



# Higher-order Cumulants of Proton Multiplicity Distributions in Au+Au Collisions at $\sqrt{s_{NN}} = 3$ GeV from RHIC-STAR

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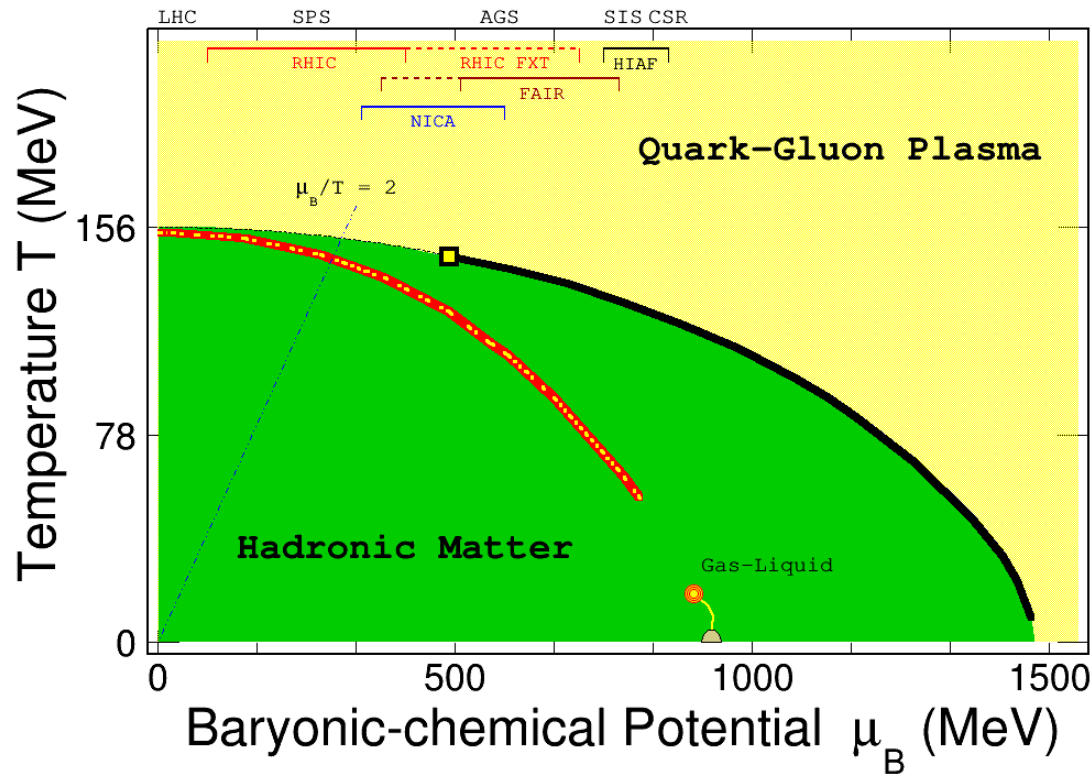


# Outline

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- Motivation
- STAR detector and fixed target program
- Analysis detail
  - Pileup effect
  - Volume fluctuation effect
- Summary

# QCD Phase Diagram



- Crossover at  $\mu_B = 0$  *Y. Aoki et al, Nature 443, 675(2006)*
- Models predict 1<sup>st</sup> order phase transition at non-zero  $\mu_B$
- Possible QCD critical point?
- Change collision energy to scan phase diagram

# Higher moments of conserved quantities

- Cumulants of conserved quantities (B, Q, S) are extensive variables (intensive when taken ratio)

$$\delta N = N - \langle N \rangle$$

$$C_1 = \langle N \rangle, C_2 = \langle (\delta N)^2 \rangle, C_3 = \langle (\delta N)^3 \rangle$$

$$C_4 = \langle (\delta N)^4 \rangle - 3\langle (\delta N)^2 \rangle^2$$

$$S = C_3 / (C_2)^{3/2}, \kappa = \frac{C_4}{(C_2)^2},$$

$$\frac{C_2}{C_1} = \frac{\sigma^2}{M}, \quad \frac{C_3}{C_2} = S\sigma, \quad \frac{C_4}{C_2} = \kappa\sigma^2$$

- Sensitive quantities to correlation length  $\xi$

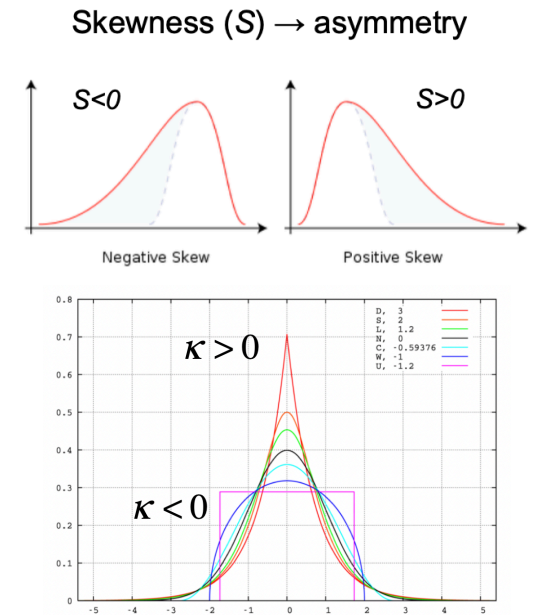
$$C_3 = \langle (\delta N)^3 \rangle \sim \xi^{4.5}$$

$$C_4 = \langle (\delta N)^4 \rangle - 3\langle (\delta N)^2 \rangle^2 \sim \xi^7$$

