### Transverse Single-Spin Asymmetry for Diffractive Electromagnetic Jets with  $p^{\uparrow} + p$  Collisions at √  $\overline{s} = 200 \text{ GeV}$

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December 12, 2024

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# <span id="page-8-0"></span>**Introduction**

3 Transverse single-spin asymmetries  $(A_N)$ , which are defined as left-right asym- metries of the particle production with respect to the plane defined by the momentum and spin directions of the polarized beam, have been observed to be large for charged- and neutral-hadron production in hadron-hadron collisions over a couple of decades  $[1, 2, 3, 4, 5]$  $[1, 2, 3, 4, 5]$  $[1, 2, 3, 4, 5]$  $[1, 2, 3, 4, 5]$  $[1, 2, 3, 4, 5]$ . In pQCD, however, the  $A_N$  is predicted to be small and close to zero in high energy collisions [\[6\]](#page-66-5). There are two major frameworks that can provide a potential explanation for such sizeable asymme- tries. The first one is the transverse-momentum-dependent (TMD) contribu- $_{11}$  tions from the initial-state quark and gluon Sivers functions and/or the final- $_{12}$  state Collins fragmentation functions. In the Sivers mechanism, the asymmetry comes from the correlation between the proton spin and the parton transverse momentum [\[7\]](#page-66-6), while the Collins effect arises from the correlation between the spin of the fragmenting quark and the outgoing hadron's transverse momentum [\[8\]](#page-66-7). Another framework is based on the twist-3 contributions in the collinear factorization framework, including the quark-gluon or gluon-gluon correlations and fragmentation functions [\[9\]](#page-66-8).

 According to the study by CMS Collaboration [\[10\]](#page-66-9), diffractive interactions 20 contribute to about a significant fraction ( $\sim 25\%$ ) of the total inelastic p+p cross section at high energies. The simulation for hard diffractive events based on PYTHIA-8 predicts that the fraction of diffractive cross section in the total inclusive cross section at the forward region is about 20% [\[4\]](#page-66-3). In recent years, analyses of  $A_N$  for forward  $\pi^0$  and electromagnetic jets (EM-jets) in  $p^{\uparrow} + p$  collisions at STAR indicated that there might be non-trivial contributions to <sup>26</sup> the large  $A_N$  from diffractive processes [\[5,](#page-66-4) [11\]](#page-66-10). Measuring the  $A_N$  of diffractive process will provide an opportunity to study the properties and understand the 28 diffractive exchange in  $p+p$  collisions.

In this study, we will explore the *A<sup>N</sup>* for the events with unpolarized proton

- intact (single diffractive process) and the events with polarized proton intact
- (the semi-exclusive process).

# <span id="page-10-0"></span> **Dataset and Quality Assurance (QA)**

### <span id="page-10-1"></span>**2.1 General information for the dataset**

 The single diffractive and the semi-exclusive EM-jet *A<sup>N</sup>* analyses utilize polar- $\frac{1}{37}$  ized p+p collision at  $\sqrt{s} = 200$  GeV taken in run 15. Details of the data set are listed as follow:

- Trigger setup name: production\_pp200trans\_2015
- Data stream: fms
- Production tag: P15ik
- File type: MuDst files in Distributed Disk (DD)

 The analysis generates smaller size data stream files (NanoDst) from the MuDst files, applying trigger filter (described in Sec. [\(2.2\)](#page-10-2)) and jet reconstruc- tion (described in Sec. [3.1\)](#page-15-0). In addition, the events with at least one Roman Pot track are required for diffractive EM-jet  $A_N$  analysis when generating the DST files.

#### <span id="page-10-2"></span>**2.2 Triggers**

 9 triggers for FMS are used for this analysis. The triggers with their ID are listed in Table [\(2.1\)](#page-11-1). However, the FMS-sm-bs3 trigger is also considered a source of background. Therefore, the effect of this trigger will be studied as systematic uncertainty, which will be explained in [8.3.](#page-42-1)

<span id="page-11-1"></span>

Trigger name	Trigger ID
FMS-JP0	480810 / 480830
FMS-JP1	480809 / 480829
FMS-JP2	480808 / 480828
$FMS$ -sm-bs1	480801 / 480821 / 480841
$FMS$ -sm-bs2	480802 / 480822
$FMS$ -sm-bs3	480803 / 480823 / 480843
FMS-lg-bs1	480804 / 480824 / 480844
$\overline{\text{FMS-lg-bs2}}$	480805 / 480825
FMS-lg-bs3	480806 / 480826

Table 2.1: Trigger name lists and trigger ID for run 15

### <span id="page-11-0"></span><sup>53</sup> **2.3 Calibration**

<sup>54</sup> The calibration for run 15 FMS dataset are from existing STAR framework [\[12\]](#page-66-11), <sup>55</sup> but with some additional steps. They mainly include the following items:

 • Bit shift (BS): It refers to the binary bit, used to store the ADC value, not starting from the normal lowest bit. The BS will affect a cell's ADC distribution and the corresponding hit energy. The approach to check the BS is to use the ADC of each FMS hit to check with its corresponding BS value of the cell [\[12\]](#page-66-11).

61 • Gain and gain correction: The energy of the hit = ADC  $\times$  gain  $\times$  gain  $\epsilon$ <sup>2</sup> correction. The gain is the calculated value based on a cell's *η* position, <sup>63</sup> while the gain correction is obtained from offline calibration [\[12\]](#page-66-11). The flag <sup>64</sup> of the gain and the gain correction for each tower in the STAR database <sup>65</sup> is "fmsGainCorr-BNL-C".

 • Hot channel and bad channel masking: A hot channel refers to the tower with a number of hits far more than the average number of hits for the whole detector towers within some time range. A bad channel refers to the problematic towers that might suffer from hardware issues. Both hot and bad channels can affect the quality of the calibration and the analyses since there are quite a lot of non-physical signals that are contaminated. To mask out these channels, the gain values are set to zero. In addition to

<span id="page-12-0"></span>

Figure 2.1: Example of EM-jet distribution at FMS before additional hot channel masking. The red color area in this plot indicates the possible hot channels.

 the existing hot channel and bad channel masking from STAR calibration [\[12\]](#page-66-11), the fill-by-fill hot channel masking is applied in this analysis. The EM-jet distribution before any event selections for every fill is checked to find out any possible hot channels. The EM-jet reconstruction is discussed  $\pi$  in [3.1.](#page-15-0) Figure [\(2.1\)](#page-12-0) shows one example of the EM-jet distribution at the FMS. The areas with extremely high EM-jet entries compared to the overall average entries in the plot are assumed to be the hot channel area. The channels within these areas are considered hot channels and added manually to the hot channel lists. Figure [\(2.2\)](#page-13-0) shows the EM-jet distribution for fill 18827 as an example after the additional hot channel masking. From the plot, the hot channels disappear, and the majority of towers have entries close to the average.

<span id="page-13-0"></span>

Figure 2.2: Example of EM-jet distribution at FMS after additional hot channel masking.

# <span id="page-14-0"></span> **Single Diffractive Process and Event Selection**

 One of the major characteristics of the diffractive processes is the presence of the rapidity gap. This analysis utilizes the proton track from east RP and the EM-jet at FMS, which allows for the large rapidity gap. Since there is only 1 proton in the final state process, this diffractive process is called the single diffractive process. The diagram for this process is shown in Fig. [\(3.1\)](#page-14-1).

 In order to determine the single diffractive process and minimize the effect of accidental coincidence events (AC) and pile-up events, the event selections and corrections include the following items:

1. Triggers: The triggers used for this analysis are the FMS BS triggers and

- <sup>97</sup> FMS JP triggers. They are listed in Table[\(2.1\)](#page-11-1). Only the events with any triggers fired are kept.
- 2. EM-jet cut: Details of the EM-jet cuts are in Section [\(3.1\)](#page-15-0)
- 
- EM-jet reconstruction: EM-jets are reconstructed by FMS points

<span id="page-14-1"></span>

Figure 3.1: Diagram for single diffractive process.



### <span id="page-15-0"></span>**3.1 Electromagnetic jet reconstruction and cuts**

 Electromagnetic jets (EM-jets) are jets consisting of only photons. The photon candidates for EM-jets reconstruction are the FMS points. The description of FMS points can be found in [\[14\]](#page-66-12).

128 In order to reduce the noise background, only the FMS points with  $E > 1$  $_{129}$  GeV and  $E_T > 0.2$  GeV are applied to the EM-jet reconstruction. The EM-130 jets are reconstructed with the anti- $k_T$  algorithm from the FastJet package [\[13\]](#page-66-13), <sup>131</sup> with the resolution parameter  $R = 0.7$ . The primary vertex of the EM-jets is determined according to the priority of the TPC vertex, BBC vertex, and VPD  vertex. If the primary vertex cannot be determined among these three detectors, <sup>134</sup> it will be set to be (0,0,0). The EM-jet transverse momentum  $(p_T)$  is required to pass the trigger threshold and the fixed threshold 2 GeV/*c* threshold. The trigger thresholds are listed in Table [\(3.1\)](#page-17-1). All of them have a 15% increase compared to the original trigger threshold setup.

 The EM-jet vertex is determined by the primary vertex following the priority of TPC, VPD, and BBC. If the primary vertex can be obtained by TPC, the TPC vertex will be the primary vertex. Otherwise, check the VPD vertex on the next step. If there is no VPD vertex, then check the BBC vertex. If there is still  $_{142}$  no BBC vertex, the primary vertex is set to be  $z=0$ . The fraction of the vertex z obtained from TPC, VPD, and BBC are 1%, 33%, and 50%, respectively. The 144 vertex z cut on  $|z| < 80$  cm is considered.

 $\frac{1}{45}$  In addition, we apply the cut on EM-jet pseudorapidity  $(\eta)$ , which aims to get rid of the badly reconstructed EM-jets and the EM-jets hitting outside the <sup>147</sup> FMS. Therefore, the  $\eta$  of the EM-jet cut is required to be within [2.8, 3.8].

Also, the events with EM-jet energy  $E > 100$  GeV or  $|x_F| > 1$  are discarded. 149 where Feynman-x  $x_F$  can be estimated by the EM-jet energy divided by the <sup>150</sup> beam energy  $(x_F = \frac{2E}{\sqrt{s}})$ . These events are about 0.17% of the entire dataset. Those events with these unreasonable EM-jets are possibly pile-up events.

152 The general raw EM-jet  $p_T$  vs energy distribution is shown in Fig.  $(3.2)$ .

 Finally, the number of EM-jets in each event is required to be only one. This can satisfy the requirement for single diffractive events and minimize the effect of the pile-up events. Figure [\(3.3\)](#page-18-0) shows the number of EM-jets distribution, about 92% of the events are containing only one EM-jet at FMS.

