

# Dynamics of particle emission probed by femtoscopic correlations at the STAR experiment

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Partially funded by:



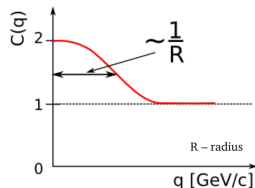
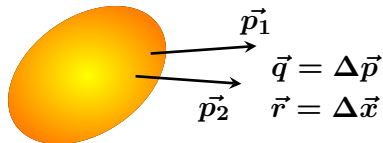
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Science



NATIONAL SCIENCE CENTRE  
POLAND

**Workshop on Particle Correlation and Femtoscopy**  
East Lansing, Michigan, July 18-22, 2022

# Femtoscopy



calculate size ( $R$ ) of the source

$$C(\vec{p}_1, \vec{p}_2) = \frac{P_{12}(\vec{p}_1, \vec{p}_2)}{P_1(\vec{p}_1)P_1'(\vec{p}_2)}$$

experiment

theory (models)

$$C(\vec{q}) = \frac{A(\vec{q})}{B(\vec{q})}$$

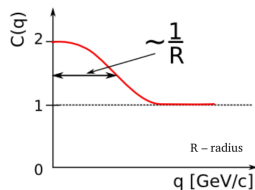
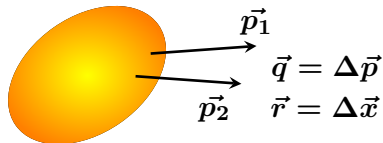
$$C(\vec{q}) = \int d^3r S(\vec{r}) |\Psi(\vec{q}, \vec{r})|^2$$

$A(\vec{q})$  - correlated  
 $B(\vec{q})$  - uncorrelated

$S(\vec{r})$  - source function  
 (distribution of relative positions of particles)

$\Psi(\vec{q}, \vec{r})$  - pair wave function  
 (describes interactions between particles)

# Femtoscscopy



calculate size (R) of the source

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experiment

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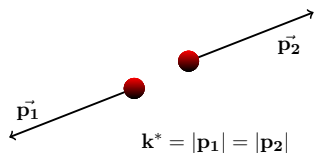
$$C(\vec{q}) = \int d^3r S(\vec{r}) |\Psi(\vec{q}, \vec{r})|^2$$

$$S(\vec{r}) = \exp\left(-\frac{(r_{out} - \mu_{out})^2}{R_{out}^2} - \frac{r_{side}^2}{R_{side}^2} - \frac{r_{long}^2}{R_{long}^2}\right)$$

$\mu_{out}$  — asymmetry in the *outward* direction

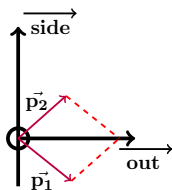
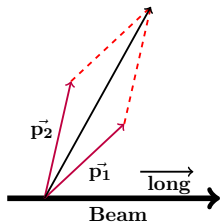
# Reference frame

## Pair Rest Frame (PRF)



## Longitudinally Co-Moving System (LCMS)

G. Bertsch, et al. S. Pratt.  
Phys. Rev. C37, 1896, (1988) Phys. Rev. D33, 1314 (1986)



**Long:** determined by the beam axis

**Out:** determined by the direction of the pair momentum in the transverse plane

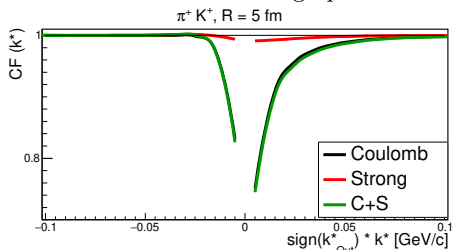
**Side:** perpendicular to the long and out axes

# Final State Interactions (FSI)

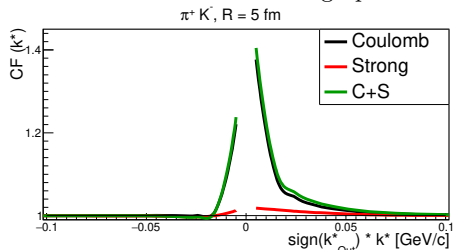
The shape of non-identical particle CF depends on FSI:

- Strong interaction
- *Coulomb force*
- ~~Quantum Statistic effect~~

Correlation between like-sign pairs



Correlation between unlike-sign pairs



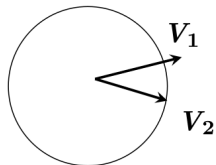
\*Theoretical functions using Lednicky weights

\*\*Source assumed as a 3-dimensional Gauss distribution

# Space-time asymmetry

Time asymmetry

$$t_1 \neq t_2$$
$$\Delta r = 0$$

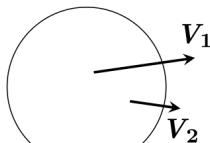


$t_1 > t_2$  - Catching up

$t_1 < t_2$  - Run away

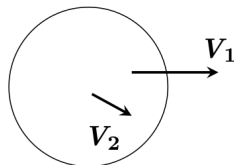
Space asymmetry

$$t_1 = t_2$$
$$\Delta r \neq 0$$



Catching up

$$t_1 = t_2$$
$$\Delta r \neq 0$$



Run away

$t$  — emission time

$r$  — emission point distance from the center

R. Lednicky, et al.,  
Phys. Lett. B373,  
30-34 (1996)

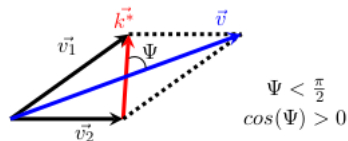
**Catching up**  
longer interaction, strong  
correlation

**Running away**  
shorter interaction,  
weaker correlation

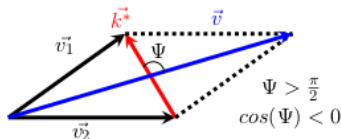
## Double ratio method

CFs are calculated in two groups of pairs:

$C_+(k^*)$  — lighter particle is faster  
( $\cos(\Psi) > 0$ )



$C_-(k^*)$  — heavier particle is faster  
( $\cos(\Psi) < 0$ )



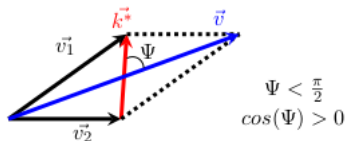
$C_+$  shows a larger deviation from unity than  $C_-$  → particles are not emitted at the same place and/or time

$C_+$  and  $C_-$  are identical → the average space-time emission points of both types of particles

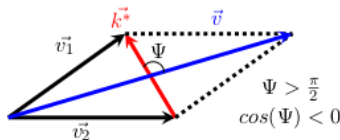
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Double ratio:

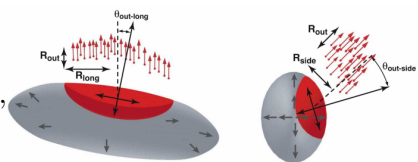
$$DR(k^*) = \frac{C_+(k^*)}{C_-(k^*)}$$



# Emission asymmetries

Collective behavior

- **radial flow** in the transverse plane:  
matter is collectively moving "outward"  
from the central axis of the source  
to the outside



*Ann. Rev. Nucl. Part. Sci 55, 357 (2005)*

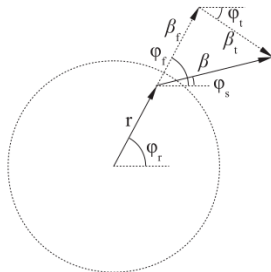
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$\beta_f$  - flow velocity

$\beta_t$  - thermal velocity (with random direction)



*Nonidentical-particle femtoscopy at  $\sqrt{s_{NN}} = 200$  GeV  
in hydrodynamics with statistical hadronization*, A. Kisiel  
Phys. Rev. C 81, 064906 (2010)

Space-momentum (x-p) correlation:  
direction  $\phi_f$  of transverse velocity is aligned with transverse  
position vector direction  $\phi_r$

# Emission asymmetries

Collective behavior

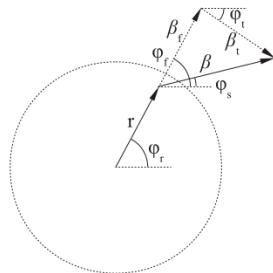
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The thermal component has  
a smaller impact on heavier particles