- directly related to susceptibility  $\chi$  of the system.

$$C_{n,q} = VT^3 \chi_q^{(n)} = \frac{\partial^n (p/T)}{\partial (\mu_q/T)^n}, \quad q = B, Q, S$$

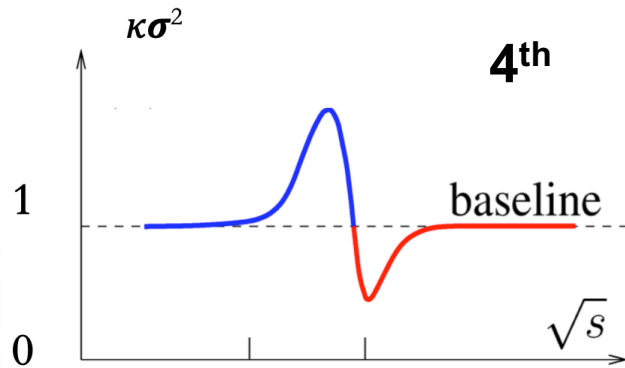
**Higher moments and ratios are sensitive to QCD phase structure.**



*M. A. Stephanov Phys. Rev. Lett. 102, 032301*

*M. Asakawa, S. Ejiri and M. Kitazawa, Phys. Rev. Lett. 103, 262301 (2009).*

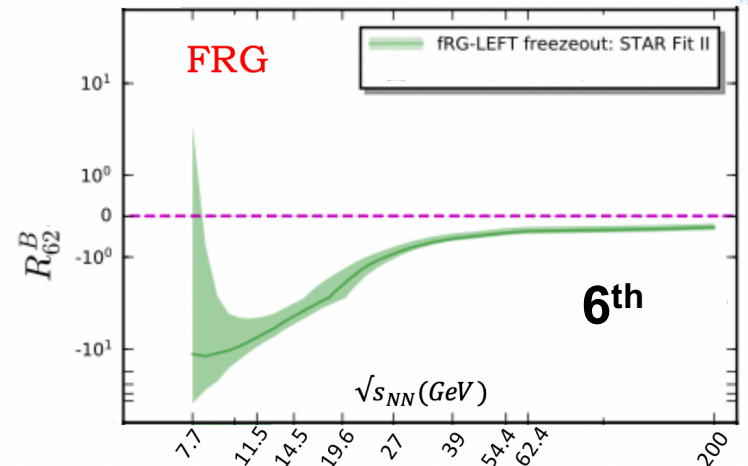
# Theoretical Expectations



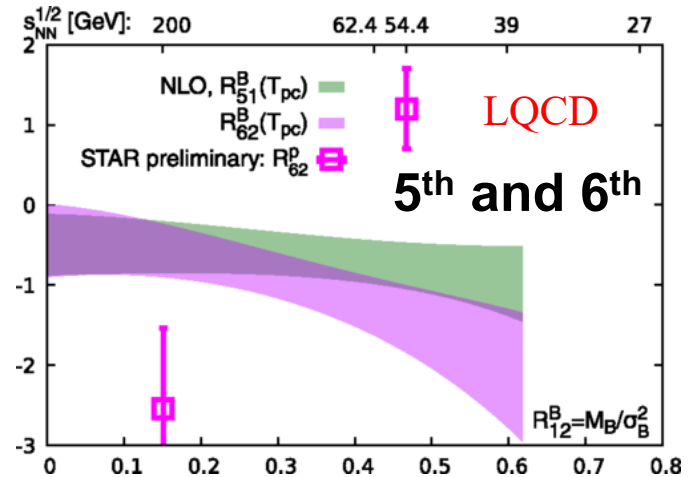
$\kappa\sigma^2 = 1$  (Poisson Fluctuations)

M.A.Stefanov,PRL107,052301(2011).  
 Schaefer, Wanger,PRD 85, 034027 (2012)  
 JW Chen et al., PRD93, 034037 (2016); PRD95,  
 014038 (2017).

