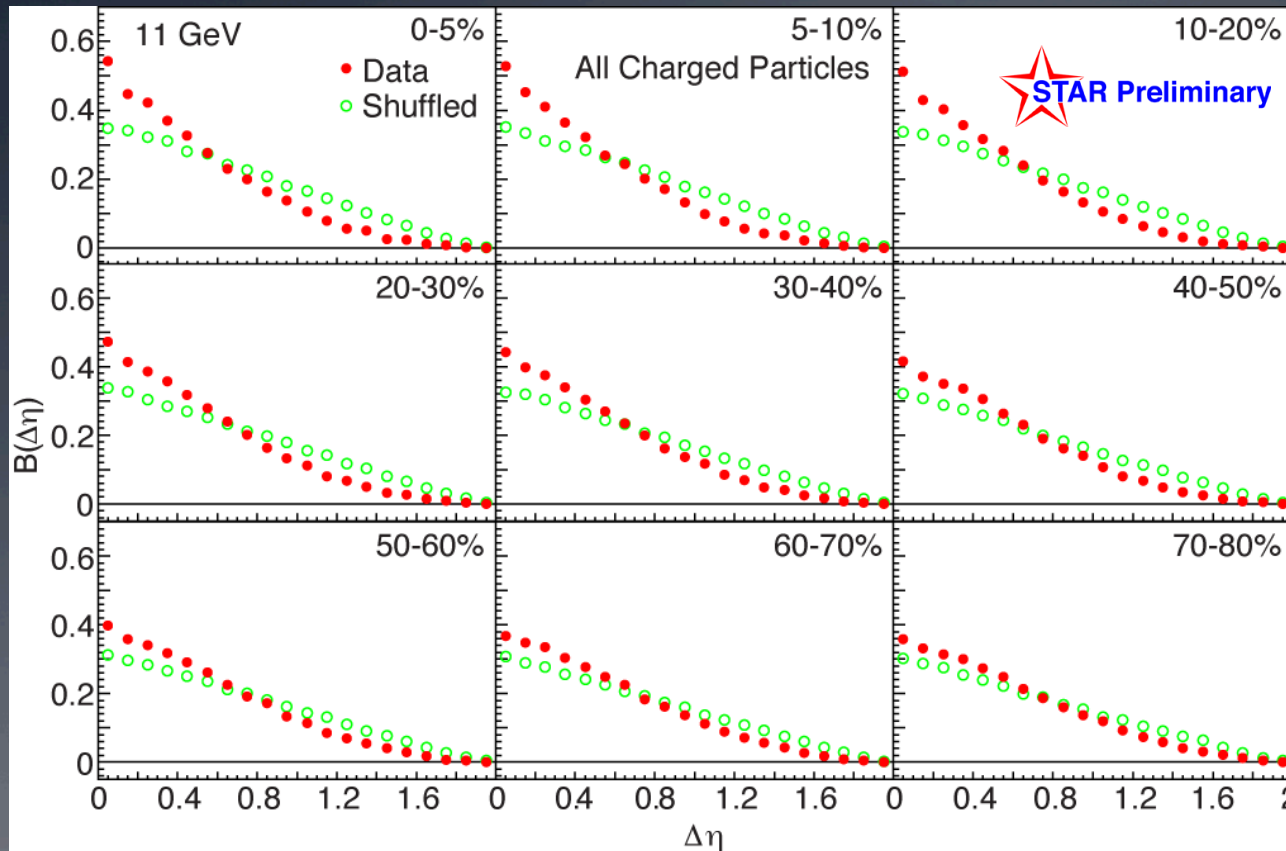
# Balance Function for $\Delta\eta$



- 39 GeV
- 9 Centralities
- Data are narrower than shuffled events
- Data narrow in central collisions

$$B(\Delta\eta) = \frac{1}{2} \left\{ \frac{N_{+-}(\Delta\eta) - N_{++}(\Delta\eta)}{N_+} + \frac{N_{-+}(\Delta\eta) - N_{--}(\Delta\eta)}{N_-} \right\}$$