#### <span id="page-16-0"></span>**3.2 Event property cut**

 The abort gap for both blue beam and yellow beam is within bunch ID [31, 39] and [111, 119] for run 15. The events with either blue beam or yellow beam with the abort gap are discarded.

<sup>161</sup> The spin patterns for each beam, either up or down, are obtained from the bunch crossing of each event. The translation from the database for the spin patterns is described in Tab. [\(3.2\)](#page-18-1). The spin patterns for both blue and yellow beam are combined as 4-spin bit. The events satisfying the following 4 4-spin bit cases in Table [\(3.2\)](#page-18-1) are considered in this analysis. These patterns require the polarizations of both blue and yellow beam are either up or down.

<span id="page-17-1"></span>

Trigger name	Trigger ID	15% increase $p_T$ cut [GeV]
FMS-JP0	480810 / 480830	1.84
FMS-JP1	480809 / 480829	2.76
FMS-JP2	480808 / 480828	3.68
$FMS$ -sm-bs $1$	480801	1.26
$FMS$ -sm-bs1	480841 480821 /	1.15
$FMS$ -sm-bs $2$	480802 / 480822	1.84
$FMS$ -sm-bs3	480803	2.53
$FMS$ -sm-bs3	480823 / 480843	2.18
$FMS-lg-bs1$	480804	1.26
$FMS-lg-bs1$	480824 / 480844	1.15
$FMS-lg-bs2$	480425 480405 /	1.84
$FMS-lg-bs3$	480426 480406 /	2.76

Table 3.1: EM-jet trigger threshold *p<sup>T</sup>* cut, listed by trigger name and trigger ID.

<span id="page-17-0"></span>

Figure 3.2: EM-jet transverse momentum  $(p_T)$  vs energy  $(E)$  before correction.

<span id="page-18-0"></span>

Figure 3.3: Number of EM-jets in the event.

Table 3.2: 4 acceptable 4-bit spin patterns

<span id="page-18-1"></span>

4-bit spin	<b>Translate</b>	Blue beam polarization	Yellow beam polarization
0101		up	up
0110		up	down
1001		down	up
1010		down	down

<span id="page-19-2"></span>

Figure 3.4: East RP  $\theta_X$  and  $\theta_Y$  distributions for 7 different East RP track  $\xi$ ranges with only applying East BBC ADC sum < 150.

#### <span id="page-19-0"></span>**3.3 BBC East veto cut**

 The major goal for the BBC East veto cut is to minimize accidental coincidence events (AC), also called multiple collision events. Furthermore, it helps to ensure the rapidity gap requirement for the single diffractive process since the BBC East 171 detector covers  $-5 < \eta < -2.1$ .

 The study of BBC East veto cuts is carried out simultaneously with the East RP track cut study. To begin with, the rough cut on a small BBC East ADC sum < 150 is applied to get rid of some of the backgrounds because the events with high BBC East ADC sum are more likely to be AC events. Then, with 176 the rough BBC East ADC sum cut, the East RP  $\theta_X$  and  $\theta_Y$  distributions for East RP track with different *ξ* ranges are checked, where *ξ* is the fraction of proton momentum loss in the collision. The goal of checking the rough East 179 RP  $\theta_X$  and  $\theta_Y$  distributions is to figure out the rough East RP  $\theta_X$  and  $\theta_Y$  cuts and use them to further checking the proper small/large BBC East ADC sum distribution to determine the BBC East veto cuts. Figure [\(3.4\)](#page-19-2) shows the rough East RP *θ<sup>X</sup>* and *θ<sup>Y</sup>* distributions for 7 different East RP *ξ* regions. From the hot areas for every single figure, which are shown in red and yellow color, 184 we determine the rough cut for East RP  $\theta_X$  and  $\theta_Y$ . The rough East RP  $\theta_Y$ <sup>185</sup> cuts are:  $2.0 < |\theta_Y| < 4.0$  mrad, and The rough East RP  $\theta_X$  cuts are shown 186 in Tab. [\(3.3\)](#page-20-1). Then, with the rough East RP  $\theta_X$  and  $\theta_Y$  cuts applied, we explore the small/large east BBC ADC sum distributions to determine the cuts on small/large east BBC cuts. The left panel of Fig. [\(3.5\)](#page-20-0) shows the small east BBC ADC sum distribution, while the right panel of Fig. [\(3.5\)](#page-20-0) shows the large east BBC ADC sum distribution. According to Fig. [\(3.5\)](#page-20-0), we decide the small 191 BBC east ADC sum  $< 90$  and the large BBC east ADC sum  $< 80$ .

### <span id="page-19-1"></span>**3.4 Roman Pot track cut**

 The proton track is detected from the RP detector, where the description of the RP detector can be found in [\[15\]](#page-66-14). For this analysis, we only accept the case with

<span id="page-20-1"></span>

$\xi$ range	$\theta_X$ rough cuts [mrad]
$0.00 < \xi < 0.05$	$-1.0 < \theta_X < 1.5$
$0.05 < \xi < 0.10$	$-1.25 < \theta_X < 1.25$
$0.10 < \xi < 0.15$	$-1.5 < \theta_X < 1.25$
$0.15 < \xi < 0.20$	$-2.0 < \theta_X < 0.75$
$0.20 < \xi < 0.25$	$-2.5 < \theta_X < 0.75$
$0.25 < \xi < 0.30$	$-3.0 < \theta_X < 0.5$
$0.30 < \xi < 0.50$	$-5.0 < \theta_X < -0.25$

Table 3.3: Rough cuts for East RP track *θ<sup>X</sup>* by different East RP track *ξ*

<span id="page-20-0"></span>

Figure 3.5: The small (left) and large (right) East BBC ADC sum distribution after the rough East RP  $\theta_X$  and  $\theta_Y$  cuts

<span id="page-21-0"></span>

Figure 3.6: East RP  $\theta_X$  and  $\theta_Y$  distributions for three East RP track  $\xi$  ranges.

<span id="page-21-1"></span>

$\xi$ range	$\theta_X$ final cuts [mrad]
	$0.00 < \xi < 0.05$   $-1.0 < \theta_X < 1.5$
$0.05 < \xi < 0.10$	$-1.25 < \theta_X < 1.25$
	$0.10 < \xi < 0.15$   $-1.5 < \theta_X < 1.25$

Table 3.4: Final cuts for East RP track  $\theta_X$  by three  $\xi$  regions

<sup>195</sup> only one East RP track detected. To ensure the RP track is well reconstructed, <sup>196</sup> the RP track must hit at least 7 RP silicon planes. Also, the BBC East veto <sup>197</sup> cuts (details in Sec. [\(3.3\)](#page-19-0)) are also applied to explore the East RP track cuts. <sup>198</sup> Furthermore, according to the Particle Data Book [\[16\]](#page-66-15), the proton *ξ* for the <sup>199</sup> diffractive process should be less than 0.15. Therefore, the cut on East RP <sup>200</sup> track  $0 < \xi < 0.15$  is also applied. With all of these cuts applied, first of all, <sup>201</sup> the East RP track  $\theta_X$  and  $\theta_Y$  distributions are further explored. Figure [\(3.6\)](#page-21-0) <sup>202</sup> shows the East RP track *θ<sup>X</sup>* and *θ<sup>Y</sup>* distributions for three *ξ* ranges. The hot 203 area will be considered as acceptable final East RP  $\theta_X$  and  $\theta_Y$  cuts. The final <sup>204</sup> East RP track *θ<sup>Y</sup>* cuts are uniform for all three *ξ* ranges: 2 *<* |*θ<sup>Y</sup>* | *<* 4 mrad. <sup>205</sup> However, the final East RP track  $θ_X$  cuts are  $ξ$  dependent, shown in Tab. [\(3.4\)](#page-21-1).  $_{206}$  Finally, with then the final East RP  $\theta_X$  and  $\theta_Y$  cuts applied, the East RP track <sup>207</sup> *p<sup>X</sup>* and *p<sup>Y</sup>* distributions are also explored to study their cuts. The idea is the <sup>208</sup> same as investigating the East RP track  $θ_X$  and  $θ_Y$  cuts. Figure [\(3.7\)](#page-22-0) shows 209 the East RP track  $p_X$  and  $p_Y$  distributions for three  $\xi$  ranges. The shape of a  $_{210}$  rectangle with a quarter circle is used to describe the final East RP track  $p_X$ 211 and  $p_Y$  cuts. The expressions are detailed in Tab.  $(3.5)$ .

<sup>212</sup> In summary, the cuts on East RP track include all the following: Number 213 of RP Silicon planes hits greater than 6;  $0 < \xi < 0.15$ ; East RP track  $\theta_X$  and <sup>214</sup>  $\theta_Y$  cuts; East RP track  $p_X$  and  $p_Y$  cuts.

<span id="page-22-0"></span>

Figure 3.7: East RP track  $p_X$  and  $p_Y$  distributions for three East RP track  $\xi$ ranges. The black curves indicate the ranges of accepted East RP track *p<sup>X</sup>* and *p<sup>Y</sup>* cuts.

<span id="page-22-1"></span>

$\xi$ range	$p_X$ and $p_Y$ final cuts [GeV/c]
	$(0.00 < \xi < 0.05)$ $(p_X + 0.02)^2 + ( p_Y  - 0.2)^2 < 0.15^2$ or $-0.08 < p_X < -0.02$ and $0.2 <  p_Y  < 0.35$
	$\left[0.05 < \xi < 0.10\right]$ $\left(p_X + 0.02\right)^2 + \left( p_Y  - 0.2\right)^2 < 0.13^2$ or $-0.10 < p_X < -0.02$ and $0.2 <  p_Y  < 0.33$
	$\left[0.10 < \xi < 0.15\right]$ $(p_X + 0.02)^2 + ( p_Y  - 0.18)^2 < 0.13^2$ or $-0.12 < p_X < -0.02$ and $0.18 <  p_Y  < 0.31$

Table 3.5: East RP track  $p_X$  and  $p_Y$  final cuts

# <span id="page-23-0"></span>**Corrections**

### <span id="page-23-1"></span>**4.1 Underlying Event (UE) correction**

 The underlying event contribution is part of a jet, not from the parton fragmen- tation but from secondary scattering or other processes. This will deposit some energy into the jet, so the correction on UE is required to subtract its energy from the jet. The "off-axis" method [\[17\]](#page-66-16) is used. In this method, first of all, <sup>222</sup> two off-axis jets with the same pseudorapidity but at  $\pm \pi/2$  azimuthal angle at the edge of the original jet are reconstructed as UE background. Then, the UE energy density ( $\rho$ ) can be calculated using  $\rho = E/(\pi R^2)$ , where E is the average UE energy and R is the UE jet radius. The fastjet program uses the "ghost  $_{226}$  particle" technique to calculate the jet area  $(A)$ . The maximum "ghost particle" *η* is 5.0, and the "ghost area" is 0.04. Finally, the jet energy will be subtracted <sup>228</sup> by the UE energy:  $E_{corrected} = E_{original} - \rho \times A$ , where the corrected EM-jet energy is  $E_{corrected}$ , and the original EM-jet energy is  $E_{original}$ .