The final velocity direction of lighter particles,  
on average,  
is less correlated with emission points than that of heavier particles



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$$\langle x_{out} \rangle = \frac{\langle r\beta_f \rangle}{\langle \sqrt{\beta_t^2 + \beta_f^2} \rangle} = \frac{r_0\beta_0\beta}{\beta_0^2 + T/m_T}$$

where:  $\beta_f = \beta_0 \frac{r}{r_0}$

# Emission asymmetries

Collective behavior

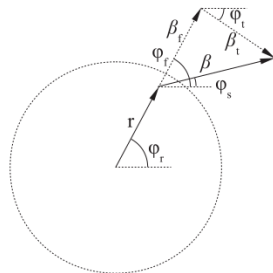
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**Emission asymmetry arises in a system where both thermal and  
collective velocities exist and are comparable in magnitude**

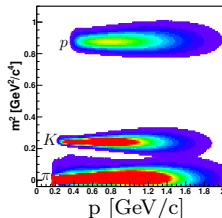
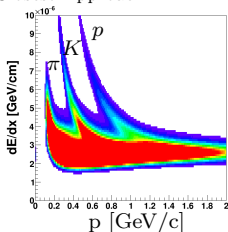
## Particle identification

# Data selection

Au+Au collisions at  $\sqrt{s_{NN}} = 39$  GeV, 0-10%

|   | $\pi$         | K            | p            |
|---|---------------|--------------|--------------|
| $p_T$ [GeV/c]                             | [0.1, 1.2]    | [0.1, 1.2]   | [0.4, 2.5]   |
| p [GeV/c]                                 | [0.1, 1.2]    | [0.1, 1.2]   | [0.4, 3.0]   |
| $ N\sigma $                               | < 3.0         |              |              |
| Z [cm]                                    | [-30.0, 30.0] |              |              |
| $ \eta $                                  | < 0.5         |              |              |
| $m^2$ [GeV <sup>2</sup> /c <sup>4</sup> ] | [0.01, 0.03]  | [0.21, 0.28] | [0.76, 1.03] |
| DCA [cm]                                  | < 3.0         |              |              |

DCA - Distance of Closest Approach



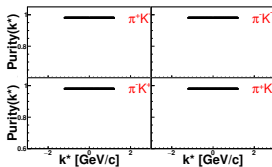
# Data selection

|                       | $\pi$ | K    | p   |
|-----------------------|-------|------|-----|
| ToF threshold [GeV/c] | 0.2   | 0.41 | 0.8 |

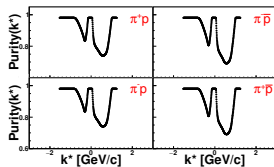
- $p > \text{ToF threshold} \Rightarrow \text{TPC} + \text{ToF}$   
 $p < \text{ToF threshold and information from ToF} \Rightarrow \text{TPC} + \text{ToF}$   
 $p < \text{ToF threshold and no information from ToF} \Rightarrow \text{TPC}$
- 

