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Measurement of CollinearDrop jet mass and its correlation with substructure observables in pp collisions at $\sqrt{s} = 200$ GeV

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Jets are collimated sprays of final-state particles produced from initial high-momentum-transfer partonic scatterings in particle collisions. Substructure variables aim to reveal details of the parton fragmentation and hadronization processes that create a jet. By removing collinear radiation while maintaining most of the low-momentum (soft) radiation components, one can construct CollinearDrop jet observables, which have enhanced sensitivity to the soft phase space within jets. With data collected with the STAR detector, we present the first CollinearDrop jet measurement, corrected for detector effects with a machine learning method, MultiFold, and its correlation with SoftDrop groomed jet observables. We observe that the amount of grooming affects the angular and momentum scales of the first hard splitting of the jet and is related to the formation time of such splitting. These measurements indicate that the non-perturbative effects are strongly correlated with the perturbative fragmentation process.

Introduction High-energy particle collisions provide op- 58 15 portunities to study experimentally quarks and gluons 59 16 (partons), the fundamental degree of freedom in the $_{60}$ 17 theory of Quantum Chromodynamics (QCD). In some 18 of these collisions, incoming quarks and gluons (par-61 19 tons) interact with each other through the exchange of 20 a high-momentum virtual particle, producing outgoing 62 21 partons with high transverse momentum $(p_{\rm T})$. Such 63 22 outgoing partons are highly virtual and will undergo 64 23 a series of splitting processes as they come on mass 65 24 This process is called the parton shower, and shell. 25 can be described perturbatively in terms of the Dok-⁶⁶ 26 shitzer-Gribov-Lipatov-Altarelli-Parisi (DGLAP) evo-27 lution equations [1-3]. When the virtuality of the partons $_{68}$ 28 is comparable to the confinement scale Λ_{QCD} , the non-29 perturbative transition to baryons and mesons (hadrons), 70 30 known as hadronization, begins. Experimentally, the 71 31 spray of the final-state hadrons can be measured and $_{72}$ 32 clustered into jets. Jets reconstructed with a clustering $_{73}$ 33 algorithm [4] can serve as a proxy for the kinematics of $_{74}$ 34 the outgoing partons. 35 75

While the interaction among partons can be well 76 36 understood with the principles of perturbative QCD $_{77}$ 37 (pQCD), the non-perturbative components of the parton ₇₈ 38 shower and hadronization remain challenging for theo-79 39 retical calculations and rely mostly on phenomenological ⁸⁰ 40 models in Monte Carlo event generators. Measurements 81 41 of observables sensitive to such non-perturbative QCD $_{82}$ 42 (npQCD) effects will provide important tests for the 83 43 theories and constraints on the models. Together with 84 44 studies of observables calculable from pQCD, investiga- 85 45 tion of those sensitive to npQCD effects offers an avenue $_{86}$ 46 for a comprehensive understanding of the full parton-to- 87 47 hadron evolution picture. 48

Beyond the jet $p_{\rm T}$, or other combinations of the jet ⁸⁹ 49 four-momentum observables, jet substructure observ-90 50 ables [5] are useful tools that can provide insight into 91 51 the parton shower and hadronization processes. To en- 92 52 hance perturbative contributions, SoftDrop [6] grooming 93 53 is often used to remove wide-angle soft radiation within 94 54 the jet. The procedure, detailed in Ref. [6], starts by re- 95 55 clustering the jet with an angular-ordered sequential re- 96 56 combination algorithm called Cambridge/Aachen [7, 8]. 97 57

Then the last step of the clustering is undone and the softer prong is removed until the SoftDrop condition is satisfied:

$$z = \frac{\min(p_{\mathrm{T},1}, p_{\mathrm{T},2})}{p_{\mathrm{T},1} + p_{\mathrm{T},2}} > z_{\mathrm{cut}} (R/R_{\mathrm{jet}})^{\beta}$$
(1)

where $z_{\rm cut}$ is the SoftDrop momentum fraction threshold, β is an angular exponent, $R_{\rm jet}$ is the jet resolution parameter, $p_{\rm T,1,2}$ are the transverse momenta of the two prongs that constitute a subjet, and R is defined as

$$R = \sqrt{(y_1 - y_2)^2 + (\phi_1 - \phi_2)^2}$$
(2)

with $y_{1,2}$ and $\phi_{1,2}$ being the rapidities and azimuthal angles of the two prongs, respectively.

z and R describe the momentum imbalance and the opening angle of the subjet, respectively. They are subscripted "g" when the subjet passes the SoftDrop condition Eq. 1 and the procedure stops.