 Figure [\(4.1\)](#page-24-0) shows the UE correction distribution for EM-jet energy. The left plot shows the subtraction term for the UE correction for EM-jet energy. The right plot shows the EM-jet energy distribution after the UE correction. If the EM-jet energy after subtraction is less than 0 GeV, the energy will be set to 0 GeV.

### <span id="page-23-2"></span> **4.2 Detector level to particle level EM-jet en-ergy correction**

 The EM-jet energy obtained from FMS is considered detector-level EM-jet en- ergy. Therefore, a correction for detector level to particle level EM-jet energy is necessary. The correction is based on the Monte Carlo simulation for FMS. For

<span id="page-24-0"></span>

Figure 4.1: UE distribution for diffractive EM-jet analysis. The left plot shows the subtraction term  $\rho \times A$ . The right plot shows the EM-jet energy distribution after the UE correction.

the PYTHIA simulation, the proton-proton collisions with  $\sqrt{s} = 200$  GeV are generated, with the tune setting of Perugia2012 (Tune parameter 370) [\[18,](#page-67-0) [19\]](#page-67-1). Then, the GEANT3 with FMS detector response implemented under STAR simulation framework ("starsim") is used for the FMS simulation. The Big Full Chain (BFC) proceeds with the event reconstruction. The chain options are "ry2015a agml usexgeom MakeEvent McEvent vfmce Idst BAna l0 l3 Tree logger fmsSim fmspoint evout -dstout IdTruth bigbig fzin geantout clearmem sdt20150417.193427". The EM-jet reconstruction is proceeded along with the <sup>248</sup> BFC process. The Anti- $k_T$  algorithm with R=0.7 is used for the EM-jet recon-struction, the same as the EM-jet reconstruction for data.

 For the simulation results, the EM-jets with both particle level and detector level are recorded. Figure [\(4.2\)](#page-25-0) shows the EM-jet energy distribution in particle level (y-axis) and detector level (x-axis). Figure [\(4.3\)](#page-25-1) shows the profile of the EM-jet energy distribution with particle level and detector level. The black points are the correlation between the EM-jet energy at the particle level and detector level. The red curves are fit for the points in two different detector level <sup>256</sup> regions:  $5 < E < 10$  GeV and  $10 < E < 60$  GeV. The 6th-order polynomial function is used for fitting the former region and the linear function is used for fitting the latter region. The parameters of the 6th-order polynomial are shown <sup>259</sup> in Tab. [\(4.1\)](#page-25-2), while the linear function is:  $E_{par} = 1.07 * E_{det} + 1.13$ , where  $E_{par}$  is the particle level EM-jet energy and  $E_{det}$  is the detector level EM-jet energy. These functions are used to calculate the corrected energy from the original detector level energy. The corrected EM-jet energy will finally applied <sup>263</sup> for the  $x_F$  calculation and  $A_N$  extraction.

<span id="page-25-0"></span>

Figure 4.2: EM-jet energy distribution in particle level (y-axis) and detector level (x-axis) from the FMS simulation.

<span id="page-25-1"></span>

Figure 4.3: The profile of the EM-jet energy distribution with particle level and detector level. The black points are the correlation between the EM-jet energy at the particle level and detector level. The red curves are the fit for the black points.

<span id="page-25-2"></span>

	$\left\lceil 2 \right\rceil$	$\lceil 3 \rceil$	[4]	$\lceil 6 \rceil$
		8.93e0   -6.64e-1   1.51e-1   -6.66e-3   1.56e-4   -1.85e-6   8.65e-9		

Table 4.1: Parameters for the 6th-order polynomial

# <span id="page-26-0"></span>**Rapidity Gap (RG) events study**

### <span id="page-26-1"></span>**5.1 Motivation**

 The rapidity gap (RG) events are also within our interest in studying the po- tential background for the single diffractive events. The RG events are the type of events coinciding with FMS EM-jets and East BBC veto, with the schematic  $_{271}$  diagram shown in Fig. [\(5.1\)](#page-27-1). The details description for the FMS EM-jets and east BBC veto are in Sec. [\(5.2\)](#page-26-2). Since there is no requirement on the RP track (proton) on any side, the RG events are considered as the subset of the inclu- sive events, and they can also serve as additional enrichment for the inclusive process. According to the Pythia 8 simulation for hard QCD process (can be considered as non-single diffractive events) and the single diffractive events, the east BBC veto cuts are able to cut out about 84% of the non-single diffractive events, but just cut out about 14% of the single diffractive events with a proton on the east side. Therefore, such a process can help separate the diffractive and non-diffractive processes with the rapidity gap requirement. Studying the RG events can allow us to investigate the single diffractive process without the effects on the limited Roman Pot acceptance for tagging the scattered proton.

#### <span id="page-26-2"></span>**5.2 Event selection for RG events**

 The dataset used for the RG events is the same as single diffractive events,  $_{285}$  shown in Sec.  $(2.1)$ . The event selection criteria of the FMS EM-jets, event property cuts, and the East BBC veto for the RG events are the same as those  $_{287}$  for the single diffractive events, which are shown in Sec.  $(3.1)$ , Sec.  $(3.2)$  and

<span id="page-27-1"></span>

Figure 5.1: Diagram for rapidity gap events.

 Sec. [\(3.3\)](#page-19-0), respectively. The idea behind choosing the same FMS EM-jet cuts and East BBC veto cuts is to make them consistent and comparable to the single diffractive process.

### <span id="page-27-0"></span> **5.3 Fraction of single diffractive events in rapid-ity gap events**

 The study on the fraction of single diffractive events in rapidity gap events in data can be measured using the simulation. The simulation is using the Pythia 8 single diffractive process (SoftQCD:singleDiffractive). Both the east BBC detector simulation (via GEANT3 based STAR detector level simulation) and the east RP detector simulation (via pp2pp simulation [\[25\]](#page-67-2)) are used for the simulation study. The same east BBC veto (detailed in Sec. [\(3.3\)](#page-19-0)) is applied in the simulation to determine the veto on the east BBC region (rapidity gap) as well. The cut on the east RP track hitting more than 6 east RP planes is used for determining the good east RP track. In addition, only one RP track is allowed as the east RP cut for the single diffractive events.

 Based on the criteria above, we define the single diffractive events (SD) in the simulation as the events passing the east BBC veto and the east RP cut. Also, we define the rapidity gap events (RG) in the simulation as the events passing the east RP cut without requirement on the east RP cut. The RG events in simulation are all real single diffractive events (RSD). The definition of single diffractive events and rapidity gap events in data are the same as mentioned in previous sections. However, the RG events in data contain real single diffractive events (RSD) and non-single diffractive events (NSD). When we calculate the fraction of single diffractive events to the rapidity gap events in simulation and data, the equation for simulation and data can be expressed as  $_{313}$  Equ. [\(5.1\)](#page-28-0) and Equ. [\(5.2\)](#page-28-1), respectively. In the calculation,  $frac(sim) = 16.03\%$  $_{314}$  and  $frac(data) = 11.08\%$ . Since the purity of the single diffractive events in data is high, we can consider the fraction of single diffractive events (SD) to the real single diffractive events in rapidity gap event (RSD),  $\frac{SD}{RSD}$ , is same

<sup>317</sup> between data and simulation. Considering the major systematic uncertainty <sup>318</sup> of the fraction comes from the uncertainty of BBC detector (6.5%) [\[26\]](#page-67-3) and  $_{319}$  RP detector (10%) [\[25\]](#page-67-2). The SD fraction in RG events in data  $\left(\frac{RSD}{RSD+NSD}\right)$  is 320 68.7%  $\pm$  0.6%  $\pm$  8.2%.

<span id="page-28-0"></span>
$$
frac(sim) = \frac{SD}{RSD} \tag{5.1}
$$

<span id="page-28-1"></span>
$$
frac(data) = \frac{SD}{RSD + NSD} \tag{5.2}
$$

# <span id="page-29-0"></span> **Semi-exclusive process study**

 The semi-exclusive process requires only one EM-jet at FMS and one proton detected in west side RP. The event selections of the EM-jet are same as that used in single diffractive process and rapidity gap events, showing in Sec. [3.1.](#page-15-0) Additionally, an exclusive constraint on the sum of the energy of the EM-jet and the west RP track (energy sum) is applied. It requires the energy sum are same as proton beam energy within resolution. Therefore, this process is termed as semi-exclusive process. The schematic diagram for semi-exclusive process is  $_{331}$  shown in Fig.  $(6.1)$ .

 In order to determine the single diffractive process and minimize the effect of accidental coincidence events (AC) and pile-up events, the event selections and corrections include the following items:

 1. Triggers: The triggers used for this analysis are the FMS BS triggers and FMS JP triggers. They are listed in Table[\(2.1\)](#page-11-1). Only the events with any triggers fired are kept.

<span id="page-29-1"></span>

Figure 6.1: Diagram for semi-exclusive process.



### <span id="page-30-0"></span>**6.1 West BBC veto cuts**

 The major goal for the BBC West veto cut is to minimize accidental coincidence events (AC), which are called multiple collision events. However, the west BBC

<span id="page-31-1"></span>

West RP $\xi$ range	West RP $\theta_X$ rough cut  mrad
$0 < \xi < 0.05$	$-1 < \theta_X < 1.75$
$0.05 < \xi < 0.1$	$-1.5 < \theta_X < 1.5$
$0.1 < \xi < 0.15$	$-1.75 < \theta_X < 1.25$
$0.15<\xi<0.2$	$-2.5 < \theta_X < 1.25$
$0.2 < \xi < 0.25$	$-3 < \theta_X < 1$
$0.25<\xi<0.3$	$-3.25 < \theta_X < 0.5$
$0.3 < \xi < 0.35$	$-3.75 < \theta_X < 0$
$0.35<\xi<0.4$	$-4.25 < \theta_X < -0.5$
$0.4 < \xi < 0.45$	$-5 < \theta_X < -1$

Table 6.1: Rough west RP  $\theta_X$  cuts

 coverage is partially overlapped with the FMS coverage. Therefore, this west BBC veto can not provide enough size of rapidity gap to satisify the requirement of the diffractive process.

 The idea for determining the west BBC veto cuts are similar as for deter- mining the east BBC veto cuts. To begin with, the rough cuts on west RP  $\theta_X$  and  $\theta_Y$  are applied to check the small BBC west ADC sum distribution. The 375 distribution of west RP  $\theta_Y$  vs  $\theta_X$  are showing in Fig.[\(6.2\)](#page-32-0), with the rough cut on west small BBC ADC sum < 150. From the plots, we determine the rough <sup>377</sup> west RP  $\theta_Y$  cut on: 1.5 <  $|\theta_Y|$  < 4 mrad, with the rough west RP  $\theta_X$  cuts are listed in Tab. [\(6.1\)](#page-31-1).