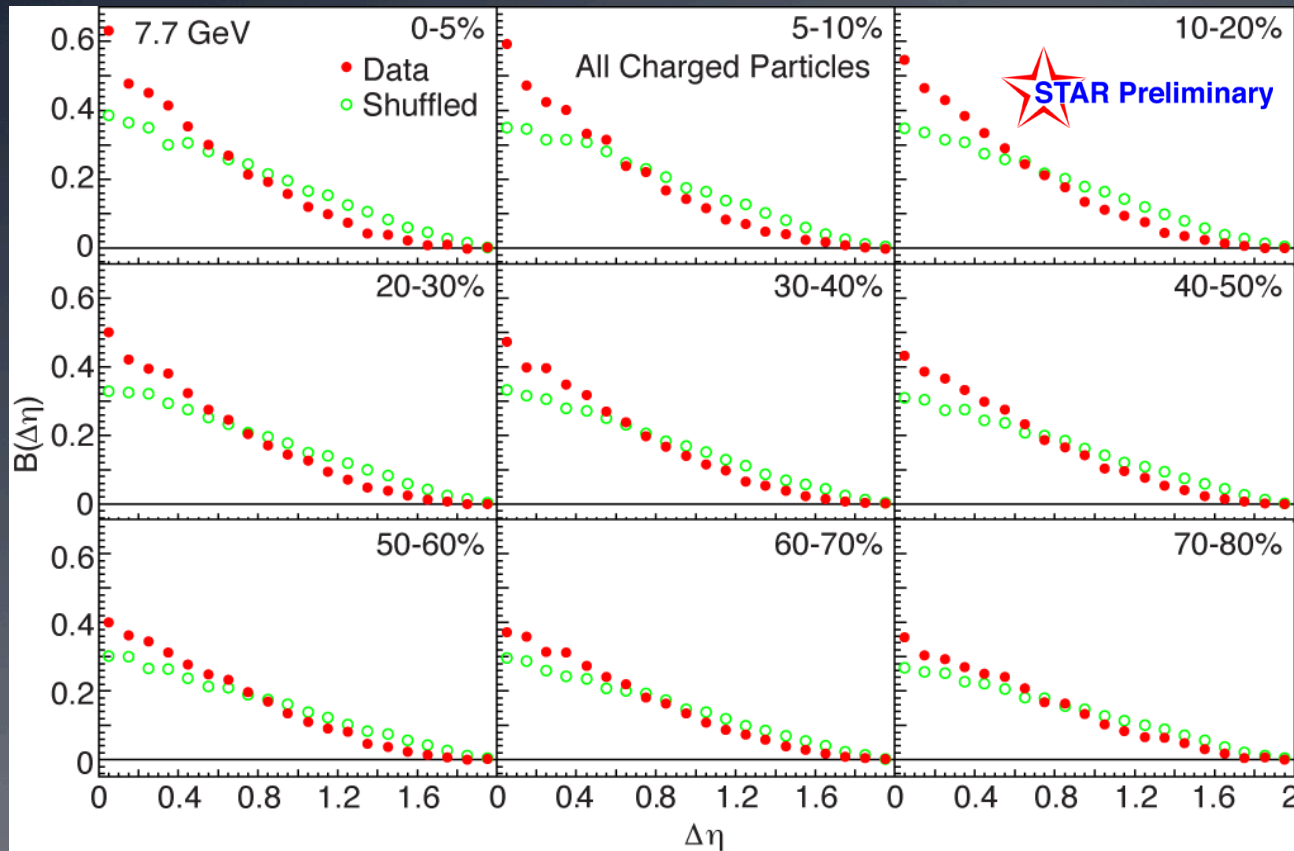
# Balance Function for $\Delta\eta$



- 11 GeV
- 9 Centralities
- Data are narrower than shuffled events
- Data narrow in central collisions

$$B(\Delta\eta) = \frac{1}{2} \left\{ \frac{N_{+-}(\Delta\eta) - N_{++}(\Delta\eta)}{N_+} + \frac{N_{-+}(\Delta\eta) - N_{--}(\Delta\eta)}{N_-} \right\}$$

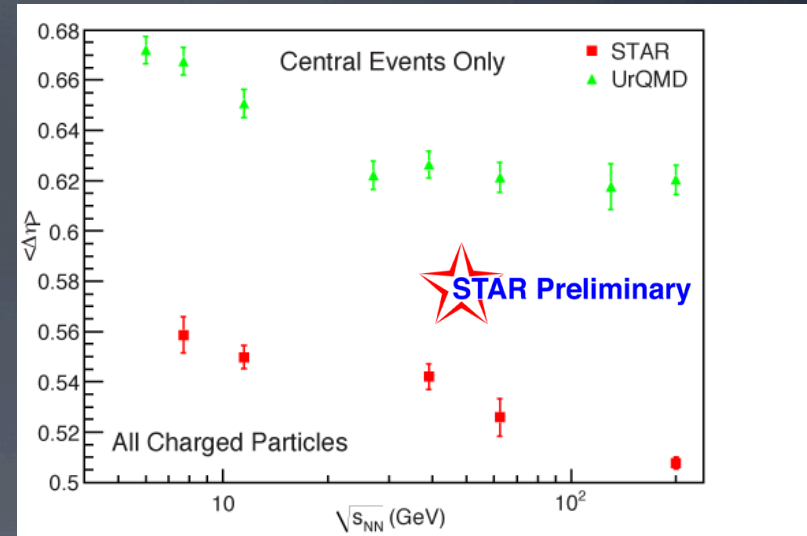
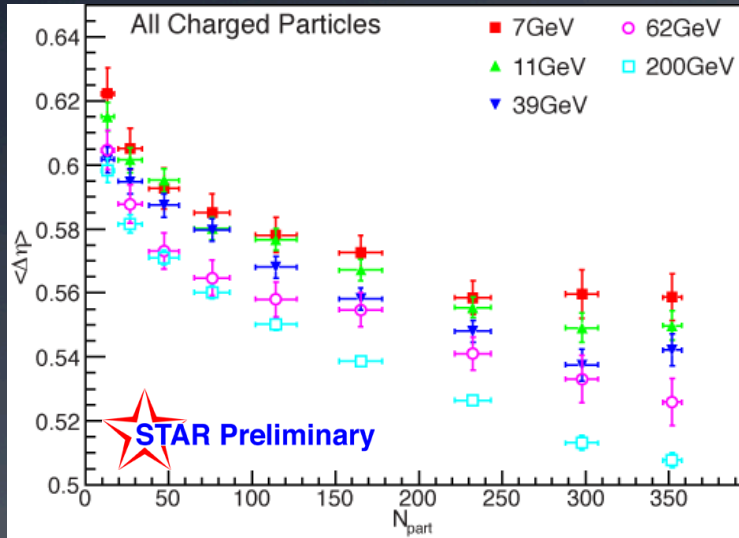
# Balance Function for $\Delta\eta$



- 7.7 GeV
- 9 Centralities
- Data are narrower than shuffled events
- Data narrow in central collisions

$$B(\Delta\eta) = \frac{1}{2} \left\{ \frac{N_{+-}(\Delta\eta) - N_{++}(\Delta\eta)}{N_+} + \frac{N_{-+}(\Delta\eta) - N_{--}(\Delta\eta)}{N_-} \right\}$$