Although the SoftDrop groomed jet substructure observables have been extensively studied both experimentally [9–14] and theoretically [15], the wide-angle and soft radiation which are dominated by npQCD processes, have not yet been explored in detail.

One set of observables that are sensitive to the soft wide-angle radiation are known as CollinearDrop [16]. The general case involves the difference of two different SoftDrop selections $SD_1 = (z_{cut,1}, \beta_1)$ and $SD_2 = (z_{cut,2}, \beta_2)$ on the same jet. For nonzero values of SD_1 and SD_2 parameters with $z_{cut,1} \leq z_{cut,2}$ and $\beta_1 \geq \beta_2$, SD_1 reduces the wide-angle contributions from initialstate radiation (ISR), underlying event (UE) and pileup, while removing what is left after applying SD_2 also reduces the collinear contributions from fragmentation.

As the QCD parton shower is angular ordered [17], the soft wide-angle radiation captured by the CollinearDrop jet observables happens on average at an early stage of the shower. Unlike CollinearDrop, SoftDrop then captures the late stage collinear and perturbative splittings. Therefore, a simultaneous measurement of CollinearDrop jet and SoftDrop jet observables can help illustrate how the different stages of the parton shower are correlated. Note that both the CollinearDrop and SoftDrop observables also could be sensitive to hadronization effects.

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⁹⁸ However, simulations from Monte Carlo event genera-¹⁵¹
⁹⁹ tors show that the correlations between them are robust¹⁵²
¹⁰⁰ against such effects. ¹⁵³

The CollinearDrop jet mass is defined in terms of the¹⁵⁴ ungroomed jet mass M and the SoftDrop groomed jet¹⁵⁵ mass $M_{\rm g}$: ¹⁵⁶

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$$M_{(g)} = \left| \sum_{i \in (\text{groomed}) \text{ jet}} p_i \right| = \sqrt{E_{(g)}^2 - |\vec{\mathbf{p}}_{(g)}|^2}, \quad (3)_{159}^{158}$$

where p_i is the four-momentum of the *i*th constituent₁₆₁ in a (groomed) jet, and $E_{(g)}$ and $\vec{\mathbf{p}}_{(g)}$ are the energy₁₆₂ and three-momentum vector of the (groomed) jet, respec-₁₆₃ tively. We denote the CollinearDrop groomed jet mass₁₆₄ by *a*:

$$a = \frac{M^2 - M_{\rm g}^2}{p_{\rm T}^2}.$$
 (4)¹⁶⁷₁₆₈

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¹¹¹ *a* is calculable in Soft Collinear Effective Field Theory¹⁰⁹₁₇₀ ¹¹² (SCET) at the parton level [16].

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In this paper, we present measurements of the 113 CollinearDrop groomed jet mass, to study the less-114 explored phase space of soft and wide-angle radiation; 115 we also measure the correlation of the CollinearDrop 175116 groomed mass with $R_{\rm g}$ and $z_{\rm g}$, in pp collisions at \sqrt{s} = 117 176 200 GeV at STAR. One notable feature of these measure-118 ments is that they are fully corrected for detector effects 119 177 with MultiFold, a novel machine learning method which 120 preserves the correlations in the multi-dimensional ob-121 servable phase space on a jet-by-jet basis [18]. We then₁₇₈ 122 compare our fully corrected measurements with predic-179 123 tions from event generators and analytical calculations180 124 done in the SCET framework. 125 181