<sup>379</sup> With these rough west RP  $\theta_X$  and  $\theta_Y$  cuts, the small BBC west ADC sum and the large BBC west ADC sum distributions are then checked. Figure [\(6.3\)](#page-32-1) shows the small BBC west ADC sum, and Fig. [\(6.4\)](#page-33-1) shows the large BBC west ADC sum. From the plots, we apply the cuts on small BBC west ADC sum  $\lt$ 80 and large BBC west ADC sum  $< 60$ .

### <span id="page-31-0"></span>**6.2 Roman Pot (RP) track cut**

 The proton track for semi-exclusive process is detected from the west side RP detector. Only one west side RP track is accepted for this process, with no constrain on east side tracks. In addition, this west side RP track requires to 388 hit more than 6 planes. The first set of cuts are the west RP  $\theta_X$  and  $\theta_Y$  cuts. Before exploring these cuts, the west BBC veto cuts are applied. Figure [\(6.5\)](#page-34-0) 390 shows the final distribution of west RP  $\theta_Y$  vs  $\theta_X$ . From the distributions, we

<span id="page-32-0"></span>

Figure 6.2: West RP *θ<sup>X</sup>* and *θ<sup>Y</sup>* distributions for 9 different East RP track *ξ* ranges with only applying West BBC ADC sum  $<$  150.

<span id="page-32-1"></span>

Figure 6.3: Small BBC west ADC sum distribution after the rough west RP cuts.

<span id="page-33-1"></span>

Figure 6.4: Large BBC west ADC sum distribution after the rough west RP cuts.

391 determine the  $\theta_Y$  cuts on: 1.5  $\lt |\theta_Y|$   $lt 4$  [mrad]; and the  $\theta_X$  cuts shown in 392 Tab. [\(6.2\)](#page-34-1). Then, with applying the west RP  $\theta_X$  and  $\theta_Y$  cuts, the west RP  $p_X$  and *p<sup>Y</sup>* cuts are explored. Figure [\(6.6\)](#page-35-0) shows the final distribution of west RP  $\partial_X$  and  $\partial_Y$  with the black curve region indicating the ranges of the cuts. The cut values are shown in Tab. [\(6.3\)](#page-35-1).

#### <span id="page-33-0"></span>**6.3 Energy sum cuts**

 For the semi-exclusive process, the final state includes the EM-jet and the pro- ton. Both are on the same side (west side). Therefore, an exclusive constrain on the sum of the energy for EM-jet and the proton should be consistent with the beam energy within resolution. This is the reason for naming this process as semi-exclusive process.

 The energy sum cuts are explored with applying the west BBC veto cuts 403 and the west RP cuts. They are shown with EM-jet  $x_F$  dependent in Fig. [\(6.7\)](#page-36-0). and in Tab. [\(6.4\)](#page-36-1).

<span id="page-34-0"></span>

Figure 6.5: West RP *θ<sup>X</sup>* and *θ<sup>Y</sup>* distributions for 9 different East RP track *ξ* ranges after applying West BBC veto cuts.

<span id="page-34-1"></span>

West RP $\xi$ range	West RP $\theta_X$ final cut [mrad]
$0 < \xi < 0.05$	$-1 < \theta_X < 1.75$
$0.05 < \xi < 0.1$	$-1.5 < \theta_X < 1.5$
$0.1 < \xi < 0.15$	$-1.75 < \theta_X < 1.25$
$0.15<\xi<0.2$	$-2 < \theta_X < 1$
$0.2 < \xi < 0.25$	$-2.75 < \theta_X < 0.5$
$0.25<\xi<0.3$	$-3.25 < \theta_X < 0.5$
$0.3 < \xi < 0.35$	$-3.75 < \theta_X < 0$
$0.35<\xi<0.4$	$-4.5 < \theta_X < -0.5$
$0.4 < \xi < 0.45$	$-5.5 < \theta_X < -1.25$

Table 6.2: Final west RP  $\theta_X$  cuts

<span id="page-35-0"></span>

Figure 6.6: West RP track  $p_X$  and  $p_Y$  distributions for nine West RP track  $\xi$ ranges. The black curves indicate the ranges of accepted West RP track *p<sup>X</sup>* and *p<sup>Y</sup>* cuts.

<span id="page-35-1"></span>

West RP $\xi$ range	West RP $p_X$ and $p_Y$ final cut [GeV/c]
$0 < \xi < 0.05$	$(p_X - 0.03)^2 + (p_Y - 0.18)^2 < 0.14^2$ and $0.18 <  p_Y  < 0.32$
$0.05 < \xi < 0.1$	$(p_X - 0.01)^2 + (p_Y - 0.18)^2 < 0.14^2$ and $0.18 <  p_Y  < 0.32$
$0.1 < \xi < 0.15$	$(p_X + 0.02)^2 + (p_Y - 0.16)^2 < 0.14^2$ and $0.16 <  p_Y  < 0.3$
$0.15 < \xi < 0.2$	$(p_X + 0.04)^2 + (p_Y - 0.16)^2 < 0.12^2$ and $0.16 <  p_Y  < 0.28$
$0.2 < \xi < 0.25$	$(p_X + 0.07)^2 + (p_Y - 0.14)^2 < 0.12^2$ and $0.14 <  p_Y  < 0.26$
$0.25 < \xi < 0.3$	$(p_X + 0.1)^2 + (p_Y - 0.14)^2 < 0.12^2$ and $0.14 <  p_Y  < 0.26$
$0.3 < \xi < 0.35$	$(p_X + 0.11)^2 + (p_Y - 0.12)^2 < 0.12^2$ and $0.12 <  p_Y  < 0.24$
$0.35 < \xi < 0.4$	$(p_X + 0.14)^2 + (p_Y - 0.12)^2 < 0.11^2$ and $0.12 <  p_Y  < 0.23$
$0.4 < \xi < 0.45$	$(p_X + 0.17)^2 + (p_Y - 0.12)^2 < 0.1^2$ and $0.12 <  p_Y  < 0.22$

Table 6.3: Final west RP  $p_X$  and  $p_Y$  cuts

<span id="page-36-0"></span>

Figure 6.7: Energy sum cuts for 5 different EM-jet  $x_F$  regions

<span id="page-36-1"></span>

EM-jet $x_F$	Energy sum $(E_{sum})$ cut
$0.2 - 0.25$	$E_{sum}$ < 110 GeV
$0.25 - 0.3$	$E_{sum}$ < 110 GeV
$0.3 - 0.35$	$E_{sum}$ < 115 GeV
$0.35 - 0.4$	$E_{sum}$ < 115 GeV
$0.4 - 0.45$	$E_{sum}$ < 120 GeV

Table 6.4: Energy sum cuts for semi-exclusive process

# <span id="page-37-0"></span>**Background study**

#### <span id="page-37-1"></span>**7.1 Zerobias event study**

 The Zerobias events are the highly scaled events with the zerobias trigger. The details for the events are shown below:

- Trigger setup name: production\_pp200trans\_2015
- Data stream: zerobias
- Production tag: P16id

 Since there are only a small fraction of events containing good EM-jets at the FMS, the Zerobias events are only used to estimate the accidental background for the analysis. To begin with, the NanoDst files are generated from the MuDst files. For the Zerobias events, there are no requirement on the EM-jets on FMS and no requirement on RP track. Then, the BBC East veto cuts (detailed in Sec. [\(3.3\)](#page-19-0) and East RP track cuts (detailed in Sec. [\(3.4\)](#page-19-1)) are applied to the Zerobias events, where both cuts are the same as single diffractive process. About 0.2% of the events pass the cuts mentioned above. Therefore, about  $0.2\%$  of the events are accidental coincidences and should be the same rate for every process.

<sup>422</sup> With the Zerobias events, we also estimate the accidental coincidences (AC) for the measured single diffractive process. The AC events are coming from the situation that the FMS EM-jets and the east RP tracks are not correlated. For example, the FMS EM-jets and the east RP tracks are coming from multiple collisions, but they are recorded in one event in the data. Equation [\(7.1\)](#page-38-1) shows  $_{427}$  the formula for calculating the fraction for the AC events.  $n_{AC}$  is the number of <sup>428</sup> the AC events, but it is difficult to count directly.  $n_{mea}$  is the number of event <sup>429</sup> counts per  $x_F$  bin in the asymmetry calculation for the single diffractive process.  $n_{RG}$  is the number of event counts per  $x_F$  bin in the asymmetry calculation for

the RG events, where the description for RG events is in Sec. [\(5.1\)](#page-26-1).  $\frac{n_{AC}}{n_{RG}}$  can be <sup>432</sup> considered as the AC events fraction for RG events, which is 0.2%. By counting <sup>433</sup> the events per  $x_F$  bin for measured single diffractive process and RG events, the  $434$  fraction for the AC events is about 1.8% for each  $x_F$  bin. This fraction is small, <sup>435</sup> so its effect will be assigned to the systematic uncertainty, detailed in Appendix  $436$  [\(B\)](#page-64-0).

<span id="page-38-1"></span>
$$
frac_{bkg} = \frac{n_{AC}}{n_{mea}} = \frac{n_{AC}}{n_{RG}} \times \frac{n_{RG}}{n_{mea}} \tag{7.1}
$$

### <span id="page-38-0"></span><sup>437</sup> **7.2 Mix event background for energy sum cut** <sup>438</sup> **study**

 The energy sum cuts constrain the sum of the EM-jet energy and the west RP track energy. For the accidental coincidence (AC) in the semi-exclusive process, the energy sum is usually much higher than the beam energy because the west RP track is coming from the proton from the non-diffractive process, especially from the elastic scattering process. Therefore, in order to estimate the contribution to the semi-exclusive events from the AC events, the mix event background is studied to estimate such contribution.

 For the mix event background study for energy sum, we use the distribution for the west RP track energy (momentum) in the zerobias event [\(7.1\)](#page-37-1), and the distribution for the EM-jet energy from the inclusive process. The mix event energy sum background distribution is studied in different EM-jet *x<sup>F</sup>* regions. The idea for the mix event energy sum background is to calculate all the possible combinations of the energy sum with west RP track momentum and EM-jet energy. Equation [\(7.2\)](#page-39-2) shows the simple idea for the mix event energy sum calculation (Esum(i+j)). P(i) is the fraction of EM-jet yields in <sup>454</sup> the inclusive EM-jet energy distribution for [i,i+1] (GeV) within the specific  $x_F$  $_{455}$  range. n(j) is the yield in zerobias events west RP momentum distribution for  $_{456}$  [i,j+1] (GeV/c). Figure [\(7.1\)](#page-39-0) shows one example of the mix event energy sum spectrum. In this example, The left panel of Fig. [\(7.1\)](#page-39-0) shows the inclusive EM-<sup>458</sup> jet energy spectrum for  $0.2 < x_F < 0.25$ , which corresponds to  $20 \leq i \leq 25$ . The middle panel of Fig. [\(7.1\)](#page-39-0) shows the zerobias events west RP momentum distribution, and only west RP momentum between 40 GeV and 100 GeV will <sup>461</sup> be used for mix event background study, which corresponds to  $40 \leq j \leq 100$ . The right panel of Fig. [\(7.1\)](#page-39-0) show the energy sum distribution using the mix <sup>463</sup> event background study for EM-jet with  $0.2 < x_F < 0.25$ .