# $\langle \Delta\eta \rangle$

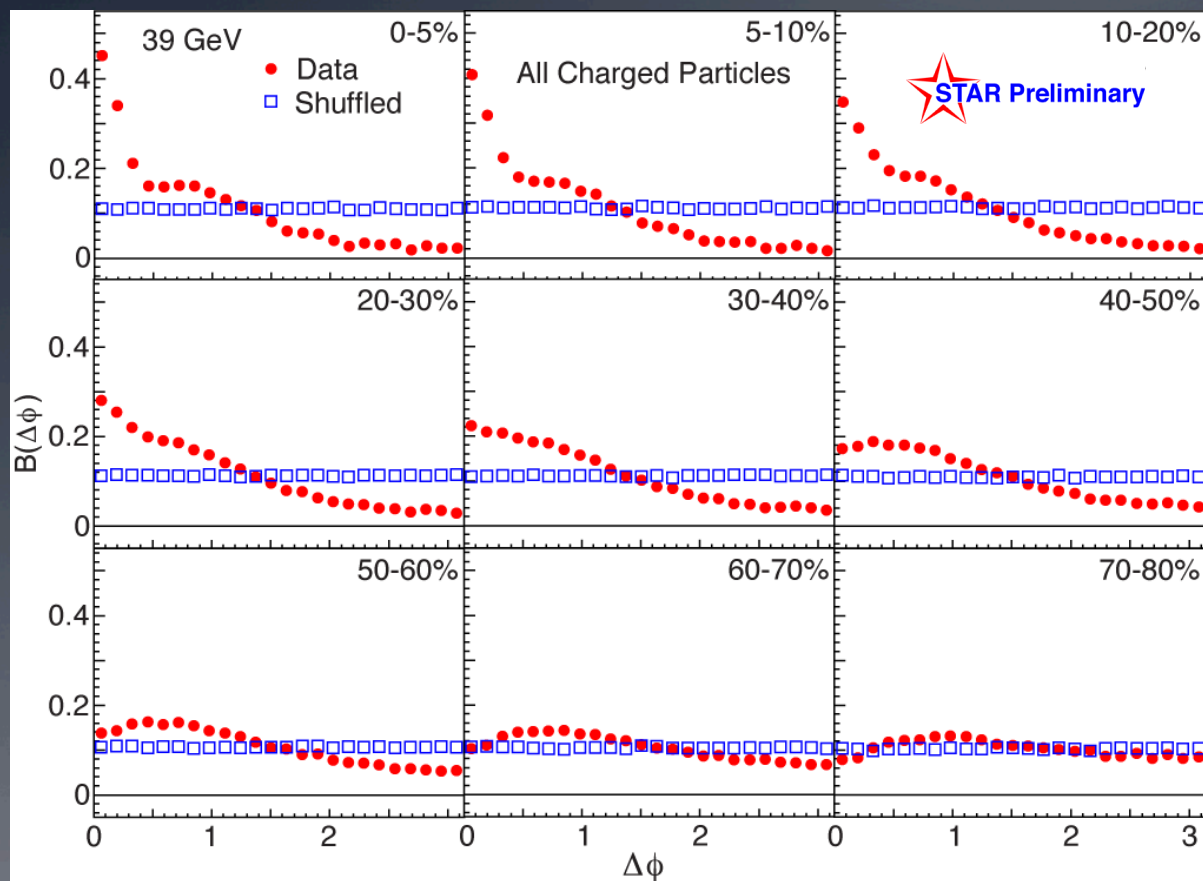


- Narrows in central collision and at higher energy
- Due to later hadronization time and stronger radial flow

$$\langle \Delta\eta \rangle = \frac{\sum B(\Delta\eta)\Delta\eta}{\sum B(\Delta\eta)}$$

- UrQMD is wider than the data
- UrQMD assumes early charge creation and little flow

# Balance Function for $\Delta\phi$

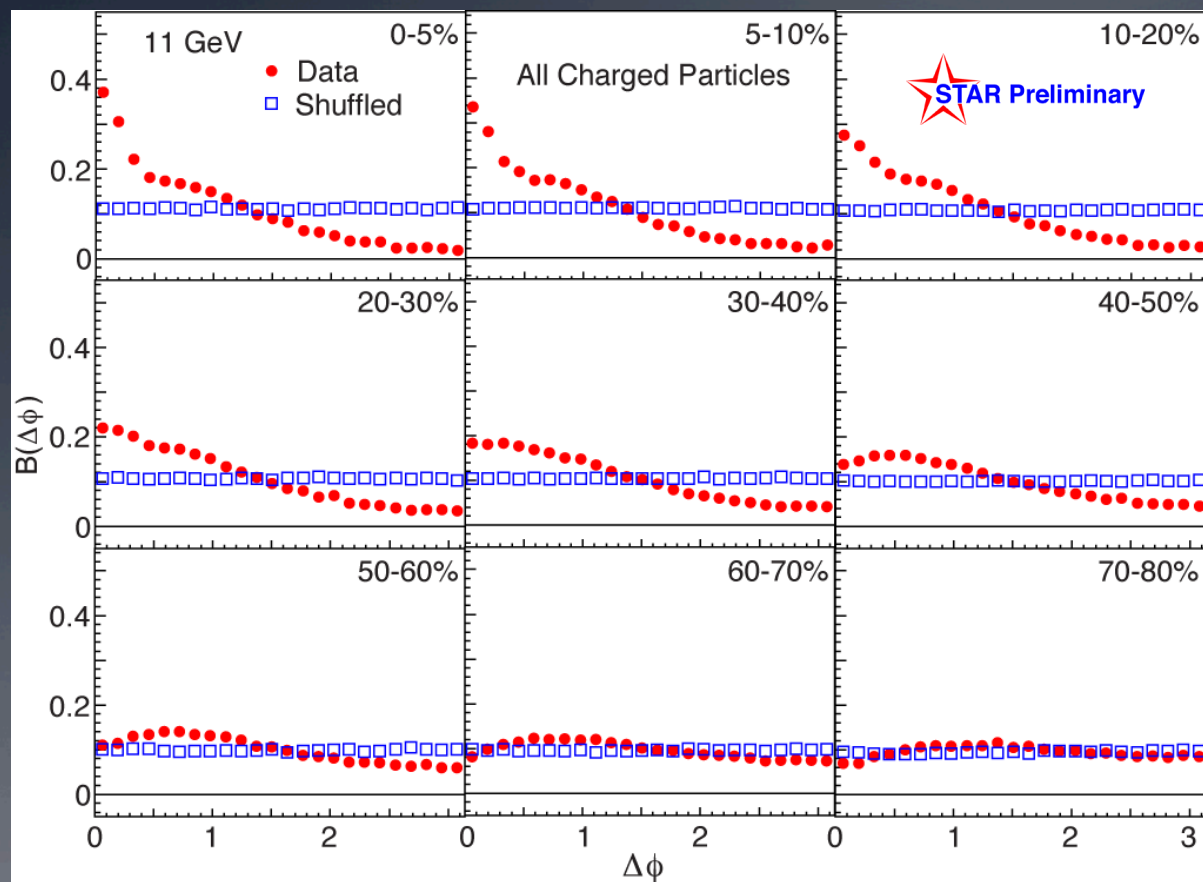


- 39 GeV
- 9 Centralities
- Data show a peak in central collision
- Lowest 3 bins show strong correlation

$$B(\Delta\phi) = \frac{1}{2} \left\{ \frac{N_{+-}(\Delta\phi) - N_{++}(\Delta\phi)}{N_+} + \frac{N_{-+}(\Delta\phi) - N_{--}(\Delta\phi)}{N_-} \right\}$$