Analysis details The STAR experiment [19] recorded₁₈₂ 126 data from $\sqrt{s} = 200 \text{ GeV} pp$ collisions during the 2012₁₈₃ 127 RHIC run. As energetic charged particles travel from the184 128 interaction point to the perimeter of the Time Projection₁₈₅ 129 Chamber (TPC), they ionize the gas atoms in the TPC₁₈₆ 130 and leave hits, from which we reconstruct tracks. Neu-187 131 tral particles do not interact with the gas in the TPC and 188 132 instead deposit their energy through the development₁₈₉ 133 of electromagnetic showers in Barrel Electro-Magnetic₁₉₀ 134 Calorimeter (BEMC) towers. Both the TPC and BEMC₁₉₁ 135 have a coverage of $|\eta| < 1$ and full azimuth. Events¹⁹² 136 are required to pass the jet patch trigger with a mini-193 137 mum transverse energy $E_{\rm T} > 7.3$ GeV be deposited in a¹⁹⁴ 138 1×1 patch in $\eta \times \phi$ in the BEMC. Before any run selec-195 139 tions, 65M events pass this trigger selection, correspond-196 140 ing to an integrated luminosity of 23 pb^{-1} . In addition,¹⁹⁷ 141 events are required to have primary vertices within $\pm 30_{198}$ 142 cm from the center of the detector along the beam axis.¹⁹⁹ 143 We apply a 100% hadronic correction to tower energy₂₀₀ 144 measurement: if a charged track extrapolates to a tower,201 145 then the whole track's $p_{\rm T}$ is removed from the tower $E_{\rm T}$;202 146 if the track $p_{\rm T}$ is greater than the tower $E_{\rm T}$, then the₂₀₃ 147 tower is removed completely. The same track and tower₂₀₄ 148 selections are applied as in Ref. [11] and [14]. We re-205 149 construct jets from TPC tracks $(0.2 < p_{\rm T} < 30 \text{ GeV}/c_{206})$ 150

with a charged pion mass assignment) and BEMC towers $(0.2 < E_{\rm T} < 30 \text{ GeV}, \text{ assuming massless})$ using the anti- $k_{\rm T}$ sequential recombination clustering algorithm [4] with a resolution parameter of R = 0.4. We apply the selections of $p_{\rm T} > 15 \ {\rm GeV}/c, |\eta| < 0.6$, transverse energy fraction of all neutral components < 0.9, and M > 1 GeV/c^2 on reconstructed jets, consistent with the selections in Ref. [14]. Similar to Ref. [11] and [14], no background subtraction is done, because the UE contribution to jets is low for STAR kinematics and unfolding can correct for any fluctuation in it. In addition, we select jets that pass SoftDrop grooming with the standard cuts of $SD = SD_2 = (z_{cut}, \beta) = (z_{cut,2}, \beta_2) = (0.1, 0).$ For this analysis, the less aggressive SoftDrop grooming criteria is set to no grooming, $SD_1 = (z_{cut,1}, \beta_1) = (0,0)$, so the CollinearDrop groomed observables are the difference in the ungroomed and SoftDrop groomed observables. This simplification can be made since the wide-angle contributions from ISR, UE and pileup are not significant for the dataset used in this analysis. Specifically, the contribution of UE to jet $p_{\rm T}$ for a jet with $20 < p_{\rm T} < 25$ GeV/c is less than 1% [20].

We measure the following jet observables: $p_{\rm T}$, $z_{\rm g}$ (defined in Eq. 1), $R_{\rm g}$ (defined in Eq. 2), M (defined in Eq. 3), $M_{\rm g}$ (defined in Eq. 3), and jet charge $Q^{\kappa=2}$. $Q^{\kappa=2}$ is defined as:

$$Q^{\kappa=2} = \frac{1}{p_{\mathrm{Tjet}}^2} \sum_{i \in \mathrm{jet}} q_i \cdot p_{\mathrm{T}_i}^2, \qquad (5)$$

where q_i and p_{T_i} are the electric charge and p_T of the *i*th jet constituent, respectively.

Experimentally, jet measurements need to be corrected for detector effects to compare with theoretical calculations and model predictions. The traditional correction procedure uses Bayesian inference in as many as three dimensions and requires the observables to be binned based on the resolution [21]. On the other hand, MultiFold is a machine learning technique that is able to correct data at a higher dimensionality in an un-binned fashion. As it preserves the correlation between the input and corrected observables across dimensionality, MultiFold is desirable for this study.