<span id="page-39-0"></span>

Figure 7.1: Example for mix event energy sum background study for EM-jet with  $0.2 < x_F < 0.25$ .

<span id="page-39-1"></span>

EM-jet $x_F$	Signal region [GeV]	Background region [GeV]
$0.2 - 0.25$	$Esum < 110$ GeV	$Esum > 110$ GeV
$0.25 - 0.3$	$Esum < 110$ GeV	$Esum > 110$ GeV
$0.3 - 0.35$	$Esum < 115$ GeV	$Esum > 115$ GeV
$0.35 - 0.4$	$Esum < 115$ GeV	$Esum > 115$ GeV
$0.4 - 0.45$	$Esum < 120$ GeV	$Esum > 120$ GeV

Table 7.1: Signal region and background region for energy sum spectrum in data

<span id="page-39-2"></span>
$$
Esum(i + j) = \sum_{i,j} P(i) \times n(j) \tag{7.2}
$$

 Then, we use the shape of the mix event energy sum background to estimate its contribution to the semi-exclusive events. For the energy sum plots in data, we define the signal region and the background region based on the energy sum cut in Sec. [\(6.3\)](#page-33-0). The signal region and the background region for each EM-jet  $x_F$  region are shown in Tab. [\(7.1\)](#page-39-1). Then, the shape of the mix event energy sum background is scaled to the maximum bin value of the background region in each EM-jet  $x_F$  region. Figure [\(7.2\)](#page-40-0) shows the mix event background results for each EM-jet  $x_F$  region. In each plot, the red curve indicates the energy sum distribution in data, while the black curve indicates the scaled mix event energy sum background. The fraction of the mix event energy sum background to the data can be calculated as the ratio of the integrated yields for the scaled mix event energy sum background within the signal region to the integrated yields for the data within the signal region. Table [\(7.2\)](#page-40-1) shows this mix event energy sum background fraction. Since this fraction is small (less than  $3\%$ ), we assign such fraction to the systematic uncertainty as the background term.

<span id="page-40-0"></span>

Figure 7.2: Mix event energy sum background study results for each EM-jet  $x_F$ regions. In each plot, the red curve indicates the energy sum distribution in data, while the black curve indicates the scaled mix event energy sum background.

<span id="page-40-1"></span>

$x_F$	Fraction of background $(\%)$
$0.2 - 0.25$	$\perp$ 1.3
$0.25 - 0.3$	1.3
$0.3 - 0.35 \pm 2.1$	
$0.35 - 0.4$	2.0
$0.4 - 0.45 \pm 2.7$	

Table 7.2: Fraction of the mix event energy sum background for each EM-jet  $x_F$  region

# <span id="page-41-0"></span> **Systematic Uncertainty for**  $A_N$

 The systematic uncertainty for single diffractive process includes the cuts on East BBC veto cuts (details in [8.2\)](#page-42-0), Ring of Fire (details in [8.3\)](#page-42-1) and AC back- ground (details in [7.1\)](#page-37-1). The systematic uncertainty for rapidity gap events includes the cuts on East BBC veto cuts (details in [8.2\)](#page-42-0) and Ring of Fire (de- tails in [8.3\)](#page-42-1). The systematic uncertainty for semi-exclusive process includes the cuts on West BBC veto cuts (details in [8.2\)](#page-42-0), Ring of Fire (details in [8.3\)](#page-42-1), energy sum cuts (details in [8.4\)](#page-42-2) and AC background (details in [8.4\)](#page-42-2).

### <span id="page-41-1"></span>**8.1 Method for systematic uncertainty**

 To study the systematic uncertainty for the BBC veto cuts, Ring of Fire and the energy sum cuts the Bayesian method is applied [\[21\]](#page-67-4). For each term of systematic uncertainty study, we calculate the *A<sup>N</sup>* standard deviation among the variation cuts. However, only the cuts with variations deemed significant would be included. If a cut with variations produces a maximum value with 495 statistical uncertainty  $A_N(1) \pm \delta_1$  and a minimum value with statistical uncertainty  $A_N(2) \pm \delta_2$ , only when  $\frac{|A_N(1) - A_N(2)|}{\sqrt{X^2 - \delta_2^2}}$  $\frac{1}{2}$  tainty  $A_N(2) \pm \delta_2$ , only when  $\frac{|A_N(1) - A_N(2)|}{\sqrt{|\delta_1^2 - \delta_2^2|}} > 1$  the standard variation will be used for this systematic uncertainty term, otherwise this systematic uncertainty term will be assigned 0 (Barlow check) [\[21\]](#page-67-4). All the systematic uncertainty for each  $x_F$  bin will be calculated individually.

<span id="page-42-3"></span>

Variation	$-20$		$-10$ + $+10$	$+20$
East Large BBC ADC sum cut	60	70	90	100
East Small BBC ADC sum cut	70	80	100	110
West Large BBC ADC sum cut	40	50	70	80
West Small BBC ADC sum cut	60	70		100

Table 8.1: List of BBC veto cut values for systematic uncertainty study.

### <span id="page-42-0"></span> **8.2 Systematic uncertainty for the BBC veto cuts**

 The BBC veto cuts include East Large BBC ADC sum < 80 and East Small BBC ADC sum < 90, for the single diffractive process and the rapidity gap events. They also include West Large BBC ADC sum < 60 and West Small BBC ADC sum < 80, for the semi-exclusive process. We change the cut values for Large BBC and Small BBC ADC sum to study the systematic uncertainty, as shown in Tab. [\(8.1\)](#page-42-3). We calculate the  $A_N$  with its statistical uncertainty for each cut standard variation with varying the cuts. Then, we use the Barlow check to determine whether to keep the standard derivation as systematic uncertainty [\[21\]](#page-67-4). Note, the systematic uncertainty for Large BBC and Small BBC ADC sum cuts are studied separately for each process.

#### <span id="page-42-1"></span>**8.3 Ring of Fire**

 The Ring of Fire is a kind of background related to the FMS-sm-bs3 trigger. This trigger is targeted at the inner region of FMS, which is close to the beam. It's generally recognized that the beam remnants are accepted by FMS-sm-bs3 trigger. Therefore, the effect of this trigger will be considered as one source of systematic uncertainty. The systematic uncertainty for the Ring of Fire will be the  $A_N$  result difference between considering this trigger and excluding this trigger. In addition, the Barlow check is applied to determine whether to keep the standard derivation as systematic uncertainty.

### <span id="page-42-2"></span>**8.4 Energy sum cut uncertainty**

522 To study the energy sum cut uncertainty, we varied the energy cut per  $x_F$  bin by  $\pm 10$  GeV and  $\pm 5$  GeV. Table [\(8.2\)](#page-43-1) shows the exact values for studying the  $\frac{1}{524}$  energy sum cut uncertainty. We calculate the  $A_N$  with its statistical uncertainty for each cut standard variation with varying these energy sum cuts. Then, we

<span id="page-43-1"></span>

EM-jet $x_F$	$E_{sum}$ cut (-10 GeV)	$E_{sum}$ cut (-5 GeV)	$E_{sum}$ cut (+5 GeV)	$E_{sum}$ cut (+10 GeV)
$0.2 - 0.25$	$E_{sum}$ < 100 GeV	$E_{sum}$ < 105 GeV	$E_{sum}$ < 115 GeV	$E_{sum}$ < 120 GeV
$0.25 - 0.3$	$E_{sum}$ < 100 GeV	$E_{sum}$ < 105 GeV	$E_{sum}$ < 115 GeV	$E_{sum}$ < 120 GeV
$0.3 - 0.35$	$E_{sum}$ < 105 GeV	$E_{sum}$ < 110 GeV	$E_{sum}$ < 120 GeV	$E_{sum}$ < 125 GeV
$0.35 - 0.4$	$E_{sum}$ < 105 GeV	$E_{sum}$ < 110 GeV	$E_{sum}$ < 120 GeV	$E_{sum}$ < 125 GeV
$0.4 - 0.45$	$E_{sum}$ < 110 GeV	$E_{sum}$ < 115 GeV	$E_{sum}$ < 125 GeV	$E_{sum}$ < 130 GeV

Table 8.2: Energy sum cuts for semi-exclusive process in the energy sum cut uncertainty study

<sup>526</sup> use the Barlow check to determine whether to keep the standard derivation as <sup>527</sup> systematic uncertainty [\[21\]](#page-67-4).

#### <span id="page-43-0"></span><sup>528</sup> **8.5 Polarization uncertainty**

 The blue beam and yellow beam polarization are used to calculate the  $A_N$  results. As a habit, the uncertainty of beam polarization uncertainty is listed  $_{531}$  independently. The beam polarization measurement results are provided by the CNI group, which develops, maintains, and operates the RHIC polarimeter measurement. The beam polarization measurement results are listed in the table  $\epsilon_{534}$  on the webpage [\[22\]](#page-67-5). In the webpage, the starting time  $(t_0)$ , the polarization of the blue (yellow) beam at the beginning of every fill  $(P_0)$ , the decay rate <sup>536</sup>  $\left(\frac{dP}{dt}\right)$  are provided for each fill. For each event, the beam polarization can be calculated from the time difference from the beginning of the fill using Equ. [\(8.1\)](#page-43-2), where *tevent* is the time of each event. The beam polarization for each  $_{539}$  run can be calculated by Equ.  $(8.2)$ , where  $t_{run}$  is the time of the center of the run. The beam polarization for each fill can be calculated using the weighted average run polarization with Equ.  $(8.3)$ , where  $L_{run}$  is the luminosity of each run. However, since *Lrun* is proportional to the number of events in each run, the number of events in each run will be replacing the luminosity of each run in the calculation.

<span id="page-43-2"></span>
$$
P_{event} = P_0 + \frac{dP}{dt}(t_{event} - t_0)
$$
\n
$$
(8.1)
$$

<span id="page-43-3"></span>
$$
P_{run} = P_0 + \frac{dP}{dt}(t_{run} - t_0)
$$
\n(8.2)

<span id="page-43-4"></span>
$$
P_{fill} = \frac{\sum_{run} L_{run} P_{run}}{\sum_{run} L_{run}} \tag{8.3}
$$

<sup>545</sup> The beam polarization uncertainty includes the scale uncertainty, fill-to-fill <sup>546</sup> uncertainty, and uncertainty from the profile correction procedure [\[23\]](#page-67-6).