- 4<sup>th</sup> order cumulant ratio shows non-monotonic energy dependence because of contribution from critical point
- 5<sup>th</sup> and 6<sup>th</sup> : Predicted to be negative by lattice QCD from 200 to 39 GeV ( $25 < \mu_B < 112$  MeV ); Positive for UrQMD and HRG model without QCD phase transition

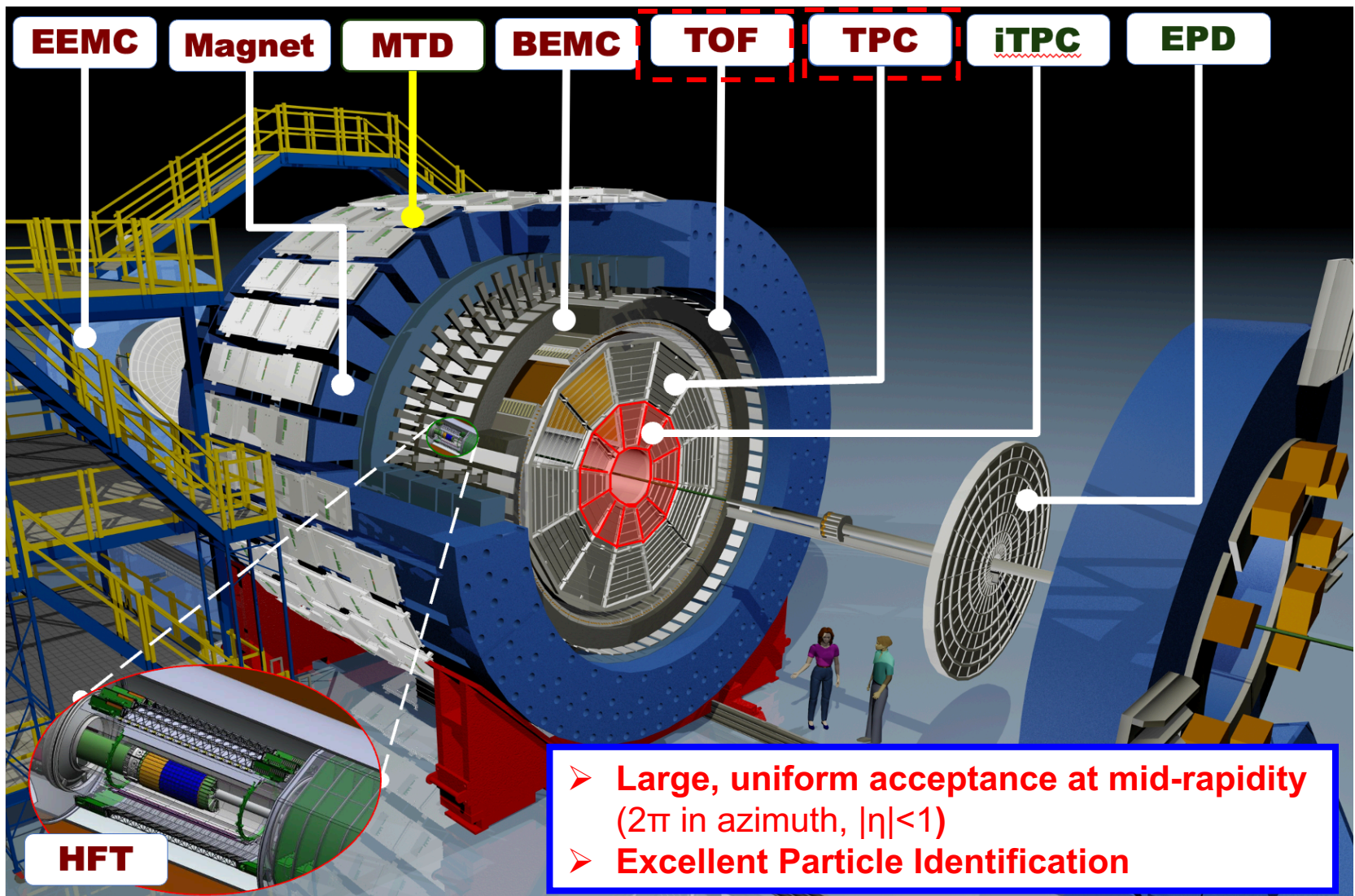


Wei-jieFu et al, arXiv:2101.06035

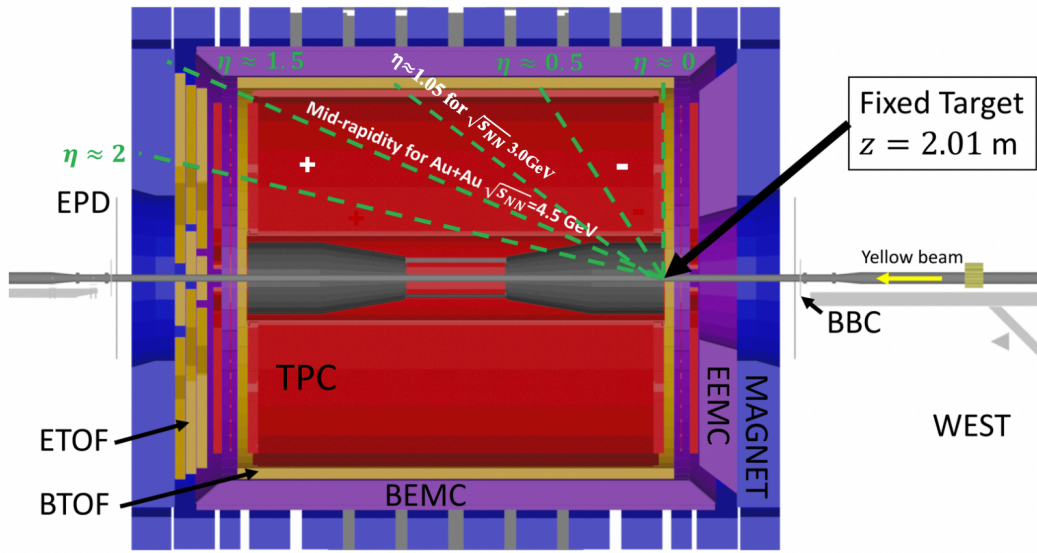


A. Bazavov et al. Phys. Rev. D **101**, 074502