We fully corrected six jet observables simultaneously for detector effects using MultiFold. In addition to jets from data, matched pairs of jets from simulations with (detector-level) and without (particle-level) detector effects are input for MultiFold. The particle-level prior used for unfolding is jets from events generated with PYTHIA6 [22] with the STAR tune [23]. This is a singleparameter modification to the Perugia 2012 tune [24] to better match STAR data. Consistent with [Dmitri's paper], at particle-level, hadron weak decays are not enabled while strong and electromagnetic decays are. The PYTHIA events are run through GEANT3 [25] simulation of the STAR detector, and embedded into data from zero-bias events from the same run period as the analyzed data. The detector-level jets are then reconstructed after this embedding procedure. We geometri-

cally match a detector-level jet to a particle-level jet by₂₆₅ 207 requiring $\Delta R < 0.4$ between the two in the same event. 266 208 MultiFold achieves the goal of unfolding through itera-267 209 tively reweighting the weights assigned to each jet in sim-268 210 ulations [18]. It is naturally unbinned since these weights²⁶⁹ 211 are per-jet quantities. There are two steps for each iter-270 212 ation. In the first step, a neural network classifier is₂₇₁ 213 trained with the binary cross-entropy loss function, to272 214 distinguish jets from data and jets from the (reweighted)₂₇₃ 215 detector-level simulation. The input to the neural net- $_{274}$ 216 work has as many dimensions as the number of jet ob-275 217 servables of interest (in our case, 6), and the output di_{276} 218 mension is 2, each of which represents the probabilities $_{277}$ 219 that the jet comes from data and from simulation, respec-278 220 tively. It has been shown in Ref. [26] that, the output of_{279} 221 such a neural network can be used to estimate a set of new₂₈₀ 222 weights to apply to the detector-level simulation ($possi_{281}$) 223 bly reweighted from the previous iteration). This effec-282 224 tively allows us to convert a high-dimensional reweighting₂₈₃ 225 problem to a classification problem. Since the detector- $_{284}$ 226 level jets and the particle-level jets are matched, these₂₈₅ 227 weights can be applied to the particle-level jets (possibly₂₈₆ 228 reweighted from the previous iteration) as well. How-287 229 ever, due to the stochastic nature of detector response,₂₈₈ 230 identical particle-level jets are likely to match to differ-289 231 ent detector-level jets. A second step is then needed to₂₉₀ 232 convert these "per-instance" [18] (where each instance is $_{291}$ 233 a detector-level and particle-level pair) weights to a $\mathsf{func-}_{_{292}}$ 234 tion that gives a unique prescription to any particle-level $_{\scriptscriptstyle 293}$ 235 jet. These weights obtained from the second step are then $_{294}$ 236 either applied to the detector-level and particle-level jets $_{205}$ 237 in the next iteration, or quoted as the final $\operatorname{prescription}_{\scriptscriptstyle 296}$ 238 to obtain the unfolded jets if it is the last iteration. 239 297

We utilize the default settings of MultiFold as in [18],298 240 with two dense neural networks, each with three dense₂₉₉ 241 layers and 100 nodes per layer. We train the neural₃₀₀ 242 networks with TensorFlow [27] and Keras [28] using the₃₀₁ 243 Adams optimization algorithm [29]. In addition, we also₃₀₂ 244 use the default setting for the choice of activation func-₃₀₃ 245 tions, loss function, fraction of sample size for valida-304 246 tion, and maximum number of epochs. To prevent over-305 247 training, an early stopping is implemented after 50 con_{-306} 248 secutive epochs in which the loss value for the validation $_{307}$ 249 sample has not improved. 250

To correct for fake jets, i.e., detector-level jets arising₃₀₉ from background, fake rates were obtained from simula-₃₁₀ tions and used as initial weights for the data as an input₃₁₁ to MultiFold. For particle-level jets that are missed at de-₃₁₂ tector level due to effects such as tracking inefficiency, an₃₁₃ efficiency correction was done post-unfolding in a multi-₃₁₄ dimensional fashion. 315

The correction procedure was validated using a Monte₃₁₆ Carlo closure test, which showed good performance of₃₁₇ the unfolding among all observables for jets with 20 <₃₁₈ $p_{\rm T} < 50 \ {\rm GeV}/c$. In addition, we compared the fully cor-₃₁₉ rected jet mass distributions for three different $p_{\rm T}$ bins,₃₂₀ using both MultiFold and RooUnfold [14]. The ratios₃₂₁ of MultiFold distributions over RooUnfold distributions₃₂₂ are confirmed to be consistent with unity. These establish further confidence in application of MultiFold to the data.

The statistical uncertainty is estimated with the bootstrap technique [30]. In particular, 50 pseudo-datasets are created and used to repeat the unfolding procedure, where each jet from data has been resampled from a Poisson distribution with a mean of 1.