<sup>547</sup> The scale uncertainty is related to the polarization measurement methods. <sup>548</sup> It includes H-jet scale, H-jet background and pC scale. For run 15, the scale  $549$  uncertainty is  $3\%$  [\[23\]](#page-67-6).

<sup>550</sup> The relative uncertainty of the profiles correction for one beam in one fill <sup>551</sup> is 2.2%. For a set of M fills, the relative profile correction for the single-spin asymmetry measurement is  $\sigma(profile)/P = 2.2\%/$ √ 552 asymmetry measurement is  $\sigma(profile)/P = 2.2\% / \sqrt{M}$  [\[23\]](#page-67-6). For the run 15 <sup>553</sup> FMS dataset, this uncertainty is about 0.3%.

<sup>554</sup> The fill-to-fill uncertainty is propagated based on Equ. [\(8.3\)](#page-43-4) with the uncertainty of  $P_0$  and  $\frac{dP}{dt}$ . The uncertainty for these two terms  $(\sigma(P_0))$  and  $(\sigma(\frac{dP}{dt}))$ <sup>556</sup> for either blue beam or yellow beam can be obtained in [\[22\]](#page-67-5). This uncertainty  $557$  can be expressed in Equ.  $(8.4)$ . The third term on the right side of the equation <sup>558</sup> is due to the sensitivity of the measurement of the energy scale of the nuclei in  $\frac{1}{559}$  the pC polarimetry [\[14\]](#page-66-12), and it's negligible. However, for the term (Equ.  $(8.5)$ ), <sup>560</sup> this correction is overcounting for the measurement using a fraction of the run <sup>561</sup> period. Therefore, a correction scale factor  $\sqrt{1 - \frac{M}{N}}$  is applied for the second  $_{562}$  term, which is shown in Equ. [\(8.6\)](#page-44-3). For this analysis, N=54 and M=142. The <sup>563</sup> fill-to-fill uncertainty for single diffractive EM-jet analysis is about 0.3%.

<span id="page-44-1"></span>
$$
\sigma^{2}(P_{fill}) = \sigma^{2}(P_{0}) + \sigma^{2}(\frac{dP}{dt}) \cdot (\frac{\sum_{run} t_{run} L_{run}}{L_{fill}} - t_{0})^{2} + (\frac{\sigma(fill - to - fill)}{P})^{2} \cdot P_{fill}^{2}
$$
\n(8.4)

<span id="page-44-2"></span>
$$
P_{set}^2 = \left(\frac{\sum_{run} t_{run} L_{run}}{L_{fill}}\right) \tag{8.5}
$$

<span id="page-44-3"></span>
$$
P_{fill-to-fill\ scale}^{2} = (1 - \frac{N}{M}) \cdot P_{set}^{2}
$$
 (8.6)

<sup>564</sup> Finally, the polarization uncertainty is calculated in the quadrature. For the <sup>565</sup> single diffractive EM-jet analysis, it's about 3%.

### <span id="page-44-0"></span><sup>566</sup> **8.6 Summary for the systematic uncertainty**

 The final systematic uncertainty for single diffractive process and rapidity gap boss events will be counted bin by bin  $(x_F \text{ bin})$ , and they are calculated as  $\sqrt{\sum_i \sigma_i^2}$ . Table [\(8.3\)](#page-45-0) and Table [\(8.4\)](#page-45-1) show the systematic uncertainty for each and final term for the blue beam  $A_N$  and yellow beam  $A_N$  for all photon multiplicity EM-jets from single diffractive process, respectively. Table [\(8.5\)](#page-45-2) and Table [\(8.6\)](#page-46-0) show the systematic uncertainty for each and final term for the blue beam  $A_N$  and yellow beam  $A_N$  for one or two-photon multiplicity EM-jets from single diffractive process, respectively. Table [\(8.7\)](#page-46-1) and Table [\(8.8\)](#page-46-2) show the systematic uncertainty for each and final term for the blue beam  $A_N$  and yellow beam  $A_N$  for three or more photon multiplicity EM-jets from single diffractive process, respectively.

<span id="page-45-0"></span>

$x_F$	Small BBC east	Large BBC east	Ring of Fire	Background	Summary
$0.2 - 0.25$	0.0026	0.0041		0.0044	0.0064
$0.25 - 0.3$			0.0022	0.0034	0.0041
$0.3 - 0.35$		0.0020		0.0032	0.0037
$0.35 - 0.4$	0.0017	0.0034		0.0035	0.0052
$0.4 - 0.45$	0.0022	0.0052	0.012	0.0041	0.014

Table 8.3: Systematic uncertainty for blue beam  $A_N$  for all photon multiplicity EM-jets from single diffractive process

<span id="page-45-1"></span>

$x_F$	Small BBC east	Large BBC east	Ring of Fire	Background	Summary
$0.2 - 0.25$	0.0027	0.0054		0.0043	0.0074
$0.25 - 0.3$	0.0028	0.0025		0.0034	0.0051
$0.3 - 0.35$		0.0046		0.0031	0.0056
$0.35 - 0.4$	0.0018	0.0048	0.0051	0.0035	0.0080
$0.4 - 0.45$	0.0013	0.0022		0.0040	0.0048

Table 8.4: Systematic uncertainty for yellow beam  $A_N$  for all photon multiplicity EM-jets from single diffractive process

 Also, table [\(8.9\)](#page-46-3) and Table [\(8.10\)](#page-46-4) show the systematic uncertainty for each and final term for the blue beam  $A_N$  and yellow beam  $A_N$  for all photon mul- tiplicity EM-jets from rapidity gap events, respectively. Table [\(8.11\)](#page-47-0) and Table [\(8.12\)](#page-47-1) show the systematic uncertainty for each and final term for the blue beam  $A_N$  and yellow beam  $A_N$  for one or two-photon multiplicity EM-jets from rapid- ity gap events, respectively. Table [\(8.13\)](#page-47-2) and Table [\(8.14\)](#page-47-3) show the systematic uncertainty for each and final term for the blue beam  $A_N$  and yellow beam  $A_N$  for three or more photon multiplicity EM-jets from rapidity gap events, respectively.

<sup>587</sup> Finally, Table [\(8.15\)](#page-48-0) and Table [\(8.16\)](#page-48-1) show the systematic uncertainty for  $\epsilon_{588}$  each and final term for the blue beam  $A_N$  and yellow beam  $A_N$  for one or <sup>589</sup> two-photon multiplicity EM-jets from semi-exclusive process, respectively.

<span id="page-45-2"></span>

$x_F$	Small BBC east	Large BBC east	Ring of Fire	Background	Summary
$0.2 - 0.25$	0.0040	0.0033		0.0057	0.0077
$0.25 - 0.3$	0.0024		0.0022	0.0046	0.0056
$0.3 - 0.35$	0.0018	0.0018	$\cup$	0.0044	0.0051
$0.35 - 0.4$	0.0032	0.0034	$\left($	0.0047	0.0066
$0.4 - 0.45$	0.0055	0.0072	0.022	0.0052	0.024

Table 8.5: Systematic uncertainty for blue beam *A<sup>N</sup>* for 1 or 2 photon multiplicity EM-jets from single diffractive process

<span id="page-46-0"></span>

$x_F$	Small BBC east	Large BBC east	Ring of Fire	Background	Summary
$0.2 - 0.25$	0.0035			0.0056	0.0065
$0.25 - 0.3$	0.0021	0.0035		0.0045	0.0061
$0.3 - 0.35$	0.0025	0.0041		0.0043	0.0064
$0.35 - 0.4$		0.0062		0.0046	0.0077
$0.4 - 0.45$	0.0016	0.0036	0.020	0.0052	0.021

Table 8.6: Systematic uncertainty for yellow beam  $A_N$  for 1 or 2 photon multiplicity EM-jets from single diffractive process

<span id="page-46-1"></span>

$x_F$	Small BBC east	Large BBC east	Ring of Fire	Background	Summary
$0.2 - 0.25$		0.0076		0.0068	0.010
$0.25 - 0.3$	0.0022	0.0028	0.0023	0.0051	0.0066
$0.3 - 0.35$				0.0046	0.0046
$0.35 - 0.4$		0.0047	0.0076	0.0055	0.010
$0.4 - 0.45$	0.0035	0.0053		0.0066	0.0091

Table 8.7: Systematic uncertainty for blue beam  $A_N$  for 3 or more photon multiplicity EM-jets from single diffractive process

<span id="page-46-2"></span>

$x_F$	Small BBC east	Large BBC east	Ring of Fire	Background	Summary
$0.2 - 0.25$	0.0098	0.014		0.0067	0.019
$0.25 - 0.3$	0.0037	0.0033	$\left( \right)$	0.0046	0.0071
$0.3 - 0.35$	0.0030	0.0081	0.0046	0.0045	0.011
$0.35 - 0.4$	0.0037	0.0047	0.0051	0.0052	0.011
$0.4 - 0.45$			0.015	0.0065	0.017

Table 8.8: Systematic uncertainty for yellow beam *A<sup>N</sup>* for 3 or more photon multiplicity EM-jets from single diffractive process

<span id="page-46-3"></span>

$x_F$	Small BBC east	Large BBC east	Ring of Fire	Summary
$0.1 - 0.2$		0.0064		0.0064
$0.2 - 0.25$	0.0016			0.0016
$0.25 - 0.3$	0.00051	0.00096	0.00042	0.0011
$0.3 - 0.35$	0.00084			0.00084
$0.35 - 0.4$	0.0014		0.0033	0.0036
$0.4 - 0.45$	0.0010	0.0011	$\theta$	0.0015

Table 8.9: Systematic uncertainty for blue beam  $\mathcal{A}_N$  for all photon multiplicity EM-jets from rapidity gap events

<span id="page-46-4"></span>

$x_F$	Small BBC east	Large BBC east	Ring of Fire	Summary
$0.1 - 0.2$	0.0027		$\left( \right)$	0.0027
$0.2 - 0.25$	0.00052	0.0019	0	0.0019
$0.25 - 0.3$	0.00064	0.0012	0	0.0013
$0.3 - 0.35$	0.00066	0.00047		0.00081
$0.35 - 0.4$	0.00092	0.0013	0.0023	0.0029
$0.4 - 0.45$		0.0012	$\theta$	0.0012

Table 8.10: Systematic uncertainty for yellow beam *A<sup>N</sup>* for all photon multiplicity EM-jets from rapidity gap events

<span id="page-47-0"></span>

$x_F$	Small BBC east	Large BBC east	Ring of Fire	Summary
$0.1 - 0.2$	0.0028	0.0061		0.0067
$0.2 - 0.25$	0.0018	0.0019		0.0026
$0.25 - 0.3$			0.00070	0.00070
$0.3 - 0.35$	$\mid 0.00094$		0.0023	0.0025
$0.35 - 0.4$	$\sqrt{0.0024}$	0.0017		0.0030
$0.4 - 0.45 \pm 0.00074$		0.0019	0	0.0020