## Pair purity:

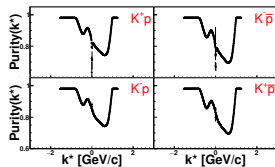
$$\pi^\pm K^\pm$$



$$\pi^\pm p/\bar{p}$$



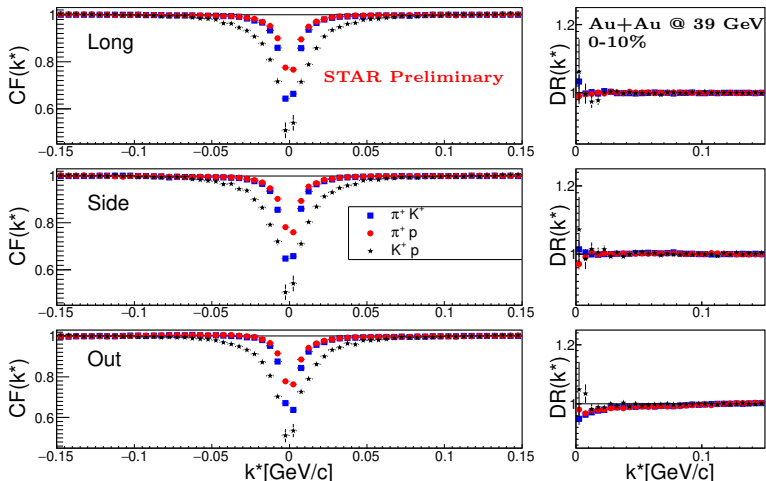
$$K^\pm p/\bar{p}$$



System dependence  
of nonidentical particle correlations



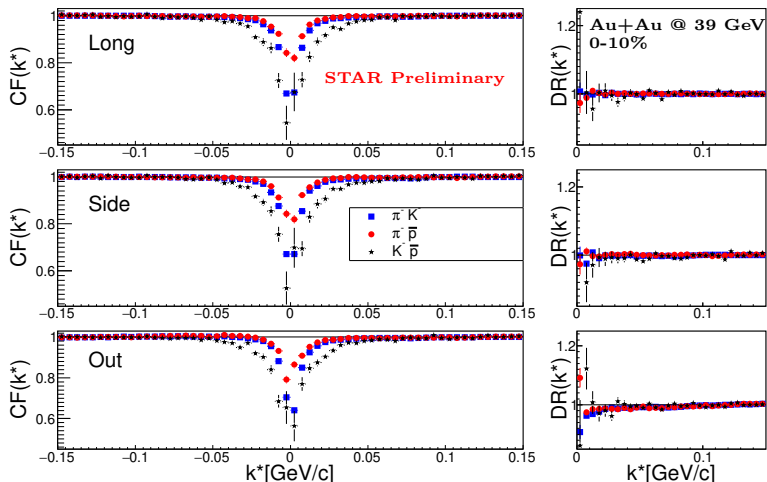
# System comparison ++



- Like sign pairs are dominated by Coulomb interaction

- $Kp \rightarrow$  strongest correlation
- Visible signal of emission asymmetry

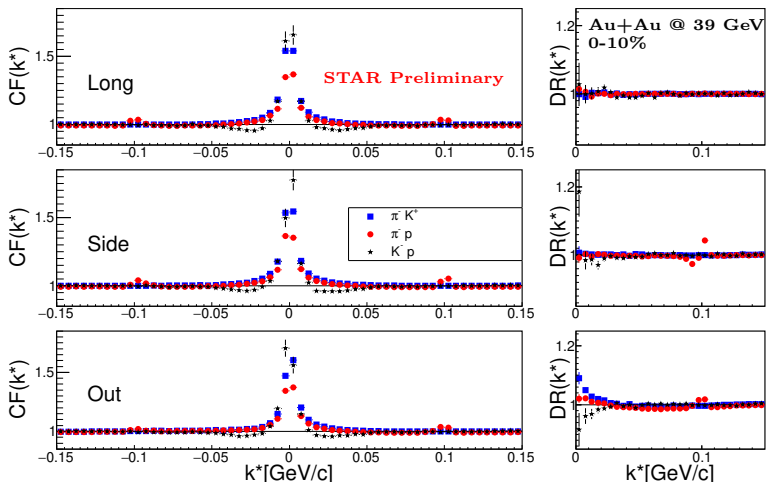
# System comparison —



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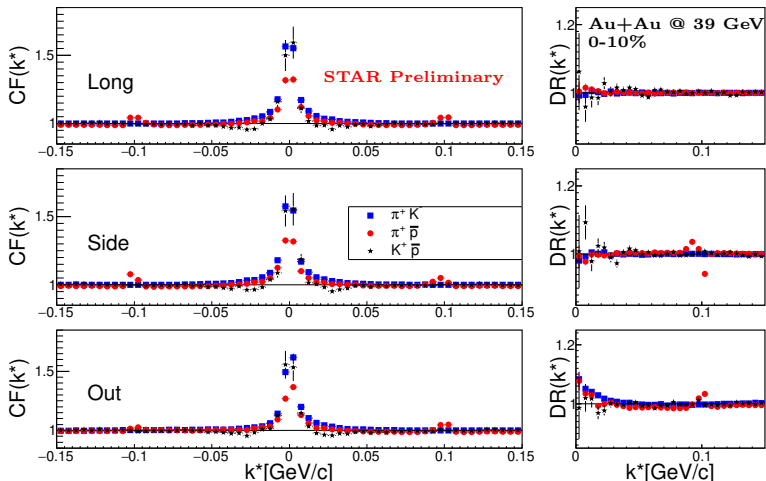
- $Kp \rightarrow$  strongest correlation
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# System comparison $-+$