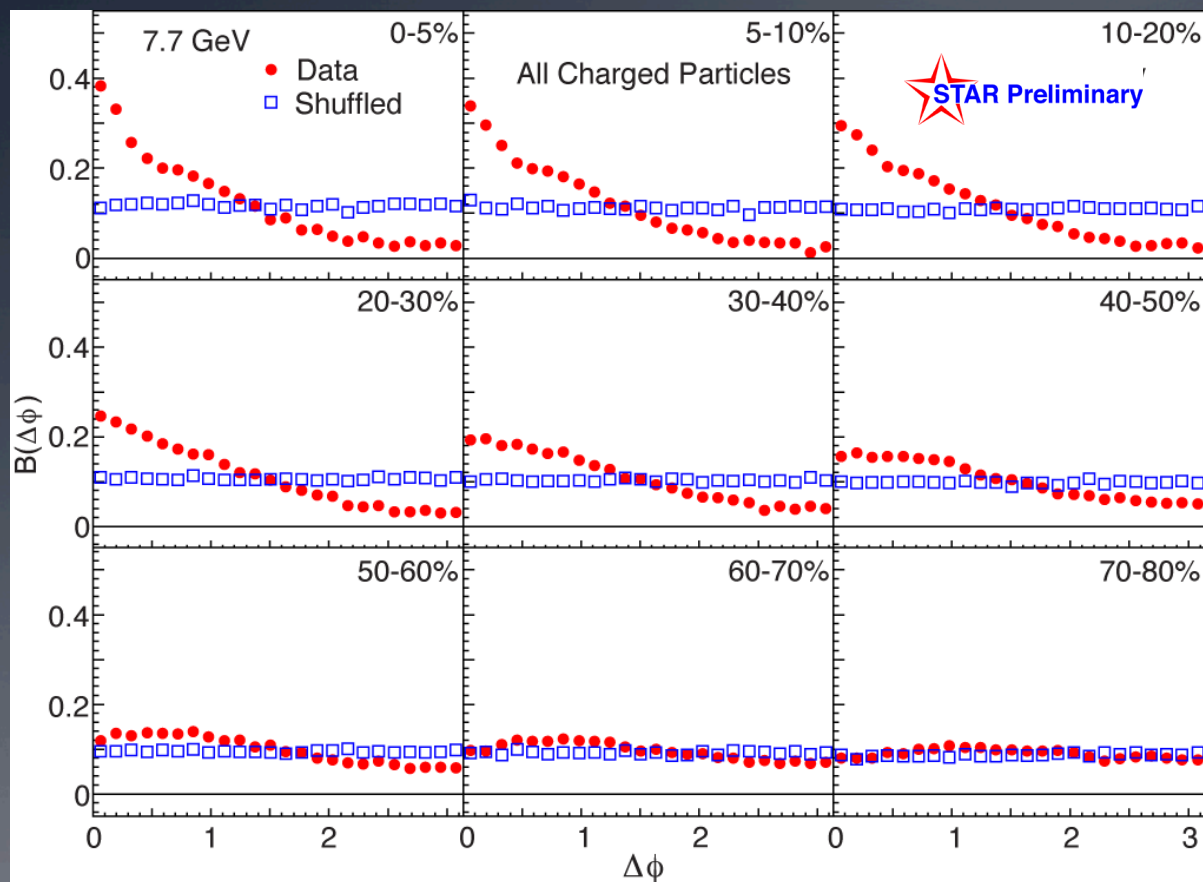
# Balance Function for $\Delta\phi$



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$$B(\Delta\phi) = \frac{1}{2} \left\{ \frac{N_{+-}(\Delta\phi) - N_{++}(\Delta\phi)}{N_+} + \frac{N_{-+}(\Delta\phi) - N_{--}(\Delta\phi)}{N_-} \right\}$$