# STAR Detector System



# STAR Fixed-target Experiment Setup and BES-II



**Extend the coverage of baryon chemical potential to 720 MeV !**

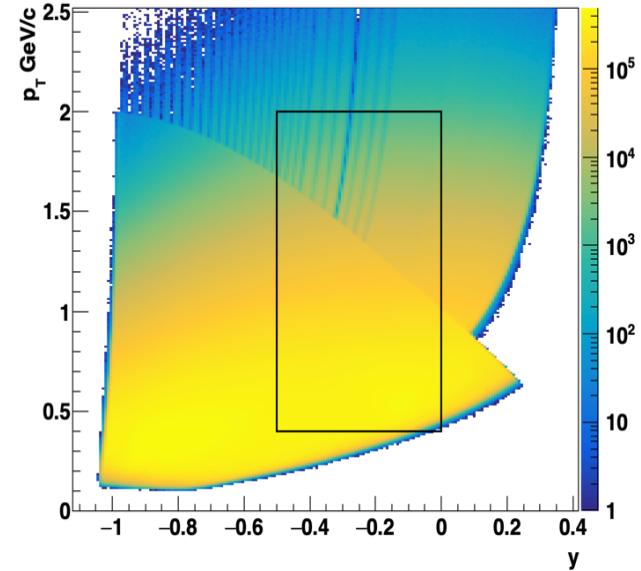
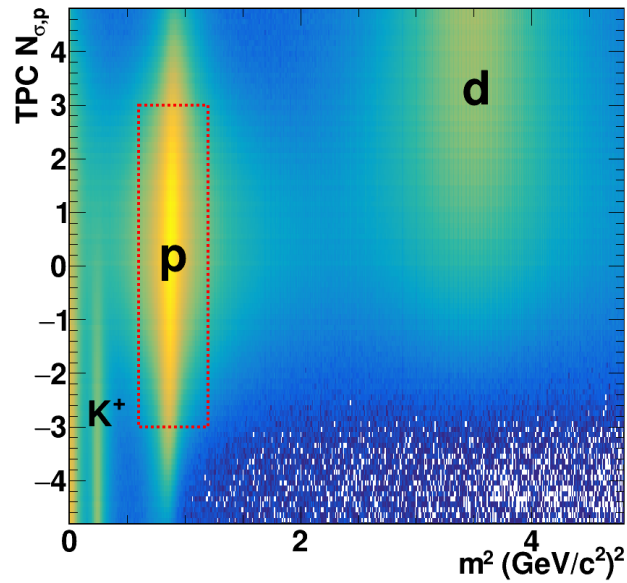
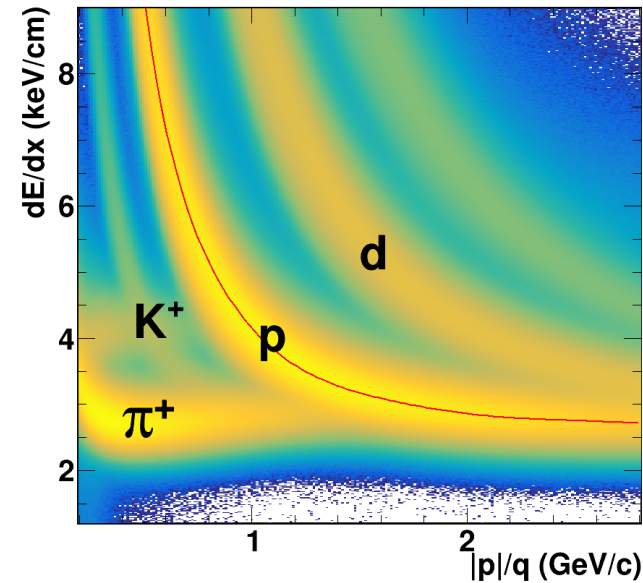
Beam Energy Scan - II	
$\sqrt{s_{NN}}$ (GeV)	Events ( $\times 10^6$ )
19.6	~400
<b>17.3</b>	~250
14.5	~300
11.5	~230
9.1	~160
7.7	~100
7.7(FXT)	~160
6.2(FXT)	~120
5.2(FXT)	~100
4.5(FXT)	~100
3.9(FXT)	~120
3.5(FXT)	~120
3.2(FXT)	~200
3 (FXT)	2000