The sources of systematic uncertainties are variations of hadronic correction scale (from 100% to 50%), tower energy resolution (varied by 3.8%), tracking efficiency (varied by 4%) and unfolding procedure. The first three sources are treated in the same way as Ref. [11] and [14]. The dominant source for systematic uncertainty is the variation of unfolding procedure, up to x% in the peak region for jets in $20 < p_{\rm T} < 30 \text{ GeV}/c$, and y% for jets in $30 < p_{\rm T} < 50 {\rm ~GeV}/c$. The unfolding variation includes variation of the prior and random seed. The prior variation is accounted for through simultaneous reweighting of all six unfolded observables as well as a, based on prior distributions from PYTHIA 8.303 with Detroit tune [31] and HERWIG 7.2 with Default tune [32]. The variation of the random seed affects the initialization of the weights of the neural networks, and is accounted for with the standard error on the fully corrected result obtained from 100 different initial seeds.

Different from analyses that use RooUnfold, Ref. [11] and [14], this analysis does not explicitly account for the variation of the number of iterations as a separate source of uncertainty. Going to a higher number of iterations reduces the prior dependence bias; in fact, mathematically, the most correct number of iterations is infinity [18]. However, the statistical limitations would introduce unwanted fluctuations at such high number of iterations [18]. This can manifest through a large uncertainty from the variation of initial seeds, as well as the statistical uncertainty obtained with the bootstrap technique. The deviation of the result due to the inability to perform an infinite number of iterations shows up as the prior dependence. Therefore, the prior variation uncertainty effectively accounts for the uncertainty due to the number of iterations not being ideal, and the number of iterations can be selected by considering when a) the prior dependence uncertainty, b) seed uncertainty, and c) statistical uncertainty are low. We select an iteration number of 15, low enough such that the uncertainty due to seed variation and statistical uncertainty are both reasonable, at the cost of a non-negligible prior dependence uncertainty.

Results Figure 1 shows the distribution of fully corrected CollinearDrop groomed jet masses for jets with 20 < $p_{\rm T}$ < 30 GeV/c and 30 < $p_{\rm T}$ < 50 GeV/c in star markers with the red band indicating the systematic uncertainties. This figure excludes jets with $M = M_{\rm g}$ (?% of jets in this 20 < $p_{\rm T}$ < 30 GeV/c and ?% of jets in 30 < $p_{\rm T}$ < 50 GeV/c), which corresponds to the jets whose first splittings pass the criterion of ($z_{\rm cut}, \beta$) = (0.1,0) without the need of SoftDrop grooming, because the lower- $p_{\rm T}$ prong of the splitting

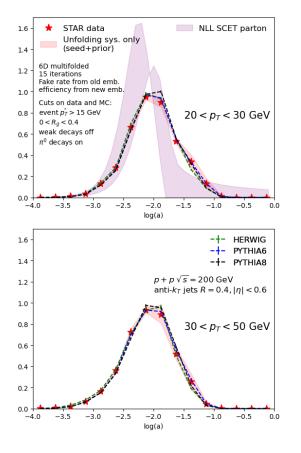


FIG. 1. CollinearDrop jet mass distributions.

carries at least 10% of the total jet $p_{\rm T}$. As a rough cal-₃₇₉ 323 culation, for a jet of 20 GeV, if we take the mean values₃₈₀ 324 $\langle M \rangle = 4.27 \text{ GeV}/c^2 \text{ and } \langle M_{\rm g} \rangle = 3.67 \text{ GeV}/c^2 \text{ for a jet}_{381}$ 325 with $20 < p_{\rm T} < 25 \text{ GeV}/c$ from Ref. [14], then we get₃₈₂ 326 a value of $\log(a) = -1.92$, similar to the peak value of₃₈₃ 327 our measurement, even though the latter excludes the₃₈₄ 328 $M = M_{\rm g}$ case. It is worth noting that even though M_{385} 329 and $M_{\rm g}$ both increase as a function of $p_{\rm T}$ as shown Ref.₃₈₆ 330 [14], $\log(a)$ has a weak dependence on $p_{\rm T}$. This is con-₃₈₇ 331 sistent with the prediction from Ref. [16] that at $O(\alpha_s)_{388}$ 332 (?), $a^2 = R^2 z_{\text{cut},2}$, independent of p_{T} and dependent on₃₈₉ 333 the grooming criteria. 334 390