Table 8.11: Systematic uncertainty for blue beam *A<sup>N</sup>* for 1 or 2 photon multiplicity EM-jets from rapidity gap events

<span id="page-47-1"></span>

$x_F$	Small BBC east	Large BBC east	Ring of Fire	Summary
$0.1 - 0.2$	0.0027			0.0027
$0.2 - 0.25$	0.00081	0.0024	$\theta$	0.0018
$0.25 - 0.3$	0.0015	0.0011	$\theta$	0.0019
$0.3 - 0.35$	0.00086	0.0011	0.0017	0.0022
$0.35 - 0.4$		0.0015	0.0034	0.0037
$0.4 - 0.45$	$-0.00069$	0	0.0059	0.0060

Table 8.12: Systematic uncertainty for yellow beam  $A_N$  for 1 or 2 photon multiplicity EM-jets from rapidity gap events

<span id="page-47-2"></span>

$x_F$	Small BBC east	Large BBC east	Ring of Fire	Summary
$0.1 - 0.2$		0.0088		0.0088
$0.2 - 0.25$	0.0015			0.0015
$0.25 - 0.3$				
$0.3 - 0.35$	0.00082		0.0018	0.0020
$0.35 - 0.4$			0.0040	0.0040
$0.4 - 0.45$	0.0028	$0.0021\,$	0.0036	0.0050

Table 8.13: Systematic uncertainty for blue beam  $A_N$  for 3 or more photon multiplicity EM-jets from rapidity gap events

<span id="page-47-3"></span>

$x_F$	Small BBC east	Large BBC east	Ring of Fire	Summary
$0.1 - 0.2$	0.0045			0.0045
$0.2 - 0.25$		0.0028		0.0028
$0.25 - 0.3$	0.0014	0.0026		0.0029
$0.3 - 0.35$	0.0014			0.0014
$0.35 - 0.4$	0.0017	0.0014		0.0022
$0.4 - 0.45$	0.0017	0.0021	0.0046	0.0053

Table 8.14: Systematic uncertainty for yellow beam *A<sup>N</sup>* for 3 or more photon multiplicity EM-jets from rapidity gap events

<span id="page-48-0"></span>

Blue beam $x_F$	Small BBC west	Large BBC west	Ring of Fire	. Energy sum	Background	Bummary
$0.2 - 0.25$		0.033		0.028	0.0033	0.043
$0.25 - 0.3$	0.0081	0.021	0		0.0031	0.023
$0.3 - 0.35$	0.0058		0.010	0.011	0.0027	0.017
$0.35 - 0.4$	0.0072	0.011	0	0.040	0.0011	0.041
$0.4 - 0.45$	0.012	0.015	0		0.0045	0.019

Table 8.15: Systematic uncertainty for blue beam *A<sup>N</sup>* for 1 or 2 photon multiplicity EM-jets from semi-exclusive process

<span id="page-48-1"></span>

Yellow beam $x_F$	Small BBC west	Large BBC west	Ring of Fire	Energy sum	Background	Summary '
$0.2 - 0.25$	0.018	0.014			0.00059	0.023
$0.25 - 0.3$	0.012		0.0045	0.027	0.00068	0.030
$0.3 - 0.35$		0.015		0.0012	0.0011	0.019
$0.35 - 0.4$		0.010	0.017		0.0042	0.020
$0.4 - 0.45$				0.011	0.0032	0.012

Table 8.16: Systematic uncertainty for yellow beam *A<sup>N</sup>* for 1 or 2 photon multiplicity EM-jets from semi-exclusive process

# <span id="page-49-0"></span><sup>591</sup> *AN* **Analysis Method and** <sup>592</sup> **Results**

### <span id="page-49-1"></span><sup>593</sup> **9.1** *A<sup>N</sup>* **Extraction**

 $594$  The cross-ratio method is used to extract the  $A_N$ , and the corresponding for-595 mulas are shown in Equ. [\(9.1\)](#page-49-2) and Equ. [\(9.2\)](#page-49-3). In both equations,  $\epsilon$  stands 596 for the raw asymmetry.  $N^{\uparrow(\downarrow)}(\phi)$ ,  $N^{\uparrow(\downarrow)}(\phi + \pi)$  are the yields detected at  $\phi$ ,  $\phi + \pi$  for spin up (down) state, where  $\phi$  is the azimuthal angle of the EM-jet <sup>598</sup> in the lab frame. In this analysis, the full 2*π* azimuthal coverage is split into 16 <sup>599</sup> ranges. *P* is the average polarization of the proton beam, where the polariza-600 tion for each event is calculated from Equ. [\(8.1\)](#page-43-2). A cosine fit  $(p_0 \cos(\phi) + p_1)$  is  $\epsilon_{601}$  applied to the entire data after all the event selection criteria to extract the  $A_N$  $602$  from the raw asymmetry in Eq.  $(9.2)$ , while the constant term  $p_1$  could provide <sup>603</sup> cross-check for possible unidentified asymmetry, but this analysis does not take <sup>604</sup> it into account.

<span id="page-49-2"></span>
$$
\epsilon = \frac{\sqrt{N^{\dagger}(\phi)N^{\dagger}(\phi+\pi)} - \sqrt{N^{\dagger}(\phi)N^{\dagger}(\phi+\pi)}}{\sqrt{N^{\dagger}(\phi)N^{\dagger}(\phi+\pi)} + \sqrt{N^{\dagger}(\phi)N^{\dagger}(\phi+\pi)}}
$$
(9.1)

<span id="page-49-3"></span>
$$
\epsilon = P A_N \cos(\phi) \tag{9.2}
$$

<sup>605</sup> This method takes advantage of detector azimuthal symmetry and cancels <sup>606</sup> effects due to the non-uniform detector efficiency and the time-dependent lumi-<sup>607</sup> nosity.

### <span id="page-50-0"></span><sup>608</sup> **9.2 Single diffractive EM-jet** *A<sup>N</sup>*

609 Three cases of EM-jet are studied for  $A_N$  of the single diffractive process: the <sup>610</sup> EM-jet with all photon multiplicity, with only one or two-photon multiplicity, <sup>611</sup> and with three or more photon multiplicity. Figure [\(9.1\)](#page-51-0) shows the results for 612 the single diffractive EM-jet  $A_N$  as a function of  $x_F$  for the three cases of photon <sup>613</sup> multiplicity mentioned above. Among the three panels in the figure, the blue  $\epsilon_{614}$  points are for the blue beam  $A_N$ , represented as  $x_F > 0$ , while the red points 615 are for the yellow beam  $A_N$ , represented as  $x_F < 0$ . The top panel is the results <sup>616</sup> for all photon multiplicity. The statistical uncertainty is shown in bar, while the  $617$  systematic uncertainty is shown in shaded box. The 2.7  $\sigma$  non-zero significance 618 is observed for the blue beam  $A_N$ . The blue beam  $A_N$  for the EM-jets with one 619 or two photon multiplicity case shows about 2.5  $\sigma$  non-zero significance, showing  $620$  in the middle panel. However, the blue beam  $A_N$  for the EM-jets with three or  $\epsilon_{621}$  more photon multiplicity cases is consistent with zero. The EM-jet  $A_N$  for one <sup>622</sup> or two-photon multiplicity case is larger than that for all photon multiplicity <sup>623</sup> case and for three or more-photon multiplicity case, which is consistent with the <sup>624</sup> results shown in the inclusive processes [\[24\]](#page-67-7).

### <span id="page-50-1"></span>625 **9.3** Rapidity gap events EM-jet  $A_N$

 $\epsilon_{626}$  For the  $A_N$  of the rapidity gap events, the same three cases of the EM-jet are <sup>627</sup> explored: the EM-jet with all photon multiplicity, with only one or two-photon  $628$  multiplicity, and with three or more photon multiplicity. Figure  $(9.2)$  shows the 629 results for the EM-jet  $A_N$  of the rapidity gap events as a function of  $x_F$  for  $\epsilon_{630}$  the three cases of photon multiplicity mentioned above. The  $A_N$  of all photon <sup>631</sup> multiplicity and one or two-photon multiplicity cases shows the non-zero value  $632$  but with a similar scale as for the  $A_N$  of the inclusive process with the same  $\frac{633}{100}$  two cases of photon multiplicity [\[24\]](#page-67-7). The  $A_N$  of the three or more photon <sup>634</sup> multiplicity EM-jets are shown to be consistent with zero. In addition, the  $\epsilon_{\text{55}}$  yellow beam  $A_N$  is also consistent with zero, regardless of photon multiplicity.  $\epsilon_{366}$  Furthermore, to better visualize the  $A_N$  contributions of the single diffractive <sup>637</sup> process and the rapidity gap events to the inclusive process, a direct comparison  $\epsilon_{38}$  plot among the  $A_N$  for inclusive process, diffractive process, and rapidity gap <sup>639</sup> events for one or two-photon multiplicity, and three or more-photon multiplic- $\epsilon_{40}$  ity are shown in Fig. [\(9.3\)](#page-54-0). The  $A_N$  for the single diffractive process and the <sup>641</sup> rapidity gap events are consistent with that for inclusive process within uncer- $642$  tainty coverage for most of the  $x_F$  regions for both multiplicity cases. The  $A_N$ <sup>643</sup> for the three processes for EM-jets with three or more-photon multiplicity are <sup>644</sup> all consistent with each other. These direct comparison results indicate that

<span id="page-51-0"></span>

Figure 9.1:  $A_N$  for single diffractive events as a function of  $x_F$  for three different photon multiplicity cases: all photon multiplicity (top), one or two-photon multiplicity (middle), and three or more photon multiplicity (bottom). The *A<sup>N</sup>* for  $x_F<0$  (red points) shifts -0.013 along the x-axis.

<sup>645</sup> the single diffractive process can not provide evidence that it contributes to the  $_{646}$  large  $A_N$  in the inclusive process.

### <span id="page-52-0"></span>647 **9.4** Semi-exclusive EM-jet  $A_N$

<sup>648</sup> For the semi-exclusive process, only the case of EM-jet with 1 or 2 photon is  $\epsilon_{49}$  explored to extract the  $A_N$ , because the majority of the events are with 1 or <sup>650</sup> 2 photon multiplicity EM-jet. Figure [\(9.4\)](#page-55-0) shows the semi-exclusive EM-jet  $A_N$  as a function of EM-jet  $x_F$ . Constant fit is applied to check the n-sigma  $\epsilon_{652}$  significance for non-zero  $A_N$  value among these  $x_F$  regions. The blue beam 653 *A<sub>N</sub>* is 3.1 $\sigma$  to be non-zero, while the yellow beam  $A_N$  is 1.4 $\sigma$  to be non-zero. 654 However, the semi-exclusive EM-jet  $A_N$  is negative, which is different from  $A_N$ <sup>655</sup> in the inclusive process. Further theories are needed to understand such different <sup>656</sup> sign.