# Proton Identification (FXT Mode)

Fixed-target data at  $\sqrt{s_{NN}} = 3$  GeV:

TPC PID

TOF PID



Kinematics cuts:  $0.4 < p_T < 2.0$  GeV/c,  $-0.5 < y < 0$

Proton identification:  $0.4 < p_T < 2.0$  GeV/c  $\rightarrow$  TPC

$p > 2.0$  GeV/c  $\rightarrow$  TPC+TOF



# Analysis Detail

- Detector efficiency correction:  
TPC tracking efficiency + TOF matching

Xiaofeng Luo *Phys. Rev. C* 91, 034907

*Phys. Rev. C* 95, 064912 Toshihiro Nonaka, Masakiyo Kitazawa, ShinIchi Esumi

*Phys. Rev. C* 99, 044917 Xiaofeng Luo, Toshihiro Nonaka

- Statistical error estimation:

Delta method and bootstrap method

Xiaofeng Luo 2012 *J. Phys. G: Nucl. Part. Phys.* 39 025008

- Centrality bin width correction:  
suppress initial volume fluctuation

Xiaofeng Luo et al 2013 *J. Phys. G: Nucl. Part. Phys.* 40 105104

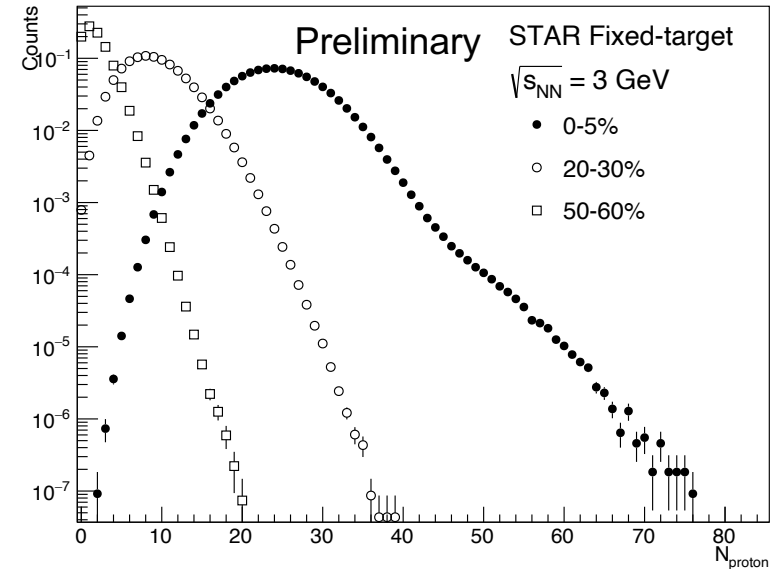
- Pileup correction (at FXT  $\sqrt{s_{NN}} = 3\text{GeV}$ )

Toshihiro Nonaka, Masakiyo Kitazawa, ShinIchi Esumi, J-PARC-TH-0220,

arXiv:2006.15809

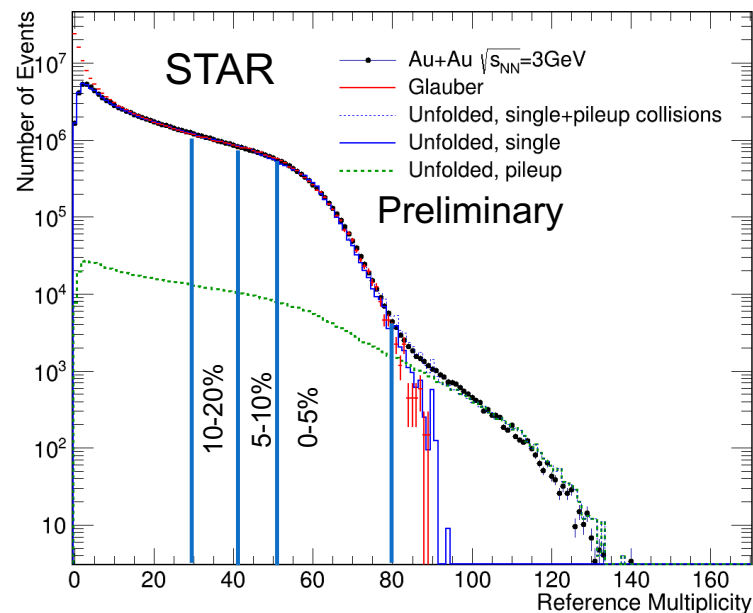
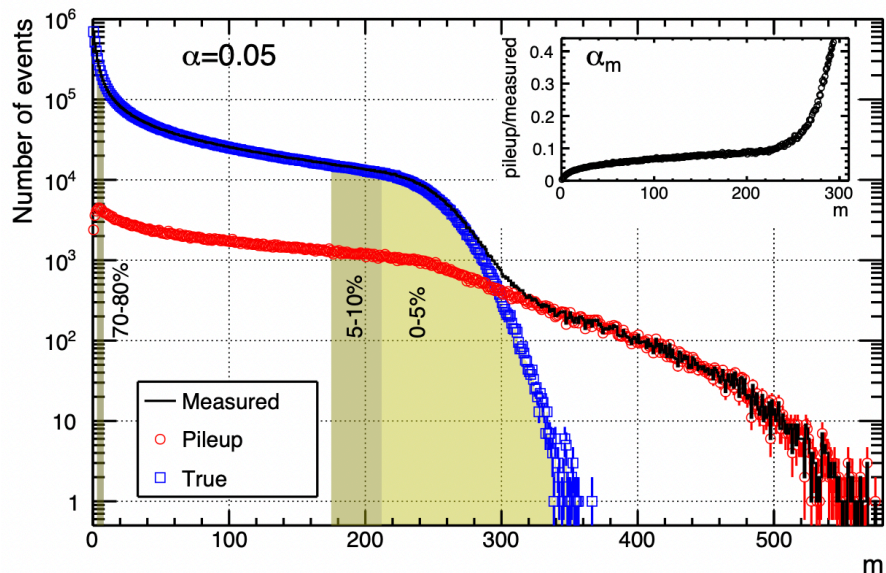
- Initial volume fluctuation correction