- Strong interaction not negligible in  $K^- p / K^+ \bar{p}$
- $\Lambda$  peak visible in  $\pi^- p / \pi^+ \bar{p}$
- Visible signal of emission asymmetry

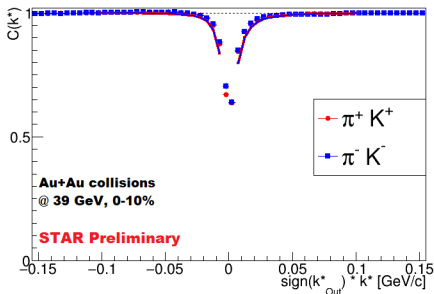
# System comparison $+-$



- Strong interaction not negligible in  $K^- p / K^+ \bar{p}$

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- Visible signal of emission asymmetry

# $\pi K$ fits



$$\pi^+ K^+$$

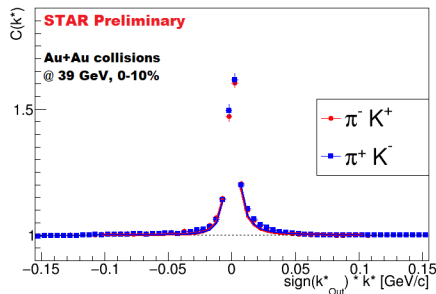
$$R = 9.2 \pm 0.8 \pm 0.7 \text{ fm}$$

$$\mu = -4.8 \pm 0.6 \pm 1.0 \text{ fm}$$

$$\pi^- K^-$$

$$R = 9.0 \pm 0.7 \pm 0.8 \text{ fm}$$

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$$\pi^- K^+$$

$$R = 12.2 \pm 0.7 \pm 0.7 \text{ fm}$$

$$\mu = -4.5 \pm 0.6 \pm 0.9 \text{ fm}$$

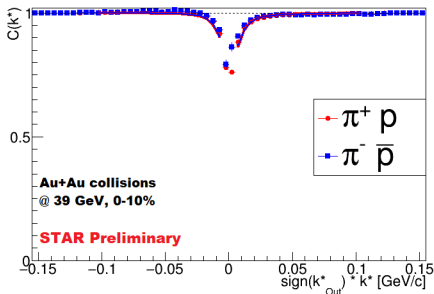
$$\pi^+ K^-$$

$$R = 11.8 \pm 0.8 \pm 0.7 \text{ fm}$$

$$\mu = -6.1 \pm 0.7 \pm 1.1 \text{ fm}$$

- Difference between source sizes for like and unlike sign pairs
- Influence of resonance decays?