<span id="page-53-0"></span>

Figure 9.2:  $A_N$  for rapidity gap events as a function of  $x_F$  for three different photon multiplicity cases: all photon multiplicity (top), one or two-photon multiplicity (middle), and three or more photon multiplicity (bottom). The  $A_N$  for  $x_F < 0$  (red points) shifts -0.013 along the x-axis.

<span id="page-54-0"></span>

Figure 9.3:  $A_N$  for inclusive process (red), single diffractive process (blue), and the rapidity gap events (purple) as a function of  $x_F$  for one or two-photon multiplicity case (top panel) and three or more-photon multiplicity (bottom panel). The  $A_N$  for single diffractive process shifts  $-0.008$  along the x-axis, and the  $A_N$  for rapidity gap events shifts  $+0.008$  along the x-axis

<span id="page-55-0"></span>

Figure 9.4:  $A_N$  for the semi-exclusive process with 1 or 2 photon multiplicity EM-jets as a function of EM-jet  $x_F$ . The blue points are for  $x_F > 0$ , while the red points are for  $x_F < 0$ .

## <span id="page-56-0"></span><sup>658</sup> **Cross section fraction study**

 The cross section fraction is the fraction of the cross section in the single diffrac- tive process to the cross section in the inclusive process at forward region. This study can provide evidence to develop theories to understand the underlying  $\epsilon_{662}$  mechanism for the  $A_N$  in the diffractive process.

 $\epsilon_{663}$  The cross section for the single diffractive process ( $\sigma_{SD}$ ) can be calculated using Equ. [\(10.1\)](#page-56-1). The cross section for the inclusive process ( $\sigma_{inc}$ ) can be calcu-665 lated using Equ. [\(10.2\)](#page-56-2).  $N_{SD}$  and  $N_{inc}$  denote as the yields of single diffractive 666 events and inclusive events, respectively.  $\varepsilon_{RP}$  and  $\varepsilon_{BBC}$  are the Roman Pot efficiency and BBC efficiency, respectively. Purity indicate the fraction of the real single diffractive process in the single diffractive process. *εFMS* denotes as 669 FMS efficiency,  $\varepsilon_{trigger}$  denotes as trigger efficiency,  $\pounds$  denotes as integrated lu- minosity. However, it is difficult to calculate the FMS efficiency and the trigger efficiency. Therefore, we do not calculate the absolute cross section for either process. However, if we assume the FMS efficiency, the trigger efficiency and the integrated luminosity are the same between two processes, all these terms can cancel out between each other when we calculate their ratio. In that case, the cross section fraction can be calculated using Equ. [\(10.3\)](#page-56-3).

<span id="page-56-1"></span>
$$
\sigma_{SD} = \frac{N_{SD} \times purity}{\mathcal{L} \times \varepsilon_{RP} \times \varepsilon_{BBC} \times \varepsilon_{FMS} \times \varepsilon_{trigger}} \tag{10.1}
$$

<span id="page-56-2"></span>
$$
\sigma_{inc} = \frac{N_{inc}}{\mathcal{L} \times \varepsilon_{FMS} \times \varepsilon_{trigger}} \tag{10.2}
$$

<span id="page-56-3"></span>
$$
\frac{sigma_{SD}}{\sigma_{inc}} = \frac{N_{SD} \times purity}{N_{inc} \times \varepsilon_{RP} \times \varepsilon_{BBC}} \tag{10.3}
$$

<sup>676</sup> Purity can be calculated using the zerobias event background estimation  $677$  (detail in Sec. [\(7.1\)](#page-37-1)). The fraction of the accidental coincidence is  $1.8\% \pm 0.1\%$ , 678 so the purity is  $98.2\% \pm 0.1\%$ .

 The RP efficiency can be estimated using the single diffractive process sim- ulation using the Pythia simulation and RP simulation (pp2pp). It can be calculated by the fraction of the events with good east RP track after the RP simulation in the detector level to the events with proton on east side in the Pythia simulation in the particle level. Both the good east RP track in the RP simulation and the proton track in the particle level simulation are required to 685 be within  $0 < \xi < 0.15$  region. The RP efficiency is about 11.4%.

 The BBC efficiency be estimated using the single diffractive process simu- lation using the Pythia simulation and STAR simulation (Geant3) with BBC simulation option. This efficiency can be calculated by the fraction of the events passing the BBC east veto (detail in Sec. [\(3.3\)](#page-19-0)) to all the events with east proton intact. The BBC efficiency is about 99.9%.

 The systematic uncertainty for the RP efficiency is 6.5%, based on the STAR central exclusive analysis [\[25\]](#page-67-2). The systematic uncertainty for the BBC efficiency  $\epsilon_{93}$  is 10%, based on STAR single diffractive study [\[26\]](#page-67-3).

 $F_{694}$  The overall cross section fraction is  $0.586\% \pm 0.070\%$ . The differential cross 695 section is studied as a function of EM-jet  $x_F$  region, shown in Fig. [\(10.1\)](#page-58-0). The single diffractive process cross section is very small compared to the inclusive process cross section, which shows that it can not have significant contribution  $\epsilon_{698}$  to the large  $A_N$  in inclusive process.

<span id="page-58-0"></span>

Figure 10.1: Cross section fraction of the single diffractive process  $(\sigma_{SD})$  to the inclusive process  $(\sigma_{inc})$  as a function of  $x_F$ .

# <span id="page-59-0"></span>**Conclusion**

 The transverse single-spin asymmetry as a function of EM-jet  $x_F$  from single diffractive process is explored. The all photon multiplicity and one or two- photon multiplicity EM-jet  $A_N$  for  $x_F > 0$  from the single diffractive process show the non-zero values with more than 2- $\sigma$  significance. The  $A_N$  for  $x_F < 0$  from the single diffractive process and rapidity gap events are shown to be consistent with zero. Furthermore, the  $A_N$  for inclusive process, the single diffractive process, and the rapidity gap events are consistent with each other within uncertainty. In addition, the cross section fraction study provide evidence that the single diffractive process cross section is very small compared to the inclusive process cross section. Therefore, no strong evidence exists that these process with the unpolarized proton intact will contribute to the large  $A_N$  in the inclusive process.

 The transverse single-spin asymmetry for semi-exclusive process with polar- ized proton intact is negative with more than  $3\sigma$  significance to be non-zero, which also can not have great contribution to the large  $A_N$  in the inclusive  $_{716}\,$  process. Such a different sign on the  $A_N$  requires further theories to explain.

# <span id="page-60-0"></span><sup>717</sup> **Appendix A**

# <sup>718</sup> **Run list**

<span id="page-60-1"></span>

<sup>719</sup> Continued on next page

### Table A.1: Run list (Continued)



### Table A.1: Run list (Continued)



Table A.1: Run list (Continued)

16089003	16089004	16089005	16089015	16089016	16089017	16089018
16089019	16089020	16089024	16089026	16089027	16089028	16089029
16089030	16089031	16089041	16089042	16089043	16089044	16089045
16089046	16089047	16089048	16089049	16089050	16089051	16089052
16089053	16089054	16090001	16090002	16090003	16090004	16090005
16090015	16090016	16090017	16090018	16090019	16090020	16090021
16090022	16090023	16090024	16090025	16090026	16090027	16090028
16090029	16090030	16090038	16090039	16090041	16090042	16090044
16090045	16090046	16090047	16090048	16090049	16090050	16090051
16090052	16090053	16091003	16091004	16091005	16091006	16091007
16091008	16091009	16091010	16091011	16091012	16091013	16091014
16091039	16091040	16091042	16091057	16091061	16091062	16091063
16092001	16092002	16092003	16092014	16092015	16092016	16092017
16092018	16092019	16092020	16092021	16092022	16092023	16092031
16092033	16092034	16092035	16092036	16092037	16092040	16092042
16092044	16092048	16092049	16092050	16092051	16092052	16092053
16092054	16092055	16092063	16092064	16092065	16092066	16092067
16092068	16092069	16092070	16092071	16093001	16093002	16093003
16093004	16093010	16093011	16093012	16093013	16093014	16093015
16093016	16093017	16093018				

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## <span id="page-64-0"></span>**Appendix B**

# **Derivation for the AC events effect to the uncertainty**

 The effect for the uncertainty in  $A_N$  calculation regarding the AC events is derived as follows. First of all, the corrected  $A_N$  is shown in Equ. [\(B.1\)](#page-64-1).  $A_N(sig)$  is the corrected  $A_N$ , while  $A_N(mea)$  is the measured  $A_N$  which contains the effect of AC events. *frac*(*sig*) is the signal fraction, while *frac*(*bkg*) is the AC background fraction, which is about 1.8% (detailed in Sec.  $(7.1)$ ). The error propagation for Equ. [\(B.1\)](#page-64-1) is expressed in Equ. [\(B.2\)](#page-65-0). Since the AC background fraction and its uncertainty are very small, the second and the third term are neglectable. Therefore, only the first term related to the statistical uncertainty of the measured asymmetry will be kept. The difference in the uncertainty between with and without the AC event correction will be assigned as systematic uncertainty.

<span id="page-64-1"></span>
$$
A_N(sig) = \frac{A_N(mea) - frac(bkg) * A_N(bkg)}{frac(sig)} = \frac{A_N(mea) - frac(bkg) * A_N(bkg)}{1 - frac(bkg)}
$$
(B.1)

<span id="page-65-0"></span>
$$
\sigma^2 = \left(\frac{\partial A_N(sig)}{\partial A_N(mea)}\right)^2 \sigma A_N^2(mea) + \left(\frac{\partial A_N(sig)}{\partial frac(bkg)}\right)^2 \sigma frac^2(bkg) + \left(\frac{\partial A_N(sig)}{\partial A_N(bkg)}\right)^2 \sigma A_N^2(bkg)
$$
  
\n
$$
= \left(\frac{1}{1 - frac(bkg)}\right)^2 \sigma A_N^2(mea) + \left(\frac{A_N(sig)}{1 - frac(bkg)}\right)^2 \sigma frac^2(bkg) + \left(\frac{frac(bkg)}{1 - frac(bkg)}\right)^2 \sigma A_N^2(bkg)
$$
  
\n
$$
= \left(\frac{1}{frac(sig)}\right)^2 \sigma A_N^2(mea) + \left(\frac{A_N(sig)}{frac(sig)}\right)^2 \sigma frac^2(bkg) + \left(\frac{frac(bkg)}{frac(sig)}\right)^2 \sigma A_N^2(bkg)
$$
  
\n
$$
\approx \left(\frac{1}{frac(sig)}\right)^2 \sigma A_N^2(mea)
$$
  
\n(B.2)

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