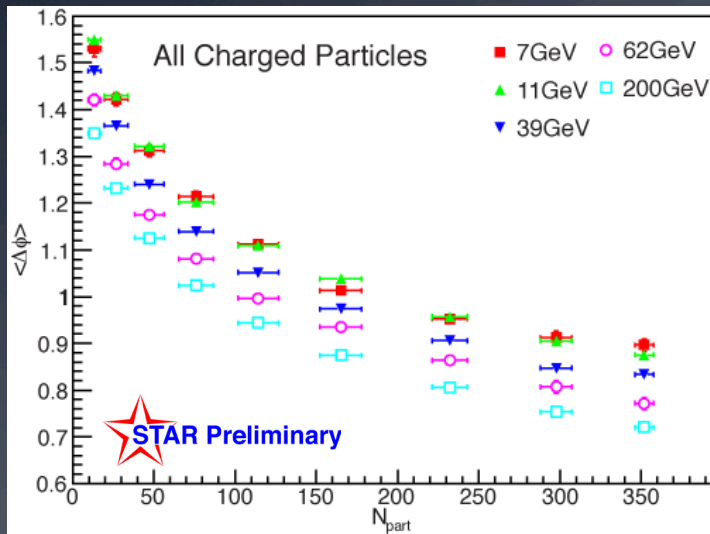
# Balance Function for $\Delta\phi$



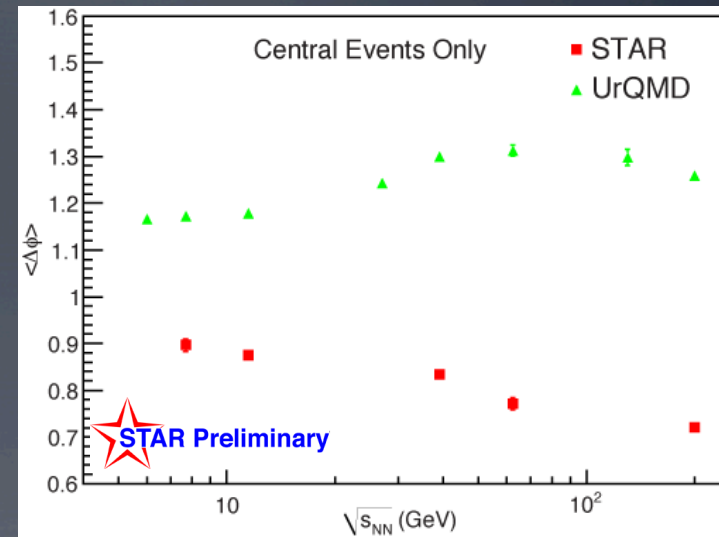
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$$\langle \Delta\phi \rangle$$

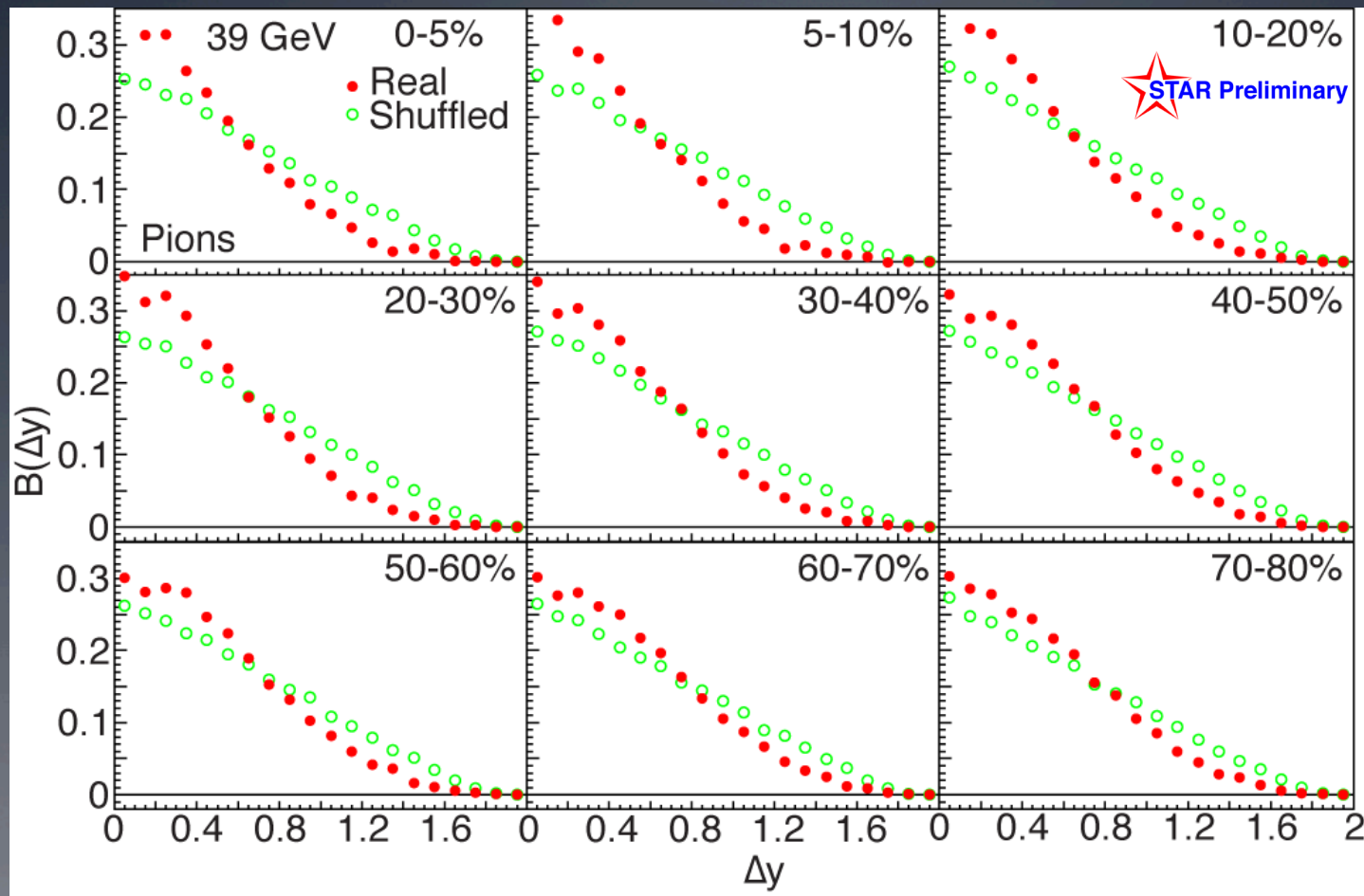


- Narrows in central collision and higher energy
- Due to later hadronization time and stronger radial flow