# $\pi p(\bar{p})$ fits



$$\pi^+ p$$

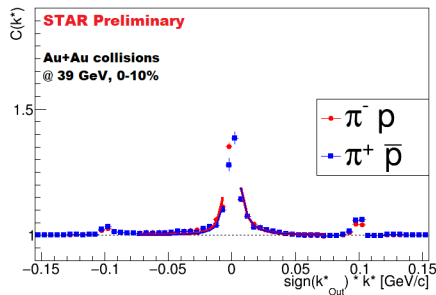
$$R = 11.9 \pm 1.7 \pm 1.2 \text{ fm}$$

$$\mu = -3.0 \pm 0.7 \pm 0.6 \text{ fm}$$

$$\pi^- \bar{p}$$

$$R = 11.9 \pm 0.7 \pm 0.8 \text{ fm}$$

$$\mu = -6.0 \pm 2.9 \pm 1.7 \text{ fm}$$



$$\pi^- p$$

$$R = 11.9 \pm 1.4 \pm 0.8 \text{ fm}$$

$$\mu = -4.0 \pm 2.9 \pm 0.8 \text{ fm}$$

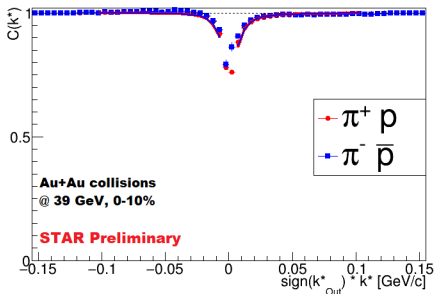
$$\pi^+ \bar{p}$$

$$R = 12.5 \pm 1.0 \pm 0.9 \text{ fm}$$

$$\mu = -6.5 \pm 1.5 \pm 1.0 \text{ fm}$$

- Source sizes comparable for like and unlike sign pairs
- Difference between asymmetry sizes for  $p$  and  $\bar{p}$  pairs

# $\pi p(\bar{p})$ fits



$$\pi^+ p$$

$$R = 11.9 \pm 1.7 \pm 1.2 \text{ fm}$$

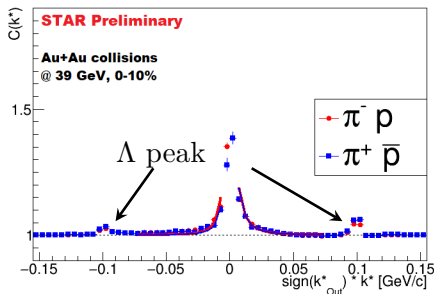
$$\mu = -3.0 \pm 0.7 \pm 0.6 \text{ fm}$$

$$\pi^- \bar{p}$$

$$R = 11.9 \pm 0.7 \pm 0.8 \text{ fm}$$

$$\mu = -6.0 \pm 2.9 \pm 1.7 \text{ fm}$$

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$$\pi^- p$$

$$R = 11.9 \pm 1.4 \pm 0.8 \text{ fm}$$

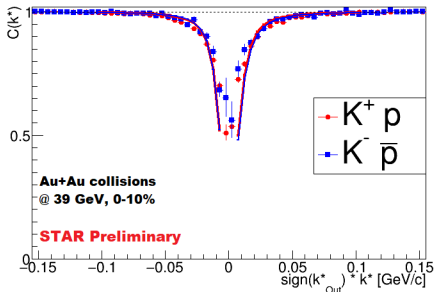
$$\mu = -4.0 \pm 2.9 \pm 0.8 \text{ fm}$$

$$\pi^+ \bar{p}$$

$$R = 12.5 \pm 1.0 \pm 0.9 \text{ fm}$$

$$\mu = -6.5 \pm 1.5 \pm 1.0 \text{ fm}$$

# $Kp(\bar{p})$ fits



$$K^+ p$$

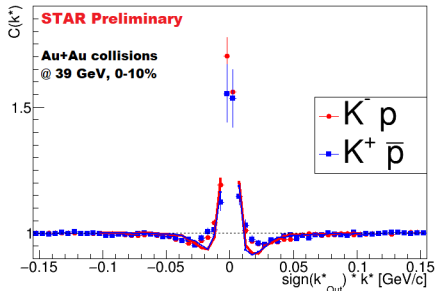
$$R = 7.5 \pm 0.3 \pm 1.7 \text{ fm}$$

$$\mu = -1.5 \pm 0.6 \pm 1.0 \text{ fm}$$

$$K^- \bar{p}$$

$$R = 9.0 \pm 1.0 \pm 1.2 \text{ fm}$$

$$\mu = -2.5 \pm 0.6 \pm 1.5 \text{ fm}$$



$$K^- p$$

$$R = 8.3 \pm 0.5 \pm 1.5 \text{ fm}$$

$$\mu = -0.5 \pm 0.7 \pm 0.7 \text{ fm}$$

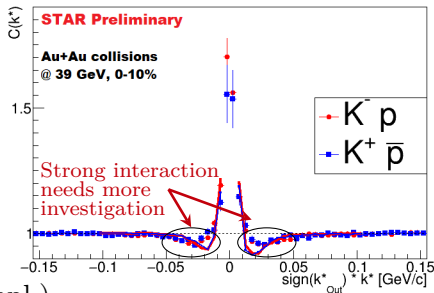
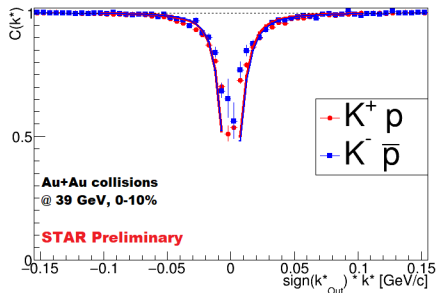
$$K^+ \bar{p}$$