P.Braun-Munzinger, A.Rustamov, J.Stachel, arxiv:1612.00702v1



# Analysis Detail: Pileup Correction

Toshihiro Nonaka, Masakiyo Kitazawa, Shinichi Esumi, arXiv:2006.15809



## Probability distribution:

$$P_m(N) = (1 - \alpha_m)P_m^t(N) + \alpha_m P_m^{\text{pu}}(N)$$

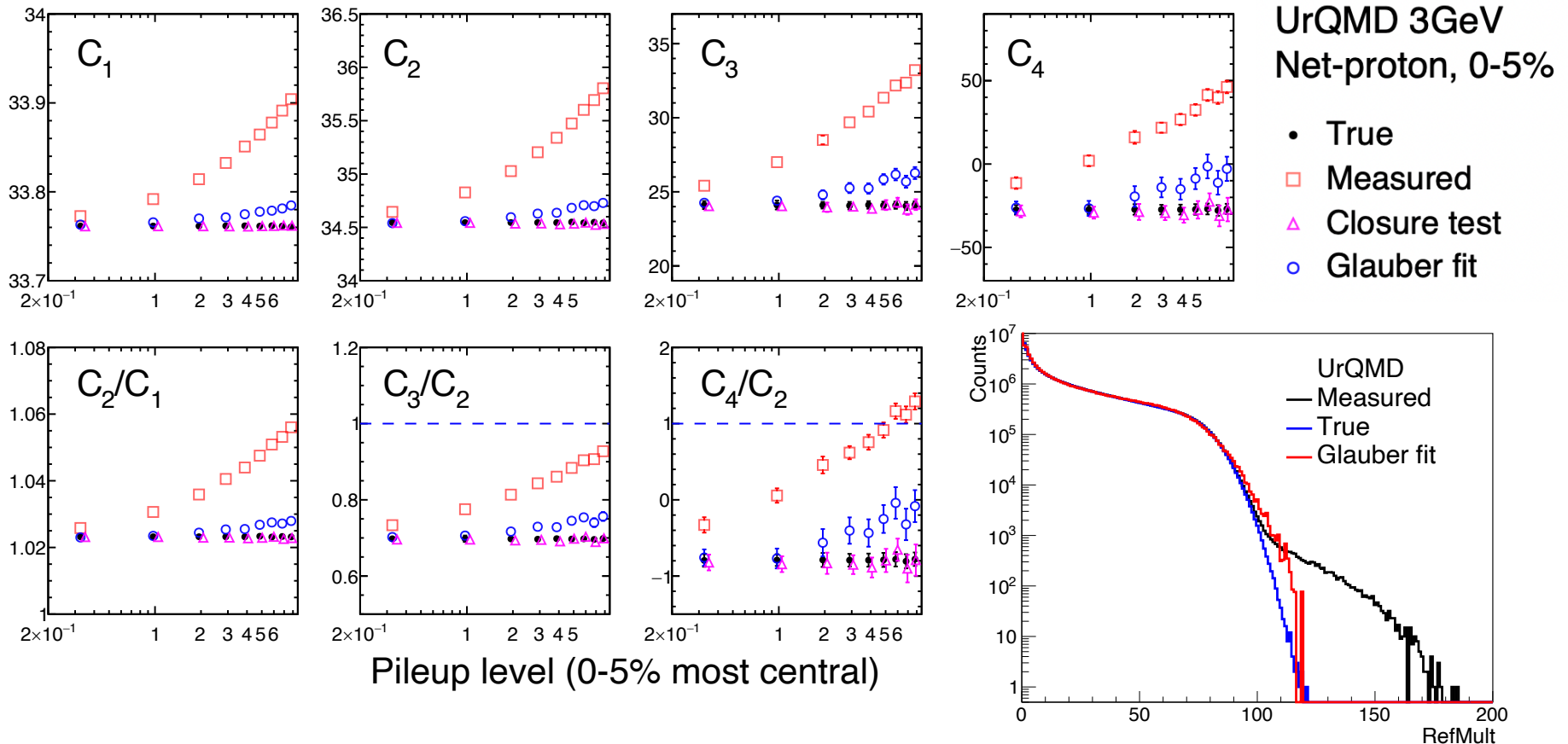
w/o pileup

pileup

- Introduce pileup term in probability distribution
- With estimated pileup probability and single collision distribution, obtain pileup corrected cumulants analytically