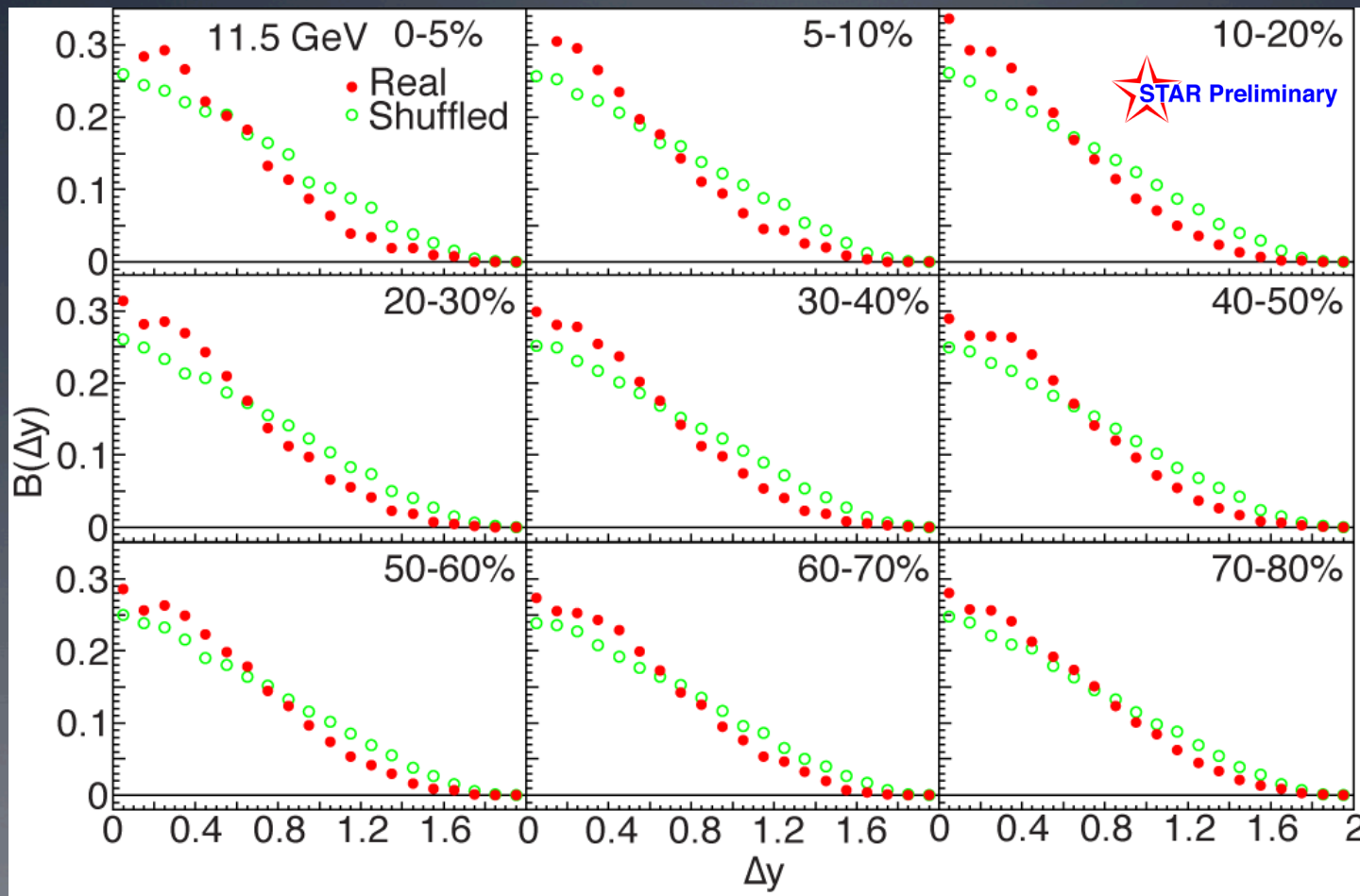


- UrQMD is wider than data
- UrQMD narrows at lower energy

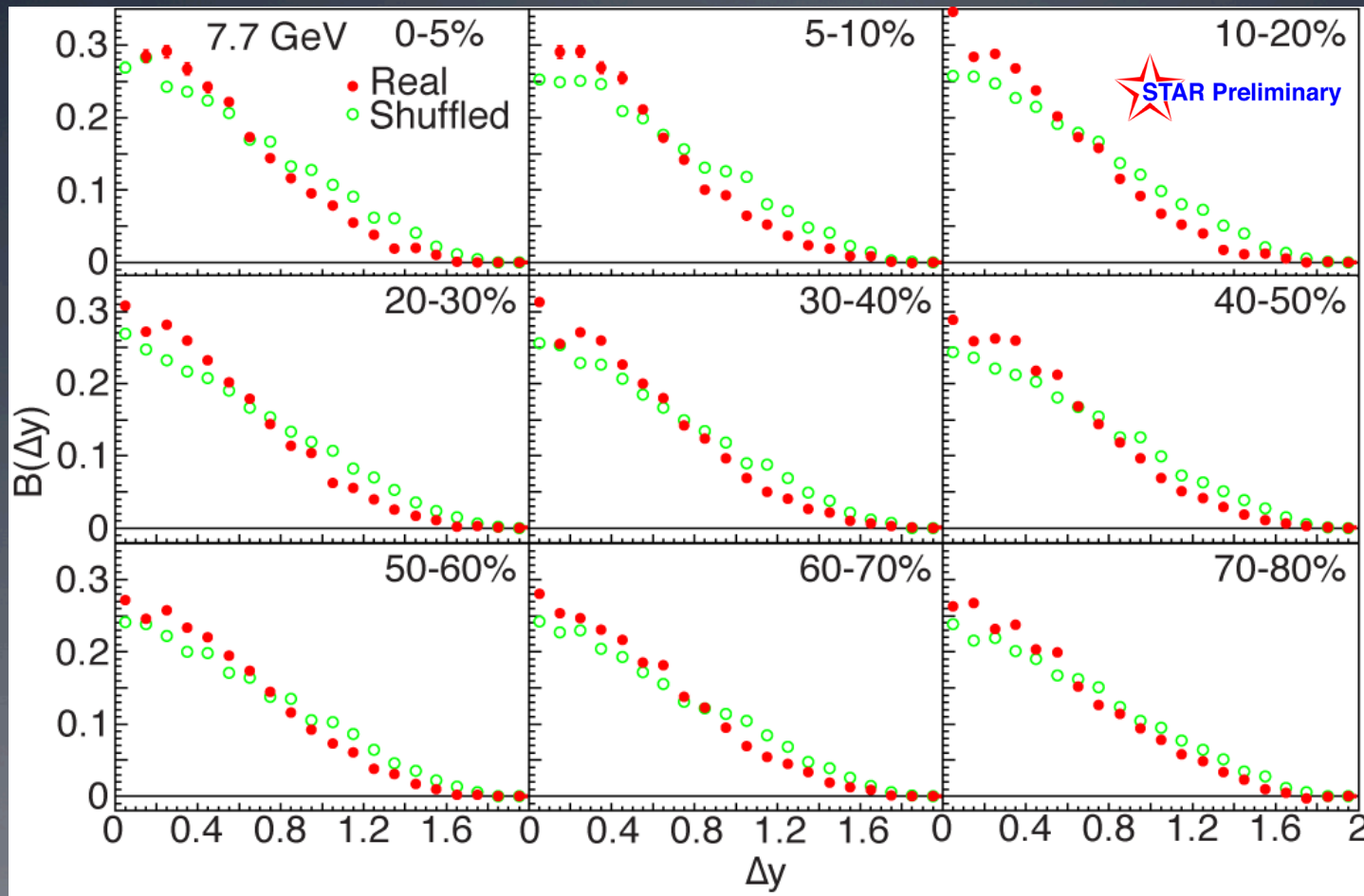
# Balance Function for Pions



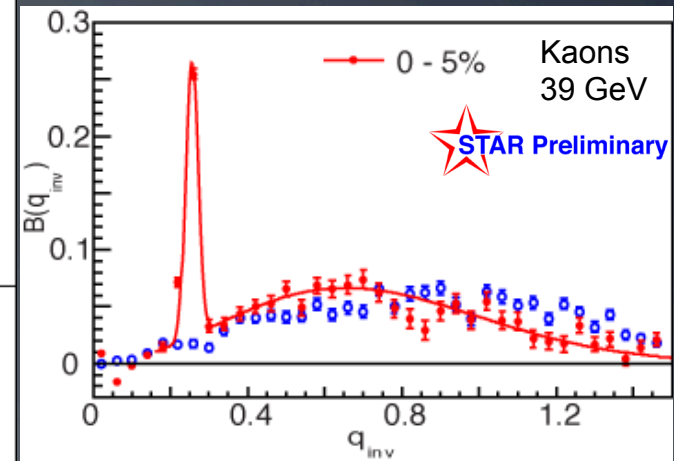
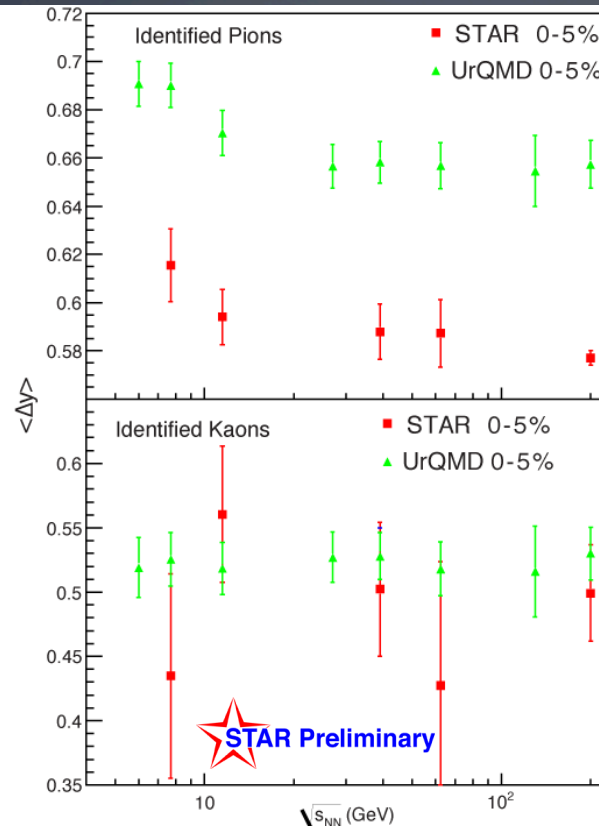
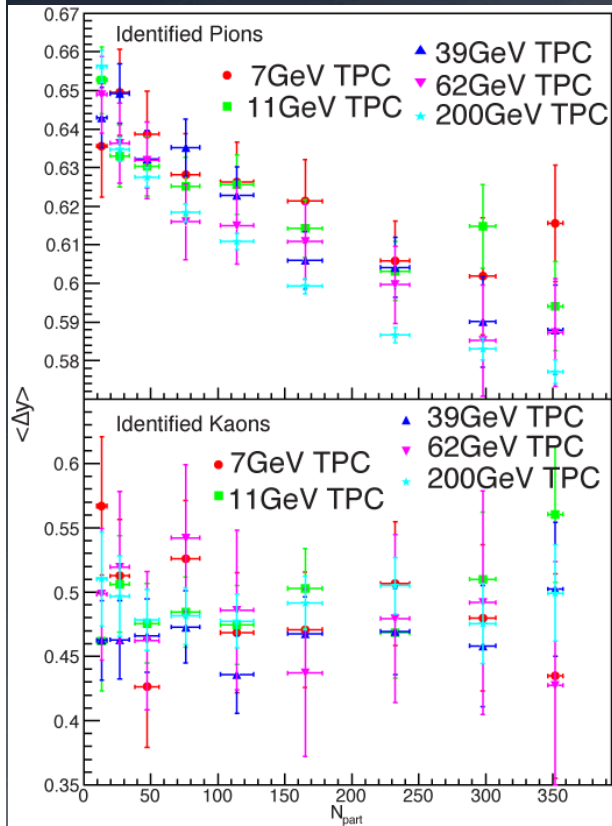
# Balance Function for Pions



# Balance Function for Pions



$$\langle \Delta y \rangle$$



Kaon balance function is dominated by  $\phi$  decay

- Balance functions for pions narrow in central collision and higher energy
- Balance functions for kaons do not narrow

# Summary - I

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- Balance functions show strong event plane dependence
  - Signature of elliptic flow
  
- Balance functions can reproduce most of the measured charge-dependent azimuthal correlations
  - Charge conservation
  - Flow effect



# Summary - II

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- Balance functions narrow in central collisions and at higher collision energies
  - Radial flow effect
  - Later hadronization time
  
- Balance function for identified Kaons do not narrow
  - Dominated by  $\phi$  decay