$$R = 8.5 \pm 0.5 \pm 1.6 \text{ fm}$$

$$\mu = -0.5 \pm 0.6 \pm 1.0 \text{ fm}$$



# $Kp(\bar{p})$ fits



Lednicky code ( $K^- p$  s-wave scatt. ampl.)

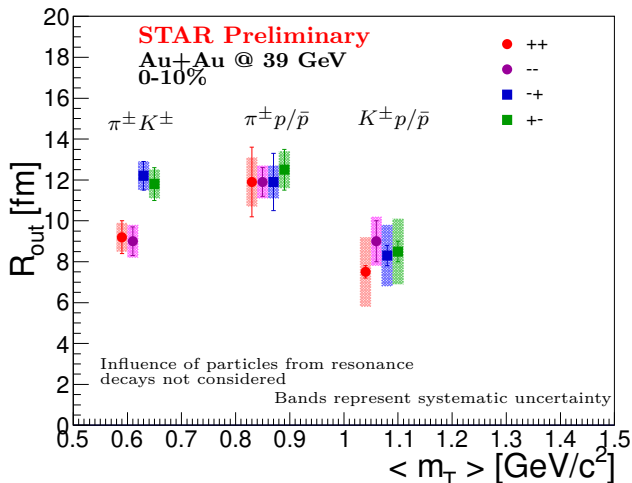
$$\Re a_{K^- p} = -1.05 \text{ fm}$$

$$\Im a_{K^- p} = 0.75 \text{ fm}$$

Values from

B. Borasoy, U.-G. Meißner, and R. Nißler,  
Phys. Rev. C 74, 055201 (2006)

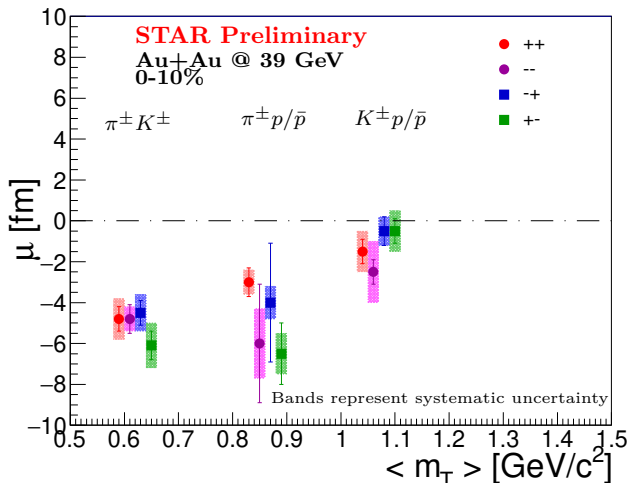
# Source size dependence on the system



- Similar source sizes for  $\pi K$ ,  $\pi p$ , and significantly smaller for  $K p$  expected ✓

A. Kisiel, Phys. Rev. C 81, 064906 (2010)

# Emission asymmetry dependence on the system



- Expected dependence:  $\mu_{\pi p} \gtrsim \mu_{\pi K} > \mu_{K p}$  ✓

A. Kisiel, Phys. Rev. C 81, 064906 (2010)

# Summary

- Asymmetry is visible in each kind of analyzed pair
- Lighter particles are emitted closer to the center and/or later (indicated by negative values of  $\mu$ )
- Model calculations are needed to estimate the influence of particles from resonance decays
- Pairs from lambda resonances have a negligible impact on the correlation effect
- Only kaon-proton  $C(k^*)$  has visible and significant strong interaction
  - ▶  $Kp$  strong interaction needs more investigation

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**Thank you for your attention!**