Unfolded single collision distribution  
at 3 GeV data

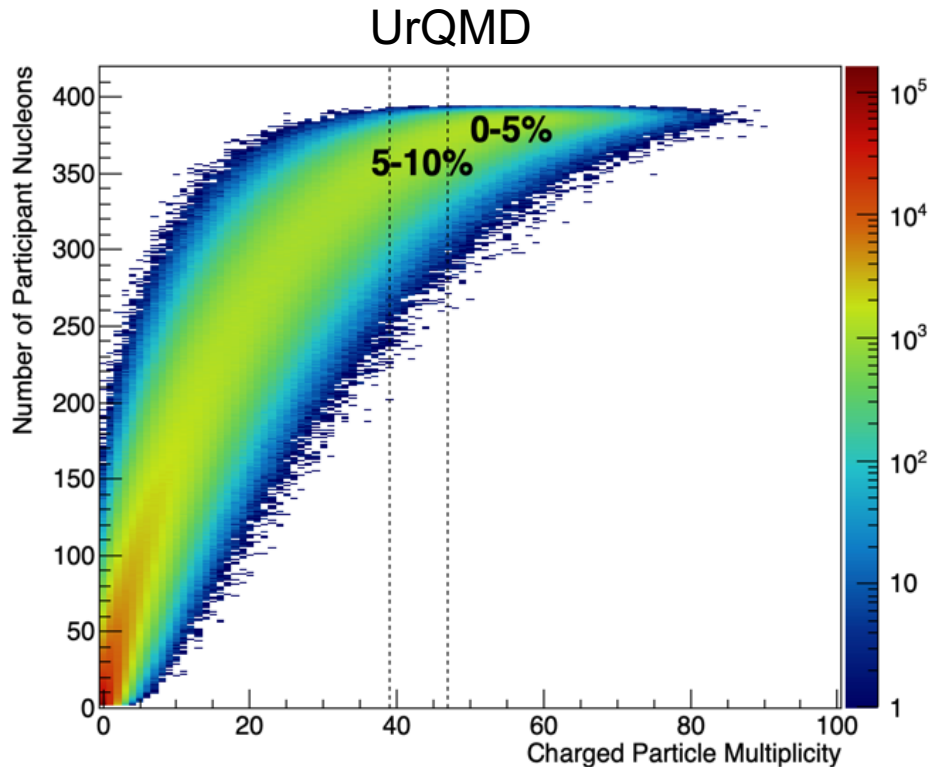
# Pileup Correction closure test with UrQMD



- With well estimated pileup probability, cumulants can be well corrected
- The correction depends on the accuracy of estimation on pileup probability

# Initial Volume Fluctuation and Correction

P. Braun-Munzinger, A. Rustamov, J. Stachel  
arXiv:1612.00702



Assumption: wounded nucleon model: particle production is a superposition of **independent** contributions from wounded nucleons.