Also shown in Fig. 1 are comparisons with event gen-₃₉₁ 335 erator descriptions in dashed lines, with vertical error₃₉₂ 336 bars indicating statistical uncertainties. Both PYTHIA6₃₉₃ 337 STAR tune [23] and HERWIG 7.2.2 [32] capture the data, 394 338 although there is some tension with PYTHIA 8.303 with₃₉₅ 339 Detroit tune [31] (finalize after systematics are done). In₃₉₆ 340 purple band, analytic calculation with NLL SCET per-397 341 formed at the parton level shows deviation from both₃₉₈ 342 event generator predictions and data, indicating that the₃₉₉ 343 CollinearDrop groomed mass is sensitive to hadroniza-400 344 tion effects. The error band indicates typical scale vari-401 345 ations in theoretical calculation. 346 402

Figure 2 shows the correlation between a and the⁴⁰³ SoftDrop groomed shared momentum fraction $z_{\rm g}$ and⁴⁰⁴ groomed jet radius $R_{\rm g}$ in 20 < $p_{\rm T}$ < 30 GeV/c, where⁴⁰⁵

the average value of the CollinearDrop groomed jet mass is indicated by the color of each bin in the $z_{\rm g} - R_{\rm g}$ plane, which is calculated as a weighted sum of a from the unfolded matched jets and particle-level missed jets. The $M = M_{\rm g}$ jets are included. This plane captures the Lund Plane [33] of the first groomed splitting. We see that a is strongly correlated with $R_{\rm g}$ while weakly correlated with $z_{\rm g}$.

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Also shown in Fig. 2 are curves of constant formation time t, which approximates the time it takes for a parton to radiate a gluon. This can be estimated as the life-time of the parton using the Heisenberg uncertainty principle [17]. It is related to other parton kinematic variables by:

$$t = \frac{1}{2Ez(1-z)(1-\cos(\theta))},$$
 (6)

where E is the energy of the parent parton, z is the momentum fraction carried by the lower- $p_{\rm T}$ daughter parton, and θ is the opening angle between the two daughters. E can be approximated by the jet $p_{\rm T}$; for a perturbative hard splitting, z and θ can be approximated by the SoftDrop $z_{\rm g}$ and $R_{\rm g}$, respectively [11]. We obtain the curves shown by replacing the parton variables in Eq. 6 with their (SoftDrop) jet counterparts, so t can be interpreted as the time that the first hard splitting to pass the SoftDrop criterion takes to develop. Our result hints at a correlation between the amount of early-stage radiation and the time at which the hard splitting happens. Specifically, to shed a significant amount of mass at the early stage of the parton shower, which is predominantly done via soft gluon radiation, the hard splitting needs to happen relatively late on average (or roughly at small R_{g}).

The curves of constant formation time can potentially help explain the dependence that a has on $R_{\rm g}$ and $z_{\rm g}$. In the region of $z_{\rm g} \ge z_{\rm cut,2} = 0.1$, the slopes of the formation time curves are relatively large, so it depends on $R_{\rm g}$ more than $z_{\rm g}$. To obtain a larger $z_{\rm g}$ dependence, one can choose a lower value of $z_{\rm cut,2}$ to access the smaller $z_{\rm g}$ values, where the formation time slopes decrease. A dependence of a on $z_{\rm cut,2}$ is also expected via $a^2 = R^2 z_{\rm cut,2}$.

It is also worth emphasizing that the measurement shown in Fig. 2 showcases the power of MultiFold, which enabled us to make selections in three variables, $p_{\rm T}$, $z_{\rm g}$ and $R_{\rm g}$, and study a fourth one *a* which itself is composite of a few variables; all of these observables have been fully corrected for detector effects.