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# Back Up

# Data Set

Energy (GeV)	Species	Year	Events (M)*	$ V_z $ cut (cm)
200	Au + Au	Run 7	48	15
62.4	Au + Au	Run 4	4	15
39	Au + Au	Run 10	10	30
11.5	Au + Au	Run 10	12	30
7.7	Au + Au	Run 10	4	70

\*Number of events used in balance function calculation

- All Charge Particles

$$|\eta| < 1.0$$

$$0.2 < p_t < 2.0 \text{ GeV}/c$$

- Identified Particles

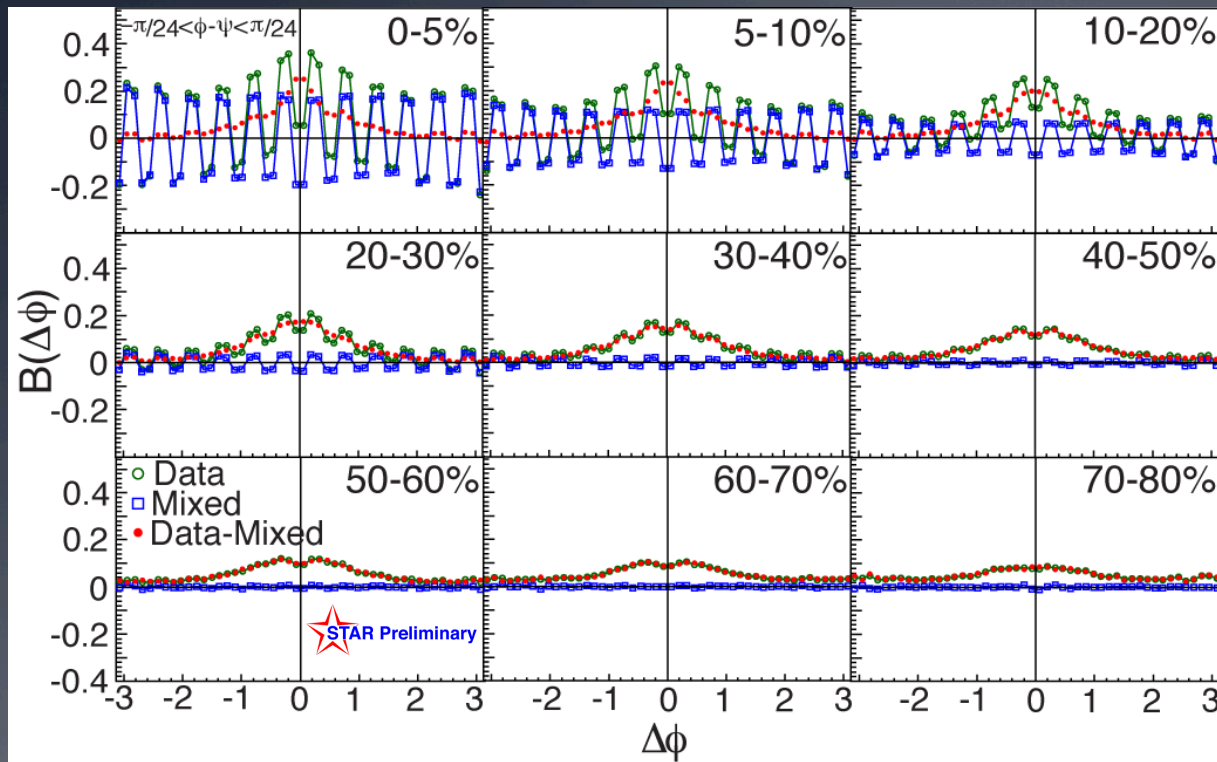
$$|\eta| < 1.0$$

TPC PID

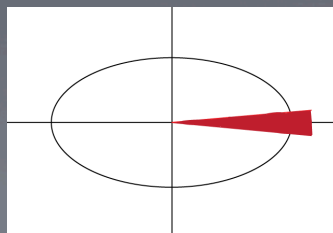
$$\pi: \quad n_{\sigma\pi} < 2.0, \quad n_{\sigma K} > 2.0, \quad 0.2 < p_t < 0.6$$

$$K: \quad n_{\sigma\pi} > 2.0, \quad n_{\sigma K} < 2.0, \quad 0.2 < p_t < 0.6$$

# Sector Boundary Effect

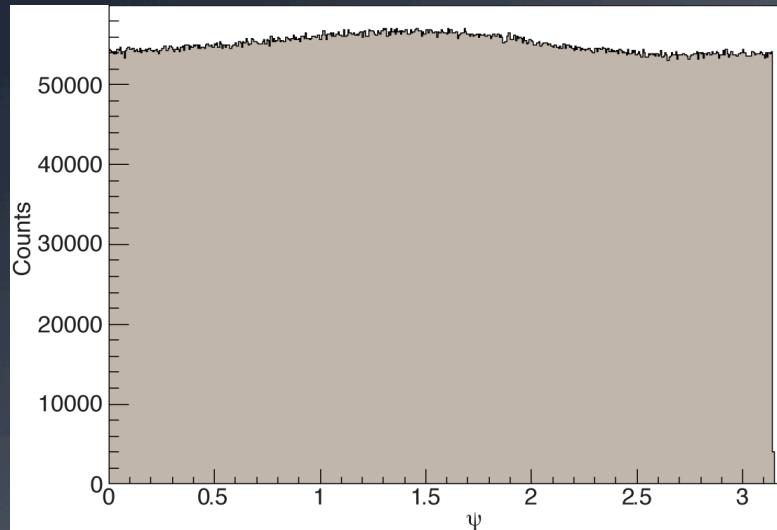


- Au+Au 200 GeV
- In plane balance function
- Mixed events are not zero due to sector boundaries
- Still some residual effects after subtraction



$$-7.5^\circ < \phi - \psi < 7.5^\circ$$

# Event Plane



- Use second harmonic event plane

$$\psi_2 = \left( \tan^{-1} \frac{\sum_i w_i \sin(2\phi_i)}{\sum_i w_i \cos(2\phi_i)} \right) / 2$$

- Apply  $\Phi$  weight and pt weight

- $\Phi$  weight are calculated run by run, centrality by centrality
- Use pt as weight when fill  $\Phi$  histogram