$$M_{\Delta N}(t) = [M_{\Delta n}(t)]^{N_W}$$

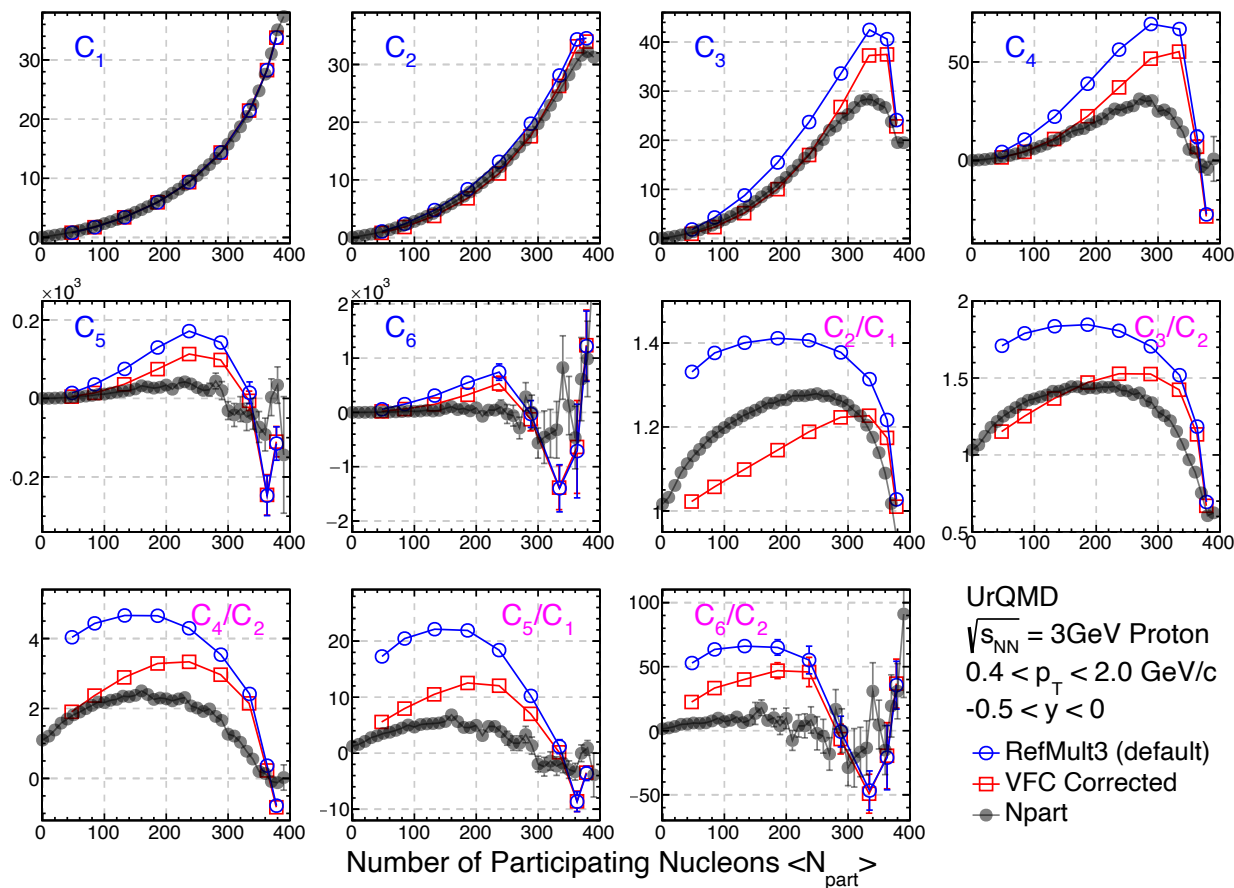
number of wounded nucleons

↑

↑

**total moment generating function** is then a product of generating function from **independent proton sources**

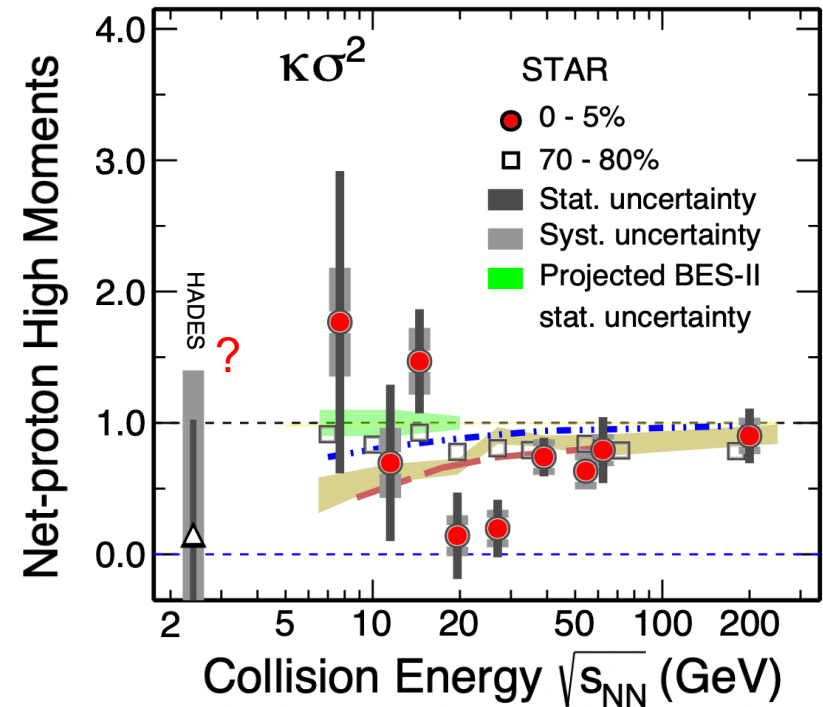
# Volume fluctuation Correction (VFC) on UrQMD



- The correction strongly depends on input Npart distribution
- The assumption in VFC method might not be valid in data

# Summary

- 1) Pileup correction and volume fluctuation correction tested on UrQMD; Application on data needs to be considered with caution.
- 2) Results from STAR  $\sqrt{s_{NN}} = 3$  GeV are around the corner!



J. Adam *et al.* (STAR Collaboration) Phys. Rev. Lett. 126, 092301;  
arXiv:2101.12413

*Thank you!*