Figure 3 shows the log(a) distributions for specific regions of the $z_{\rm g} - R_{\rm g}$ plane for jets with $20 < p_{\rm T} < 30$ GeV/c. The leftmost bin includes the a = 0 jets, which do not have anything removed by SoftDrop and are therefore possibly dominated by jets whose first splittings in the parton shower are already perturbative. Region 3 (0.15 < $R_{\rm g} < 0.25$ and 0.1 < $z_{\rm g} < 0.2$) includes asymmetric and intermediate-angle splittings while Region 2 (0.15 < $R_{\rm g} < 0.25$ and 0.4 < $z_{\rm g} < 0.5$) includes symmetric and intermediate-angle splittings. Despite the different $z_{\rm g}$ selections, the fraction of a = 0 jets and the

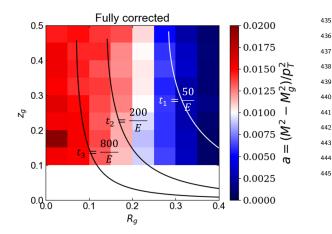


FIG. 2. CollinearDrop groomed mass as a function of $z_q - R_q$

dos distributions in a > 0 are similar. The weak dependence of a on $z_{\rm g}$ is consistent with our observation made for Fig. 2.

However, as we continue to scan across the plane, we 409 notice drastic changes in the fraction of jets with a = 0 as 410 well as differences in shape in the a > 0 region. We first 411 move onto Region 1 ($0 < R_{\rm g} < 0.1$ and $0.4 < z_{\rm g} < 0.5$), 412 which includes symmetric and collinear radiation from 413 the first hard splitting. Fig. 3 also shows that, compared 414 to Regions 2 and 3, Region 1 is more likely to have soft 415 radiation groomed away by SoftDrop as indicated by the 416 decreased count for a = 0, and has a broader tail for the₄₄₆ 417 small but nonzero a region. On the other hand, we ob-447 418 serve from Fig. 2 that we have on average higher values $_{\scriptscriptstyle 448}$ 419 of a in this region, which can be understood as mostly₄₄₉ 420 affected by the slightly higher values in $\log(a) > -1.5$. 421 The distribution of $\log(a)$ is wider in both directions due₄₅₁ 422 to the fact that a selection of narrow hard splitting $opens_{452}$ 423 up a large phase space for the amount of radiation $\text{pre-}_{_{453}}$ 424 ceding the splitting. 425

Region 4 (0.3 < $R_{\rm g}$ < 0.4 and 0.1 < $z_{\rm g}$ < 0.2) in-455 426 cludes asymmetric and wide-angle splittings, character-456 427 istic of perturbative early emissions. Again compared to₄₅₇ 428 Regions 2 and 3, in Region 4, the significant fraction of_{458} 429 a = 0 jets indicates that it is highly probable that no₄₅₉ 430 non-perturbative early emission has happened before the₄₆₀ 431 perturbative emission. This is likely the explanation for₄₆₁ 432 why the z-axis values are also close to 0 in this region in_{462} 433 Fig. 2. 463 434

Conclusions In this Letter, we have presented the first CollinearDrop groomed observable measurement, the CollinearDrop groomed mass, and its correlations with groomed jet substructure observables, in pp collisions at $\sqrt{s} = 200$ GeV with the STAR experiment. A machine learning driven method to correct for detector effects, MultiFold, has been applied for the first time to hadronic collision data, which allows for access of multidimensional correlations on a jet-by-jet basis. We demonstrate how MultiFold allows us to present measurements in N dimensions and shows promising potential for fu-

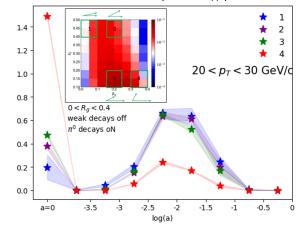


FIG. 3. Distribution of $\log(a)$ with various selections of $R_{\rm g}$ and $z_{\rm g}$.

ture multi-differential measurements as the community enters a high-statistics, precision QCD era.

Event generator predictions and theoretical calculation were shown to qualitatively describe the data for the CollinearDrop groomed mass, which probes the soft radiation within jets. From the investigation of the correlation between the CollinearDrop groomed mass a and the SoftDrop groomed observables $z_{\rm g}$ and $R_{\rm g}$, we observe that on average, a large nonperturbative radiation biases the perturbative splitting to happen late. We also observed a strong correlation between the CollinearDrop groomed mass and $R_{\rm g}.$ In particular, a large $R_{\rm g}$ biases toward a higher probability that the jet has no radiation prior to the perturbative splitting, and a small R_{g} biases towards a higher probability that the jet has some radiation prior to the splitting. These measurements demonstrate the interplay between the nonperturbative processes and the perturbative jet fragmentation.

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